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New space vector modulation algorithms applied to multilevel converters with balanced DC-link voltage

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Abstract

This work presents a survey of new space vector modulation algorithms for high power voltage source multilevel converters. These techniques provide the nearest switching vectors sequence to the reference vector and calculates the on-state durations of the respective switching state vectors without involving trigonometric functions, look-up tables or coordinate system transformations which increase the computational load corresponding to the modulation of a multilevel converter. These algorithms drastically reduce the computational load maintained permitting the on-line computation of the switching sequence and the on-state durations of the respective switching state vectors. The on-state durations are reduced to a simple addition. In addition, the low computational cost of the proposed methods is always the same and it is independent of the number of levels of the converter. The algorithms have been satisfactorily implemented in very low-cost microcontrollers.

1 Introduction

In the recent years, multilevel converters are becoming popular in medium and high power applications due to their ability to meet the increasing demand of power ratings and power quality associated with reduced harmonic distortion and lower EMI [1]. The advantages of multilevel converters are well known since Akira Nabae proposed the topology of NPC (Neutral Point Clamped) inverter in 1981 [2]. We can stress the importance of their capability of increasing the output voltage magnitude and reducing the output voltage and current harmonic content, the switching frequency and the voltage supported by each power semiconductors. In that respect, they permit to use the double voltage under the same type of switches. By synthesizing the ac output voltage from several levels of voltages, staircase waveforms are produced, which approach the sinusoidal waveform with low harmonic distortion. Multilevel converter enables the ac voltage to be increased without a transformer. In addition, the cancellation of low frequency harmonics from the ac voltages at different levels means that the size of the ac inductances can be reduced. Due to these attractive characteristics, several control algorithms of multilevel converter have been recently proposed [3-6]. However, the carrier-based PWM methods [3,4] highly increase the algorithm complexity and the computational load with the number of levels of the multilevel converter, and the most of the space vector modulation algorithms proposed in the literature involve trigonometric function calculations or look-up tables or memories [6]. As far as the author knows the first space vector modulation for three-level and multilevel inverters for calculating the nearest switching vectors sequence to the reference vector and the on-state durations of the respective switching state vectors without trigonometric function calculations, look-up tables or coordinate system transformations was presented in [7,8]. The results obtained using this iterative algorithm [7,8] are improved using the fast modulation algorithm based on geometrical considerations proposed in the section B of this paper. Finally, a new three-dimensional space vector modulation is presented in this survey in order to generalize the conventional two-dimensional techniques; both the algorithms presented in this work and the algorithms modulations can be found in the literature. The methods proposed in this paper can be applied to the cascade [9], flying capacitor [10], and Neutral Point Clamped (NPC) [11] topologies.

2 Modulation techniques description

2.1 Iterative algorithm for multilevel converters

The first two-dimensional space vector modulation presented in this survey is an iterative algorithm for multilevel converters with very low computational cost. This method is based on the decision based pulse width modulation developed by Holtz [12] for a conventional two-level converter. Three-phase quantities are usually transformed into the phasor representation since it simplifies the analysis of the modelled system [13].

In this paper, the problem is solved for a voltage vector in the first sextant. However, this reference vector can be located in any of the six sectors of the regular hexagon which contains the switching state vectors. This problem is easily solved rotating u^* counterclockwise by angle $(n-1)\frac{\pi}{3}$, where n is the sextant number, $n = 1, \dots, 6$. This rotation displaces any reference vector to the first 60° to be studied there. The switching state vectors for the multilevel inverter control are determined by the reverse rotation. The input to the modulation algorithm of the three-level converter is the normalized reference voltage vector. The normalization depends on the number of levels of the multilevel converter and the voltage level value of the DC-link capacitors. As a result, V_a , V_b , and V_c (1) take entire values between 0 and $n-1$, where n is the number of the level of the multilevel converter. Thus, the first step of the method consists in localizing the sextant $n = 1, \dots, 6$ where the reference voltage vector u^* is located. The voltage vector u^* is transformed into u_{flat}^* . This transformation consists in scaling imaginary part by multiplying it by $\frac{1}{\sqrt{3}}$. The hexagon is flattened. Fig. 1 shows the regular hexagon defined by the switching state vectors before and after transformation in the complex plane. Since the transformed sextants are separated by 45° lines, the sextant can now be readily identified by comparing the real and imaginary parts of the complex transformed reference voltage vector u_{flat}^* . In addition, it can be easily proven [12] that, once the sextant has been determined, the numeric evaluation of the switching times gets reduced to a single addition involving u_α and u_β . Summing up, the transformation of u^* into u_{flat}^* makes it possible to avoid on-line computations. These computations are substituted by decision making. The states space consists of a main regular hexagon. Each sextant of this hexagon is now divided into several sectors. The number of sectors depends on the number of levels of the multilevel converter.

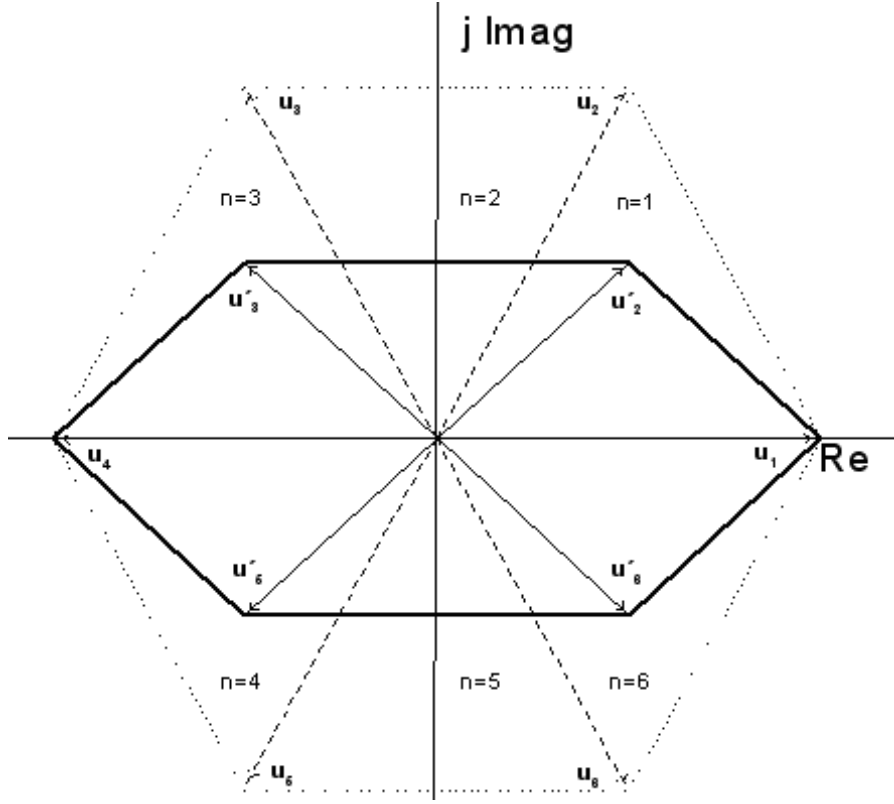


Figure 1: Switching state vectors before and after the transformation in the complex plane.

2.1.1 Determination of the sextant of the reference voltage vector

Once the sextant n has been localized into the main regular hexagon, the identification of the sector into the sextant, the nearest switching sequence to approximate a reference voltage vector u^* and the on-state durations are calculated by rotating u^* to the first sextant. The rotated reference voltage vector is:

$$u_g = u_{ga} + ju_{gb} = u^* \exp\left(-j(n-1)\frac{\pi}{3}\right); \quad n = 1, \dots, 6. \quad (1)$$

This vector u_g is transformed in another one with identical real part and reduced imaginary part

$$u_{gf} = u_{ga} + j\frac{\sqrt{3}}{3}u_{gb} = u_{gfa} + ju_{gfb}. \quad (2)$$

This simplifies the sector identification. In general, a vector u_{gf}^* can be expressed in function of the time of its surrounding state vectors

$$u_{gf}^* = t_1 u_{gf}^1 + t_2 u_{gf}^2 + t_3 u_{gf}^3. \quad (3)$$

In the algorithm the sub cycle T_{nm} is normalized to the unit

$$T_{nm} = 1 = t_1 + t_2 + t_3. \quad (4)$$

u_{gf}^* can be studied from the centre of the regular hexagon which corresponds to u_{gf}^2 . The new vector to approximate by its surrounding state vectors is $u_{gf}^* - u_{gf}^2$. u_{gf}^* must be related to its surrounding state vectors, as it is shown in Fig. 2. In this case $t_2 = 1 - t_1 - t_3$ and u_{gf}^* can be expressed:

$$u_{gf}^* = t_1(u_{gf}^1 - u_{gf}^2) + t_3(u_{gf}^3 - u_{gf}^2) + u_{gf}^2. \quad (5)$$

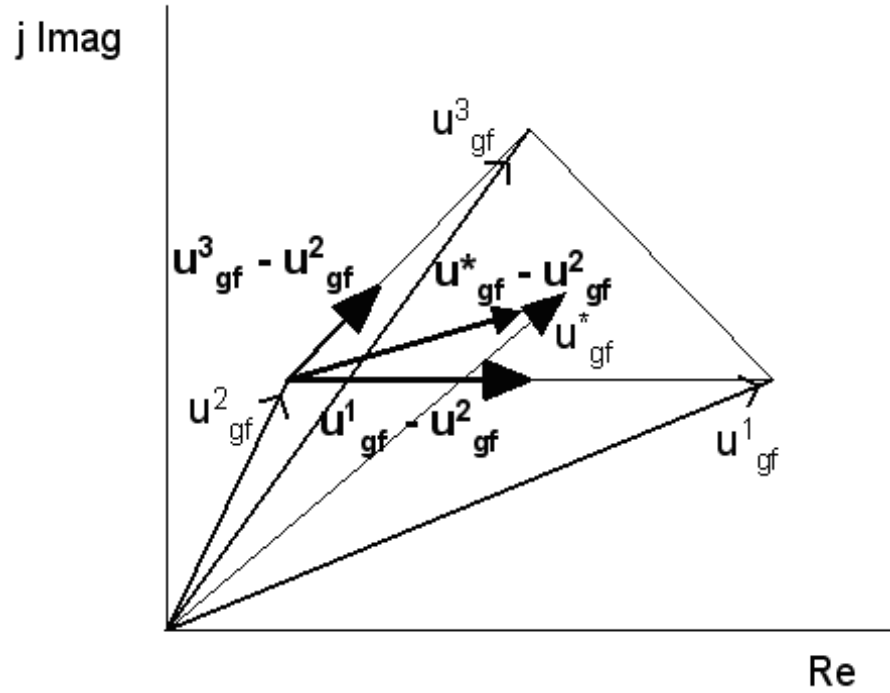


Figure 2: Example for studying u_{gf}^* from the centre of the regular sub-hexagon corresponding to u_{gf}^2 .

2.1.2 Determination of the sector

It is necessary to locate the triangular sector and the sub hexagon where u_{gf}^* is found. To determine the sector where u_{gf}^* is, a displacement to the centre node of each regular sub hexagon is done. Localization of the vertical and horizontal positions of the centre node is necessary. A fundamental step of the approach is to localize the triangular sector where u_{gf}^* is found. As stated above, this is equivalent to determining the sub-hexagons and the sextant of the hexagon where u_{gf}^* points to [13,18]. This problem is equivalent to the problem of finding the sextant for a regular hexagon of a conventional two-level inverter. However, the above-described searching algorithm ensures that the imaginary part of u_{gfd}^* is either positive or zero and therefore, the lower sextants ($n = 4, 5, 6$ in Fig. 1) can be ignored. This simplifies the searching.

Once the sector where u_{gf}^* is located has been determined, the on-state durations can be calculated from the real and imaginary parts of u_{gfd}^* by using the expressions reported in [13,18]. Finally, a reverse rotation and transformation to obtain the definitive state vectors and on-state durations, which generate the original normalized reference voltage vector, is done.

Note that the proposed algorithm runs on-line only for the times it is necessary. There is no need to generate, save and retrieve all the sectors, state vectors, and on-state durations. On the other hand, this method uses the minimum number of possible comparators. The algorithm used in this work presents the advantage of eliminating the angle from the calculations. Moreover, the numeric evaluation of the on-state durations is reduced to a simple addition. This efficient method uses the minimum number of possible comparators.

2.2 Space vector modulation algorithm based on geometrical considerations

An alternative space vector modulation algorithm for voltage source multi-level converters is explained in the present section. This technique is based on the above reported. However, this method calculates the switching times and the space vectors using simple geometrical considerations. In addition, the low computational cost of the proposed method is always the same and is independent of the number of levels of the converter.

2.2.1 Introduction to the method

Three-phase quantities are usually transformed into phasor representation for simplifying the calculations. Three vectors u_1 , u_2 , and u_3 are used to approximate the desired voltage vector u^* in polar coordinates in a control cycle T_m . The modulation law requires the actual voltage vector u to equal its reference value u^* where u^* is represented in the stationary reference frame

$$u = u^* = E_a + E_b \exp\left(\frac{j2\pi}{3}\right) + E_c \exp\left(\frac{j4\pi}{3}\right) = \text{Re}\{u^*\} + j\text{Im}\{u^*\}. \quad (6)$$

During each modulation sub cycle of duration T_m , a switching sequence is generated. It is composed of three switching state vectors $u_1(t_1)$, $u_2(t_2)$, and $u_3(t_3)$, where t_1 , t_2 , and t_3 are the on-state durations of the active switching state vectors. The three vectors nearest to the reference vector must be identified.

The input to the modulation algorithm of the multi-level converter is the normalized reference voltage vector u_n^* . The states space normalization permits the developed algorithm to be independent of the DC-link voltage and the numbers of levels of voltages of the converter. The states space of a four level converter in the complex plane d-q is shown in [13,18], where the coordinates of each triangle's vertex represent the levels of the DC link voltage necessary to connect to each phase of the inverter to obtain the corresponding state. They take integer values between 0 and $n - 1$, where n is the number of the level of the multilevel converter.

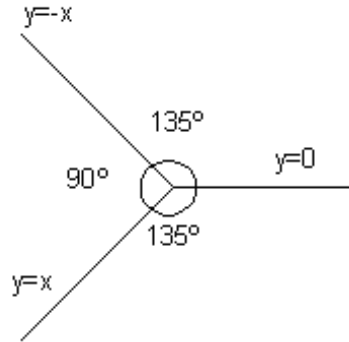


Figure 3: Equations of the straight lines which divide the flattened complex plane.

The voltage vector u^* is transformed into u_{flat}^* . This transformation consists of scaling imaginary part multiplying it by $1/\sqrt{3}$ [7,8,13,18]. The transformation of u^* into u_{flat}^* allows us to use simple on-line computations of the states and switching times [7,8,13,18]. The hexagon where the state vectors are represented, is flattened and the three zones shown in Fig. 3 are found in the complex plane d-q.

The computations are substituted by decision making with a very low number of instructions and the numeric evaluation of the switching times gets reduced to a single addition involving the real u_d and imaginary u_q parts of the reference voltage vector [7,8,13].

2.2.2 Determination of the region

The first step of this method consists of determining the region of the flattened d-q space where the normalized reference voltage vector u_n^* is located. In Fig. 4 the flow chart for determining the region is shown.

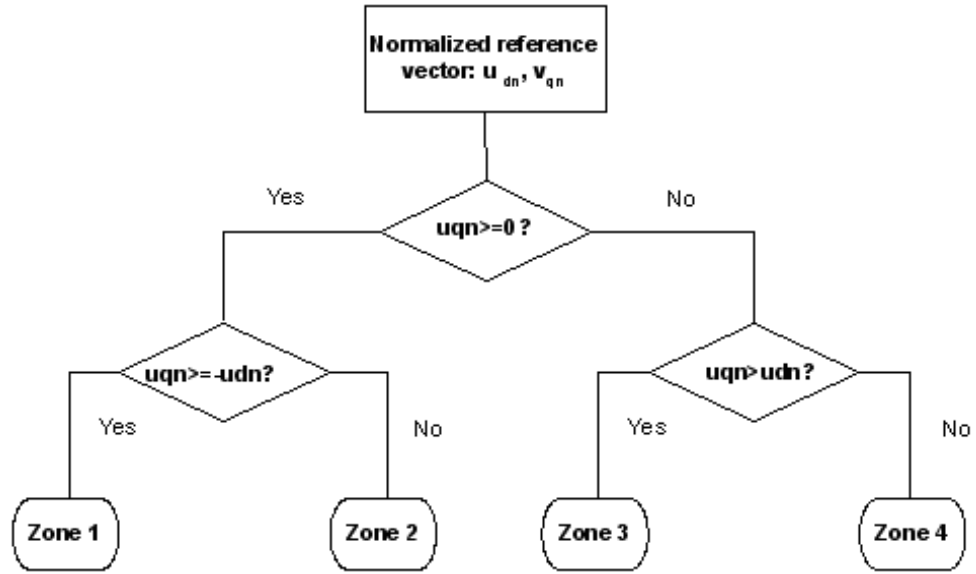


Figure 4: Flow chart for determining the region in the normalized flattened complex plane.

2.2.3 Calculation of a triangle's vertex

The proposed algorithm can be explained while assuming that the reference vector is located in zone 1. Two other cases are solved in the same way [14,18].

The developed algorithm always requires the same computational cost because it is independent of the number of levels of the multilevel converter. This is one of the attractive advantages that this modulation presents if it is compared with most of the algorithms found in the bibliography [3-6]. For example, the representation of the states of a five level three phase inverter in zone 1 is shown in Fig. 5.

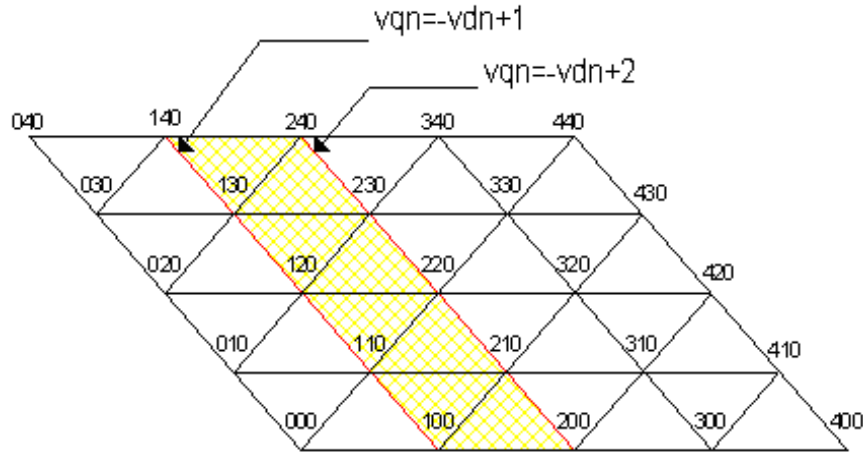


Figure 5: States of a five level converter in zone 1.

E_a, E_b, E_c are the coordinates of one of the vertices in the triangle where the reference vector is pointing to. Whatever voltage reference vector located between both lines shown in Fig. 3, it satisfies the following expressions:

$$-u_{dn} + 1 < u_{qn} < -u_{dn} + 2 \quad \Rightarrow \quad 1 < u_{qn} + u_{dn} < 2. \quad (7)$$

Every reference vector in this region of the complex plane has one vertex of the triangle where u_n^* is found with $E_a = 1$. In general, this value can be calculated in zone 1 as:

$$E_a = \text{integer}(u_{dn} + u_{qn}). \quad (8)$$

2.2.4 Determination of the orientation of the triangle

Once the lower left hand corner vertex coordinates are known, it is necessary to find out in which of the two triangles is the reference vector located for determining other states and the switching times [14,18].

If the reference vector is found in the triangle called 1, the geometrical condition in this region is:

$$u_{qn} < u_{dn} + E_b - E_a \quad \Rightarrow \quad u_{qn} - u_{dn} < (E_b - E_a). \quad (12)$$

However, if this geometrical condition is not fulfilled then the reference vector is located in triangle 2.

2.2.5 Calculation of the three nearest vectors to the reference vector

The three nearest states to the reference vector are obtained when the coordinates E_a , E_b , E_c and the orientation of the triangle are known. In zone 1 they are as follows:

Triangle(1)	Triangle(2)	
State 1 : “ E_a, E_b, E_c ”	State 1 : “ E_a, E_b, E_c ”	
State 2 : “ $E_a + 1, E_b, E_c$ ”	State 2 : “ $E_a + 1, E_b + 1, E_c$ ”	(13)
State 3 : “ $E_a + 1, E_b + 1, E_c$ ”	State 3 : “ $E_a, E_b + 1, E_c$ ”.	

2.2.6 Calculation of the switching times of the active vectors

The switching times are calculated from the geometrical coordinates of the active vectors. Therefore, the numeric evaluation of the switching times gets reduced to a single addition involving only real and imaginary parts of the reference voltage vector and the coordinates E_a, E_b, E_c .

The normalized geometrical components are obtained from the following expression:

$$\begin{pmatrix} u_{dn}^{E_a E_b E_c} \\ u_{qn}^{E_a E_b E_c} \end{pmatrix} = \begin{pmatrix} 1 & -\frac{1}{2} & -\frac{1}{2} \\ 0 & \frac{1}{2} & -\frac{\sqrt{3}}{2} \end{pmatrix} \begin{pmatrix} E_a \\ E_b \\ E_c \end{pmatrix} \quad (14)$$

where

$$\begin{pmatrix} u_d^{E_a E_b E_c} \\ u_q^{E_a E_b E_c} \end{pmatrix} = \begin{pmatrix} 1 & -\frac{1}{2} & -\frac{1}{2} \\ 0 & \frac{\sqrt{3}}{2} & -\frac{\sqrt{3}}{2} \end{pmatrix} \begin{pmatrix} E_a \\ E_b \\ E_c \end{pmatrix}, \quad (15)$$

$$\begin{pmatrix} u_{dn}^{E_a E_b E_c} \\ u_{qn}^{E_a E_b E_c} \end{pmatrix} = \begin{pmatrix} u_d^{E_a E_b E_c} \\ \frac{1}{\sqrt{3}} u_q^{E_a E_b E_c} \end{pmatrix}.$$

In [14,18] the geometrical coordinates of the sub-region in zone 1 is illustrated.

The following step consists of calculating the switching time from the equations:

Triangle 1

$$\begin{aligned} d_1 * (E_a - \frac{E_b}{2}) + d_2 * (E_a - \frac{E_b}{2} + 1) + d_3 * (E_a - \frac{E_b}{2} + \frac{1}{2}) &= u_{dn} \\ d_1 * \frac{E_b}{2} + d_2 * \frac{E_b}{2} + d_3 * (\frac{E_b+1}{2}) &= u_{qn} \end{aligned} \quad (16)$$

$$d_1 + d_2 + d_3 = 1$$

Triangle 2

$$\begin{aligned} d_1 * (E_a - \frac{E_b}{2}) + d_2 * (E_a - \frac{E_b}{2} + \frac{1}{2}) + d_3 * (E_a - \frac{E_b}{2} - \frac{1}{2}) &= u_{dn} \\ d_1 * \frac{E_b}{2} + d_2 * \frac{E_b+1}{2} + d_3 * (\frac{E_b+1}{2}) &= u_{qn} \end{aligned} \quad (17)$$

$$d_1 + d_2 + d_3 = 1$$

where the switching times $t_i = d_i T_m$, with $i = 1, 2, 3$ and T_m is the control cycle.

Solving this system of equations for each considered triangle, we obtain the following simple expressions of the duty cycles:

Triangle 1

$$\begin{aligned} d_1 &= 1 + E_a - u_{dn} - u_{qn} \\ d_2 &= -E_a + E_b + u_{dn} - u_{qn} \\ d_3 &= -E_b + 2u_{qn} \end{aligned} \quad (18)$$

Triangle 2

$$\begin{aligned}
 d_1 &= 1 + E_b - 2u_{qn} \\
 d_2 &= -E_a + u_{dn} + u_{qn} \\
 d_3 &= E_a - E_b - u_{dn} + u_{qn}.
 \end{aligned} \tag{19}$$

2.2.7 Summary of results

Table 1 shows summaries of state vectors and the duty cycles in the three regions in the complex plane d-q.

Finally, in order to validate the explained technique, experimental results obtained in a 50kW back-to-back NPC three-level converter prototype, show a satisfactorily good performance of the proposed algorithm. In these figures, the phase voltage, the phase-phase voltage, and the neutral-phase voltage are illustrated.

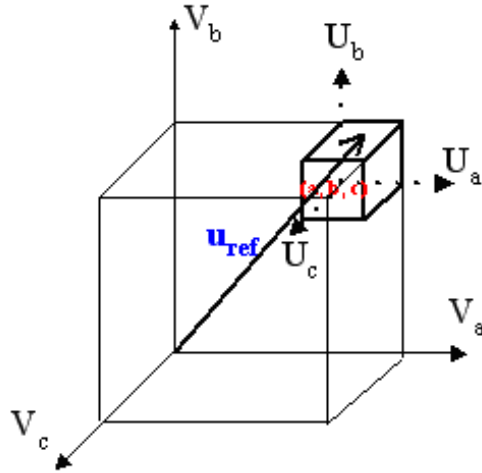


Figure 7: Origin of the sub-cube where the reference vector is supposed to be found.

	Zone 1		Zone 2		Zone 3	
	Triangle 1	Triangle 2	Triangle 1	Triangle 2	Triangle 1	Triangle 2
E_a	$u_{qp}-u_{dn} \leq E_b-E_a$	$u_{qp}-u_{dn} > E_b-E_a$	$u_{qp} \geq (E_b-E_c)/2$	$u_{qp} < (E_b-E_c)/2$	$u_{qp}+u_{dn} \leq E_a-E_c$	$u_{qp}+u_{dn} > E_a-E_c$
E_b	Integer($u_{dn}+u_{qp}$)		0		Integer($u_{dn}-u_{qp}$)	
E_c	Integer(2^*u_{qp})		Integer($u_{qp}-u_{dn}$)		0	
	0		Integer($-u_{dn}-u_{qp}$)		Integer(-2^*u_{qp})	
State 1	E_a, E_b, E_c	E_a+1, E_b+1, E_c	E_a, E_b, E_c	E_a, E_b, E_c	E_a, E_b, E_c	E_a, E_b, E_c
State 2	E_a+1, E_b, E_c	E_a, E_b+1, E_c	E_a, E_b+1, E_c+1	E_a, E_b, E_c+1	E_a, E_b, E_c+1	E_a+1, E_b, E_c+1
State 3	E_a+1, E_b+1, E_c	E_a, E_b, E_c	E_a, E_b+1, E_c	E_a, E_b+1, E_c+1	E_a+1, E_b, E_c+1	E_a+1, E_b, E_c
d_1	$1+E_a-u_{dn}-u_{qp}$	$1+E_b-2^*u_{qp}$	$1+E_b+u_{dn}-u_{qp}$	$1+E_c+u_{dn}+u_{qp}$	$1+E_c+2^*u_{qp}$	$1+E_a-u_{dn}+u_{qp}$
d_2	$E_b-E_a+u_{dn}-u_{qp}$	$-E_a+u_{dn}+u_{qp}$	$-E_c-u_{dn}-u_{qp}$	$E_b-E_c-2^*u_{qp}$	$E_a-E_c-u_{dn}-u_{qp}$	$-E_c-2^*u_{qp}$
d_3	$-E_b+2^*u_{qp}$	$E_a-E_b-u_{dn}+u_{qp}$	$E_c-E_b+2^*u_{qp}$	$-E_b-u_{dn}+u_{qp}$	$-E_a+u_{dn}-u_{qp}$	$E_c-E_a+u_{dn}+u_{qp}$

Table 1. Summary of state vectors and the duty cycles.

2.3 Three-dimensional space vector algorithm of multilevel converters

Finally, a three-dimensional (3D) space vector algorithm of multilevel converters for compensating harmonics and zero sequence in three phase four wire systems with neutral is presented in this section. The low computational cost of the proposed method is always the same and it is independent of the number of levels of the converter. The conventional two-dimensional space vector algorithms represent a particular case of the proposed generalized modulation algorithm. In general, the presented algorithm is useful in systems with or without neutral, unbalanced load, triple harmonics, and for generating whatever 3D control vector.

The algorithm presented in this work is a generalization of the well known 2D space vector technique, including the algorithms explained above [16].

The replacement of conventional two level converters by multilevel converters in active filters highly improves the harmonic content of the output signal of the converter. Most of the active filter control techniques found in the bibliography are based on current control pulse width modulation (PWM) or bang-bang [15], where each leg of the converter is independently controlled. However, it would be desirable to use an effective 3D Space Vector Modulation for this kind of applications because it can drastically reduce the control complexity and the computational load.

It is necessary to develop a new 3D space vector algorithm for multilevel converters to compensate a zero sequence in active power filters with neutral with single-phase distorting loads, which generate large neutral currents.

In general, the proposed algorithm is useful in systems with or without neutral, unbalanced load, triple harmonics and for generating whatever 3D control vector.

The space vectors will coplanar if the system is balanced without triple harmonics. However, it is necessary to generalize the approach to a 3D space if the system is unbalanced or if there is zero sequence or triple harmonics because the reference vectors are not on a plane.

The proposed algorithm is the first 3D space vector modulation technique for multilevel converters which permits the on-line calculation of the sequence of the nearest space vector for generating the reference voltage vector [16,18]. This generalized method provides the nearest switching vectors sequence to the reference vector and calculates the on-state durations of the respective switching state vectors without involving trigonometric functions, look-up tables, or coordinate system transformations which increase the computational load corresponding to the modulation of multilevel con-

verters. In this work, a very simple and fast 3D modulation algorithm based on geometrical considerations is presented. The computational cost of the proposed method is very low and independent of the number of levels of the converter. This technique can be used as modulation algorithm in all applications which provide a 3D vector control.

2.3.1 Reference vector synthesis

During each modulation subcycle of duration T_m , a switching sequence is generated. It is composed of four switching state vectors $u_1(t_1)$, $u_2(t_2)$, $u_3(t_3)$, and $u_4(t_4)$, where t_1 , t_2 , t_3 , and t_4 are the on-state durations of the active switching state vectors. The four vectors nearest to the reference vector must be identified [18]. The proposed 3D Space Vector Modulation (SVM) algorithm easily calculates the four state vectors which generate the reference vector. In general, with unbalanced systems or with triple harmonics, the reference vector could be not placed in the 2D plane of the multilevel converter. In this way, it is necessary to use a switching sequence with four state vectors. Thus, the reference vector will be pointing to a volume which is a tetrahedron. The vertices of that tetrahedron are the state vectors of the switching sequence. In addition, the algorithm permits to obtain the corresponding duty cycles without using tables or trigonometric functions. The modulation algorithm input is the normalized voltage vector. The normalization only depends on the number of levels of the multilevel converter n , and the voltage level value of the DC-link capacitors, V_{DC} [16]. The reference vector must be multiplying by the normalization constant $\sqrt{\frac{2}{3}} \frac{V_{DC}}{n-1}$.

Step 1: Find the sub-cube where the reference vector is pointing to.

The space vectors of a multilevel converter form a cube in a 3D space. This space can be decomposed into several tetrahedrons which generate the cube total volume. For a certain reference vector in three-phase coordinates (u_a, u_b, u_c) , the integer part of each component (a, b, c) is calculated, where

$$\begin{aligned} a &= \text{integer}(u_a), \\ b &= \text{integer}(u_b), \\ c &= \text{integer}(u_c). \end{aligned} \tag{20}$$

The 3D space is formed by a certain number of sub-cubes depending on the number of the levels of the converter. (a, b, c) are the origin coordinates

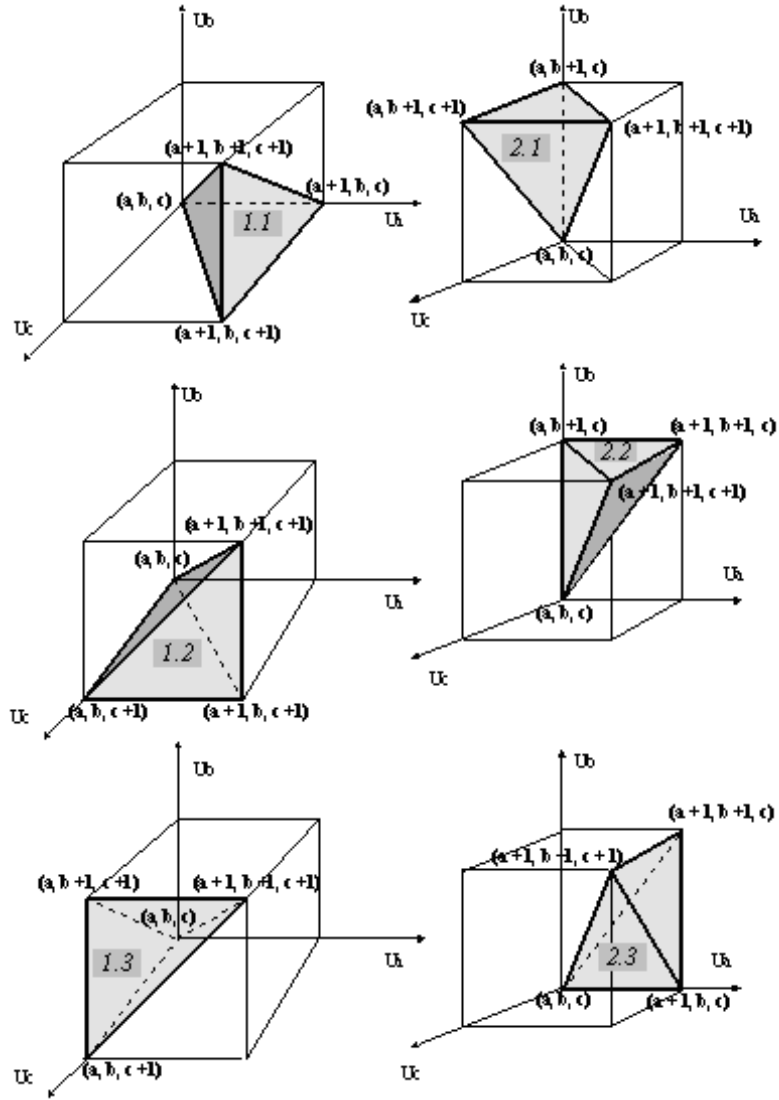


Figure 8: Tetrahedrons into the cube with the corresponding state vectors.

corresponding to the reference system of the sub-cube where the reference vector is pointing to.

Step 2: Six tetrahedrons are considered into each sub-cube. Therefore, it is necessary to define the tetrahedron where the reference vector is pointing to. This tetrahedron is easily found by comparing with three planes into the 3D space which define the six tetrahedrons inside the sub-cube. The three planes which define the six tetrahedrons are shown in [16,18]. Only the maximum of three comparisons is needed.

Step 3: Once (a, b, c) coordinates are known, the main step of the algorithm consists in calculating the four space vectors corresponding to the four vertices of a tetrahedron into the selected sub-cube (in step 1). These vectors will generate the reference vector. Configurations of the 3D space with different number of tetrahedrons into the cube have been studied. However, the minimum number of comparisons is obtained using six tetrahedrons [16,18]. In Fig. 8, the tetrahedrons in the cube with the corresponding state vectors are illustrated.

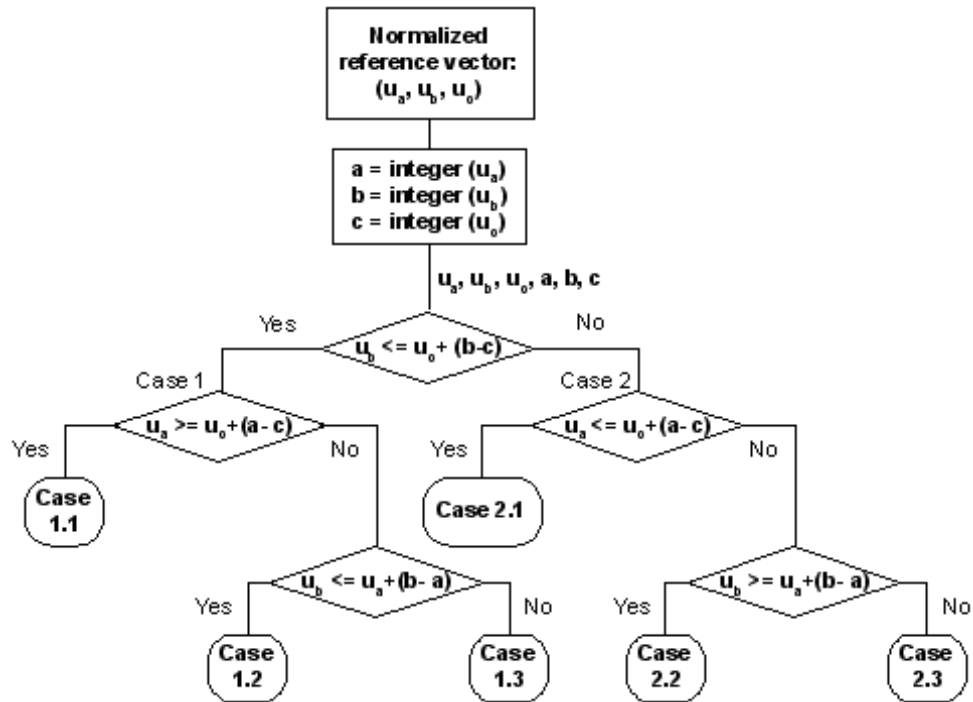


Figure 9: Algorithm for the selection of each tetrahedron with the corresponding state vectors.

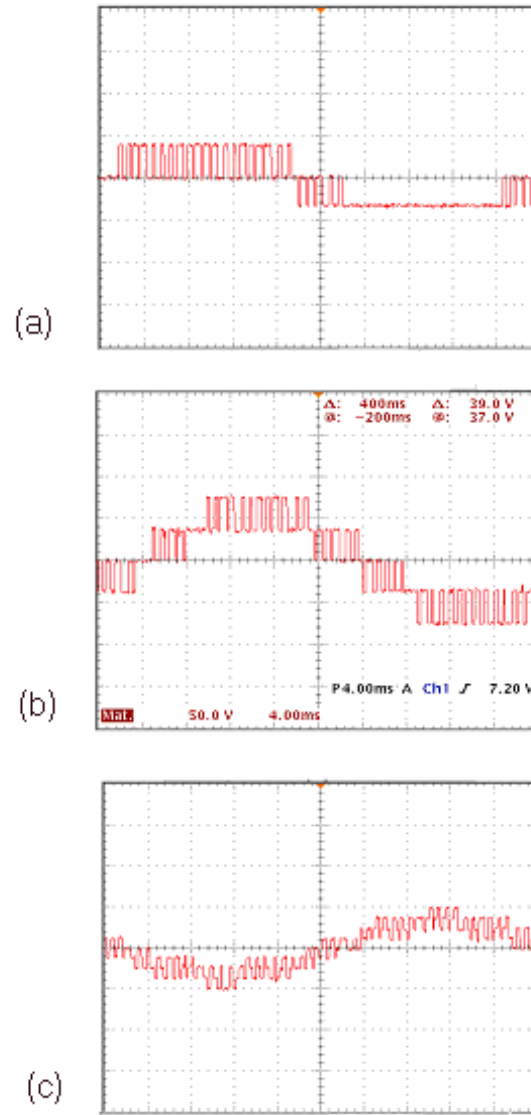


Figure 10: Experimental results obtained in a 50kW back-to-back NPC three-level converter prototype: a) phase voltage; b) phase-phase voltage; c) neutral-phase voltage.

Step 4: Calculation of the switching times.

The new algorithm calculates on-line the four state vectors in the 3D space and the corresponding duty-cycles using only sixty nine instructions and a maximum of three comparisons for calculating the suitable tetrahedron. The computational load is always the same and is independent of the number of levels of the multilevel converter. In addition, the algorithm provides the switching sequence that minimizes the total harmonic distortion and the commutation number of the semiconductor devices.

General structure of the algorithm

The flow diagram of the new 3D modulation algorithm for choosing the tetrahedron where the reference vector is pointing to is shown in Fig. 9.

Notice that the algorithm is extremely simple.

2.3.2 Calculation of duty-cycles

Once the state vectors which generate each reference vector are known, the corresponding duty-cycles are calculated. The algorithm generates a matrix with four state vectors and the corresponding switching times t_i .

$$S = \begin{bmatrix} S_a^1 S_b^1 S_c^1 d_1 \\ S_a^2 S_b^2 S_c^2 d_2 \\ S_a^3 S_b^3 S_c^3 d_3 \\ S_a^4 S_b^4 S_c^4 d_4 \end{bmatrix} \quad (21)$$

$$ti = d_i T_m, i = 1, \dots, 4$$

where T_m is the sample time.

The state vectors are the vertices of the corresponding tetrahedron which generates the reference vector. The equations to be solved are:

$$\begin{aligned} u_a &= S_a^1 d_1 + S_a^2 d_2 + S_a^3 d_3 + S_a^4 d_4, \\ u_b &= S_b^1 d_1 + S_b^2 d_2 + S_b^3 d_3 + S_b^4 d_4, \\ u_c &= S_c^1 d_1 + S_c^2 d_2 + S_c^3 d_3 + S_c^4 d_4, \\ d_1 + d_2 + d_3 + d_4 &= 1. \end{aligned} \quad (22)$$

The numeric evaluation of the duty cycles or on-state durations of the switching states are reduced to a simple addition as shown in Table 2. a , b , and c represent the different voltage levels of the capacitors battery. They

acquire values between zero and $n - 1$ where n is the number of levels of the multilevel converter.

The duty cycles are functions only of the reference vector components and the integer part of reference vector coordinates.

In addition, the optimized switching sequence is selected in order to minimize the switching number. The space vectors sequence in half cycle is: $u_1 = (S_a^1, S_b^1, S_c^1)$, $u_2 = (S_a^2, S_b^2, S_c^2)$, $u_3 = (S_a^3, S_b^3, S_c^3)$, and $u_4 = (S_a^4, S_b^4, S_c^4)$. In the second half cycle the space vectors form a reverse sequence.

Tetrahedron	Space vectors sequence	Switching times
Case 1.1	$(S_a^1, S_b^1, S_c^1) = (a, b, c)$ $(S_a^2, S_b^2, S_c^2) = (a + 1, b, c)$ $(S_a^3, S_b^3, S_c^3) = (a + 1, b, c + 1)$ $(S_a^4, S_b^4, S_c^4) = (a + 1, b + 1, c + 1)$	$d_1 = 1 + a - u_a,$ $d_2 = -a + c + u_a - u_c,$ $d_3 = b - c - u_b + u_c,$ $d_4 = -b + u_b,$
Case 1.2	$(S_a^1, S_b^1, S_c^1) = (a, b, c)$ $(S_a^2, S_b^2, S_c^2) = (a, b, c + 1)$ $(S_a^3, S_b^3, S_c^3) = (a + 1, b, c + 1)$ $(S_a^4, S_b^4, S_c^4) = (a + 1, b + 1, c + 1)$	$d_1 = 1 + c - u_c,$ $d_2 = a - c - u_a + u_c,$ $d_3 = -a + b + u_a - u_b,$ $d_4 = -b + u_b,$
Case 1.3	$(S_a^1, S_b^1, S_c^1) = (a, b, c)$ $(S_a^2, S_b^2, S_c^2) = (a, b, c + 1)$ $(S_a^3, S_b^3, S_c^3) = (a, b + 1, c + 1)$ $(S_a^4, S_b^4, S_c^4) = (a + 1, b + 1, c + 1)$	$d_1 = 1 + c - u_c,$ $d_2 = b - c - u_b + u_c,$ $d_3 = a - b - u_a + u_b,$ $d_4 = -a + u_a,$
Case 2.1	$(S_a^1, S_b^1, S_c^1) = (a, b, c)$ $(S_a^2, S_b^2, S_c^2) = (a, b + 1, c)$ $(S_a^3, S_b^3, S_c^3) = (a, b + 1, c + 1)$ $(S_a^4, S_b^4, S_c^4) = (a + 1, b + 1, c + 1)$	$d_1 = 1 + b - u_b,$ $d_2 = -b + c + u_b - u_c,$ $d_3 = a - c - u_a + u_c,$ $d_4 = -a + u_a,$
Case 2.2	$(S_a^1, S_b^1, S_c^1) = (a, b, c)$ $(S_a^2, S_b^2, S_c^2) = (a, b + 1, c)$ $(S_a^3, S_b^3, S_c^3) = (a + 1, b + 1, c)$ $(S_a^4, S_b^4, S_c^4) = (a + 1, b + 1, c + 1)$	$d_1 = 1 + b - u_b,$ $d_2 = a - b - u_a + u_b,$ $d_3 = -a + c + u_a - u_c,$ $d_4 = -c + u_c,$
Case 2.3	$(S_a^1, S_b^1, S_c^1) = (a, b, c)$ $(S_a^2, S_b^2, S_c^2) = (a + 1, b, c)$ $(S_a^3, S_b^3, S_c^3) = (a + 1, b + 1, c)$ $(S_a^4, S_b^4, S_c^4) = (a + 1, b + 1, c + 1)$	$d_1 = 1 + a - u_a,$ $d_2 = -a + b + u_a - u_b,$ $d_3 = -b + c + u_b - u_c,$ $d_4 = -c + u_c.$

Table 2. States sequence and switching times.

The proposed 3D technique is a generalization of the 2D space vector algorithms. One should notice the behaviour of a balanced system without triple harmonics using the 3D algorithm. In this case, one of the four active vectors given by the algorithm has the switching time equal to zero. Then, the problem is reduced to the well known 2D situation.

The algorithm has been successfully implemented with a micro controller in order to prove the technique using a reference vector with triple harmonics and zero sequence. The modulation is the output signal of the micro controller which has been digitally filtered with a low pass filter that eliminates the higher frequencies. In this way, this permits to obtain the output signals of Diode Clamped Inverter (V_a , V_b , and V_c) obtaining signals that follow the input reference signals.

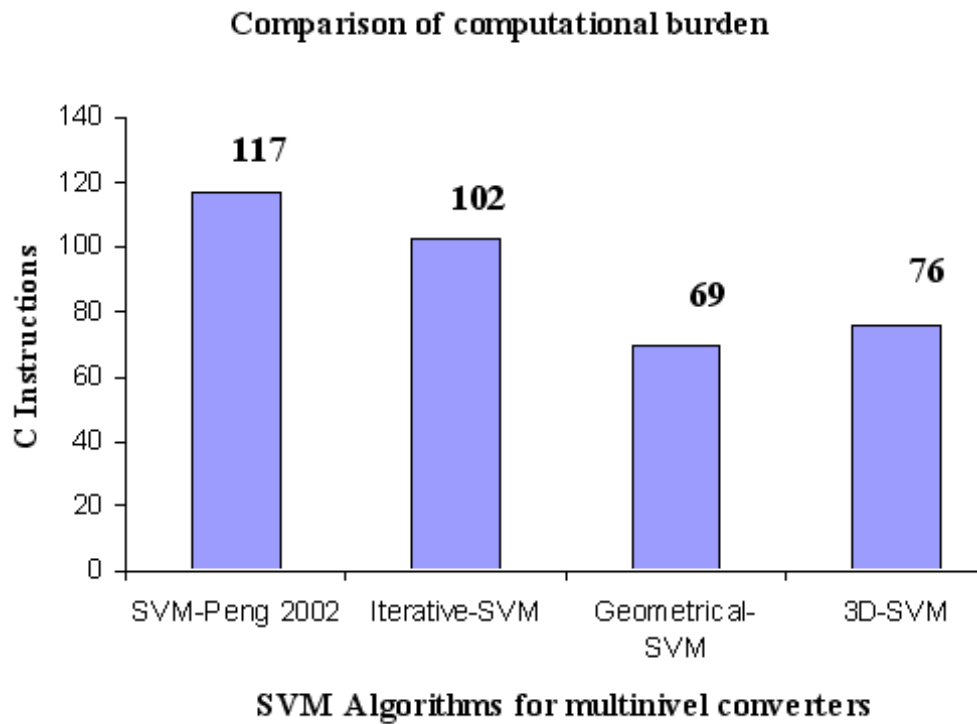


Figure 11: Comparison of computational burden.

Finally, the comparison between the proposed modulation algorithms and a SVM with very low computational burden found in the literature [17], is illustrated in Fig. 11. This figure shows that the complexity of the algorithms and the number of instructions using the proposed methods are drastically reduced compared with other conventional Space Vector Modulation (SVM) and sinusoidal PWM modulation techniques.

3 Conclusions

Three new space vector modulation techniques for multilevel converters are explained in this survey. These algorithms are very useful for the on-line computation of the switching sequence and the on-state durations of the respective switching state vectors corresponding to the modulation of multilevel converters without physical affecting the connected load. The vector selection is adjusted according to the input reference to improve the voltage generation being balanced the DC-link capacitor voltage. These techniques permit an economic and simple electronic implementation and the on-line computation of the switching state vectors for the modulation of a multilevel inverter. Moreover, the space vector modulations present the advantage of eliminating the angle from the calculations and the numeric evaluation of the on-state durations are reduced to a simple addition. The computational burden, the complexity of the algorithms and the number of instructions using the proposed methods are drastically reduced compared with other conventional Space Vector Modulation (SVM) and sinusoidal PWM modulation techniques.

The 3D space vector modulation algorithm, explained in the last section of this paper, directly allows compensating zero sequence in systems with a neutral and optimizing the switching sequence minimizing the number of switching. The computational complexity is very low and independent of the number of levels of the converter. This algorithm does not use trigonometric functions or look-up tables. It has been satisfactorily implemented in very low-cost micro controllers. This technique can be used as a modulation algorithm in all applications needing a 3D control vector such as active filters with four wires with single-phase distorting loads which generate large neutral currents, where the conventional 2D space vector modulations cannot be used.

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