# Layered Ensemble Model for Short-Term Traffic Flow Forecasting with Outlier Detection 

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#### Abstract

Real time traffic forecasting is a necessary requirement for traffic management in order to be able to evaluate the effects of different available strategies or policies. This paper focuses on short-term traffic flow forecasting by taking into consideration both spatial (road links) and temporal (lag or past traffic flow values) information. We propose a Layered Ensemble Model (LEM) which combines Artificial Neural Networks and Graded Possibilistic Clustering obtaining an accurate forecast of the traffic flow rates with outlier detection. Experimentation has been carried out on two different data sets. The former was obtained from real UK motorway and the later was obtained from simulated traffic flow on a street network in Genoa (Italy). The proposed LEM model for short-term traffic forecasting provides promising results and given the ability for outlier detection, accuracy, robustness of the proposed approach, it can be fruitful integrated in traffic flow management systems.


## I. Introduction

Traffic flow forecasting is one of the fundamental components in Intelligent Transportation Systems (ITS). There are mainly three approaches to solve problem of traffic forecasting in urban and network scale areas: Parametric models ([1], [2], [3]); Machine Learning and Computational Intelligence methods (non-parametric models) ([4], [5], [6]); Hybrid approaches which combine the features and capabilities of parametric and non-parametric models as in ([7], [8], [9]). Since the eighties, short term traffic forecasting has been part of most intelligent transportation systems. Many traffic forecasting approaches focus on the problem of freeway traffic forecasting in which the state of the road traffic is almost stable. In contrast, traffic forecasting in urban and network-scale areas is more complex because of the rapid change of traffic behavior and limited availability of sensors that can cover the whole network.

Many researches have developed approaches bases on nonparametric models, such as multilayer perceptron with a learning rule based on a Kalman filter [10], wavelet-based neural network [11], fuzzy-neural model [12], ARIMA model [13], graphical-lasso neural network [14], multi-task neural network [15], multi-task ensemble neural network [16], k-nearest neighbor non-parametric regression [17]. A good survey on the current literature is given in In [18].

In this paper we present a robust model for short-term traffic forecasting with online outlier detection combining clustering and Neural Network (NN).

## II. Methodology

The proposed method consists of an ensemble of Neural Networks (NN), each specialized on a region of the data space. The first layer provides this local specialization, as well as providing a measure of pattern outlierness that is used to


Fig. 1. Flow chart of training stage in the proposed model
estimate the expected quality of the forecast. In the following we outline the methods used for clustering and forecasting.

## A. LEM model

The Layered Ensemble Model (LEM) consists of 2 layers as shown in Figure 1. In the first layer we employ a clustering process called Graded Possibilistic $c$ Means (GPCM) [19] that is able to adapt to the changes in the traffic flow, by implementing a continuous learning that exploits the input patterns as they arrive. So the first layer has two tasks: 1) Group patterns into K groups where pattern in the same group have similar behavior. 2) Measure outlierness degree of each pattern. The measure of outlierness will be used to assess and improve the accuracy of the second layer (forecaster). In the second layer we have an ensemble method based on base learners (in our case multilayer perceptron neural networks); each of them is trained on traffic flow patterns belonging to a different cluster.

## B. Data preprocessing

For any forecaster model there are some issues that affect its performance:

- Lag period: As shown in Figure 1 the first issue is the proper selection of the lag period which is crucial because it affects the correct representation of the traffic flow in time. If the lag period is chosen to be smaller than needed, then we will not be able to distinguish between the time-lag vectors in the vector space (redundancy) [20]; hence, the prediction process will be practically impossible because data doesn't carry enough valuable information. If the lag period is chosen to be larger than needed, the vectors in the vector space will be almost uncorrelated (irrelevance) [21]. In [22] they proposed an


Fig. 2. Flow chart of the test stage in the proposed model
approach to tackle this problem by using the time-lag mutual information as a tool to determine a reasonable value of the lag period.

- Historical period: This refer to the number of observation patterns that will be used to train the forecasters.
- Traffic flow patterns and outliers: Learning patterns with a different behavior together in a Large data set tends to reduce the models performance. As a solution to this problem, we employ a clustering process called GPCM that is able to group patterns into K groups, where patterns in the same group have similar behavior as shown in Figure 3, and measures the degree of outlierness of each pattern. This measures will be used to improve the forecaster accuracy.


## C. The Graded Possibilistic c Means Model

In central clustering data objects are points or vectors in data space, and $c$ clusters are represented by means of their "central" points or centroids $\mathbf{y}_{j}$. The Graded Possibilistic model is a soft central clustering method, implying that cluster membership can be partial. This is usually represented by means of cluster indicators (or membership functions) which are real-valued rather than integer.

In many cases methods are derived as the iterative optimization of a constrained objective function [23], usually the mean squared distortion:

$$
\begin{equation*}
D=\frac{1}{n} \sum_{l=1}^{n} \sum_{j=1}^{c} u_{l j}\left\|x_{l}-\mathbf{y}_{i}\right\|^{2} \tag{1}
\end{equation*}
$$



Fig. 3. First five traffic flow patterns (UK motorway Site 30012533 (AL2989A) 2009) in (a) cluster 1; (b) cluster 2; (c) cluster 3.

Centroids are obtained by imposing $\nabla D=0$ :

$$
\begin{equation*}
\mathbf{y}_{j}=\frac{\sum_{l=1}^{n} u_{l j} x_{l}}{\sum_{l=1}^{n} u_{l j}} \tag{2}
\end{equation*}
$$

Usually constraints are placed on the sum $\zeta_{l}=\sum_{j=1}^{c} u_{l j}$ of all memberships for any given observation $x_{l}$. The value $\zeta_{l}$ can be interpreted as the total membership mass of observation $x_{l}$. We now survey from this perspective two related soft clustering method.

The Maximum Entropy (ME) approach [24] imposes $\zeta_{l}=1$, so we are in the "probabilistic" case, where memberships are formally equivalent to probabilities.

The objective $J_{\mathrm{ME}}$ includes an entropic penalty with weight $\beta$, and $\nabla J_{\mathrm{ME}}=0$ yields

$$
\begin{equation*}
u_{l j}=\frac{e^{-d_{l j} / \beta}}{\zeta_{l}} \tag{3}
\end{equation*}
$$

On the other end of the spectrum, the Possibilistic $c$-Means in its second formulation (PCM-II) [25] does not impose any constraint on $\zeta_{l}$, so memberships are not formally equivalent to probabilities; they represent degrees of typicality.

The objective $J_{\mathrm{PCM}-\mathrm{II}}$ includes an individual parameter $\beta_{j}$ for each cluster, and $\nabla J_{\mathrm{PCM}-\mathrm{II}}=0$ yields

$$
\begin{equation*}
u_{l j}=e^{-d_{l j} / \beta_{j}} \tag{4}
\end{equation*}
$$

Note that eq. (4) is a special case of eq. (3) with $\zeta_{l}$ replaced by $1 \forall l$, whereas eq. (3) is a special case of eq. (4) with $\beta_{j}=\beta \forall j$. In other words, both can be generalized to a unique formulation. This was done in [19] as follows:

$$
\begin{equation*}
u_{l j}=\frac{v_{l j}}{Z_{l}} \tag{5}
\end{equation*}
$$

where the free membership $v_{l j}=e^{-d_{l j} / \beta_{j}}$ is normalized with some term $Z_{l}$, a function of (but not necessarily equal to) $\zeta_{l}$. This allows us to add a continuum of other, intermediate cases to the two extreme models just described, respectively characterized by $Z_{l}=\zeta_{j}=\sum_{j=1}^{c} v_{l j}$ (probabilistic) and $Z_{l}=$ 1 (possibilistic). Here we use the following formulation:

$$
\begin{equation*}
Z_{l}=\zeta_{l}^{\alpha}=\left(\sum_{j=1}^{c} v_{l j}\right)^{\alpha}, \quad \alpha \in[0,1] \subset \mathbb{R} \tag{6}
\end{equation*}
$$

The parameter $\alpha$ controls the "possibility level", from a totally probabilistic $(\alpha=1)$ to a totally possibilistic $(\alpha=0)$ model, with all intermediate cases for $0<\alpha<1$.

## D. Ensemble forecast model

As shown in Figure 1, for each cluster a forecaster with architecture shown in Table I is trained and $\zeta_{l}$ is obtained which is a vector of size size $m$ where $m$ is number of traffic patterns in the training data set.

After training stage, we start online test stage as shown in Figure 2 where patterns comes as a streams and for each upcoming test pattern $\zeta_{i}$ is computed and compared to a threshold. In the proposed model we use $\min \left(\zeta_{l}\right)$ as a threshold where $\zeta_{i}<\min \left(\zeta_{l}\right)$ means that the test pattern is an extreme outlier and will be dropped. The drop rate of the test pattens depend on the value of $\alpha$ which controls the sensitivity of the model to outliers. A high value if $\alpha$ means less sensitivity to outlier and a lower drop rate.

The final output of the LEM is computed as a weighted sum of the individual base learner forecasts, as follows:

$$
\begin{equation*}
y_{i}=\sum_{j=1}^{c} y_{j} u_{j} / \zeta_{i} \tag{7}
\end{equation*}
$$

In eq. (7) we see that the output of each forecaster is weighted by $u_{j}$, which is the membership degree of each pattern to each cluster so that $u_{j}$ will have high value for the most suitable forecaster(s) and low to the others.

## III. EXPERIMENTS AND RESULTS

## A. Data sets

UK road network: Multiple data sets are obtained from different road links in the United Kingdom (UK) [26]. This data series provides traffic flow information for 15-minute periods since 2009 on most of road links in UK. The data sets are obtined from different loop sensors but we selected

TABLE I
LEM MODEL PARAMETERS

|  | UK data set | Genoa dataset |
| :--- | :--- | :--- |
| Lag period | 1 day (96 observations) | 25 min <br> (5 observations from 3 road links) |
| Observation period | 15 min | 5 min |
| Historical period for training | 9 months | 6 hours |
| Test period (forecasting period) | 3 months | 3 hours |
| Validation | 10 -fold cross validation | 10 -fold cross validation |
| Forecaster | Artificial Neural Network | Artificial Neural Network |
| Number of layers | 3 (input,hidden,output) | 3 |
| Neural Network architecture | $95-10-1$ | $4-10-1$ |
| Number of clusters | 5 | 5 |
| $\alpha$ | $0<\alpha<1$ | $0<\alpha<1$ |
| $\beta$ | .1 | .01 |

the loop sensor id AL2989A (TMU Site 30012533) to obtain traffic flow as done in [27].

Genoa Data set: The data were obtained as follows. An urban area of the city of Genoa, in the north-west of Italy, was mapped with the aid of Open Street Map data. Traffic parameters were obtained from actual observations and several days of traffic were estimated by using the SUMO open source traffic simulator [28]. The simulation yielded observations at time intervals of five minutes. in this data set we obtain traffic flow not only from main link but also from the adjacent links to forecast the future.

## B. Experiments parameters and Results

The results in Figure 4 show on the top the scatter plot of the forecasted traffic flow in UK, and on the bottom the forecasted traffic flow in Genoa both with zero drop rate. In Figure 5 we show the effect of $\alpha$ on the accuracy (Mean square error) of the LEM model. The selected range of alpha values are $.93 \leq \alpha \leq 1$ and the drop rate is computed as follow:

$$
\begin{equation*}
\text { drop rate }=1-\left(\frac{\text { Number of output patterns }}{\text { Number of target patterns }}\right) \tag{8}
\end{equation*}
$$

## IV. Conclusion

The experiments show that the proposed method offers the ability to deal with typical patterns, tuning the forecaster in the most appropriate manner, while detecting atypical patterns.

In future work, the method will be expanded by using the outlierness information to estimate the presence of concept drift in the data.

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Fig. 4. (a) Scatter plot between the target and the output (UK data set) (b) Forecasted output and the target (Genoa data set).


Fig. 5. LEM model accuracy w.r.t $\alpha$ in UK for 3 months.
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