

Automation Systems Design and Laboratory Prototyping Aimed at Mature Petroleum Drilling Rig Retrofitting

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Abstract: This paper presents a control system design methodology for the drill-string rotary drive and draw-works hoist system aimed at mature drilling rig retrofitting. The rotary drive is equipped with an active damping speed control system featuring a proportional-integral speed controller readily available within modern controlled electrical drives, extended with drill-string back-spinning prevention scheme for the case of stuck tool. The draw-works hoist system features a tool normal force (Weight-on-Bit) controller with tool longitudinal speed (Rate-of-Penetration) limiting functionality. The design of proposed control systems has been based on suitable control-oriented process models and damping optimum criterion which guarantees a desired level of closed-loop system damping. The proposed drilling control systems have been verified on a downscaled laboratory experimental setup, which represents a necessary pre-requirement before these systems are tested in the field.

Keywords: active damping; draw-work; laboratory setup; petroleum drilling; proportional-integral controller; retrofitting; top-drive; torsional vibrations

1 INTRODUCTION

Diminishing petroleum reserves and related increase in its prices [1] generally stimulate the discovery of new reserves [2], and implementation of advanced drilling technologies [3], especially those aimed at enhanced recovery of hydrocarbons [4]. However, a notable portion of mature petroleum drilling rigs is still equipped with quite functional "legacy" drilling hardware [5], whose useful service life may be prolonged through retrofitting, primarily in terms of control system upgrades [6].

Figure 1 shows the principal schematic representation of one such mature petroleum drilling rig [6]. Borehole drilling is achieved by simultaneous rotary action of the so-called top-drive (based either on the hydraulic or electric motor) and the draw-works hoist electrical drive, wherein the former transfers the torque to the drilling tool via the drill-string, and the latter facilitates drill-string longitudinal motion (Rate-of-Penetration, *RoP*) and establishing of drilling tool normal force (Weight-on-Bit, *Wob*). Thus, the drilling tool pulverizes the rock material, and the resulting drilling cuttings are removed by drilling fluid (mud) circulated by dedicated mud pumps.

In the case of aforementioned "legacy" drilling systems, the top-drive is typically controlled without regard to the drill-string compliance coupled with the so-called drilling tool stick-slip effect, which cause drill-string system torsional vibrations [7]. These vibrations may, in turn, result in mechanical component wear and fatigue, and decreased borehole drilling rates due to drilling safety concerns (see e.g. [6] and references therein). On the other hand, the draw-works system on such mature drilling rigs is typically manually controlled by means of a mechanical brake [5], which makes these systems' drilling productivity and operational safety less competitive compared to state-of-the-art drilling systems. In order to improve the performance of these mature rigs, they may be retrofitted with advanced drill-string system controls [6]. Moreover, these upgrades are likely to comprise only a fraction of brand new drilling rig cost, which would be affordable to small-to-medium size service companies [8]. To this end, a number of advanced drilling control system concepts have been researched and tested both in the laboratory and

in the field, wherein detailed modelling of the drill-string system is key for subsequent control system design [7-17].

An early concept of torsional vibrations suppression system based on passive vibration absorber emulation has been proposed in [7]. Its subsequent development has been directed towards implementation of vibration absorber functionality in servo-controlled rotary electrical drives featuring a standard proportional-integral (PI) speed controller [9]. As shown in [10], PI speed controller tuned for active damping of torsional vibrations may result in notable vibration suppression and increased borehole drilling rates. In order to avoid re-tuning of PI speed controller altogether, the torsional vibrations suppression system in [11] proposes an external drill-string torque feedback, thus including an additional state variable within the control system framework. Even though state control approaches such as those based on H_∞ controller [12] and linear quadratic regulator (LQR) controller [13] can achieve favourable torsional vibration suppression, their implementation requires complete state feedback. For a detailed overview of torsional vibration suppression approaches, the reader is referred to [14].

The retrofitting efforts of draw-works hoist systems have included: (i) servo-pneumatic or servo-hydraulic disk brake system control [15], (ii) electrical servo control of the mechanical brake actuator [16], and (iii) utilization of the main or auxiliary draw-works electric motor [17]. The *Wob* control can be realized by using a conventional cascade control system structure [15], or more advanced controllers such as the fuzzy logic controller [17], or the passivity-based controller [18]. The latter reference also suggests that additional attenuation of torsional vibrations is possible by means of precise draw-works hoist control.

Having this in mind, the main contribution of this paper is the comprehensive design methodology for the drill-string rotary drive torsional vibration active damping and draw-works hoist-based *Wob* control systems based on suitable control-oriented process models and damping optimum criterion [19]. In both cases, control systems are based on the well-established PI controllers, with the rotary drilling drive PI speed controller augmented with the back-spinning prevention scheme for the case of stuck drilling

tool. The proposed control systems are verified on a downscaled laboratory experimental setup.

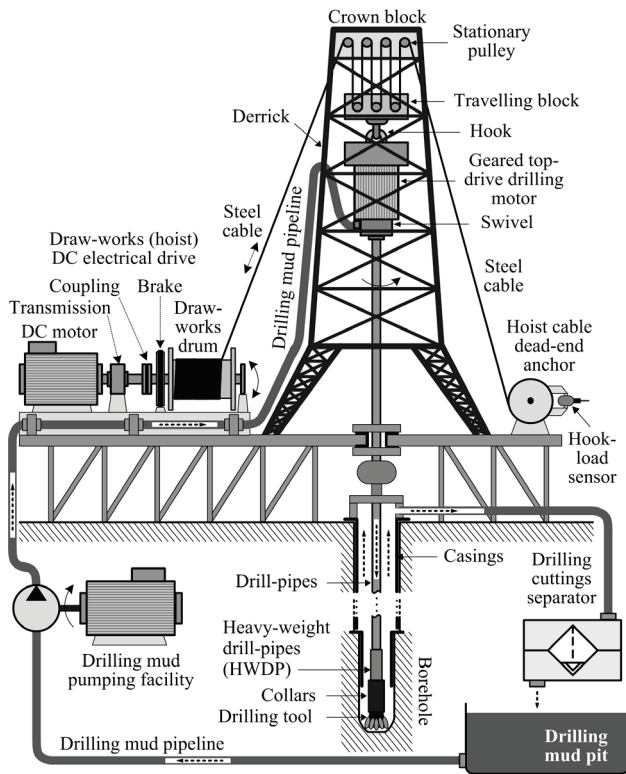


Figure 1 Schematic layout of petroleum drilling rig with top-drive and draw-works drives for drill-string rotary and longitudinal motion

2 DRILL-STRING SYSTEM MODELLING

This section presents the drill-string system models for rotational and longitudinal motion along with the accompanying electrical drives and transmission systems.

2.1 Model for Drill-String Rotational Motion

The drill-string rotational dynamics are modelled by the so-called two mass elastic system in Fig. 2, wherein drill-pipes act as a torsional spring with their stiffness and damping coefficients k and c , respectively [7]. The motor and gearbox inertias are lumped into the motor-side inertia J_1 , while the heavy-weight drill-pipe (HWDP), collar and drill-pipe inertias (J_{hw} , J_c and J_{dp}) and drilling tool inertia J_{tool} are lumped into the inertia J_2 at the side of bottom-hole assembly (BHA):

$$J_2 = J_{tool} + J_c + J_{hw} + J_{dp} \quad (1)$$

The model in Fig. 2 is characterized by the following resonance frequencies corresponding to the cases of stuck drilling tool, stiff motor-side speed control, and freely-oscillating drill-string, respectively [4]:

$$\Omega_{01} = \sqrt{\frac{k}{J_1 i^2}}, \quad \Omega_{02} = \sqrt{\frac{k}{J_2}}, \quad \Omega_0 = \sqrt{\Omega_{01}^2 + \Omega_{02}^2}, \quad (2)$$

The drilling tool-side friction torque m_{f2} can be described by the generalized Stribeck static curve [20]:

$$m_{f2}(\omega_2) = \left[M_C + (M_S - M_C) e^{-|\omega_2/\omega_s|^\delta} \right] \text{sgn}(\omega_2) \quad (3)$$

where M_C is the Coulomb friction torque, M_S is the maximum static friction torque, δ is the so-called Stribeck coefficient and ω_s is the Stribeck speed.

In order to achieve favourable numerical computation efficiency in the zero-speed (stiction) region, the so-called Karnopp friction model modification can be used instead [20]. For the sake of simplicity, a Coulomb model may be used to simulate motor-side friction ($m_{f1} = M_{Cm} \text{sgn}(\omega_1)$).

It is assumed that the top-drive electrical motor is equipped with an appropriate power converter unit with embedded fast current/torque control loop, characterized by a rather small overall torque lag T_Σ with respect to torque reference m_{1R} within the closed-loop model [21]:

$$m_1(s) = \frac{1}{T_\Sigma s + 1} m_{1R}(s) \quad (4)$$

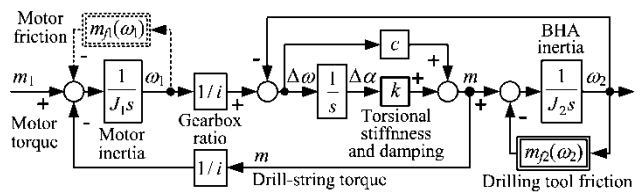


Figure 2 Block-diagram of drill-string system model for rotational motion

2.2 Model for Drill-String Longitudinal Motion

The drill-string model for longitudinal motion is depicted by the block diagram in Fig. 3, which comprises several sub-models. It is assumed herein that the draw-works electrical drive is driven by a power converter unit with embedded torque and speed controllers, tuned to achieve fast and well-damped speed control loop response. In that case, the load effect due to steel-rope force tension can be effectively dealt with the fast speed controller [21], and the draw-works motor speed ω_w vs. speed target ω_{Rw} response dynamics can be approximated by a first order lag term:

$$\omega_w(s) = \frac{1}{T_{ew}s + 1} \omega_{Rw}(s) \quad (5)$$

The resulting draw-works drive speed ω_w is translated to the steel rope tangential speed v_r at the drum through the ratio of drum radius r_d and motor gearbox ratio i_g . The steel rope speed v_r represents the input of the steelrope and travelling block mass-spring subsystem, characterized by its mass m_h and steel rope stiffness and damping coefficients k_r and c_r , respectively. The hook mass is accelerated by the sum of forces acting upon it, which include the rope force F_r transmitted through the pulley system with transmission ratio z , the gravity-related hook-load $m_h g$ ($g = 9.81 \text{ m/s}^2$) and the dilatation force F_{ds} of the drill-string.

The travelling block longitudinal speed v_h is fed to the drill-string vs. BHA mass-spring subsystem [15], characterized by its stiffness and damping coefficients k_{ds} and c_{ds} , and total mass m_B at the BHA side, which is subject

unwinding in case of stuck drilling tool, and draw-works drive-based Weight-on-Bit control.

3.1 Damping Optimum Criterion

The controller tuning herein is based on the damping optimum (or double ratios) criterion [19], which is a pole-placement-like method of design of linear continuous-time closed-loop systems with a full-order or reduced-order controller. The controller tuning procedure is based on the following formulation of the closed-loop characteristic polynomial:

$$A(s) = D_2^{n-1} D_3^{n-2} \dots D_n T_e^n s^n + \dots + D_2 T_e^2 s^2 + T_e s + 1 \quad (9)$$

where T_e is the closed-loop system equivalent time constant, and D_2, D_3, \dots, D_n are the so-called characteristic ratios, and n is the closed-loop system order.

When all characteristic ratios are set to optimal values $D_2 = D_3 = \dots = D_n = 0.5$ (by means of a full-order controller), the closed-loop system has a quasi-aperiodic step response with an overshoot of approximately 6% and the approximate settling time of 1.8-2.1 T_e . If a reduced-order controller of order r is used, only the dominant characteristic ratios D_2, \dots, D_{r+1} are set to desired values.

The closed-loop damping is primarily determined by the value of the most dominant characteristic ratio D_2 . By decreasing its value (i.e. for $D_2 \leq 0.35$) the closed-loop system is characterized by aperiodic step reference response without overshoot. Moreover, by increasing the T_e value, the control system robustness and noise sensitivity are generally improved, with the consequence of slower response and less efficient disturbance rejection.

3.2 Torsional Vibrations Active Damping System

Fig. 5a shows the block diagram representation of the cascade control system for drill-string electrical drive speed control, wherein the superimposed PI speed controller commands the torque reference m_{1R} to the inner torque control system within the power converter. Assuming that the overall torque lag T_Σ is small ($T_\Sigma \ll \Omega_{02}$) [10], the drilling tool is freely rotating ($|\omega_2| > 0, m_2 = 0$), and the drill-string damping coefficient is negligible ($c = 0$), the following fourth-order transfer function model is obtained between the speed reference ω_R and tool speed ω_2 referred to the motor side (cf. Figs. 2 and 5a):

$$G_c(s) = \frac{i\omega_2(s)}{\omega_R(s)} = \frac{1}{a_{c4}s^4 + a_{c3}s^3 + a_{c2}s^2 + a_{c1}s + 1} \quad (10)$$

with the transfer function coefficients defined as:

$$a_{c4} = (J_1 + J_2 / i^2) T_{c\omega} K_{c\omega}^{-1} \Omega_0^{-2} \quad (11)$$

$$a_{c3} = T_{c\omega} \Omega_{02}^{-2} \quad (12)$$

$$a_{c2} = (J_1 + J_2 / i^2) T_{c\omega} K_{c\omega}^{-1} + \Omega_{02}^{-2} \quad (13)$$

$$a_{c1} = T_{c\omega} \quad (14)$$

In order to obtain the analytical expressions for the PI controller integral time constant $T_{c\omega}$ and proportional gain $K_{c\omega}$, the transfer function (10) denominator coefficients a_{c1}, a_{c2}, a_{c3} and a_{c4} are equated with the coefficients of the fourth-order damping optimum characteristic polynomial according to (9). The final result reads as follows:

$$T_{c\omega} = T_e = \frac{1}{D_{2\omega} \sqrt{D_{3\omega}} \Omega_{02}} \quad (15)$$

$$K_{c\omega} = \frac{T_{c\omega} (J_1 + J_2 / i^2) \Omega_{02}^2}{D_{2\omega} T_{c\omega}^2 \Omega_{02}^2 - 1} \quad (16)$$

thus indicating that the PI speed controller is tuned with respect to the drilling tool-side resonance frequency Ω_{02} , and the closed-loop system dominant dynamics should be well-damped for the optimal characteristic ratio values ($D_{2\omega} = D_{3\omega} = 0.5$). Note, however, that the PI controller has only two parameters ($K_{c\omega}$ and $T_{c\omega}$), and is thus unable to optimally tune the damping of high-frequency modes related to the non-dominant characteristic ratio $D_{4\omega}$ [10].

In contrast to the above tuning approach the more commonly-used symmetrical optimum tuning criterion [21] only accounts for the overall inertia and torque lag:

$$T_{c\omega} = 4T_\Sigma \quad (17)$$

$$K_{c\omega} = \frac{J_1 + J_2 / i^2}{2T_\Sigma} \quad (18)$$

which results in "stiff" control of motor speed, but does not account for drill-string compliance effects [10].

The torsional vibration active damping system based on PI speed controller is extended with the prevention of the so-called back-spinning effect [10], which is based on simple flip-flop logic, and superimposed to the speed control system as shown in Fig. 5b. Namely, detection of stuck drilling tool condition is indicated if notable error of model-based rotary drive speed prediction ω_m occurs simultaneously with large torque command m_{1R} to the top-drive motor. In that case, the flip-flop is set, and a small negative speed reference is commanded to unwind the drill-string in a controllable way. The speed reference ω_R is returned to the operator's reference $\omega_{R,op}$ (the flip-flop is reset) when the drill-string is sufficiently unwound.

An additional torque reserve should be added to the operator's torque limit $M_{m,op}$ during constrained motion to enable safe unwinding of the rotary drilling drive [10]:

$$M_{res} = J_1 \omega_{1s} \Omega_{01} \quad (19)$$

which accounts for the accumulated motor momentum under constrained motion conditions $J_1 \omega_{1s}$ and the natural frequency of drilling motor vibrations Ω_{01} under stuck drilling tool conditions (see [10]). The steady-state top-drive speed ω_{1s} under constrained motion conditions can be estimated from the commanded speed target $\omega_{R,op}$ by using the following straightforward relationship [10]:

$$\omega_{1s} = (1 + J_1 \Omega_{01}^2 T_{c\omega} / K_{c\omega})^{-1} \omega_{R,op} \quad (20)$$

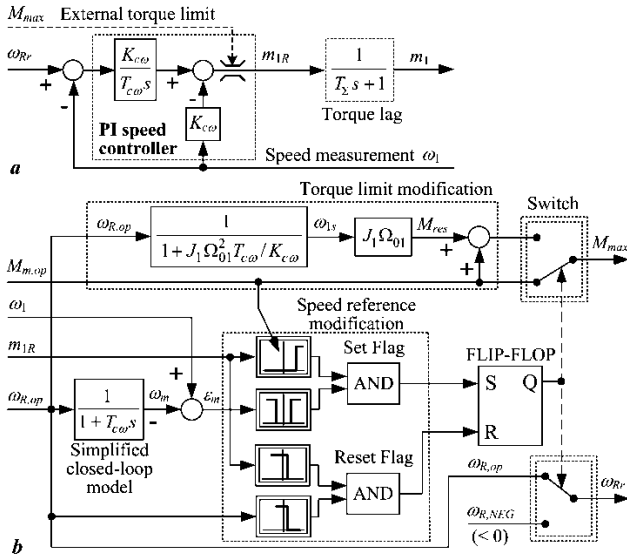


Figure 5 Block diagram of active damping control strategy featuring PI speed controller (a) and back-spinning prevention algorithm (b)

3.3 Weight-on-Bit Control System

Fig. 6 shows the block diagram of the WoB PI controller, which supplies the speed reference ω_R to the lower-level draw-works electrical drive speed control loop (WoB controller is cascaded to the draw-works inner speed control loop). The speed reference ω_R provided by the WoB controller is limited for the downward motion of the drill-string to the maximum safe value ω_{max} predefined by the operator. The controller output sign reversal is due to WoB sensor model in Fig. 3.

The controller design is based on the simplified control-oriented process model (8), which results in the following WoB control system closed-loop model:

$$G_c(s) = \frac{K_{wob} K_{pw}}{T_{pw} T_{wob} s^2 + (1 + K_{wob} K_{pw}) T_{wob} s + K_{wob} K_{pw}} \quad (21)$$

Again, by applying the damping optimum tuning procedure (with $n = 2$ in equation (9)), the following analytical expressions are obtained for the PI controller gain and integral time constant, respectively:

$$K_{wob} = \frac{1}{K_{pw}} \left(\frac{T_{pw}}{D_{2w} T_{ewob}} - 1 \right) \quad (22)$$

$$T_{wob} = T_{ewob} \left(1 - \frac{D_{2w} T_{ewob}}{T_{pw}} \right) \quad (23)$$

$$0 < T_{ewob} < \frac{T_{pw}}{D_{2w}} \quad (24)$$

wherein the inequality condition (24) relates to the feasibility of equivalent closed-loop time constant T_{ewob} in terms of obtaining non-negative controller parameters.

Note that a smaller value of the equivalent time constant T_{ewob} may result in increased sensitivity of the closed-loop system high-frequency modes to model approximation error (cf. Eqs. (6) and (8)). Hence, a larger

T_{ewob} choice should be preferred in order to obtain robust closed-loop behaviour in the high-frequency range. Moreover, in order to avoid the WoB response overshoot beyond the target value, the characteristic ratio D_{2w} should also be decreased below the optimal value.

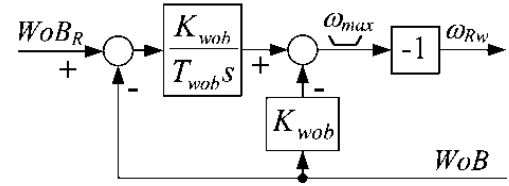


Figure 6 Block diagram of Weight-on-Bit PI controller

4 EXPERIMENTAL RESULTS

The proposed drilling control systems have been verified experimentally on a downscaled drill-string system laboratory setup developed in [22], whose principal schematic is shown in Fig. 7. It comprises a dual electrical drive with identical torque and speed ratings ($M_r = 3.78$ Nm and $\omega_r = 1390$ rpm). One of the servo-controlled induction motors (IMs) is used as the controlled electrical drive, while the second motor is used to emulate a realistic load from the working mechanism. The load "emulator" drive receives a suitable torque reference from the industrial PC, which runs the real-time simulation of rotary or draw-works drive dynamics, and also performs on-line data logging. An additional inertia disk with inertia $J_r = 0.0122$ kgm² is inserted between the motors in order to achieve similar starting dynamics of the downscaled drive and the actual drive in the field. Tabs. 2 and 3 list the parameters of the realistic drill-string system, downscaled to the low-power laboratory setup based on the methodology presented in [10]. For the sake of simplicity, the recorded variables (with the exception of WoB) are presented in per unit (p.u.) system, with the normalization of variables based on actual top-drive speed and torque ratings and gearbox ratios in Tabs. 2 and 3.

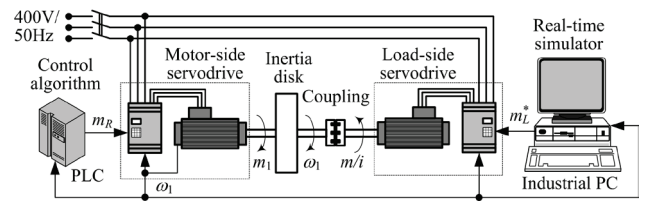


Figure 7 Principal schematic of down-scaled laboratory experimental setup

Table 2 Parameters of realistic drill-string system for rotational motion

Parameter	Value
Rated top-drive motor torque M_n	3200 Nm
Rated top-drive motor speed ω_n	187.5 rad/s
Overall motor torque lag T_Σ	4 ms
Gearbox ratio i	12.5
Top-drive motor-side inertia J_1	10 kgm ²
BHA-side inertia J_2	301.1 kgm ²
Drill-string stiffness coefficient k	618.3 Nm/rad
Drill-string damping coefficient c	15.3 Nms/rad
Drilling tool-side static friction torque M_S	4000 Nm
Drilling tool-side Coulomb torque M_C	2500 Nm
Stribeck speed ω_s	0.1 rad/s
Stribeck coefficient δ_s	1.0

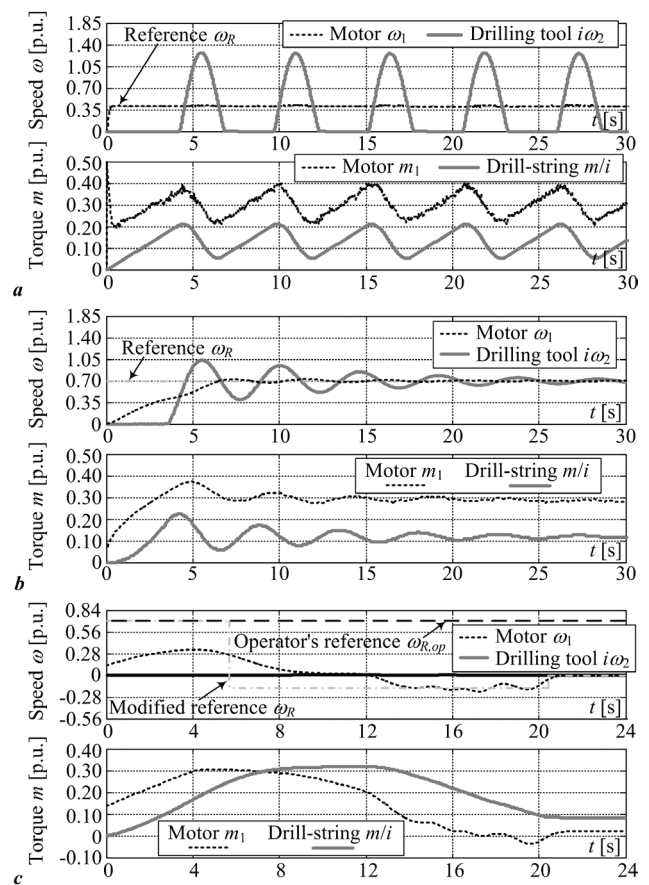
Table 3 Parameters of realistic drill-string system for longitudinal motion

Parameter	Value
Rated draw-works motor torque M_n	7920 Nm
Rated draw-works motor speed ω_n	101.5 rad/s
Draw-works drum inertia at motor side J_m	42 kgm ²
Motor speed control loop lag $T_{e\omega}$	16 ms
Gearbox ratio i_g	12.5
Drum radius r_d	0.381 m
Travelling block mass m_{hook}	11013 kg
Total mass at BHA side m_{tot}	74138 kg
Steel rope stiffness coefficient k_r	$2.16 \cdot 10^6$ N/m
Steel rope damping coefficient c_r	100 Ns/m
Drill-string stiffness coefficient k_{ds}	$1.14 \cdot 10^5$ N/m
Drill-string damping coefficient c_{ds}	100 Ns/m
WoB measurement model gain K_f	1/9810 t/N
WoB measurement model time constant T_f	1 s

Fig. 8 shows the experimental results for the case of drill-string rotary speed control system. The benchmark results for the case of fast PI speed controller tuned according to Eqs. (17) and (18), and subject to drill-string compliance and variable drilling tool friction torque are shown in Fig. 8a. The fast PI controller is capable of maintaining the motor speed in the close vicinity of the target value regardless of the load caused by the drill-string compliance and drilling tool stick-slip friction resulting in notable limit-cycle oscillations of the drilling tool speed ω_2 and drill-string torque m (see Subsection 3.3). The relatively large bias between the motor torque and the drill-string torque is caused by the friction within the laboratory system transmission mechanism, with the Coulomb torque estimated to $M_{Cm} = 0.16$ per units. The aforementioned undesirable torsional vibrations are effectively damped by means of active damping PI speed controller tuned according to Eqs. (15) and (16), as illustrated in Fig. 8b. This consequently leads to rather favourable damping of both the motor-side and drilling tool-side vibration modes, and results in effective suppression of stick-slip motion effect. Fig. 8c shows the responses of the drill string speed control system in the case of stuck drilling tool with the back-spinning intervention turned on. The proposed back-spinning prevention scheme enables safe unwinding of the drill-string by internally applying a negative speed reference until a rather small (safe) torque value is reached. Once unwound, the rotary drilling drive may be commanded by a zero speed reference in order to keep it at standstill.

Fig. 9 shows the WoB control system responses for different operating conditions. Figure 9a shows the WoB reference step responses ($WoB_R = 8$ t) for the case of drilling tool penetration resistance coefficient $c_t = 10^7$ Ns/m and WoB PI controller tuned for step response without overshoot ($T_{enob} = 36$ s and $D_{2w} = 0.25$). The draw-works drive rotational speed ω_w is characterized by a notable initial drop, which is requested by the superimposed WoB controller in order to develop the requested WoB . This, in turn, compresses the drill-string in the longitudinal direction during the WoB transient phase, which is characterized by zero overshoot. Once the steady-state WoB value of 8 t is achieved, constant drilling tool penetration rate (draw-works drive speed ω_w) is maintained by the draw-works drive under the steady-state command from the WoB controller. In the case when the drilling tool encounters a rock formation characterized by different penetration resistance (Figs. 9b and 9c), WoB controller

adjusts the draw-works drive speed ω_w in order to achieve the desired WoB value. In the case of drilling tool penetration resistance decrease from $c_t = 10^7$ Ns/m to $c_t = 3 \cdot 10^6$ Nm/s (Fig. 9b), the WoB controller output becomes saturated, because the drive speed reference is limited to $\omega_{max} = 4$ rad/s in order to avoid possibly hazardous fast unwinding of the steel rope from the drum. Hence, the WoB control system is characterized by steady-state WoB control error of approximately 1.5 t in this scenario. Figure 9c shows that when encountering a "harder" rock formation (c_t increases from 10^7 Ns/m to $2 \cdot 10^7$ Nm/s), the controller needs to effectively decrease the drive speed ω_w . In particular, the controller quite effectively suppresses the resulting WoB excursion due to increased penetration resistance, i.e. only 6% overshoot occurs with respect to the WoB target value.


Figure 8 Experimental responses of drill-string speed control system without active damping (a), with active damping (b), and for stuck tool case with back-spinning prevention turned on (c)

5 CONCLUSION

The paper has presented the results of petroleum drilling drill-string modelling and control system design for rotary and longitudinal motion aimed at mature petroleum drilling rig retrofitting. In particular, the rotary drive active damping speed control system and the draw-works hoist-based Weight-on-Bit (WoB) control system have been based on proportional-integral controllers. The controller tuning has been based on the simplified linear control-oriented process models and damping optimum criterion, resulting in straightforward expressions between

controller parameters, process model parameters and damping tuning parameters (i.e. characteristic ratios).

The presented drilling control systems have been verified on a downscaled laboratory experimental setup. The active damping rotary speed control system has been able to effectively suppress the torsional vibrations due to drilling tool stick-slip effect. Moreover, the proposed back-spinning prevention scheme accurately detects the stuck drilling tool condition and safely unwinds the drill-string under the proposed speed control scheme. The proposed *WoB* control system has been able to achieve well-damped closed-loop *WoB* response under different drilling conditions. This is particularly emphasized in the case of the drilling tool suddenly encountering "softer" or "harder" rock formations. In the former case, the target penetration rate has been limited in order to avoid potentially hazardous fast unwinding of the steel rope from the draw-works drum, while in the latter case the penetration rate has been decreased in order to quickly suppress the *WoB* excursion from the target value.

The main advantages of the proposed control system design methodology are: (i) utilization of modular cascade control system structure, (ii) realization by means of well-established proportional-integral (PI) control laws for both control tasks, and (iii) simplicity of the controller design based on suitably-chosen control-oriented process models and damping optimum criterion. These features are in fact desirable, because they do not require significant modifications of the existing control platforms.

Future work is going to be directed towards detailed testing of the proposed control systems in the field. Additional research efforts may also include different aspects of drilling process modelling and control related to directional drilling and well-bore interaction.

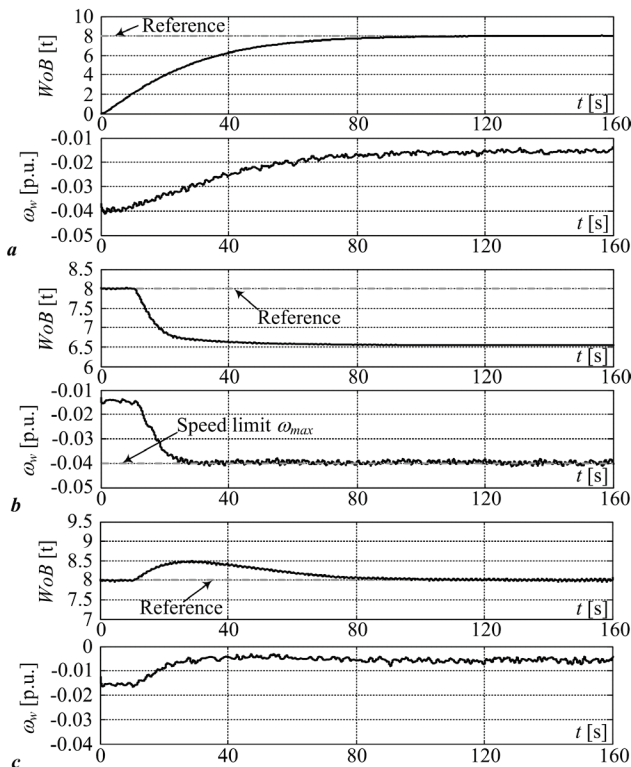


Figure 9 Experimental responses of drill-string *WoB* control system for constant penetration resistance (a), penetration resistance decrease (b), and penetration resistance increase (c)

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Nomenclature

Abbreviations

BHA	Bottom-hole assembly
HWDP	Heavy-weight drill-pipes
H_∞	H-infinity robust controller design
IM	Induction machine
LQR	Linear quadratic regulator
PI	Proportional-integral (controller)
<i>RoP</i>	Rate-of-Penetration

Variables

F_b, F_t	Buoyancy and tool penetration force
F_r, F_{ds}	Steel rope force and drill-string dilatation force
m_1, m	Rotary drive motor torque, drill-string torque
m_{f1}, m_{f2}	Rotary drive motor and BHAside friction torque
$M_{m,op}$	Operator's torque limit for rotary drive
M_{max}	Modified torque limit for rotary drive
v_B, v_r	BHA and steel rope longitudinal speed, respectively
<i>WoB</i>	Weight-on-Bit (measurement)
WoB_R	<i>WoB</i> reference (target) value
$\Delta v_r, \Delta x_r$	Steel rope dilatation speed and dilatation
$\Delta v_d, \Delta x_d$	Drill-string dilatation speed and dilatation
$\Delta \omega, \Delta \alpha$	Rotary speed difference and torsional angle
$\omega_{R,op}$	Operator's speed target for rotary drive
ω_{Rr}	Modified speed target for rotary drive
ω_w, ω_{Rw}	Draw-works drive speed and reference value
ω_1, ω_2	Rotary drive motor speed and BHA-side speed
ω_{1s}	Constrained motion rotary drive speed

Parameters

c_t	Tool penetration resistance coefficient
D_2, \dots, D_n	Damping optimum characteristic ratios
g	Gravity (free-fall) acceleration
i, i_g	Rotary and draw-works drive transmission ratios
J_1, J_2	Rotary drive motor-side and BHA-side inertia
J_{tool}, J_c	Tool and collar inertia
J_{hw}, J_{dp}	HWDP and drill-pipe inertia
k, c	Drill-string torsional stiffness and damping
k_r, c_r	Steel rope longitudinal stiffness and damping
k_{ds}, c_{ds}	Drill-string longitudinal stiffness and damping
$K_{c\omega}, T_{c\omega}$	Rotary drive PI controller gain and time constant
K_{wob}, T_{wob}	<i>WoB</i> PI controller gain and time constant
K_{pw}, T_{pw}	Simplified model equivalent gain and time constant
m_h, m_B	Hook mass and BHA mass
M_C, M_S	Rotary drive BHA-side Coulomb and static friction
M_{Cm}	Rotary drive motor-side Coulomb friction
r_d	Draw-works drum radius
T_c	Damping optimum equivalent time constant
T_{ewob}	<i>WoB</i> control system equivalent time constant
T_f	<i>WoB</i> measurement time constant
T_Σ	Rotary drive torque lag
$T_{e\omega}$	Draw-works drive speed control loop lag
z	Pulley transmission ratio
δ, ω_s	Stiction coefficient and Stiction speed
$\Delta \omega$	Zero-speed region (Karnopp friction model)
Ω_0	Freely-oscillating resonance frequency
Ω_{01}	Motor-side resonance frequency
Ω_{02}	Tool-side resonance frequency
Ω_{0w}	Bandwidth of longitudinal dynamics model

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