

LLC RESONANT CONVERTER TOPOLOGIES FOR PLUG-IN ELECTRIC VEHICLE BATTERY CHARGING

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**LLC RESONANT CONVERTER TOPOLOGIES FOR PLUG-IN ELECTRIC
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by

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