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# What do economic water storage valuations reveal about optimal vs. historical water management?

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## Abstract

What is the economic value of storing water for future droughts, and what are the consequences of this valuation for water management? One way to answer this question is to ask: ‘what is the valuation, which if used, would maximize a region’s economic use of water?’ This prescriptive valuation can be done by linking classical hydro-economic models to global search methods. Another way to answer this question is to ask: ‘what do historical water management operations reveal about water’s economic value?’ Indeed, past reservoir uses reveal the empirical inter-temporal valuations of past water managers. Although they may not have been optimized in a formal sense, in mature water resource systems with economic water demands, reservoir storage rules evolve via a socio-political process to embody societies’ valuation of water. This empirical, ‘positive’, or descriptive valuation is captured by calibrating a hydro-economic model such that carry-over storage functions enable simulated storage to match a historical benchmark. This paper compares both valuations for California’s Central Valley revealing that carryover storage values derived from historical operations are typically greater than prescribed values. This leads to a greater reliance on groundwater use in historical operations than would have been achieved with system-wide optimization. More generally, comparing the two approaches to water valuations can provide insights into managers’ attitudes as well as the impact of regulatory and institutional constraints they have to deal with – and that are not necessarily included in optimization models.

**Keywords:** Water storage valuation, Historical water management, descriptive vs. prescriptive approaches, hydro-economic modeling, California Central Valley.

## 1 Introduction

What can water storage valuation tell us of the difference between optimal and historical water management decisions? Economic valuation of water across space and time informs water allocation

36 and the design of the physical and regulatory infrastructure that supports it; this valuation reflects  
37 the hydrological, economic, institutional and ecological situation of a river basin [1, 2]. Modeling-  
38 based approaches that derive water values aim to integrate these various aspects within a river  
39 basin model. Such approaches can be descriptive or prescriptive, used to examine historical or  
40 optimal water management decisions respectively. Descriptive approaches generally integrate the  
41 existing allocation rules and benefits from water allocation into a simulation framework to derive a  
42 valuation [3]. Prescriptive approaches use optimization to find a “best” system-wide allocation  
43 strategy according to a benefit-maximization criterion, and get an economically “efficient” valuation  
44 of water as a by-product of optimization [4-6]. Economic valuation of water according to these two  
45 types of approaches has different interpretations. Water values in descriptive models come from the  
46 actual allocation whereas in prescriptive models, they correspond to value extracted from optimal  
47 use. What is more, descriptive valuations are generally set to reflect the rules that direct water  
48 management rather than reproduce historical operations – i.e., historical outcomes of this rule  
49 system.

50 This paper contributes a methodology to infer a descriptive valuation directly from historical  
51 operations, in a way that makes it comparable to a prescriptive valuation. It uses a recent modeling  
52 framework fit for prescriptive valuation of surface water storage in large-scale conjunctive use  
53 systems [6], and instead finds the valuation of water storage that calibrates the model against a  
54 historical benchmark - making it a descriptive valuation approach. A higher water value in a given  
55 reservoir from one approach to another would reflect a premium placed on conservation of water  
56 from that reservoir. This enables further investigation of the cause for these discrepancies: is it  
57 because managers had a myopic behaviour in historical operations? Or is the prescriptive model  
58 missing something? Previous “positive” approaches [7] aimed to calibrate users’ benefit functions in  
59 hydro-economic models, generally focusing on agriculture [8, 9]. In contrast, this framework aims to  
60 investigate the water value implications of already derived benefit functions.

61 These modeling-based approaches are a type of non-market valuation techniques – such techniques  
62 can also be survey-based [10]. In contrast, in market valuation techniques the value of an asset is  
63 based on the selling price or the price that consumers are willing to pay for a commodity in the  
64 market. Water markets are common in Western US [11-13], Australia [14-17], and the UK [18, 19].

65 In theory, descriptive and prescriptive market valuations are the same as actual water prices  
66 converge towards the socially optimal value. Yet, water markets are far from a universal solution [5]  
67 and further, they often fail to achieve their primary objective of economic efficiency unless an  
68 adequate regulatory and institutional framework is designed and implemented to sustain them [20-  
69 22]. In conjunctive use systems, different prices between local and non-local water, and between  
70 surface water and groundwater, may lead to overexploitation of groundwater resources even with a  
71 functioning market [23]. Optimization models tend to behave like water markets in the sense that  
72 they allocate water to most beneficial uses first, therefore comparing prescribed valuation to a  
73 historical benchmark has the potential to unveil some of the mechanisms that separate current  
74 operations from those that would result from a water market. Besides, system scale and complexity  
75 make water valuation more complicated. Under the phrase “curse of dimensionality”, scale by itself  
76 is a major obstacle to most optimization methods (e.g., SDP, most recently [24-26]). Even methods  
77 that can circumvent this limitation (e.g. SDDP; [27]) are subject to restricting assumptions. In the  
78 case of SDDP for instance, it is necessary for future benefits to be convex, which is a problem when  
79 studying conjunctive use systems [28]. It is noteworthy that the present work builds on an approach  
80 [6] that handles system scale as well as non-linearity and non-convexity. That approach was the first  
81 to the link an evolutionary algorithm (EA) to a hydro-economic model [2] for this purpose.

82 Application of EAs to aid decision-making in economics can be seen in several studies [29-31]. The  
 83 comparison of optimization results to water valuation from a historical benchmark is applied to the  
 84 California Central Valley system, a system with 30 reservoirs in an agricultural area that also relies on  
 85 groundwater, especially in times of drought [32-36]. Results are used to compare the two  
 86 management practices using the concept of risk aversion. Risk aversion is the behaviour of decision-  
 87 makers when they are exposed to uncertainty. This is quantified by risk aversion coefficient [37, 38]  
 88 whose positive (negative) sign reveals risk-taking (risk-averse) attitudes.

89 The remainder of this paper is structured as follows. Section 2 explains the proposed approach;  
 90 section 2.5 presents the California Central Valley application; results are shown in section 4, followed  
 91 by discussion and conclusions in sections 0 and **Error! Reference source not found.**, respectively.

## 92 2 Methods

### 93 2.1 Water storage valuations

94 This work looks at the value of water storage for future uses, in a context where benefits from  
 95 different water uses are already known. Valuation of water storage in reservoir balances current and  
 96 future uses through the carry-over storage value function (COSVF). The COSVF describes water value  
 97 as a function of reservoir storage. This work focuses on the end-of-year COSVF that determines the  
 98 value of water for next years' uses. It compares carryover storage values obtained from a  
 99 prescriptive optimization framework, to those that enable reservoir operations to most closely fit a  
 100 historical benchmark. Therefore, there needs to be a common and easily interpretable functional  
 101 form from which to derive carryover storage values in both cases.

102 At each point on the end-of-year COSVF, marginal benefits from an additional unit of storage for  
 103 future uses are a unit value of water. In other words, end-of-year COSVF is the integral of the  
 104 function known as the demand curve [39], that describes the unit value of water as a function of  
 105 storage (Figure 1). This unit value can be interpreted as the marginal price that water users are  
 106 willing to pay, and is therefore noted  $P$ . In its most general form, the end-of-year COSVF of a single  
 107 reservoir is a function of that reservoir's storage  $S$  and of the parametrisation vector  $\pi$  chosen for  
 108 the demand curve:

$$COSVF(S; \pi) = \int_{S_{min}}^S P(s; \pi) ds \quad (1)$$

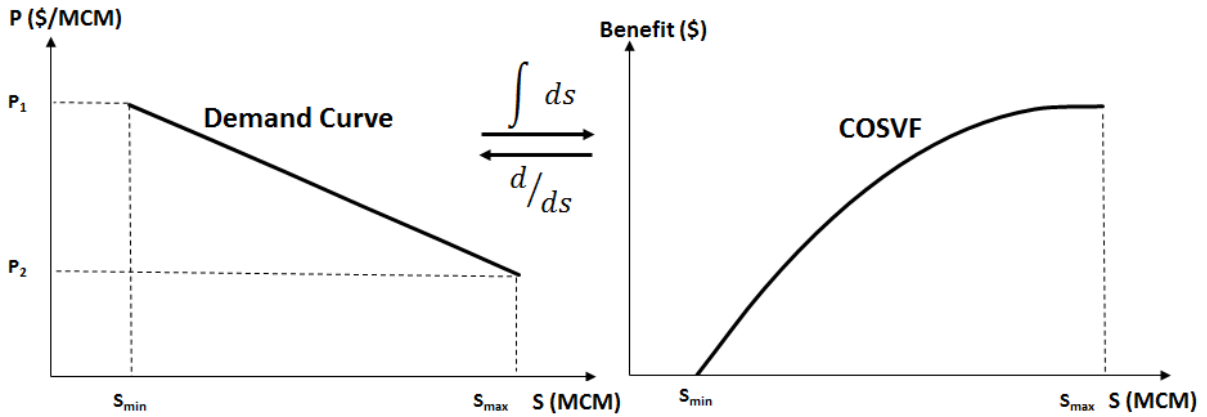
109 A direct consequence of equation (1) is that a reservoir's COSVF is a growing function of storage,  
 110 with  $COSVF(S_{min}; \pi) = 0$ . In its simplest form, the demand curve is linear, therefore the  
 111 parameters  $\pi$  are water values at minimal and maximal storage ( $p_1$  and  $p_2$  respectively):

$$P(S; \pi) = P(S; p_1, p_2) = p_1 + (p_2 - p_1) \frac{S - S_{min}}{S_{max} - S_{min}} \quad (2)$$

112

113 This means that the integral of equation (2), the end-of-year COSVF, is quadratic; since it is 0 at  
 114 minimal storage, it is entirely defined by  $\pi = (p_1, p_2)$ . When storage in reservoirs is close to dead  
 115 storage  $S_{min}$ , water is scarce for future uses, therefore each unit of stored water is close to its  
 116 maximal value  $p_1$ . Conversely, when reservoir levels get close to the maximum allowable storage  
 117  $S_{max}$ , water is more abundant for future uses, leading to lowering the value of an additional unit of  
 118 water towards its minimum value  $p_2$  (see Figure 1). In practice, this paper will use the linear demand

119 curve of equation (2), and the associated two-parameter end-of-year COSVF, to compare  
 120 prescriptive and descriptive valuations.  
 121



122  
 123 **Figure 1.** Relation between demand curve and benefit function of a surface reservoir, in the case of a linear  
 124 demand function.

125 In a river basin comprising multiple reservoirs, end-of-year carry-over storage values can be summed  
 126 across all reservoirs, and a total end-of-year carry-over storage value function  $COSVF_{all}$  can be  
 127 written as a function of the vector of system state  $x$ , usually including storage values at all the  
 128 reservoirs, and the vector  $\pi$  of end-of-year COSVF parameters  $\pi_i$  at each individual reservoirs:

$$COSVF_{all}(x; \pi) = \sum_{i=1}^n COSVF(S_i; \pi_i) \quad (3)$$

129 where  $n$  is the number of reservoirs in the system. For instance with a linear demand function,  $\pi_i$   
 130 comprises the values of  $p_1$  and  $p_2$  at each reservoir  $i$ .

## 131 2.2 Prescriptive water valuation

132 Prescriptive water valuation corresponds to the storage valuations that are obtained by maximizing  
 133 operating benefits from water uses in a water resource system over a given time frame  $[1, T]$ , with  
 134 discrete time-steps of a month or less. This is expressed by:

$$Z = E \left[ \sum_{t=1}^T f_t(x_t, u_t, q_t) + v_{T+1}(x_{T+1}, u_{T+1}) \right] \quad (4)$$

135 where  $E[.]$  is the expectation operator and  $f_t(.)$  represents the net benefits from water usage  
 136 (consumptive uses, hydropower generation, ecological benefits, etc.) at stage  $t$ . As introduced for  
 137 equation (3), vector  $x_t$  is the state of the system at  $t$ , typically including storage in the different  
 138 reservoirs.  $u_t$  is the vector of operational decisions taken at that stage  $t$ , such as reservoir releases  
 139 and water allocations to spatially distributed users, including farmers, industries or domestic uses  
 140 from cities.  $q_t$  is the vector of inflows. Finally,  $v_{T+1}(.)$  is a final value function that expresses that  
 141 reservoirs should not be simply emptied at the end of the optimization horizon, because water has  
 142 value beyond that. In short,  $v_{T+1}(.)$  expresses the carry-over value of water within the system. This  
 143 optimization problem is subject to a number of constraints such as the water balance equation,  
 144 lower/upper bounds on flows and storage levels, or hydropower generation capacity, to name a few.  
 145 Solving the stochastic maximization problem of equation (4) requires mapping decisions  $u_t$  as a

146 function of system state and expected inflows. Except for situations where specific assumptions such  
 147 as convexity hold [40], this maximization problem is plagued by the well-known curse of  
 148 dimensionality, whereby the required computational resources increase exponentially, making the  
 149 resolution of large-scale problems intractable.

150 Khadem et al. [6] proposed a general approximate solution methodology to the problem of  
 151 maximizing (4), based on two key remarks. The first relates the general optimization problem of  
 152 equation (4) to prescriptive water valuation in reservoirs across the water resource system of  
 153 interest. Indeed, defining single-year maximization problems involves end-of-year COSVF as a final  
 154 boundary condition. For year ( $k = 1 \dots K$ ) spanning  $[t_k + 1, t_{k+1}]$ , the single-year maximization  
 155 objective can be written as a function of current year inflows  $Q_k = (q_{t_k+1}, \dots, q_{t_{k+1}})$  and end-of-  
 156 year COSVF parameter vector  $\pi$ :

$$Z_k(Q_k, \pi) = \sum_{t=t_k+1}^{t_{k+1}} f_t(x_t, u_t, q_t) + COSVF_{all}(x_{t_{k+1}}; \pi) \quad (5)$$

157 Contrary to the stochastic problem of equation (4), each maximization of the single-year objective  
 158  $Z_k$  is a deterministic optimization problem that can be handled by state-of-the-art solvers (e.g. the  
 159 30-reservoir problem in the application is solved in 15 seconds for each year). Then, the second key  
 160 remark is that maximizing the objective of equation (4) can be approximated by the following  
 161 objective function (see [6] for details):

$$Z(\pi) = \sum_{k=1}^K \left( \max_{u_t} \{Z_k(Q_k, \pi)\} - COSVF_{all}(x_{t_{k+1}}; \pi) \right) \quad (6)$$

162 The problem of maximizing equation (6) and that of equation (4) are subject to the same physically-  
 163 based constraints (water balance, limits on reservoir storage and hydropower production, etc.), but  
 164 crucially, equation (6) transforms the decision problem of equation (4) (intractable for large systems)  
 165 into a problem of finding the end-of-year COSVF parameters in the system reservoirs. Evolutionary  
 166 algorithms are well-suited to searching this large parameter space provided they can associate a  
 167 value to each parameter vector. This value is:

$$\min_{\pi} F_{pres}(\pi) = \min_{\pi} [-Z(\pi)] \quad (7)$$

168 It is interpreted as “prescriptive” and noted  $F_{pres}$  because the vector  $\pi$  that solves the maximization  
 169 problem of equation (6) directly gives the functional form of end-of-year COSVF at each of a system’s  
 170 reservoirs. This enables a prescriptive valuation of end-of-year water storage.

### 171 2.3 Descriptive valuation

172 In contrast to the prescriptive valuation, a descriptive valuation seeks end-of-year COSVF parameters  
 173 that maximize the fit with benchmark time series, reflecting the system’s states (e.g., storages)  
 174 across the study area. The descriptive case seeks to find COSVFs that reflect how water storage has  
 175 been valued in practice, which is not necessarily equal to marginal benefits from future water uses in  
 176 the prescriptive case. For a given vector  $\pi$ , we can compute  $Z(\pi)$  as in equation (6), by sequentially  
 177 solving the single-year optimization problem of equation (5). Yet, instead of being interested in  
 178 maximizing the value of the economic objective  $Z(\pi)$  itself, we are now interested in the vector of  
 179 system states  $x(\pi)$  that has been computed to obtain  $Z(\pi)$  – recall that those typically include  
 180 reservoir storage. We explore the parameter space to find the parameter vector that minimizes the  
 181 mean-squared errors with the benchmark:

$$\min_{\pi} F_{desc}(\pi) = \min_{\pi} \left[ \frac{1}{N \cdot T} \sum_{n=1}^N \sum_{i=1}^T (x_{t,i}(\pi) - x_{t,i}^{benchmark})^2 \right] \quad (8)$$

182 where  $N$  is the number of state variables used for calibration and  $F_{desc}$  is the descriptive objective  
 183 function to minimize.

184

## 185 2.4 Workflow

186 For both water storage valuations, parameter values that maximize the respective objectives are  
 187 found by evolutionary computation. Yet in both cases, many reservoirs will be refilled every year if  $p_2$   
 188 is above a threshold value  $p_2^0$ . Then, any value of  $p_2$  above this threshold (i.e., in  $[p_2^0, +\infty]$ ) produces  
 189 the same operations – stored water is valuable enough to warrant the reservoir to be full at the end  
 190 of any water year. Then, the algorithm could return a marginal water value of \$5 million per MCM  
 191 without affecting the system’s operations at all. To ensure the parameter values found by the  
 192 algorithm make economic sense, a second objective is introduced to limit the value of  $p_1$  and  $p_2$ ,  
 193 similar to what was done in [6]:

$$\min_p F_2 = \min_p \frac{1}{N} \sum_{n=1}^N \frac{p_{\min n} + p_{\max n}}{2} \quad (9)$$

194 This second objective turns the single objective optimization problem into a multi-objective  
 195 optimization problem. This type of problem is solved by multi-objective evolutionary algorithms  
 196 (MOEA) which are broadly similar to genetic algorithms except for the fact that they can optimize  
 197 two objectives or more at once. As a result, contrary to traditional genetic algorithms that return a  
 198 single solution, a MOEA generally returns a set of solutions such that one cannot improve any  
 199 objective without degradation in another objective. These solutions are called non-dominated and  
 200 are collectively called the Pareto front (see [41] for details on MOEA). In this work, the MOEA is  
 201 meant to find the set of states such that one cannot find a better solution both in the minimization  
 202 of the first objective (either  $F_{norm}$  or  $F_{desc}$ ) and in the minimization of the second objective  $F_2$ . Each  
 203 solution associates to these objectives a vector of parameters that fully define the COSVF for all  
 204 reservoirs.

## 205 2.5 Post-Pareto analysis

206 The output of a multi-objective optimization problem is the Pareto front, a set of non-dominated  
 207 ‘best’ solutions. This often contains hundreds of solutions which sometimes complicate the decision-  
 208 making process: which solution or group of solutions are preferred? This paper answers this using a  
 209 post-Pareto stage which prunes the non-dominated set of solutions following the concept of knee  
 210 points [42]. In knee points, small improvement in either of objectives will cause a large degradation  
 211 in other objective(s) [42]. This essentially means moving in either direction is less desirable. This  
 212 method is chosen owing to the fact that without any knowledge about users’ preferences, the zone  
 213 around the knee is most likely to be favourable for decision-makers [43].

214 Here, we measure the level of degradation of objectives by looking at slope (or difference) between  
 215 any two adjacent solution points from the Pareto trade-off. The judgement on when a severe  
 216 deterioration happened is made visually. This is where the slope notably changes compared to its  
 217 next immediate value. This process creates a box within which lies Pareto non-dominated solutions  
 218 with high optimality quality with respect to all objectives. This box is called “zone of concentration”.

## 219 2.6 Risk aversion coefficient

220 Since COSVFs are utility functions, a common way of comparing the two management practices (that  
221 is used to derive descriptive and prescriptive valuation) in terms of how cautious they are, is to  
222 illustrate it through risk aversion coefficient [37, 38]. This coefficient determines how much  
223 satisfaction or utility can be obtained from an experience, a commodity, or money [44]. We use  
224 Arrow-Pratt risk aversion coefficient ( $AP$ ), also known as absolute risk aversion coefficient, which is  
225 mathematically described as:

$$AP = -\frac{COSVF''(x_{t_{k+1}})}{COSVF'(x_{t_{k+1}})} \quad (10)$$

226 Considering the functional form of the quadratic COSVF used in this study ( $a$  and  $b$  being the  
227 quadratic and linear coefficients of COSVF respectively; see equation 21), the above equation for  
228 each reservoir  $sr$  is:

$$AP^{sr} = -\frac{2a_{t_{k+1}}^{sr}}{2a_{t_{k+1}}^{sr}x_{t_{k+1}} + b_{t_{k+1}}^{sr}} \quad (11)$$

229

## 230 3 Application

### 231 3.1 California's Central Valley

232 California's Central Valley (Figure 2) is one of the world's most productive agricultural regions [45]  
233 with over 2.3 million ha of irrigated farmland [46]. More than 250 different crops are grown in the  
234 Central Valley with an estimated value of \$17 billion per year [47]. About 75 percent of California's  
235 irrigated land is in the Central Valley, which depends heavily on surface water diversions and  
236 groundwater pumping [45]. Nearly 75 percent of renewable water supply originates in the northern  
237 third of the state in the wet winter and early spring while almost 80 percent of agricultural and  
238 urban water use is in the southern two-thirds of the state in the dry late spring and summer [48]. In  
239 the context of California's Mediterranean climate, perfect within-year foresight is consistent with  
240 early spring measurements of the depth and water content of the snowpack which enable predicting  
241 discharge months ahead with reasonable accuracy and until the end of the water year [49]. The  
242 Central Valley often suffers from droughts such as 1918-20, 1923-26, 1928-35, 1947-50, 1959-62,  
243 1976-77, 1987-92, 2007-09, and 2012-16 [50].





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**Figure 2.** The Central Valley reservoir and river system (Adopted from Khadem et al, 2018).

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The illustrative case of this paper is built upon CALifornia Value Integrated Network (CALVIN; [51]). CALVIN OP, a hydro-economic model [2] with perfect foresight, is the ‘unconstrained’ run of CALVIN used to simulate the Central Valley water system by maximizing the system-wide net economic benefit from water allocation. CALVIN OP applies economic drivers to allocate water rather than existing system of water rights and contracts [49]. Yet, the perfect hydrological foresight of CALVIN limits its applicability. We use an extended version of CALVIN OP for calibration which corrects the perfect foresight by dividing the planning horizon into year-long runs with initial condition of each run being the ending condition of the previous one and an end-of-year COSVF, representing the potential benefit of allocating water for future uses, set as the terminal condition of each run. Another extension to CALVIN comes from improving the groundwater pumping cost scheme. The CALVIN model represents pumping costs by multiplying the unit pumping cost of \$49.42 per MCM/m lift (\$0.20 per *af/ft* lift; MCM is a million  $m^3$ ) by a static estimate of the average pumping head in each aquifer [52]. The extended version of CALVIN includes pumping costs that dynamically vary with head in the aquifer. This head-dependent pumping cost introduces non-convexity into the problem.

261 The water system is represented as a network of nodes and arcs [53], where nodes include surface  
 262 and groundwater reservoirs, urban and agricultural demand points, junctions, etc., and arcs (links)  
 263 include canals, pipes, natural streams, etc.. The water network of the Central Valley comprises 30  
 264 surface reservoirs, 22 groundwater sub-basins, 21 agricultural demand sites, 30 urban demand sites,  
 265 220 junction and 4 outflows nodes; and over 500 links (river channels, pipelines, canals, diversions,  
 266 and recharge and recycling facilities). The period-of-analysis is 72 years, 1922-93, and monthly time-  
 267 steps are chosen for the hydro-economic model run. This accounts for the strong seasonality of  
 268 water supply and demands, a key feature of many irrigated water systems [54].

269

### 270 3.2 Model formulation

271 This section describes in detail how the generic equation (7) was implemented for this California  
 272 Central Valley application. For details, please see [6].  $f_t(\cdot)$ , the net benefit function at date  $t$ , is  
 273 composed of the following terms:

$$f_t(x_t, u_t, q_t) = UR_t(x_t) + AG_t(x_t) + HP_t(x_t) - NW_t(x_t) - GW_t(h_t, x_t) - INF_t(x_t) \quad (12)$$

with

$$UR_t(x_t) = \sum_{ur} a_t^{ur} x_t^2 + b_t^{ur} x_t \quad (13)$$

$$AG_t(x_t) = \sum_{ag} a_t^{ag} x_t^2 + b_t^{ag} x_t \quad (14)$$

$$HP_t(x_t) = \sum_{hp} x_t^{hp} PF_t^{hp} p_t \quad (15)$$

$$NW_t(x_t) = \sum_{i,j} c_t^{i,j} x_t^{i,j} \quad (16)$$

$$GW_t(x_t, u_t) = \sum_{gw,j} PC_t^{gw} x_t^{gw,j} \quad (17)$$

$$PC_t^{gw,j} = unitc \cdot (elev^{gw} - h_t^{gw}) \quad (18)$$

$$h_t^{gw} = h_{t-1}^{gw} + \frac{q_t^{gw} + \sum_j x_t^{j,gw} - \sum_j x_t^{gw,j}}{sc^{gw} \cdot area^{gw}} \quad (19)$$

$$INF_t(x_t) = \sum_{i,j} inf x_t^{i,j} \cdot m \quad (20)$$

274 Here,  $UR$  is the urban benefit (utility) function with  $a^{ur}$  and  $b^{ur}$  being the quadratic and linear  
 275 coefficients of the function respectively and  $x_t$  showing the flow to urban node  $ur$ ; Similarly,  $AG$  is  
 276 the agricultural benefits form allocating water to farms with  $a^{ag}$  and  $b^{ag}$  being the quadratic and  
 277 linear coefficients of the utility function respectively;  $HP$  is the linear economic benefit produced  
 278 from hydropower generation where  $PF$  is the power factor of hydropower plant  $hp$  that relates  
 279 release to hydropower generation and  $p$  is the monthly-varying hydropower unit price;  $NW$  shows  
 280 the network cost, cost incurred due to treatment, conveyance, and conjunctive uses with  $c$   
 281 representing such cost per unit of flow in link between nodes  $i$  and  $j$ ;  $GW$  is the groundwater cost  
 282 from aquifer  $gw$  which is the product of pumping cost  $PC$  and discharge rate  $x$ ;  $PC$  varies dynamically  
 283 as the piezometric head  $h$  in the aquifer changes. The calculation of  $PC$  follows storage coefficient  
 284 formulation [55] where a unit pumping cost  $unitc$  is multiplied by the distance that water needs to  
 285 be lifted to reach ground level for allocation.  $elev$  is the mean ground elevation above aquifer  $gw$ .  
 286 According to the storage coefficient formulation,  $sc$  is the mean storage coefficient and  $area$  is the  
 287 surface area of an aquifer.  $INF$  represents the infeasibility costs. Numerical infeasibilities may appear  
 288 in the model, making the network problem infeasible. In order to guarantee feasibility, artificial

289 inflows (*infx*) are made available to the model at each node. These flows are included in model's  
290 conservation of mass equations to ensure that such flows are accounted for. These artificial flows  
291 which are in fact slack/surplus variables in a mathematical programming context, are not desirable  
292 therefore in order to deter the model from introducing infeasibility flows, they are penalised by a  
293 high cost (*m*) coefficient in the objective function.

294 In implementing above equations for the case of California Central Valley few points must be  
295 considered: (1) A piece-wise linear equivalent of equation (14) was used for farms. This was due to  
296 the slope of the benefit function (marginal value of water delivered) at or near full demand being  
297 zero which caused farmers to opt not pumping as it would be more economic to not pay for  
298 groundwater pumping costs while any additional unit of allocated water produces near zero benefit.  
299 (2) In California, the presence of "high-head" facilities where the effect of reservoir storage on  
300 turbine head is small allows for a linear relationship between head and hydropower generation [56,  
301 57].

302 As explained in Section 2, the model is solved sequentially on a year-by-year basis for all the 72  
303 hydrological years considered, using the maximization problem defined by equation (5). In that  
304 equation, end-of-year COSVFs are set as boundary conditions at the end of each year-long model run  
305 to prevent depletion of reservoirs. This function represents the potential benefit gained from not  
306 releasing for immediate uses and preserving water for future droughts. End-of-year COSVFs are  
307 quadratic utility function:

$$COSVF_t(\pi; x_t) = \sum_{sr} a_t^{sr} x_t^2 + b_t^{sr} x_t \quad \forall t = t_{k+1} \quad (21)$$

308 where  $a^{sr}$  and  $b^{sr}$  are the quadratic and linear coefficient of the COSVF for reservoir  $sr$ , deduced from  
309 the demand curve parameters  $\pi$  using equations (1) and (2). In this case, the end of year is the end  
310 of the water year, that is, September 30 in the U.S.

311

### 312 3.3 Historical benchmark

313 In order to produce water marginal values that are descriptive of historical operations, storage data  
314 from a historical benchmark are required. In the Central Valley, this benchmark is CALVIN BC, a 'base  
315 case' or 'constrained' run of the CALVIN model which applies constraints to reproduce historical  
316 events [51]. It is used because observed storage data is not available for all reservoirs for the entire  
317 period of analysis. CALVIN BC is an effort to integrate surface and groundwater hydrology developed  
318 for the two models of the Central Valley's water system, i.e., DWRSIM and CVGSM. It reconciles  
319 inconsistent assumptions in these two separate models, as well as agricultural water demand  
320 assumptions with water deliveries. More details on CALVIN BC's modeling approach and  
321 assumptions can be found in [51]. Khadem et. al., [6] compared observed storage level data of  
322 Shasta, the largest reservoir in the Central Valley, with those of CALVIN BC's and demonstrated a  
323 close match between them. As such, we refer to CALVIN BC's results as the historical benchmark  
324 hereafter [58].

325

### 326 3.4 Getting water values

327 Borg [59] was used as the multi-objective evolutionary algorithm (MOEA) because Borg's self-  
328 adaptive features increase its robustness and effectiveness while minimizing the search  
329 parametrization by the user. Borg has been proved to be a top performing MOEA in systems

330 comprising nonlinearities [60] and for multi-objective reservoir management problems [61]. There  
 331 are 30 surface reservoirs, so there are 60 decision variables for the evolutionary algorithm to find.  
 332 End-of-year carryover storage values are positive and bounded by the maximal value among the  
 333 urban and agricultural water demand curves, i.e., \$5,291,378 per MCM. For the case study, an initial  
 334 population size of 100, 100,000 maximum number of function evaluations as the stopping criterion,  
 335 and epsilon (search resolution) value of 100,000 MCM<sup>2</sup>, \$1,000,000, and \$8,107 per MCM (\$10 per  
 336  $\alpha$ ) for the objective functions ( $F_{desc}$ ,  $F_{pres}$ , and  $F_2$  respectively) were used. The nonlinear hydro-  
 337 economic model of the California system was coded in Generalized Algebraic Modeling System  
 338 (GAMS) and solved using the Minos solver version 5.5 [62]. Minos applies the generalized reduced  
 339 gradient method, which is suitable for nonlinear programming problems with linear constraints  
 340 [63]. The case presented here was solved using 96 Intel processors working jointly on a Unix-based  
 341 computing cluster. Results took about 45,000 hours of computation time to produce for the  
 342 descriptive valuations and 42,000 for the prescriptive valuation (see [6]).

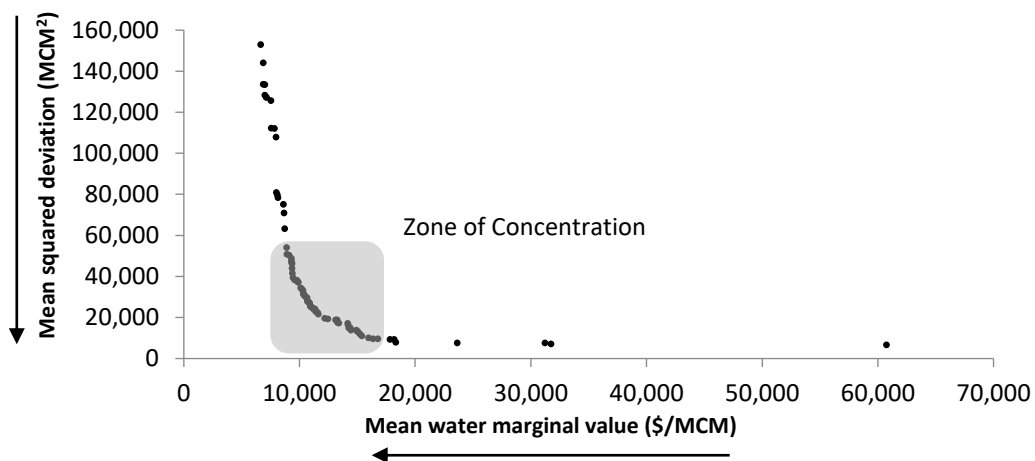
### 343 4 Results

344 This section uses the solution analysed in-depth in [6] as the prescriptive solution. For this reason,  
 345 Section 4.1 and 4.2 focus respectively on the obtaining of descriptive valuations and on their fit with  
 346 the historical benchmark. Then, Section 4.3 compares the two valuations and Section 4.4  
 347 investigates what they mean for water management in the Central Valley.

#### 348 4.1 Trade-off analysis for the descriptive valuation of storage

349 A five-seed Random Seed (RS) analysis was performed to obtain the Pareto trade-off and to ensure  
 350 robust algorithm convergence towards the same Pareto-set. By definition, a Pareto front (Figure 3)  
 351 consists of non-dominated solutions with respect to the two objective functions, where any  
 352 improvement on the value of either objective function comes at the expense of the other.

353



354

355 **Figure 3.** Pareto non-dominated solutions of the two objective functions (arrows show the direction of  
 356 preference).

357 This analysis focuses on the zone of concentration (ZC) within the Pareto set (grey box in Figure 3, as  
 358 outlined in section 2.5). Concentration of solution points in this zone suggest that the estimate for  
 359 historical water marginal values can be sought there. The analysis will consider both this ensemble

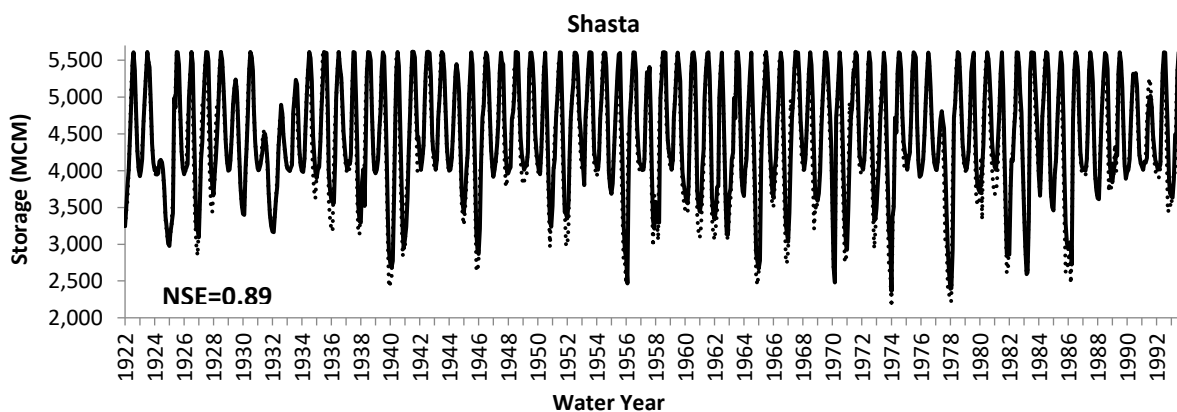
360 of solutions and a “representative solution” obtained by simulating the system using for each  
361 reservoir the average  $p_{min}$  and  $p_{max}$  across all solutions within the zone of concentration.

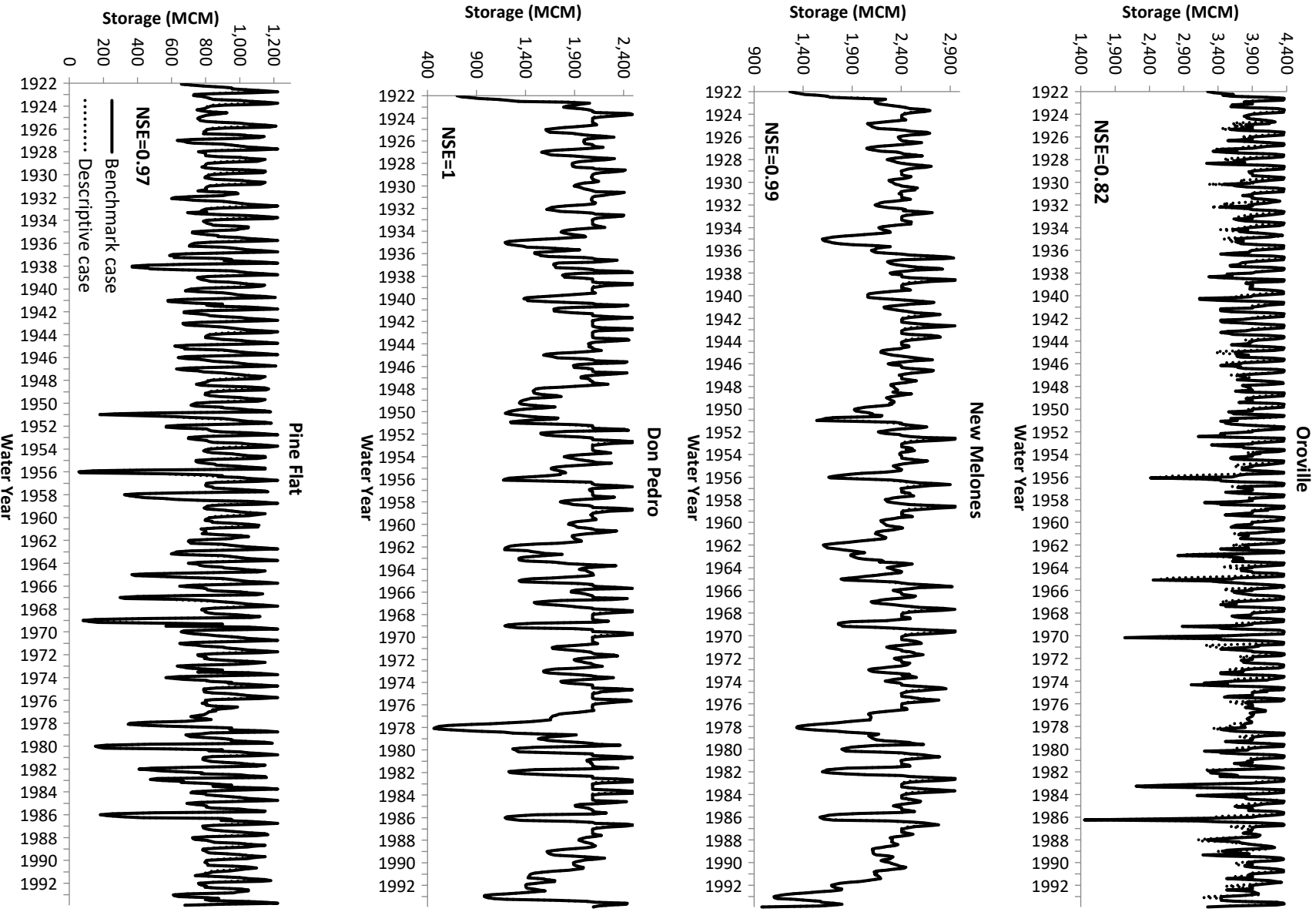
362

#### 363 4.2 Quality of the fit with the historical benchmark

364 The quality of the fit is evaluated through the classical Nash-Sutcliffe efficiency criterion (NSE; [64])  
365 at individual reservoirs by comparing benchmark historical storage values with storage from the  
366 representative solution (Table 1 and Figure 4). NSE is chosen as a goodness-of-fit criterion because it  
367 is coherent with the MOEA’s first objective; it determines the relative magnitude of the residual  
368 variance compared to the observed data variance [65]. It has a range of  $(-\infty, 1]$ , with NSE=1  
369 indicating a complete match between the modeled and observed values. A value between 0 and 1  
370 shows an acceptable calibration performance and a negative NSE means that observed value is a  
371 better predictor than the simulated value, which indicates unacceptable performance. In Table 1,  
372 NSE values ranging from 0.82 to 1 indicate an excellent fit with the historical benchmark, which  
373 becomes close to perfection for some reservoirs (Figure 4). To better understand the quality of  
374 different solutions across the Pareto trade-off (Figure 3), solutions with the best and worst quality  
375 (those with lowest and highest value of  $F_{desc}$  respectively) are compared to the representative  
376 solution (average of solutions from zone of concentration) in Table 1. The quality of fit is also  
377 expressed by the fact that average relative deviations from the historical benchmark are relatively  
378 low.

379 This quality-of-fit at individual reservoirs holds across the ensemble of solutions within the zone of  
380 concentration, because operations are robust to different water valuations within this zone.  
381 Supplementary material illustrates this with three of the system’s major reservoirs. This said, it is  
382 worth noting that the zone of concentration figures a range of valuations and not a single valuation,  
383 be it at dead storage (Figure 5.a) or full storage (Figure 5.b). This means that this range, and not only  
384 the representative solution, must be used when comparing descriptive and prescriptive storage  
385 valuations.





386 **Figure 4.** Comparison of the calibrated storage trajectories of major reservoirs to the benchmark values.

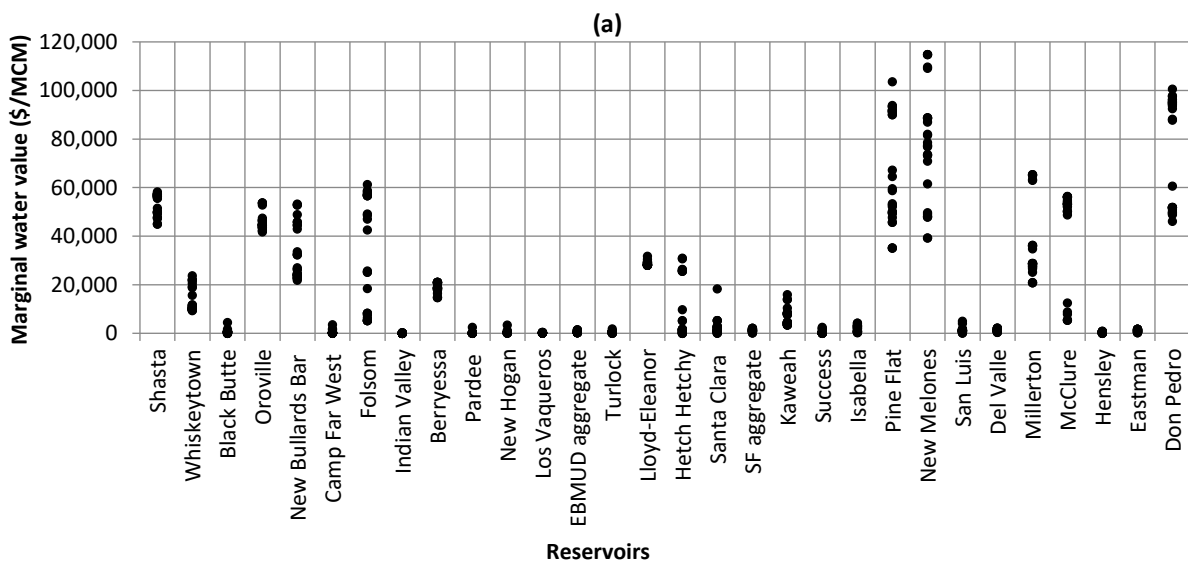
387 **Table 1.** Quality of fit quantified by Nash-Sutcliffe efficiency and deviation from observed values as a percentage of storage  
 388 capacity for the 30 reservoirs of the Central Valley system. Values are presented for three solution qualities from the

389 Pareto trade-off (Figure 3): Worst NSE with the lowest value of Y axis, Average NSE with the values from the average of  
 390 zone of concentration (ZC)-this is also called representative solution, and Best NSE with the highest value of Y axis.

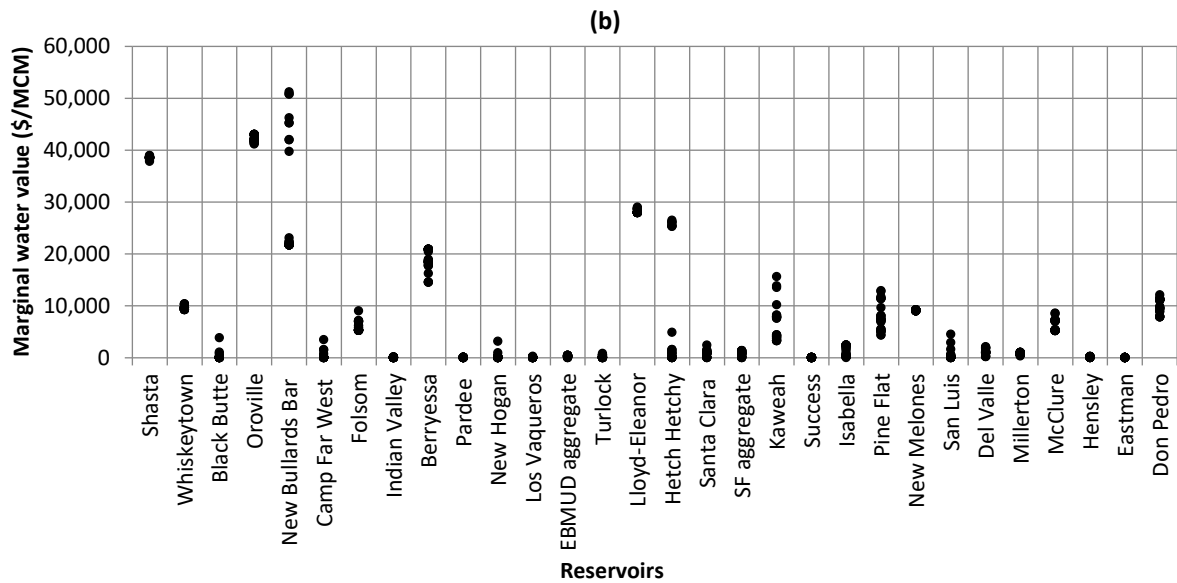
Reservoirs	Worst NSE		Average of ZC NSE		Best NSE	
	NSE	Deviation (%)	NSE	Deviation (%)	NSE	Deviation (%)
Shasta	0.87	3.29	0.89	3.12	0.95	2.31
Whiskeytown	0.60	10.11	0.92	3.05	0.97	2.13
Black Butte	0.82	9.42	0.97	3.53	0.98	2.50
Oroville	0.78	2.85	0.82	1.51	0.98	0.47
New Bullards Bar	0.94	4.19	0.95	3.27	0.95	3.17
Camp Far West	0.87	7.46	0.99	2.04	0.99	1.15
Folsom	0.91	5.09	0.94	3.96	0.96	3.22
Indian Valley	0.99	1.78	1.00	0.12	1.00	0.12
Berryessa	0.99	1.40	0.99	1.23	0.99	1.20
Pardee	0.93	5.13	0.99	1.72	1.00	0.12
New Hogan	0.95	4.50	0.98	2.26	0.98	2.05
Los Vaqueros	0.65	5.32	0.97	1.00	1.00	0.21
EBMUD	0.66	4.53	0.94	1.63	0.98	0.67
New Melones	0.98	1.02	0.99	0.61	0.99	0.49
Turlock	0.55	9.16	0.82	4.97	0.87	3.43
Lloyd-Eleanor	0.96	4.09	0.98	2.38	0.99	1.68
Don Pedro	0.99	1.02	1.00	0.19	1.00	0.12
Hetch Hetchy	0.93	5.86	0.96	3.46	0.96	2.73
Del Valle	0.59	10.37	0.80	2.35	1.00	0.14
San Luis	0.97	1.12	1.00	0.15	1.00	0.03
Santa Clara	0.57	12.92	0.91	5.05	0.96	2.98
SF aggregate	0.22	8.74	0.79	4.03	0.93	1.87
McClure	0.98	2.10	0.99	1.32	0.99	1.14
Eastman	0.89	4.45	0.96	2.45	0.96	1.83
Hensley	0.57	11.50	0.91	5.22	0.94	3.73
Kaweah	0.75	8.62	0.96	5.51	0.97	3.07
Success	0.78	11.27	0.95	5.12	0.97	3.95
Isabella	0.98	2.00	0.99	1.21	0.99	1.09
Pine Flat	0.95	3.04	0.97	1.69	0.97	1.51
Millerton	0.96	3.43	0.99	0.95	0.99	0.65

Note: EBMUD stands for East Bay Municipal Utility District and SF is San Francisco.

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**Figure 5.** Dispersion of descriptive marginal water value solutions from zone of concentration at: a) dead storage, and b) full storage.

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### 4.3 Comparison of reservoir storage valuations

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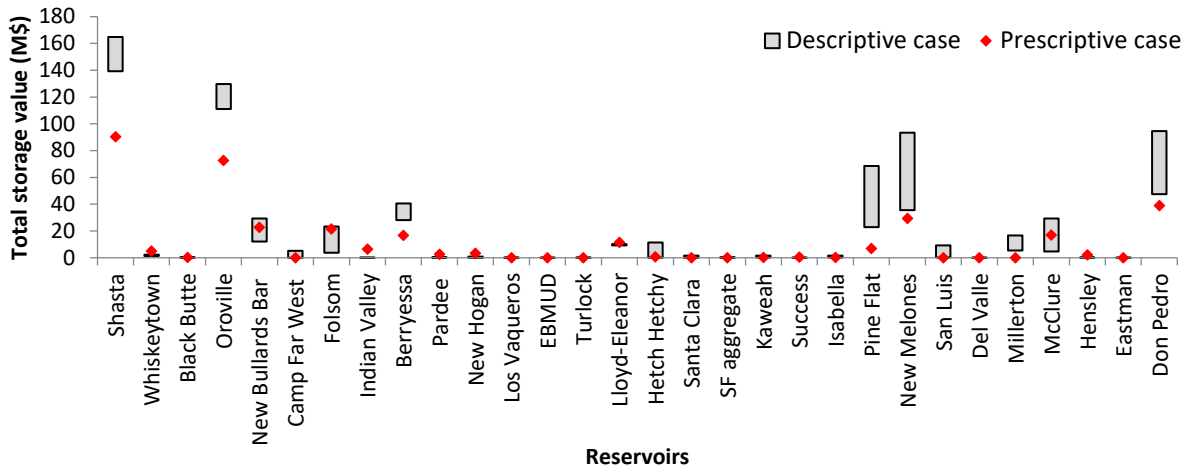
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Having verified that the descriptive valuation of water storage led to a good fit between the benchmark historical operations and simulated operations, we compare the descriptive and prescriptive storage valuations, using both the ensemble of descriptive solutions (Figure 6), and the representative solution (Table 2). Column (1) of Table 2 contains active storage (full storage – dead storage) of surface reservoirs in the last month of the water year, i.e. September. Note that maximum capacity varies per month due to flood control requirements. The second column shows the annual net inflow calculated as annual surface runoff minus any loss (e.g. seepage and evaporation). Columns (3) and (4) include the descriptive marginal water values for the representative solution. Values in column (5) are the average of values in columns (3) and (4), which corresponds to the average marginal value of water from the representative solution – total water value (Figure 6) is then the product of that figure and the active storage. Column (5) of Table 2 can be used as an economic proxy for comparing reservoirs valuation, and to contrast descriptive valuation against its prescriptive counterpart (column 6).



412



413

414 **Figure 6.** Distribution of the total storage value from the solution points of the zone of concentration. Red  
 415 points show the maximum COSVF of the prescriptive solution.

416 **Table 2.** Descriptive marginal water values of end-of-year surface reservoirs' storage in the Central Valley,  
 417 listed from north to south compared with prescriptive values.

Reservoir	End-of-year active storage (MCM) (1)	Annual average net inflow (MCM) (2)	Descriptive marginal value at dead storage (\$/MCM) (3)	Descriptive marginal value at full storage (\$/MCM) (4)	Descriptive average marginal value (\$/MCM) (5)	Prescriptive average marginal value (\$/MCM) (6)
Shasta	3,344	6,816	52,666	38,549	45,608	29,576
Whiskeytown	138	1,144	12,484	9,542	11,013	39,923
Black Butte	122	488	480	189	334	393
Oroville	2,682	4,966	45,830	42,139	43,985	22,263
New Bullards Bar	560	1,496	32,382	28,429	30,406	38,775
Camp Far West	126	458	1,872	1,817	1,844	108
Indian Valley	731	529	15	13	14	10,825
Folsom	701	3,271	27,638	5,830	16,734	34,979
Berryessa	1,926	438	18,915	18,865	18,890	10,656
Pardee	235	840	107	14	60	13,334
New Hogan	263	184	347	120	234	15,416
New Melones	1,507	1,285	74,067	9,108	41,588	19,500
EBMUD	63	0	516	286	401	48
Los Vaqueros	41	0	145	27	86	8
Lloyd-Eleanor	333	542	28,437	28,129	28,283	27,953
Hetch Hetchy	399	936	7,911	7,104	7,507	1,403
Del Valle	23	0	1,273	1,181	1,227	276
Don Pedro	1,727	792	69,837	10,213	40,025	23,716
Turlock	69	0	369	94	232	182
McClure	907	1,128	42,123	5,940	24,032	20,314
SF aggregate	277	0	1,071	650	860	0
Eastman	99	82	959	10	485	264
Santa Clara	209	156	1,766	727	1,246	89
Hensley	79	101	329	135	232	30,892

San Luis	1,958	0	1,275	467	871	1
Millerton	495	2,082	35,190	747	17,969	37
Pine Flat	1,177	2,041	63,661	7,752	35,706	5,767
Kaweah	101	581	5,884	5,747	5,816	913
Success	81	170	281	8	144	5,387
Isabella	453	876	1,670	1,011	1,340	526

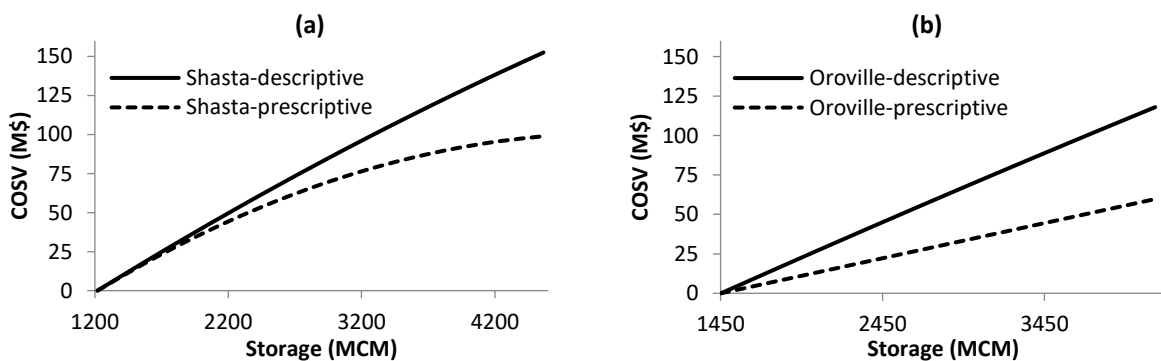
Note: EBMUD stands for East Bay Municipal Utility District and SF is San Francisco.

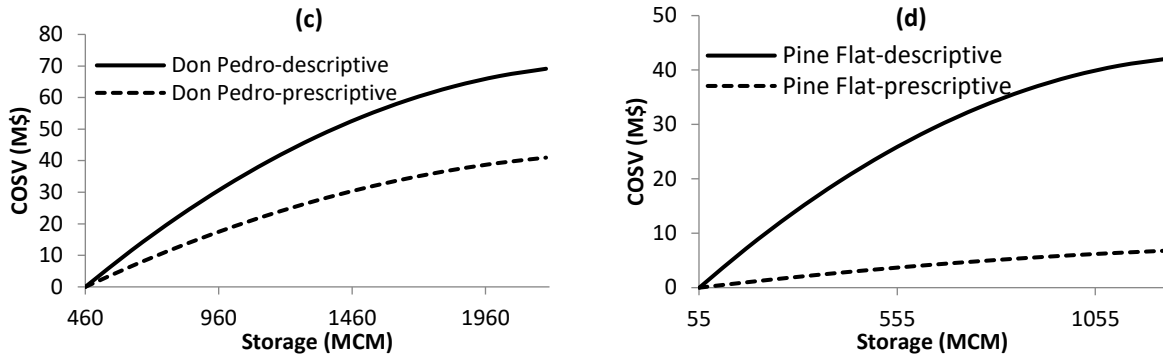
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419 Compared with the prescriptive valuation, the descriptive one is higher for most major reservoirs.  
 420 Examples are Shasta, Oroville, Berryessa, New Melones, Don Pedro, San Luis, and Pine Flat; and  
 421 those located in the Sierra Nevada on the eastern range of the Central Valley (e.g. Oroville, New  
 422 Bullards Bar, Folsom, New Melones, Lloyd & Eleanor, Don Pedro, McClure, and Pine Flat – note how  
 423 some reservoirs make both groups). These results hold for both Figure 6 and Table 2. This higher  
 424 valuation in the descriptive solution means that operations conserve surface water in large reservoir  
 425 by implicitly valuing it more than in smaller surface reservoirs and groundwater reservoirs alike. This  
 426 has two consequences: (1) groundwater resources are first to supply water; and (2) when it comes  
 427 to surface reservoirs, smaller reservoirs are prioritised for release. End-of-year COSVF for each  
 428 reservoir can be derived from values in columns (3) and (4) of Table 2.

429 COSVF of four large Central Valley reservoirs are compared (Figure 7). To better interpret this result,  
 430 one can look at the average volumetric water value of these four reservoirs at their full storage i.e.  
 431 maximum of COSV divided by maximum storage capacity. For the descriptive case, the average  
 432 volumetric water values at full storage are 33419, 28527, 31605, and 34086 \$/MCM for Shasta,  
 433 Oroville, Don Pedro, and Pine Flat respectively. This suggests that attitudes to water conservation in  
 434 the historical benchmark are similar across these large reservoirs, regardless of their situation within  
 435 the basins. For the prescriptive case however, the same figures drop to 21672, 14439, 18727, and  
 436 5505 \$/MCM respectively. This suggests different water storage values depending on location within  
 437 the basin: reservoirs situated upstream can redirect water for use in larger portions of the basin and  
 438 this makes them more valuable than reservoir situated downstream. More generally, the  
 439 comparison of these valuations confirms that the descriptive case values stored water more than the  
 440 prescriptive case, regardless of location.

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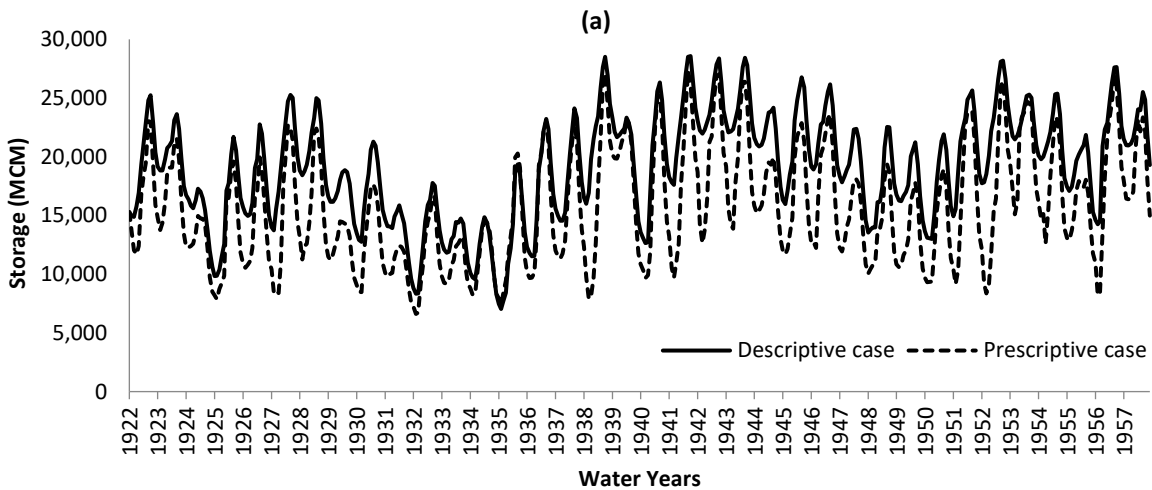


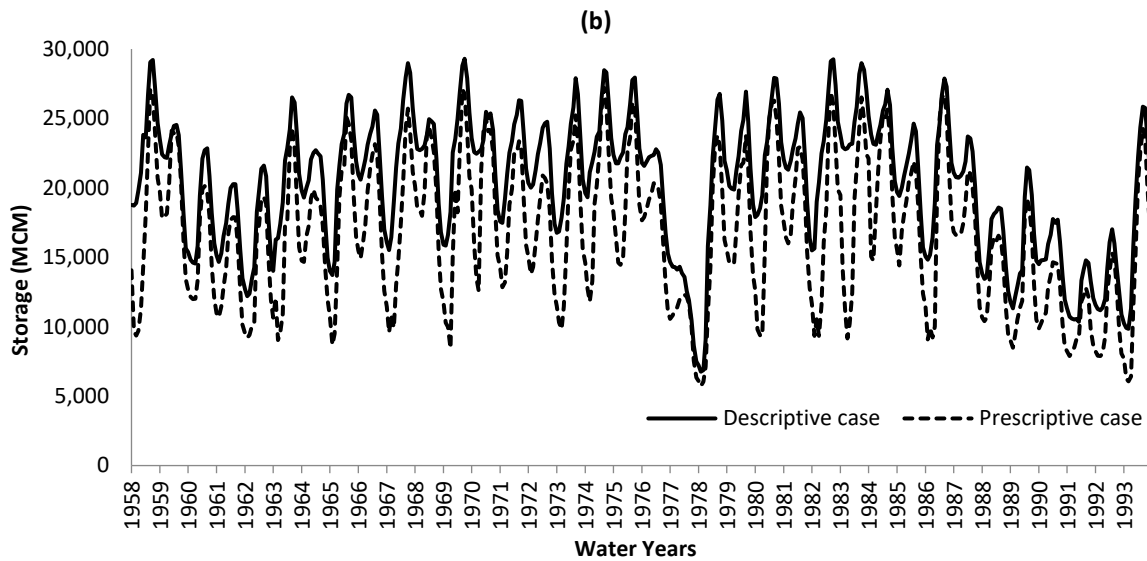


442 **Figure 7.** Comparison of the representative solution in descriptive and normative valuation, COSV of  
 443 reservoirs in (a) Shasta, (b) Oroville, (c) Don Pedro, and (d) Pine Flat.

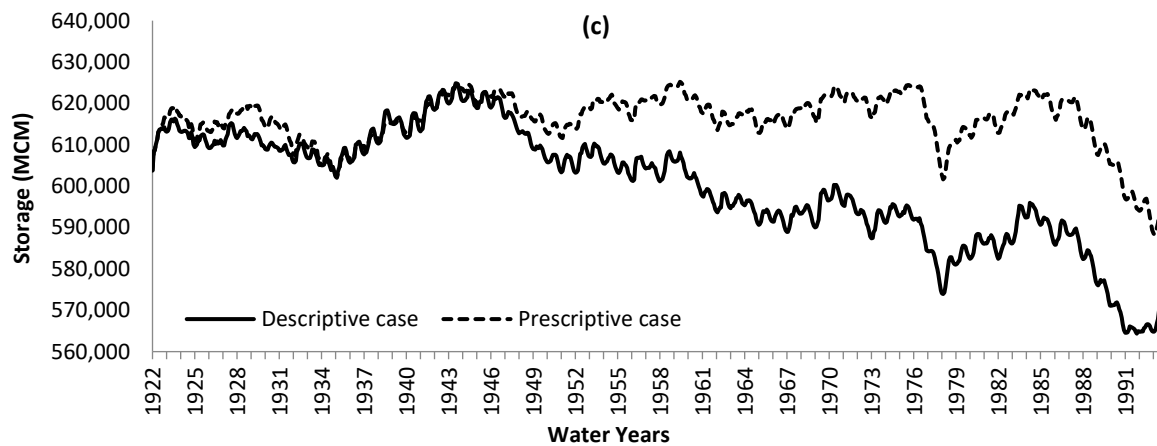
444 **4.4 Consequences for water management in California**

445 The system-wide consequences of the difference between the two valuations of water storage are  
 446 clear through comparison of aggregated surface and groundwater storage during 1922-93 (Figure 8).  
 447 Implicit overvaluation of surface reservoirs with operations based on a descriptive valuation resulted  
 448 in a comparative overexploitation of aquifers. At the level of individual reservoirs, columns (1) and  
 449 (5) of Table 2 show that the historical operation favoured smaller reservoirs when it comes to  
 450 surface reservoir releases. This can become problematic when a small reservoir is the sole supplier  
 451 to a demand site (e.g. New Hogan supplying for Stockton). This overcautious operation has led to  
 452 80% increase in the annual average scarcity volume [6] compared with operations derived from an  
 453 “optimal”, prescriptive valuation, and to a 5% increase in the average unit pumping cost across the  
 454 Central Valley.





456



457

458 **Figure 8.** Comparison of the historical simulation and the optimized model for: a) surface reservoirs over 1922-  
 459 57; b) surface reservoirs over 1958-93; and c) groundwater over 1922-93.

460 To better demonstrate how risk averse the two reservoir operations are, the absolute risk aversion  
 461 coefficient for each reservoir is computed and illustrated in Table 3. COSVFs derived from (equation  
 462 1) the obtained marginal water values of Table 2 for the descriptive model and [6] for the  
 463 prescriptive model, are used to calculate the risk aversion (*AP*).

464 **Table 3.** Absolute risk aversion coefficient for each reservoir of the descriptive and the prescriptive model.  
 465 Note that wherever no *AP* is reported, the first derivative of the COSVF i.e. marginal water value is zero.

Reservoirs	September storage (MCM)			AP of the descriptive model (1/MCM)			AP of the prescriptive model (1/MCM)		
	Dead storage	Mean storage	Full storage	at dead storage	at mean storage	at full storage	at dead storage	at mean storage	at full storage
Shasta	1,220	2,892	4,564	0	0	0	0	0	0.002
Whiskeytown	152	221	290	0.002	0.002	0.002	0.006	0.011	0.048
Black Butte	12	73	134	0.005	0.007	0.013	0.008	0.016	-
Oroville	1,453	2,794	4,135	0	0	0	0	0	0.000
New Bullards Bar	310	590	870	0	0	0	0.001	0.002	0.003
Camp Far West	1	64	127	0	0	0	0.007	0.012	0.052
Folsom	102	453	803	0.001	0.002	0.005	0.001	0.002	0.016

Indian Valley	0	366	731	0	0	0	0.001	0.003	2.274
Berryessa	13	976	1,939	0	0	0	0.001	0.001	-
Pardee	15	133	250	0.004	0.007	0.028	0.004	0.008	-
New Hogan	22	153	285	0.002	0.004	0.007	0.004	0.008	4.675
Los Vaqueros	89	109	130	0.020	0.034	0.107	0.025	0.049	-
EBMUD	102	134	165	0.007	0.009	0.013	0.016	0.032	-
Turlock	14	48	83	0.011	0.017	0.042	0.014	0.029	-
Lloyd-Eleanor	38	205	371	0	0	0	0	0	0
Hetch Hetchy	45	245	444	0	0	0	0	0	0
Santa Clara	46	128	210	0.004	0.005	0.009	0.005	0.009	0.035
SF aggregate	38	158	278	0.002	0.002	0.003	-	-	-
Kaweah	1	51	101	0	0	0	0.010	0.020	-
Success	1	41	81	0.012	0.023	0.444	0.012	0.025	-
Isabella	0	226	453	0.001	0.001	0.001	0.002	0.003	0.011
Pine Flat	56	645	1,233	0.001	0.001	0.006	0.001	0.001	0.002
New Melones	978	1,732	2,485	0.001	0.001	0.005	0	0.001	0.002
San Luis	99	1,078	2,057	0	0	0.001	0.001	0.001	-
Del Valle	12	23	35	0.003	0.003	0.003	0.045	0.089	-
Millerton	148	395	643	0.002	0.004	0.093	0.002	0.004	-
McClure	143	596	1,050	0.001	0.002	0.007	0.001	0.002	0.006
Hensley	5	44	84	0.007	0.011	0.018	0.013	0.025	-
Eastman	12	62	111	0.010	0.020	0.948	0.009	0.017	0.124
Don Pedro	460	1,324	2,187	0	0.001	0.003	0	0.001	0.002
Aggregate storage	5,586	15,957	26,329	0.097	0.157	1.761	0.190	0.372	7.252

466 Table 3 reveals that the prescriptive model is in fact more risk averse in the face of uncertain  
467 hydrology. This is consistent with the fact that prescriptive operations minimize shortage. Less  
468 intuitively, it shows that even though they value surface water storage more, operations observed in  
469 the historical benchmark are not necessarily less risk averse. In fact, this higher valuation is linked  
470 with excessive water conservation for future uses in a way that sometimes penalises current uses.  
471 This behaviour could be explained by regulatory constraints that water managers have to deal with,  
472 but that the model does not account for, such as stream temperature requirements that necessitate  
473 cold water released from deep reservoirs lakes to favour salmon habitats.

## 474 5 Discussion and Conclusion

475 This paper proposes a methodology to derive comparable descriptive and prescriptive valuations of  
476 water storage. In both approaches, values are deduced from a hybrid setup where an EA is linked to  
477 a hydro-economic model. While EA searches for the value of stored water, the role of the hydro-  
478 economic model is to link water allocation decisions with the space and time distribution of the  
479 value of stored water for future uses. In the prescriptive approach, the EA aims at optimizing long-  
480 term benefits from water use, whereas in the descriptive approach, the objective is to provide a  
481 valuation that calibrates a historical benchmark. To avoid unrealistic storage valuations in small  
482 reservoirs, an auxiliary objective is introduced, meaning that both problems are formulated as being  
483 multi-objective, and solved using an MOEA. The resulting modeling approach is generalizable  
484 because 1) its applicability is not plagued by the curse of dimensionality linked with system size, and

485 2) it is assumption free, e.g., it does not require non-convexity assumptions that do not apply in  
486 conjunctive use systems. The proposed approach is illustrated through valuation of 30 surface  
487 reservoirs in California's Central Valley water system.

488 The descriptive approach is descriptive insofar as it matches a historical benchmark whose outcome  
489 – storage levels across time and space – reflects the regulatory and institutional setting that resulted  
490 in the operations that led to this outcome. Yet, the approach itself is not based on simulation but on  
491 hybrid optimization, in that it uses an intra-annual optimization model coupled with an EA. The EA  
492 calibrates water marginal values to find those that replicate real-world observations. This is done by  
493 first taking water marginal values as EA's decision variables (calibration parameters). EA randomly  
494 assigns values to these parameters and the water resources system is simulated using these values  
495 and a hydro-economic model. Note that this optimization-based descriptive approach, though  
496 counter-intuitive, is necessary to adequately compare descriptive and prescriptive valuations. This  
497 approach is generalizable and can readily be used when market valuation is absent or inefficient and  
498 when non-market methods are plagued with non-convexity and/or curse of dimensionality. Yet, the  
499 necessity to assume intra-annual foresight means that this approach may be difficult to apply to  
500 tropical and temperate areas where runoff is not snow-dominated.

501 Results are also interesting in several respects. First, they vindicate the choice to represent intra-  
502 annual operations with a perfect foresight optimization models. This indicates that this complex  
503 system could be simulated with this simple assumption. In particular, it shows that regardless of the  
504 uncertainty concerning snowpack, monthly operations are robust to the consequences of that  
505 uncertainty. This robustness may break down on a finer, e.g. daily, timescale, but it is worth noting  
506 that most state-of-the-art global hydrological models representing complex multi-reservoir systems  
507 use a monthly time step [66], and that their results are not yet accurate enough [67] to justify a finer  
508 time resolution.

509 Beyond, the comparison of descriptive and prescriptive operations is a two-way street. On one hand,  
510 it provides insights into the differences between the historical benchmark and optimized operations,  
511 by providing comparable valuations of surface water storage. In the case of California, this translates  
512 into showing how surface water valuation leads to using groundwater instead. On the other hand,  
513 interpreting this finding beyond the confines afforded by the models' formulation provides insights  
514 into possible causes of historical management decisions. For instance, the quality of the calibration  
515 given constant storage valuations, constant groundwater pumping costs, and constant crop prices,  
516 shows a remarkable stability of their relative values throughout most of the twentieth century. But  
517 both groundwater pumping costs and crop retail prices have changed through time: the storage  
518 valuation could suggest that cheap energy may have favoured mining groundwater – a resource for  
519 which no strong management institutions exist in California – whereas surface water rights ensured  
520 a greater conservation of surface water. This would link cheap energy prices with unsustainable  
521 water management practices, a speculative insight that deserves further investigation. More  
522 generally, the difference in surface water valuation from the two approaches reflects the role of  
523 institutions providing incentives for surface water conservation, and that are traditionally difficult to  
524 represent in an optimization model of that size. This was evidenced by further analysis involving risk  
525 aversion coefficients. The exercise revealed that the prescriptive valuation showed a more risk-  
526 averse approach to managing water resources. The overcautious operation observed in the historical  
527 benchmark was perhaps due to other constraints not seen in the model.

528 Finally, it is worth elaborating on the fact that different storage valuations could lead to a similar fit  
529 of the descriptive model with the historical benchmark it is meant to reproduce. The existence of  
530 different parametrisations leading to similar goodness-of-fit is well-known in hydrology as

531 equifinality [68, 69]. Equifinality had also been found in water resources systems models, but only in  
532 the fact of producing very different reservoir operations leading to similar value of an economic  
533 objective [70, 71]. In the descriptive approach proposed here, the opposite occurs as, similar to  
534 hydrological modeling; different parametrisations lead to similar operations. This finding runs  
535 contrary to the idea that there exists a unique water price that water markets can organically find to  
536 arrive to a near-optimal solution.

537

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## References

- 550 1. Cai, X.M., *Implementation of holistic water resources-economic optimization models for river*  
551 *basin management - Reflective experiences*. Environmental Modelling & Software, 2008.  
552 **23**(1): p. 2-18.
- 553 2. Harou, J.J., et al., *Hydro-economic models: Concepts, design, applications, and future*  
554 *prospects*. Journal of Hydrology, 2009. **375**(3-4): p. 627-643.
- 555 3. Pulido-Velazquez, M., E. Alvarez-Mendiola, and J. Andreu, *Design of Efficient Water Pricing*  
556 *Policies Integrating Basinwide Resource Opportunity Costs*. Journal of Water Resources  
557 Planning and Management, 2013. **139**(5): p. 583-592.
- 558 4. Pulido-Velazquez, M., J. Andreu, and A. Sahuquillo, *Economic optimization of conjunctive use*  
559 *of surface water and groundwater at the basin scale*. Journal of Water Resources Planning  
560 and Management, 2006. **132**(6): p. 454-467.
- 561 5. Tilmant, A., D. Pinte, and Q. Goor, *Assessing marginal water values in multipurpose*  
562 *multireservoir systems via stochastic programming*. Water Resources Research, 2008. **44**(12).
- 563 6. Khadem, M., et al., *Estimating the Economic Value of Interannual Reservoir Storage in Water*  
564 *Resource Systems*. Water Resources Research, 2018. **54**(11): p. 8890-8908.
- 565 7. Howitt, R.E., *Positive Mathematical Programming*. American Journal of Agricultural  
566 Economics, 1995. **77**(2): p. 329-342.
- 567 8. Cai, X. and D. Wang, *Calibrating holistic water resources-economic models*. Journal of Water  
568 Resources Planning and Management, 2006. **132**(6): p. 414-423.
- 569 9. Kang, M. and S. Park, *Modeling water flows in a serial irrigation reservoir system considering*  
570 *irrigation return flows and reservoir operations*. Agricultural Water Management, 2014. **143**:  
571 p. 131-141.
- 572 10. Thayer, M.A., *Contingent valuation techniques for assessing environmental impacts: Further*  
573 *evidence*. Journal of Environmental Economics and Management, 1981. **8**(1): p. 27-44.
- 574 11. Hadjigeorgalis, E., *A Place for Water Markets: Performance and Challenges*. Review of  
575 Agricultural Economics, 2009. **31**(1): p. 50-67.
- 576 12. Hansen, K.M., R. Howitt, and J. Williams, *An Econometric Test of Water Market Structure in*  
577 *the Western United States*. Natural Resources Journal, 2014. **55**(1): p. 127-152.
- 578 13. Wheeler, S.A., et al., *Developing a water market readiness assessment framework*. Journal of  
579 Hydrology, 2017. **552**: p. 807-820.
- 580 14. Wheeler, S.A., et al., *Evaluating water market products to acquire water for the environment*  
581 *in Australia*. Land Use Policy, 2013. **30**(1): p. 427-436.
- 582 15. Garrick, D.E., N. Hernández-Mora, and E. O'Donnell, *Water markets in federal countries:*  
583 *comparing coordination institutions in Australia, Spain and the Western USA*. Regional  
584 Environmental Change, 2018. **18**(6): p. 1593-1606.
- 585 16. Lewis, D. and H. Zheng, *How could water markets like Australia's work in China?* International  
586 Journal of Water Resources Development, 2018: p. 1-21.
- 587 17. Owens, K., *Environmental Water Markets and Regulation: A comparative legal approach*.  
588 2016: Taylor & Francis.
- 589 18. Erfani, T., O. Binions, and J.J. Harou, *Protecting environmental flows through enhanced water*  
590 *licensing and water markets*. Hydrol. Earth Syst. Sci., 2015. **19**(2): p. 675-689.
- 591 19. Parker, F., *The legalities of competition in water markets - Comparing Scotland with England*  
592 *and Wales*. Journal of Water Law, 2007. **18**(5): p. 167-170.
- 593 20. Livingston, M.L., *Designing water institutions: Market failures and institutional response*.  
594 Water Resources Management, 1995. **9**(3): p. 203-220.
- 595 21. Casado Pérez, V., *Missing Water Markets: A Cautionary Tale of Governmental Failure*. NYU  
596 Environmental Law Journal, 2015. **21**: p. 85.
- 597 22. Grafton, R.Q., J. Horne, and S.A. Wheeler, *On the Marketisation of Water: Evidence from the*  
598 *Murray-Darling Basin, Australia*. Water Resources Management, 2016. **30**(3): p. 913-926.



- 599 23. Marques, G.F., et al., *Economically driven simulation of regional water systems: Friant-Kern, California*. Journal of Water Resources Planning and Management, 2006. **132**(6): p. 468-479.
- 600
- 601 24. Scarcelli, R.O.C., et al., *Ensemble of Markovian stochastic dynamic programming models in*
- 602 *different time scales for long term hydropower scheduling*. Electric Power Systems Research,
- 603 2017. **150**: p. 129-136.
- 604 25. Soleimani, S., O. Bozorg-Haddad, and H.A. Loáiciga, *Reservoir Operation Rules with*
- 605 *Uncertainties in Reservoir Inflow and Agricultural Demand Derived with Stochastic Dynamic*
- 606 *Programming*. Journal of Irrigation and Drainage Engineering, 2016. **142**(11): p. 04016046.
- 607 26. Zhou, D., et al., *Cloud Computing Stochastic Dynamic Programming Algorithms for Long-term*
- 608 *Optimal Operation of Cascaded Hydropower Stations*. Zhongguo Dianji Gongcheng
- 609 Xuebao/Proceedings of the Chinese Society of Electrical Engineering, 2017. **37**(12): p. 3437-
- 610 3448.
- 611 27. Pereira, M.V.F. and L.M.V.G. Pinto, *Multi-stage stochastic optimization applied to energy*
- 612 *planning*. Mathematical Programming, 1991. **52**(1): p. 359-375.
- 613 28. Macian-Sorribes, H., A. Tilmant, and M. Pulido-Velazquez, *Improving operating policies of*
- 614 *large-scale surface-groundwater systems through stochastic programming*. Water Resources
- 615 Research, 2017. **53**(2): p. 1407-1423.
- 616 29. Lewis, A. and M. Randall, *Solving multi-objective water management problems using*
- 617 *evolutionary computation*. Journal of Environmental Management, 2017. **204**: p. 179-188.
- 618 30. Wan, J., et al., *Groundwater Resource Planning to Preserve Streamflow: Where Environmental*
- 619 *Amenity Meets Economic Welfare Loss*. Journal of Water Resources Planning and
- 620 Management, 2013. **139**(4): p. 440-448.
- 621 31. Fotakis, D. and E. Sidiropoulos, *A new multi-objective self-organizing optimization algorithm*
- 622 *(MOSOA) for spatial optimization problems*. Applied Mathematics and Computation, 2012.
- 623 **218**(9): p. 5168-5180.
- 624 32. Marston, L. and M. Konar, *Drought impacts to water footprints and virtual water transfers of*
- 625 *the Central Valley of California*. Water Resources Research, 2017. **53**(7): p. 5756-5773.
- 626 33. Li, R., et al., *Evaluation of groundwater resources in response to agricultural management*
- 627 *scenarios in the Central Valley, California*. Journal of Water Resources Planning and
- 628 Management, 2018. **144**(12).
- 629 34. Nelson, K.S. and E.K. Burchfield, *Effects of the Structure of Water Rights on Agricultural*
- 630 *Production During Drought: A Spatiotemporal Analysis of California's Central Valley*. Water
- 631 Resources Research, 2017. **53**(10): p. 8293-8309.
- 632 35. MacEwan, D., et al., *Hydroeconomic modeling of sustainable groundwater management*.
- 633 Water Resources Research, 2017. **53**(3): p. 2384-2403.
- 634 36. Konikow, L.F., *Long-Term Groundwater Depletion in the United States*. Groundwater, 2015.
- 635 **53**(1): p. 2-9.
- 636 37. Arrow, K.J., *Liquidity preference*, in *The Economics of Uncertainty, Lecture Notes for*
- 637 *Economics*. 1963: Stanford University. p. 33-53.
- 638 38. Pratt, J.W., *Risk Aversion in the Small and in the Large*. Econometrica, 1964. **32**(1/2): p. 122.
- 639 39. Griffin, R.C., *Achieving water use efficiency in irrigation districts*. Journal of Water Resources
- 640 Planning and Management, 2006. **132**(6): p. 434-442.
- 641 40. Tilmant, A. and R. Kelman, *A stochastic approach to analyze trade-offs and risks associated*
- 642 *with large-scale water resources systems*. Water Resources Research, 2007. **43**(6).
- 643 41. Knowles, J., D. Corne, and K. Deb, *Multiobjective Problem Solving from Nature: From Concepts*
- 644 *to Applications*. 2007: Springer Berlin Heidelberg.
- 645 42. Zhang, X.Y., Y. Tian, and Y.C. Jin, *A Knee Point-Driven Evolutionary Algorithm for Many-*
- 646 *Objective Optimization*. Ieee Transactions on Evolutionary Computation, 2015. **19**(6): p. 761-
- 647 776.
- 648 43. Branke, J., et al. *Finding Knees in Multi-objective Optimization*. 2004. Berlin, Heidelberg:
- 649 Springer Berlin Heidelberg.

- 650 44. Thomas, P.J., *Measuring risk-aversion: The challenge*. Measurement: Journal of the  
651 International Measurement Confederation, 2016. **79**: p. 285-301.
- 652 45. Faunt, C.C., *Groundwater Availability of the Central Valley Aquifer*. 2009, U.S. Department of  
653 the Interior: U.S. Geological Survey, Reston, Virginia.
- 654 46. CDWR, *California Water Plan Update 2009*. 2009, California Department of Water Resources:  
655 Sacramento, California.
- 656 47. GreatValleyCenter, *Assessing the Region via Indicators – The Economy 1999 – 2004*. 2005,  
657 Great Valley Center: Modesto, California.
- 658 48. CNRA, *California Climate Adaptation Strategy*. 2009, California Natural Resources Agency:  
659 Sacramento, California.
- 660 49. Draper, A.J., *Implicit Stochastic Optimization with Limited Foresight for Reservoir Systems*.  
661 2001, University of California.
- 662 50. CDWR, *California's Most Significant Droughts: Comparing Historical and Recent Condition*.  
663 2015, California Department of Water Resources: Sacramento, California.
- 664 51. Draper, A.J., et al., *Economic-Engineering Optimization for California Water Management*.  
665 Journal of Water Resources Planning and Management, 2003. **129**(3): p. 155-164.
- 666 52. Hansen, K., *Contractual Mechanisms to Manage Water Supply Risk in the Western United*  
667 *States*. 2007, University of California, Davis: California.
- 668 53. Maass, A., *Design of water-resource systems: new techniques for relating economic objectives,*  
669 *engineering analysis, and governmental planning*. 1962: Harvard University Press.
- 670 54. Torres, M., R. Howitt, and L. Rodrigues, *Analyzing rainfall effects on agricultural income: Why*  
671 *timing matters*. *EconomiA*, 2019. **20**(1): p. 1-14.
- 672 55. Harou, J.J. and J.R. Lund, *Ending groundwater overdraft in hydrologic-economic systems*.  
673 *Hydrogeology Journal*, 2008. **16**(6): p. 1039-1055.
- 674 56. Madani, K. and J.R. Lund, *High-Elevation Hydropower and Climate Warming in California, in*  
675 *World Environmental and Water Resources Congress 2007: Restoring Our Natural Habitat*.  
676 2007: Tampa, Florida.
- 677 57. Vicuna, S., et al., *Climate change impacts on high elevation hydropower generation in*  
678 *California's Sierra Nevada: a case study in the Upper American River*. *Climatic Change*, 2008.  
679 **87**(1): p. 123-137.
- 680 58. Jenkins, M.W., et al., *Optimization of California's water supply system: Results and insights*.  
681 *Journal of Water Resources Planning and Management-Asce*, 2004. **130**(4): p. 271-280.
- 682 59. Hadka, D. and P. Reed, *Borg: An Auto-Adaptive Many-Objective Evolutionary Computing*  
683 *Framework*. *Evolutionary Computation*, 2013. **21**(2): p. 231-259.
- 684 60. Ward, V.L., et al., *Confronting tipping points: Can multi-objective evolutionary algorithms*  
685 *discover pollution control tradeoffs given environmental thresholds?* *Environmental Modelling*  
686 *& Software*, 2015. **73**: p. 27-43.
- 687 61. Zatarain Salazar, J., et al., *A diagnostic assessment of evolutionary algorithms for multi-*  
688 *objective surface water reservoir control*. *Advances in Water Resources*, 2016. **92**: p. 172-185.
- 689 62. Murtagh, B. and M. Saunders, *MINOS 5.5 user's guide*. 1998: Stanford, California.
- 690 63. Labadie, J.W., *Optimal operation of multireservoir systems: State-of-the-art review*. *Journal of*  
691 *Water Resources Planning and Management*, 2004. **130**(2): p. 93-111.
- 692 64. Nash, J.E. and J.V. Sutcliffe, *River flow forecasting through conceptual models part I — A*  
693 *discussion of principles*. *Journal of Hydrology*, 1970. **10**(3): p. 282-290.
- 694 65. Moriasi, D.N., et al., *Model evaluation guidelines for systematic quantification of accuracy in*  
695 *watershed simulations*. *Transactions of the ASABE*, 2007. **50**(3): p. 885-900.
- 696 66. Masaki, Y., et al., *Intercomparison of global river discharge simulations focusing on dam*  
697 *operation - Part II: Multiple models analysis in two case-study river basins, Missouri-*  
698 *Mississippi and Green-Colorado*. *Environ Res Lett*, 2017. **12**(5): p. 055002.

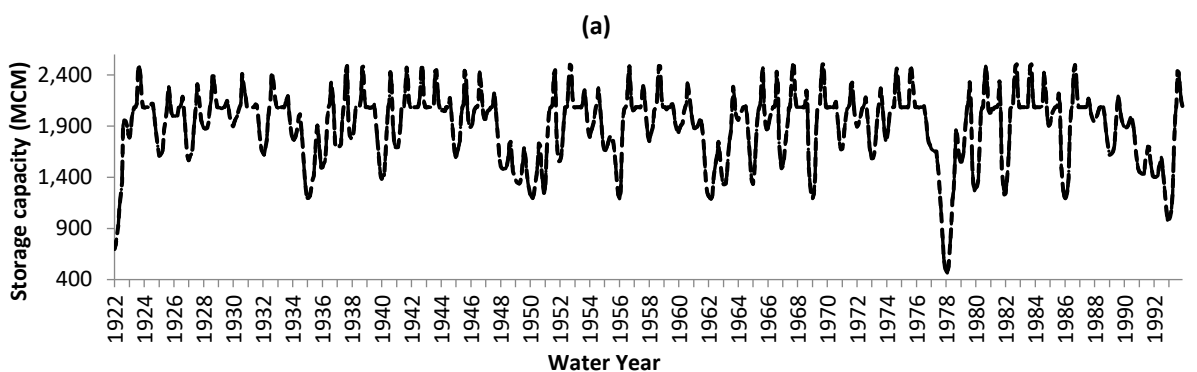
- 699 67. Zaherpour, J., et al., *Worldwide evaluation of mean and extreme runoff from six global-scale*  
700 *hydrological models that account for human impacts*. Environmental Research Letters, 2018.  
701 **13**(6): p. 065015.
- 702 68. Beven, K., *Prophecy, Reality and Uncertainty in Distributed Hydrological Modeling*. Advances  
703 in Water Resources, 1993. **16**(1): p. 41-51.
- 704 69. Beven, K., *A manifesto for the equifinality thesis*. Journal of Hydrology, 2006. **320**(1-2): p. 18-  
705 36.
- 706 70. Liu, P., X.M. Cai, and S.L. Guo, *Deriving multiple near-optimal solutions to deterministic*  
707 *reservoir operation problems*. Water Resources Research, 2011. **47**(8).
- 708 71. Rouge, C. and A. Tilmant, *Using stochastic dual dynamic programming in problems with*  
709 *multiple near-optimal solutions*. Water Resources Research, 2016. **52**(5): p. 4151-4163.

710

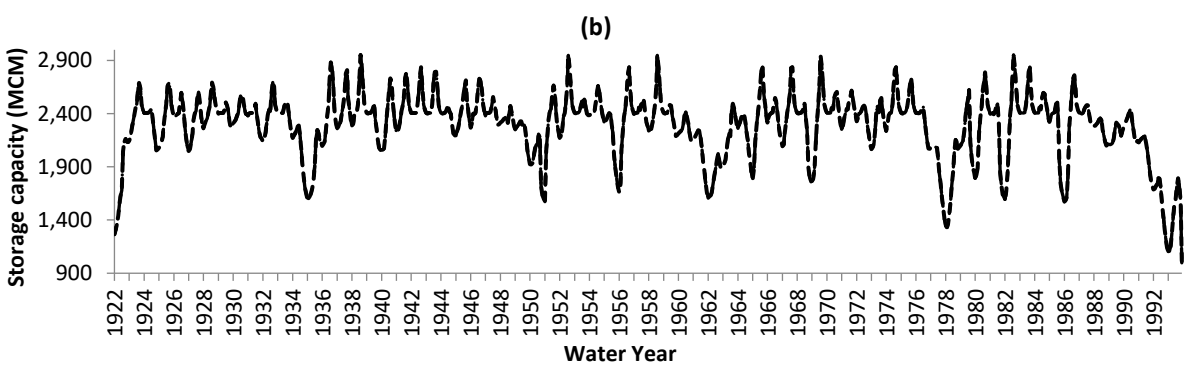
711

712 **Supplementary Material: Impact of different water valuation clusters on major**  
713 **reservoirs' operation**

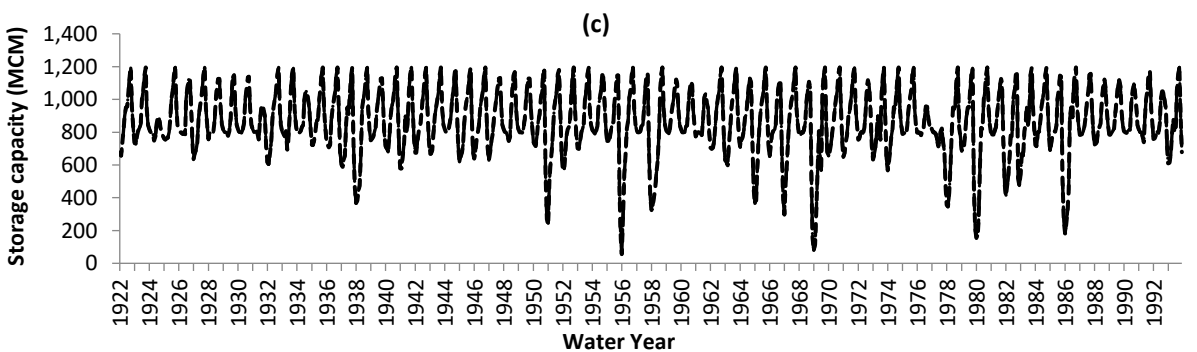
714 Here we investigate how the diversity in reservoir storage valuation of Don Pedro, New Melones,  
715 and Pine Flat manifests in the operation of these reservoirs. The storage trajectory of these three  
716 reservoirs is simulated using valuation solutions that created average, minimum, and maximum  
717 values in Figure 6. These three valuations of storage are used in three separate runs of the model,  
718 with all other parameters unchanged (including COSVF from other reservoirs). This is depicted in  
719 Figure S 1. Resulting end-of-year storage levels of the above three reservoirs prove to be identical  
720 regardless of which marginal value of water is chosen (Figure S 1). Therefore, it is the "average"  
721 valuation that is reported in Table 2 and forms the 'representative solution'.



722 ----- Calibrated with average values    - . - . Calibrated with maximum values    - - - Calibrated with minimum values



723 ----- Calibrated with average values    - . - . Calibrated with maximum values    - - - Calibrated with minimum values



724 ----- Calibrated with average values    - . - . Calibrated with maximum values    - - - Calibrated with minimum values

725 **Figure S 1.** Calibrated storage trajectories with average, minimum and maximum valuations in: a) Don Pedro,  
726 b) New Melones, and c) Pine Flat.