



# Optimality-Based Non-Redfield Plankton-Ecosystem Model (OPEM v1.0) in the UVic-ESCM 2.9. Part II: Sensitivity Analysis and Model Calibration

Chia-Te Chien, Markus Pahlow, Markus Schartau, and Andreas Oschlies

GEOMAR Helmholtz Centre for Ocean Research Kiel

**Correspondence:** Chia-Te Chien (cchien@geomar.de)

## Abstract.

We analyse 400 perturbed-parameter simulations for two configurations of an optimality-based plankton-ecosystem model (OPEM), implemented in the University of Victoria Earth-System Climate Model (UVic-ESCM), using a Latin-Hypercube sampling method for setting up the parameter ensemble. A likelihood-based metric is introduced for model assessment and selection of the model solutions closest to observed distributions of  $\text{NO}_3^-$ ,  $\text{PO}_4^{3-}$ ,  $\text{O}_2$ , and surface chlorophyll *a* concentrations. According to our metric the optimal model solutions comprise low rates of global  $\text{N}_2$  fixation and denitrification. These two rate estimates turned out to be poorly constrained by the data. For identifying the “best” model solutions we therefore also consider the model’s ability to represent current estimates of water-column denitrification. We employ our ensemble of model solutions in a sensitivity analysis to gain insights into the importance and role of individual model parameters as well as correlations between various biogeochemical processes and tracers, such as POC export and the  $\text{NO}_3^-$  inventory. Global  $\text{O}_2$  varies by a factor of two and  $\text{NO}_3^-$  by more than a factor of six among all simulations. Remineralisation rate is the most important parameter for  $\text{O}_2$ , which is also affected by the subsistence N quota of ordinary phytoplankton ( $Q_{0,\text{phy}}^{\text{N}}$ ) and zooplankton maximum specific ingestion rate.  $Q_{0,\text{phy}}^{\text{N}}$  is revealed as a major determinant of the oceanic  $\text{NO}_3^-$  pool. This indicates that unraveling the driving forces of variations in phytoplankton physiology and elemental stoichiometry, which are tightly linked via  $Q_{0,\text{phy}}^{\text{N}}$ , is a prerequisite for understanding the marine nitrogen inventory.

## 1 Introduction

Earth system climate models (ESCMs) are powerful tools for analysing variations in climate, while resolving interdependencies between changes in the atmosphere, on land, and in the ocean (Flato, 2011; Prinn, 2013). In this regard, the dynamics of marine ecosystems is a critical link. On long timescales it regulates atmospheric  $\text{CO}_2$  on the basis of biotic uptake of carbon dioxide ( $\text{CO}_2$ ) over vast oceanic regions and due to the export of photosynthetically fixed carbon into the deep ocean, which affects the Earth’s climate (Reid et al., 2009; Sigman and Boyle, 2000). Plankton ecosystem models are widely applied to understand marine biogeochemical cycles, by estimating fluxes of major elements, e.g., nitrogen, phosphorus, and carbon, as well as the sources and sinks of marine oxygen (Maier-Reimer et al., 1995; Six and Maier-Reimer, 1996; Schmittner et al., 2005; Bopp et al., 2013; Vallina et al., 2017; Everett et al., 2017; Ward et al., 2018).



25 The basic structure of most marine ecosystem models has been designed for resolving mass fluxes between nutrients, phytoplankton, zooplankton and detritus, typically referred to as NPZD models. Mathematical formulations that describe growth and fate of marine phytoplankton and zooplankton biomass have been successfully applied over a range of scales, from local 0D-ecosystem models (e.g., Fasham et al., 1990; Edwards, 2001) to global 3D models (Sarmiento et al., 1993; Keller et al., 2012; Nickelsen et al., 2015). However, most of these NPZD models lack a sound mechanistic foundation, preventing them  
30 from explicitly accounting for the organisms' regulation of their internal physiological state. For example, N<sub>2</sub> fixation by algae is often diagnosed from the availability of dissolved nutrients, so that it only occurs when the ratio of nitrate-to-phosphate concentrations falls below the Redfield ratio of 16:1 (Deutsch et al., 2007; Ilyina et al., 2013). As these assumptions neglect a number of environmental and ecological controls (e.g., grazing, often also temperature), they do not adequately describe the behaviour of plankton organisms and their sensitivity to changes in their environment. With the introduction of refined  
35 mechanistic (physiological) descriptions we here aim at alleviating this deficiency. In this study we introduce a new marine ecosystem model coupled to the University of Victoria Earth System Climate Model (UVic-ESCM, based on the configurations of Keller et al., 2012; Getzlaff and Dietze, 2013; Nickelsen et al., 2015). Doing so we anticipate the model not only to provide improved mass flux estimates, but also to exhibit more realistic sensitivities of these fluxes to varying climate conditions, e.g., in simulations of the last glacial maximum or in future projections.

40 In order to better represent plankton physiology, the new ecosystem model relies on optimality-based considerations for phytoplankton growth, including N<sub>2</sub> fixation (Pahlow et al., 2013; Pahlow and Oschlies, 2013), as well as zooplankton behaviour (Pahlow and Prowe, 2010). These two optimality-based models have been shown to be superior to traditional model approaches in reproducing phytoplankton and zooplankton growth and grazing under various environmental conditions (e.g., Fernández-Castro et al., 2016). Our new ecosystem model, the optimality-based plankton ecosystem model (OPEM v1.0) coupled to the  
45 UVic-ESCM, offers new features and it improves the representation of some biogeochemical tracers on the global scale (see accompanying study, Pahlow et al. (2019)). One of the novel features is the representation of variable quotas of carbon (C), nitrogen (N), and phosphorus (P) in ordinary phytoplankton, diazotrophs, and particulate organic matter (detritus) exported to the deep ocean. This model approach yields mass flux estimates with spatial and temporal variations in the elemental C:N:P stoichiometry of both inorganic nutrients and organic matter.

50 Here we analyse the model's performance and evaluate model-ensemble results against observations. Since the model is based on plankton physiology, it includes new parameters whose values have not been estimated for global model applications. Also, we set up two configurations, OPEM and OPEM-H, with different temperature dependences for diazotrophs to investigate the effects of different temperature functions on distributions of diazotrophs and N<sub>2</sub> fixation. Our analysis relies on ensembles of solutions of the two different model configurations, where every single simulation within each ensemble is subject to a  
55 different combination of parameter values. The ensembles allow assessing the sensitivity of biogeochemical tracer distributions and budgets to variations of the model's parameters. We introduce a likelihood-based metric that quantifies the global misfit between model results and observations. Amongst the ensemble simulations we regard those model solutions as the best that yield low misfits according to the metric and are also close to current estimates of water-column denitrification. The specific objectives of the present paper are (1) to identify and compare those model solutions that correspond to the best representation



60 of observed tracer concentrations and (2) to specify the sensitivity of simulations to variations of the model's parameter values. We make inferences about the model's overall behavior, especially focusing on data constraints, limitations and advantages of resolving variable C:N:P stoichiometry for estimations of global net primary production (NPP), net community production (NCP), biogenic C export, and the global O<sub>2</sub>, N, and C inventories.

## 2 Materials and Methods

### 65 2.1 The non-Redfield, optimality-based plankton ecosystem model in the UVic-ESCM

The optimality-based plankton ecosystem model (OPEM) has been implemented into the UVic-ESCM (Weaver et al., 2001; Eby et al., 2013), version 2.9, in the configuration of Nickelsen et al. (2015) with the isopycnal diffusivity modifications by Getzlaff and Dietze (2013), vertically increasing sinking velocity of detritus (Kriest, 2017), and several bug-fixes (some of which were already introduced by Kvale et al., 2017). The UVic-ESCM comprises three components including a simple one-  
70 layer atmospheric energy-moisture balance model (Weaver et al., 2001), a terrestrial model and a three-dimensional general ocean circulation model. The horizontal resolution of the land and ocean model components is 1.8° latitude × 3.6° longitude, and the ocean has 19 vertical levels with a thickness ranging from 50 m in the surface layer to 590 m in the deep ocean.

The OPEM and its implementation into the UVic-ESCM, are described in the companion paper (Pahlow et al., 2019). Briefly, the major new features of the new model include (1) an optimality-based model of phytoplankton growth and diazotrophy with  
75 variable C:N:P stoichiometry (Pahlow et al., 2013), (2) the optimal current-feeding model for zooplankton (Pahlow and Prowe, 2010), and (3) variable stoichiometry in detritus. The focus on physiology in the construction of the OPEM enables us to study how biogeochemical tracer distributions and fluxes respond to different assumptions about plankton physiology.

#### 2.1.1 Simulation setup

Our setup comprises ensembles of 400 simulations for each of two model configurations. The two model configurations differ  
80 in how temperature affects diazotrophy. The original temperature dependence of diazotrophs ( $f_{\text{dia}}(T)$ ) in the UVic-ESCM (and other models, e.g., Aumont et al., 2015), which we also employ for the OPEM configuration, limits both growth and N<sub>2</sub> fixation of diazotrophs to above 15 °C,

$$f_{\text{dia}}(T)_{\text{OPEM}} = \max(1.066^T - 2.6, 0)/2 \quad (1)$$

where  $T$  is seawater temperature. In the OPEM-H configuration, the temperature dependence of nitrogenase activity in terres-  
85 trial systems by Houlton et al. (2008) is implemented as affecting only N<sub>2</sub> fixation,

$$f_{\text{dia}}(T)_{\text{OPEM-H}} = 0.0266 * (1.066^T)^{(4.22 - 1.3166 * \ln(1.066^T))} \quad (2)$$

while growth and nutrient uptake of diazotrophs follow the same temperature dependence as ordinary phytoplankton (see Pahlow et al. (2019)). Note that some models do not enforce any temperature limitation on nitrogen fixation (e.g., Dunne et al.,



2012; Ilyina et al., 2013; Jickells et al., 2017). In the present ocean, waters colder than about 15 °C are generally replete with  
90 fixed inorganic nitrogen. For existing parameterisations of N<sub>2</sub> fixation, which are functions of the nitrate deficit with respect to  
phosphate, there has been little indication of substantial impacts of the formulation of temperature control at low temperatures  
on the distribution of nitrogen fixation (Somes and Oschlies, 2015; Landolfi et al., 2017). Such differences in formulation may,  
however, gain importance in environmental conditions different from today's.

For all simulations we impose preindustrial (A.D. 1850) boundary conditions with a CO<sub>2</sub> concentration of 284 ppm. The  
95 models have been integrated over a period of at least 10,000 years, until they reached steady-state.

The 400 parameter combinations are obtained via Latin Hypercube Sampling (LHS) (McKay et al., 1979). We vary 15  
parameters in total, within the ranges shown in Table 1. In order to reduce the number of possible parameter combinations, we  
vary nutrient affinities for macronutrient uptake and half-saturation concentration for iron uptake for ordinary phytoplankton  
and diazotrophs in constant proportions ( $A_0 : A_{0,D} = 4 : 3$ ,  $K_{Fe} : K_{Fe,D} = 1 : 2$ ), so that diazotrophs have a lower nutrient  
100 affinity (Pahlow et al., 2013) and higher Fe half-saturation concentration (Dutkiewicz et al., 2012; McGillicuddy Jr., 2014;  
Ward et al., 2013) than ordinary phytoplankton. Since our parameter sets are independent of each other, the simulations can be  
carried out in parallel. Apart from the computational time, the parallel setup with different parameter combinations has a some  
advantages compared to systematic (often iterative) model calibration approaches, e.g., parameter-optimisation: (i) Individual  
model simulations do not depend on any other (i.e. previous) combinations of parameter values, (ii) the ensemble results can  
105 always be re-evaluated with different metrics, perhaps with substantial differences between selected “best” solutions, depending  
on the error model applied, and (iii) the ensembles provide insight to the sensitivities and thus to uncertainties of particular  
model results with respect to parameter variations.

## 2.2 Sensitivity Analysis and Model Calibration

### 2.2.1 Sensitivity analysis

110 The sensitivity ( $Sensitivity_T$ ) of a tracer  $T$  to a parameter  $P$  is defined here as

$$Sensitivity_T = \frac{\Delta T}{\Delta P} \times \frac{\bar{P}}{\bar{T}} \quad (3)$$

where the  $\Delta$  indicates the change and the overbar the mean of  $P$  or  $T$ . If  $Sensitivity_T < 0$ , the tracer and the parameter  
vary in opposite directions. We evaluate the sensitivities of globally and annually averaged net primary production (NPP), net  
community production (NCP), particulate organic carbon (POC) export, nitrogen fixation by diazotrophs (N<sub>2</sub> fixation), and  
115 the concentrations of oxygen (O<sub>2</sub>), nitrate (NO<sub>3</sub><sup>-</sup>), DIC, POC, dissolved and particulate iron (DFe and PFe), Chl, ordinary  
phytoplankton, diazotrophs, particles (ordinary phytoplankton + diazotrophs + zooplankton + detritus) and their elemental  
stoichiometry to the parameters listed in Table 1.



**Table 1.** Parameter names, ranges, identified “best” values for trade-off simulations in OPEM and OPEM-H, units and descriptions.

Symbol	Range	OPEM/OPEM-H	Units	Definition
$A_{0, \text{phy}}$	120–280	229	$\text{m}^3 (\text{mol C})^{-1} \text{d}^{-1}$	phytoplankton potential nutrient affinity
$Q_{0, \text{phy}}^{\text{N}}$	0.04–0.06	0.04128	$\text{mol} (\text{mol C})^{-1}$	phytoplankton subsistence N quota
$Q_{0, \text{dia}}^{\text{N}}$	0.06–0.12	0.067	$\text{mol} (\text{mol C})^{-1}$	diazotroph subsistence N quota
$Q_{0, \text{phy}}^{\text{P}}$	0.0013–0.0023	0.0022	$\text{mol} (\text{mol C})^{-1}$	phytoplankton subsistence P quota
$Q_{0, \text{dia}}^{\text{P}}$	0.0025–0.0035	0.00271	$\text{mol} (\text{mol C})^{-1}$	diazotroph subsistence P quota
$k_{\text{Fe}, \text{phy}}$	0.04–0.08	0.066	$\mu\text{mol m}^{-3}$	phytoplankton half-saturation constant for Fe
$g_{\text{max}}$	1–2	1.75	$\text{d}^{-1}$	zooplankton maximum specific ingestion rate
$\phi_{\text{phy}}$	100–200	118	$\text{m}^3 (\text{mol C})^{-1}$	capture coefficient of phytoplankton
$\phi_{\text{dia}}$	150–250	232	$\text{m}^3 (\text{mol C})^{-1}$	capture coefficient of diazotrophs
$\phi_{\text{det}}$	20–100	94	$\text{m}^3 (\text{mol C})^{-1}$	capture coefficient of detritus
$\phi_{\text{zoo}}$	100–200	118	$\text{m}^3 (\text{mol C})^{-1}$	capture coefficient of zooplankton
$\lambda_{0, \text{phy}} = M_{0, \text{dia}}$	0.01–0.03	0.018	$\text{d}^{-1}$	specific mortality rate
$\nu_{\text{det}}$	0.04–0.09	0.087	$\text{d}^{-1}$	rem mineralization rate

## 2.2.2 Likelihood-based metric assessing global biogeochemical model results

We consider four different types of observations for quantitatively assessing the model simulations. The first three are the objectively analysed monthly (upper 550 m) and annual (below 550 m) concentrations of nitrate, phosphate, and oxygen of the World Ocean Atlas 2013 (WOA 2013, Garcia et al., 2013a, b). The fourth is the monthly mean chlorophyll concentration derived from remote sensing data (MODIS/Aqua level 3), based on monthly climatologies for 10 years from 2008 to 2017, provided by the ocean biology processing group (Ocean Biology Processing Group, 2014). The satellite-derived chlorophyll (Chl) concentrations are used for data-model comparison only for the UVic model’s top layer, i.e. the upper 50 m.

We define our metric in terms of spatial averages of 17 distinct biogeochemical biomes, as derived and described by Fay and McKinley (2014). The individual biomes are regarded as regions of common biogeochemistry and thus account for spatial differences between ocean regions on the largest possible (global) scale. Using 56 biogeochemical provinces, as defined by Longhurst (2007), might have hampered our data-model comparison, because a higher resolution of individual regions can accentuate spatial pattern errors in tracer concentrations, resulting from differences in advection and mixing. In our view the biomes of Fay and McKinley (2014) are coarse enough for avoiding this problem, but still sufficiently informative for identifying representative parameter values.

For every depth-level of the UVic model ( $k \in \{1, 2, 3, \dots, 19\}$ ), average log-transformed tracer concentrations ( $\overline{\ln X}$ ) of type X are determined as spatial arithmetic means for our 17 biomes (indexed as  $j$  in Eq. 4) for the observations and model results:

$$(\overline{\ln X})_{jk} = \frac{1}{N_{jk}} \sum_{n=1}^{N_{jk}} \left( \ln \left[ \frac{\max(X_{(n)}, X_{(0)})}{X_{(0)}} \right] \right), \quad X \in \{\text{Chl}, \text{O}_2, \text{NO}_3^-, \text{PO}_4^{3-}\} \quad (4)$$



135 where  $N_{jk}$  is the number of available data points within biome  $j$  in depth level  $k$ . Prior to log-transformation, all tracer concentrations have been normalised to lower detection (uncertainty) thresholds ( $X_{(0)}$ ) respectively. Measured or derived concentrations below these thresholds are treated as noise and therefore remain unresolved. Thus, the log-transformed normalised concentrations are non-negative. The threshold-values are:  $\text{Chl}_{(0)} = 0.1 \text{ mg m}^{-3}$ ,  $\text{O}_2_{(0)} = 1 \text{ mmol m}^{-3}$ ,  $\text{NO}_3^-_{(0)} = 0.05 \text{ mmol m}^{-3}$ , and  $\text{PO}_4^{3-}_{(0)} = 0.01 \text{ mmol m}^{-3}$ .

140 Our metric is derived from a likelihood, assuming a Gaussian error distribution for the residuals, which describe the discrepancy between mean values derived from observations ( $\overline{\ln X^{(\text{obs})}}$ ) and model simulations ( $\overline{\ln X^{(\text{mod})}}$ ). Hereafter we refer to this metric as our cost function ( $J$ ). Our cost function is split up into two major parts:

$$J = \sum_{k=1}^5 J_k^{(u)} + \sum_{k=6}^{19} J_k^{(l)} \quad (5)$$

$$J_k^{(u)} = \sum_{i=1}^{12} \sum_{j=1}^{17} [\mathbf{d}^T R^{-1} \mathbf{d}]_{ijk} + \left( \mathbf{v}^{(\text{obs})} - \mathbf{v}^{(\text{mod})} \right)_{ijk}^T V_{ijk}^{-1} \left( \mathbf{v}^{(\text{obs})} - \mathbf{v}^{(\text{mod})} \right)_{ijk} \quad (6)$$

145  $J_k^{(l)} = \sum_{j=1}^{17} [\mathbf{d}^T R^{-1} \mathbf{d}]_{jk} + \left( \mathbf{v}^{(\text{obs})} - \mathbf{v}^{(\text{mod})} \right)_{jk}^T V_{jk}^{-1} \left( \mathbf{v}^{(\text{obs})} - \mathbf{v}^{(\text{mod})} \right)_{jk} \quad (7)$

where  $\mathbf{d}$  is the residual vector (see Eq. (8) below),  $R$  the covariance matrix (Eq. 9),  $\mathbf{v}^{(\text{obs})}$  and  $\mathbf{v}^{(\text{mod})}$  the spatial variance estimates of the observed and modelled tracers, and  $V^{-1}$  are diagonal matrices with the variances (uncertainties) of  $\mathbf{v}^{(\text{obs})}$ . The first part ( $J_k^{(u)}$ ) of the cost function resolves seasonal changes between the surface and 550 m depth, corresponding to the upper five depth-levels of the model. The second part ( $J_k^{(l)}$ ) represents the lower depth range below 550 m and does not account for  
 150 seasonal changes, as only annual mean data are available.

The residual vector ( $\mathbf{d}$ ) (whose components represent the tracer types  $X$ ) used for  $J$  describes the differences between the log-transformed observations and their model counterparts:

$$\mathbf{d}_{ijk} = \left( \overline{\ln X_{ijk}^{(\text{obs})}} - \overline{\ln X_{ijk}^{(\text{mod})}} \right) \quad (8)$$

where  $i$  and  $j$  are the month and biome indices, respectively. We recall that  $\mathbf{d}$  has four components only for the UVic model's  
 155 top layer ( $k = 1$ ) where chlorophyll data are regarded as well. For  $k > 1$  the residual vector contains three components:  $\text{O}_2$ ,  $\text{NO}_3^-$ , and  $\text{PO}_4^{3-}$ . Both parts of the cost function ( $J_k^{(u)}$  and  $J_k^{(l)}$ ) in turn contain two terms, one with respect to the residuals, as defined in Eq. (8), and another that accounts for the differences between the spatial variances (vectors  $\mathbf{v}_{ijk}^{(\text{obs})}$  and  $\mathbf{v}_{ijk}^{(\text{mod})}$ ) within each biome (and month for  $J_k^{(u)}$ ) at each depth-level. The covariance matrices  $R_{ijk}$  account for temporal correlations ( $C_{jk}$ ) between different variables ( $X^{(\text{obs})}$ ), that are specified for every biome and depth level separately:

160  $R_{ijk} = S_{ijk} \cdot C_{jk} \cdot S_{ijk} \quad (9)$

where the elements of the diagonal matrices  $S_{ijk}$  are the standard errors of the mean log-transformed tracer concentrations ( $\overline{\ln X_{ijk}^{(\text{obs})}}$ ) calculated in Eq. (4) for every month  $i$ , biome  $j$ , and depth level  $k$ . For  $J_k^{(l)}$  the  $R_{jk}$  contain only the squared standard errors of the annual data as diagonal elements ( $R_{jk} = S_{jk}^2$ ).



165 With the consideration of standard errors instead of standard deviations, we implicitly impose weights to differences in  
the spatial expansion (i.e. number of data points of the gridded product used) of individual biomes. Overall, the final cost  
function  $J$  resolves spatial differences between regions (biomes) as well as temporal differences for those depth levels where  
monthly data are available. It is thus a trade-off in combining time-varying and spatial information for the assessment of our  
biogeochemical model results on a global scale.

### 3 Results

170 Table 2 lists the ranges of selected simulated tracers and processes for the full ensemble of parameter values generated by  
the Latin Hypercube Sampling for the OPEM and OPEM-H configurations. Our results exhibit wide ranges of tracer con-  
centrations and fluxes in these two configurations. In particular, globally-averaged  $\text{NO}_3^-$  concentrations range from 10.2 to  
66.2  $\text{mmol m}^{-3}$  and integrated  $\text{N}_2$  fixation from 0 to 518  $\text{Tg N yr}^{-1}$ . Tracers in OPEM and OPEM-H show similar ranges,  
except for globally averaged  $\text{NO}_3^-$ , which ranges from 10.2 to 66.2  $\text{mmol m}^{-3}$  in OPEM and 13.0 to 55.0  $\text{mmol m}^{-3}$  in  
175 OPEM-H.

**Table 2.** Ranges of global averages of major tracer concentrations or fluxes in the OPEM and OPEM-H configurations. Chl concentrations  
are depth integrated.

Tracer	OPEM	OPEM-H	Units
Oxygen	99.6–219	103–214	$\text{mmol m}^{-3}$
Nitrate	10.2–66.2	13.0–55.0	$\text{mmol m}^{-3}$
DIC	2.239–2.439	2.248–2.430	$\text{mol m}^{-3}$
DFe	0.47–0.71	0.47–0.69	$\mu\text{mol m}^{-3}$
PFe	0.44–0.75	0.44–0.70	$\text{nmol m}^{-3}$
Chl	37.6–101.2	38.0–103.5	$\text{mg m}^{-2}$
NPP	27.8–88.0	27.2–88.0	$\text{Pg C yr}^{-1}$
NCP	0.86–3.01	0.79–3.20	$\text{Pg C yr}^{-1}$
POC Export	0.66–3.01	0.68–3.08	$\text{Pg C yr}^{-1}$
$\text{N}_2$ Fixation	0–480	0–518	$\text{Tg N yr}^{-1}$

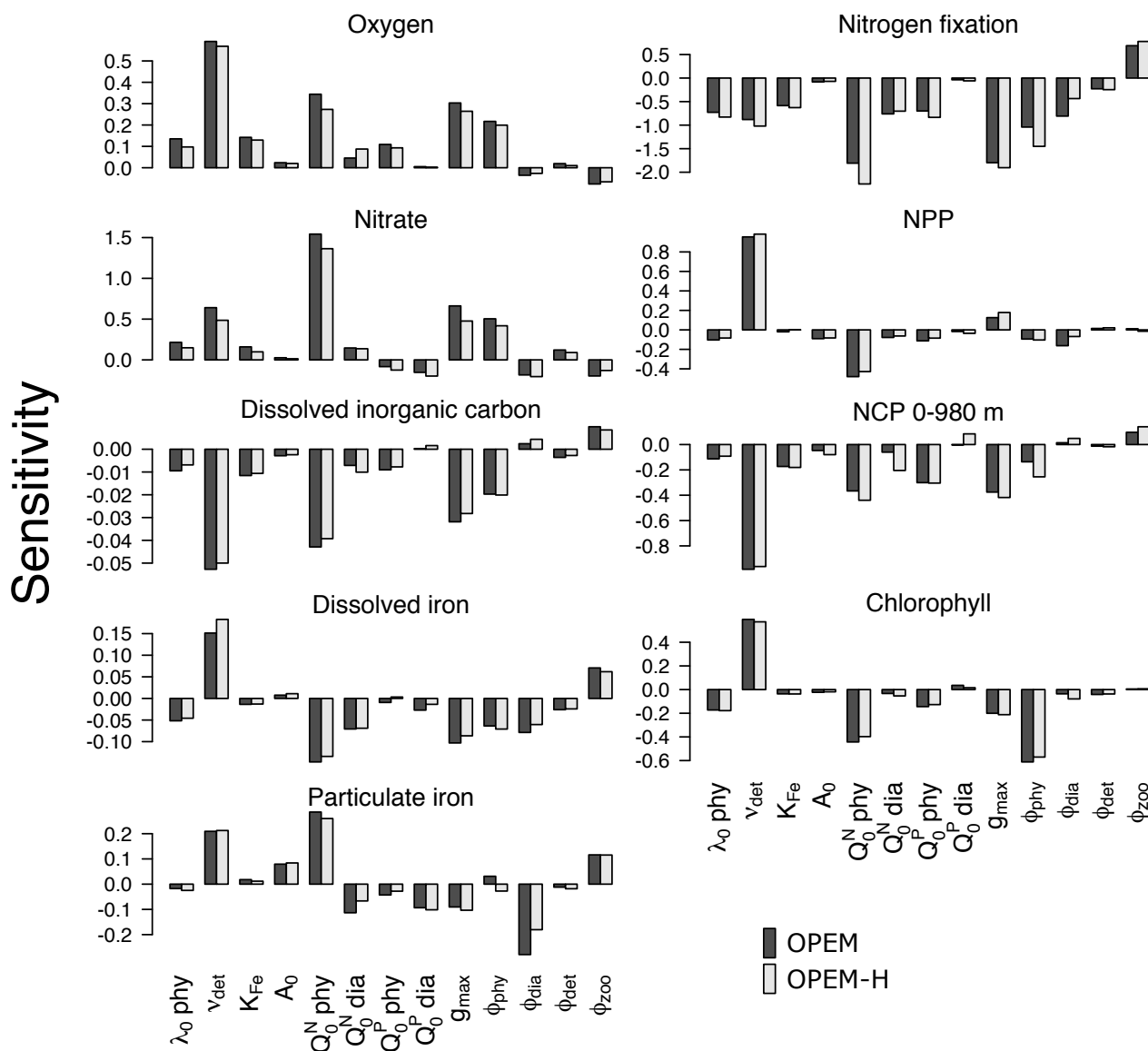
### 3.1 Sensitivity to Model Parameters

#### 3.1.1 Biogeochemical tracer inventories and governing processes

The sensitivities of globally averaged biogeochemical properties to the variations of each of the 13 parameters in Table 2 are  
comparable for OPEM and OPEM-H (Figure 1). Global mean oxygen concentration is most sensitive to  $\nu_{\text{det}}$  (remineralization  
180 rate). Higher  $\nu_{\text{det}}$  increases oxygen consumption in shallow water, where oxygen resupply from the atmosphere is stronger. Less



oxygen is consumed below the surface ocean, hence the total oxygen inventory increases. Maximum ingestion rate ( $g_{\max}$ ) and grazing rate on ordinary phytoplankton ( $\phi_{\text{phy}}$ ) also correlate positively with oxygen. Higher  $g_{\max}$  or  $\phi_{\text{phy}}$  means more ordinary phytoplankton is grazed and less particles are formed, which then decreases oxygen consumption through remineralization. Oxygen is less sensitive to  $\phi_{\text{dia}}$ , because the biomass of diazotrophs is much smaller than that of ordinary phytoplankton.



**Figure 1.** Sensitivities of globally averaged  $\text{O}_2$ ,  $\text{NO}_3^-$ , dissolved inorganic carbon, dissolved iron, particulate iron,  $\text{N}_2$  fixation, net primary production (NPP), Chlorophyll, and net community production (NCP) integrated from 0 to 980 m to individual model parameters, computed according to Eq. (3). Note the different vertical scales in the different panels.





185 A surprising finding is that oxygen is sensitive to, and positively correlated with, the subsistence nitrogen quota of ordinary phytoplankton ( $Q_{0, \text{phy}}^{\text{N}}$ ). From a classic point of view, oxygen levels in the ocean are dominated by physical supply processes as well as biogeochemical consumption processes such as remineralization (Feely et al., 2004). Nevertheless, in our simulations the sensitivity to  $Q_{0, \text{phy}}^{\text{N}}$  is more than half (58%) of that to  $\nu_{\text{det}}$  in OPEM and 48% in OPEM-H (Figure 1). In our model,  $Q_{0, \text{phy}}^{\text{N}}$  has no effect on the spatial distribution of cellular C:N ratios in phytoplankton, which is determined by ambient light and nutrient conditions. However,  $Q_{0, \text{phy}}^{\text{N}}$  affects the average phytoplankton C:N ratio. The average phytoplankton C:N ratio decreases  
190 when  $Q_{0, \text{phy}}^{\text{N}}$  increases, with less carbon being fixed for the same  $\text{NO}_3^-$  supply. Oxygen consumption (due to remineralization) per mole of nitrogen thus decreases in consequence.  $Q_{0, \text{phy}}^{\text{N}}$  in turn affects  $\text{NO}_3^-$ : A higher  $Q_{0, \text{phy}}^{\text{N}}$  yields a higher oxygen level and hence less denitrification in oxygen deficient zones (ODZs) and therefore leads to more  $\text{NO}_3^-$ . In fact, we identify this as a major process that controls the  $\text{NO}_3^-$  inventory in our simulations (Figure 1). While  $\text{NO}_3^-$  is also sensitive to other parameters,  
195 its sensitivity to  $Q_{0, \text{phy}}^{\text{N}}$  is more than twice that to any other parameter (Figure 1).

The sensitivity of dissolved inorganic carbon (DIC) is generally low, because of the relatively large DIC pool compared to the variations in fluxes among the different parameter sets. Similar to oxygen, DIC is most sensitive to  $\nu_{\text{det}}$ ,  $Q_{0, \text{phy}}^{\text{N}}$ ,  $g_{\text{max}}$  and  $\phi_{\text{phy}}$ . Faster carbon recycling in the surface layer due to higher  $\nu_{\text{det}}$  generates a higher surface DIC concentration and hence more outgassing, which decreases the DIC inventory. A somewhat lower DIC inventory is also induced by a larger  $Q_{0, \text{phy}}^{\text{N}}$ , as  
200 less carbon is fixed and exported per unit nitrogen in phytoplankton, and by enhanced zooplankton grazing with larger  $g_{\text{max}}$ .

Dissolved iron (DFe) is most sensitive to the remineralisation rate ( $\nu_{\text{det}}$ ). Unlike  $\text{NO}_3^-$ , which has dynamic source ( $\text{N}_2$  fixation) and sink (denitrification) processes, iron has a fixed source from atmospheric deposition and the size of the DFe pool is mainly determined by its internal cycle. A higher remineralisation rate prolongs the residence time and thus increases the DFe pool. The parameter  $\nu_{\text{det}}$  also indirectly affects the internal DFe cycle via its effect on  $\text{O}_2$ . While the detritus remineralisation  
205 rate drops when  $\text{O}_2$  falls below  $5 \text{ mmol m}^{-3}$  (Nickelsen et al., 2015), scavenging of DFe stops below the same oxygen threshold. Detritus remineralisation rate dominates variations in DFe when globally averaged  $\text{O}_2$  is above  $135 \text{ mmol m}^{-3}$ , in which case DFe is positively correlated with  $\nu_{\text{det}}$  and  $\text{O}_2$ . When globally averaged  $\text{O}_2$  is below  $135 \text{ mmol m}^{-3}$ , the wide-spread ODZs (below  $5 \text{ mmol m}^{-3}$ ) inhibit the scavenging of DFe and this effect dominates. As a result, DFe becomes anti-correlated with  $\text{O}_2$ . Particulate iron (PFe) is also positively correlated with  $\nu_{\text{det}}$  when globally averaged  $\text{O}_2$  is above  $135 \text{ mmol m}^{-3}$ , but below  
210 that PFe shows no correlation with  $\nu_{\text{det}}$ . When globally averaged  $\text{O}_2$  is below  $135 \text{ mmol m}^{-3}$ , inhibition of scavenging of DFe in ODZs decreases PFe there but a higher DFe increases PFe elsewhere, because PFe is coupled to DFe through scavenging and remineralisation. As mentioned above,  $Q_{0, \text{phy}}^{\text{N}}$  controls the average nitrogen quota in phytoplankton and thus in particles. Since PFe is proportional to the amount of nitrogen in particles,  $Q_{0, \text{phy}}^{\text{N}}$  also affects PFe. This (positive) sensitivity is much stronger than the indirect (negative) effect via DFe leading to opposite sensitivities of DFe and PFe to  $Q_{0, \text{phy}}^{\text{N}}$ . Other than  $\nu_{\text{det}}$   
215 and  $Q_{0, \text{phy}}^{\text{N}}$ , PFe is also sensitive to  $\phi_{\text{dia}}$  because dead diazotrophs enter the particulate pool (detritus) and diazotrophs are very sensitive to  $\phi_{\text{dia}}$  (Figure 2).

No single parameter dominates the sensitivity of  $\text{N}_2$  fixation in the simulations (Figure 1), which resembles the result of Tang et al. (2019) that no single environmental property predicts global  $\text{N}_2$  fixation, even with a data-based machine-learning method. Interestingly, other than  $\nu_{\text{det}}$  and  $Q_{0, \text{phy}}^{\text{N}}$ ,  $\text{N}_2$  fixation is also sensitive to zooplankton parameters, indicating that zooplankton



220 grazing on diazotrophs is an important factor controlling not just diazotroph biomass but also  $N_2$  fixation. Compared to  $Q_{0, \text{phy}}^N$ ,  $g_{\text{max}}$ ,  $\phi_{\text{zoo}}$  and  $\nu_{\text{det}}$ ,  $N_2$  fixation is not very sensitive to the iron half-saturation constant  $k_{\text{Fe, phy}}$ , probably because iron limitation occurs mainly in regions where relatively high nitrate concentrations impede  $N_2$  fixation anyway.

Of particular interest are the sensitivities of global net primary production (NPP) and net community production (NCP). Particle fluxes in marine biogeochemical models tend to agree most closely with sediment trap data for depths of about 1000 m  
225 or below (Kriest et al., 2012). Therefore, we integrate NCP from 0 to 980 m (7<sup>th</sup> layer of the ocean in the UVic-ESCM), which in steady state is equivalent to POC export flux at 980 m. NPP is sensitive to  $\nu_{\text{det}}$  and  $Q_{0, \text{phy}}^N$ . A higher  $\nu_{\text{det}}$  causes faster nutrient recycling in surface waters, which increases NPP and reduces particle export and hence NCP. Increasing  $Q_{0, \text{phy}}^N$  lowers both NPP and NCP and hence also the fixed-carbon inventory. A higher ingestion rate of zooplankton ( $g_{\text{max}}$ ) removes more particles and thus is negatively correlated with NCP. Chl is the principal agent of C fixation in the OPEM and hence Chl has a similar  
230 sensitivity pattern as NPP except for  $g_{\text{max}}$  and  $\phi_{\text{phy}}$ .

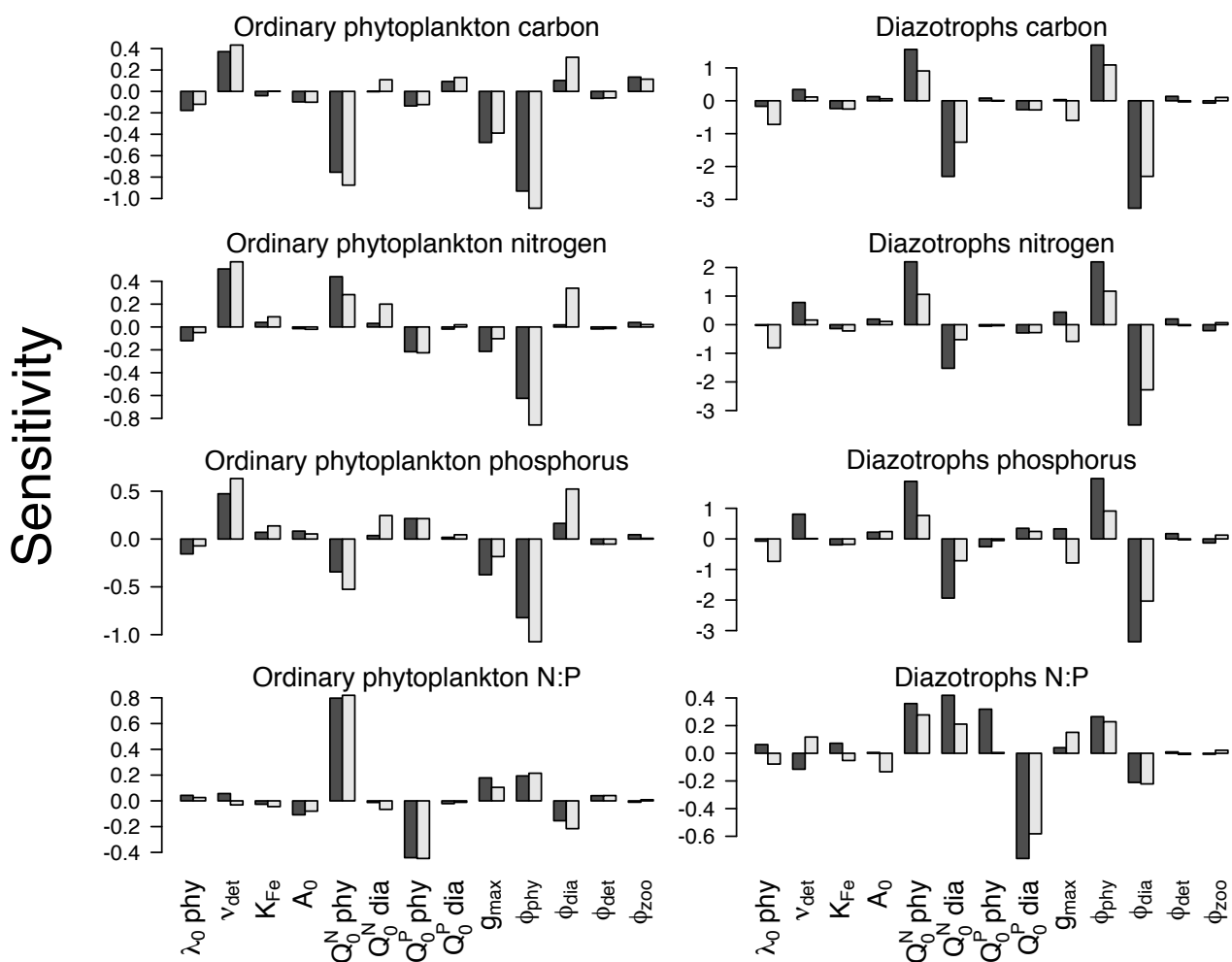
### 3.1.2 Ordinary phytoplankton, diazotrophs, particles, export and their elemental stoichiometry

First we discuss the proportions of carbon, nitrogen and phosphorus in ordinary phytoplankton and diazotrophs, since variations in elemental stoichiometry in autotrophs originate in differential uptake of nutrients under different environmental conditions.

Globally averaged C, N, P concentrations and ratios of globally averaged N and P of ordinary phytoplankton and diazotrophs  
235 are sensitive to  $\nu_{\text{det}}$ ,  $Q_{0, \text{phy}}^N$ ,  $\phi_{\text{phy}}$  and  $\phi_{\text{dia}}$  (Figure 2). As expected, C, N and P of ordinary phytoplankton and diazotrophs increase for higher  $\nu_{\text{det}}$ , which generates higher nutrient concentrations in the surface ocean. They are also sensitive to zooplankton grazing, especially to  $\phi_{\text{phy}}$  and  $\phi_{\text{dia}}$ .  $Q_{0, \text{phy}}^N$  and  $Q_{0, \text{phy}}^P$  are negatively correlated with ordinary phytoplankton C, indicating that the negative effect of higher subsistence quotas on competitive ability dominates their effect on biomass. A similar behavior is found in diazotrophs except that  $Q_{0, \text{dia}}^N$  is also negatively correlated with diazotroph N and hence also nitrogen fixation  
240 (Figure 1). Although an increase in  $Q_{0, \text{phy}}^N$  makes ordinary phytoplankton less competitive, it also raises the oceanic  $\text{NO}_3^-$  inventory, which eventually leads to more phytoplankton N (Figure 2) and less nitrogen fixation (Figure 1).

Diazotroph C, N and P are generally more sensitive to parameter variations than phytoplankton, due to the much smaller total biomass of diazotrophs, which is also the reason why diazotrophs are less sensitive in OPEM-H, the model configuration in which their biomass is generally larger (Figure 2). Since ordinary phytoplankton dominates autotrophic biomass, it tends  
245 to control nutrient distributions. This explains why ordinary phytoplankton parameters such as  $Q_{0, \text{phy}}^N$  and  $\phi_{\text{phy}}$  have strong effects on diazotrophs but not vice versa. The zooplankton grazing preferences  $\phi_{\text{phy}}$  and  $\phi_{\text{dia}}$  drive the competition between ordinary phytoplankton and diazotrophs and hence have strong and opposing effects on their biomass. Owing to the relatively small total biomass, diazotroph C is more sensitive to changes in  $\phi_{\text{phy}}$  and  $\phi_{\text{dia}}$  than ordinary phytoplankton C.

Particulate C:N and N:P ratios are most sensitive to  $Q_{0, \text{phy}}^N$  (Figure 3). This sensitivity is related to biomass, as we see from  
250 the OPEM-H configuration, where diazotrophs are abundant in high latitudes and consequently the sensitivity of high-latitude C:N to  $Q_{0, \text{dia}}^N$  is high, even higher than to  $Q_{0, \text{phy}}^N$  (Figure 3). We do not find this behavior for high-latitude regions in the OPEM configuration, as well as low-latitude regions, where diazotrophs are not as abundant. The parameter  $Q_{0, \text{phy}}^P$  was expected to be the most important parameter for particulate C:P ratios, just like  $Q_{0, \text{phy}}^N$  is for the C:N ratio. However, this is only true for OPEM



**Figure 2.** Parameter sensitivities of globally averaged concentrations of ordinary phytoplankton and diazotrophs carbon, nitrogen, phosphorus, and ratios of globally averaged N and P. Black and grey shading denote OPEM and OPEM-H configurations, respectively.



at high latitudes. At low latitudes, and for the global ocean, particulate C:P ratios are most sensitive to  $Q_{0, \text{phy}}^{\text{N}}$  (Figure 3). The  
255 supply of nitrate and phosphate at different latitudes is the major reason for this pattern. Phosphate is not a limiting nutrient in  
the high-latitude Southern Ocean. Therefore, the cellular C:P ratio of ordinary phytoplankton, which dominates total particles,  
is negatively correlated with  $Q_{0, \text{phy}}^{\text{P}}$ . The effects of  $Q_{0, \text{phy}}^{\text{P}}$  are suppressed by the prevalence of N limitation in low latitude  
regions, and hence  $Q_{0, \text{phy}}^{\text{N}}$  affects particulate C:P variations more than  $Q_{0, \text{phy}}^{\text{P}}$ .

The sensitivities of dissolved N:P ratio to parameters in the three geographical settings (low, high latitudes and global)  
260 follow similar patterns. However, we find sensitivities to be generally higher in the low-latitudes, especially to variations of  
the phytoplankton parameters. Again this is because  $\text{NO}_3^-$  is often limiting in lower latitudes, particularly in the oligotrophic  
gyres, where the dissolved nitrogen pool is more sensitive to changes in phytoplankton as well as  $\text{N}_2$  fixation. This is also why  
grazing pressure on diazotrophs ( $\phi_{\text{dia}}$ ) has a much stronger effect at low than at high latitudes.

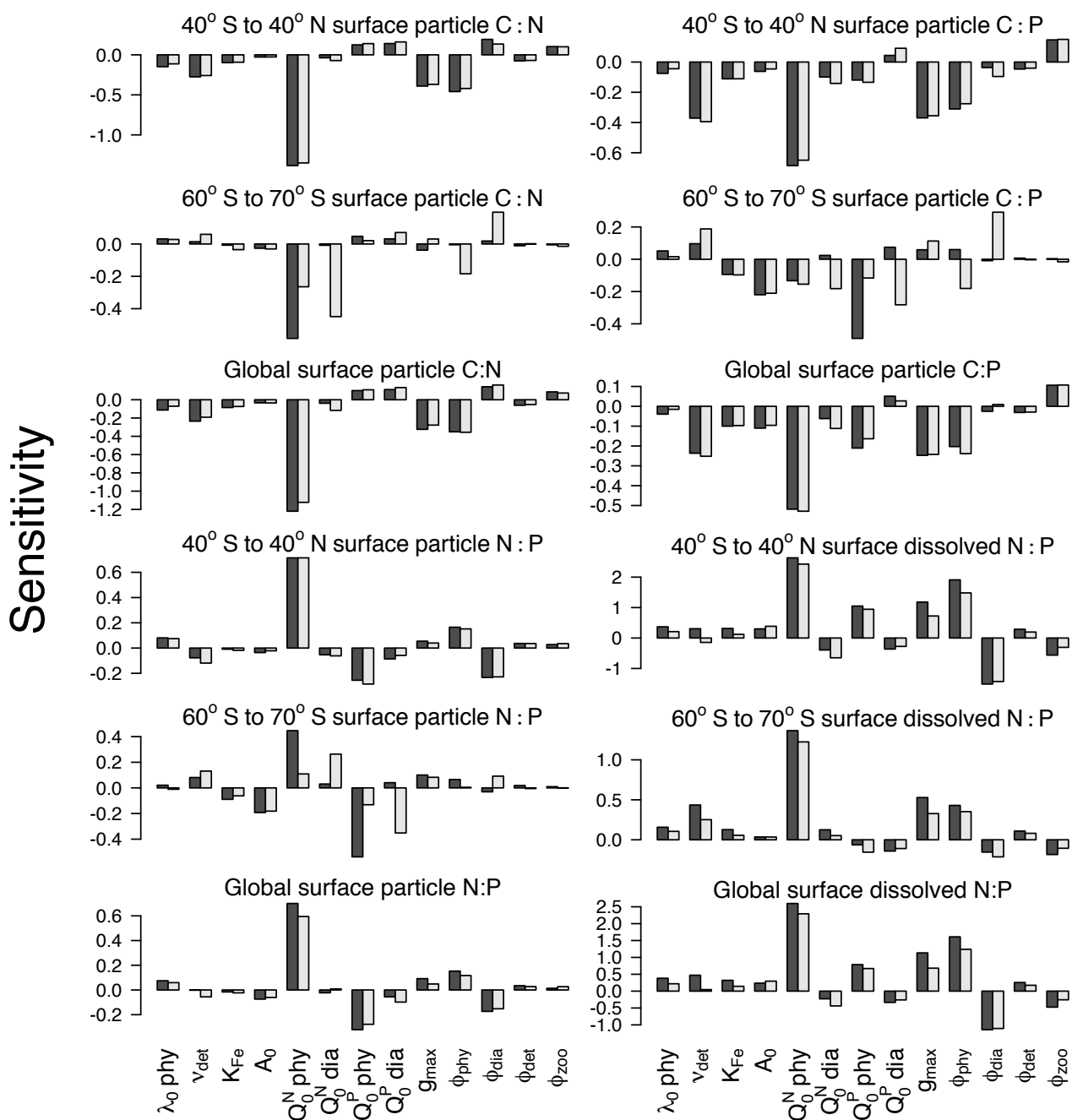
### 3.2 Cost function values of the ensemble simulations

#### 265 3.2.1 Constraining global rate estimates and inventories

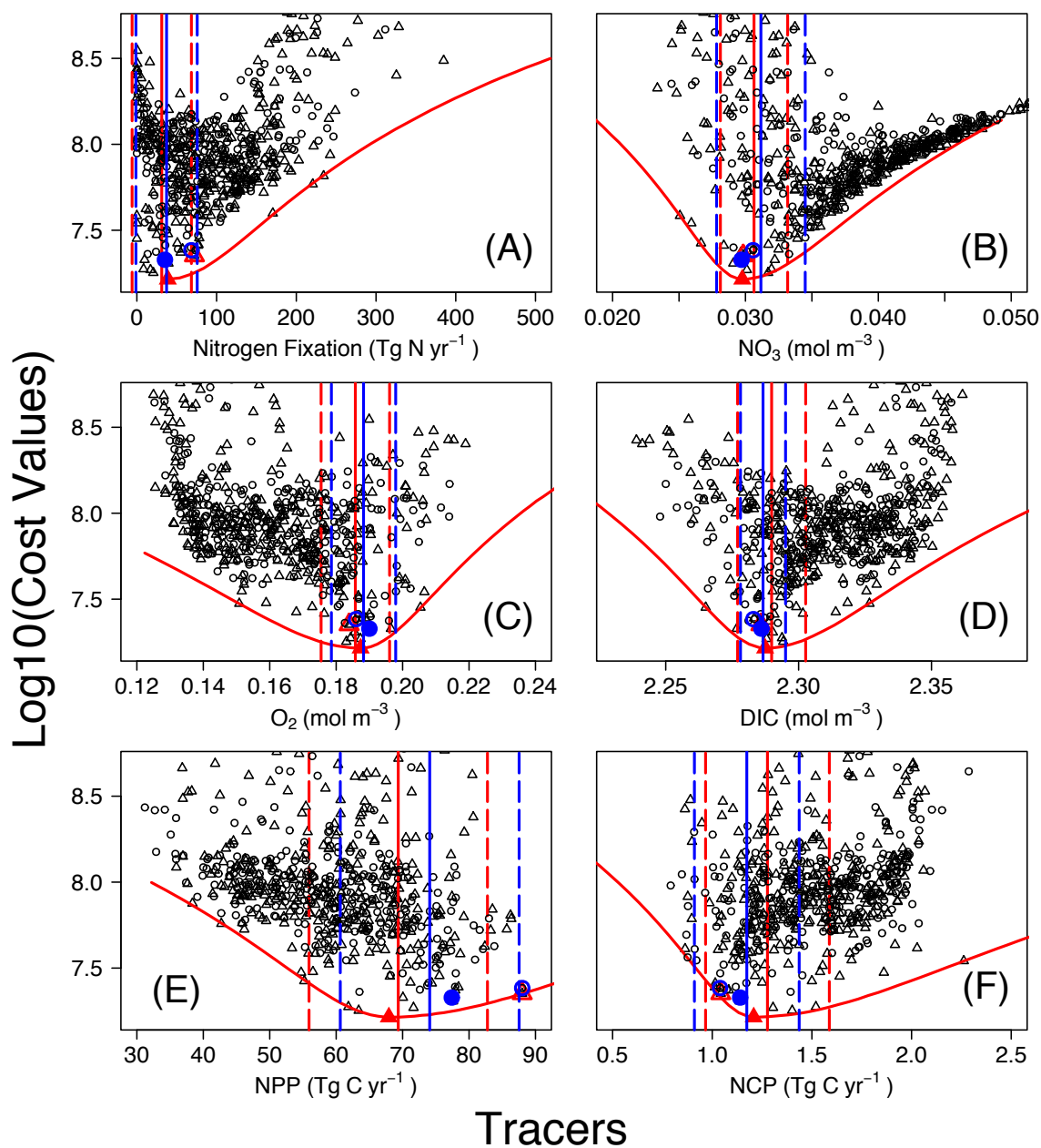
The cost function (introduced in Section 2.2.2) was devised for identifying the best solutions among the ensemble runs. For the  
model's upper layers (0 – 550 m) observational monthly mean concentrations of nitrate and phosphate enter the cost function,  
thereby reflecting regional and seasonal variations in the N:P uptake ratio of ordinary phytoplankton and diazotrophs. Variations  
in nitrate and phosphate availability affect the growth of diazotrophs and thus determine global  $\text{N}_2$  fixation in both OPEM and  
270 OPEM-H. In our UVic configurations, water column denitrification is the only fixed-N loss term. Therefore, the simulated  $\text{N}_2$   
fixation is expected to match water column denitrification under a steady-state nitrogen cycle. Nevertheless, the simulation with  
the lowest cost yields a global  $\text{N}_2$ -fixation rate estimate of  $38.8 \text{ Tg N year}^{-1}$  (Figure 4A), much lower than recent estimates of  
water column denitrification ( $55.8 - 72.9 \text{ Tg N year}^{-1}$ ; Somes et al., 2017; Wang et al., 2019).

The cost function penalises solutions that yield  $\text{N}_2$  fixation rates greater than  $90 \text{ Tg N year}^{-1}$ , but shows no clear relation  
275 to  $\text{N}_2$  fixation at lower rates (Figure 4A). For example, among the simulations with the 5 lowest cost function values in the  
OPEM configuration, the global ocean  $\text{N}_2$  fixation rate varies between 8 and  $40 \text{ Tg N year}^{-1}$ . These model solutions also  
differ with respect to their  $\text{O}_2$  inventories. The tendency of the cost function to favor very low global  $\text{N}_2$  fixation is caused  
by a compensatory effect, whereby improving  $\text{NO}_3^-$  deteriorates  $\text{O}_2$  and vice versa (see also Pahlow et al. (2019) and the  
Discussion section below). Thus, instead of selecting the reference parameter sets based only on the cost function, we also take  
280 the ability to yield reasonable  $\text{N}_2$  fixation rates into account, whereby we deem rates of about  $70 \text{ Tg N year}^{-1}$  as reasonable,  
since this matches current estimates of water-column denitrification (Somes et al., 2017; Wang et al., 2019). As these solutions  
represent a somewhat subjective trade-off between low cost and reasonable  $\text{N}_2$  fixation, we refer to them as trade-off solutions  
and details of their behaviour are shown and discussed in the companion paper Pahlow et al. (2019). For OPEM the trade-off  
solution corresponds to the seventh-lowest cost function value, and the fourth-lowest for OPEM-H.

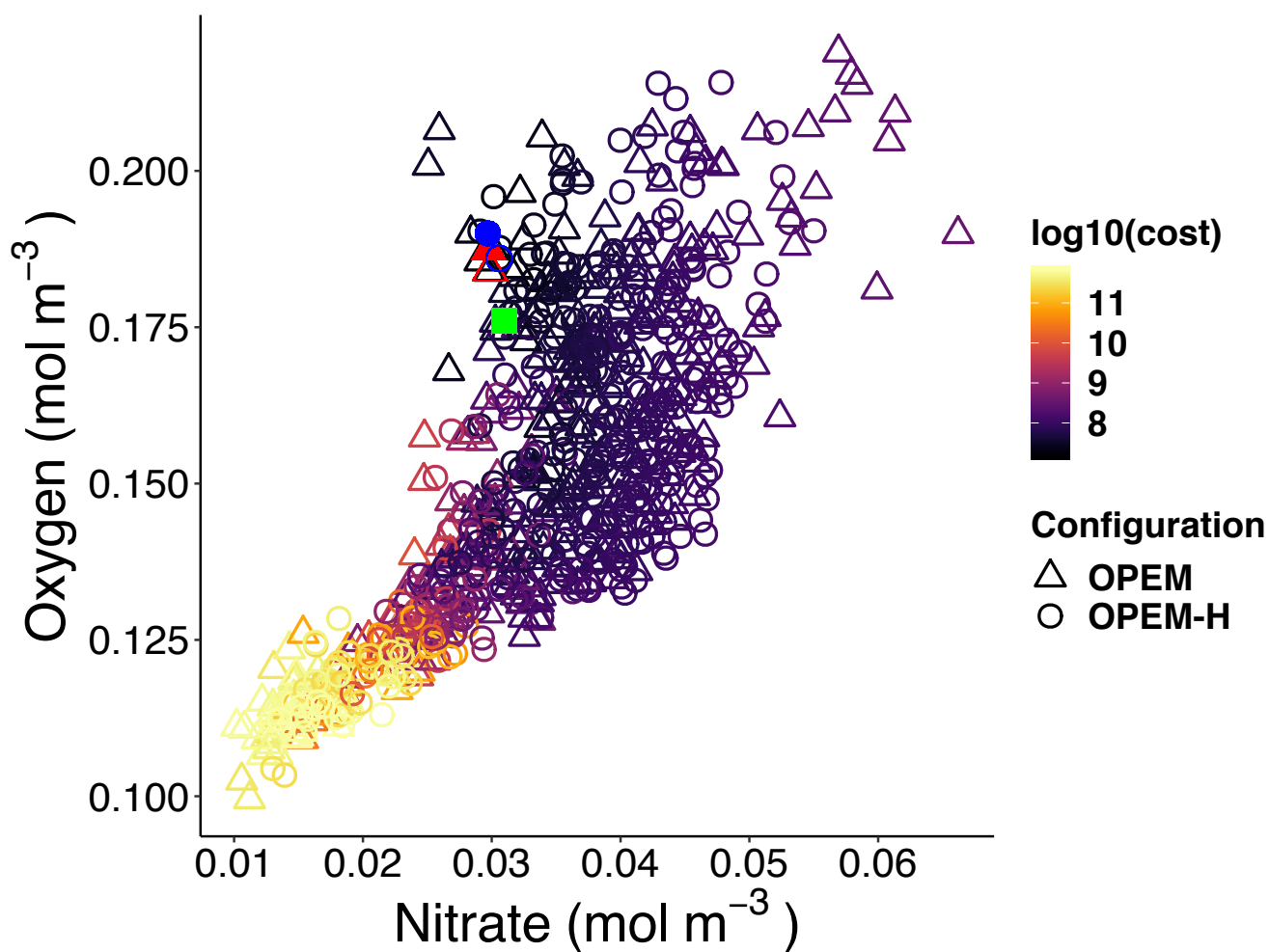
285 To understand the uncertainty range of our model results, we apply a bootstrap method to obtain an uncertainty quantifi-  
cation for our  $\text{N}_2$  fixation rate estimates, based on the available ensemble model runs. We collect the best solutions (lowest



**Figure 3.** Parameter sensitivities of averaged particulate elemental C:N, C:P, and N:P ratios for different latitude bands and the global ocean.



**Figure 4.** Costs vs. tracer concentrations and fluxes for annual  $N_2$  fixation (A), globally averaged  $NO_3^-$  (B),  $O_2$  (C) and dissolved inorganic carbon (DIC) (D) concentrations, as well as annual net primary production (NPP) (E) and net community production (NCP) (F). Red and blue symbols and lines are for OPEM (triangles) and OPEM-H (circles), respectively. Solid and open symbols represent minimum-cost and trade-off simulations, respectively. Vertical solid and dashed lines represent mean and 95% confidence interval of best solutions of 1000 randomly selected subsets of 100 ensemble members. Red parabolas fit the lowest costs at different rates or tracer concentrations.



**Figure 5.** Globally averaged oxygen vs. nitrate in OPEM and OPEM-H. Color represents cost value. Solid red triangle and blue circle annotate the simulations with minimum cost in OPEM and OPEM-H, respectively, and open red triangle and blue circle are the trade-off simulations. The green square indicates the WOA 2013 value.



cost function value) of 1000 randomly selected subsets of 100 ensemble members. Mean and 95% confidence interval of these estimates provide an uncertainty range in the vicinity of the  $\text{N}_2$  fixation rate estimate of the full ensemble. Globally averaged  $\text{N}_2$  fixation rates of our trade-off solutions of OPEM and OPEM-H are just outside and within this uncertainty range, respectively (Figure 4A). In the following we will describe the lowest-cost solutions together with the trade-off solutions, as well as respective uncertainty ranges. The width of the uncertainty ranges (95% confidence intervals) in Figure 4 indicates the metric's ability to constrain the inventory or rate under consideration.

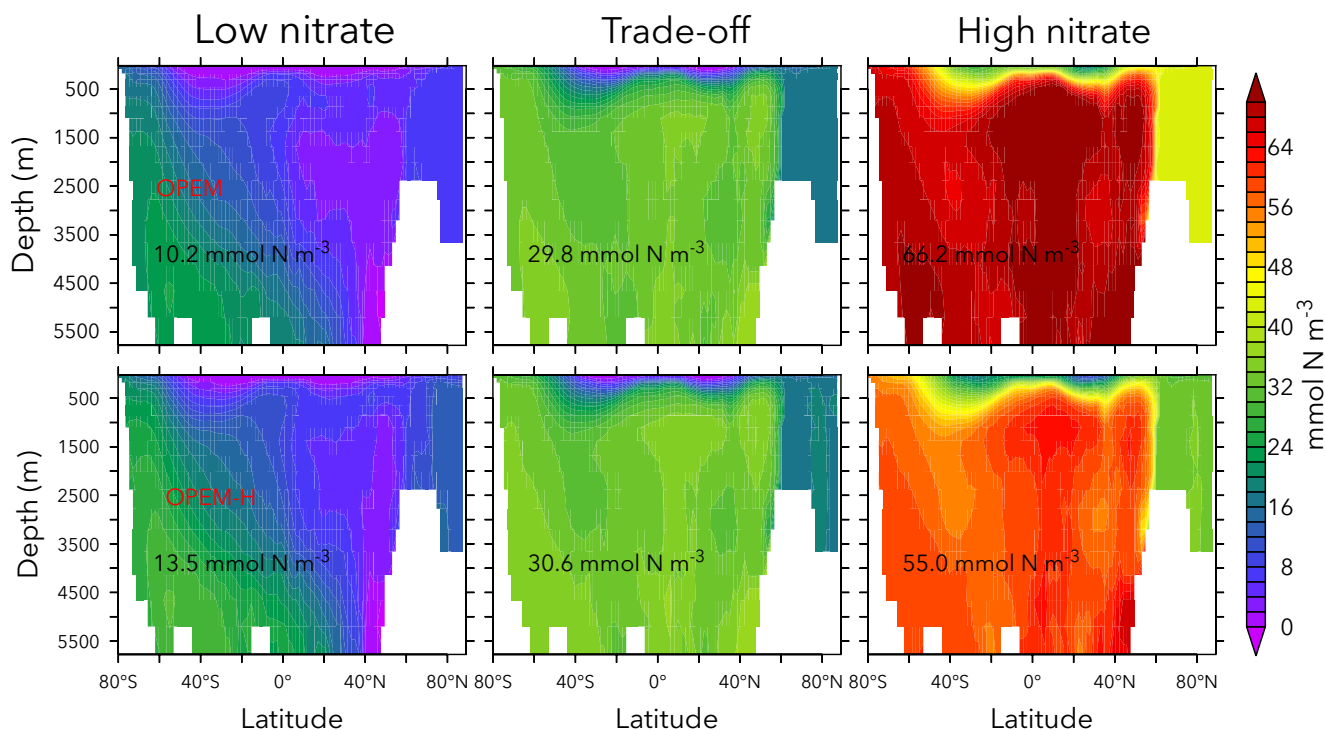
The global  $\text{NO}_3^-$  inventory turns out to be remarkably well constrained (Figure 4B). The mean global estimates are  $30.6 \text{ mmol N m}^{-3}$  and  $31.4 \text{ mmol N m}^{-3}$  for OPEM and OPEM-H, respectively. Ensemble solutions that deviate from these estimates have high costs and therefore the uncertainty ranges remain narrow. The trade-off and minimum-cost solutions are hardly distinguishable. The uncertainty of the simulated global  $\text{O}_2$  is comparable to that of the  $\text{NO}_3^-$  inventory. Global mean  $\text{O}_2$  concentrations of OPEM and OPEM-H are  $186 \text{ mmol O}_2 \text{ m}^{-3}$  and  $187 \text{ mmol O}_2 \text{ m}^{-3}$ . Our metric effectively constrains global DIC estimates,  $2.290 \text{ mol C m}^{-3}$  for OPEM and  $2.287 \text{ mol C m}^{-3}$  for OPEM-H (Figure 4D), although DIC data have not been explicitly considered in the cost function.

While the trade-off solutions exhibit  $\text{NO}_3^-$ ,  $\text{O}_2$  and DIC inventories well within their respective uncertainty ranges, we find somewhat larger deviations for the predicted global mean net primary production (NPP, Figure 4E). For OPEM and OPEM-H the trade-off solutions produce a, respectively, 30 % and 14 % higher NPP than the minimum-cost solutions. The net community production (NCP) estimates in Figure 4F are better constrained than NPP for both configurations. The trade-off solution of OPEM corresponds to a global NCP of  $1.043 \text{ Tg C year}^{-1}$ , which is close to the trade-off estimate of OPEM-H, where  $\text{NCP} = 1.039 \text{ Tg C year}^{-1}$ .

Figure 5 shows globally averaged concentrations of  $\text{O}_2$  versus  $\text{NO}_3^-$  of all ensemble members. The spread of the ensembles differs between the two tracers (by a factor of two for  $\text{O}_2$  and by a factor of six for  $\text{NO}_3^-$ ). Most solutions overestimate the global average  $\text{NO}_3^-$  concentration obtained from the WOA 2013 (Garcia et al., 2013a, b) and underestimate  $\text{O}_2$ . Solutions where both tracers strongly underestimate the WOA 2013 data are penalised by the cost function (Figure 5). The minimum-cost and trade-off solutions of OPEM and OPEM-H are close to the WOA 2013 estimates. The respective optimal solutions have slightly higher global mean  $\text{O}_2$  concentrations than the WOA 2013 and are in good agreement with respect to  $\text{NO}_3^-$ . In spite of larger costs, the trade-off solutions of both OPEM and OPEM-H are closer to the WOA 2013 estimate than the minimum-cost solutions (Figure 5). Overall, we stress that the minimum-cost and trade-off solutions appear at the margin of the full spread of the ensembles, which could be interpreted as indicating a model deficiency.

Figures 6 and 7 show zonally averaged  $\text{NO}_3^-$  and  $\text{O}_2$  in simulations with low and high  $\text{NO}_3^-$  and the trade-off simulations. The high- $\text{NO}_3^-$  simulations have similar  $\text{NO}_3^-$  and  $\text{O}_2$  patterns to the trade-off simulations, despite the very different mean  $\text{NO}_3^-$  and  $\text{O}_2$  concentrations. The patterns are different in the low- $\text{NO}_3^-$  simulations because of stronger deoxygenation and denitrification, which occur mostly in North Pacific deep water. The greater similarity of global mean  $\text{O}_2$  than  $\text{NO}_3^-$  reflects the influence of atmospheric  $\text{O}_2$  but also indicates that  $\text{NO}_3^-$  is more sensitive to changes in the physiology of diazotrophs.



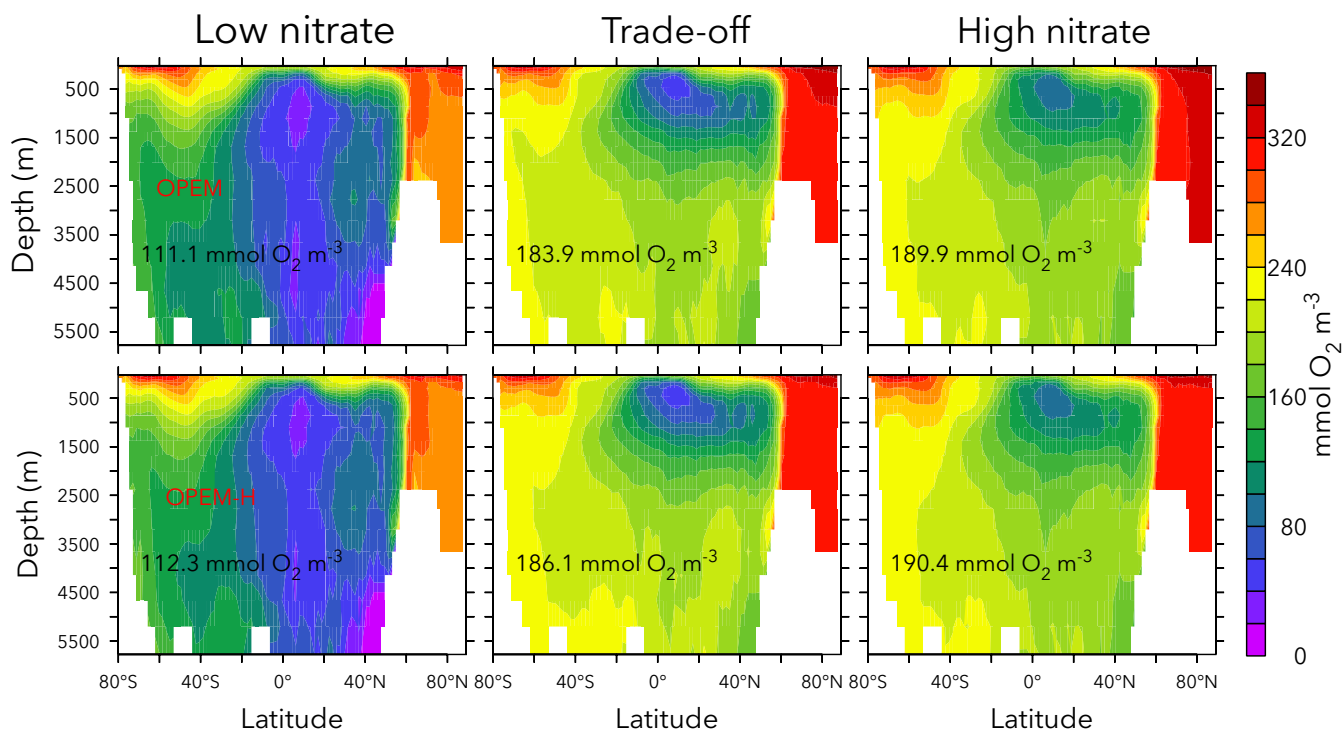


**Figure 6.** Zonally averaged  $\text{NO}_3^-$  in low- and high- $\text{NO}_3^-$  and the trade-off simulations for OPEM (upper row) and OPEM-H (lower row). Globally averaged  $\text{NO}_3^-$  concentrations are shown in each panel.

### 320 3.2.2 How well can model parameters be constrained?

Cost is conspicuously correlated only with  $\nu_{\text{det}}$ ,  $Q_{0, \text{phy}}^{\text{N}}$ , and  $\phi_{\text{dia}}$  (Figure 8).  $\text{O}_2$  and  $\text{NO}_3^-$  are sensitive to  $\nu_{\text{det}}$  and  $Q_{0, \text{phy}}^{\text{N}}$  but not to  $\phi_{\text{dia}}$  (Figure 1), which indicates that  $\phi_{\text{dia}}$  becomes more important at lower-cost simulations. The minimum-cost and trade-off simulations in OPEM and OPEM-H are usually closer to each other when parameters show strong correlations with costs (Figure 8).

325 Figure 9 shows how different biomes contribute to the misfit and variance parts of the total cost. For simulations with high cost function values ( $J > 10^{10}$ ), we find the variance term to be dominant in the deep ocean (below 550 m). Among the 17 biomes this is well expressed in NP.SPSS (North Pacific subpolar seasonally stratified), NP.STSS (North Pacific subtropical seasonally stratified), NP.STPS (North Pacific subtropical permanently stratified), Pac.EQU.E (Eastern Pacific equatorial), Pac.EQU.W (Western Pacific equatorial), and IND.STPS (Indian Ocean subtropical permanently stratified) biomes,  
 330 overwhelming contributions from all other parts of the cost function and all other biomes for the 100 simulations with the highest total costs. These high-cost simulations tend to have low  $\text{NO}_3^-$  and  $\text{O}_2$  concentrations (Figure 5). Low  $\text{NO}_3^-$  concentrations are coupled to low  $\text{O}_2$  because of intense denitrification in the ODZs. Accordingly, simulations with very low  $\text{NO}_3^-$



**Figure 7.** Same as Figure 6 but for  $O_2$ .

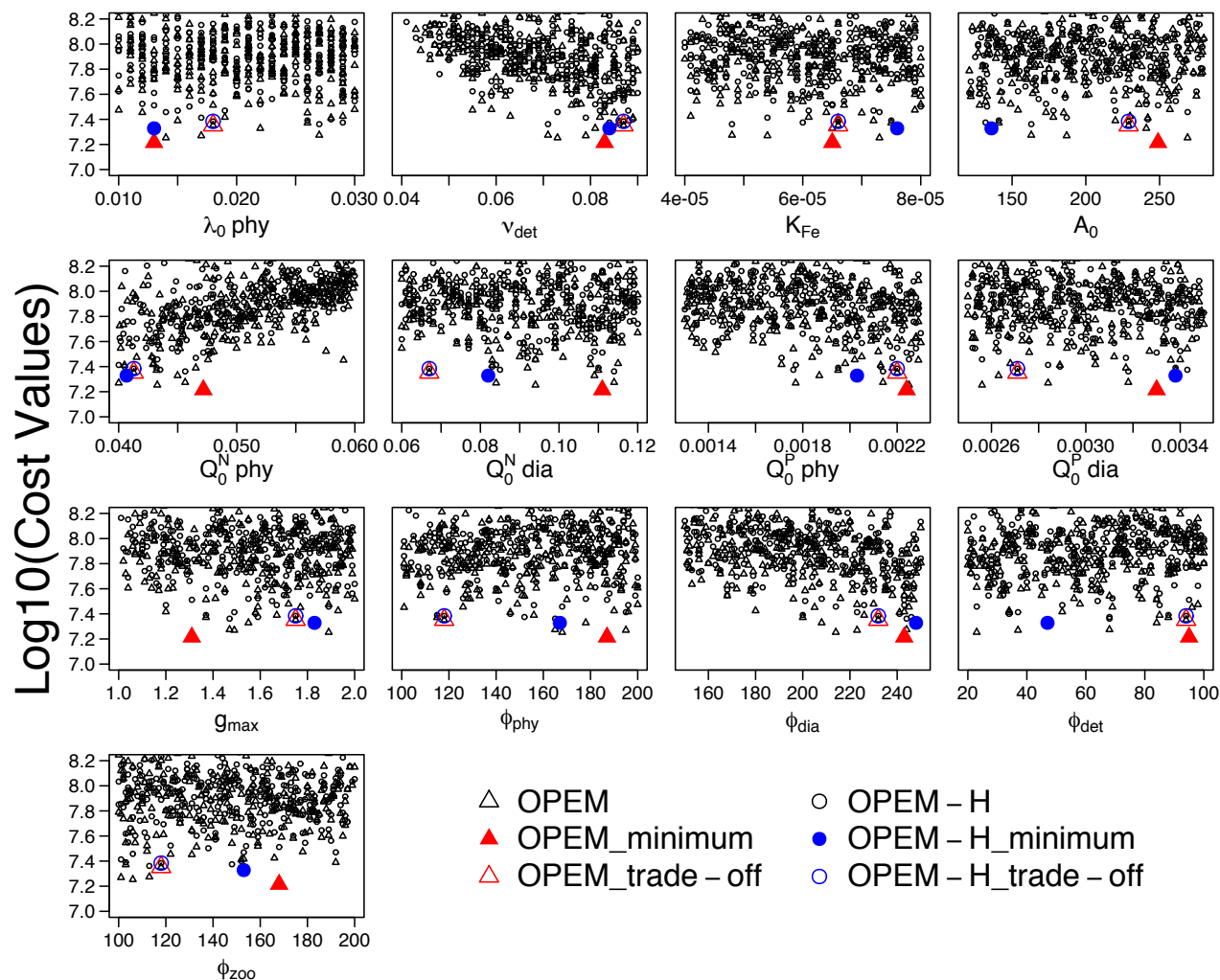
inventories suffer from widespread ODZs, occupying much of the deep water in the northern and equatorial Pacific as well as the Indian Ocean (Figure 6). This is the main reason for the high variance in the deep water of these biomes (Figure 9).

## 335 4 Discussion

### 4.1 Parameter sensitivities

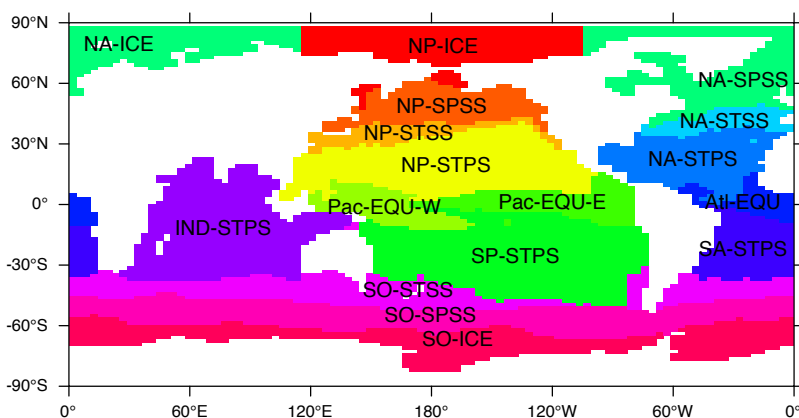
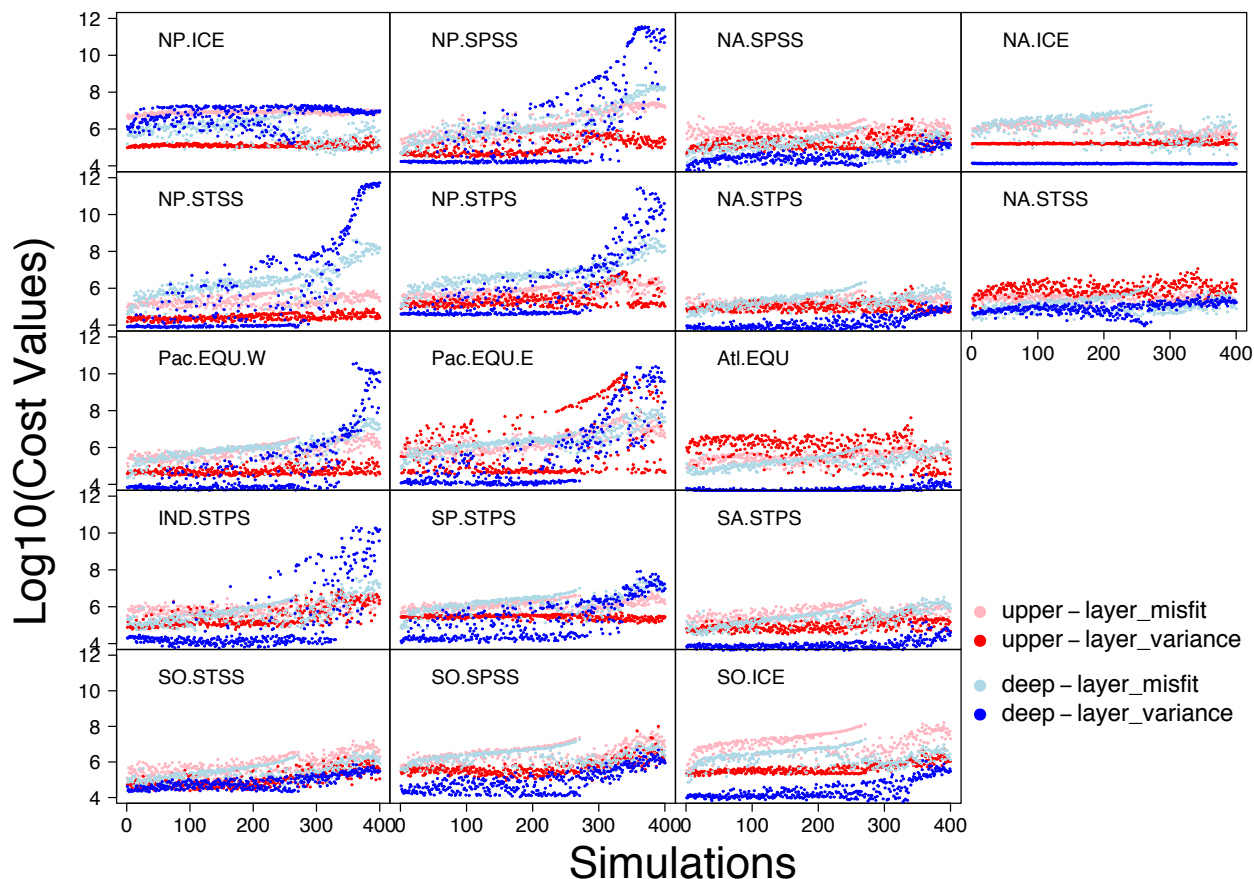
#### 4.1.1 Remineralisation rate $\nu_{det}$ and phytoplankton subsistence nitrogen quota $Q_{0,phy}^N$

Remineralisation rate ( $\nu_{det}$ ) and phytoplankton subsistence nitrogen quota ( $Q_{0,phy}^N$ ) are the two parameters with the strongest correlations for most tracers as well as particulate elemental stoichiometry. The importance of  $\nu_{det}$  was expected, because it is an important driver of nutrient recycling in the surface ocean (Thomas, 2002; Anderson and Sarmiento, 1994; Eppley and Peterson, 1979), which strongly affects NPP, NCP, Chl, DIC, DFe and  $N_2$  fixation (Kriest et al., 2012).  $\nu_{det}$  also determines the rate of  $O_2$  consumption, hence also the  $NO_3^-$  level, due to denitrification in ODZs (Cavan et al., 2017). The strong influence of  $Q_{0,phy}^N$ , however, was unexpected. The subsistence quota was first introduced by Droop (1968) in phytoplankton growth models. While it has been applied in Earth System Models (Kwiatkowski et al., 2018; Wang et al., 2019), a sensitivity analysis



## Parameters

**Figure 8.** Lower parts (cost  $< 10^{8.2}$ ) of cost-value distributions for the parameter ranges in Table 1. Solid red triangles and blue circles represent the minimum-cost simulations in OPEM and OPEM-H, respectively, and open red triangles and blue circles are the trade-off simulations.



**Figure 9.** Top panels: Cost-value distributions in the 17 biomes in OPEM. The order of the simulations is based on the total cost from low to high in OPEM. Upper-layer and deep-layer in the legend represent upper (0 – 550 m) and lower (below 550 m) components of the cost function (Eq. 5). Misfit and variance are calculated by the first and second parts of the cost function components (Eqs. 6 and 7), respectively. Bottom: Map of biome locations.



345 similar to the present study has not been done before. A higher  $Q_{0, \text{phy}}^{\text{N}}$  implies that more nitrogen is required for phytoplankton growth, but it also can be interpreted as a lessening of carbon fixation for a given nitrogen supply. Our results demonstrate a strong effect of  $Q_{0, \text{phy}}^{\text{N}}$  on NPP, Chl, POC export (NCP) and consequently oxygen consumption and denitrification.

These results also put forward a new point of view on the relation between  $\text{NO}_3^-$  inventory and carbon export. In classic biogeochemistry, a larger  $\text{NO}_3^-$  inventory in the ocean stimulates primary production and POC export. This feedback is intuitive and easy to understand, as for a given C:N in phytoplankton, carbon is proportional to the nitrogen pool. This feedback is well recognized and has been widely applied in marine sciences, especially since it forms the foundation of one of the hypotheses explaining the lower atmospheric  $\text{pCO}_2$  during the last glacial maximum (LGM) (McElroy, 1983; Falkowski, 1997). However, our analysis suggests another, very different point of view.  $\text{NO}_3^-$  concentration is positively correlated with  $Q_{0, \text{phy}}^{\text{N}}$ , but negatively with NPP and POC export (NCP, Figure 1), which means that an increased  $\text{NO}_3^-$  inventory can be related to a lower POC export if caused by a change in  $Q_{0, \text{phy}}^{\text{N}}$ . The dynamic C:N ratio in our model explains part of this negative correlation. When the  $\text{NO}_3^-$  inventory increases due to an increase in  $Q_{0, \text{phy}}^{\text{N}}$ , the nitrogen demand in phytoplankton also increases, which yields a lower C:N ratio in phytoplankton, and hence changes in carbon fixation due to increases in  $\text{NO}_3^-$  inventory remain relatively small. The increase in  $Q_{0, \text{phy}}^{\text{N}}$  increases nitrogen in phytoplankton structure and decreases the C:N ratio in phytoplankton as well as detritus. The two effects together both lower POC production and raise the  $\text{NO}_3^-$  inventory. Changes in  $\nu_{\text{det}}$  also contribute to the negative correlation between  $\text{NO}_3^-$  and POC export (NCP) in our simulations: A more intense remineralisation in the surface ocean reduces POC export, and thus decreases oxygen consumption and denitrification, resulting in a larger nitrate inventory.

#### 4.1.2 Zooplankton parameters

While in many global biogeochemical models zooplankton is described by non-mechanistic formulations, such as Holling-type functions (Holling and Buckingham, 1976), in this study we apply a more realistic zooplankton model (Pahlow and Prowe, 2010). Among the five zooplankton parameters, the maximum specific ingestion rate ( $g_{\text{max}}$ ) and the capture coefficients of phytoplankton ( $\phi_{\text{phy}}$ ) and diazotrophs ( $\phi_{\text{dia}}$ ) are the most important, whereas the preference for detritus ( $\phi_{\text{det}}$ ) is generally less important. Grazing on zooplankton itself ( $\phi_{\text{zoo}}$ ) counters the effect of  $g_{\text{max}}$  because it lowers zooplankton biomass and thus total ingestion. These parameters together dominate controls on  $\text{N}_2$  fixation and Chl (Figure 1), and C, N and P of ordinary phytoplankton and diazotrophs (Figure 2). It is interesting that zooplankton parameters also exert some control on particulate N:P as well as the dissolved nutrient pools (Figure 3). This can be understood via their controls on  $\text{N}_2$  fixation and the ensuing changes in N:P in the dissolved and particulate pools.

#### 4.1.3 Other parameters and the OPEM-H configuration

Other parameters in the sensitivity analysis appear less important for the tracer distributions, but this does not necessarily mean that they are negligible. Specific mortality rate ( $\lambda_{0, \text{phy}}$ ) and the phytoplankton half-saturation constant for Fe ( $k_{\text{Fe}, \text{phy}}$ ) do contribute some variations to most of the tracers (Figure 1), and particulate C:P is somewhat sensitive to potential nutrient affinity ( $A_0$ ). Phytoplankton subsistence P quota ( $Q_{0, \text{phy}}^{\text{P}}$ ) affects major tracers much less than phytoplankton subsistence N



quota ( $Q_{0, \text{phy}}^{\text{N}}$ ), but it is still important for particulate C:P and particulate N:P ratios, particularly at high latitudes and globally (Figure 3). Diazotroph subsistence N quota ( $Q_{0, \text{dia}}^{\text{N}}$ ) and diazotroph subsistence P quota ( $Q_{0, \text{dia}}^{\text{P}}$ ) in general have much less  
380 influence than  $Q_{0, \text{phy}}^{\text{N}}$  and  $Q_{0, \text{phy}}^{\text{P}}$  because diazotrophs are much less abundant than ordinary phytoplankton. Nevertheless, they are still important for  $\text{N}_2$  fixation and the elemental stoichiometry of diazotrophs.

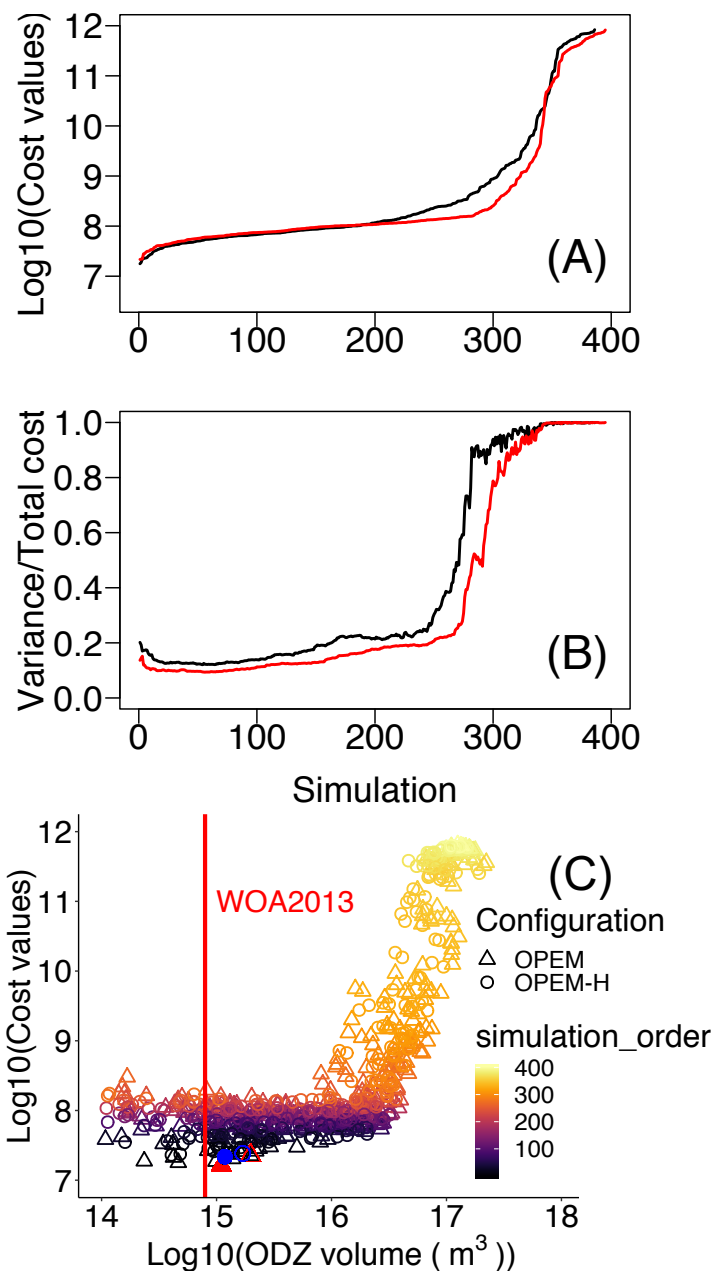
In general, tracer sensitivities to parameters in OPEM-H configuration are similar to those in OPEM.  $\text{O}_2$  and  $\text{NO}_3^-$  levels are slightly less sensitive to the remineralisation rate,  $Q_{0, \text{phy}}^{\text{N}}$ , and  $g_{\text{max}}$  in OPEM-H because this configuration allows (facultative) diazotroph to grow in high-latitude cold waters, hence the overall biomass of diazotrophs is greater (Pahlow et al., 2019). This  
385 is also the reason why  $Q_{0, \text{dia}}^{\text{N}}$  and  $Q_{0, \text{dia}}^{\text{P}}$  exert a stronger effect on surface-particle elemental stoichiometry at high latitudes in OPEM-H (Figure 3).

Several studies have revealed that  $\text{N}_2$  fixation occurs at high latitude regions (Sipler et al., 2017; Harding et al., 2018; Shiozaki et al., 2018; Mulholland et al., 2019), which supports a wider temperature range of  $\text{N}_2$  fixation, similar to what we have in OPEM-H. In the trade-off simulation for OPEM-H we do find some  $\text{N}_2$  fixation in the eastern North Pacific and the  
390 Arctic Ocean (Pahlow et al., 2019). The different temperature function for diazotrophy is also the reason for the differences in the sensitivities of particulate C:N:P to diazotroph subsistence quotas in high-latitude regions (Figure 3).

## 4.2 Model limitations

The strong correlation between  $\text{O}_2$  and  $\text{NO}_3^-$  (Fig. 5) indicates that  $\text{O}_2$  and denitrification are tightly coupled. Lack of benthic denitrification leaves water column denitrification as the only loss of  $\text{NO}_3^-$  and  $\text{O}_2$  becomes the primary factor controlling  
395 the  $\text{NO}_3^-$  inventory. This also implies that sensitivities of  $\text{NO}_3^-$  to the model-parameters could be different when benthic denitrification is incorporated in our model.

Several of our simulations have relatively small misfit in  $\text{O}_2$  and  $\text{NO}_3^-$  compared to the WOA 2013, and have high  $\text{N}_2$  fixation rates, comparable to those estimated in previous model simulations (e.g., Somes et al., 2017; Wang et al., 2019). On the one hand low  $\text{O}_2$  is connected with high rates of water-column denitrification in the eastern equatorial Pacific Ocean (Pac.EQU.E),  
400 causing a depression of  $\text{NO}_3^-$  concentration and a rather high variance in  $\text{NO}_3^-$  concentration, both of which conflict with the observations. Hence cost in this biome is very high, especially in the upper 550 m, where denitrification is strongest. On the other hand, although the volume of oxygen deficient zones (ODZs) in the minimum-cost simulations in OPEM and OPEM-H is greater than in the WOA 2013 (Figure 10C), they yield rather low  $\text{N}_2$  fixation rates (38.8 and 35.1  $\text{TgN year}^{-1}$  for OPEM and OPEM-H, respectively). ODZ volumes in the trade-off simulations are more than twice that in the WOA 2013 (Figure 10)  
405 and yield global  $\text{N}_2$  fixation rates close to current estimates of water-column denitrification (about 70  $\text{TgN year}^{-1}$ , Somes et al., 2017; Wang et al., 2019). The mismatch between ODZ volume and  $\text{N}_2$  fixation rate indicates that a refined description of water-column denitrification setting may be needed (Sauerland et al., 2019). Clearly, only by considering all major nitrogen sources and sinks, such as atmospheric deposition and benthic denitrification, a better representation of  $\text{N}_2$  fixation and the global marine nitrogen cycle can be achieved.



**Figure 10.** Cost values across all parameter sensitivity simulations ordered from low to high for the two model configurations. Cost values in both misfit and variance (A) and the contributions of variance (B). Black and red lines are for OPEM and OPEM-H, respectively. Total cost versus volume of ODZ (oxygen deficient zone  $< 5 \text{ mmol O m}^{-3}$ ) in the simulations (C), color represents the simulation order as shown in (A) and (B), Solid red triangle and blue circle annotate the simulations with minimum cost in OPEM and OPEM-H, respectively, and open red triangle and blue circle are the trade-off simulations.



## 410 4.3 Likelihood-based metric

### 4.3.1 Applicability of the cost function and usefulness of introducing variance information

The cost function introduced above is a metric that quantifies the discrepancy between objectively analyzed observational data and simulation results. Our cost function proves useful for exploring the 400 ensemble model solutions and identifies model solutions that reproduce deep ocean gradients in the  $\text{NO}_3^-:\text{PO}_4^{3-}$  ratio better than a classic fixed-stoichiometry model (Pahlow et al., 2019). In addition, the optimal model solutions yield improved NCP rate estimates. In particular, the trade-off solutions of OPEM and OPEM-H can resolve observed latitudinal patterns in dissolved and particulate C:N:P within the upper productive ocean layers (0–130 m, Pahlow et al. (2019)). The consideration of monthly mean  $\text{O}_2$ ,  $\text{NO}_3^-$ ,  $\text{PO}_4^{3-}$  data for the upper 550 m and surface Chl remote sensing data introduces important constraints on the representation of the relation between light and nutrient limitation, thereby also specifying the degrees of N and P limitation.

420 Even within the 5% of the simulations with the lowest costs, the estimates of global  $\text{N}_2$  fixation rate vary considerably. The mean global estimates  $\pm 1$  standard deviation in OPEM and OPEM-H are  $(37 \pm 26) \text{ Tg N yr}^{-1}$  and  $(51 \pm 29) \text{ Tg N yr}^{-1}$ , respectively. We initially expected that the  $\text{NO}_3^-$  and  $\text{PO}_4^{3-}$  data in the cost function would effectually constrain  $\text{N}_2$  fixation. This is clearly not the case and additional information has to be considered. One explanation may be that considerable  $\text{N}_2$  fixation can occur during short periods and may also be confined to regions smaller than the biomes. Regional differences with respect to  $\text{N}_2$  fixation remain unresolved if only biome-specific monthly mean  $\text{NO}_3^-$  and  $\text{PO}_4^{3-}$  data are considered for the upper layers in the cost function.

Also, the minimum-cost solution yields very low global  $\text{N}_2$  fixation rates. Thus, for the identification of the trade-off solutions we had to consider prior information about global water column denitrification, whose rate is balanced by  $\text{N}_2$  fixation according to our models. Incorporating  $\text{N}_2$  fixation as a single global rate estimate into our Likelihood-based cost function as a single additional term would become overwhelmed by the many tracer and variance terms defined in Eqs. (6) and (7). Rather, the additional information is treated as a second objective, which is similar to applying a multi-objective approach for model calibration (e.g., Sauerland et al., 2019), where a trade-off between two or more objectives (cost functions) is resolved. A refined cost function may incorporate monthly mean N:P ratios or  $\text{N}^*$  values based on WOA 2013 data (e.g., for the upper 130 m) for clustered sub-regions of some biomes. Such addition to the cost function would require some careful preprocessing, e.g., cluster analysis of the spatial N:P or  $\text{N}^*$  patterns, but may suffice to constrain simulated  $\text{N}_2$  fixation rates.

A peculiarity of our cost function is that it complements the data-model misfit, i.e. the residuals of spatial mean log-transformed values, with an additional term that resolves differences in spatial variances. How the neglect of this term affects the global mean tracer concentrations and flux estimates is depicted in Figures (S1 – S6) in the supplemental material. The cost function's variance term introduces a strong penalty to approximately 30% of all ensemble model solutions (Figure 10). The highest cost-function values ( $J > 10^9$ ) are associated with discrepancies in spatial variances that exceed the misfits in the log-transformed tracer concentrations. For large parts of the ensemble solutions the variance term contributes between 15 and 20% to the total costs. Interestingly, for those model solutions that yield low cost function values ( $J < 4 \times 10^7$ ) the relative contribution rises again when the misfit in the log-transformed tracer concentrations gradually decreases (Figure 10B).





### 4.3.2 Contribution of biomes

445 The 17 biomes derived by Fay and McKinley (2014) represent a scale similar to that addressed in global efforts to establish surface-ocean air-sea carbon-flux estimates (Wanninkhof et al., 2013; Rödenbeck et al., 2015). Accordingly, our cost function can be easily extended by incorporating air-sea CO<sub>2</sub> flux estimates in the future. Further improvements may be possible by introducing sub-regions in some biomes, e.g., for constraining N<sub>2</sub> fixation rate estimates, as discussed above.

For low cost function values the contribution of the variance term is generally small in most biomes for the deep layers (Figure 9), where variances of the log-transformed tracer concentrations compare very well between the simulations and the WOA 2013. For high costs this term can become dominant, e.g., for some biomes in the North Pacific as well as the Indian Ocean. A remarkable exception is the North Pacific Arctic biome (NP-ICE), where the deep layer's variance term remains dominant for most of the ensemble solutions. This is somewhat different in the Arctic biome of the North Atlantic (NA-ICE) and the Southern Ocean (SO-ICE), where the variance term remains low throughout almost the entire ensemble. For SO-ICE 455 the cost function is mainly affected by the misfit in log-transformed tracer concentrations. The misfit is associated mainly with discrepancies between observed and simulated NO<sub>3</sub><sup>-</sup> within the SO-ICE biome. Interestingly, these misfits in both upper and deeper layers drop again after around the 280<sup>th</sup> simulation. Simulations with high NO<sub>3</sub><sup>-</sup> do not result in total cost values as high as in simulations with very low NO<sub>3</sub><sup>-</sup> (Figure 5), but they have larger misfits for NO<sub>3</sub><sup>-</sup> in SO-ICE. A similar behaviour can be seen in the other Southern Ocean biome (SO-SPSS) as well as in NA-ICE.

460 The upper layer's variance term contributes strongly for low costs in North Atlantic biomes. This is particularly striking for the Equatorial Atlantic biome (Atl-EQU). The main reason is water column denitrification that results in a high variance in NO<sub>3</sub><sup>-</sup>. Likewise the Eastern Equatorial Pacific biome (Pac-EQU-E) reveals major model limitations in the upper layers. Overall, the unfolding of biome-specific contributions to the cost function clearly points to those regions where improving model performance appears most worthwhile. Our present cost function may then be reapplied to quantify and highlight 465 specific model improvements.

## 5 Conclusions

We demonstrate sensitivities of various tracers and processes to parameters in two configurations of a new optimality-based plankton-ecosystem model (OPEM) in the UVic-ESCM. While OPEM-H predicts a wider geographical range for N<sub>2</sub> fixation (Pahlow et al., 2019) and shows some differences in the sensitivities of diazotroph C, N and P to parameters when compared 470 to OPEM, the tracer sensitivity to model parameters is very similar in both configurations. The trade-off simulations in the OPEM and OPEM-H happen to have the same parameter set. Among our model simulations, varying model parameters within reasonable ranges results in variations in O<sub>2</sub> by a factor of two and in NO<sub>3</sub><sup>-</sup> concentration by a factor of six. The sensitivity analysis provides important information regarding the new models' behaviour. The O<sub>2</sub> inventory is mainly influenced by the remineralisation rate ( $\nu_{\text{det}}$ ) as well as phytoplankton subsistence nitrogen quota ( $Q_{0, \text{phy}}^{\text{N}}$ ) and zooplankton maximum specific 475 ingestion rate ( $g_{\text{max}}$ ). Changes in  $Q_{0, \text{phy}}^{\text{N}}$  strongly impact the NO<sub>3</sub><sup>-</sup> inventory, as well as the elemental stoichiometry of ordinary phytoplankton, diazotrophs and detritus.  $Q_{0, \text{phy}}^{\text{N}}$  also affects N<sub>2</sub> fixation, Chl, DIC and iron levels. Furthermore, our sensitivity



analysis resolves correlations between various biogeochemical tracers. For example, POC export is negatively correlated with the  $\text{NO}_3^-$  inventory. We would like to point out that these changes in model behaviour are solely caused by variations in parameters. Thus, the correlations between tracers and rates might not stand when tracer variations are caused by other factors.

480 For example, an increase in the  $\text{NO}_3^-$  inventory due to anthropogenic emissions may be accompanied by an increase in POC export (Fernández-Castro et al., 2016). Also, although we did evaluate sensitivities of particulate elemental stoichiometry at different latitudes, most tracer sensitivities and correlations should be considered valid only for global but not regional scales.

We introduce a new likelihood-based metric for model calibration. The metric appears capable of constraining globally averaged  $\text{O}_2$ ,  $\text{NO}_3^-$  and DIC concentrations as well as NCP. In particular, the minimum-cost and trade-off model solutions

485 resolve observed latitudinal patterns in particulate C:N:P within the surface layers (0 – 130 m). However, the metric does not effectually constrain the models' global  $\text{N}_2$  fixation rate estimates. Incorporating additional terms such as monthly mean  $\text{N}^*$  in the surface layer into the cost function might provide an additional constraint on simulated  $\text{N}_2$  fixation rates. Individual contributions of the biomes to the cost function provide details of how tracer distributions in each biome respond differently under different ecosystem settings. The consideration of spatio-temporal variations in the stoichiometry of  $\text{NO}_3^-$ ,  $\text{PO}_4^-$ , and

490  $\text{O}_2$  in our metric favours model solutions with low  $\text{N}_2$  fixation rates that are solely balanced by water column denitrification. From our findings we conclude that an explicit consideration of benthic denitrification and atmospheric deposition seem critical for improving the representation of the complete global nitrogen cycle in our model.

*Code availability.* The University of Victoria Earth System Climate Model version 2.9 (Original Model) is available at <http://www.climate.uvic.ca/model/>. The OPEM v1.0 code is available at [http://dx.doi.org/10.3289/SW\\_1\\_2020](http://dx.doi.org/10.3289/SW_1_2020). The instructions needed to reproduce the model

495 results described in this article are in the supplemental material.

*Author contributions.* Chia-Te Chien and Markus Pahlow performed the ensemble solutions and selected the reference simulations. Markus Schartau set up the likelihood-based metric. All authors contributed to the manuscript text.

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