

Guided propagation of extremely intense lasers in plasma via ion motion

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Abstract

The upcoming 10 – 100 petawatt laser facilities may deliver laser pulses with unprecedented intensity of $10^{22} - 10^{25} \text{ Wcm}^{-2}$. Such laser pulses interacting with ultra-relativistic electrons accelerated in plasma can trigger various nonlinear quantum electrodynamic processes. Usually, ion motion is expected to be ignorable since the laser intensities below 10^{25} Wcm^{-2} are under-relativistic for ions. Here, we find that ion motion becomes significant even with the intensity around 10^{22} Wcm^{-2} when electron cavitation is formed by the strong laser ponderomotive force. Due to the electron cavitation, guided laser propagation becomes impossible via usual plasma electron response to laser fields. However, we find that ion response to the laser fields may effectively guide laser propagation at such high intensity levels. The corresponding conditions of the required ion density distribution and laser power are presented and verified by three-dimensional particle-in-cell simulations.

With the new progress in high power laser technologies, laser pulses with the peak powers of multi-petawatts (PW) are becoming available recently [1–4]. Even higher power laser systems at the 100 PW level are planned or under construction [5–7]. With these systems one may achieve focused laser intensity at the unprecedented level of $10^{22} - 10^{25} \text{ Wcm}^{-2}$. This enables one to explore fundamental physics and applications at high intensity frontiers such as quantum electrodynamics (QED) effects in plasma and vacuum [8–11], electron acceleration over 10 GeV [12–18], GeV ion acceleration [19–27], and high-energy gamma-ray generation [28–30], etc.

In such laser fields, electron oscillation velocities are ultra-relativistic with energies up to GeV, but ion oscillation velocities are still under-relativistic. Usually, the ion motion is expected to be ignorable in this laser-plasma interaction with a laser duration of tens of femtoseconds. However, we find in this paper that ion motion is important even with the intensity around 10^{22} Wcm^{-2} when electron cavitation is formed around the laser propagation axis by the strong laser ponderomotive force. In particular, this is clearly seen in laser propagation guided in plasma. Guided laser propagation in a plasma channel [31, 32] or in uniform plasma [33, 34] at the laser intensity less than 10^{20} W/cm^2 has been well demonstrated and adopted in applications such as laser wakefield acceleration [15, 16]. This is achieved via linear and nonlinear plasma electron response to the laser fields. At higher intensity, however, the strong laser ponderomotive force can significantly expel electrons from the laser interaction zone [35–37] and therefore, the normal channel guiding [31, 32] and relativistic self-guiding [33, 34] via the electron response do not work anymore [37]. Hence, it becomes challenging to achieve guided laser propagation with laser intensity above 10^{20} Wcm^{-2} .

Here, we show that both the channel guiding and relativistic self-guiding can be achieved *via ion response* to the laser fields even if complete electron cavitation occurs along the laser axis. When the ion density has a proper transverse density profile to provide the refractive index peaked along the channel axis, channel guiding can still occur via linear ion response. When the laser power exceeds a certain threshold, relativistic self-guiding due to nonlinear ion response also develops. The criteria for the two kinds of guiding are identified and then verified by three-dimensional (3D) particle-in-cell (PIC) simulations.

We first present examples to show how to obtain guided propagation of an ultrahigh intensity laser pulse in plasma through 3D PIC simulations with the KLAPS code [38, 39].

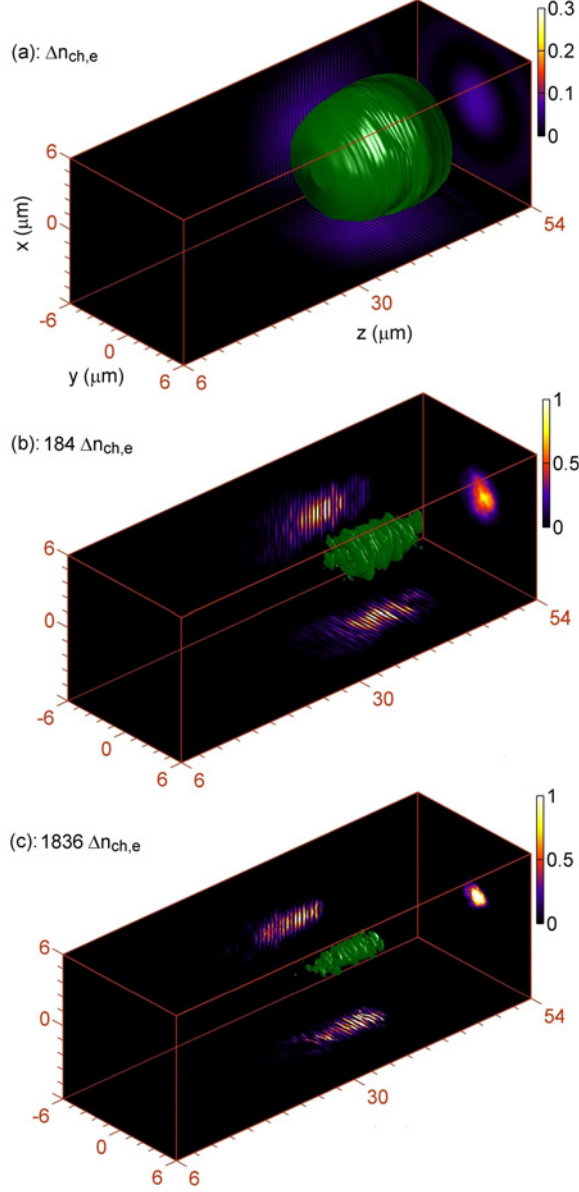


FIG. 1. Three-dimensional isosurfaces of the laser intensity I/I_0 (I_0 is the initial intensity) as well as the slices at the planes with respective peak values at the time $50 \tau_0$ or $4 z_R/c$. The plots (a), (b) and (c) correspond to different channel depths of $\Delta n_{ch,e}$, $184\Delta n_{ch,e}$, and $1836\Delta n_{ch,e}$, respectively, where $\Delta n_{ch,e}$ is the normal critical density depth due to the electron response.

Usually, to achieve sufficiently high intensities up to $10^{22} - 10^{25} \text{ Wcm}^{-2}$, tightly focusing with a spot radius down to few wavelengths is essential. In our simulations, we adopt the spot radius $r_0 = 2.0 \mu\text{m}$ and a available laser power 3.5 PW. With a higher power available in the future, a usual spot radius (e.g., $r_0 = 10 \mu\text{m}$) can be adopted. A laser pulse propagates along the $+z$ direction with the x -direction polarization, a wavelength

$\lambda_0 = 1\mu\text{m}$ (laser period $\tau_0 = 2\pi/\omega_0 = 3.33\text{fs}$), amplitude $a_0 = 200$ normalized by $m_e c \omega_0 / e$ (the corresponding intensity $5.5 \times 10^{22} \text{ Wcm}^{-2}$), and duration 40fs in full width at half maximum (FWHM). Here, e and m_e are the electron charge and mass, and c is the light speed in vacuum. The laser pulse peak arrives at the left boundary of a plasma at $12 \tau_0$. A preformed plasma channel is taken with a parabolic density profile $n = n_0 + \Delta n \times r^2/r_0^2$ within $r \leq 2r_0$ and $n = n_0 + 4\Delta n$ within $r > 2r_0$, where Δn is the channel depth. The plasma channel is composed of electrons and protons. We adopt a moving window at the light speed c . The window has a simulation box $12\mu\text{m} \times 12\mu\text{m} \times 96\mu\text{m}$ in $x \times y \times z$ directions (or $24\mu\text{m} \times 24\mu\text{m} \times 48\mu\text{m}$ in the case when laser defocusing occurs). The resolutions along the z and two transverse directions are $0.02\mu\text{m}$ and $0.25\mu\text{m}$, respectively. Eight simulation electrons and ions are taken per cell.

Under different plasma channel parameters, Fig. 1 shows laser intensity profiles after the propagation of $4 z_R$ ($z_R = \pi r_0^2/\lambda_0$ is the Rayleigh length). Figure 1(a) shows that the laser pulse of $a_0 = 200$ cannot be guided by a plasma channel with a density depth $\Delta n = \Delta n_{ch,e}$, where $\Delta n_{ch,e} = m_e c^2 / (\pi r_0^2 e^2) \simeq 0.1 n_{c,e} \times (\lambda_0 / r_0)^2$ is the critical depth determined by the electron response [31] and $n_{c,e} = m_e \omega_0^2 / 4\pi e^2 = 1.1 \times 10^{21} \text{ cm}^{-3} \times (1\mu\text{m} / \lambda_0)^2$ is the critical density of plasma electrons. Experiments and our simulations have showed that such a channel can well guide a laser pulse of $a_0 \sim 1$ over many Rayleigh lengths [15, 32] because a transverse profile of the refractive index peaked along the channel axis [31]. However, with the high amplitude of $a_0 = 200$, the laser pulse can quickly push the plasma electrons away from its interaction zone by its ponderomotive force, as illustrated in Fig. 2(a). Therefore, the refractive index profile suitable for laser guiding disappears.

As the density depth is increased to $\Delta n = 184\Delta n_{ch,e}$ and $1836\Delta n_{ch,e}$ in Figs. 1(b) and 1(c), respectively, the laser pulses are guided better. In particular, with $\Delta n = 1836\Delta n_{ch,e}$, the laser spot radius is kept around its initial value $r_0 = 2.0\mu\text{m}$ over a few Rayleigh lengths [see Figs. 1(c)]. One could explain this result as ions with higher densities tend to prevent the expulsion of electrons from the channel axis and the remaining electrons can help the laser focusing. On the other hand, we find that ion motion is key in this case.

We set the ions immobile in our simulation shown in the cyan line in Fig. 3(a). The evolution of the laser amplitude shows obvious difference from the case with the ions mobile (dark-orange line). Furthermore, immobile ions result in weaker laser focusing. Normally, immobile ions tend to prevent the electron expulsion and thus retain the electron density

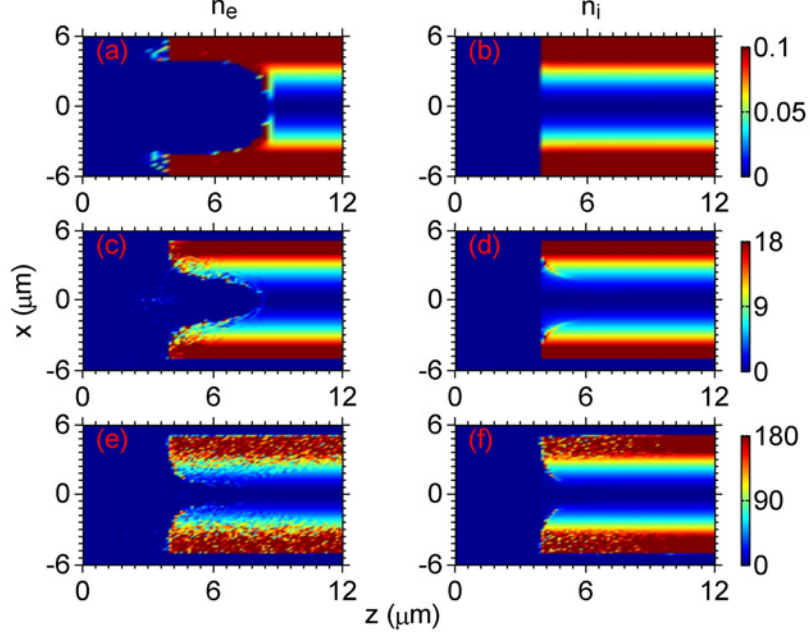


FIG. 2. Electron (left) and ion (right) density distributions at $10\tau_0$, where the channel depth is taken as $\Delta n_{ch,e}$ in (a,b), $184\Delta n_{ch,e}$ in (c, d), and $1836\Delta n_{ch,e}$ in (e, f).

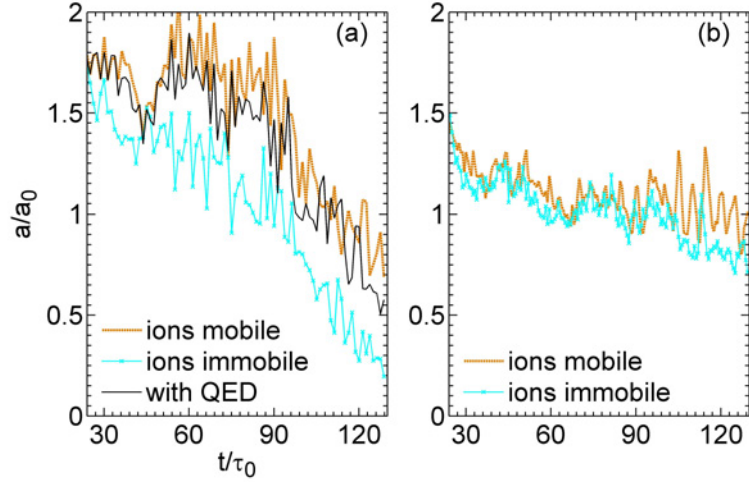


FIG. 3. Evolution of the laser amplitude peak when the channel depth is taken as $1836\Delta n_{ch,e}$ in (a) and $184\Delta n_{ch,e}$ in (b). Different curves correspond to simulations with QED effects, and ions mobile or immobile.

profile better. Hence, immobile ions should have caused stronger laser focusing. However, these results can be explained by ion response to the laser fields. Actually, Fig. 2 show that while electrons are quickly expelled from the channel axis, the high mass of the ions slows their response. Ions remain near their initial locations much longer, eventually following the electrons in a delayed fashion. The oscillation of these ions in the laser fields can lead to the refractive index distribution peaked at the channel axis, which can help laser focusing.

According to the dispersion relation of a planar laser pulse in plasma, i.e., $\omega_0^2 = k^2 c^2 + \omega_{p,e}^2/\gamma_e + \omega_{p,i}^2/\gamma_i$, the refractive index can be derived as

$$\eta \simeq 1 - \frac{n_e}{2\gamma_e n_{c,e}} - \frac{n_i}{2\gamma_i n_{c,e}} \frac{m_e q^2}{m_i e^2}, \quad (1)$$

where $\omega_{p,e} = \sqrt{4\pi n_e e^2/m_e}$ and $\omega_{p,i} = \sqrt{4\pi n_i q^2/m_i}$ are the plasma electron and ion frequencies, n_e and n_i are the electron and ion densities, γ_e and γ_i are the electron and ion Lorentz factors, and q and m_i are the ion charge and mass. To obtain Eq. (1), we have taken $n_e \ll \gamma_e n_{c,e} \sim a_0 n_{c,e}$ and $n_i \ll (m_i e^2/m_e q^2) n_{c,e}$. From Eq. (1), one can obtain

$$\frac{\partial \eta}{\partial r} \simeq -\frac{1}{2n_{c,e}} \left[\frac{\partial(n_e/\gamma_e)}{\partial r} + \frac{m_e q^2}{m_i e^2} \frac{\partial(n_i/\gamma_i)}{\partial r} \right], \quad (2)$$

where the first and second terms (defined as $\partial\eta/\partial r|_e$ and $\partial\eta/\partial r|_i$) on the right-hand side comes from the electron and ion response, respectively. With a plasma channel as used by us, both $\partial\eta/\partial r|_e$ and $\partial\eta/\partial r|_i$ are negative initially and η has a peak at the channel axis. Usually the ion contribution can be ignored because $|\partial\eta/\partial r|_i$ is at a level of $(m_e/m_i) \times |\partial\eta/\partial r|_e$. However, as the expulsion of electrons becomes stronger, $|\partial\eta/\partial r|_i$ can gradually exceed $|\partial\eta/\partial r|_e$. In particular, when full electron cavitation occurs, $|\partial\eta/\partial r|_e$ is nearly vanished around the laser interaction zone and only the ion response works. To achieve laser focusing, $|\partial\eta/\partial r|_i$ should enhance by a level of m_i/m_e (1836 for protons), which can be realized by increase the channel density depth Δn . This can explain Fig. 1(c) that as Δn is increased from $\Delta n_{ch,e}$ to $1836\Delta n_{ch,e}$, the channel guiding appears again. Note that with an insufficient high Δn of $184\Delta n_{ch,e}$, the ion response effect is not enough to cause full channel guiding [Fig. 1(b)]. Also, this effect does not lead to a significant difference between the cases of mobile and immobile ions [Fig. 3(b)].

One can notice that the laser amplitude appears a faster decay after $90 \tau_0$ in Fig. 3(a) than in Fig. 3(b), which is due to stronger depletion of the laser energy in a higher plasma

density. We also check two QED effects (the nonlinear Compton scattering and Breit-Wheeler process for pair creation) [8–10, 39]. The black line in Fig. 3(a) suggests these effects can be ignored when $a_0 \leq 200$, in agreement with Ref. [40]. It is worthwhile to point out that the channel-guiding effect with ion response can be found even when a_0 is decreased to 50. With further decreased a_0 , the electron expulsion becomes weak and the laser pulse interacts mostly with the electrons.

To quantitatively obtain conditions of the channel and self-guiding due to the ion response, we present a theory in a pure ion environment with a life-period longer than the laser pulse duration. As mentioned above, such environment with full electron cavitation around the laser axis can be formed in the laser interaction under certain laser intensities [35–37]. Also, it may be formed by a relativistic high-current electron beam in plasma [41, 42]. In this scenario, the laser pulse propagation is mainly governed by ion motion. One can use the equation for the laser envelope under the paraxial approximation,

$$\left(\nabla_{\perp}^2 - \frac{2i\omega_0}{c} \frac{\partial}{\partial z} \right) A_{s,i} = \frac{\omega_{p,i0}^2}{c^2} \left(\frac{n_i}{\gamma_i n_0} - 1 \right) A_{s,i}, \quad (3)$$

which is similar to that with electron motion considered [31, 35, 43–45]. Here, $A_{s,i}$ normalized by $m_i c^2 / e$ is the slowly varying envelope of the laser vector potential, i.e., $A = A_{s,i} \exp[i\omega_0(t - z/c)]$, the ion channel is taken as a parabolic profile $n_{i0} = n_0 + \Delta n r^2 / r_0^2$, and $\gamma_i = \sqrt{1 + |A_{s,i}|^2 / 2}$ for a linearly polarized laser pulse. We consider the rarefied density with $\omega_0^2 \gg \omega_{p,i}^2$ and weakly relativistic ion motion with $|A_{s,i}|^2 \ll 1$ and $\gamma_i \approx 1 + |A_{s,i}|^2 / 4$. With $|A_{s,i}|^2 \ll 1$, the ion density perturbation directly by the laser ponderomotive force can be ignored, i.e., $n_i \simeq n_{i0}$. To derive an evolution equation for the laser spot radius r_s , one can take the source-dependent expansion method [31, 44, 46] and assume that the laser field could be adequately approximated by the lowest order Gaussian mode $A_{s,i} = A_{s,i0}(r_0/r_s) \exp(-r^2/r_s^2)$. One can derive the evolution of the normalized spot size $R = r_s/r_0$ satisfying

$$\frac{d^2 R}{dz^2} = \frac{1}{R^3 z_R^2} \left(1 - \frac{P}{P_{c,i}} - R^4 \frac{\Delta n}{\Delta n_{ch,i}} \right), \quad (4)$$

where the second term on the right-hand side comes from nonlinear ion motion and the last term is due to ion-density channel. The critical power for relativistic self-focusing with a uniform density (taking $\Delta n = 0$) is given by

$$P_{c,i} = \frac{m_i^3 \omega_0^2 c^5}{2\pi n_0 q^4} = \left(\frac{m_i^3 e^4}{m_e^3 q^4} \right) \times \frac{n_{c,e}}{n_0} \times 17.4 \text{ GW}. \quad (5)$$

Usually $P_{c,i}$ is a large value, e.g., for protons with $n_0 = 100n_{c,e} = 0.055n_{c,i}$, $P_{c,i} = 1077$ PW well above the current laser technical capability, where $n_{c,i} = (m_i e^2 / m_e q^2) \times n_{c,e}$ is the critical density of ions. Therefore, channeling guiding is a more feasible than self-guiding for 10 to 100 PW laser pulses available currently and in the near future.

The critical channel depth can be given by

$$\Delta n_{ch,i} = \frac{m_i c^2}{\pi r_0^2 q^2} = \frac{m_i e^2}{m_e q^2} \times \Delta n_{ch,e}. \quad (6)$$

For protons $\Delta n_{ch,i} = 1836\Delta n_{ch,e} \simeq 47n_{c,e}$ with $r_0 = 2\mu\text{m}$. This is the reason why the laser pulse can be better guided by the channel with $\Delta n = 1836\Delta n_{ch,e} = \Delta n_{ch,i}$ than the ones with $\Delta n = 184\Delta n_{ch,e}$ and $\Delta n_{ch,e}$, as shown in Fig. 1. Note that $\Delta n_{ch,i} = 47n_{c,e}$ is high when $r_0 = 2\mu\text{m}$ is taken to achieve high intensities with a available laser power 3.5 PW. If a usual spot radius $r_0 = 10\mu\text{m}$ is adopted with a higher power, $\Delta n_{ch,i}$ will be decreased to $1.89n_{c,e}$, which could be provide by gas-filled capillary discharge [15, 16].

We carry out 3D PIC simulations to test the predicted critical channel depth and laser power. In Fig. 4, we adopt a proton channel with $\Delta n = \Delta n_{ch,i}$. It is shown that the laser pulse is well guided by the channel over 30 Rayleigh lengths. The channel guiding works in a large range of laser amplitude from $a_0 = 2$ to $a_0 = 2000$ (normalized by $m_e c \omega_0 / e$), as shown in Fig. 5(a). The evolution of the laser amplitudes is almost the same with $a_0 = 2$ and $a_0 = 200$ (the linear ion response is dominant) and it appears little difference when a_0 is increased to 2000, in which the ion oscillation velocity is close to c and relativistic effects work. In Fig. 5(b) we decrease Δn to $0.8\Delta n_{ch,i}$, $0.6\Delta n_{ch,i}$, and $0.2\Delta n_{ch,i}$, respectively, and the channel guiding becomes weaker and even disappears. These results are in good agreement with Eq. (6).

To examine the critical power given in Eq. (5), we take a uniform proton density of $100n_{c,e} = 0.055n_{c,i}$. Figure 5(c) shows that the derived $P_{c,i}$ is valid. When the power is less than $P_{c,i}$, the laser amplitude decays quickly because the laser pulse spreads out transversely. When the power is higher than $P_{c,i}$, self-focusing indeed occurs.

In summary, we find that a ultrahigh intensity laser pulse cannot be guided either by an underdense plasma channel or by relativistic nonlinearity due to the electron cavitation formed around the laser propagation axis. In this case, ion motion becomes important even with the intensity around 10^{22} Wcm^{-2} . Ion response to the laser fields can cause effective guiding of such a laser pulse in certain conditions. A new critical channel depth $\Delta n_{ch,i}$

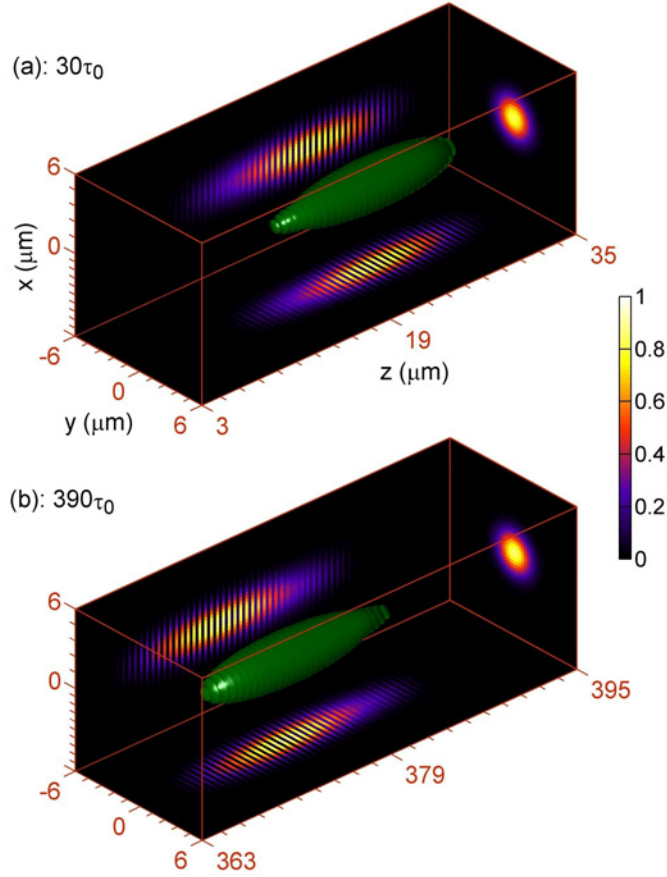


FIG. 4. Three-dimensional isosurfaces of the laser intensity I/I_0 (I_0 is the initial intensity) as well as the slices at the planes with respective peak values at the times of $30 \tau_0$ and $390 \tau_0$ ($31z_R/c$) in (a) and (b), respectively.

and a new critical power $P_{c,i}$ are derived for channel guiding and self-guiding, respectively, based upon the ion response. Our 3D PIC simulations show that $\Delta n_{ch,i}$ as the channel-guiding threshold starts to work when the laser intensity is sufficient high (e.g., $a_0 > 50$) and significant cavitation of electrons occurs. With complete cavitation (free of electrons in the laser interaction zone), both $\Delta n_{ch,i}$ and $P_{c,i}$ as guiding thresholds are very accurate. In particular, an ion channel can stably guide laser pulses with amplitudes in a large range, e.g., from $a_0 = 2$ to $a_0 = 2000$. Such an ion channel may be formed within a period before it is destroyed by Coulomb explosion, when a precursor laser pulse or a dense electron beam passes through plasma.

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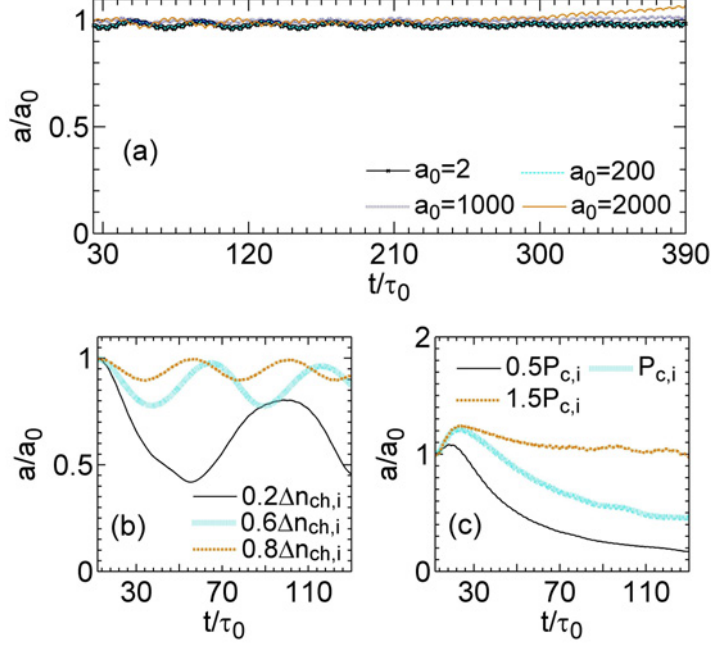


FIG. 5. Evolution of the laser amplitude peak. (a) Different initial amplitudes a_0 are taken with a fixed $\Delta n = \Delta n_{ch,i}$. (b) Different channel depths Δn are taken with a fixed $a_0 = 200$. (c) Different laser powers are taken with an initial spot radius $r_0 = 2\mu\text{m}$ and a uniform density of $100n_{c,e} = 0.055n_{c,i}$ ($n_{c,i}$ is the critical density of ions).

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