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Abstract: The aluminium incorporation mechanism of perovskite was explored by means of quantum mechanics in combination with equilibrium/off-equilibrium thermodynamics under the pressure-temperature conditions of the Earth's lower mantle (from 24 to 80 GPa). Earth's lower mantle was modelled as a geochemically "not-primitive" object because of an enrichment by 3 wt% of recycled crustal material (MORB-component). The chemical composition of the "non primitive" lower mantle takes into account both chondrite and pyrolite reference models to represent the lower mantle's primitive composition.

The capacity of perovskite to host Al was modelled through an Al2O3 exchange process in an unconstrained Mg-perovskite+Mg-Al-perovskite+free-Al203(corundum) system. Aluminium is globally incorporated principally via an increase in the amount of Al-bearing perovskite [Mg-Al-pv(80 GPa)/Mg-Al-pv(24 GPa) \Box 1.17], rather than by an increase in the Al203content of the average chemical composition which changes little (0.11-0.13, mole fraction of Al2O3) and tends to decrease in Al. The Al2O3 distribution in the lower mantle was described through the probability of the occurrence of given compositions of Al-bearing perovskite. The probability of finding Mg-Al-perovskite is comparable to Al-free Mgperovskite's. Perovskite with Al203 mole fraction up to 0.15 has an occurrence probability of ~28% at 24 GPa, increasing up to ~43% at 80 GPa; on the contrary, perovskite compositions in the range 0.19-0.30 Al203 mole fraction drop their occurrence probability from 9.8 to 2.0%, over the same P-range. In light of this, the distribution of Al in the lower mantle shows that, among the possible Al-bearing perovskite phases, the (Mg0.89Al0.11) (Si0.89Al0.11) O3 composition is the likeliest, providing from 5 to 8% of the bulk perovskite in the pressure range from 24 to 80 GPa. The occurrence of the Al-richest composition, i.e. (Mg0.71Al0.29) (Si0.71Al0.29) O3, is a rare event (probability of occurrence < 1.7%). This study predicts that perovskite may globally host Al203 in terms of 4.3 and 4.8 wt% (with respect to the non-primitive lower mantle mass), thus accounting for \sim 90% and 100% of the bulk Al2O3 estimated in the framework of pyrolite and chondrite reference models, respectively. A calcium-ferrite-type phase (on the MgAl2O4-NaAlSiO4 join) seems to be the only candidate that can compensate for the 10% gap of the perovskite Al-incorporation capacity, in the case of a pyrolite nonprimitive lower mantle model.



TO: Geochimica et Cosmochimica Acta -Editor in chief:

Jeffrey Catalano

Dear Editor,

Please find enclosed the revised manuscript "Aluminum distribution in an Earth's *non-primitive* lower mantle" by Marcello Merli, Costanza Bonadiman (corresponding author) and Alessandro Pavese for potential publication with Geochimica et Cosmochimica Acta.

The text has been revised according to the Associate Editor's and referees' suggestions.

Thank you very much for your consideration and handling.

For the authors,

Costanza Bonadiman

Efferce Bushing.

TO: Geochimica et Cosmochimica Acta -Editor in chief:

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Dear Editor,

Please find enclosed the revised manuscript "Aluminum distribution in an Earth's *non–primitive* lower mantle" by Marcello Merli, Costanza Bonadiman (corresponding author) and Alessandro Pavese for potential publication with Geochimica et Cosmochimica Acta.

The responses to the Associated Editor and Reviewer's comments, along with the changes introduced in the revised version, are discussed and reported in red below.

With best regards,

Costanza Bonadiman

Associate Editor Report: Dear Dr. Bonadiman,

The new version of your manuscript entitled "Aluminium distribution in an Earth's non-primitive lower mantle" for which you are corresponding author has been seen by one of the original reviewers and I have also looked through it myself. The reviewer and myself find that you successfully taken into account the vast majority of criticisms made and generally clarified the contribution. However, the reviewer raises a couple of minor issues that would benefit from modification. Furthermore, while I acknowledge that the English has been greatly improved the text still has some rough edges. I would just like to point out line 241 where the word "sheer" is probably not of use, and line 619 where the sentence appears to be missing something.

Reply: The text has been revised accordingly.

Reviewer #1: The authors have addressed all of my concerns, particularly in explaining their model and assumptions in significantly more detail. For example, they have added appendices that describe their procedure and have expanded the methodology section. They have also added references where needed and improved the English throughout the manuscript. Although there are many assumptions in their model, the authors have now explained the reasons for these assumptions (e.g., the choice to omit iron, how the Gibbs free energy was calculated, the omission of thermal/vibrational contributions, and the choice of Mg/Si ratio), and they have changed the wording of the text to be less dismissive of the implications of these assumptions. I believe that the study's findings on aluminum's distribution in the lower mantle is indeed important for our understanding of the chemistry of the deep Earth and combined with their thorough explanation of the methodology, this manuscript would be

a good contribution to GCA. Below are just a couple questions.

- Apologies about the repeated question, but I still don't understand how a saturation of perovskite's capacity

to host aluminum is a sign for a phase transition to post-perovskite when you don't have post-perovskite in your model?

Authors reply: We agree with R1 that care must be paid about the inferences we drew from the *cor*/perovskite ratio. In such a view, we have changed the text of the revised version accordingly and removed any mention to the question above from the Abstract. However, given that we think that these inferences might be an interesting starting point for a further discussion, we have reported, in the "Discussion" section, arguments to uphold our statements (lines 642-650). With this in mind, the caption of Fig.4 has been changed accordingly.

Also, it seems strange to describe that region as quasi-independent of pressure when you fit a polynomial that clearly has a minimum after which you add an arrow upwards to indicate the possibility of an increase in Al2O3 relative to Mg-Al-pv at higher pressure.

Authors reply: We have discussed the nature of the region 60-80 GPa in a more general way, to include the occurrence of a weak *P*-dependence or a poorly defined minimum (lines 565-566). The use of the arrow (Fig.4) is therefore to be considered in the frame of the comment above.

- line 608: "the phase fraction of Mg-Al-pv remarkably grows upon increasing P" -- I'm not sure what is implied by "remarkably" as there is only a modest increase from 0.41 to 0.48. Authors reply: "Remarkably" has been removed; however, to underline the Al-content change we mention its relative percentage of increase (16%) in the revised version (line 609);
- line 591: if the error is in fact 2.2 kJ/mol for Navrotsky's measurement, your value is in excellent agreement

Authors reply: In the revised version, we stressed that "...observation and theoretical estimate are in good agreement with one another." (line 594).

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1 Aluminium distribution in an Earth's non-primitive lower mantle

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- 11 *Correspondence: Costanza Bonadiman
- e-mail: costanza.bonadiman@unife.it
- 14 **Key-words**: Aluminium distribution, Earth's lower mantle; aluminium bearing perovskite;
- pyrolite, chondrite reference model; MORB-component; enriched lower mantle composition;
- open system.

ABSTRACT

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The aluminium incorporation mechanism of perovskite was explored by means of quantum mechanics in combination with equilibrium/off-equilibrium thermodynamics under the pressure-temperature conditions of the Earth's lower mantle (from 24 to 80 GPa). Earth's lower mantle was modelled as a geochemically "not-primitive" object because of an enrichment by 3 wt% of recycled crustal material (MORB-component). The chemical composition of the "non primitive" lower mantle takes into account both chondrite and pyrolite reference models to represent the lower mantle's primitive composition. The capacity of perovskite to host Al was modelled through an Al₂O₃ exchange process in an unconstrained Mg-perovskite+Mg-Al-perovskite+free-Al₂O₃(corundum) system. Aluminium is globally incorporated principally via an increase in the amount of Al-bearing perovskite $[Mg-Al-pv(80 \text{ GPa})/Mg-Al-pv(24 \text{ GPa})\approx 1.17]$, rather than by an increase in the Al₂O₃-content of the average chemical composition which changes little (0.11-0.13, mole fraction of Al₂O₃) and tends to decrease in Al. The Al₂O₃ distribution in the lower mantle was described through the probability of the occurrence of given compositions of Al-bearing perovskite. The probability of finding Mg-Al-perovskite is comparable to Al-free Mg-perovskite's. Perovskite with Al₂O₃ mole fraction up to 0.15 has an occurrence probability of ~28% at 24 GPa, increasing up to ~43% at 80 GPa; on the contrary, perovskite compositions in the range 0.19-0.30 Al₂O₃ mole fraction drop their occurrence probability from 9.8 to 2.0%, over the same Prange. In light of this, the distribution of Al in the lower mantle shows that, among the possible Al-bearing perovskite phases, the (Mg_{0.89}Al_{0.11})(Si_{0.89}Al_{0.11})O₃ composition is the likeliest, providing from 5 to 8% of the bulk perovskite in the pressure range from 24 to 80 GPa. The occurrence of the Al-richest composition, i.e. (Mg_{0.71}Al_{0.29})(Si_{0.71}Al_{0.29})O₃, is a rare event (probability of occurrence < 1.7%). This study predicts that perovskite may globally host Al₂O₃ in terms of 4.3 and 4.8 wt% (with respect to the non-primitive lower mantle mass),

- thus accounting for $\sim 90\%$ and 100% of the bulk Al_2O_3 estimated in the framework of pyrolite
- and chondrite reference models, respectively. A calcium-ferrite-type phase (on the MgAl₂O₄-
- NaAlSiO₄ join) seems to be the only candidate that can compensate for the 10% gap of the
- 46 perovskite Al-incorporation capacity, in the case of a pyrolite non-primitive lower mantle
- 47 model.

1. INTRODUCTION

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The mantle is the Earth's largest division by volume, originally marked by a planetary 50 Siderophile/Lithophile element fractionation. Refractory Lithophile Elements (RLE) 51 condensed from a gas of solar nebula composition at the highest temperature (>1400 K at 10^{-4} 52 atm) compatible with the nebula's physical constraints (Lodders, 2003). RLEs' chemical 53 behaviour prevented metal and sulphide phases from entering both chondrites and metallic 54 cores during the planetary differentiation (Lodders, 2003; Kaminski and Javoy, 2013; Mahan 55 et al., 2018). RLEs include Ca and Al among the major elements, the full group of rare earth 56 elements (REE), U and Th. The chemical characteristics of such elements support the 57 primitive Earth's mantle model that preserves the solar ratios of RLEs (Wasson and 58 Kallemeyn, 1988; Lodders et al., 2009; Wang and Jacobsen, 2016). 59 60 Aluminium is the sixth most abundant element on Earth: it is a purely refractory lithophile element and its natural abundance is provided by the stable isotope ²⁷Al. The radioactive 61 isotope 26 Al quickly decayed in 26 Mg (26 Al half-life = $7.17 \pm 0.24 \times 10^5$ yr; Norris et al., 1983, 62 Wu and Browne, 1997) during the early stage of the solar system's evolution (Lee et al., 63 1977; Lodders, 2003; Baker et al., 2012). The ²⁶Al decay provided substantial heating to the 64 proto planetary bodies, and its isotopic daughter is one of the most widely used extinct 65 radioactivity chronometers (Bizzarro, et al., 2005; Spivak-Birndorf et al. 2009; Wimpenny et 66 al., 2019). 67 Taking into account the geochemical behaviour of aluminium, it is unlikely that a large 68 69 amount of such element may enter the Earth's core, though it provides a major constituent of many minerals at any depth of the Earth's mantle and crust. Aluminium is also one of the 70 main components of any melt generated from the upper mantle, in terms of 9-21 wt% Al₂O₃ 71 on average (source: PetDB Petrological Database). Melt crystallization, segregation, rise and 72

cooling, led to the formation of the crust over the Earth's history. An intriguing aspect is that

- Al, as a crustal component, partially, or entirely, was transported into the mantle, through
- subduction. Such a process could involve mantle portions well below the magma source
- regions (Young et al., 2005; Tsuchiya and Tsuchiya, 2008; Wang and Jacobsen, 2016).
- 77 Seismic tomography reveals that near the Earth's mantle transition zone, which marks the
- boundary between upper and lower mantle, repositories of crustal material occur (Christensen
- and Yuen, 1984; Billen, 2010, King et al., 2015). They exhibit different dynamic behaviours:
- i) stagnation in the mantle transition zone (Japan trench; Honda, 2017 and references therein);
- 81 ii) stagnation in the uppermost lower mantle (Peruvian Andes; Fukao and Obayashi 2013); iii)
- 82 continuous descent, seemingly unhindered, into the lower mantle (Farallon plate, North
- America; Sigloch et al., 2008). Such tomographic observations suggest a mechanism of global
- 84 mantle convection with an abundant mass exchange between distinct geochemical reservoirs
- lying in both the upper and lower mantle (van der Hilst et al., 1997; Nolet et al., 2007).
- 86 More recently, geochemical models, aimed at explaining the isotopic evolution of the silicate
- 87 Earth (Kumari et al., 2016; Jones et al., 2019) or at tracing the distribution of key components
- 88 (H₂O and Fe-Mg) in the lower mantle (Walter et al., 2015; Merli et al., 2016; 2017), have
- 89 depicted the Earth's mantle as a chemical reservoir ("pyrolite") involving uninterrupted
- 90 geochemical reactions and energy/matter flows.
- 91 In particular, Kumari et al. (2016) estimated that about 60% of the entire mantle is as depleted
- 92 in fusible elements (i.e. Al and Ca) as its upper portion, whereas the remaining mantle is non-
- primitive, containing a small fraction of transient and isolated recycled crustal materials.
- Jones et al. (2019), combining the geodynamic model of mantle convection with isotope and
- 95 trace element geochemistry, suggest that the subduction and accumulation of dense oceanic
- 96 crust produce in the deep mantle a large mass of material enriched in incompatible trace
- 97 elements. The quoted authors also state that an equivalent of 50-70% of the current
- 98 continental crust mass was accumulated earlier than 3 Ga ago, and that the crustal recycling
- and reworking dominated over juvenile additions to the continental crust, since the end of the

Archean (2.5 Ga). This suggests that since the end of the Hadean age (~ 4.6-3.8 Ga) the 100 101 Earth's lower mantle has been enriched with crustal components. Understanding the structure and chemical-physical behavior of the slabs subducted into the 102 mantle is out of the scope of the present work. Conversely, we focus on the chemical 103 rearrangement of the main lower mantle mineral phases in the case of a full mixing between 104 crustal slabs and primordial lower mantle. In such a view, aluminium may be an effective 105 106 "probe" among the major elements. 107 The present work deals with the modelling of Al-incorporation in perovskite, the major phase in the lower mantle, and the resulting Al-distribution, by means of quantum mechanics 108 109 calculations in combination with equilibrium/off-equilibrium thermodynamics and cluster expansion technique. The cluster expansion approach allows the investigation of large atom 110 clusters, thus providing an effective tool to model solid mixing in a statistical framework (see 111 Merli et al. 2015, and references therein). Because of the complexity of the natural processes, 112 it is convenient to start from a "reference" mineral phase, i.e. MgSiO₃-perovskite, whose Al-113 enrichment is investigated. We explore the P-range from 24 to 80 GPa, to unquestionably 114 leave the perovskite-to-post perovskite transition aside (Murakami et al., 2004; Tsuchiya and 115 Tsuchiya, 2008; Shim et al., 2008). 116 117 Our main goal is to estimate the maximum intrinsic capacity of perovskite to incorporate aluminium and its phase proportion with respect to the Al-free perovskite fraction, as a 118 function of P-T. Subsequently, the resulting Al-partitioning will be used to discuss the global 119 120 mechanism of storage of aluminium in the lower mantle.

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2. GEOCHEMISTRY

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2.1 Lower mantle geochemical model

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Cosmochemical arguments supporting a chondritic bulk Earth composition (chondrite 126 reference model) imply that the lower mantle must be enriched in Si with respect to a 127 primitive upper mantle (PUM; Javoy et al., 2010; Murakami et al., 2012; Kaminski, and Javoy 128 2013), save that the Earth's core should be able to host ~4-6 wt% Si (McDonough 2014, 129 Badro et al., 2014) to balance the Earth's Si-budget against the Sun's and chondrite's 130 [Mg/Si_(PUM)~1.21-1.31 versus Mg/Si_(lower mantle)~1.01]. Conversely, according to petrological 131 132 data and chondritic constraints the lower mantle is chemically equivalent to the primitive upper mantle (pyrolite reference model; McDonough and Sun,1995; Lyubetskaya and 133 134 Korenaga, 2007). Tomographic images of subducted slabs plunging into the deep mantle have been interpreted 135 in terms of an efficient mass transfer between upper and lower mantle domains. This supports 136 large scale mixing and therefore a homogenous Mg/Si distribution (i.e. pyrolite) throughout 137 the mantle (Sigloch et al., 2008; van der Hilst et al., 1997). However, only a limited number 138 139 of slabs actually sink into the lower mantle, given that most of the subducted ones flatten and seem to stagnate at either ~660 km or ~1,000 km depth (Fukao and Obayashi 2013). This 140 points towards a comparatively ineffective mixing process and contrasts the notion of a 141 vigorous global mantle convection. Recently, Ballmer et al. (2017) have hypothesised the 142 presence of stable large-scale high-viscosity bridgmanite-enriched ancient mantle structures 143 (BEAMS) that have been residing in the Earth's lower mantle since the early stage of our 144 planet's formation. Their numerical model also predicts the incorporation of limited amounts 145 of crustal material from shallow to deep mantle, particularly during the early stages. Such 146 crustal portions provide stretched and stirred long-lived "fossil" fragments, in keeping with 147 tomographic observations. Therefore, large-scale heterogeneities may account for the Earth's 148 bulk composition, bringing the lower mantle's Mg/Si ratio closer to the solar-chondritic one 149 unlike the upper mantle. 150

Hereafter, we shall refer to either the "pyrolite model" (based on the pyrolite composition throughout the mantle) or the "chondrite model" (relying on different compositions between upper and lower mantle) to describe the lower mantle.

Whatever bulk composition model is used to interpret the mantle's dynamics, the crustal components plunging into the lower mantle cause large/small-scale changes of its phase composition (Irifune et al. 1996; McDonough, 2016; Nestola et al., 2018).

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2.2 Enriched (non-primitive) lower mantle bulk composition

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Both chondrite and pyrolite lower mantle models are used here to estimate the non-primitive lower mantle compositions. The bulk chemical composition of the lower mantle is generally described in terms of its five major oxides (MgO, FeO, CaO, Al₂O₃ and SiO₂), which account for ~98.5 wt% of the Earth's mantle mass (Mc Donough, 2016; Palme and O'Neill, 2014). Na₂O occurrence, even if of modest impact on the large-scale geophysical and geochemical modelling (Bina and Helffrich, 2014; Palme and O'Neill, 2014 Chust et al., 2017), is still important in terms of the resulting minor mineral phases that affect the Al distribution in the lower mantle. Experiments and observations on natural samples reveal that potential Albearing lower mantle phases may also include K, Fe³⁺ and OH as major elements (i.e.: Kato et al., 2013; Wang et al., 2015; Pamato et al., 2015; Harte and Richardson, 2012). In particular, Al-bearing phases are able to host potassium if they form in a system containing at least ~ 0.09 wt% K₂O (Kato et al., 2013). Note that the mid-ocean-ridge basalt (MORB) average composition has 0.08-0.12 wt% K₂O (Gale et al., 2013), whereas pyrolite and chondrite lower mantle models are estimated to bear ~0.03 and <0.01 wt% K₂O, respectively (McDonough and Sun, 1995; Javoy et al., 2010). Therefore, K-bearing phases are not expected to play a relevant role as potential aluminium hosts among the lower mantle phases. Although ferric iron is able to affect Al^{3+} storage in perovskite-like structures via $Fe^{3+} \leftrightarrow Al^{3+}$ replacement

(Kurnosov et al., 2017), the Fe³⁺/ \sum Fe_{tot} ratio in the primitive Earth's mantle is supposed to be 177 very small, i.e. ~0.03, according to mass balance calculations (Palme and O'Neill, 2014). 178 Bulk H₂O (hosted as OH-group) in the lower mantle influences the aluminium content 179 incorporated by perovskite through the formation of Al-bearing hydrous phases. However, the 180 bulk H₂O content is comparatively modest and estimated ~1500 ppm, in both pyrolite and 181 182 chondrite lower mantle models (Merli et al., 2016; Muir and Brodholt, 2018). 183 Let us consider the lower mantle as a geochemically non-primitive object because it is mixed with a fraction of recycled crustal material (i.e. MORB-component). In this view, Al₂O₃ and 184 185 CaO, hosted in lower mantle minerals, are potential "probes" which mark the occurrence of such a geodynamic process (Guignot and Andrault, 2004, Hirose et al., 2005; Korenaga, 186 2009; Irifune et al., 2010; Ricolleau et al., 2010). 187 The MORB chemical composition is enriched in incompatible major elements (aluminium, 188 calcium and, to a lesser extent, iron) and depleted of compatible elements (magnesium) with 189 respect to the mantle (Table 1). Therefore, a MORB-like composition at lower mantle P-T 190 conditions cannot give Fe-periclase, whereas high-pressure SiO₂-rich phases (e.g. Ca-191 perovskite and bridgmanite) and additional aluminium-rich phases are expected to occur. 192 Following experimental results about MORB bulk compositions (14-16 wt% Al₂O₃) under 193 lower mantle conditions (30-90 GPa), the newly formed Al₂O₃-rich phases (NAL-type phase 194 and CaFe₂O₄-type phase, i.e. CF-phase, on the join MgAl₂O₄-NaAlSiO₄) may account for 195 196 about 10-12 mol% by phase composition (Guignot and Andrault, 2004, Ricolleau et al., 2010). 197 Assuming that subducted crustal fragments have been sliding down into the mantle over the 198 past 4 billion years (the most generous estimate is about 11 wt% of the whole mantle; Li and 199 McNamara, 2013), aluminium-rich domains should have developed, in contrast to 200 expectations from a primitive lower mantle's composition (Stixrude and Lithgow-Bertelloni, 201 202 2012).

We model such an enrichment using the simple binary mixing equation of Faure (1986) to combine primitive lower mantle compositions (pyrolite and chondrite, corresponding to the end-members "A" and "A1", respectively; see Table 1) with a crust-type-composition (endmember "B"; MORB-like silicate glass; see Table 1). End-member B is close to the N-MORB average of Gale et al. (2013) and has been largely used in HP experiments (i.e. Hirose et al., 1999; 2005 Funamori et al., 2000; Guignot and Andrault, 2004; Ricolleau et al., 2010). According to the extensive compilation provided by the PetDB-database of chemical data from mid-ocean ridge basalts, the water concentrations lie in the range 0.05-1.0 wt%. The amount of H₂O stored in the deep mantle, computed by experiments and mass balance models (Ghosh et al., 2014; Marty, 2012), is in the range 800-2700 ppm (i.e. 0.08-0.27 wt%). Taking into account such figures and the tomographic observations that suggest that only small fractions of descending slabs reach the lower mantle (Ballmer et al. 2017), we model a nonprimitive lower mantle composition by a chemical mixing of primitive pyrolite/chondrite compositions with a 3 wt% end-member B's contribution (0.1 wt% of H₂O). The resulting compositions are reported in Table 1. Such chemical mixing ideally reproduces a nonprimitive lower mantle as predicted by modelling the isotopic evolution of the silicate Earth: ~3 wt% of the total mantle mass is expected to be stored and ultimately mixed within ~1 Ga in the lower mantle (Christensen and Hofmann 1994; Kumari et al., 2016; White, 2015).

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3. METHODS

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3.1 Chemical probability of formation: aluminium-bearing phases in the lower mantle

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The probability that a phase "J" forms at P-T, *i.e.* p(J|P,T), can be roughly estimated in terms of $p(J|P,T) \propto p(J,\text{chem}) \times \exp(-\Delta G(P,T)_{\text{formation}}/RT)$, where p(J,chem) is the probability of having the required chemical species for J under the constraint of a given available elemental budget

- and $\Delta G(P,T)_{\text{formation}}$ is the formation Gibbs energy. p(J,chem) is termed "chemical probability
- of formation", to underline that it reflects the likelihood of having the required elements to
- form the J-phase, and it is calculated as follows.
- Let us assume X_k to represent the fractional abundance value of the k^{th} -oxide, in a generic
- 233 system. Given that

$$\sum_{k=1,M} X_k = 1 {1}$$

- then X_k can also be associated with the *probability* of having the k^{th} -oxide, if the oxides are
- supposed to be uniformly distributed as a function of space. The chemical composition of the
- 237 J-phase is then expressed formally as

$$J = \sum_{k} n_k X_k \tag{2}$$

- Therefore, the probability of finding one mole of the J-phase as a function of its pure chemical
- composition, p(J,chem), is provided by the joint events of i) having $(n_1$ -moles of $X_1)(n_2$ -moles
- of X_2)... and ii) not having any species with stoichiometric coefficient equal to 0. This
- 242 corresponds to the following joint probability:

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$$p(J, \text{chem}) \propto \prod_k p(k)^{n_k} \times (1 - \sum_m p(m)) \propto \prod_i X_i^{n_j} \times (1 - \sum_m X_m)$$
 (3)

- where p(k) and p(m) are the probabilities of finding the k^{th} and m^{th} oxide, respectively; the
- subscript k is associated with the chemical species with stoichiometric coefficients other than
- zero, whereas m is related to those with stoichiometric coefficients equal to zero. The
- p(J,chem) values calculated in this way are then normalized so that their sum yields unity.
- Table 2 reports major phases and potential Al-bearing phases that experiments, numerical
- 249 modelling and exceptional observations on natural findings indicated as possible minerals in a
- 250 non-primitive lower mantle (Table 1).
- 251 Preliminary calculations led us to rule out periclase as a host of aluminium, save that the Al-
- incorporation takes place with the contribution of H (Merli et al., 2016). In such a case, the
- amount of Al involved would be negligible, anyway. Panero et al. (2006) estimated regular
- solution parameters of 12 and 66 kJ/mol for perovskite and akimotoite, respectively. Taking

- into account i) the significantly lower energy for Al-incorporation in perovskite than in
- akimotoite and ii) the restricted range of occurrence of the latter (Panero et al., 2006), we
- exclude akimotoite as a possible competitor to uptake Al in the *P-T* region under investigation
- 258 (Stebbins et al., 2001; Li et al. 2008; Tschauner et al., 2018). Majorite garnet, which is the
- 259 main host of aluminium in the mantle transition region in both pyrolite and basaltic
- 260 compositions (Irifune and Ringwood, 1993; Litasov and Ohtani, 2007), is transformed into
- 261 Mg-perovskite+Ca-perovskite at pressures corresponding to the uppermost lower mantle.
- Experiments show that aluminium is mostly incorporated by Mg-perovskite/bridgmanite in
- pyrolite or chondrite compositions under lower mantle *P-T* conditions (Irifune et al.,1996;
- Ricolleau t al., 2008), whereas separate aluminous phases form in basaltic compositions
- 265 (Hirose et a.,1999; 2005) at the same *P-T* conditions.
- In a non-primitive lower mantle, aluminium is partitioned between perovskite/bridgmanite
- and minor Al-bearing phases, such as:
- 268 i) alkali rich NAL-structure phases, like those on the join NaMg₂Al_{4.8}Si_{1.15}O₁₂-
- 269 KMg₂Al_{4.8}Si_{1.15}O₁₂ (Gasparik et al., 2000; Kato et al., 2013; Wu et al., 2016). However, as
- stated above, K-bearing phases are unlikely to develop in the lower mantle because of the lack
- of a sufficient amount of potassium;
- ii) CF-structure and NAL-structure polymorphs, on the join MgAl₂O₄-NaAlSiO₄ (Imada et al.,
- 273 2011; 2012; Irifune et al., 1991). Note that the CF-structure was observed to stabilize at a
- 274 higher pressure (~ >40 GPa) than the NAL-structure (~ 24-40 GPa) (Imada et al., 2011;
- 275 Guignot and Andrault, 2004);
- 276 iii) possible hydrous solid solutions involving D-phase, H-phase and δ -AlOOH (Ghosh and
- 277 Schmidt, 2014; Pamato et al., 2015; Walter et al., 2015; Fukuyama et al., 2017).
- 278 In the case of NAL- and CF-phases, we chose to calculate a *chemical probability of formation*
- 279 p(J,chem) for a reference NAL/CF-mineral, that is Na_{0.265}Fe_{0.245}Mg_{0.375}Ca_{0.035}Al_{1.1}Si_{0.715}O₄.
- Such a composition is obtained from Guignot and Andrault (2004), by averaging those that

the authors labelled with "CF^A" and "CF^{B1}", neglecting Ti and normalizing to 4 oxygen atoms

and 3 cations.

Hereafter we shall use the following acronyms, for the sake of brevity: Mg-pv, "Mg-

perovskite", for perovskite tout court, i.e. MgSiO3; Mg-Al-pv, "Al-perovskite", for Al bearing

Mg-perovskite, i.e. (Mg,Al)(Si,Al)O₃; Mg-Fe-pv, "bridgmanite", for Fe-bearing Mg-

perovskite, i.e. (Mg,Fe)SiO₃; Ca-pv, "Ca-perovskite", for Ca-bearing perovskite, i.e.

(Ca,Mg)SiO₃; "perovskite", for any solid mixing, or end member, occurring in the lower

mantle and having perovskite-type structure; Fe-pe, "Fe-periclase", i.e. (Mg,Fe)O; CF, "CF-

phase", for a phase in the MgAl₂O₄-NaAlSiO₄ join.

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3.2 Aluminium incorporation mechanisms of perovskite

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To evaluate the aluminium distribution in a non-primitive lower mantle, we model the Al-

uptake capacity of perovskite, which is the lower mantle phase able to host aluminium to such

an extent as to provide a relevant storage by volume (Jeanloz and Knittle, 1989; Ricolleau et

296 al.,2009).

We introduce the notion of "maximum Al-uptake capacity" of perovskite. "Maximum Al-

uptake capacity"-conditions are set through a virtual competition between MgSiO₃ and Al₂O₃

299 (ideal *pure* alumina phase) to accommodate Al, at lower mantle P-T conditions and in a SiO₂-

MgO-Al₂O₃ system. Corundum (cor) is the least "prejudicial" phase as an Al-host, given that

it does not require any further chemical species but aluminium to form and is the Al₂O₃-

polymorph stable in the *P-T* range of interest (Merli and Pavese 2018).

The incorporation mechanism of a trivalent cation in perovskite is supposed to occur through

three main reactions (Navrotsky et al., 2003; Akber-Knutson et al., 2005 and references

305 therein):

306 (i)
$$Si^{4+} + Mg^{2+} = M^{3+} + M^{3+}$$

307 (ii)
$$Si^{4+} = M^{3+} + 1/2 V_0^0$$

308 (iii)
$$Si^{4+} = M^{3+} + H^+$$
.

- Reaction (i), which takes place *via* a charge-coupled-mechanism, is the likeliest one, as shown
- 310 by energy calculations (Yamamoto et al., 2003; Akber-Knutson et al., 2005; Zhang and
- 311 Oganov, 2006). A comparison between incorporation mechanisms (i) and (ii) reveals that the
- 312 former is slightly exothermic, in contrast with the endothermic behaviour of the latter
- 313 (Navrotsky et al., 2003). NMR-measurements point to the occurrence of a charge-coupled
- mechanism (Stebbins et al., 2001), in agreement with calculations of Akber-Knutson and
- Bukowinski (2004), who suggest that Al tends to replace both Si and M²⁺, in a high pressure
- and high temperature regime. As to reaction (iii), we assume contents of H_2O , *i.e.* H^+ supplier,
- and Al_2O_3 as much as 1500 ppm (0.15 wt%) and 4.76 wt%, respectively (Table 1), in keeping
- with the lower mantle Al-richest composition obtained by mixing pyrolite with 3% MORB-
- 319 component (Table 1). In such a case, even if all the hydrogen from the dissociation
- 320 OH₂→OH⁺+H⁺ contributed to an exchange mechanism like (iii), just 0.08 mol fraction
- aluminium might be accounted for. Moreover, according to the H₂O-partitioning estimated by
- Merli et al. (2016), periclase is able to account for 1/3 of the trapped H₂O, thus reducing
- 323 further the role of reaction (iii) as a possible relevant mechanism to Al-incorporation in
- 324 perovskite.
- 325 Therefore, the Al-uptake in perovskite is modelled by the replacement of Mg-Si with Al-Al,
- according to the exchange reaction reported below using the formalism of Kröger-Vink
- 327 (Kröger, 1972)

328
$$Al_2O_3 + [Mg_{Mg}]^X + [Si_{Si}]^X \leftrightarrow [Al_{Mg}]^* + [Al_{Si}]^* + MgSiO_3.$$
 (4)

- Assuming λ -mole of Al₂O₃ to be exchanged in the Mg-Al-pv, Mg-pv and cor system, then
- equ.(4) leads to

331
$$(1-\lambda)MgSiO_3 + \lambda Al_2O_3 \Leftrightarrow (Mg_{1-\lambda}Al_{\lambda})(Si_{1-\lambda}Al_{\lambda})O_3.$$
 (5)

In reaction (5) iron can affect the energy through a replacement like $Mg^{2+} \Leftrightarrow Fe^{2+}$ and competes with aluminium in terms of $Al^{3+} \Leftrightarrow Fe^{3+}$. However, we chose to neglect Fe as we are developing a first approximation model, which would provide general trends rather than details. Our choice can be further supported by the following arguments.

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• The general reaction that accounts for Al_2O_3 entering in bridgmanite turns out to be $(Mg_{1-x}Fe_x^{2+})SiO_3 + \lambda Al_2O_3 = (Mg_{1-x-\lambda/2}Fe_{x-\lambda/2}^{2+}Al_\lambda)(Si_{1-\lambda}Al_\lambda)O_3 +$

$$\lambda \left(Mg_{\underline{1}}Fe_{\underline{1}}^{2+}\right) SiO_{3} \tag{6}$$

where we assume that Al replaces the same quantity of Mg and Fe²⁺, the latter dwelling at the 12-coordination site, only (Kaminsky and Lin, 2017). The parametrization of the Gibbs energy used in the present work relies upon the cluster expansion technique (Merli et al., 2015; 2017). Such a method leads to expressing energy as a function of the number of interacting atomic pairs that belong to the same cluster determined as a function of the distance between the involved chemical species. Assuming Fe-Al pair entering the perovskite structure as much as 0.1-0.2 moles (i.e. Kurnosov et al., 2017; Kaminsky and Lin, 2017), the probability of having a Fe-Al interacting pair belonging to the first/second cluster is ~5-6 %. Therefore, most of the interactions with aluminium atoms are due to the pure Mg-Si matrix, which governs the "maximum intrinsic capacity" of perovskite to incorporate Al. The role of Fe³⁺ is extensively debated and still largely uncertain. Mg-Fe-pv is potentially the major Fe³⁺ acceptor, but Kaminsky and Lin (2017) indicated that in natural lower mantle bridgmanites iron most likely occurs as ferrous at the 12coordination sites. Conversely, Kurnosov et al. (2017) claim $Fe^{3+}/\Sigma Fe_{tot} = 0.33$, in synthetic bridgmanite with ferric iron sited at the same coordination site, under lower mantle conditions ($P \sim 35$ GPa; 1300 km depth; Ismailova et al. 2016). Mass balance calculations, in turn, predict an impact of ferric iron in terms of Fe³⁺/ Σ Fe_{tot}~0.03, with respect to the Earth's mantle abundances (Palme and O'Neill, 2014). If we consider as a first level of approximation pyrolite (Mg-Fe-pv =76 wt%; FeO_{tot} = 8.05 wt%) and chondrite (Mg-Fe-pv =85 wt%; FeO_{tot} = 8.12 wt%) lower mantle models (Table 1), and apply the Kurnosov et al. (2017) Fe³⁺/Fe_{tot} ratio to Mg-Fe-pv, the resulting Al³⁺/Fe³⁺ mole ratios in bridgmanite are ~3.6 and ~2.9 for pyrolite and chondrite models, respectively. Tests based on calculations that we carried out to reproduce the replacement schemes Si + Mg \Leftrightarrow Al + Fe³⁺ versus Si + Mg \Leftrightarrow Al + Al, indicate that the second reaction is favoured over the former one [in agreement with the results of Nishio-Hamane et al. (2005)].

3.3 Reaction models

The Al-uptake mechanism in perovskite according to reaction (5) is addressed using two approaches: i) the *open system model*, which exploits the notion of stationary thermodynamic state and allows an exchange of matter between system and reservoir (Prigogine 1968); ii) the *closed system model*, which relies on equilibrium thermodynamics, therefore excluding any sort of matter exchange. In an open system, the stationary state replaces the equilibrium state and exhibits thermodynamic observables, which remain invariant over time. Details about the open system model are reported in APPENDIX I.1-.2-.3 and a brief overview is given below.

3.3.1 Open system model

We would like to exploit the capacity of an open system to exchange matter with a reservoir, in combination with a formalism as close as possible to the consolidated equilibrium thermodynamics' one. Such a model provides a flexible tool to address problems in which the intrinsic exchanging/incorporation capacity of a given substance can be investigated, without any sort of constraint or restraint (APPENDIX I.1).

- 383 The key requirement is the fulfilment of the following equation, associated to reaction (5) via
- the equilibrium constant K (APPENDIX I.2-3):

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$$K(P,T,\lambda) = exp[-\Delta G_0(P,T,\lambda)/RT] = a_{Mg-Al-pv}/(a_{Mg-pv}^{1-\lambda} \times a_{cor}^{\lambda}) \approx x_{Mg-Al-pv}/(a_{Mg-pv}^{1-\lambda} \times a_{cor}^{\lambda})$$

$$386 \quad \left(x_{Mq-pv}^{1-\lambda} \times x_{cor}^{\lambda}\right) \tag{7.a}$$

- 387 where x_i =phase proportion of the jth-component/phase (cor: corundum); a_i =jth-
- component/phase's activity. In equ.(7.a) the activity coefficient is approximated to unity (see
- APPENDIX I.3 and APPENDIX II). Expanding ΔG_0 , it follows that:

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$$\Delta G_0(P,T,\lambda) = \mu_0(P,T,\lambda)_{Mg-Al-pv} - \lambda \times \left[\mu_0(P,T)_{cor} - \mu_0(P,T)_{Mg-pv}\right] - \mu_0(P,T)_{Mg-pv}.$$

391
$$(7.b)$$

- where μ_0 is the part of the chemical potential depending on λ , P and T, only (Ottonello 1997;
- 393 2010). For convenience, we split the chemical potential of Al-incorporating perovskite (Mg-
- 394 Al-pv) into an Al-free part, i.e. pure perovskite (Mg-pv), and a part dependent on aluminium,
- 395 that is

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$$\mu_0(P,T,\lambda)_{Mq-Al-pv} = \mu_0(P,T)_{Mq-pv} + \Delta\mu_0(P,T,\lambda)_{Mq-Al-pv},$$
 (7.c)

- where $\Delta \mu_0(P,T,\lambda)_{Mg-Al-pv}$, which accounts for the solid mixing occurrence and provides the
- 398 very core of our computational model, is calculated by the cluster expansion method (Merli et
- 399 al 2015, 2017).
- 400 Using equ.(7.c), equ.(7.b) becomes

$$\Delta G_0(P,T,\lambda) = \Delta \mu_0(P,T,\lambda)_{Mg-Al-pv} - \lambda \left[\mu_0(P,T)_{cor} - \mu_0(P,T)_{Mg-pv} \right]. \tag{8}$$

- 402 At given (P,T,λ) -values, we seek the $\{x_{Mg-Al-pv}, x_{Mg-pv}, x_{cor}\}$ -sets that fulfil
- 403 a) equ.(7.a),
- 404 b) $x_{Mg-Al-pv}, x_{Mg-pv}, x_{cor} \ge 0$,
- 405 c) $x_{Mg-Al-pv} + x_{Mg-pv} + x_{cor} = 1$.
- 406 Among the solutions that satisfy the constraints a), b) and c), we chose the one that minimizes
- 407 the Gibbs energy, namely $x_{Mg-Al-pv} \times \mu_0(P,T,\lambda)_{Mg-Al-pv} + x_{Mg-pv} \times \mu_0(P,T)_{Mg-pv} + x_{cor} \times \mu_0(P,T)_{cor}$. In

- doing so, we obtain a triple, yielding Mg-Al-pv/Mg-pv/cor phase proportions, for each (P,T,λ)
- point, *i.e.* $\{x_{Mg-Al-pv}, x_{Mg-pv}, x_{cor}\}(P,T,\lambda)$. The preservation of the total chemical composition of
- 410 the system constituted by each $\{x_{Mg-Al-pv}, x_{Mg-pv}, x_{cor}\}(P,T,\lambda)$ -triple is not required. The
- resulting system therefore behaves as an open system that can exchange 2Al ⇔ Mg+Si with a
- reservoir. In general, we are interested in modelling observables whose values are averages
- over the λ -range, so that they depend ultimately on P-T only. For instance:

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$$\{x_{Mg-Al-pv}, x_{Mg-pv}, x_{cor}\}(P, T) = \frac{1}{c} \int_{\lambda-inf}^{\lambda-sup} \{x_{Mg-Al-pv}, x_{Mg-pv}, x_{cor}\}(P, T, \lambda) d\lambda$$
 (9. a)

415
$$\lambda_{\text{Al2O3}}(P,T) = \int_{\lambda-inf}^{\lambda-sup} \lambda \times x_{Mg-Al-pv}(P,T,\lambda) \, d\lambda/x_{Mg-Al-pv}(P,T)$$
 (9.b)

416
$$Tot_{\text{Al2O3}}(P,T) = \frac{1}{c} \int_{\lambda - inf}^{\lambda - sup} \left[\lambda \times x_{Mg-Al-pv}(P,T,\lambda) + x_{\text{Al2O3}}(P,T,\lambda) \right] d\lambda$$
 (9.c)

- where: C is a normalization constant; λ -sup=0.3 and λ -inf=0, upper and lower thresholds of λ ,
- respectively (for λ >0.3, $x_{Mg-Al-pv}$ is negligible on the *P-T* range explored); λ_{Al2O3} of (9.b) is the
- 419 average Al₂O₃ mole fraction per formula unit; Tot_{Al2O3} is the total Al₂O₃ stored by the (Mg-
- 420 Al-pv)+(Mg-pv)+cor system.
- 422 3.3.2 Closed system model

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- 423 For the sake of completeness, we also present the closed system model. We seek the
- equilibrium conditions of reaction (5) for a closed system, *i.e.* a chemically adiabatic one. Let
- 425 ξ represent the aluminium occupancy factor in Mg-Al-pv [i.e. $(Mg_{1-\xi}Al_{\xi})(Si_{1-\xi}Al_{\xi})O_3$].
- Therefore, we have to minimize, with respect to ξ , the Gibbs energy of the system (Mg-
- 427 pv)+(Mg-Al-pv)+cor, i.e.

428
$$G = n_{cor} \times \mu_0(P, T)_{cor} + n_{pv} \times \mu_0(P, T)_{Mg-pv} + n_{Mg-Al-pv} \times \mu_0(P, T, \xi)_{Mg-Al-pv}, \quad (10)$$

under the constraints of the conservation of mass:

430
$$M_{A12O3} = n_{cor} + n_{Mg-Al-pv} \times \xi$$
 (11)

431
$$M = M_{SiO2} = M_{MgO} = n_{Mg-pv} + n_{Mg-Al-pv} \times (1-\xi),$$
 (12)

- where M_{Al2O3} , M_{SiO2} and M_{MgO} are fixed total amounts in moles of Al_2O_3 , SiO_2 and MgO.
- 433 Using the constraints above, equ.(10) becomes

434
$$G = \left(M_{\text{Al2O3}} - n_{Mg-Al-pv} \times \xi\right) \times \mu_0(P, T)_{cor} + \left(M - n_{Mg-Al-pv} \times (1 - \xi)\right) \times \mu_0(P, T)_{cor}$$

435
$$\mu_0(P,T)_{Mq-pv} + n_{Mq-Al-pv} \times \mu_0(P,T,\xi)_{Mq-Al-pv}$$
 (13)

436 The Gibbs energy minimum condition requires

$$\frac{\partial G}{\partial \xi} = 0,$$

from which the following equation is derived

$$-\mu_0(P,T)_{cor} + \mu_0(P,T)_{Mg-pv} + \frac{\partial \mu_0(P,T,\xi)_{Mg-Al-pv}}{\partial \xi} = 0.$$
 (14)

- Equ.(14) formalises the equilibrium conditions for closed systems (Chust et al. 2017). Its
- solution, expressed by $\xi_{closed\ system}$, yields the composition of Al-bearing perovskite that
- minimises the Gibbs energy of equ.(13).
- 441 $\xi_{\text{closed system}}$ also minimises (7.b). In fact, taking into account equ.(7.c), equ.(14) is equivalent
- to setting $\frac{\partial \Delta G_0(P,T,\lambda)}{\partial \lambda} = 0$ in equ.(8), which implies that $K(P,T,\xi_{\text{closed system}})$ achieves an
- extreme value that shifts reaction (5) towards its right-hand side member as much as possible.

3.4 Computational

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447 Structure relaxations were performed at a given pressure and 0 K by the HF/DFT-

CRYSTAL14 program (Dovesi el al., 2009), which implements "Ab-initio Linear-

Combination-of-Atomic-Orbitals" for periodic systems. Only static pressure (P_{static} =- $\partial E_{\text{static}}$

 $_{\rm energy}/\partial V)$ and zero-point pressure ($P_{\rm zp}==-\partial E_{\rm vibration\ energy\ at\ 0K}/\partial V)$ were taken into account, given

that even adding a correction for thermal contributions would not significantly change our

results and the conclusions would be unaffected. A zero-point pressure was estimated by

quantum mechanics calculations and using pure perovskite only, resulting in ~5 GPa. The

WCGGA functional (Wu and Cohen, 2006) was used, with a hybridization rate of 28%. Such a proportion was adopted because it provides a more satisfactory agreement with observations in terms of perovskite structure, than other choices do. The tolerances governing the accuracy of the integrals of the self-consistent-field-cycles were set at (in Ha units): 10⁻⁸ for coulomb overlap, 10⁻⁸ for coulomb penetration, 10⁻⁸ for exchange overlap, 10⁻⁸ for exchange pseudo-overlap in direct space, 10⁻¹⁶ for exchange pseudo-overlap in reciprocal space and 10⁻⁹ for threshold for SCF-cycles' convergence. The Mg basis set from Causà et al. (1986) was extended by the addition of diffuse *sp* and *d* shells (85-11G* contraction). Oxygen and aluminium were modelled by means of the O8-411d1 and 85-11G* basis sets of Corà (2005) and Catti et al. (1994), respectively. The outer shells' coefficients were optimised by means of the "billy" utility by Towler (2015). The eigenvalue level shifting technique was used (level shift of 0.2 Ha) to avoid conducting solutions and accelerate convergence.

The approach of Merli et al. (2015 and 2017) relying upon the cluster expansion technique was adopted to model the solid mixing in Mg-Al-pv. Such a method makes it possible to parametrize energy as a function of pair interactions, thus allowing one to model in a statistical framework even large atom clusters that would be difficult to handle otherwise. We expressed the Al-dependent part of the chemical potentials in equ.(7.b) as

$$471 \qquad \Delta \mu_0(P,T,\lambda)_{Mg-Al-pv} = \mu_0(P,T,\lambda)_{Mg-Al-pv} - \mu_0(P,T)_{pv} = \lambda \times \left[\mu_0(P,T,\lambda)_{Mg-Al-pv} - \mu_0(P,T,\lambda)_{Mg-Al-pv} \right] + \mu_0(P,T,\lambda)_{Mg-Al-pv} = \mu_0(P,T,\lambda)_{Mg-Al-pv} + \mu_0(P,T,\lambda)_{Mg-Al-$$

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$$\mu_0(P,T)_{cor}] + \delta\mu_0(P,T,\lambda)_{Mg-Al-pv}$$
 (15)

 $\delta\mu_0(P,T,\lambda)$, in turn, was developed in terms of

$$\delta \mu_0(P, T, \lambda)_{Mg-Al-pv} = (1 - \lambda) \times \lambda \times \sum_{l=0, L; m=0, M; n=0, N} p_{lmn} P^l T^m \lambda^n.$$
 (16)

We used perovskite's supercells, composed of $(2\times2\times1)$, $(2\times1\times2)$ and $(1\times2\times2)$ elementary cells. A total of 80 independent Al-configurations were randomly sampled over the interval 24-80 GPa and used to calculate the pair-interaction parameters of the cluster expansion as a function of P, following the strategy of Merli et al. (2017). We then simulated 10^5 - 10^6 Mg-Alpv independent configurations in 1024 atom clusters, using the pair-interaction parameters previously determined, to carry out statistical thermodynamics calculations (Merli et al. 2015), and model the Gibbs energy of Al-bearing perovskite thereby. ΔG_0 in equ.(7.b) were calculated neglecting the atomic vibration contribution, i.e. the one including zero-point vibration energy, thermal vibration energy and vibration entropy (in full: $\Delta G_{0,\text{vib}}$). In general, calculating $\Delta G_{0,\text{vib}}$ in a solid mixing that is modelled via a super-cell method is a difficult task, because of the complexity of compromising between representativeness of a cluster, computing time and achievable precision (about the role of vibrational components, see: van de Walle and Ceder, 2002). However, combining quantum calculations with semi-empirical potentials (GULP code; Gale 1997; 2005), which allow the investigation of large atomic clusters' lattice dynamics, we estimated, by harmonic approximation, $\Delta G_{0,vib}$ for 4 Al-Al configurations in perovskite at 20 and 70 GPa, with 0.25 Al_2O_3 mole fraction. In this way we compared $\Delta G_{0,vib}$ with $\Delta G_{0,stat+conf}$, i.e. the static contribution with the addition of configuration entropy, which we actually calculated. We observed $\Delta G_{0,\text{vib}}/\Delta G_{0,\text{stat+conf}}$ ~3%, in the thermal range of interest, i.e. 2000-3000 K. Therefore, taking into account the modest estimated weight of the thermal contribution in the solid mixing, we chose to leave it aside (as for neglecting vibration contribution, see for instance: Mohn and Trønnes 2016; Burton and van de Walle, 2003).

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498 4. RESULTS

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4.1 Chemical probability of formation of lower mantle phases

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The bulk aluminium content (largest value: 4.76 wt%, related to pyrolite lower mantle mixed with 3% of crustal component; Table 1) and the available amounts of alkali elements and H_2O make the *chemical probability of formation* [p(J,chem)] for the minor Al-bearing phases <

0.9% with respect to the total phases formed under the constraint of a non-primitive lower mantle composition (Table 1; Table 2). As expected, the p(J,chem) of Mg-Fe-pv+Mg-pv+Ca-pv+Fe-pe in a non-primitive lower mantle is >78%, regardless of the geochemical model used. It is worth noting that p(J,chem) of Mg-Al-pv is as large as ~96%, considering the Albearing phases only (Table 3). The hydrous phases are quasi irrelevant, whereas the NAL/CF-type phase exhibits a p(J,chem) as large as 3.87-3.57% (Table 3).

distribute in terms of 4/5 versus 1/5 between Mg-Al-pv and CF (the CF-phase is able to host almost six times as much aluminium as perovskite). This estimate is to be taken with due care as p(Mg-Al-pv,chem) and p(CF,chem) quantify only the probability of having the "least condition" for a given phase to form, regardless of the energy contribution and inter-phase competition to capture the involved elements. Altogether, perovskite is the main candidate to incorporate aluminium by far, though CF, too, exhibits a potential capacity for Al-storing.

4.2 Al-uptake in perovskite: open system model versus closed system model

The main advantages of using an open system model with respect to a closed system model are the following: -neglecting the chemical composition invariance allows the system to evolve unconstrained, driven by the mixing Gibbs energy of the solid solution of Mg-Al-pv. This provides the most favourable condition to estimate the Mg-Al-pv's intrinsic maximum capacity to host Al, resorting to a simple system composed of perovskite in combination with free-alumina (cor), the latter accounting for the aluminium not incorporated by the former because of saturation; -such a method makes it possible i) to achieve an average depiction of the output of a given chemical process and ii) to explore a mechanism of Al-storage taking into account not only

- 530 the Al-occupancy in perovskite, but also the amount of perovskite that is able to host
- aluminium *versus* the fraction of Al-free perovskite (Mg-Al-pv/Mg-pv).
- Reaction (5) was investigated using the *P-T* curve parametrised by Merli et al. (2016) as
- 533 follows
- 534 $T(K) = 11.290 \times P \text{ (GPa)} + 1648,$
- for 24 < P < 80 (GPa). Such a curve represents a lower mantle in a whole mantle convention
- of limited thermal efficiency (Mattern et al., 2005; Stixrude and Lithgrow-Bertelloni, 2005),
- thus approaching the layered mantle convection models (Brown and Shankland, 1981;
- 538 Anderson, 1982; Valencia-Cardona et al., 2017).
- 539
- 540 4.2.1 Al-uptake in perovskite from open system model
- Figure 1 shows $K(P,T,\lambda)$ of equ. (7.a) as a function of λ , at three chosen P-T points. In
- general, the larger the value of K, the more reaction (5) shifts to the right, i.e. towards Mg-Al-
- 543 pv. For each P-T point, $K(P,T,\lambda)$ has a maximum that changes from about 0.17 (24 GPa/1919
- K) to 0.26 (80 GPa/2551 K). This means that there is an Al-exchange λ -value that maximises
- the tendency to promote Mg-Al-pv at each P-T point of the geotherm. We now introduce the
- function $K(P,T)_{ave}$, which corresponds to the average of the equilibrium constant of reaction
- 547 (5), i.e. $K(P,T)_{ave} = \langle K(P,T,\lambda) \rangle_{\lambda}$. $K(P,T)_{ave}$ provides an overview of the general tendency of the
- aluminium incorporation process to shift either to the right or left in reaction (5) along the
- chosen P-T path (Fig. 2). $K(P,T)_{ave}$ calculated over Al-exchange processes between corundum
- and perovskite from 0 to 0.3 λ -value, tends to increase upon increasing P, i.e. reaction (5)
- shifts more and more to its right-hand side member $[(Mg_{1-\lambda}Al_{\lambda})(Si_{1-\lambda}Al_{\lambda})O_3]$. Two trends of
- $K(P,T)_{ave}$ are observable: one below and one above ~60 GPa, characterised by 0.008 and 0.02
- 553 GPa⁻¹ slopes, respectively (Fig. 2). They are reflective of the growing differences between the
- $K(P,T,\lambda)$ -curves, for $\lambda > 0.15$ (Fig. 1). On the explored P-T interval, the content of free-Al₂O₃,

i.e. cor, takes a very small average figure of $0.0010(\pm 1)$, in terms of phase proportion.

Conversely, Al-free (Mg-pv) and Al-bearing (Mg-Al-pv) perovskite phases amount to

557 $0.56(\pm 2)$ and $0.44(\pm 2)$, respectively (Fig. 3). Mg-Al-pv increases from 0.41 to 0.48 phase

proportion, from 24 to 80 GPa: this hints at a tendency to develop more and more

559 $(Mg,Al)(Si,Al)O_3$ -phase upon P(Fig. 3).

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The *cor/Mg-Al-pv* ratio monotonically decreases with increasing pressure up to 70 GPa (Fig.

4), from more than 0.022 to about 0.017, meaning that some 98 wt% of available Al₂O₃ is

taken by perovskite, in agreement with the results shown in Figures 1-3. In the range 60-80

GPa the data are rather scattered and weakly P-dependent. They indicate either some sort of

"saturation" (with respect to perovskite) or a poorly defined minimum. The aluminium uptake

capacity of perovskite is described $via \lambda_{Al2O3}$, see equ.(9.b), that gives the average Al_2O_3 mole

fraction per formula unit (Fig. 5). At 32 GPa perovskite hosts Al₂O₃ at its maximum capacity

 $(\lambda_{A12O3} = 0.134 \text{ Al}_2O_3 \text{ mole fraction})$ and preserves such an occupancy figure up to ~50 GPa

(Fig. 5). The occupancy starts to monotonically decrease beyond 50 GPa, with a slope of

about -0.0009 GPa⁻¹ ($\lambda_{Al2O3} = 0.105 \text{ Al}_2O_3$ mole fraction, at 80 GPa; Fig. 5). This takes place

in combination with an increase of the phase fraction of Al-bearing perovskite.

572 *4.2.2 Al-uptake in perovskite from a closed system model*

The Al-occupancy factor $\xi_{\text{closed system}}$, as reported in equations (10)-(11) and (12), minimises

the Gibbs energy and maximises the equilibrium constant of equ.(7.a), i.e. if $\lambda = \xi_{closed \ system}$

then $K(P,T,\lambda)$ takes its maximum value. $\xi_{\text{closed system}}$ exhibits a linear and increasing trend,

trailing down the mantle (Fig. 6). This implies that the perovskite structure incorporates more

and more aluminium as the pressure increases, if the system is *chemically adiabatic* and *cor*

only competes to host Al. Such a result can be seen in terms of that if a given amount of Al

must be "perforce" accommodated over perovskite and cor, then aluminium chooses

progressively the former with respect to the latter with increasing P, thus yielding a shift of reaction (5) to the right.

4.3 Solid mixing model performances with respect to some experimental data

We tested the physical soundness of our mixing energy model comparing its predictions with some experimental results related to Mg-Al-pv properties.

The enthalpy formation of the reaction $0.05~Al_2O_3~(cor) + 0.95~MgSiO_3 = Mg_{0.9}Si_{0.9}Al_{0.1}O_3$ was measured to be as large as $-0.8(\pm 2.2)~kJ/mol$ by Navrotsky et al. (2003). Such a figure is to be compared with -1.1~kJ/mol from our calculations. Although our estimation is 40% larger than the experimental value, the exothermic nature of the reaction is correctly predicted and, taking into account the uncertainty of measurements, observation and theoretical estimate are in good agreement. In Figure 7, we report the absolute values of the discrepancy between measurements (Walter et al., 2004) and our predictions on the Al-bearing perovskite cell volume. In most cases, the deviation lies below 0.8%, and just for three experimental points we observe a discrepancy above 1%. Altogether, the average disagreement is about 0.4% and indicates a chemical-physical soundness of the solid mixing model we are using.

5. DISCUSSION

5.1 Aluminium storage mechanism

Our results from the open system model point to a complex mechanism of Al-uptake in perovskite as a function of pressure (Figs.3-5). In particular, the aluminium storage involves both the Mg-Al-pv phase proportion and the average Al_2O_3 -mole fraction incorporated by Mg-Al-pv (i.e. λ_{Al2O3} ; see equ.(9.b)). Whereas λ_{Al2O3} (Fig. 5) changes comparably little and, in

- general, moderately decreases at large pressures, the phase fraction of Mg-Al-pv grows by
- 607 \sim 16% upon increasing *P* (Fig. 3).
- We underline that our model relies on mass transfer reactions within a chemically
- 609 unconstrained open system constituted by Mg-pv+Mg-Al-pv+cor that act as Al-Mg-Si
- exchangers with an ideal reservoir; therefore, the calculated maximum Al-uptake capacity in
- perovskite is independent of the geochemical frame.
- A lower mantle composition with chondritic Mg/Si ratio of ~1.01 implies an amount of
- perovskite from 83 up to 90 wt%, juxtaposed to the pyrolitic composition that predicts
- perovskite in the narrow range of 75-78 wt% (Lyubetskaya and Korenaga, 2007, McDonough,
- 615 2016). The relative proportion of this phase in a lower mantle mixed with 3% of MORB-like
- component does not significantly vary with respect to the reference models (Table 1). This is
- consistent with the fact that the total *chemical probability of formation*, p(J,chem), of the Mg-
- rich perovskite-type phases (i.e. Mg-pv+Mg-Fe-pv+Mg-Al-pv) does not significantly change
- between the primitive (A and A1) and non-primitive (A+3%B and A1+3%B) lower mantle
- 620 models (Table 2).
- The predicted total Al₂O₃ that Mg-Al-pv may accommodate is shown in Figure 8, along with
- the bulk Al-content inferred for primitive and enriched lower mantle compositions. We point
- out two aspects:
- 624 (i) the average *total* Al₂O₃ that perovskite (76 and 85 wt% in pyrolite and chondrite reference
- models, respectively) hosts is 4.28 and 4.78 wt% of the lower mantle mass. Such figures
- prove that perovskite is able to accommodate *almost* the entire budget of Al₂O₃ estimated for
- 627 non-primitive lower mantle compositions. Perovskite exhibits an average Al-hosting capacity
- of $\sim 90\%$, in the case of pyrolite model (Al₂O₃: 4.76 wt%), and > 100%, in the case of
- chondrite model (Al₂O₃: 4.31wt%). See also Table 1 and Figure 8;
- (ii) the *total* Al₂O₃ stored by Mg-Al-pv as a function of P-T (Fig. 8) varies in a comparatively
- 631 narrow range from 24 to about 60 GPa (~4.18-4.24 wt% and ~4.67-4.75 wt%, for pyrolite and

chondrite models, respectively), while it decreases going down the mantle (3.99 and 4.47 wt%, for pyrolite and chondrite models, respectively), at 80 GPa. This may be related to the occurrence of the already mentioned change of trend exhibited by the average equilibrium constant (Fig. 2). The decrease of the λ_{Al2O3} -values (Fig. 5) and the "saturation" of the Al₂O₃partitioning between perovskite and cor (Fig. 4) point to: i) a progressive reduction in the Alstorage capacity of Mg-Al-pv; ii) a change of the cor/Mg-Al-pv trend that might reflect the onset of instability in perovskite, probably leading to the formation of other aluminium hosting phases (i.e. structural change to post-perovskite; Murakami et al., 2004; Shim et al., 2008; Tsuchiya and Tsuchiya, 2008; Tateno et al., 2009). We believe that it is physically incongruous that at $P \sim 60-80$ GPa the *cor*/perovskite molar ratio inverts its decreasing trend, as this suggests that Mg-Al-pv loses competitiveness with respect to cor in hosting aluminium upon increasing P. In fact: i) cor undergoes a phase transition to the rhodium-oxide-like phase in the range of ~80-100 GPa (Thomson et al., 1996; Funamori and Jeanloz, 1997; Merli and Pavese, 2018); ii) the Al-content in perovskite monotonically decreases with pressure (60-80 GPa; Fig.5), thus implying a reduction of the strain, which is due to the occurrence of species other than Mg-Si. Such a reduction of the strain is expected to promote the stability of a perovskite-like structure.

Altogether, it can be observed that:

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- 650 i) aluminium is *globally* incorporated foremost *via* an increase of the Al-bearing perovskite
- amount, rather than by an increase of the Al_2O_3 -content in Mg-Al-pv chemical composition;
- 652 ii) the perovskite phase is able to accommodate an Al-excess consistent with 3 wt% MORB-
- component mixed with primitive lower mantle compositions, up to 100% and 90% of the
- Al₂O₃-budget, in the case of chondrite and pyrolite models, respectively.
- At higher pressure than those investigated here, the transformations of corundum to a more
 - stable structure (~80-100 GPa) as above-mentioned and of perovskite to the CaIrO₃-like phase
- 657 (often called post-perovskite) at ~120 GPa (Murakami et al., 2004) might account for the

change of the trend related to the Al-storage capacity of perovskite (Fig. 4). In fact, calculated phase equilibria in the MgSiO₃-Al₂O₃ system, modelled at P-T conditions relevant for the Earth's deepest mantle (80-140 GPa/2000-4000 K), predict the appearance of (Al-bearing)-post-perovskite coexisting with Mg-perovskite between 90 and 105 GPa, at T =2000 and 3000 K, respectively (Tsuchiya and Tsuchiya, 2008). According to the phase diagrams of these authors, the perovskite structure can accommodate up to ~0.19 moles of Al₂O₃ at 80 GPa and 2000 K, whereas at 3000 K the solubility of alumina increases up to ~0.4 moles. Interpolation yields ~0.3 moles of Al₂O₃ at 80 GPa and 2550 K. Such results can be compared with ours achieved by the closed system model, which relies on the same equilibrium thermodynamics approach. It is worth noting that the closed system model yields the Al₂O₃-composition of Mg-Al-pv that mostly shifts reaction (5) to the right, *i.e.* $K(P,T,\xi_{closed system})$ has a maximum. $\xi_{closed system}$ in turn, has an increasing trend trailing down the lower mantle (Figs. 1 and 6), providing an Al₂O₃-content of ~0.26 moles at P=80 GPa, in agreement with Tsuchiya and Tsuchiya (2008).

5.2 Composition of Mg-Al-pv in the lower mantle

There is a controversy on whether the negative buoyancy associated with subducted oceanic crust can overcome the viscous forces in the dynamic regions of Core-Mantle-Boundary (CMB) and accumulate into large thermochemical piles (*i.e.* large low-shear-velocity provinces, LLSVP: Li and McNamara, 2018). Conversely, a general *consensus* is that most of the subducted crust is variably stirred into the background mantle and completely dissolved, in a time span that varies from 0.1 to 1 Ga (Kumari et al., 2016; White, 2015; Foley and Rizo, 2017; Yu et al., 2018).

Using the phase proportions of *Mg-pv*, *Mg-Al-pv* and *cor* as a function of the exchanged

Using the phase proportions of Mg-pv, Mg-Al-pv and cor as a function of the exchanged alumina according to reaction (5), we can reconstruct the probability to find Mg-Al-pv with a

given composition in Al ₂ O ₃ (i.e. occurrence probability: p ₀ %). Note that p ₀ % must not be				
confused with the chemical probability of formation, i.e. $p(J,chem)$, discussed in section 3.1				
and that represents the mere probability to have the right oxide combination to form a given				
phase.				
The probability of the occurrence of perovskite with low Al ₂ O ₃ -content per formula unit				
(0.01-0.15 mole fraction) is \sim 28% at 24 GPa/1919 K, and increases up to \sim 43% at 80				
GPa/2550 K. In general, low alumina compositions (0.01-0.15 mole fractions) are dominant at				
any P-T explored (Fig. 9). On the contrary, the occurrence of Mg-Al-pv with high alumina				
contents in the range 0.19-0.30 mole fraction drops from ~9.8% to ~2%, passing from 24				
GPa/1919 K to 80 GPa/2550 K, respectively. Compositions of natural Al-bearing perovskite,				
occurring as diamond inclusions and "claimed" to be ascribable to the lower mantle				
(Kaminsky, 2012; Harte and Richardson 2012; Harte et. 1999), lie in the Al ₂ O ₃ -range				
associated with the largest occurrence probability (i.e. p _o %). Leaving any opinion about their				
representativeness of the lower mantle mineralogy aside, there is a consistency between				
observations and our predictions (Fig. 9).				
To conclude, Mg-Al-pv competes with Mg-pv to the phase composition of the lower mantle				
(Fig. 3) and the probability to find Mg - Al - pv in the lower mantle is almost of the same order				
of magnitude as Mg-pv (Fig. 9). In addition, the distribution of Al in Mg-Al-pv shows that,				
among the possible Al-bearing perovskite phases, the $(Mg_{0.89}Al_{0.11})(Si_{0.89}Al_{0.11})O_3$				
composition is the likeliest, providing some 8% of the bulk perovskite at 80 GPa (Fig. 9). The				
occurrence of the Al-richest composition, i.e. (Mg _{0.71} Al _{0.29})(Si _{0.71} Al _{0.29})O ₃ , is always a very				
rare event, <i>i.e.</i> $p_0\% < 1.7\%$.				

6. CONCLUSIONS

- We modelled the capacity of perovskite to uptake aluminium in a non-primitive Earth's lower mantle, because of an enrichment by 3 wt% of recycled crustal material (MORB-component). The investigated region stretches from 24 to 80 GPa and is geochemically described in the framework of pyrolite and chondrite reference models. The open system model here used to predict perovskite Al-incorporation capacity is independent of the geochemical framework. Aluminium is *globally* incorporated foremost via an increase of the Al-bearing perovskite amount [Mg-Al-pv(24 GPa)/Mg-Al-pv(80 GPa) \approx 1.17], rather than by an increase of the Al₂O₃-
- capacity (λ_{Al2O3} =0.134 Al₂O₃ mole fraction) and conserves such a figure up to ~50 GPa; at higher pressure, a continuous decrease of Al₂O₃-content in *Mg-Al-pv* composition takes place up to 80 GPa (λ_{Al2O3} =0.107 Al₂O₃ mole fraction).

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content in its chemical composition. At 32 GPa perovskite hosts Al₂O₃ at its maximum

- Approaching 80 GPa, perovskite reaches some sort of "saturation" of its capacity to host aluminium, which can be considered as a prelude to instability, most likely leading to the formation of other phases (*i.e.* structural change to post-perovskite) that accommodate Al. This is in keeping with the resulting phase equilibria in the MgSiO₃-Al₂O₃ system, earlier modelled at *P-T* conditions relevant for the Earth's deepest mantle (80-140 GPa/2000-4000)
- The probability to observe a perovskite composition having an Al₂O₃ mole fraction up to 0.15 is about 28% at 24 GPa, increasing to 43% at 80 GPa; on the contrary, compositions in the range 0.19-0.30 Al₂O₃ mole fraction drop their occurrence probability from 9.8 to 2.0%. In light of this, the Al-content of perovskite cannot be directly related to *P-T* conditions of formation, save that "large" Al₂O₃ contents suggest unlikely deep provenance, within the range here explored.
- The *total* Al₂O₃ that perovskite (amounting to 76 and 85 wt%, in pyrolite and chondrite reference models, respectively) may host is on average 4.3-4.8 wt% of the lower mantle mass.

 In particular, perovskite alone can account for an Al₂O₃-storage capacity that accommodates

100% Al₂O₃ predicted by a non-primitive chondrite model, and 90% Al₂O₃, forecast by a non-primitive pyrolite model. Calcium-ferrite type phases are possible competitors of perovskite in hosting aluminium (up to 1/5 of available Al), though their low *chemical probability of formation* likely reduces such potential. In the case of a non-primitive pyrolite lower mantle, Al-bearing phases other than perovskite should exist, and the CF-type phase is a candidate that might compensate for the 10% gap in perovskite Al-incorporation capacity.

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750 APPENDIX I

I.1 Open and closed systems

An open system is permeable to both energy (heat and work) and matter, which are exchanged between the system and a reservoir (De Groot and Mazur 1984; Mikhailov and Ertl 2017). A closed system is able to exchange with a reservoir energy only. Let us assume to have a generic system in which the following reaction occurs (we restrict our discussion to one reaction only, for the sake of simplicity)

$$\sum_{i} v_{i} A_{i} = \sum_{k} v_{k} A_{k} \Longrightarrow \sum_{l} v_{l} A_{l} = 0$$
 (I.a)

where $\{A_j\}$ and $\{A_k\}$ are "reactants and products" or "phases", which we shall term "reactants" *tout court*. The evolution as a function of time of the l^{th} -reactant is given by

$$\frac{dn_l}{dt} = \nu_l \frac{d\varepsilon}{dt} + \frac{d\Delta n_l}{dt} \tag{I.b}$$

- where n_l means number of moles of the l^{th} -reactant; ε is the reaction rate; the first term of the
- right-hand side member represents the change in n_l due to the reaction (I.a); the second term
- accounts for a matter exchange with a reservoir.
- We split the entropy of such a system into two terms (Prigogine 1968):

$$\frac{dS_{ext}}{dt} = \frac{\delta Q}{T} - \sum_{l} \frac{\mu_{l}}{T} \frac{d\Delta n_{l}}{dt}$$
 (I. c)

$$\frac{dS_{int}}{dt} = -\sum_{l} \frac{v_{l}\mu_{l}}{T} \frac{d\varepsilon}{dt}$$
 (I. d)

- where S_{ext} is the contribution by an exchange of heat and matter with an external reservoir; S_{int}
- represents the entropy produced by the reaction itself. Combining equ.(I.b), (I.c) and (I.d), it
- 767 follows that

$$\frac{dS}{dt} = \frac{\delta Q}{T} - \sum_{l} \frac{\nu_{l} \mu_{l}}{T} \left(\frac{d\varepsilon}{dt} + \frac{1}{\nu_{l}} \frac{d\Delta n_{l}}{dt} \right)$$
 (I. e)

- 768 where S is the total entropy. We focus our attention on *stationary* processes, which are not
- necessarily at equilibrium. They exhibit observables that do not change over time (Pokrovskii
- 770 2013), and therefore

$$\frac{dn_l}{dt} = 0 ag{I. f. 1}$$

$$\frac{dS}{dt} = 0 ag{I.f. 2}$$

- 771 Taking into account (I.b), (I.e) and (I.f.1), the fulfilment of the constraint (I.f.2) requires that
- 772 δQ =0. Therefore, it can be concluded that a stationary system is characterized by a possible
- exchange of matter with a reservoir, but not an exchange of heat.

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The correct treatment of a system like the one introduced above requires, in principle, to be able to formulate explicitly both (I.c) and (I.d). Our aim is simpler, as we would like to exploit the capacity of an open system to freely exchange matter with a reservoir, in combination with a formalism as close as possible to the consolidated equilibrium thermodynamics' one. Such a model provides a flexible tool to approach problems in which one investigates the intrinsic exchanging/incorporation capacity of a given substance, without any sort of constraint or restraint.

An internal observer (*i.e.* an observer who measures the system's observables only, unaware of the matter flow) perceives a stationary open system as one that is under equilibrium conditions (P,T and $\{n_j\}$ do not change over time and δQ =0). Therefore, all the state functions are invariant *versus* t and the system conserves its composition), with possible forward-

$$\mu_l = \mu_{0l} + RT ln(x_l) + RT ln(\gamma_{l,int})$$
(I.g)

chemical potential of the *l*-reactant by the usual expression below,

backward reactions and without any in/out-flow of energy/matter. Let us represent the

where μ_{0l} is the component that depends on P-T only, and coincides with the Gibbs energy of the lth-reactant alone; $\gamma_{l,int}$ is the activity coefficient of the lth-reactant according to the internal observer and incorporates any sort of deviation from ideal mixing. Let us assume that $\{n_l\}$ can fluctuate, δn_i , in such a way that (I.f.1) is satisfied *on average*, yet preserving the global system's composition. Therefore, the internal observer perceives that the conservation of composition is achieved through a transformation of the reactants into each other, according to the classical relationship below

$$\frac{\delta n_l}{\nu_l} = \delta \hat{\varepsilon} \tag{I. h}$$

for any *l*-reactant; $\delta \hat{\varepsilon}$ is the infinitesimal change of the reaction ratio, seen by the internal observer. Using the equation above, we have that

$$dG = \left[\sum_{l} v_{l} \mu_{0l} + RT ln \left(\prod_{l} x_{l}^{v_{l}}\right) + RT ln \left(\prod_{l} \gamma_{l,int}^{v_{l}}\right)\right] \delta \hat{\varepsilon}$$
 (I. i)

The internal observer states that dG=0, given that the system is supposed at equilibrium, and from (I.i) the usual chemical equilibrium equation follows

$$exp\left(-\frac{\sum_{l}\nu_{l}\mu_{0l}}{RT}\right) = \frac{\prod_{k}x_{k}^{\nu_{k}}}{\prod_{j}x_{j}^{\nu_{j}}} \times \frac{\prod_{k}\gamma_{k,int}^{\nu_{k}}}{\prod_{j}\gamma_{j,int}^{\nu_{j}}} = K(P,T)_{int}$$
(I. k)

An external observer (*i.e.* an observer that is aware of the matter flow) confirms that dG=0 as the system lies in a stationary state, and using (I.b) expresses dG in terms of

$$dG = \left[\sum_{l} v_{l} \mu_{0l} + RT ln \left(\prod_{l} x_{l}^{v_{l}}\right) + RT ln \left(\prod_{l} \gamma_{l,ext}^{v_{l}}\right)\right] \delta \varepsilon$$

$$+ \left[\sum_{l} \delta \Delta n_{l} \mu_{0l} + RT ln \left(\prod_{l} x_{l}^{\delta \Delta n_{l}}\right) + RT ln \left(\prod_{l} \gamma_{l,ext}^{\delta \Delta n_{l}}\right)\right]$$
(I.1)

where $\delta \Delta n_l$ is the fluctuation due to the amount of l-reactant supplied by the reservoir via a matter flow; $\gamma_{l,ext}$ is the activity coefficient estimated by the external observer. Given that the global system's composition does not change in a stationary state, then the following relationship must hold for $\delta \Delta n_l$, too,

$$\frac{\delta \Delta n_l}{\nu_l} = \delta \zeta$$

which implies

$$dG = \left[\sum_{l} v_{l} \mu_{0l} + RT ln \left(\prod_{l} x_{l}^{\nu_{l}}\right) + RT ln \left(\prod_{l} \gamma_{l,ext}^{\nu_{l}}\right)\right] (\delta \varepsilon + \delta \zeta)$$
 (I. m)

Equ.(I.m), in combination with dG=0, leads to an expression similar to (I.k), save the term depending on the activity coefficients, *i.e.* $\prod_{l} \gamma_{l,ext}^{\nu_{l}}$, so that

$$exp\left(-\frac{\sum_{l} \nu_{l} \mu_{0l}}{RT}\right) = \frac{\prod_{k} x_{k}^{\nu_{k}}}{\prod_{j} x_{j}^{\nu_{j}}} \times \frac{\prod_{k} \gamma_{k,ext}^{\nu_{k}}}{\prod_{j} \gamma_{i,ext}^{\nu_{j}}} = K(P,T)_{ext}$$
(I. n)

Therefore, the γ activity coefficients "collect" the deviations from equilibrium that the internal and external observers detect. For (I.n) and (I.k) to coincide with one another, $\prod_{l} \gamma_{l,ext}^{\nu_{l}} = \prod_{l} \gamma_{l,int}^{\nu_{l}}$ must hold.

An open system may change its composition evolving towards a stationary state, according to the expression below, for the *l*th-reactant:

$$\int_0^\infty \frac{d\Delta n_l}{dt} dt = \Delta n_l(\infty) - \Delta n_l(0)$$

where it can be assumed that at $t\rightarrow\infty$ the open system has achieved a stationary state.

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I.3 Reactant proportions and probability

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What does it physically mean to neglect the activity coefficients in equations (I.n) and (I.k)?

Let us assume that a system has a known average Gibbs energy value, *i.e.* < G at P-T, and

that it may occupy given "states", each one with a probability $\{p_l\}$. Following a consolidated

approach of statistical mechanics and information theory (Jaynes 1957a-b), we state that the

likeliest and least prejudicial $\{p_l\}$ -set constrained to yield < G> must correspond to an extreme

of the expression beneath

$$\Phi = -R \sum_{l} p_{l} \ln(p_{l}) + \psi \left[\sum_{l} p_{l} G_{l} - \langle G \rangle \right]$$
(I.0)

where G_l is the Gibbs energy of the l^{th} -state; R is the gas constant and ψ is a lagrangian multiplier. If one requires that $\delta\Phi$ =0, then

$$p_l \propto \exp\left(-\frac{G_l}{RT}\right)$$
 (I. p)

taking $\psi=1/T$. Let us shape our system in terms of a multi-phase system, in which the "states" are represented by the "reactants" that can occur. Let the system undergo a reaction like (I.a) and be composed of the related reactants. We analyse equ.(I.a) in statistical terms. The occurrence of the left-hand or right-hand side member, can be modelled using the notion of "joint probability", thus obtaining

$$p_{left-hand\ side\ member} \propto \prod_{j} p_{j}^{\nu_{j}}$$

$$p_{right-hand\ side\ member} \propto \prod_{k} p_{k}^{\nu_{k}}$$

We take the ratio $p_{right-hand\ side\ member}/p_{left-hand\ side\ member}$, and observe that it can be either written

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$$\prod_l p_l^{
u_l}$$

835 or formulated as

$$\prod_{l} \left[exp\left(-\frac{G_{l}}{RT} \right) \right]^{v_{l}} = exp\left(-\frac{\sum_{l} v_{l} G_{l}}{RT} \right)$$

by means of (I.p). Hence, the equations above lead to

$$\prod_{l} p_{l}^{\nu_{l}} = exp\left(-\frac{\sum_{l} \nu_{l} G_{l}}{RT}\right) \tag{I.q}$$

Equ.(I.q) is readily likened to (I.n) and (I.k), neglecting the activity coefficients and setting for each phase $G_l = \mu_{0l}$. Altogether, a chemical equilibrium equation is thus formulated in a very simple and general fashion, which holds for stationary systems, too. Therefore, neglecting the activity coefficient terms in (I.n) and (I.k) leads to revising the notion of " l^{th} -reactant proportion", x_l , in terms of " l^{th} -reactant occurrence probability", p_l , *i.e.* $x_l = p_l$, once a given reaction is being considered.

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844 APPENDIX II

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846 II.1 Approximation to unity of the activity coefficients term of equ.(7.a)

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The activity coefficient term of equ.(7.a) can be simplified as

$$\gamma = \frac{\gamma_1}{\gamma_2^{1-\lambda} \times \gamma_3^{\lambda}} \tag{II.a}$$

- where we replaced Mg-Al-pv, Mg-pv and cor with 1, 2 and 3, respectively. Let us introduce
- 850 the geometric average of the $\gamma_{1,2,3}$ s, *i.e.*

$$\gamma_{ave} = (\gamma_1 \times \gamma_2 \times \gamma_3)^{1/3}$$

851 and

$$\gamma_1 = \gamma_{ave} + \delta_1 \tag{II. b. 1}$$

$$\gamma_2 = \gamma_{ave} + \delta_2 \tag{II. b. 2}$$

$$\gamma_3 = \gamma_{ave} + \delta_3 \tag{II. b. 3}.$$

852 Replacing γs in (II.a) with (II.b.1-2-3), then it is obtained

$$\gamma = \frac{\left(1 + \frac{\delta_{1}}{\gamma_{ave}}\right)}{\left(1 + \frac{\delta_{2}}{\gamma_{ave}}\right)^{1 - \lambda}} \times \left(1 + \frac{\delta_{3}}{\gamma_{ave}}\right)^{\lambda} \approx \frac{\left(1 + \frac{\delta_{1}}{\gamma_{ave}}\right)}{\left(1 - (1 - \lambda)\frac{\delta_{2}}{\gamma_{ave}}\right) \times \left(1 - \lambda\frac{\delta_{3}}{\gamma_{ave}}\right)} \approx \\
\approx \left(1 + \frac{\delta_{1}}{\gamma_{ave}}\right) \times \left(1 + (1 - \lambda)\frac{\delta_{2}}{\gamma_{ave}}\right) \times \left(1 + \lambda\frac{\delta_{3}}{\gamma_{ave}}\right) \\
\approx 1 + \frac{\delta_{1} + (1 - \lambda)\delta_{2} + \lambda\delta_{3}}{\gamma_{ave}} + o\left(\left(\frac{\delta}{\gamma_{ave}}\right)^{2}\right) \approx 1 \tag{II. c}$$

The approximation above requires $\delta \gamma_{ave} < 1$, which holds in most cases. In fact, earlier excess 853 enthalpy determinations on some HP-minerals (for instance, Fe-periclase: Sreçec et al. 1987; 854 garnets: Geiger et al. 1987; olivine: Kojitani and Akaogi 1994; Al-perovskite: Akber-Knutson 855 856 and Bukowinski 2004; Panero et al. 2006) exhibit absolute ΔH-maximum-values that yield average activity coefficients [estimated by $exp(\Delta H_{max}/RT)$, T=2000 K] lying between 1.07 and 857 1.34, with a geometric average of 1.2 and $<\delta/\gamma_{ave}>\sim$ 0.08. Note that $\delta_1+\delta_2(1-\lambda)+\delta_3\lambda$ is 858 expected to be in general small as the δs compensate each other, due to δ_1 , δ_2 , and δ_3 not 859 being of the same sign. Therefore, given that we can legitimately neglect the activity 860 coefficient in the case of equ. (7.a), x_l s and p_l s coincide with each other, according to 861 APPENDIX I.3. 862

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1191 CAPTIONS TO THE FIGURES

Figure 1. Equilibrium constant, $K(P,T,\lambda)$, of the fundamental alumina exchange reaction (5) *versus* λ , which expresses the exchanged amount of Al₂O₃ in the *Mg-Al-pv*, *Mg-pv* and *cor* system. $K(P,T,\lambda)$, calculated by the open system model, is displayed at 24 GPa/1919 K (blue line), 44 GPa/2145 K (red line) and 80 GPa/2551 K (black line), by way of example. Black filled circles indicate the maxima at the three chosen P-T points, and correspond to the λ -values that most shift the reaction $(1-\lambda)$ MgSiO₃+ λ Al₂O₃ \leftrightarrow (Mg_{1- λ}Al_{λ})(Si_{1- λ}Al_{λ})O₃ to the right (equ.5, of the text).

Figure 2. $K(P,T)_{ave}$ *versus P*, according to the chosen geotherm and calculated by the open system model. Blue line and red line show two different trends for the average equilibrium constant, $K(P,T)_{ave}$, of the reaction (5). Note that $K(P,T)_{ave} = \langle K(P,T,\lambda) \rangle_{\lambda}$ (see 4.2.1 section for further explanations).

Figure 3. Phase proportions of Al-free perovskite (Mg-pv), Al-bearing perovskite (Mg-Al-pv) and corundum (cor) versus P, according to the chosen geotherm. Mg-Al-pv fractions have an average Al₂O₃ composition provided by λ_{Al2O3} , calculated according to equ.(9.b) on the P-T range of interest and shown in Fig.5. Al-free perovskite is an extreme notion, which provides a "limit" to define a tendency of such mineral to incorporate aluminium.

Figure 4. Al₂O₃-partitioning between corundum and perovskite (cor(mol)/Mg-Al-pv(mol)) versus P, according to the chosen geotherm and calculated by the open system model. The red box shows the region of maximum Al-uptake for perovskite (saturation region), suggesting that at such P-T conditions the Al-incorporation is weakly dependent on pressure. At higher pressure, the cor/Mg-Al-pv ratio trend hints at a possible instability of perovskite (transition to another phase, such as post-perovskite, ppv?). See text for further discussion

1218 1219 **Figure 5**. Average Al₂O₃ mole fraction in perovskite, λ_{Al2O3} , determined by the open system 1220 model and calculated via equ.(9.b), as a function of P along the chosen geotherm. In the Pregion 30-50 GPa, λ_{Al2O3} is *quasi* constant (interpolation solid line). 1221 1222 Figure 6. Al₂O₃ mole fraction in perovskite, $\xi_{closed\ system}$, determined by the closed system 1223 model and calculated via equ.(14), as a function of P along the chosen geotherm. At $\lambda = \xi_{\text{closed}}$ 1224 system, $K(P,T,\lambda)$ takes an extreme value, so that reaction (5) is shifted to the right as much as 1225 1226 possible. 1227 Figure 7. Cell volume disagreement (%), between measurements and our calculations, in the 1228 1229 case of Al-bearing perovskite, as a function of P. Experimental values from Walter et al (2004).1230 1231 Figure 8. The predicted total Al₂O₃ (wt%) stored in Mg-Al-pv, calculated by the open system 1232 model, assuming perovskite amounts of 76% (red dots) and 85% (blue dots) of the lower 1233 1234 mantle mass, in pyrolite and chondrite reference models (Table 1), respectively. Bulk Al₂O₃ 1235 contents of pyrolite (A) and chondrite (A1) primitive lower mantle models are shown by red 1236 and blue solid lines, respectively. Bulk Al₂O₃ contents of pyrolite-type and chondrite-type 1237 non-primitive lower mantle models calculated by adding a 3 wt% of MORB-component (B) are represented by red and blue dotted lines, respectively. MORB composition from Hirose et 1238 1239 al. (1999). *P-T* region of 24-80 GPa/1919-2550 K is referred to the chosen geotherm. 1240 **Figure 9.** Probability (p₀%) of Mg-Al-pv occurrence with a given Al₂O₃ mole content per 1241 formula unit, according to the open system model. Each curve is associated to key P-T values 1242

(P in legend), along the chosen geotherm. The Al₂O₃ contents of natural Al-bearing

perovskite (\leftrightarrow) *claimed* from the lower mantle, are provided by Kaminsky and Lin (2017). In the inset table, the absolute probability to find Al-bearing perovskite (Mg-Al-Pv) against Mgperovskite (Mg-pv) is reported for the explored P-T region of the lower mantle.

1 Aluminium distribution in an Earth's non-primitive lower mantle

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- 14 **Key-words**: Aluminium distribution, Earth's lower mantle; aluminium bearing perovskite;
- pyrolite, chondrite reference model; MORB-component; enriched lower mantle composition;
- open system.

ABSTRACT

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The aluminium incorporation mechanism of perovskite was explored by means of quantum mechanics in combination with equilibrium/off-equilibrium thermodynamics under the pressure-temperature conditions of the Earth's lower mantle (from 24 to 80 GPa). Earth's lower mantle was modelled as a geochemically "not-primitive" object because of an enrichment by 3 wt% of recycled crustal material (MORB-component). The chemical composition of the "non primitive" lower mantle takes into account both chondrite and pyrolite reference models to represent the lower mantle's primitive composition. The capacity of perovskite to host Al was modelled through an Al₂O₃ exchange process in an unconstrained Mg-perovskite+Mg-Al-perovskite+free-Al₂O₃(corundum) system. Aluminium is globally incorporated principally via an increase in the amount of Al-bearing perovskite $[Mg-Al-pv(80 \text{ GPa})/Mg-Al-pv(24 \text{ GPa})\approx 1.17]$, rather than by an increase in the Al₂O₃-content of the average chemical composition which changes little (0.11-0.13, mole fraction of Al₂O₃) and tends to decrease in Al. The Al₂O₃ distribution in the lower mantle was described through the probability of the occurrence of given compositions of Al-bearing perovskite. The probability of finding Mg-Al-perovskite is comparable to Al-free Mg-perovskite's. Perovskite with Al₂O₃ mole fraction up to 0.15 has an occurrence probability of ~28% at 24 GPa, increasing up to ~43% at 80 GPa; on the contrary, perovskite compositions in the range 0.19-0.30 Al₂O₃ mole fraction drop their occurrence probability from 9.8 to 2.0%, over the same Prange. In light of this, the distribution of Al in the lower mantle shows that, among the possible Al-bearing perovskite phases, the (Mg_{0.89}Al_{0.11})(Si_{0.89}Al_{0.11})O₃ composition is the likeliest, providing from 5 to 8% of the bulk perovskite in the pressure range from 24 to 80 GPa. The occurrence of the Al-richest composition, i.e. (Mg_{0.71}Al_{0.29})(Si_{0.71}Al_{0.29})O₃, is a rare event (probability of occurrence < 1.7%). This study predicts that perovskite may globally host Al₂O₃ in terms of 4.3 and 4.8 wt% (with respect to the non-primitive lower mantle mass),

- thus accounting for $\sim 90\%$ and 100% of the bulk Al_2O_3 estimated in the framework of pyrolite
- and chondrite reference models, respectively. A calcium-ferrite-type phase (on the MgAl₂O₄-
- NaAlSiO₄ join) seems to be the only candidate that can compensate for the 10% gap of the
- 46 perovskite Al-incorporation capacity, in the case of a pyrolite non-primitive lower mantle
- 47 model.

1. INTRODUCTION

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The mantle is the Earth's largest division by volume, originally marked by a planetary 50 Siderophile/Lithophile element fractionation. Refractory Lithophile Elements (RLE) 51 condensed from a gas of solar nebula composition at the highest temperature (>1400 K at 10^{-4} 52 atm) compatible with the nebula's physical constraints (Lodders, 2003). RLEs' chemical 53 behaviour prevented metal and sulphide phases from entering both chondrites and metallic 54 cores during the planetary differentiation (Lodders, 2003; Kaminski and Javoy, 2013; Mahan 55 et al., 2018). RLEs include Ca and Al among the major elements, the full group of rare earth 56 elements (REE), U and Th. The chemical characteristics of such elements support the 57 primitive Earth's mantle model that preserves the solar ratios of RLEs (Wasson and 58 Kallemeyn, 1988; Lodders et al., 2009; Wang and Jacobsen, 2016). 59 60 Aluminium is the sixth most abundant element on Earth: it is a purely refractory lithophile element and its natural abundance is provided by the stable isotope ²⁷Al. The radioactive 61 isotope 26 Al quickly decayed in 26 Mg (26 Al half-life = $7.17 \pm 0.24 \times 10^5$ yr; Norris et al., 1983, 62 Wu and Browne, 1997) during the early stage of the solar system's evolution (Lee et al., 63 1977; Lodders, 2003; Baker et al., 2012). The ²⁶Al decay provided substantial heating to the 64 proto planetary bodies, and its isotopic daughter is one of the most widely used extinct 65 radioactivity chronometers (Bizzarro, et al., 2005; Spivak-Birndorf et al. 2009; Wimpenny et 66 al., 2019). 67 Taking into account the geochemical behaviour of aluminium, it is unlikely that a large 68 69 amount of such element may enter the Earth's core, though it provides a major constituent of many minerals at any depth of the Earth's mantle and crust. Aluminium is also one of the 70 main components of any melt generated from the upper mantle, in terms of 9-21 wt% Al₂O₃ 71 on average (source: PetDB Petrological Database). Melt crystallization, segregation, rise and 72

cooling, led to the formation of the crust over the Earth's history. An intriguing aspect is that

- Al, as a crustal component, partially, or entirely, was transported into the mantle, through
- subduction. Such a process could involve mantle portions well below the magma source
- regions (Young et al., 2005; Tsuchiya and Tsuchiya, 2008; Wang and Jacobsen, 2016).
- 77 Seismic tomography reveals that near the Earth's mantle transition zone, which marks the
- boundary between upper and lower mantle, repositories of crustal material occur (Christensen
- and Yuen, 1984; Billen, 2010, King et al., 2015). They exhibit different dynamic behaviours:
- i) stagnation in the mantle transition zone (Japan trench; Honda, 2017 and references therein);
- 81 ii) stagnation in the uppermost lower mantle (Peruvian Andes; Fukao and Obayashi 2013); iii)
- 82 continuous descent, seemingly unhindered, into the lower mantle (Farallon plate, North
- America; Sigloch et al., 2008). Such tomographic observations suggest a mechanism of global
- 84 mantle convection with an abundant mass exchange between distinct geochemical reservoirs
- lying in both the upper and lower mantle (van der Hilst et al., 1997; Nolet et al., 2007).
- 86 More recently, geochemical models, aimed at explaining the isotopic evolution of the silicate
- 87 Earth (Kumari et al., 2016; Jones et al., 2019) or at tracing the distribution of key components
- 88 (H₂O and Fe-Mg) in the lower mantle (Walter et al., 2015; Merli et al., 2016; 2017), have
- 89 depicted the Earth's mantle as a chemical reservoir ("pyrolite") involving uninterrupted
- 90 geochemical reactions and energy/matter flows.
- 91 In particular, Kumari et al. (2016) estimated that about 60% of the entire mantle is as depleted
- 92 in fusible elements (i.e. Al and Ca) as its upper portion, whereas the remaining mantle is non-
- primitive, containing a small fraction of transient and isolated recycled crustal materials.
- Jones et al. (2019), combining the geodynamic model of mantle convection with isotope and
- 95 trace element geochemistry, suggest that the subduction and accumulation of dense oceanic
- 96 crust produce in the deep mantle a large mass of material enriched in incompatible trace
- 97 elements. The quoted authors also state that an equivalent of 50-70% of the current
- 98 continental crust mass was accumulated earlier than 3 Ga ago, and that the crustal recycling
- and reworking dominated over juvenile additions to the continental crust, since the end of the

Archean (2.5 Ga). This suggests that since the end of the Hadean age (~ 4.6-3.8 Ga) the 100 101 Earth's lower mantle has been enriched with crustal components. Understanding the structure and chemical-physical behavior of the slabs subducted into the 102 mantle is out of the scope of the present work. Conversely, we focus on the chemical 103 rearrangement of the main lower mantle mineral phases in the case of a full mixing between 104 crustal slabs and primordial lower mantle. In such a view, aluminium may be an effective 105 106 "probe" among the major elements. 107 The present work deals with the modelling of Al-incorporation in perovskite, the major phase in the lower mantle, and the resulting Al-distribution, by means of quantum mechanics 108 109 calculations in combination with equilibrium/off-equilibrium thermodynamics and cluster expansion technique. The cluster expansion approach allows the investigation of large atom 110 clusters, thus providing an effective tool to model solid mixing in a statistical framework (see 111 Merli et al. 2015, and references therein). Because of the complexity of the natural processes, 112 it is convenient to start from a "reference" mineral phase, i.e. MgSiO₃-perovskite, whose Al-113 enrichment is investigated. We explore the P-range from 24 to 80 GPa, to unquestionably 114 leave the perovskite-to-post perovskite transition aside (Murakami et al., 2004; Tsuchiya and 115 Tsuchiya, 2008; Shim et al., 2008). 116 117 Our main goal is to estimate the maximum intrinsic capacity of perovskite to incorporate aluminium and its phase proportion with respect to the Al-free perovskite fraction, as a 118 function of P-T. Subsequently, the resulting Al-partitioning will be used to discuss the global 119 120 mechanism of storage of aluminium in the lower mantle.

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2. GEOCHEMISTRY

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2.1 Lower mantle geochemical model

Cosmochemical arguments supporting a chondritic bulk Earth composition (chondrite 126 reference model) imply that the lower mantle must be enriched in Si with respect to a 127 primitive upper mantle (PUM; Javoy et al., 2010; Murakami et al., 2012; Kaminski, and Javoy 128 2013), save that the Earth's core should be able to host ~4-6 wt% Si (McDonough 2014, 129 Badro et al., 2014) to balance the Earth's Si-budget against the Sun's and chondrite's 130 [Mg/Si_(PUM)~1.21-1.31 versus Mg/Si_(lower mantle)~1.01]. Conversely, according to petrological 131 132 data and chondritic constraints the lower mantle is chemically equivalent to the primitive upper mantle (pyrolite reference model; McDonough and Sun,1995; Lyubetskaya and 133 134 Korenaga, 2007). Tomographic images of subducted slabs plunging into the deep mantle have been interpreted 135 in terms of an efficient mass transfer between upper and lower mantle domains. This supports 136 large scale mixing and therefore a homogenous Mg/Si distribution (i.e. pyrolite) throughout 137 the mantle (Sigloch et al., 2008; van der Hilst et al., 1997). However, only a limited number 138 of slabs actually sink into the lower mantle, given that most of the subducted ones flatten and 139 seem to stagnate at either ~660 km or ~1,000 km depth (Fukao and Obayashi 2013). This 140 points towards a comparatively ineffective mixing process and contrasts the notion of a 141 vigorous global mantle convection. Recently, Ballmer et al. (2017) have hypothesised the 142 presence of stable large-scale high-viscosity bridgmanite-enriched ancient mantle structures 143 (BEAMS) that have been residing in the Earth's lower mantle since the early stage of our 144 planet's formation. Their numerical model also predicts the incorporation of limited amounts 145 of crustal material from shallow to deep mantle, particularly during the early stages. Such 146 crustal portions provide stretched and stirred long-lived "fossil" fragments, in keeping with 147 tomographic observations. Therefore, large-scale heterogeneities may account for the Earth's 148 bulk composition, bringing the lower mantle's Mg/Si ratio closer to the solar-chondritic one 149 unlike the upper mantle. 150

Hereafter, we shall refer to either the "pyrolite model" (based on the pyrolite composition throughout the mantle) or the "chondrite model" (relying on different compositions between upper and lower mantle) to describe the lower mantle.

Whatever bulk composition model is used to interpret the mantle's dynamics, the crustal components plunging into the lower mantle cause large/small-scale changes of its phase composition (Irifune et al. 1996; McDonough, 2016; Nestola et al., 2018).

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2.2 Enriched (non-primitive) lower mantle bulk composition

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Both chondrite and pyrolite lower mantle models are used here to estimate the non-primitive lower mantle compositions. The bulk chemical composition of the lower mantle is generally described in terms of its five major oxides (MgO, FeO, CaO, Al₂O₃ and SiO₂), which account for ~98.5 wt% of the Earth's mantle mass (Mc Donough, 2016; Palme and O'Neill, 2014). Na₂O occurrence, even if of modest impact on the large-scale geophysical and geochemical modelling (Bina and Helffrich, 2014; Palme and O'Neill, 2014 Chust et al., 2017), is still important in terms of the resulting minor mineral phases that affect the Al distribution in the lower mantle. Experiments and observations on natural samples reveal that potential Albearing lower mantle phases may also include K, Fe³⁺ and OH as major elements (i.e.: Kato et al., 2013; Wang et al., 2015; Pamato et al., 2015; Harte and Richardson, 2012). In particular, Al-bearing phases are able to host potassium if they form in a system containing at least ~ 0.09 wt% K₂O (Kato et al., 2013). Note that the mid-ocean-ridge basalt (MORB) average composition has 0.08-0.12 wt% K₂O (Gale et al., 2013), whereas pyrolite and chondrite lower mantle models are estimated to bear ~0.03 and <0.01 wt% K₂O, respectively (McDonough and Sun, 1995; Javoy et al., 2010). Therefore, K-bearing phases are not expected to play a relevant role as potential aluminium hosts among the lower mantle phases. Although ferric iron is able to affect Al^{3+} storage in perovskite-like structures via $Fe^{3+} \leftrightarrow Al^{3+}$ replacement

(Kurnosov et al., 2017), the Fe³⁺/ \sum Fe_{tot} ratio in the primitive Earth's mantle is supposed to be 177 very small, i.e. ~0.03, according to mass balance calculations (Palme and O'Neill, 2014). 178 Bulk H₂O (hosted as OH-group) in the lower mantle influences the aluminium content 179 incorporated by perovskite through the formation of Al-bearing hydrous phases. However, the 180 bulk H₂O content is comparatively modest and estimated ~1500 ppm, in both pyrolite and 181 182 chondrite lower mantle models (Merli et al., 2016; Muir and Brodholt, 2018). 183 Let us consider the lower mantle as a geochemically non-primitive object because it is mixed with a fraction of recycled crustal material (i.e. MORB-component). In this view, Al₂O₃ and 184 185 CaO, hosted in lower mantle minerals, are potential "probes" which mark the occurrence of such a geodynamic process (Guignot and Andrault, 2004, Hirose et al., 2005; Korenaga, 186 2009; Irifune et al., 2010; Ricolleau et al., 2010). 187 The MORB chemical composition is enriched in incompatible major elements (aluminium, 188 calcium and, to a lesser extent, iron) and depleted of compatible elements (magnesium) with 189 respect to the mantle (Table 1). Therefore, a MORB-like composition at lower mantle P-T 190 conditions cannot give Fe-periclase, whereas high-pressure SiO₂-rich phases (e.g. Ca-191 perovskite and bridgmanite) and additional aluminium-rich phases are expected to occur. 192 Following experimental results about MORB bulk compositions (14-16 wt% Al₂O₃) under 193 lower mantle conditions (30-90 GPa), the newly formed Al₂O₃-rich phases (NAL-type phase 194 and CaFe₂O₄-type phase, i.e. CF-phase, on the join MgAl₂O₄-NaAlSiO₄) may account for 195 196 about 10-12 mol% by phase composition (Guignot and Andrault, 2004, Ricolleau et al., 2010). 197 Assuming that subducted crustal fragments have been sliding down into the mantle over the 198 past 4 billion years (the most generous estimate is about 11 wt% of the whole mantle; Li and 199 McNamara, 2013), aluminium-rich domains should have developed, in contrast to 200 expectations from a primitive lower mantle's composition (Stixrude and Lithgow-Bertelloni, 201

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2012).

We model such an enrichment using the simple binary mixing equation of Faure (1986) to combine primitive lower mantle compositions (pyrolite and chondrite, corresponding to the end-members "A" and "A1", respectively; see Table 1) with a crust-type-composition (endmember "B"; MORB-like silicate glass; see Table 1). End-member B is close to the N-MORB average of Gale et al. (2013) and has been largely used in HP experiments (i.e. Hirose et al., 1999; 2005 Funamori et al., 2000; Guignot and Andrault, 2004; Ricolleau et al., 2010). According to the extensive compilation provided by the PetDB-database of chemical data from mid-ocean ridge basalts, the water concentrations lie in the range 0.05-1.0 wt%. The amount of H₂O stored in the deep mantle, computed by experiments and mass balance models (Ghosh et al., 2014; Marty, 2012), is in the range 800-2700 ppm (i.e. 0.08-0.27 wt%). Taking into account such figures and the tomographic observations that suggest that only small fractions of descending slabs reach the lower mantle (Ballmer et al. 2017), we model a nonprimitive lower mantle composition by a chemical mixing of primitive pyrolite/chondrite compositions with a 3 wt% end-member B's contribution (0.1 wt% of H₂O). The resulting compositions are reported in Table 1. Such chemical mixing ideally reproduces a nonprimitive lower mantle as predicted by modelling the isotopic evolution of the silicate Earth: ~3 wt% of the total mantle mass is expected to be stored and ultimately mixed within ~1 Ga in the lower mantle (Christensen and Hofmann 1994; Kumari et al., 2016; White, 2015).

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3. METHODS

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3.1 Chemical probability of formation: aluminium-bearing phases in the lower mantle

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The probability that a phase "J" forms at P-T, *i.e.* p(J|P,T), can be roughly estimated in terms of $p(J|P,T) \propto p(J,\text{chem}) \times \exp(-\Delta G(P,T)_{\text{formation}}/RT)$, where p(J,chem) is the probability of having the required chemical species for J under the constraint of a given available elemental budget

- and $\Delta G(P,T)_{\text{formation}}$ is the formation Gibbs energy. p(J,chem) is termed "chemical probability
- of formation", to underline that it reflects the likelihood of having the required elements to
- form the J-phase, and it is calculated as follows.
- Let us assume X_k to represent the fractional abundance value of the k^{th} -oxide, in a generic
- 233 system. Given that

$$\sum_{k=1,M} X_k = 1 {1}$$

- then X_k can also be associated with the *probability* of having the k^{th} -oxide, if the oxides are
- supposed to be uniformly distributed as a function of space. The chemical composition of the
- 237 J-phase is then expressed formally as

$$J = \sum_{k} n_k X_k \tag{2}$$

- Therefore, the probability of finding one mole of the J-phase as a function of its pure chemical
- composition, p(J,chem), is provided by the joint events of i) having $(n_1$ -moles of X_1) $(n_2$ -moles
- of X_2)... and ii) not having any species with stoichiometric coefficient equal to 0. This
- 242 corresponds to the following joint probability:

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$$p(J, \text{chem}) \propto \prod_k p(k)^{n_k} \times (1 - \sum_m p(m)) \propto \prod_i X_i^{n_j} \times (1 - \sum_m X_m)$$
 (3)

- where p(k) and p(m) are the probabilities of finding the k^{th} and m^{th} oxide, respectively; the
- subscript k is associated with the chemical species with stoichiometric coefficients other than
- zero, whereas m is related to those with stoichiometric coefficients equal to zero. The
- p(J,chem) values calculated in this way are then normalized so that their sum yields unity.
- Table 2 reports major phases and potential Al-bearing phases that experiments, numerical
- 249 modelling and exceptional observations on natural findings indicated as possible minerals in a
- 250 non-primitive lower mantle (Table 1).
- 251 Preliminary calculations led us to rule out periclase as a host of aluminium, save that the Al-
- incorporation takes place with the contribution of H (Merli et al., 2016). In such a case, the
- amount of Al involved would be negligible, anyway. Panero et al. (2006) estimated regular
- solution parameters of 12 and 66 kJ/mol for perovskite and akimotoite, respectively. Taking

- into account i) the significantly lower energy for Al-incorporation in perovskite than in
- akimotoite and ii) the restricted range of occurrence of the latter (Panero et al., 2006), we
- exclude akimotoite as a possible competitor to uptake Al in the *P-T* region under investigation
- 258 (Stebbins et al., 2001; Li et al. 2008; Tschauner et al., 2018). Majorite garnet, which is the
- 259 main host of aluminium in the mantle transition region in both pyrolite and basaltic
- 260 compositions (Irifune and Ringwood, 1993; Litasov and Ohtani, 2007), is transformed into
- Mg-perovskite+Ca-perovskite at pressures corresponding to the uppermost lower mantle.
- Experiments show that aluminium is mostly incorporated by Mg-perovskite/bridgmanite in
- pyrolite or chondrite compositions under lower mantle *P-T* conditions (Irifune et al.,1996;
- Ricolleau t al., 2008), whereas separate aluminous phases form in basaltic compositions
- 265 (Hirose et a., 1999; 2005) at the same *P-T* conditions.
- In a non-primitive lower mantle, aluminium is partitioned between perovskite/bridgmanite
- and minor Al-bearing phases, such as:
- 268 i) alkali rich NAL-structure phases, like those on the join NaMg₂Al_{4.8}Si_{1.15}O₁₂-
- 269 KMg₂Al_{4.8}Si_{1.15}O₁₂ (Gasparik et al., 2000; Kato et al., 2013; Wu et al., 2016). However, as
- stated above, K-bearing phases are unlikely to develop in the lower mantle because of the lack
- of a sufficient amount of potassium;
- ii) CF-structure and NAL-structure polymorphs, on the join MgAl₂O₄-NaAlSiO₄ (Imada et al.,
- 273 2011; 2012; Irifune et al., 1991). Note that the CF-structure was observed to stabilize at a
- 274 higher pressure (~ >40 GPa) than the NAL-structure (~ 24-40 GPa) (Imada et al., 2011;
- 275 Guignot and Andrault, 2004);
- 276 iii) possible hydrous solid solutions involving D-phase, H-phase and δ -AlOOH (Ghosh and
- 277 Schmidt, 2014; Pamato et al., 2015; Walter et al., 2015; Fukuyama et al., 2017).
- 278 In the case of NAL- and CF-phases, we chose to calculate a *chemical probability of formation*
- 279 p(J,chem) for a reference NAL/CF-mineral, that is Na_{0.265}Fe_{0.245}Mg_{0.375}Ca_{0.035}Al_{1.1}Si_{0.715}O₄.
- Such a composition is obtained from Guignot and Andrault (2004), by averaging those that

the authors labelled with "CF^A" and "CF^{B1}", neglecting Ti and normalizing to 4 oxygen atoms

and 3 cations.

Hereafter we shall use the following acronyms, for the sake of brevity: Mg-pv, "Mg-

perovskite", for perovskite tout court, i.e. MgSiO3; Mg-Al-pv, "Al-perovskite", for Al bearing

Mg-perovskite, i.e. (Mg,Al)(Si,Al)O₃; Mg-Fe-pv, "bridgmanite", for Fe-bearing Mg-

perovskite, i.e. (Mg,Fe)SiO₃; Ca-pv, "Ca-perovskite", for Ca-bearing perovskite, i.e.

(Ca,Mg)SiO₃; "perovskite", for any solid mixing, or end member, occurring in the lower

mantle and having perovskite-type structure; Fe-pe, "Fe-periclase", i.e. (Mg,Fe)O; CF, "CF-

phase", for a phase in the MgAl₂O₄-NaAlSiO₄ join.

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3.2 Aluminium incorporation mechanisms of perovskite

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To evaluate the aluminium distribution in a non-primitive lower mantle, we model the Al-

uptake capacity of perovskite, which is the lower mantle phase able to host aluminium to such

an extent as to provide a relevant storage by volume (Jeanloz and Knittle, 1989; Ricolleau et

296 al.,2009).

We introduce the notion of "maximum Al-uptake capacity" of perovskite. "Maximum Al-

uptake capacity"-conditions are set through a virtual competition between MgSiO₃ and Al₂O₃

(ideal pure alumina phase) to accommodate Al, at lower mantle P-T conditions and in a SiO₂-

MgO-Al₂O₃ system. Corundum (cor) is the least "prejudicial" phase as an Al-host, given that

it does not require any further chemical species but aluminium to form and is the Al₂O₃-

polymorph stable in the *P-T* range of interest (Merli and Pavese 2018).

The incorporation mechanism of a trivalent cation in perovskite is supposed to occur through

three main reactions (Navrotsky et al., 2003; Akber-Knutson et al., 2005 and references

305 therein):

306 (i)
$$Si^{4+} + Mg^{2+} = M^{3+} + M^{3+}$$

307 (ii)
$$Si^{4+} = M^{3+} + 1/2 V_0^0$$

308 (iii)
$$Si^{4+} = M^{3+} + H^+$$
.

- Reaction (i), which takes place *via* a charge-coupled-mechanism, is the likeliest one, as shown
- 310 by energy calculations (Yamamoto et al., 2003; Akber-Knutson et al., 2005; Zhang and
- 311 Oganov, 2006). A comparison between incorporation mechanisms (i) and (ii) reveals that the
- 312 former is slightly exothermic, in contrast with the endothermic behaviour of the latter
- 313 (Navrotsky et al., 2003). NMR-measurements point to the occurrence of a charge-coupled
- mechanism (Stebbins et al., 2001), in agreement with calculations of Akber-Knutson and
- Bukowinski (2004), who suggest that Al tends to replace both Si and M²⁺, in a high pressure
- and high temperature regime. As to reaction (iii), we assume contents of H_2O , *i.e.* H^+ supplier,
- and Al_2O_3 as much as 1500 ppm (0.15 wt%) and 4.76 wt%, respectively (Table 1), in keeping
- with the lower mantle Al-richest composition obtained by mixing pyrolite with 3% MORB-
- 319 component (Table 1). In such a case, even if all the hydrogen from the dissociation
- 320 OH₂→OH⁺+H⁺ contributed to an exchange mechanism like (iii), just 0.08 mol fraction
- aluminium might be accounted for. Moreover, according to the H₂O-partitioning estimated by
- Merli et al. (2016), periclase is able to account for 1/3 of the trapped H₂O, thus reducing
- 323 further the role of reaction (iii) as a possible relevant mechanism to Al-incorporation in
- 324 perovskite.
- 325 Therefore, the Al-uptake in perovskite is modelled by the replacement of Mg-Si with Al-Al,
- according to the exchange reaction reported below using the formalism of Kröger-Vink
- 327 (Kröger, 1972)

328
$$Al_2O_3 + [Mg_{Mg}]^X + [Si_{Si}]^X \leftrightarrow [Al_{Mg}]^* + [Al_{Si}]^* + MgSiO_3.$$
 (4)

- Assuming λ -mole of Al₂O₃ to be exchanged in the Mg-Al-pv, Mg-pv and cor system, then
- equ.(4) leads to

331
$$(1-\lambda)MgSiO_3 + \lambda Al_2O_3 \Leftrightarrow (Mg_{1-\lambda}Al_{\lambda})(Si_{1-\lambda}Al_{\lambda})O_3.$$
 (5)

In reaction (5) iron can affect the energy through a replacement like $Mg^{2+} \Leftrightarrow Fe^{2+}$ and competes with aluminium in terms of $Al^{3+} \Leftrightarrow Fe^{3+}$. However, we chose to neglect Fe as we are developing a first approximation model, which would provide general trends rather than details. Our choice can be further supported by the following arguments.

• The general reaction that accounts for Al₂O₃ entering in bridgmanite turns out to be

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$$(Mg_{1-x}Fe_x^{2+})SiO_3 + \lambda Al_2O_3 = (Mg_{1-x-\lambda/2}Fe_{x-\lambda/2}^{2+}Al_\lambda)(Si_{1-\lambda}Al_\lambda)O_3 +$$
338
$$\lambda (Mg_{\frac{1}{2}}Fe_{\frac{1}{2}}^{2+})SiO_3$$
 (6)

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where we assume that Al replaces the same quantity of Mg and Fe²⁺, the latter dwelling at the 12-coordination site, only (Kaminsky and Lin, 2017). The parametrization of the Gibbs energy used in the present work relies upon the cluster expansion technique (Merli et al., 2015; 2017). Such a method leads to expressing energy as a function of the number of interacting atomic pairs that belong to the same cluster determined as a function of the distance between the involved chemical species. Assuming Fe-Al pair entering the perovskite structure as much as 0.1-0.2 moles (i.e. Kurnosov et al., 2017; Kaminsky and Lin, 2017), the probability of having a Fe-Al interacting pair belonging to the first/second cluster is ~5-6 %. Therefore, most of the interactions with aluminium atoms are due to the pure Mg-Si matrix, which governs the "maximum intrinsic capacity" of perovskite to incorporate Al. The role of Fe³⁺ is extensively debated and still largely uncertain. Mg-Fe-pv is potentially the major Fe³⁺ acceptor, but Kaminsky and Lin (2017) indicated that in natural lower mantle bridgmanites iron most likely occurs as ferrous at the 12coordination sites. Conversely, Kurnosov et al. (2017) claim $Fe^{3+}/\Sigma Fe_{tot} = 0.33$, in synthetic bridgmanite with ferric iron sited at the same coordination site, under lower mantle conditions ($P \sim 35$ GPa; 1300 km depth; Ismailova et al. 2016). Mass balance calculations, in turn, predict an impact of ferric iron in terms of Fe³⁺/ Σ Fe_{tot}~0.03, with respect to the Earth's mantle abundances (Palme and O'Neill, 2014). If we consider as a first level of approximation pyrolite (Mg-Fe-pv =76 wt%; FeO_{tot} = 8.05 wt%) and chondrite (Mg-Fe-pv =85 wt%; FeO_{tot} = 8.12 wt%) lower mantle models (Table 1), and apply the Kurnosov et al. (2017) Fe³⁺/Fe_{tot} ratio to Mg-Fe-pv, the resulting Al³⁺/Fe³⁺ mole ratios in bridgmanite are ~3.6 and ~2.9 for pyrolite and chondrite models, respectively. Tests based on calculations that we carried out to reproduce the replacement schemes Si + Mg \Leftrightarrow Al + Fe³⁺ versus Si + Mg \Leftrightarrow Al + Al, indicate that the second reaction is favoured over the former one [in agreement with the results of Nishio-Hamane et al. (2005)].

3.3 Reaction models

The Al-uptake mechanism in perovskite according to reaction (5) is addressed using two approaches: i) the *open system model*, which exploits the notion of stationary thermodynamic state and allows an exchange of matter between system and reservoir (Prigogine 1968); ii) the *closed system model*, which relies on equilibrium thermodynamics, therefore excluding any sort of matter exchange. In an open system, the stationary state replaces the equilibrium state and exhibits thermodynamic observables, which remain invariant over time. Details about the open system model are reported in APPENDIX I.1-.2-.3 and a brief overview is given below.

3.3.1 Open system model

We would like to exploit the capacity of an open system to exchange matter with a reservoir, in combination with a formalism as close as possible to the consolidated equilibrium thermodynamics' one. Such a model provides a flexible tool to address problems in which the intrinsic exchanging/incorporation capacity of a given substance can be investigated, without any sort of constraint or restraint (APPENDIX I.1).

- 383 The key requirement is the fulfilment of the following equation, associated to reaction (5) via
- the equilibrium constant K (APPENDIX I.2-3):

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$$K(P,T,\lambda) = exp[-\Delta G_0(P,T,\lambda)/RT] = a_{Mg-Al-pv}/(a_{Mg-pv}^{1-\lambda} \times a_{cor}^{\lambda}) \approx x_{Mg-Al-pv}/(a_{Mg-pv}^{1-\lambda} \times a_{cor}^{\lambda})$$

$$386 \quad \left(x_{Mq-pv}^{1-\lambda} \times x_{cor}^{\lambda}\right) \tag{7.a}$$

- 387 where x_i =phase proportion of the jth-component/phase (cor: corundum); a_i =jth-
- component/phase's activity. In equ.(7.a) the activity coefficient is approximated to unity (see
- APPENDIX I.3 and APPENDIX II). Expanding ΔG_0 , it follows that:

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$$\Delta G_0(P,T,\lambda) = \mu_0(P,T,\lambda)_{Mg-Al-pv} - \lambda \times \left[\mu_0(P,T)_{cor} - \mu_0(P,T)_{Mg-pv}\right] - \mu_0(P,T)_{Mg-pv}.$$

391
$$(7.b)$$

- where μ_0 is the part of the chemical potential depending on λ , P and T, only (Ottonello 1997;
- 393 2010). For convenience, we split the chemical potential of Al-incorporating perovskite (Mg-
- 394 Al-pv) into an Al-free part, i.e. pure perovskite (Mg-pv), and a part dependent on aluminium,
- 395 that is

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$$\mu_0(P, T, \lambda)_{Mq-Al-pv} = \mu_0(P, T)_{Mq-pv} + \Delta \mu_0(P, T, \lambda)_{Mq-Al-pv},$$
 (7.c)

- where $\Delta \mu_0(P,T,\lambda)_{Mg-Al-pv}$, which accounts for the solid mixing occurrence and provides the
- 398 very core of our computational model, is calculated by the cluster expansion method (Merli et
- 399 al 2015, 2017).
- 400 Using equ.(7.c), equ.(7.b) becomes

$$\Delta G_0(P,T,\lambda) = \Delta \mu_0(P,T,\lambda)_{Mg-Al-pv} - \lambda \left[\mu_0(P,T)_{cor} - \mu_0(P,T)_{Mg-pv} \right]. \tag{8}$$

- 402 At given (P,T,λ) -values, we seek the $\{x_{Mg-Al-pv}, x_{Mg-pv}, x_{cor}\}$ -sets that fulfil
- 403 a) equ.(7.a),
- 404 b) $x_{Mg-Al-pv}, x_{Mg-pv}, x_{cor} \ge 0$,
- 405 c) $x_{Mg-Al-pv} + x_{Mg-pv} + x_{cor} = 1$.
- 406 Among the solutions that satisfy the constraints a), b) and c), we chose the one that minimizes
- 407 the Gibbs energy, namely $x_{Mg-Al-pv} \times \mu_0(P,T,\lambda)_{Mg-Al-pv} + x_{Mg-pv} \times \mu_0(P,T)_{Mg-pv} + x_{cor} \times \mu_0(P,T)_{cor}$. In

- doing so, we obtain a triple, yielding Mg-Al-pv/Mg-pv/cor phase proportions, for each (P,T,λ)
- point, *i.e.* $\{x_{Mg-Al-pv}, x_{Mg-pv}, x_{cor}\}(P,T,\lambda)$. The preservation of the total chemical composition of
- 410 the system constituted by each $\{x_{Mg-Al-pv}, x_{Mg-pv}, x_{cor}\}(P,T,\lambda)$ -triple is not required. The
- resulting system therefore behaves as an open system that can exchange 2Al ⇔ Mg+Si with a
- reservoir. In general, we are interested in modelling *observables* whose values are averages
- over the λ -range, so that they depend ultimately on P-T only. For instance:

414
$$\{x_{Mg-Al-pv}, x_{Mg-pv}, x_{cor}\}(P, T) = \frac{1}{C} \int_{\lambda-inf}^{\lambda-sup} \{x_{Mg-Al-pv}, x_{Mg-pv}, x_{cor}\}(P, T, \lambda) d\lambda$$
 (9. a)

415
$$\lambda_{\text{Al2O3}}(P,T) = \int_{\lambda-inf}^{\lambda-sup} \lambda \times x_{Mg-Al-pv}(P,T,\lambda) \, d\lambda/x_{Mg-Al-pv}(P,T)$$
 (9.b)

416
$$Tot_{\text{Al2O3}}(P,T) = \frac{1}{c} \int_{\lambda - inf}^{\lambda - sup} \left[\lambda \times x_{Mg-Al-pv}(P,T,\lambda) + x_{\text{Al2O3}}(P,T,\lambda) \right] d\lambda$$
 (9.c)

- where: C is a normalization constant; λ -sup=0.3 and λ -inf=0, upper and lower thresholds of λ ,
- respectively (for λ >0.3, $x_{Mg-Al-pv}$ is negligible on the *P-T* range explored); λ_{Al2O3} of (9.b) is the
- 419 average Al₂O₃ mole fraction per formula unit; Tot_{Al2O3} is the total Al₂O₃ stored by the (Mg-
- 420 Al-pv)+(Mg-pv)+cor system.
- 422 3.3.2 Closed system model

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- 423 For the sake of completeness, we also present the closed system model. We seek the
- equilibrium conditions of reaction (5) for a closed system, *i.e.* a chemically adiabatic one. Let
- 425 ξ represent the aluminium occupancy factor in Mg-Al-pv [i.e. $(Mg_{1-\xi}Al_{\xi})(Si_{1-\xi}Al_{\xi})O_3$].
- Therefore, we have to minimize, with respect to ξ , the Gibbs energy of the system (Mg-
- 427 pv)+(Mg-Al-pv)+cor, i.e.

428
$$G = n_{cor} \times \mu_0(P, T)_{cor} + n_{pv} \times \mu_0(P, T)_{Mg-pv} + n_{Mg-Al-pv} \times \mu_0(P, T, \xi)_{Mg-Al-pv}, \quad (10)$$

under the constraints of the conservation of mass:

430
$$M_{A12O3} = n_{cor} + n_{Me-Al-pv} \times \xi$$
 (11)

431
$$M = M_{SiO2} = M_{MgO} = n_{Mg-pv} + n_{Mg-Al-pv} \times (1-\xi),$$
 (12)

- where M_{Al2O3} , M_{SiO2} and M_{MgO} are fixed total amounts in moles of Al_2O_3 , SiO_2 and MgO.
- 433 Using the constraints above, equ.(10) becomes

434
$$G = \left(M_{\text{Al2O3}} - n_{Mg-Al-pv} \times \xi\right) \times \mu_0(P, T)_{cor} + \left(M - n_{Mg-Al-pv} \times (1 - \xi)\right) \times \mu_0(P, T)_{cor}$$

435
$$\mu_0(P,T)_{Mq-pv} + n_{Mq-Al-pv} \times \mu_0(P,T,\xi)_{Mq-Al-pv}$$
 (13)

436 The Gibbs energy minimum condition requires

$$\frac{\partial G}{\partial \xi} = 0,$$

from which the following equation is derived

$$-\mu_0(P,T)_{cor} + \mu_0(P,T)_{Mg-pv} + \frac{\partial \mu_0(P,T,\xi)_{Mg-Al-pv}}{\partial \xi} = 0.$$
 (14)

- Equ.(14) formalises the equilibrium conditions for closed systems (Chust et al. 2017). Its
- solution, expressed by $\xi_{closed\ system}$, yields the composition of Al-bearing perovskite that
- minimises the Gibbs energy of equ.(13).
- 441 $\xi_{\text{closed system}}$ also minimises (7.b). In fact, taking into account equ.(7.c), equ.(14) is equivalent
- to setting $\frac{\partial \Delta G_0(P,T,\lambda)}{\partial \lambda} = 0$ in equ.(8), which implies that $K(P,T,\xi_{\text{closed system}})$ achieves an
- extreme value that shifts reaction (5) towards its right-hand side member as much as possible.

3.4 Computational

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447 Structure relaxations were performed at a given pressure and 0 K by the HF/DFT-

CRYSTAL14 program (Dovesi el al., 2009), which implements "Ab-initio Linear-

Combination-of-Atomic-Orbitals" for periodic systems. Only static pressure (P_{static} =- $\partial E_{\text{static}}$

 $_{\rm energy}/\partial V)$ and zero-point pressure ($P_{\rm zp}==-\partial E_{\rm vibration\ energy\ at\ 0K}/\partial V)$ were taken into account, given

that even adding a correction for thermal contributions would not significantly change our

results and the conclusions would be unaffected. A zero-point pressure was estimated by

quantum mechanics calculations and using pure perovskite only, resulting in ~5 GPa. The

WCGGA functional (Wu and Cohen, 2006) was used, with a hybridization rate of 28%. Such a proportion was adopted because it provides a more satisfactory agreement with observations in terms of perovskite structure, than other choices do. The tolerances governing the accuracy of the integrals of the self-consistent-field-cycles were set at (in Ha units): 10^{-8} for coulomb overlap, 10^{-8} for coulomb penetration, 10^{-8} for exchange overlap, 10^{-8} for exchange pseudo-overlap in direct space, 10^{-16} for exchange pseudo-overlap in reciprocal space and 10^{-9} for threshold for SCF-cycles' convergence. The Mg basis set from Causà et al. (1986) was extended by the addition of diffuse *sp* and *d* shells (85-11G* contraction). Oxygen and aluminium were modelled by means of the O8-411d1 and 85-11G* basis sets of Corà (2005) and Catti et al. (1994), respectively. The outer shells' coefficients were optimised by means of the "billy" utility by Towler (2015). The eigenvalue level shifting technique was used (level shift of 0.2 Ha) to avoid conducting solutions and accelerate convergence.

The approach of Merli et al. (2015 and 2017) relying upon the cluster expansion technique was adopted to model the solid mixing in Mg-Al-pv. Such a method makes it possible to parametrize energy as a function of pair interactions, thus allowing one to model in a statistical framework even large atom clusters that would be difficult to handle otherwise. We expressed the Al-dependent part of the chemical potentials in equ.(7.b) as

$$471 \qquad \Delta \mu_0(P,T,\lambda)_{Mg-Al-pv} = \mu_0(P,T,\lambda)_{Mg-Al-pv} - \mu_0(P,T)_{pv} = \lambda \times \left[\mu_0(P,T,\lambda)_{Mg-Al-pv} - \mu_0(P,T,\lambda)_{Mg-Al-pv} \right] + \mu_0(P,T,\lambda)_{Mg-Al-pv} = \mu_0(P,T,\lambda)_{Mg-Al-pv} + \mu_0(P,T,\lambda)_{Mg-Al-$$

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$$\mu_0(P,T)_{cor}] + \delta \mu_0(P,T,\lambda)_{Mg-Al-pv}$$
 (15)

 $\delta\mu_0(P,T,\lambda)$, in turn, was developed in terms of

$$\delta \mu_0(P, T, \lambda)_{Mg-Al-pv} = (1 - \lambda) \times \lambda \times \sum_{l=0, L; m=0, M; n=0, N} p_{lmn} P^l T^m \lambda^n.$$
 (16)

We used perovskite's supercells, composed of $(2\times2\times1)$, $(2\times1\times2)$ and $(1\times2\times2)$ elementary cells. A total of 80 independent Al-configurations were randomly sampled over the interval 24-80 GPa and used to calculate the pair-interaction parameters of the cluster expansion as a function of P, following the strategy of Merli et al. (2017). We then simulated 10^5 - 10^6 Mg-Alpv independent configurations in 1024 atom clusters, using the pair-interaction parameters previously determined, to carry out statistical thermodynamics calculations (Merli et al. 2015), and model the Gibbs energy of Al-bearing perovskite thereby. ΔG_0 in equ.(7.b) were calculated neglecting the atomic vibration contribution, i.e. the one including zero-point vibration energy, thermal vibration energy and vibration entropy (in full: $\Delta G_{0,\text{vib}}$). In general, calculating $\Delta G_{0,\text{vib}}$ in a solid mixing that is modelled via a super-cell method is a difficult task, because of the complexity of compromising between representativeness of a cluster, computing time and achievable precision (about the role of vibrational components, see: van de Walle and Ceder, 2002). However, combining quantum calculations with semi-empirical potentials (GULP code; Gale 1997; 2005), which allow the investigation of large atomic clusters' lattice dynamics, we estimated, by harmonic approximation, $\Delta G_{0,vib}$ for 4 Al-Al configurations in perovskite at 20 and 70 GPa, with 0.25 Al_2O_3 mole fraction. In this way we compared $\Delta G_{0,vib}$ with $\Delta G_{0,stat+conf}$, i.e. the static contribution with the addition of configuration entropy, which we actually calculated. We observed $\Delta G_{0,\text{vib}}/\Delta G_{0,\text{stat+conf}}$ ~3%, in the thermal range of interest, i.e. 2000-3000 K. Therefore, taking into account the modest estimated weight of the thermal contribution in the solid mixing, we chose to leave it aside (as for neglecting vibration contribution, see for instance: Mohn and Trønnes 2016; Burton and van de Walle, 2003).

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498 4. RESULTS

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4.1 Chemical probability of formation of lower mantle phases

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The bulk aluminium content (largest value: 4.76 wt%, related to pyrolite lower mantle mixed with 3% of crustal component; Table 1) and the available amounts of alkali elements and H_2O make the *chemical probability of formation* [p(J,chem)] for the minor Al-bearing phases <

0.9% with respect to the total phases formed under the constraint of a non-primitive lower mantle composition (Table 1; Table 2). As expected, the p(J,chem) of Mg-Fe-pv+Mg-pv+Ca-pv+Fe-pe in a non-primitive lower mantle is >78%, regardless of the geochemical model used. It is worth noting that p(J,chem) of Mg-Al-pv is as large as ~96%, considering the Albearing phases only (Table 3). The hydrous phases are quasi irrelevant, whereas the NAL/CF-type phase exhibits a p(J,chem) as large as 3.87-3.57% (Table 3).

If we used p(J,chem) as an "actual" probability of finding a given phase, then Al would distribute in terms of 4/5 versus 1/5 between Mg-Al-pv and CF (the CF-phase is able to host almost six times as much aluminium as perovskite). This estimate is to be taken with due care as p(Mg-Al-pv,chem) and p(CF,chem) quantify only the probability of having the "least condition" for a given phase to form, regardless of the energy contribution and inter-phase competition to capture the involved elements. Altogether, perovskite is the main candidate to incorporate aluminium by far, though CF, too, exhibits a potential capacity for Al-storing.

4.2 Al-uptake in perovskite: open system model versus closed system model

The main advantages of using an open system model with respect to a closed system model are the following: -neglecting the chemical composition invariance allows the system to evolve unconstrained, driven by the mixing Gibbs energy of the solid solution of Mg-Al-pv. This provides the most favourable condition to estimate the Mg-Al-pv's intrinsic maximum capacity to host Al, resorting to a simple system composed of perovskite in combination with free-alumina (cor), the latter accounting for the aluminium not incorporated by the former because of saturation; -such a method makes it possible i) to achieve an average depiction of the output of a given chemical process and ii) to explore a mechanism of Al-storage taking into account not only

- 530 the Al-occupancy in perovskite, but also the amount of perovskite that is able to host
- aluminium *versus* the fraction of Al-free perovskite (Mg-Al-pv/Mg-pv).
- Reaction (5) was investigated using the *P-T* curve parametrised by Merli et al. (2016) as
- 533 follows
- 534 $T(K) = 11.290 \times P \text{ (GPa)} + 1648,$
- for 24 < P < 80 (GPa). Such a curve represents a lower mantle in a whole mantle convention
- of limited thermal efficiency (Mattern et al., 2005; Stixrude and Lithgrow-Bertelloni, 2005),
- thus approaching the layered mantle convection models (Brown and Shankland, 1981;
- 538 Anderson, 1982; Valencia-Cardona et al., 2017).
- 539
- 540 4.2.1 Al-uptake in perovskite from open system model
- Figure 1 shows $K(P,T,\lambda)$ of equ. (7.a) as a function of λ , at three chosen P-T points. In
- general, the larger the value of K, the more reaction (5) shifts to the right, i.e. towards Mg-Al-
- 543 pv. For each P-T point, $K(P,T,\lambda)$ has a maximum that changes from about 0.17 (24 GPa/1919
- K) to 0.26 (80 GPa/2551 K). This means that there is an Al-exchange λ -value that maximises
- the tendency to promote Mg-Al-pv at each P-T point of the geotherm. We now introduce the
- function $K(P,T)_{ave}$, which corresponds to the average of the equilibrium constant of reaction
- 547 (5), i.e. $K(P,T)_{ave} = \langle K(P,T,\lambda) \rangle_{\lambda}$. $K(P,T)_{ave}$ provides an overview of the general tendency of the
- aluminium incorporation process to shift either to the right or left in reaction (5) along the
- chosen P-T path (Fig. 2). $K(P,T)_{ave}$ calculated over Al-exchange processes between corundum
- and perovskite from 0 to 0.3 λ -value, tends to increase upon increasing P, i.e. reaction (5)
- shifts more and more to its right-hand side member $[(Mg_{1-\lambda}Al_{\lambda})(Si_{1-\lambda}Al_{\lambda})O_3]$. Two trends of
- $K(P,T)_{ave}$ are observable: one below and one above ~60 GPa, characterised by 0.008 and 0.02
- 553 GPa⁻¹ slopes, respectively (Fig. 2). They are reflective of the growing differences between the
- $K(P,T,\lambda)$ -curves, for $\lambda > 0.15$ (Fig. 1). On the explored P-T interval, the content of free-Al₂O₃,

i.e. cor, takes a very small average figure of $0.0010(\pm 1)$, in terms of phase proportion.

Conversely, Al-free (Mg-pv) and Al-bearing (Mg-Al-pv) perovskite phases amount to

 $0.56(\pm 2)$ and $0.44(\pm 2)$, respectively (Fig. 3). Mg-Al-pv increases from 0.41 to 0.48 phase

proportion, from 24 to 80 GPa: this hints at a tendency to develop more and more

559 $(Mg,Al)(Si,Al)O_3$ -phase upon P(Fig. 3).

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The *cor/Mg-Al-pv* ratio monotonically decreases with increasing pressure up to 70 GPa (Fig.

4), from more than 0.022 to about 0.017, meaning that some 98 wt% of available Al₂O₃ is

taken by perovskite, in agreement with the results shown in Figures 1-3. In the range 60-80

GPa the data are rather scattered and weakly P-dependent. They indicate either some sort of

"saturation" (with respect to perovskite) or a poorly defined minimum. The aluminium uptake

capacity of perovskite is described $via \lambda_{Al2O3}$, see equ.(9.b), that gives the average Al_2O_3 mole

fraction per formula unit (Fig. 5). At 32 GPa perovskite hosts Al₂O₃ at its maximum capacity

 $(\lambda_{Al2O3} = 0.134 \text{ Al}_2O_3 \text{ mole fraction})$ and preserves such an occupancy figure up to ~50 GPa

(Fig. 5). The occupancy starts to monotonically decrease beyond 50 GPa, with a slope of

about -0.0009 GPa⁻¹ ($\lambda_{Al2O3} = 0.105 \text{ Al}_2O_3$ mole fraction, at 80 GPa; Fig. 5). This takes place

in combination with an increase of the phase fraction of Al-bearing perovskite.

572 *4.2.2 Al-uptake in perovskite from a closed system model*

The Al-occupancy factor $\xi_{\text{closed system}}$, as reported in equations (10)-(11) and (12), minimises

the Gibbs energy and maximises the equilibrium constant of equ.(7.a), i.e. if $\lambda = \xi_{closed\ system}$

then $K(P,T,\lambda)$ takes its maximum value. $\xi_{\text{closed system}}$ exhibits a linear and increasing trend,

trailing down the mantle (Fig. 6). This implies that the perovskite structure incorporates more

and more aluminium as the pressure increases, if the system is *chemically adiabatic* and *cor*

only competes to host Al. Such a result can be seen in terms of that if a given amount of Al

must be "perforce" accommodated over perovskite and cor, then aluminium chooses

progressively the former with respect to the latter with increasing P, thus yielding a shift of reaction (5) to the right.

4.3 Solid mixing model performances with respect to some experimental data

We tested the physical soundness of our mixing energy model comparing its predictions with some experimental results related to Mg-Al-pv properties.

The enthalpy formation of the reaction $0.05~Al_2O_3~(cor) + 0.95~MgSiO_3 = Mg_{0.9}Si_{0.9}Al_{0.1}O_3$ was measured to be as large as $-0.8(\pm 2.2)~kJ/mol$ by Navrotsky et al. (2003). Such a figure is to be compared with -1.1~kJ/mol from our calculations. Although our estimation is 40% larger than the experimental value, the exothermic nature of the reaction is correctly predicted and, taking into account the uncertainty of measurements, observation and theoretical estimate are in good agreement. In Figure 7, we report the absolute values of the discrepancy between measurements (Walter et al., 2004) and our predictions on the Al-bearing perovskite cell volume. In most cases, the deviation lies below 0.8%, and just for three experimental points we observe a discrepancy above 1%. Altogether, the average disagreement is about 0.4% and indicates a chemical-physical soundness of the solid mixing model we are using.

5. DISCUSSION

5.1 Aluminium storage mechanism

Our results from the open system model point to a complex mechanism of Al-uptake in perovskite as a function of pressure (Figs.3-5). In particular, the aluminium storage involves both the Mg-Al-pv phase proportion and the average Al_2O_3 -mole fraction incorporated by Mg-Al-pv (i.e. λ_{Al2O3} ; see equ.(9.b)). Whereas λ_{Al2O3} (Fig. 5) changes comparably little and, in

- general, moderately decreases at large pressures, the phase fraction of Mg-Al-pv grows by
- 607 \sim 16% upon increasing *P* (Fig. 3).
- We underline that our model relies on mass transfer reactions within a chemically
- 609 unconstrained open system constituted by Mg-pv+Mg-Al-pv+cor that act as Al-Mg-Si
- exchangers with an ideal reservoir; therefore, the calculated maximum Al-uptake capacity in
- perovskite is independent of the geochemical frame.
- A lower mantle composition with chondritic Mg/Si ratio of ~1.01 implies an amount of
- perovskite from 83 up to 90 wt%, juxtaposed to the pyrolitic composition that predicts
- perovskite in the narrow range of 75-78 wt% (Lyubetskaya and Korenaga, 2007, McDonough,
- 615 2016). The relative proportion of this phase in a lower mantle mixed with 3% of MORB-like
- component does not significantly vary with respect to the reference models (Table 1). This is
- consistent with the fact that the total *chemical probability of formation*, p(J,chem), of the Mg-
- rich perovskite-type phases (i.e. Mg-pv+Mg-Fe-pv+Mg-Al-pv) does not significantly change
- between the primitive (A and A1) and non-primitive (A+3%B and A1+3%B) lower mantle
- 620 models (Table 2).
- The predicted total Al₂O₃ that Mg-Al-pv may accommodate is shown in Figure 8, along with
- the bulk Al-content inferred for primitive and enriched lower mantle compositions. We point
- out two aspects:
- 624 (i) the average *total* Al₂O₃ that perovskite (76 and 85 wt% in pyrolite and chondrite reference
- models, respectively) hosts is 4.28 and 4.78 wt% of the lower mantle mass. Such figures
- prove that perovskite is able to accommodate *almost* the entire budget of Al₂O₃ estimated for
- 627 non-primitive lower mantle compositions. Perovskite exhibits an average Al-hosting capacity
- of $\sim 90\%$, in the case of pyrolite model (Al₂O₃: 4.76 wt%), and > 100%, in the case of
- chondrite model (Al₂O₃: 4.31wt%). See also Table 1 and Figure 8;
- (ii) the *total* Al₂O₃ stored by Mg-Al-pv as a function of P-T (Fig. 8) varies in a comparatively
- 631 narrow range from 24 to about 60 GPa (~4.18-4.24 wt% and ~4.67-4.75 wt%, for pyrolite and

chondrite models, respectively), while it decreases going down the mantle (3.99 and 4.47 wt%, for pyrolite and chondrite models, respectively), at 80 GPa. This may be related to the occurrence of the already mentioned change of trend exhibited by the average equilibrium constant (Fig. 2). The decrease of the λ_{Al2O3} -values (Fig. 5) and the "saturation" of the Al₂O₃partitioning between perovskite and cor (Fig. 4) point to: i) a progressive reduction in the Alstorage capacity of Mg-Al-pv; ii) a change of the cor/Mg-Al-pv trend that might reflect the onset of instability in perovskite, probably leading to the formation of other aluminium hosting phases (i.e. structural change to post-perovskite; Murakami et al., 2004; Shim et al., 2008; Tsuchiya and Tsuchiya, 2008; Tateno et al., 2009). We believe that it is physically incongruous that at $P \sim 60-80$ GPa the *cor*/perovskite molar ratio inverts its decreasing trend, as this suggests that Mg-Al-pv loses competitiveness with respect to cor in hosting aluminium upon increasing P. In fact: i) cor undergoes a phase transition to the rhodium-oxide-like phase in the range of ~80-100 GPa (Thomson et al., 1996; Funamori and Jeanloz, 1997; Merli and Pavese, 2018); ii) the Al-content in perovskite monotonically decreases with pressure (60-80 GPa; Fig.5), thus implying a reduction of the strain, which is due to the occurrence of species other than Mg-Si. Such a reduction of the strain is expected to promote the stability of a perovskite-like structure. Altogether, it can be observed that: i) aluminium is *globally* incorporated foremost *via* an increase of the Al-bearing perovskite amount, rather than by an increase of the Al₂O₃-content in Mg-Al-pv chemical composition; ii) the perovskite phase is able to accommodate an Al-excess consistent with 3 wt% MORB-

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Al₂O₃-budget, in the case of chondrite and pyrolite models, respectively.

At higher pressure than those investigated here, the transformations of corundum to a more stable structure (~80-100 GPa) as above-mentioned and of perovskite to the CaIrO₃-like phase (often called post-perovskite) at ~120 GPa (Murakami et al., 2004) might account for the

component mixed with primitive lower mantle compositions, up to 100% and 90% of the

change of the trend related to the Al-storage capacity of perovskite (Fig. 4). In fact, calculated phase equilibria in the MgSiO₃-Al₂O₃ system, modelled at P-T conditions relevant for the Earth's deepest mantle (80-140 GPa/2000-4000 K), predict the appearance of (Al-bearing)-post-perovskite coexisting with Mg-perovskite between 90 and 105 GPa, at T =2000 and 3000 K, respectively (Tsuchiya and Tsuchiya, 2008). According to the phase diagrams of these authors, the perovskite structure can accommodate up to ~0.19 moles of Al₂O₃ at 80 GPa and 2000 K, whereas at 3000 K the solubility of alumina increases up to ~0.4 moles. Interpolation yields ~0.3 moles of Al₂O₃ at 80 GPa and 2550 K. Such results can be compared with ours achieved by the closed system model, which relies on the same equilibrium thermodynamics approach. It is worth noting that the closed system model yields the Al₂O₃-composition of Mg-Al-pv that mostly shifts reaction (5) to the right, *i.e.* $K(P,T,\xi_{closed system})$ has a maximum. $\xi_{closed system}$ in turn, has an increasing trend trailing down the lower mantle (Figs. 1 and 6), providing an Al₂O₃-content of ~0.26 moles at P=80 GPa, in agreement with Tsuchiya and Tsuchiya (2008).

5.2 Composition of Mg-Al-pv in the lower mantle

There is a controversy on whether the negative buoyancy associated with subducted oceanic crust can overcome the viscous forces in the dynamic regions of Core-Mantle-Boundary (CMB) and accumulate into large thermochemical piles (*i.e.* large low-shear-velocity provinces, LLSVP: Li and McNamara, 2018). Conversely, a general *consensus* is that most of the subducted crust is variably stirred into the background mantle and completely dissolved, in a time span that varies from 0.1 to 1 Ga (Kumari et al., 2016; White, 2015; Foley and Rizo, 2017; Yu et al., 2018).

Using the phase proportions of *Mg-pv*, *Mg-Al-pv* and *cor* as a function of the exchanged

Using the phase proportions of Mg-pv, Mg-Al-pv and cor as a function of the exchanged alumina according to reaction (5), we can reconstruct the probability to find Mg-Al-pv with a

given composition in Al ₂ O ₃ (i.e. occurrence probability: p ₀ %). Note that p ₀ % must not be
confused with the <i>chemical probability of formation</i> , i.e. p(J,chem), discussed in section 3.1
and that represents the mere probability to have the right oxide combination to form a given
phase.
The probability of the occurrence of perovskite with low Al ₂ O ₃ -content per formula unit
(0.01-0.15 mole fraction) is \sim 28% at 24 GPa/1919 K, and increases up to \sim 43% at 80
GPa/2550 K. In general, low alumina compositions (0.01-0.15 mole fractions) are dominant at
any P-T explored (Fig. 9). On the contrary, the occurrence of Mg-Al-pv with high alumina
contents in the range 0.19-0.30 mole fraction drops from ~9.8% to ~2%, passing from 24
GPa/1919 K to 80 GPa/2550 K, respectively. Compositions of natural Al-bearing perovskite,
occurring as diamond inclusions and "claimed" to be ascribable to the lower mantle
(Kaminsky, 2012; Harte and Richardson 2012; Harte et. 1999), lie in the Al ₂ O ₃ -range
associated with the largest occurrence probability (i.e. po%). Leaving any opinion about their
representativeness of the lower mantle mineralogy aside, there is a consistency between
observations and our predictions (Fig. 9).
To conclude, Mg-Al-pv competes with Mg-pv to the phase composition of the lower mantle
(Fig. 3) and the probability to find Mg - Al - pv in the lower mantle is almost of the same order
of magnitude as Mg-pv (Fig. 9). In addition, the distribution of Al in Mg-Al-pv shows that,
among the possible Al-bearing perovskite phases, the $(Mg_{0.89}Al_{0.11})(Si_{0.89}Al_{0.11})O_3$
composition is the likeliest, providing some 8% of the bulk perovskite at 80 GPa (Fig. 9). The
occurrence of the Al-richest composition, i.e. (Mg _{0.71} Al _{0.29})(Si _{0.71} Al _{0.29})O ₃ , is always a very
rare event, <i>i.e.</i> $p_0\% < 1.7\%$.

6. CONCLUSIONS

- We modelled the capacity of perovskite to uptake aluminium in a non-primitive Earth's lower 709 710 mantle, because of an enrichment by 3 wt% of recycled crustal material (MORB-component). The investigated region stretches from 24 to 80 GPa and is geochemically described in the 711 712 framework of pyrolite and chondrite reference models. The open system model here used to predict perovskite Al-incorporation capacity is independent of the geochemical framework. 713 Aluminium is globally incorporated foremost via an increase of the Al-bearing perovskite 714 amount [Mg-Al-pv(24 GPa)/Mg-Al-pv(80 GPa)≈1.17], rather than by an increase of the Al₂O₃-715 content in its chemical composition. At 32 GPa perovskite hosts Al₂O₃ at its maximum 716 capacity (λ_{Al2O3}=0.134 Al₂O₃ mole fraction) and conserves such a figure up to ~50 GPa; at 717 higher pressure, a continuous decrease of Al₂O₃-content in Mg-Al-pv composition takes place 718 up to 80 GPa (λ_{Al2O3} =0.107 Al₂O₃ mole fraction). 719 Approaching 80 GPa, perovskite reaches some sort of "saturation" of its capacity to host 720 aluminium, which can be considered as a prelude to instability, most likely leading to the 721 formation of other phases (i.e. structural change to post-perovskite) that accommodate Al. 722 This is in keeping with the resulting phase equilibria in the MgSiO₃-Al₂O₃ system, earlier 723 724 modelled at P-T conditions relevant for the Earth's deepest mantle (80-140 GPa/2000-4000 K). 725 The probability to observe a perovskite composition having an Al₂O₃ mole fraction up to 0.15 726 is about 28% at 24 GPa, increasing to 43% at 80 GPa; on the contrary, compositions in the 727 728 range 0.19-0.30 Al₂O₃ mole fraction drop their occurrence probability from 9.8 to 2.0%. In light of this, the Al-content of perovskite cannot be directly related to P-T conditions of 729
- The *total* Al₂O₃ that perovskite (amounting to 76 and 85 wt%, in pyrolite and chondrite reference models, respectively) may host is on average 4.3-4.8 wt% of the lower mantle mass.

 In particular, perovskite alone can account for an Al₂O₃-storage capacity that accommodates

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range here explored.

formation, save that "large" Al₂O₃ contents suggest unlikely deep provenance, within the

100% Al₂O₃ predicted by a non-primitive chondrite model, and 90% Al₂O₃, forecast by a non-primitive pyrolite model. Calcium-ferrite type phases are possible competitors of perovskite in hosting aluminium (up to 1/5 of available Al), though their low *chemical probability of formation* likely reduces such potential. In the case of a non-primitive pyrolite lower mantle, Al-bearing phases other than perovskite should exist, and the CF-type phase is a candidate that might compensate for the 10% gap in perovskite Al-incorporation capacity.

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750 APPENDIX I

I.1 Open and closed systems

An open system is permeable to both energy (heat and work) and matter, which are exchanged between the system and a reservoir (De Groot and Mazur 1984; Mikhailov and Ertl 2017). A closed system is able to exchange with a reservoir energy only. Let us assume to have a generic system in which the following reaction occurs (we restrict our discussion to one reaction only, for the sake of simplicity)

$$\sum_{i} v_{i} A_{i} = \sum_{k} v_{k} A_{k} \Longrightarrow \sum_{l} v_{l} A_{l} = 0$$
 (I.a)

where $\{A_j\}$ and $\{A_k\}$ are "reactants and products" or "phases", which we shall term "reactants" *tout court*. The evolution as a function of time of the l^{th} -reactant is given by

$$\frac{dn_l}{dt} = \nu_l \frac{d\varepsilon}{dt} + \frac{d\Delta n_l}{dt} \tag{I.b}$$

- where n_l means number of moles of the l^{th} -reactant; ε is the reaction rate; the first term of the
- right-hand side member represents the change in n_l due to the reaction (I.a); the second term
- accounts for a matter exchange with a reservoir.
- We split the entropy of such a system into two terms (Prigogine 1968):

$$\frac{dS_{ext}}{dt} = \frac{\delta Q}{T} - \sum_{l} \frac{\mu_{l}}{T} \frac{d\Delta n_{l}}{dt}$$
 (I. c)

$$\frac{dS_{int}}{dt} = -\sum_{l} \frac{v_{l}\mu_{l}}{T} \frac{d\varepsilon}{dt}$$
 (I. d)

- where S_{ext} is the contribution by an exchange of heat and matter with an external reservoir; S_{int}
- represents the entropy produced by the reaction itself. Combining equ.(I.b), (I.c) and (I.d), it
- 767 follows that

$$\frac{dS}{dt} = \frac{\delta Q}{T} - \sum_{l} \frac{\nu_{l} \mu_{l}}{T} \left(\frac{d\varepsilon}{dt} + \frac{1}{\nu_{l}} \frac{d\Delta n_{l}}{dt} \right)$$
 (I. e)

- where S is the total entropy. We focus our attention on stationary processes, which are not
- necessarily at equilibrium. They exhibit observables that do not change over time (Pokrovskii
- 770 2013), and therefore

$$\frac{dn_l}{dt} = 0 ag{1. f. 1}$$

$$\frac{dS}{dt} = 0 ag{I.f. 2}$$

- 771 Taking into account (I.b), (I.e) and (I.f.1), the fulfilment of the constraint (I.f.2) requires that
- 772 δQ =0. Therefore, it can be concluded that a stationary system is characterized by a possible
- exchange of matter with a reservoir, but not an exchange of heat.

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The correct treatment of a system like the one introduced above requires, in principle, to be able to formulate explicitly both (I.c) and (I.d). Our aim is simpler, as we would like to exploit the capacity of an open system to freely exchange matter with a reservoir, in combination with a formalism as close as possible to the consolidated equilibrium thermodynamics' one. Such a model provides a flexible tool to approach problems in which one investigates the intrinsic exchanging/incorporation capacity of a given substance, without any sort of constraint or restraint.

An internal observer (*i.e.* an observer who measures the system's observables only, unaware of the matter flow) perceives a stationary open system as one that is under equilibrium conditions (P,T and { n_i } do not change over time and δQ =0). Therefore, all the state functions are invariant *versus* t and the system conserves its composition), with possible forward-backward reactions and without any in/out-flow of energy/matter. Let us represent the

$$\mu_l = \mu_{0l} + RT ln(x_l) + RT ln(\gamma_{l,int})$$
(I.g)

chemical potential of the *l*-reactant by the usual expression below,

where μ_{0l} is the component that depends on P-T only, and coincides with the Gibbs energy of the lth-reactant alone; $\gamma_{l,int}$ is the activity coefficient of the lth-reactant according to the internal observer and incorporates any sort of deviation from ideal mixing. Let us assume that $\{n_l\}$ can fluctuate, δn_i , in such a way that (I.f.1) is satisfied *on average*, yet preserving the global system's composition. Therefore, the internal observer perceives that the conservation of composition is achieved through a transformation of the reactants into each other, according to the classical relationship below

$$\frac{\delta n_l}{\nu_l} = \delta \hat{\varepsilon} \tag{I. h}$$

for any *l*-reactant; $\delta \hat{\varepsilon}$ is the infinitesimal change of the reaction ratio, seen by the internal observer. Using the equation above, we have that

$$dG = \left[\sum_{l} v_{l} \mu_{0l} + RT ln \left(\prod_{l} x_{l}^{v_{l}}\right) + RT ln \left(\prod_{l} \gamma_{l,int}^{v_{l}}\right)\right] \delta \hat{\varepsilon}$$
 (I. i)

The internal observer states that dG=0, given that the system is supposed at equilibrium, and from (I.i) the usual chemical equilibrium equation follows

$$exp\left(-\frac{\sum_{l}\nu_{l}\mu_{0l}}{RT}\right) = \frac{\prod_{k}x_{k}^{\nu_{k}}}{\prod_{j}x_{j}^{\nu_{j}}} \times \frac{\prod_{k}\gamma_{k,int}^{\nu_{k}}}{\prod_{j}\gamma_{j,int}^{\nu_{j}}} = K(P,T)_{int}$$
(I. k)

An external observer (*i.e.* an observer that is aware of the matter flow) confirms that dG=0 as the system lies in a stationary state, and using (I.b) expresses dG in terms of

$$dG = \left[\sum_{l} v_{l} \mu_{0l} + RT ln \left(\prod_{l} x_{l}^{v_{l}}\right) + RT ln \left(\prod_{l} \gamma_{l,ext}^{v_{l}}\right)\right] \delta \varepsilon$$

$$+ \left[\sum_{l} \delta \Delta n_{l} \mu_{0l} + RT ln \left(\prod_{l} x_{l}^{\delta \Delta n_{l}}\right) + RT ln \left(\prod_{l} \gamma_{l,ext}^{\delta \Delta n_{l}}\right)\right]$$
(I.1)

where $\delta \Delta n_l$ is the fluctuation due to the amount of l-reactant supplied by the reservoir via a matter flow; $\gamma_{l,ext}$ is the activity coefficient estimated by the external observer. Given that the global system's composition does not change in a stationary state, then the following relationship must hold for $\delta \Delta n_l$, too,

$$\frac{\delta \Delta n_l}{\nu_l} = \delta \zeta$$

which implies

$$dG = \left[\sum_{l} v_{l} \mu_{0l} + RT ln \left(\prod_{l} x_{l}^{\nu_{l}}\right) + RT ln \left(\prod_{l} \gamma_{l,ext}^{\nu_{l}}\right)\right] (\delta \varepsilon + \delta \zeta)$$
 (I. m)

Equ.(I.m), in combination with dG=0, leads to an expression similar to (I.k), save the term depending on the activity coefficients, *i.e.* $\prod_{l} \gamma_{l,ext}^{\nu_{l}}$, so that

$$exp\left(-\frac{\sum_{l} \nu_{l} \mu_{0l}}{RT}\right) = \frac{\prod_{k} x_{k}^{\nu_{k}}}{\prod_{j} x_{j}^{\nu_{j}}} \times \frac{\prod_{k} \gamma_{k,ext}^{\nu_{k}}}{\prod_{j} \gamma_{i,ext}^{\nu_{j}}} = K(P,T)_{ext}$$
(I. n)

Therefore, the γ activity coefficients "collect" the deviations from equilibrium that the internal and external observers detect. For (I.n) and (I.k) to coincide with one another, $\prod_{l} \gamma_{l,ext}^{\nu_{l}} = \prod_{l} \gamma_{l,int}^{\nu_{l}}$ must hold.

An open system may change its composition evolving towards a stationary state, according to the expression below, for the *l*th-reactant:

$$\int_0^\infty \frac{d\Delta n_l}{dt} dt = \Delta n_l(\infty) - \Delta n_l(0)$$

where it can be assumed that at $t\rightarrow\infty$ the open system has achieved a stationary state.

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I.3 Reactant proportions and probability

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What does it physically mean to neglect the activity coefficients in equations (I.n) and (I.k)?

Let us assume that a system has a known average Gibbs energy value, *i.e.* < G at P-T, and

that it may occupy given "states", each one with a probability $\{p_l\}$. Following a consolidated

approach of statistical mechanics and information theory (Jaynes 1957a-b), we state that the

likeliest and least prejudicial $\{p_l\}$ -set constrained to yield < G> must correspond to an extreme

of the expression beneath

$$\Phi = -R \sum_{l} p_{l} \ln(p_{l}) + \psi \left[\sum_{l} p_{l} G_{l} - \langle G \rangle \right]$$
(I.0)

where G_l is the Gibbs energy of the l^{th} -state; R is the gas constant and ψ is a lagrangian multiplier. If one requires that $\delta\Phi$ =0, then

$$p_l \propto \exp\left(-\frac{G_l}{RT}\right)$$
 (I. p)

taking $\psi=1/T$. Let us shape our system in terms of a multi-phase system, in which the "states" are represented by the "reactants" that can occur. Let the system undergo a reaction like (I.a) and be composed of the related reactants. We analyse equ.(I.a) in statistical terms. The occurrence of the left-hand or right-hand side member, can be modelled using the notion of "joint probability", thus obtaining

$$p_{left-hand\ side\ member} \propto \prod_{j} p_{j}^{\nu_{j}}$$

$$p_{right-hand\ side\ member} \propto \prod_{k} p_{k}^{\nu_{k}}$$

We take the ratio $p_{right-hand\ side\ member}/p_{left-hand\ side\ member}$, and observe that it can be either written

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$$\prod_l p_l^{
u_l}$$

835 or formulated as

$$\prod_{l} \left[exp\left(-\frac{G_{l}}{RT} \right) \right]^{v_{l}} = exp\left(-\frac{\sum_{l} v_{l} G_{l}}{RT} \right)$$

by means of (I.p). Hence, the equations above lead to

$$\prod_{l} p_{l}^{\nu_{l}} = exp\left(-\frac{\sum_{l} \nu_{l} G_{l}}{RT}\right) \tag{I.q}$$

Equ.(I.q) is readily likened to (I.n) and (I.k), neglecting the activity coefficients and setting for each phase $G_l = \mu_{0l}$. Altogether, a chemical equilibrium equation is thus formulated in a very simple and general fashion, which holds for stationary systems, too. Therefore, neglecting the activity coefficient terms in (I.n) and (I.k) leads to revising the notion of " l^{th} -reactant proportion", x_l , in terms of " l^{th} -reactant occurrence probability", p_l , *i.e.* $x_l = p_l$, once a given reaction is being considered.

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844 APPENDIX II

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846 II.1 Approximation to unity of the activity coefficients term of equ.(7.a)

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The activity coefficient term of equ.(7.a) can be simplified as

$$\gamma = \frac{\gamma_1}{\gamma_2^{1-\lambda} \times \gamma_3^{\lambda}} \tag{II.a}$$

- where we replaced Mg-Al-pv, Mg-pv and cor with 1, 2 and 3, respectively. Let us introduce
- 850 the geometric average of the $\gamma_{1,2,3}$ s, *i.e.*

$$\gamma_{ave} = (\gamma_1 \times \gamma_2 \times \gamma_3)^{1/3}$$

851 and

$$\gamma_1 = \gamma_{ave} + \delta_1 \tag{II. b. 1}$$

$$\gamma_2 = \gamma_{ave} + \delta_2 \tag{II. b. 2}$$

$$\gamma_3 = \gamma_{ave} + \delta_3 \tag{II. b. 3}.$$

852 Replacing γs in (II.a) with (II.b.1-2-3), then it is obtained

$$\gamma = \frac{\left(1 + \frac{\delta_{1}}{\gamma_{ave}}\right)}{\left(1 + \frac{\delta_{2}}{\gamma_{ave}}\right)^{1 - \lambda}} \times \left(1 + \frac{\delta_{3}}{\gamma_{ave}}\right)^{\lambda} \approx \frac{\left(1 + \frac{\delta_{1}}{\gamma_{ave}}\right)}{\left(1 - (1 - \lambda)\frac{\delta_{2}}{\gamma_{ave}}\right) \times \left(1 - \lambda\frac{\delta_{3}}{\gamma_{ave}}\right)} \approx \\
\approx \left(1 + \frac{\delta_{1}}{\gamma_{ave}}\right) \times \left(1 + (1 - \lambda)\frac{\delta_{2}}{\gamma_{ave}}\right) \times \left(1 + \lambda\frac{\delta_{3}}{\gamma_{ave}}\right) \\
\approx 1 + \frac{\delta_{1} + (1 - \lambda)\delta_{2} + \lambda\delta_{3}}{\gamma_{ave}} + o\left(\left(\frac{\delta}{\gamma_{ave}}\right)^{2}\right) \approx 1 \tag{II. c}$$

The approximation above requires $\delta \gamma_{ave} < 1$, which holds in most cases. In fact, earlier excess 853 enthalpy determinations on some HP-minerals (for instance, Fe-periclase: Sreçec et al. 1987; 854 garnets: Geiger et al. 1987; olivine: Kojitani and Akaogi 1994; Al-perovskite: Akber-Knutson 855 856 and Bukowinski 2004; Panero et al. 2006) exhibit absolute ΔH-maximum-values that yield average activity coefficients [estimated by $exp(\Delta H_{max}/RT)$, T=2000 K] lying between 1.07 and 857 1.34, with a geometric average of 1.2 and $<\delta/\gamma_{ave}>\sim$ 0.08. Note that $\delta_1+\delta_2(1-\lambda)+\delta_3\lambda$ is 858 expected to be in general small as the δs compensate each other, due to δ_1 , δ_2 , and δ_3 not 859 being of the same sign. Therefore, given that we can legitimately neglect the activity 860 coefficient in the case of equ. (7.a), x_l s and p_l s coincide with each other, according to 861 APPENDIX I.3. 862

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1191 CAPTIONS TO THE FIGURES

Figure 1. Equilibrium constant, $K(P,T,\lambda)$, of the fundamental alumina exchange reaction (5) *versus* λ , which expresses the exchanged amount of Al₂O₃ in the Mg-Al-pv, Mg-pv and cor system. $K(P,T,\lambda)$, calculated by the open system model, is displayed at 24 GPa/1919 K (blue line), 44 GPa/2145 K (red line) and 80 GPa/2551 K (black line), by way of example. Black filled circles indicate the maxima at the three chosen P-T points, and correspond to the λ -values that most shift the reaction $(1-\lambda)$ MgSiO₃+ λ Al₂O₃ \leftrightarrow (Mg_{1- λ}Al_{λ})(Si_{1- λ}Al_{λ})O₃ to the right (equ.5, of the text).

Figure 2. $K(P,T)_{ave}$ *versus P*, according to the chosen geotherm and calculated by the open system model. Blue line and red line show two different trends for the average equilibrium constant, $K(P,T)_{ave}$, of the reaction (5). Note that $K(P,T)_{ave} = \langle K(P,T,\lambda) \rangle_{\lambda}$ (see 4.2.1 section for further explanations).

Figure 3. Phase proportions of Al-free perovskite (Mg-pv), Al-bearing perovskite (Mg-Al-pv) and corundum (cor) $versus\ P$, according to the chosen geotherm. Mg-Al-pv fractions have an average Al₂O₃ composition provided by λ_{Al2O3} , calculated according to equ.(9.b) on the P-T range of interest and shown in Fig.5. Al-free perovskite is an extreme notion, which provides a "limit" to define a tendency of such mineral to incorporate aluminium.

Figure 4. Al₂O₃-partitioning between corundum and perovskite (cor(mol)/Mg-Al-pv(mol)) versus P, according to the chosen geotherm and calculated by the open system model. The red box shows the region of maximum Al-uptake for perovskite (saturation region), suggesting that at such P-T conditions the Al-incorporation is weakly dependent on pressure. At higher pressure, the cor/Mg-Al-pv ratio trend hints at a possible instability of perovskite (transition to another phase, such as post-perovskite, ppv?). See text for further discussion.

1218 1219 **Figure 5**. Average Al₂O₃ mole fraction in perovskite, λ_{Al2O3} , determined by the open system 1220 model and calculated via equ.(9.b), as a function of P along the chosen geotherm. In the Pregion 30-50 GPa, λ_{Al2O3} is *quasi* constant (interpolation solid line). 1221 1222 Figure 6. Al₂O₃ mole fraction in perovskite, $\xi_{closed\ system}$, determined by the closed system 1223 model and calculated via equ.(14), as a function of P along the chosen geotherm. At $\lambda = \xi_{\text{closed}}$ 1224 system, $K(P,T,\lambda)$ takes an extreme value, so that reaction (5) is shifted to the right as much as 1225 1226 possible. 1227 Figure 7. Cell volume disagreement (%), between measurements and our calculations, in the 1228 1229 case of Al-bearing perovskite, as a function of P. Experimental values from Walter et al (2004).1230 1231 Figure 8. The predicted total Al₂O₃ (wt%) stored in Mg-Al-pv, calculated by the open system 1232 model, assuming perovskite amounts of 76% (red dots) and 85% (blue dots) of the lower 1233 1234 mantle mass, in pyrolite and chondrite reference models (Table 1), respectively. Bulk Al₂O₃ 1235 contents of pyrolite (A) and chondrite (A1) primitive lower mantle models are shown by red 1236 and blue solid lines, respectively. Bulk Al₂O₃ contents of pyrolite-type and chondrite-type 1237 non-primitive lower mantle models calculated by adding a 3 wt% of MORB-component (B) are represented by red and blue dotted lines, respectively. MORB composition from Hirose et 1238 1239 al. (1999). *P-T* region of 24-80 GPa/1919-2550 K is referred to the chosen geotherm. 1240 **Figure 9.** Probability (p₀%) of Mg-Al-pv occurrence with a given Al₂O₃ mole content per 1241 formula unit, according to the open system model. Each curve is associated to key P-T values 1242

(P in legend), along the chosen geotherm. The Al₂O₃ contents of natural Al-bearing

1243

perovskite (\leftrightarrow) *claimed* from the lower mantle, are provided by Kaminsky and Lin (2017). In the inset table, the absolute probability to find Al-bearing perovskite (Mg-Al-Pv) against Mgperovskite (Mg-pv) is reported for the explored P-T region of the lower mantle.

Table 1. Lower mantle (pyrolite, end-member A, and chondrite, end-member A1) and MORB-like silicate glass (end-member B) major oxides compositions. Enriched LM models according to Faure(1986) mixing equation.

Pyrolitic lower mantle model	A	A+3% B	В
wt%			
${ m SiO_2}$	45.00	45.14	49.64
Al_2O_3	4.45	4.76	14.88
FeO_t	8.05	8.15	11.43
MgO	37.80	36.92	8.51
CaO	3.55	3.76	10.52
Na2O	0.36	0.44	2.90
H_2O	*0.15	0.149	**0.10
(Mg-pv+Mg-Fe-pv+Mg-Al-pv) +	76.00	75.56	31.30
Chondritic lower mantle			
model	A1		В
	A1+3% B		
wt%			
${ m SiO}_2$	47.30	47.37	49.64
Al_2O_3	3.99	4.31	14.88
FeO_t	8.12	8.22	11.43
$_{ m MgO}$	37.36	36.50	8.51
CaO	2.29	2.54	10.52
Na_2O	0.34	0.42	2.90
H_2O	*0.15	0.149	**0.10
$\left(Mg\text{-}pv\text{+}Mg\text{-}Fe\text{-}pv\text{+}Mg\text{-}Al\text{-}pv\right)^+$	85.00	84.89	31.30

end member A from McDonough and Sun (1995) end member A1 from Merli et al. (2016), modified end member B= MORB-like silicate glass of Hirose et al.(1999)

^{+ =} global estimates (wt%) of pure perovskite (Mg-pv), bridgmanite (Mg-Fe-pv) and Al beraring perovskite (Mg-Al-pv)

^{*=} lower mantle water estimates from Merli et al. (2016) and Muir and Brodholt (2018)

^{**=} MORB water estimates from Ghosh et al.(2014) and Marty (2012)

Table 2. Probability, expressed in %, of having the appropriate elemental availability to form a given phase (chemical probability of formation = p (J,chem); see section 3.1). Calculations are carried out by Pyrolite (A) and Chondrite (A1) lower mantle reference models, and by their compositions mixed with 3 wt% of MORB-component (A+3%B; A1+3%B)

		Pyrolite		Chondrite	
Phase name	Composition	A	A+3%B	A1	A1+3%B
Fe-periclase	$(\mathrm{Mg}_{0.8}\mathrm{Fe}_{0.2})\mathrm{O}$	33.59	33.24	32.22	31.91
Ca-perovskite	$CaSiO_3$	0.674	0.745	0.452	0.523
Mg-perovskite	${ m MgSiO_3}$	23.89	23.84	24.63	24.55
Bridgmanite	$(\mathrm{Mg}_{0.9}\mathrm{Fe}_{0.1})\mathrm{SiO}_3$	20.76	20.83	21.44	21.49
Mg-Al-perovskite	$(Mg_{0.9}Al_{0.1})(Si_{0.9}Al_{0.1})O_3$	20.24	20.41	20.49	20.66
sum		64.90	65.08	66.56	66.70
δ-phase ¹	AlO(OH)	0.052	0.058	0.044	0.049
H-phase ²	$(MgSi,Al_2)O_4H_2$	0.045	0.047	0.043	0.045
D-phase ³	$Al_2SiO_4(OH)_2$	0.002	0.002	0.002	0.002
NAL/CF ⁴	$Na_{0.265}Fe_{0.245}Mg_{0.375}Ca_{0.035}Al_{1.1}Si_{0.715}O_{4} \\$	0.737	0.825	0.679	0.769
sum		0.836	0.932	0.768	0.865

end-member A from McDonough and Sun (1995) end-member A1 from Merli et al.(2016), modified end-member B= MORB-like silicate glass of Hirose et al. (1999)

1: Ohtani et al. (2001); 2: Ohtani et al. (2014); 3: Pamato et al. (2015); 4: Guignot and Andrault (2004)

Table 3. Chemical probability of formation [p (J,chem)] expressed in % of potential lower mantle Al-bearing phases.

		Pyrolite		Cho	ondrite
Phase name	Composition	A	A+3%B	A1	A1+3%B
Mg-Al-perovskite	$(Mg_{0.9}Al_{0.1})(Si_{0.9}Al_{0.1})O_3$	96.04	95.63	96.39	95.98
δ -phase ¹	AlO(OH)	0.25	0.27	0.20	0.23
H-phase ²	$(MgSi,Al_2)O_4H_2$	0.21	0.22	0.20	0.21
D-phase ³	$Al_2SiO_4(OH)_2$	0.01	0.01	0.01	0.01
NAL/CF ⁴	$Na_{0.265}Fe_{0.245}Mg_{0.375}Ca_{0.035}Al_{1.1}Si_{0.715}O_{4} \\$	3.50	3.87	3.20	3.57
		100.00	100.00	100.00	100.00

end-member A from McDonough and Sun (1995) end-member A1 from Merli et al.(2016), modified end-member B= MORB-like silicate glass of Hirose et al. (1999)

1: Ohtani et al. (2001); 2: Ohtani et al. (2014); 3: Pamato et al. (2015); 4: Guignot and Andrault (2004)

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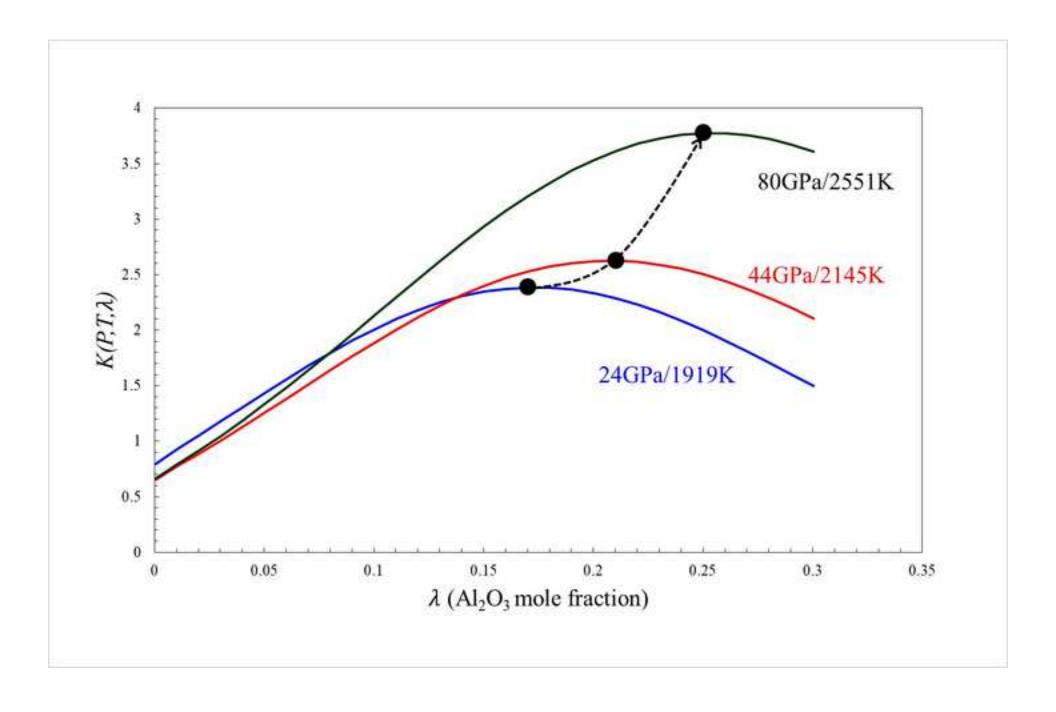


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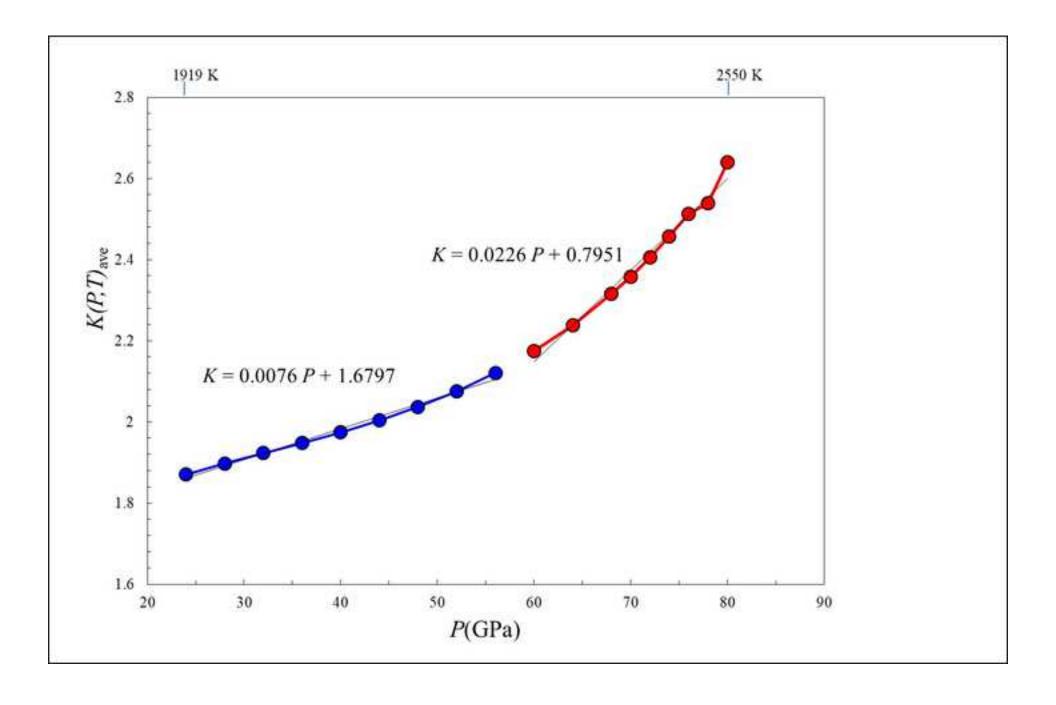


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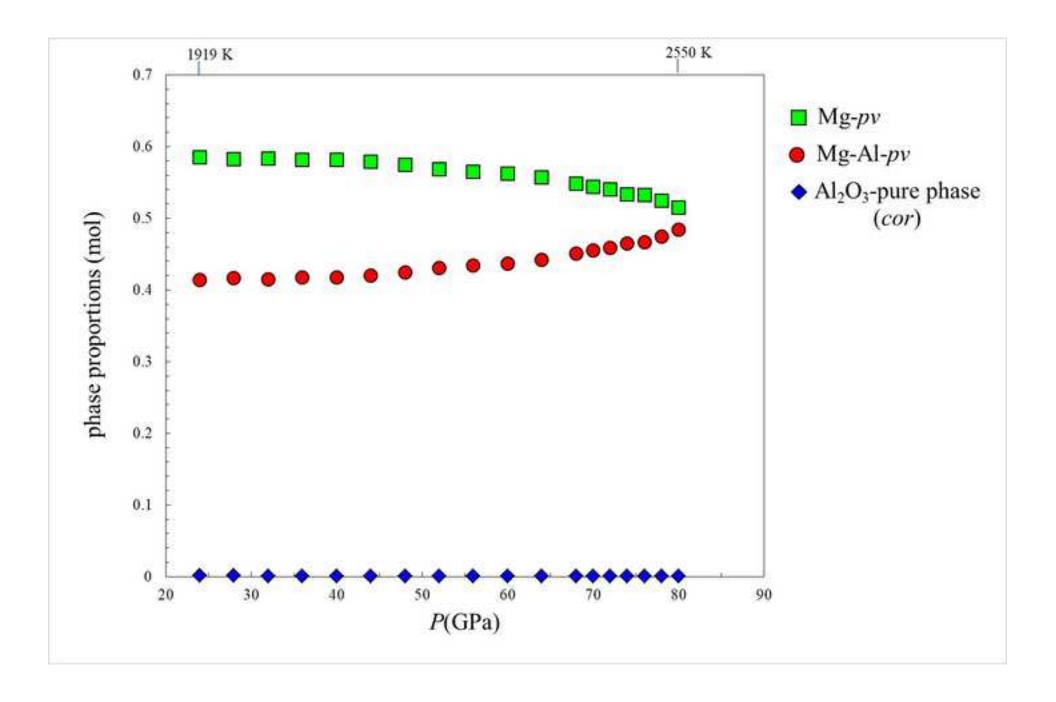


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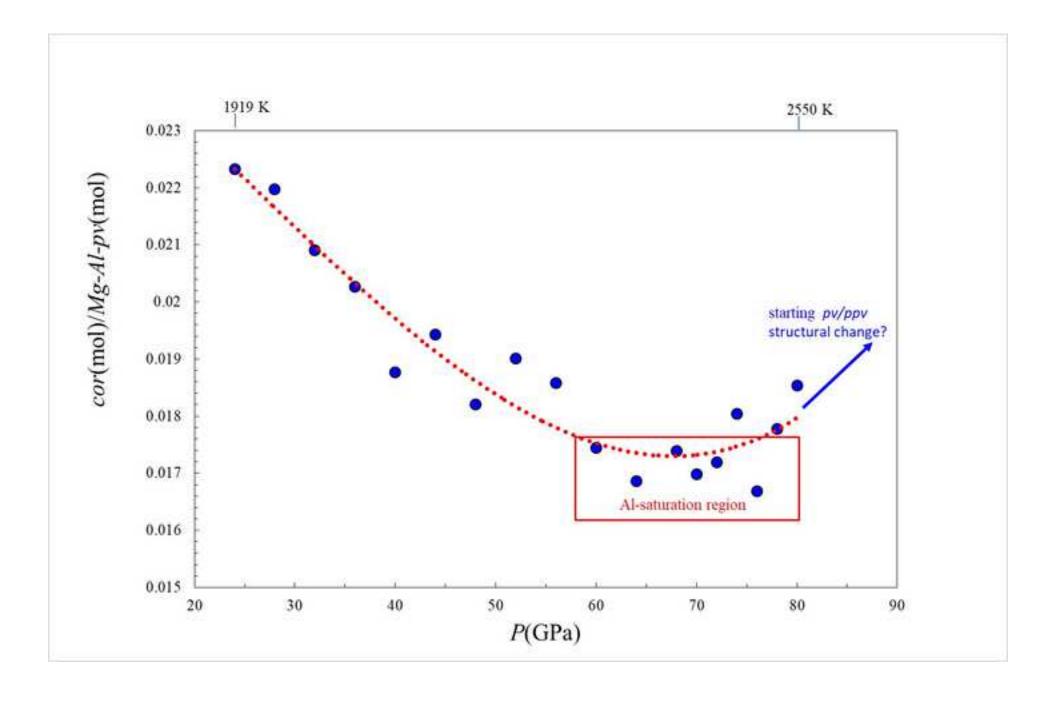


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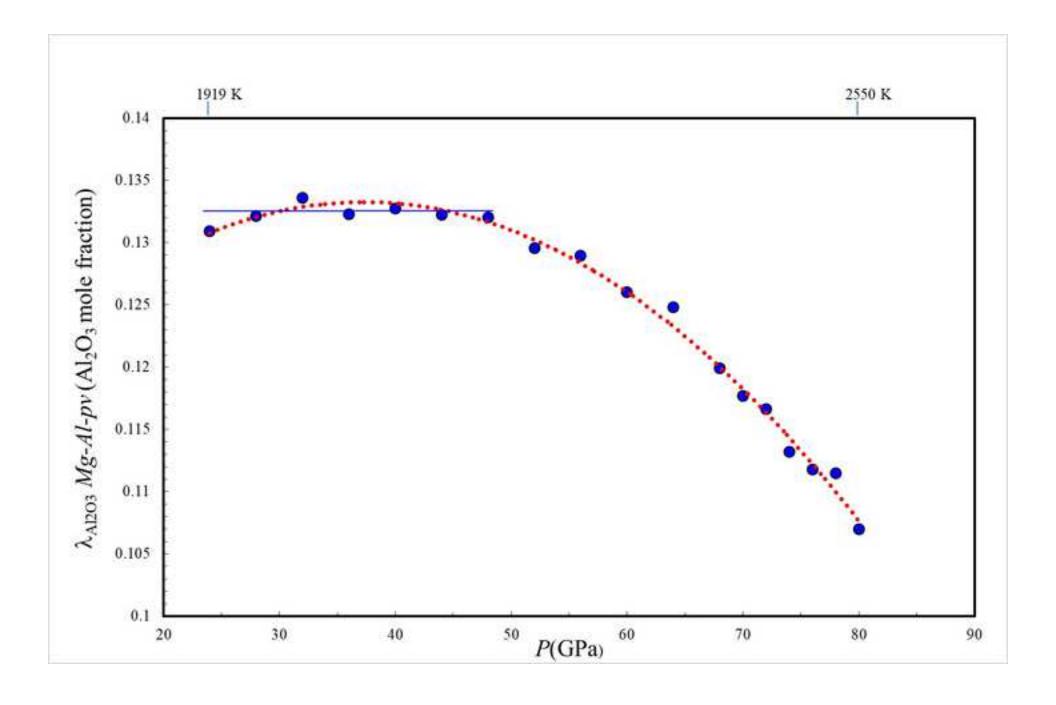


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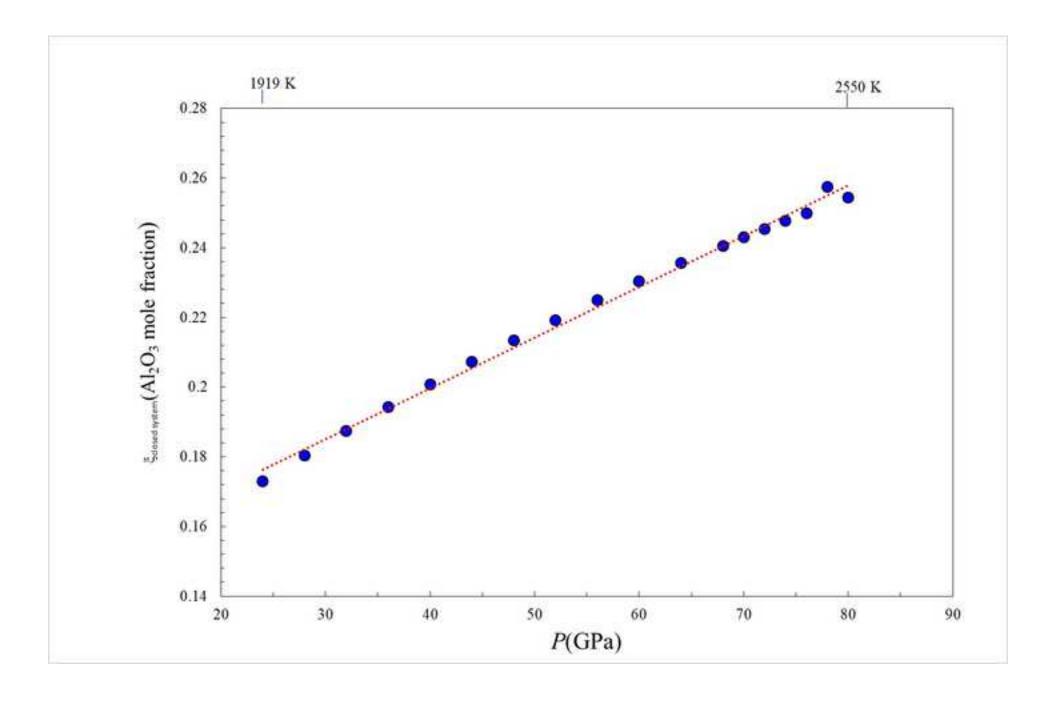


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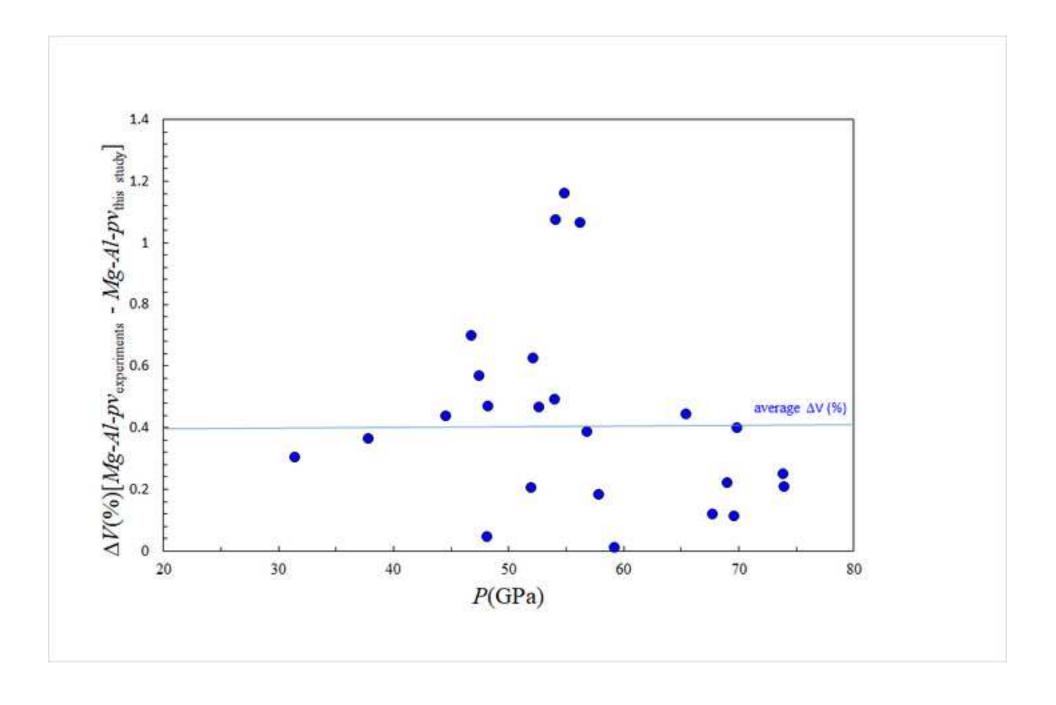


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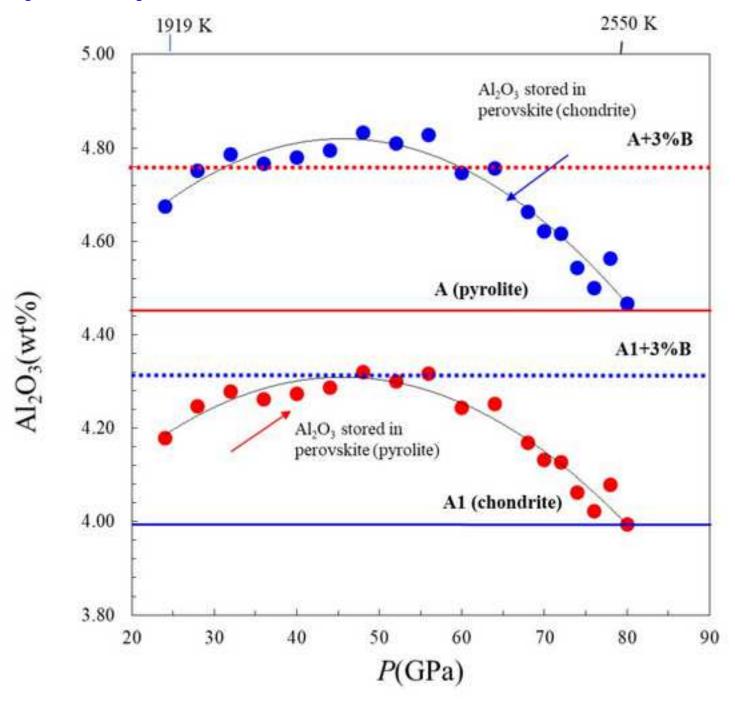
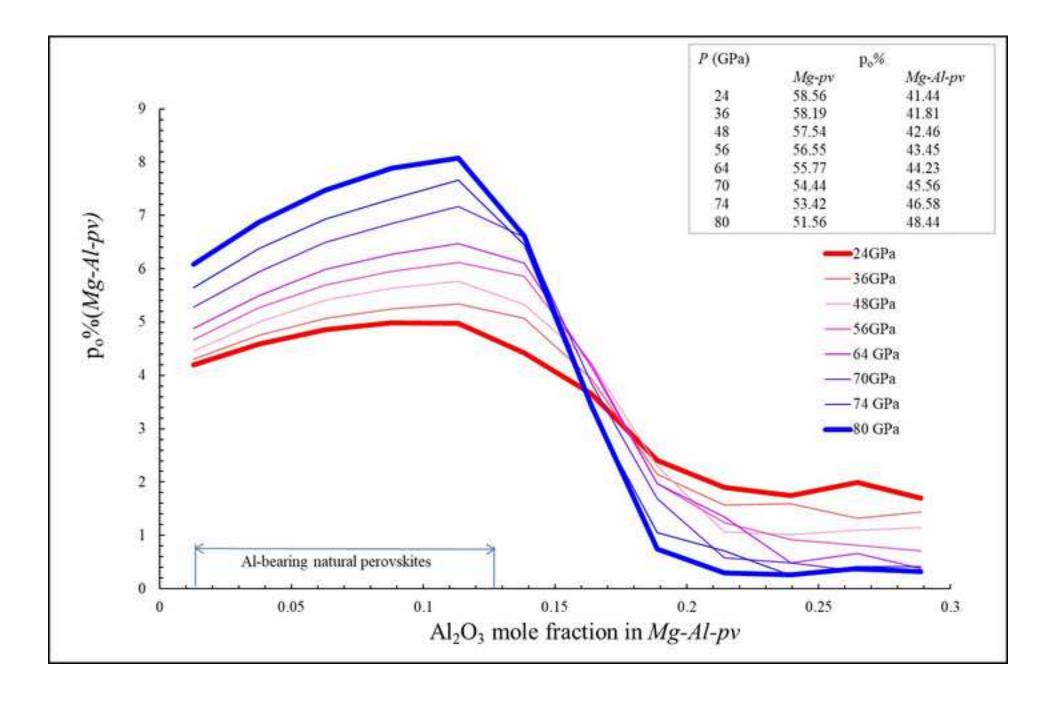


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	0.3	upper-x	
P		Т	K
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	28	1964	1.8972
	32	2009	1.9226
	36	2054	1.9479
	40	2100	1.9745
	44	2145	2.0036
	48	2190	2.0367
	52	2235	2.0753
	56	2280	2.1207
	60	2325	2.1746
	64	2371	2.2387
	68	2416	2.3149
	70	2438	2.3582
	72	2461	2.4053
	74	2484	2.4566
	76	2506	2.5125
	78	2829	2.5396
	80	2551	2.6393

Р	Т		Χ	K
	24	1919	0.0005	0.7937262
	24	1919	0.0105	0.9293135
	24	1919	0.0205	1.0568378
	24	1919	0.0305	1.1839746
	24	1919	0.0405	1.3111602
	24	1919	0.0505	1.4376564
	24	1919	0.0605	1.5622545
	24	1919	0.0705	1.6835027
	24	1919	0.0805	1.7998221
	24	1919	0.0905	1.9095857
	24	1919	0.1005	2.0111818
	24	1919	0.1105	2.1030729
	24	1919	0.1205	2.1838465
	24	1919	0.1305	2.2522621
	24	1919	0.1405	2.3072891
	24	1919	0.1505	2.3481417
	24	1919	0.1605	2.3742988
	24	1919	0.1705	2.38552
	24	1919	0.1805	2.3818495
	24	1919	0.1905	2.3636093
	24	1919	0.2005	2.3313859
	24	1919	0.2105	2.2860057
	24	1919	0.2205	2.2285073
	24	1919	0.2305	2.1601033

0.1705 2.3855