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Spider web-inspired acoustic metamaterials

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Spider silk is a remarkable example of bio-material with superior mechanical characteristics. Its multilevel structural organization of dragline and viscid silk leads to unusual and tunable properties, extensively studied from a quasi-static point of view. In this study, inspired by the *Nephila* spider orb web architecture, we propose a design for mechanical metamaterials based on its periodic repetition. We demonstrate that spider-web metamaterial structure plays an important role in the dynamic response and wave attenuation mechanisms. The capability of the resulting structure to inhibit elastic wave propagation in sub-wavelength frequency ranges is assessed, and parametric studies are performed to derive optimal configurations and constituent mechanical properties. The results show promise for the design of innovative lightweight structures for tunable vibration damping and impact protection, or the protection of large scale infrastructure such as suspended bridges. Published by AIP Publishing. [<http://dx.doi.org/10.1063/1.4961307>]

Many natural materials display outstanding properties that can be attributed to their complex structural design, developed in the course of millions of years of evolution.^{1–3} Particularly fascinating are spider silks, which exhibit unrivalled strength and toughness when compared to most materials.^{4–7} Previous studies have revealed that mechanical performance of spider webs is not only due to the remarkable properties of the silk material, but also to an optimized architecture that is adapted to different functions.^{8,9}

Structural behaviour of orb spider webs has been extensively analyzed under quasi-static^{6,8,10} and dynamic^{11,12} loading conditions. However, the spider-web structure has yet to be exploited for the design of phononic structures. These are usually periodic composites capable of inhibiting the propagation of elastic waves in specific frequency ranges called band gaps. This unique ability opens a wide range of application opportunities, such as seismic wave insulation,¹³ noise reduction,¹⁴ sub-wavelength imaging and focusing,¹⁵ phonon transport,¹⁶ strain-dependent thermal conductivity,¹⁷ acoustic cloaking,¹⁸ and thermal control.¹⁹ In phononic structures, band gaps are induced by either Bragg scattering from periodic inhomogeneities²⁰ or by local resonances.²¹ The latter are commonly achieved by employing heavy constituents.^{21–24} Recently, it has been found that hierarchically organized continuous²⁵ or lattice-type^{26,27} structures exhibit band gaps due to the two mentioned mechanisms. From this perspective, a spider web-inspired, lattice-based elastic metamaterial seems to be another promising alternative to simultaneously control wave propagation at multi-scale frequencies. In this letter, we design a metamaterial inspired by

the *Nephila* orb web architecture and analyze the dynamics of elastic waves propagating therein, with the aim of obtaining improved structures compared to simple lattices.²⁸

We consider a spider web-inspired metamaterial in the form of an infinite in-plane lattice modeled by periodically repeating representative unit cells in a square array. The primary structure of the unit cell is a square frame with supporting radial ligaments (Fig. 1(a)). The ligaments intersect the frame at right-angle junctions acting as “hinge” joints (square junctions in Fig. 1(a)). The secondary frame is defined by a set of equidistant circular ligaments (or ring resonators) attached to the radial ligaments by hinge joints, in the following called “connectors” to distinguish them from the joints in the first frame (Fig. 1(b)). The geometry of the metamaterial is completely defined by 5 parameters: unit cell pitch a , size of square joints b , thickness of radial and circular ligaments c , number of ring resonators N , and radius of a ring resonator R_N . We initially consider $a = 1\text{m}$, $b = 0.04 \cdot a$, $c = 0.01 \cdot a$, $N = 7$, and $R_N = 0.1 \cdot a \cdot (N + 1)/2$. The material properties

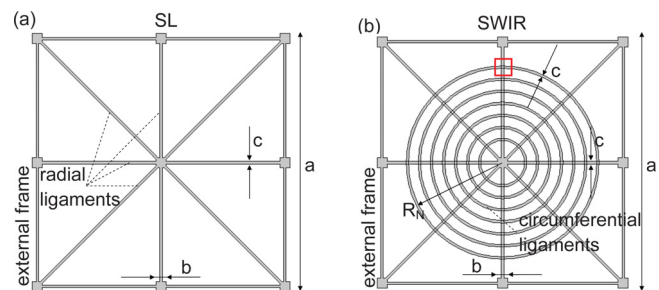


FIG. 1. (a) Bearing frame and (b) spider web-inspired unit cells for lattice-type metamaterials.

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of the primary and secondary frames correspond to the parameters of dragline ($E_d = 12$ GPa, $\nu_d = 0.4$, $\rho_d = 1200$ kg/m³) and viscid ($E_v = 1.2$ GPa, $\nu_v = 0.4$, $\rho_v = 1200$ kg/m³) silks of the *Nephila orb* spider web,⁹ respectively. Material properties of the connectors can assume dragline or viscid silk values. The propagation of elastic waves is investigated numerically by using the Finite Element commercial package COMSOL Multiphysics. Wave dispersion in infinite lattices is studied by applying the Bloch conditions²³ at the unit cell boundaries and performing the frequency modal analysis for wavenumbers along the borders ΓXM of the first irreducible Brillouin zone.²⁹

First, we study small-amplitude elastic waves propagating in an infinite structure formed by the primary frame unit cell (Fig. 1(a)), called “regular lattice” metamaterial. Fig. 2(a) shows band diagrams for the regular lattice as a function of reduced wave vector $k^* = [k_x a/\pi; k_y a/\pi]$. The color scale, here and in other diagrams, shows polarization of waves propagating along the x direction that varies from pure shear (blue) to pure longitudinal (red). Up to 400 Hz, there is one negligible band gap around 80 Hz. The band structure exhibits localized modes at various frequencies represented by (almost) flat bands. Analysis of the vibration forms reveals that the motion is localized within the radial ligaments, which are mainly subjected to flexural deformation (Fig. 2(e)).

Next, the circular elements are introduced to analyze the wave dispersion in a spider web-inspired metamaterial (Fig. 1(b)). Here, we explore three possibilities: (1) the circular ligaments have the same material properties as the radial ligaments (dragline silk); (2) the circular ligaments are made of

viscid silk, while connectors of radial and circular ligaments have the properties of dragline silk, and (3) both the circular ligaments and the connectors are made of viscid silk. This allows evaluating the influence of material parameters on the performance in the spider-web structures. Fig. 2(b) shows the band diagram for the metamaterial made of the dragline silk with a complete band gap at frequencies from 346.5 to 367.4 Hz, which is shaded in light gray. As the band gap bounds are formed by non-flat curves and the whole unit cell is involved in the motion at the band gap bound (Fig. 2(f)), this band gap is not due to local resonances. Also, the band gap cannot be induced by Bragg scattering, as it is located at least twice below the frequencies at which a half-wavelength of either longitudinal (2314 Hz) or shear (945 Hz) waves in the silk is equal to the unit cell size. Further analysis of the band gap origin is beyond the scope of this letter, since we are focusing on a spider web-inspired structure with *different* mechanical properties for radial and circular ligaments.^{8,9} Another remarkable feature of the band structure in Fig. 2(b) is the smaller number of localized modes compared to Fig. 2(a), which may be explained with the elimination of local resonances due to the coupling between motions in radial and circular ligaments.

By assigning viscid silk material properties to ring resonators, two band gaps appear in Figs. 2(c) and 2(d), regardless of the material properties of the connectors joining radial and circular ligaments. Due to the compliant behaviour of the resonators, the band gaps are located at lower frequencies compared to those in Fig. 2(b). These are so-called hybridization band gaps induced by local resonances, since

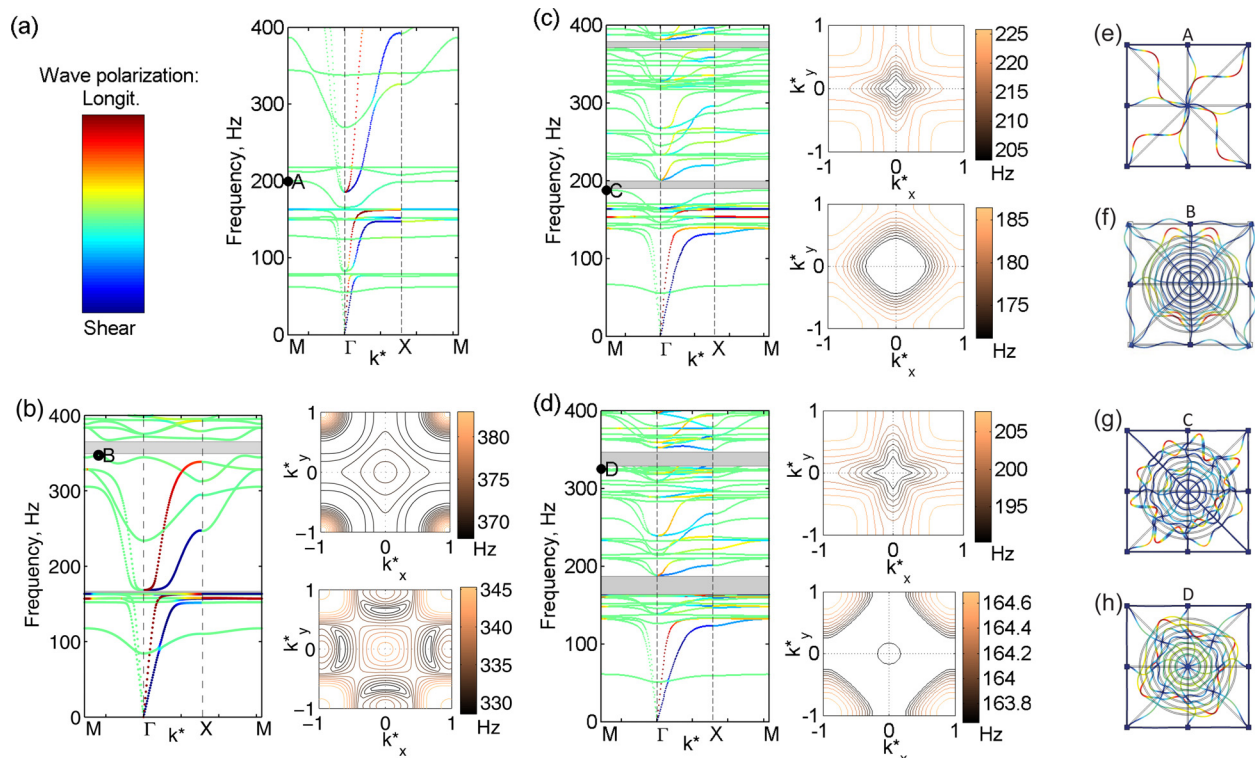


FIG. 2. (a) Band structure for the regular lattice. (b)–(d) Band structures and contour plots of dispersion surfaces at the upper and lower BG boundaries for spider web-inspired lattices: (b) stiff ring resonators (dragline silk), (c) compliant ring resonators (viscid silk) and rigid connectors (dragline silk), and (d) compliant ring resonators and connectors. Band gaps are shaded in gray and the color of pass bands represents the mode polarization ranging from pure shear (blue) to pure longitudinal (red). (e)–(h) Mode shapes referring to points A, B, C, and D of the dispersion diagrams.

the lower bounds are formed by flat curves representing localized motions (Figs. 2(g) and 2(h)), and the Bloch wave vector k^* changes by π inside each band gap.³¹ When the ring resonators and the connectors have the same mechanical properties (viscid silk), the band gaps are shifted to lower frequencies due to a more compliant behaviour of the connectors (compare Figs. 2(c) and 2(d)).

To investigate the wave directionality, we evaluate dispersion surfaces for all directions within the first Brillouin zone. The results are shown as contour plots for pass bands at the band gap bounds (bottom and top figures on the right of each band diagram in Fig. 2). The color scales represent the values at which frequency cuts are performed. The contour plots reveal preferred directions of propagation at $\theta = 0^\circ$ ($\theta = 90^\circ$) that indicates strong anisotropy in the wave dispersion near the band gaps, as in other phononic structures.³⁰

Another peculiarity of the band diagrams in Figs. 2(c) and 2(d) in comparison to Figs. 2(a) and 2(b) is a larger number of localized modes. In the former case, these modes are associated with standing waves mostly dominated by high inertia of the resonators (Figs. 2(g) and 2(h)). If the connectors between radial and circular ligaments have the same material properties as the ring resonators (the closest configuration to a real spider web), it appears that the standing waves may be associated with the resonators only.

The natural frequencies ω_n for non-axisymmetric in-plane flexural vibrations of these resonators can be expressed³² in closed form as: $\omega_n = k \frac{n(n^2-1)}{R^2 \sqrt{n^2+1}}$, with $n > 1$. Here, R stands for the radius of a ring resonator, and k is a dimensional constant that depends on the elastic modulus of the ring resonator, the mass density, and its cross-section. Vibrational modes for several values of n are shown in the [supplementary material](#). However, this analytical solution does not describe the dynamics of spider-web lattice systems satisfactorily, since their response is governed by the entire structure and not the individual decoupled resonators (see the [supplementary material](#) for details). More insight into the wave dynamics in the proposed metamaterials is achieved by analyzing the mode transformations for varying geometrical and mechanical parameters (see the [supplementary material](#)). Next, we vary the stiffness of ring resonators by choosing

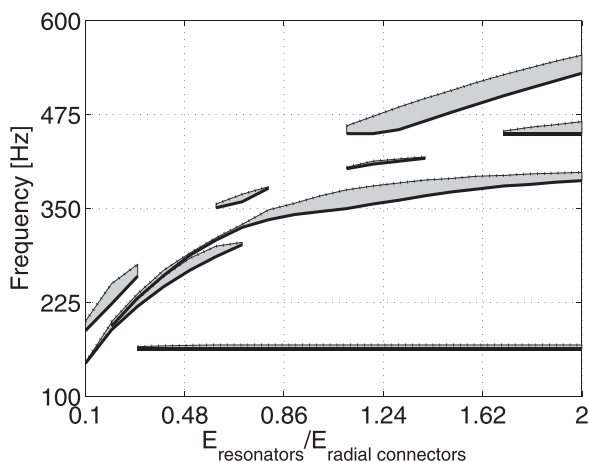


FIG. 3. Band gap frequencies for the lowest band gaps as functions of ratio E_{rr}/E_{rl} ($E_{rr} = 12$ GPa).

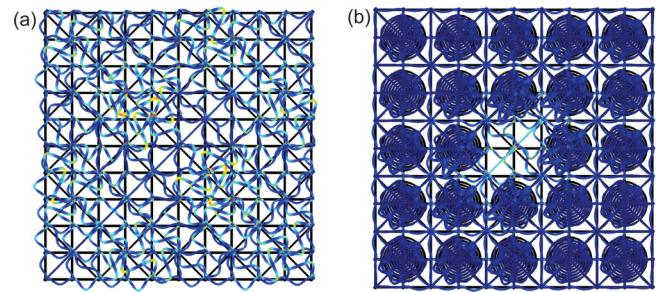


FIG. 4. Frequency domain in-plane displacements (scaled by 45 000) for a point excitation of frequency 186 Hz applied at an angle $\pi/4$ with respect to the horizontal axis in (a) a regular-lattice structure and (b) spider web-inspired system with viscidsilk ring resonators. Red and blue colors indicate maximum and minimum displacements, respectively.

intermediate values between those of dragline and viscidsilks. The overall band diagrams resemble those shown in Figs. 2(c) and 2(d). Thus, we focus our attention only on the band gaps. Fig. 3 shows band gap frequencies versus ratios E_{rr}/E_{rl} , where $E_{rr} = 12$ GPa and E_{rl} are the stiffnesses of the ring resonators and radial ligaments, respectively. In general, as the stiffness of the ring resonators increases, inhibited frequency ranges are translated towards higher frequencies, except the lowest band gap around 150 Hz with frequencies independent of the mechanical parameters of the resonators.

Now we investigate the transmission in finite-size spider-web inspired structures. The analysed model comprises 25 unit cells placed in a square array with traction-free boundary conditions. The structure is excited at the central point by applying harmonic in-plane displacement at a frequency of 186 Hz (within a band gap) at an angle of $\pi/4$ with respect to the horizontal axis. Fig. 4 presents frequency-domain responses (scaled by a factor of 45 000) in terms of in-plane displacements for two structures formed by the regular and spider-web lattice unit cells with viscidsilk ring resonators. Maximum and minimum values of displacements are shown in red and dark blue, respectively. Notice that all of the regular-lattice structure vibrates (Fig. 4(a)), while the spider web-inspired system is capable of strongly attenuating vibrations after a few unit cells (Fig. 4(b)). A similar behaviour is observed for other excitation frequencies within the band gaps. These results confirm the predictions derived from the wave dispersion analysis. Fig. 4(b) suggests as an application the generation of a defect mode in a cluster with localized vibrations around its center for efficient wave attenuation at desired frequencies.

In summary, we have numerically studied the propagation characteristics of elastic waves in regular and spider web-inspired beam lattices, based on the *Nephila orb* web architecture. Our results indicate that these lattices possess locally resonant band gaps induced by either ring-shaped resonators or parts of the bearing frame. Dispersion analysis reveals strong anisotropic dynamics of spider-web lattices and the mixed character of localized modes. The band gaps can be easily tuned in a wide range of frequencies by varying the mechanical properties or the number of the resonators, or even the properties of the connectors between resonators and the frame. Despite the fact that the ring resonators are responsible for the generation of band gaps, their eigenfrequencies

cannot be directly used to predict the band gap bounds, since the overall structure plays an important role in their formation. Though lattice systems with locally resonant band gaps have already been reported,^{26,27} this study shows that spider web-inspired lattice metamaterials are particularly efficient in inducing low-frequency band gaps despite being light-weight. Also, they possess more parameters to tune the band gaps to desired frequencies and are easier to manipulate/manufacture compared to hierarchically organized lattice structures. Thus, results from this study can inspire further designs of light-weight and robust metamaterial structures with tunable properties. This work also suggests an advanced functionality for spider webs and future applications for the corresponding metamaterials and metastructures, e.g., for earthquake protection of suspended bridges.

See [supplementary material](#) for more details.

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