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High-energy sources at low radio frequency: the Murchison Widefield Array view of *Fermi* blazars*

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ABSTRACT

Context. Low-frequency radio arrays are opening a new window for the study of the sky, both to study new phenomena and to better characterize known source classes. Being flat-spectrum sources, blazars are so far poorly studied at low radio frequencies.

Aims. We characterize the spectral properties of the blazar population at low radio frequency, compare the radio and high-energy properties of the gamma-ray blazar population, and search for radio counterparts of unidentified gamma-ray sources.

Methods. We cross-correlated the 6100 deg² Murchison Widefield Array Commissioning Survey catalogue with the Roma blazar catalogue, the third catalogue of active galactic nuclei detected by *Fermi*-LAT, and the unidentified members of the entire third catalogue of gamma-ray sources detected by *Fermi*-LAT. When available, we also added high-frequency radio data from the Australia Telescope 20 GHz catalogue.

Results. We find low-frequency counterparts for 186 out of 517 (36%) blazars, 79 out of 174 (45%) gamma-ray blazars, and 8 out of 73 (11%) gamma-ray blazar candidates. The mean low-frequency (120–180 MHz) blazar spectral index is $\langle \alpha_{low} \rangle = 0.57 \pm 0.02$: blazar spectra are flatter than the rest of the population of low-frequency sources, but are steeper than at ~GHz frequencies. Low-frequency radio flux density and gamma-ray energy flux display a mildly significant and broadly scattered correlation. Ten unidentified gamma-ray sources have a (probably fortuitous) positional match with low radio frequency sources.

Conclusions. Low-frequency radio astronomy provides important information about sources with a flat radio spectrum and high energy. However, the relatively low sensitivity of the present surveys still misses a significant fraction of these objects. Upcoming deeper surveys, such as the GaLactic and Extragalactic All-Sky MWA (GLEAM) survey, will provide further insight into this population.

Key words. BL Lacertae objects: general – catalogs – gamma rays: galaxies – quasars: general – radiation mechanisms: non-thermal – radio continuum: galaxies

1. Introduction

Blazars are the most numerous source population in gamma-ray catalogues (Abdo et al. 2010; Nolan et al. 2012; Acero et al. 2015). They are radio-loud active galactic nuclei (AGNs) with relativistic jets pointing near to the line of sight. They include flat-spectrum radio quasars (FSRQ), with prominent emission lines in their optical spectra, and BL Lac objects (BL Lacs), with nearly featureless optical spectra. In addition to these markedly different emission line properties, the two classes also have other observational differences; however, the underlying physical processes at work in the two classes are the same, with a beamed relativistic jet powered by accretion onto a supermassive black hole dominating the spectral energy distribution (SED) from radio to gamma rays. In the radio band, at GHz frequencies,

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blazars of all classes show a flat spectrum ($\alpha < 0.5$, in the $S(\nu) \propto \nu^{-\alpha}$ convention). Several recent works demonstrated that blazars largely also maintain a flat spectrum at lower frequency, down to the 300 MHz band (Massaro et al. 2013a; Nori et al. 2014) and even 74 MHz (Massaro et al. 2013b). However, these studies were based on the comparison of data from low-frequency surveys to ~GHz surveys carried out at a different epoch. Therefore, they provide only two-point non-simultaneous spectra, which could be affected by time variability (a key feature of blazars), and they are not sensitive to any possible curvature, important information about the physical properties of the emission region, such as the relative contribution of different spectrum components, and breaks in the electron energy distribution.

In the context of the Murchison Widefield Array (MWA, Tingay et al. 2013) instrument commissioning, Hurley-Walker et al. (2014) performed the Murchison Widefield Array Commissioning Survey (MWACS). The MWACS is a multiwavelength low-frequency radio sky survey, covering approximately 6100 sq. deg in the southern sky over three bands centred

^{*} Tables 5–7 are only available at the CDS via anonymous ftp to cdsarc.u-strasbg.fr (130.79.128.5) or via

Table 1. List of quantities.

Symbol	Quantity
$S_{0.18}$	flux density at 180 MHz (from MWACS)
S_1	flux density at ~1 GHz (0.8 GHz from SUMSS or
	1.4 GHz from NVSS, if Dec $< -30^{\circ}$ or $> -30^{\circ}$,
	respectively)
S_{20}	flux density at 20 GHz (from AT20G)
$\alpha_{\rm low}$	spectral index between 120 and 180 MHz (MWACS)
$\alpha_{0.18-1}$	spectral index between 180 MHz and ~1 GHz
α_{1-20}	spectral index between ~1 and 20 GHz

at 119, 150, and 180 MHz. Nearly at the same time, Massaro et al. (2015) published the fifth edition of the Roma-BZCat, the most recent multi-wavelength list of blazars.

At the other end of the electromagnetic spectrum, Acero et al. (2015) have just released the third *Fermi*-LAT catalogue of gamma-ray sources (3FGL), based on Large Area Telescope (LAT) data collected with a longer exposure and an improved instrument and analysis characterization; furthermore, Ackermann et al. (2015) have realized the accompanying third catalogue of LAT AGNs (3LAC). These surveys therefore represent an invaluable resource to tackle the spectral characterization of gamma-ray blazars at low frequency with unprecedented detail and to discuss statistical significance and physical implications of the correlation between emission in the two bands. Indeed, Ackermann et al. (2011a) have studied with great accuracy the radio-gamma connection in the several GHz radio band, while only preliminary studies have been attempted for low-frequency radio data.

In this paper, we cross-correlate the MWACS catalogue with the BZCat, the 3LAC, and the list of unassociated sources of the 3FGL; when available, we also add high-frequency data from the Australia Telescope 20 GHz survey (AT20G, Murphy et al. 2010). All cross-correlations and analyses are carried out within the MWACS footprint, which is given in Sect. 2, along with an outline of the other radio and gamma-ray surveys and catalogues. Then we describe in Sect. 3 the construction of our working samples (blazars in the MWACS, gamma-ray AGNs in the MWACS, other gamma-ray sources in the MWACS) and present their overall properties in Sect. 4; finally, we discuss the results and give our conclusions in Sect. 5.

Throughout the paper, we use a Λ CDM cosmology with h = 0.71, $\Omega_{\rm m} = 0.27$, and $\Omega_{\Lambda} = 0.73$ (Komatsu et al. 2009). The radio spectral index α is defined such that $S_{\nu} \propto \nu^{-\alpha}$ and the gamma-ray photon index Γ such that $dN_{\rm photon}/dE \propto E^{-\Gamma}$. In Table 1 we give a list of the quantities used for flux densities and spectral indices throughout the paper.

2. Selected surveys and catalogues

2.1. MWACS catalogue

The MWACS catalogue (Hurley-Walker et al. 2014) is our main reference catalogue; we downloaded the final table from Vizier¹. This catalogue lists 14 110 sources, in the sky area approximately $0^{\circ} \leq RA \leq 127.5^{\circ}$ or $307.5^{\circ} \leq RA \leq 360^{\circ}$ ($20.5^{h} \leq RA \leq 8.5^{h}$) and $-58.0^{\circ} < Dec < -14.0^{\circ}$. Data were taken in October 2012. All the sources in this area have high absolute Galactic latitude, which is ideal for blazar studies (e.g. the 3LAC only contains high-latitude sources by construction).

For each source, the catalogue reports the flux density $S_{0.18}$ at 180 MHz and the spectral index α_{low} derived across the three frequency bands centred on 119, 150, and 180 MHz. The survey has ~3' angular resolution and a typical noise level of 40 mJy beam⁻¹, with reduced sensitivity near the field boundaries and bright sources. The faintest source has $S_{0.18} = 0.12$ Jy. Sources are marked with a spectral fit flag if the identification at the three frequencies is problematic: a type 1 fit classification indicates a spectral index determined by integrating an extended source, and a type 2 a forced fit.

2.2. BZCat

The BZCat is a multi-wavelength list of blazars, regularly updated since the release of the first edition in 2009 (Massaro et al. 2009). Massaro et al. (2015) have recently released the fifth edition, in which they report coordinates, redshift, and multifrequency (radio, millimetre, optical, X-ray, and gamma-ray) data for 3561 sources. The sources are classified as FSRQs, BL Lacs, and BL Lacs with significant contamination from the host galaxy, or blazars of uncertain type (BCU). All the sources in the BZCat are detected in the radio, and we used the radio flux density at ~1 GHz as reported in the catalogue: the radio data reported in the BZCat come partly from the NRAO VLA Sky Survey (NVSS, Condon et al. 1998) at 1.4 GHz or the Sydney University Molonglo Sky Survey (SUMSS, Bock et al. 1999; Mauch et al. 2003) at 0.8 GHz, for sources above or below Dec = -30° , respectively. In the following, we simply indicate this radio flux density as S_1 ; however, we considered the actual frequency at which the flux density was obtained whenever we used it to determine the spectral index.

2.3. 3FGL

The third Fermi-LAT catalogue (3FGL) is the deepest in the 100 MeV-300 GeV energy range. It is based on the first four years of science operation data from the Fermi mission, between 2008 August 4 and 2012 July 31, and it includes 3033 sources. Each source is characterized by its position, gamma-ray flux (photon flux, energy flux, flux in different energy ranges and in 48 monthly time bins), and photon index. The typical 95% positional confidence radius is ~0.1°. Most 3FGL sources are identified with or statistically associated with² blazars (see Sect. 2.4), but about one-third of the 3FGL does not have a plausible counterpart at other wavelengths. These socalled unassociated gamma-ray sources (hereafter, UGS) are not distributed uniformly in the sky: 468 fall in the Galactic plane $(|b| < 5^{\circ})$; they are most likely a mix of galactic and extragalactic discrete sources embedded in complex diffuse emission; the remaining 542 sources are presumably of extragalactic nature, possibly faint and as yet unrecognised blazars. In the present work, we have considered the data available through the Fermi Science Support Center³.

2.4. 3LAC

The third LAT AGN catalogue (3LAC) includes a total of 1563 gamma-ray sources among the $2192 |b| > 10^{\circ}$ 3FGL sources. These 3LAC sources are identified

¹ ftp://cdsarc.u-strasbg.fr/pub/cats/VIII/98

² An identification is claimed when correlated variability is observed, while the more common association between LAT sources and AGNs is based on statistical methods.

³ http://fermi.gsfc.nasa.gov/ssc/data/access/lat/4yr_ catalog/gll_psc_v16.fit

or statistically associated with AGNs by means of a Bayesian association (Abdo et al. 2010) or a likelihood ratio (Ackermann et al. 2011b) method. These 1563 gamma-ray sources are associated with 1591 objects (28 sources have double associations), consisting mostly (98%) of blazars or blazar candidates.

From the entire sample, Ackermann et al. (2015) have defined a "clean" subset of 3LAC single-association sources free of any analysis problems (e.g. sources strongly affected by changes in the diffuse emission model). In the following, whenever we mention the 3LAC we implicitly refer to this clean subset, which includes 1444 objects with 414 FSRQs, 604 BL Lacs, 49 BCUs, 353 blazar candidates, and 24 non-blazar AGNs.

We note that Ackermann et al. (2015) classify as blazar candidates both confirmed blazars of uncertain type (which have an optical spectrum and are also included in BZCat) and other blazar candidates (which do not appear in BZCat, but still present multi-wavelength features typical of blazars, such as a flat radio spectrum or a two-humped broadband SED). For consistency with the BZCat, we here consider separately gammaray blazars of uncertain type (which we indicate as BCU, as in BZCat) and gamma-ray blazar candidates.

In particular, we carried out our analysis starting from the machine-readable form of Table 4 in Ackermann et al. $(2015)^4$.

2.5. AT20G

The Australia Telescope 20 GHz (AT20G) survey is a radio survey carried out at 20 GHz with the Australia Telescope Compact Array (ATCA). It covers the whole sky south of Dec < 0° and includes 5890 sources above a 20 GHz flux-density limit of 40 mJy. The survey was carried out in two steps from 2004 to 2008: in a first phase, the ATCA realized a fast-scanning blind survey characterized by an overall rms noise of $1\sigma \sim 10 \text{ mJy beam}^{-1}$; then, all the sources brighter than 50 mJy were followed up to produce the final catalogue, with additional near-simultaneous flux-density measurements at 5 and 8 GHz for most sources.

The source composition of the AT20G is rather heterogeneous; however, high-frequency observations naturally favour the detection of flat-spectrum sources like blazars and in particular gamma-ray blazars (Mahony et al. 2010). As it also covers the entire MWACS footprint, we used it to complement the MWA data with higher frequency information for the blazar samples that we describe in the following section. In particular, we made use of the data in version 1.0 provided by the Vizier archive⁵.

3. Sample construction

After restricting the BZCat, the 3LAC, and the 3FGL lists to the MWACS footprint, we cross-matched them with the MWACS catalogue using TOPCAT (Taylor 2005). In the following subsections, we give details of the procedure.

3.1. BZCat-MWACS sample

Within the entire MWACS field, the BZCat contains 517 sources, divided into 153 BL Lacs, 327 FSRQs, and 37 blazars of uncertain kind. We cross-matched this subset with the MWACS catalogue, using a positional uncertainty of 5" on the BZCat coordinates and the 95% confidence error ellipse for each

MWACS source (obtained as $1.621\times$ the RA and Dec 1σ uncertainty reported in the MWACS catalogue). The 5" value for the BZCat positions is very conservative for most sources, some of which have positions from VLBI observations that are accurate at the subarcsecond level. However, we verified that a few additional sources are picked up if we increase the uncertainty from 1" to 5", although further increases do not pick up any more sources.

We also tried to cross-match the two catalogues with a fixed radius, using the same procedure based on the generation of 100 mock replicas that we adopted in our previous papers (Massaro et al. 2013a,b, 2014). This method provided a sanity check that the errors quoted in the MWACS catalogue are sensible. Therefore, we continued our analysis using the rigorous association method based on the source-by-source uncertainty. The accuracy of the MWA coordinates is affected by two components, one of random intensity that is due to the ionospheric phase contribution, and one dependent on the source flux density. Since sources with higher flux density have better constrained positions, this method maximizes the efficiency of our selection and the use of information retained from the data.

In total, we found 186 matches: 23 BL Lacs, 147 FSRQs, and 16 blazars of uncertain type. Within these 186 matches, 10 sources have MWACS spectral fit classification of type 1 or 2 (five sources of each type). By constructing 100 mock replicas of the BZCat sample, in which we shifted each position by 2° along a random position angle, and repeating the association procedure for each replica, we estimate that less than 1 of these 186 matches arises by chance (on average, 0.8 sources per fake sky).

We furthermore collected high-frequency data for the BZCat-MWACS sample by cross-correlating it with the AT20G survey catalogue. Murphy et al. (2010) calculated the uncertainty in right ascension and declination for the full AT20G sample as $\sigma_{RA} = 0.9''$ and $\sigma_{Dec} = 1.0''$, respectively. Using these values for AT20G and extending the positional uncertainty for BZCat sources from 1" to 5", the number of matches increases from 155 to 170, and then does not increase any further up to 30". We then considered all the 170 matches as bona fide associations. The 16 sources that do not have a match are all rather faint at both 180 MHz and 1 GHz, and they also have a steep spectral index ($\langle \alpha_{0.18-1} \rangle = 0.68$) and extrapolated flux densities generally below the AT20G sensitivity.

3.2. 3LAC-MWACS sample

The subset of the clean 3LAC sources localized within the MWACS footprint contains 249 objects; there are 87 BL Lacs, 71 FSRQ, 16 BCU, 73 blazar candidates, and 2 radio galaxies.

Similar to the BZCat sources, these objects have accurately known coordinates, therefore we followed the same association method described above. We stress that we used the positions of the low-energy counterparts listed in the 3LAC and not those of the gamma-ray sources, which are significantly less well determined and could result in a large number of spurious associations.

From our starting list, we found counterparts in the MWACS for 88 3LAC sources, divided into 19 BL Lacs, 52 FSRQ, 8 BCU, 8 blazar candidates, and 1 radio galaxy (PKS 0625–35). We note that the other LAT radio galaxy (Pictor A) does indeed appear in the MWACS data as a bright source, but was not entered in the final MWACS catalogue because of calibration difficulties brought about by its high brightness and

⁴ http://iopscience.iop.org/0004-637X/810/1/14/

suppdata/apj517471t4_mrt.txt

⁵ ftp://cdsarc.u-strasbg.fr/pub/cats/J/MNRAS/402/2403

large extent. It therefore does not enter our catalogue crosscorrelation either. Given the very low statistics for the population of gamma-ray radio galaxies, in the following we only focus on the 87 3LAC blazars and blazar candidates with counterparts in the MWACS. All but three of the sources (PKS 0451–28, PKS 2245–328, and PKS 2333–415) have spectral fit class 0. Following the same procedure as in Sect. 3.1 and considering the smaller number of sources in this case, we do not expect more than one of these matches to be spurious.

We also cross-matched this sample of 87 sources with the AT20G catalogue and obtained 81 matches. The six missing sources again have fairly steep spectral indices ($\langle \alpha_{0.18-1} \rangle = 0.66$) and low extrapolated flux densities (only the blazar candidate PKS 0302–16 exceeds an extrapolated flux density of $S_{20} = 100 \text{ mJy}$).

3.3. Other gamma-ray sources in the MWACS

The MWACS footprint covers 96 3FGL UGS. These sources have by definition no clearly localized counterpart, therefore we performed the cross correlation of this list with MWACS catalogue using the 95% confidence radius for each gamma-ray source that is reported in the 3FGL and the positional uncertainty associated with the MWACS coordinates as described in Sect. 3.1. We found 13 MWACS counterparts for 10 UGS, with seven single matches and three double matches. Three sources have a spectral index flag of 1, and one has 2.

Given the large positional uncertainty of the UGS positions and the local space density of the MWACS sources, we investigated the possibility that these are chance matches. To do this, we created 100 mock replicas of the UGS list, shifting the position by 2° in a random position angle, and repeated the association procedure with the same method as in the original list. We find 15 ± 3 MWA matches even starting with a random UGS catalogue.

For completeness, we also cross-correlated the remaining sources in the 3FGL (i.e. those that are neither associated with AGNs nor are UGS), again using the gamma-ray positional uncertainty. We found three more matches: two pulsars (PSR J0437–4715, PSR J0742–2822) and one starburst galaxy (NGC 253).

4. Results

Our three catalogues are presented in Tables 5–7, that are the list of MWACS sources associated with BZCat blazars (Table 5), with 3LAC gamma-ray blazars (Table 6), and with un-associated 3FGL gamma-ray sources (Table 7). In the next three subsections, we analyse these catalogues.

4.1. Blazars in the MWACS: catalogue and demographics

The 186 matches between BZCat and MWACS listed in Table 5 correspond to a detection rate of 36%. In Cols. 2 and 3 of Table 2, we report the detection rates divided by source class, which is clearly higher for FSRQs (45%) than for BL Lacs (15%); BCUs appear to have a similar detection rate as FSRQs (albeit with some uncertainty due to the small sample size).

In Fig. 1 we plot the histogram of the \sim 1 GHz flux density for the entire BZCat sources divided into two subsets according to whether they were detected at low frequency (green histogram) or not (red histogram). This plot shows that the MWACS detection probability has a strong dependence on the GHz flux density; in other words, the faintest blazars are very rarely associated with MWACS counterparts. This immediately explains

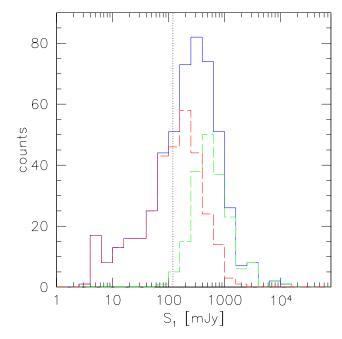


Fig. 1. Blazar flux density distribution at 1 GHz for the entire BZCat (blue solid line) and for the detected (green dashed line) and not detected (red dashed line) subset in MWACS. The dotted vertical line corresponds to $S_1 = 120$ mJy, i.e. the flux density limit of the MWACS survey extrapolated with $\alpha = 0.0$.

the highest detection rate found for FSRQs, since FSRQs are on average brighter than BL Lacs. However, it is still remarkable that about a half of the not detected blazars still have a ~1 GHz flux density higher than that of the faintest source in the MWACS catalogue (167/331 sources have $S_1 > 120$ mJy). If these sources had non-inverted spectra ($\alpha_{0.18-1} \ge 0.0$), we would expect them to be detected by MWACS, which implies that they have either an inverted spectrum or that they are strongly variable.

In Fig. 2 we also plot the simultaneous low-frequency spectral index α_{low} distribution for the entire MWACS catalogue and for the blazars. The cumulative distribution is also shown in the right panel. Even in the 120–180 MHz range, blazars have much flatter spectra than the rest of the radio sources in the extragalactic sky: the weighted average MWACS spectral index for blazars is $\langle \alpha_{low} \rangle = 0.57 \pm 0.02$, significantly flatter than the one obtained for the entire MWACS population, for which it is $\langle \alpha_{low} \rangle = 0.866 \pm 0.002$. FSRQs are marginally steeper ($\langle \alpha_{low} \rangle = 0.56 \pm 0.02$) than BL Lacs ($\langle \alpha_{low} \rangle = 0.49 \pm 0.05$).

For each source, we also calculated the non-simultaneous spectral index $\alpha_{0.18-1}$ between 180 MHz and ~1 GHz. The results show a flattening of the spectra from low to higher frequency for FSRQs of about $\langle \Delta \alpha \rangle = \langle \alpha_{0.18-1} \rangle - \langle \alpha_{low} \rangle \sim -0.25$, while BL Lacs maintain the same spectral index. This difference between FSRQs and BL Lacs stems from the average low flux density of BL Lacs at ~1 GHz because faint sources can reach the MWACS detection threshold more easily if they steepen at low frequency.

Finally, for the subset of sources with AT20G counterparts, we also computed the high-frequency spectral index $\langle \alpha_{1-20} \rangle$ between ~1 and 20 GHz. In this frequency range, the spectra are much flatter ($\langle \alpha_{1-20} \rangle = 0.096 \pm 0.004$), and no difference is found between FSRQs and BL Lacs. We report all the weighted mean values and the associated errors for the spectral indices in the various frequency ranges in Table 3.

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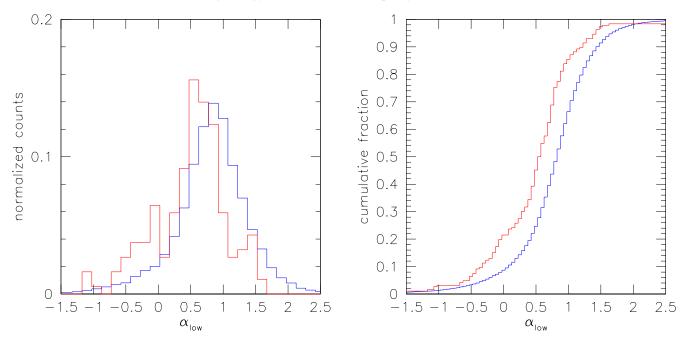


Fig. 2. Low-frequency spectral index counts (*left*) and cumulative (*right*) distributions for the entire MWACS catalogue (blue line) compared with BZCat-MWACS blazars (red line). Because the population counts are very different, normalized distributions are shown. The *x*-axis range is limited to the interval $-1.5 < \alpha_{low} < 2.5$ for illustration purposes.

Table 2. Low-frequency detection rates for BZCat and 3LAC source classes in the MWACS footprint.

	BZC	at	3LA	C
Class	ratio	%	ratio	%
Total	186/517	36%	87/247	35%
FSRQ	147/327	45%	52/71	73%
BLL	23/153	15%	19/87	22%
BCU	16/37	43%	8/16	50%
Candidates			8/73	11%

Notes. By construction, the BZCat does not contain blazar candidates. For the 3LAC, we did not include radio galaxies.

4.2. Gamma-ray blazars in the MWACS: catalogue and demographics

Table 6 reports the list of the 87 matches between the 3LAC and the MWACS catalogues. In Table 2 (Cols. 4 and 5) we also report the detection rate for the entire sample and for the individual sub-classes. The overall low-frequency detection rate is 35.2%. If we only consider the confirmed blazars, however, it increases to 45.4%, which is significantly higher than for the overall blazar population discussed in Sect. 4.1. In the sub-classes, the detection rate is highest for FSRQ (73.2%) and much lower for BL Lacs (21.8%); BCUs are in between (50.0%). Again, within each single class, gamma-ray detected sources have a larger detection rate at low frequency than the same kind of sources considered independently of their gamma-ray activity. Blazar candidates have a low detection rate of 11.0%, not surprisingly given their low average 1 GHz radio flux densities.

In Fig. 3 we show the histogram of the gamma-ray energy flux above E > 100 MeV averaged over the four years of the *Fermi*-LAT data. We indicate separately the set of all the 3LAC sources and the subsets of MWACS detected and not detected sources. The detected sources have higher gamma-ray fluxes or, in other words, the MWACS detection rate is

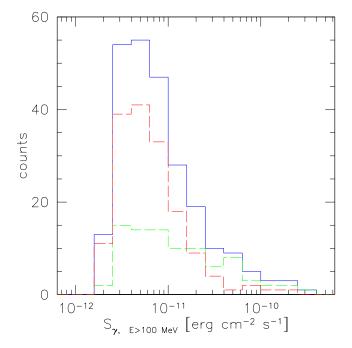


Fig. 3. Gamma-ray flux at E > 100 MeV distribution for the entire 3LAC sample (solid blue line). Dashed lines show separately the distribution for 3LAC sources with or without an MWACS counterpart (green and red lines, respectively).

higher for higher gamma-ray fluxes. Moreover, the detection rate above 4×10^{-11} erg cm⁻² s⁻¹ is 76% (16/21) and quite uniform across source types. The lower overall MWACS detection rate for BL Lacs with respect to FSRQs arises from the lower gamma-ray flux sources. This indicates that long-term gamma-ray and low-frequency radio fluxes are somehow correlated (see Sect. 4.3).

The low-frequency spectral index of the gamma-ray blazars is slightly flatter (by about $\Delta \alpha = 0.07$) than the index of the

Sample (1)	Class (2)	$\langle \alpha_{\rm low} \rangle \pm \sigma_{\langle \alpha_{\rm low} \rangle}$ (3)	$ \begin{array}{l} \langle \alpha_{0.18-1} \rangle \pm \sigma_{\langle \alpha_{0.18-1} \rangle} \\ (4) \end{array} $	$n_{\text{low, 0.18-1}}$ (5)	$\langle \alpha_{1-20} \rangle \pm \sigma_{\langle \alpha_{1-20} \rangle}$
BZCat-MWACS	Total	0.57 ± 0.02	0.337 ± 0.013	186	0.096 ± 0.004
	FSRQ	0.56 ± 0.02	0.297 ± 0.014	147	0.097 ± 0.005
	BLL	0.49 ± 0.05	0.46 ± 0.03	23	0.105 ± 0.014
3LAC-MWACS	Total	0.50 ± 0.03	0.305 ± 0.017	87	0.074 ± 0.005
	FSRO	0.49 ± 0.04	0.18 ± 0.02	52	0.038 ± 0.006

Table 3. Average spectral indices for BZCat and 3LAC source classes.

Notes. For each set, we report the weighted average and the error on the weighted average. Weights w_i on each spectral index α_i are determined as $1/\sigma_i$, where σ_i is the uncertainty on the spectral index as provided in the MWACS catalogue at low frequency, or is determined through propagation of the uncertainty on the measured flux density for $\alpha_{0.18-1}$ and α_{1-20} . The weighted average is then $\langle \alpha \rangle = \sum_{i=1}^{n} w_i \alpha_i / \sum_{i=1}^{n} w_i$ and the associated error is $\sigma_{\langle \alpha \rangle}^2 = 1/\sum_{i=1}^{n} w_i$.

 0.39 ± 0.04

19

 0.138 ± 0.012

Table 4. Correlation coefficient and significance for gamma-ray vs. MWACS data.

BLL

 0.42 ± 0.06

Sample	# objects	# redshift bins	r	ρ	<i>p</i> -value
(1)	(2)	(3)	(4)	(5)	(6)
All sources	87	_	0.26	0.27	_
All sources, with z	76	7	0.29	0.31	6.1×10^{-2}
FSRQ	52	5	0.21	0.25	0.15

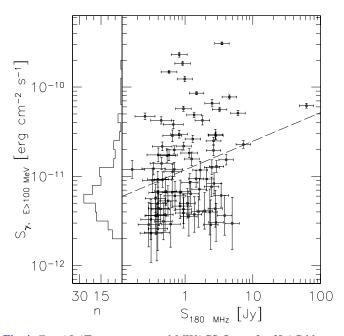
Notes. In each row, we indicate the sample considered in Col. (1), the number of objects included (Col. 2), and the redshift bins used for the statistical analysis (Col. 3), the Pearson *r* and Spearman ρ correlation coefficients and the statistical significance for the correlation between MWACS flux density and gamma-ray energy flux S_{γ} (Cols. 4–6) determined using the method of Pavlidou et al. (2012). The method does not consider sources without a measured redshift, therefore values in Cols. 3 and 6 are not determined for the entire sample.

entire blazar population (Table 3, Col. 3). Some flattening is also present in the low-to-mid and mid-to-high spectral indices. For the whole gamma-ray population and within each sub-class, the trend overall is one of flatter spectral indices as higher frequency ranges are considered.

4.3. Radio and gamma-ray correlation

As suggested in the previous section, it is relevant to search for a possible correlation between low-frequency radio flux densities and gamma-ray fluxes in blazars. We show in Fig. 4 the scatter plot of the gamma ray energy flux at E > 100 MeV vs. $S_{0.18}$. The *x*-axis range starts at $S_{0.18} = 120$ mJy, which corresponds to the lowest flux density of sources included in the MWACS. Below this threshold, we show the distribution of the gamma-ray flux for the blazars not detected in MWACS.

A simple linear fit yields a slope of $m = 0.32 \pm 0.13$, a linear correlation coefficient of r = 0.26, and a null-hypothesis *p*-value of $p = 1.5 \times 10^{-2}$, with 87 data points. This fit is somewhat influenced by the brightest radio source (PKS 0521-36). When we exclude this source from the sample, however, we still obtain a correlation coefficient of r = 0.22 and a slightly flatter, but still consistent, slope $m = 0.30 \pm 0.14$. To assess the significance of the observed correlation for the detected sources, we carried out a dedicated analysis based on the method described by Pavlidou et al. (2012) that has been applied by Ackermann et al. (2011a); this method combines data randomization in luminosity space (to ensure that the randomized data are intrinsically, and not just apparently, uncorrelated) and significance assessment in flux space (to explicitly avoid Malmquist bias and automatically account for the limited dynamic range in both frequencies and the presence of undetected sources). Since the method randomizes luminosities, we considered only sources with a measured redshift, which constitute the large majority of our sample (76 out of 87); moreover, it was shown that for reasonable assumptions



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Fig. 4. *Fermi*-LAT gamma-ray and MWACS fluxes for 3LAC blazars. In the main panel (*right*), we show the 4 yr gamma-ray energy flux at E > 100 MeV vs. MWACS radio flux density at 180 MHz; the dashed line is the best-fit linear regression. In the smaller *left panel*, we show the gamma-ray flux distribution for blazars that are not detected in MWACS; gamma-ray flux increases along the *y*-axis, and simple counts increase right-to-left along the *x*-axis.

on the redshift distribution of the sources without a known z, the method provides a conservative estimate of the significance.

We show the results in Table 4. The observed distributions provide evidence of only a low-significance correlation for the entire population ($p = 6.1 \times 10^{-2}$), and of no significant correlation at all when only FSRQs are considered (p = 0.15). We did not consider other smaller sub-samples (e.g. only BL Lacs, or only the flattest spectrum sources) because the number of objects would not have provided a statistically significant result.

The histogram in the left panel of Fig. 4 shows that the gamma-ray flux distribution of the gamma-ray blazars without a MWACS counterpart is consistent with the trend estimated for the detected sources. Future, deeper low-frequency surveys will probe this population and provide deeper insight into the possible correlation.

4.4. Other gamma-ray sources in the MWACS

We list in Table 7 the ten UGS that have one or more counterparts in the MWACS catalogue. Given the high spatial density of MWACS sources, it is not possible to claim any of them as a statistically significant association. We nonetheless list them here as a reference for possible follow-ups. In particular, 3FGL J0026.2–4812 and 3FGL J2130.4–4237 are spatially consistent with two moderately bright and flat-spectrum MWACS and SUMSS sources: MWACS J0025.6–4816, with $S_{0.18} = 0.65$ Jy and $\alpha_{0.18-1} = 0.50$, and MWACS J2131.1-4234, with $S_{0.18} = 1.04$ Jy and $\alpha_{0.18-1} = 0.63$.

5. Discussion and conclusions

The MWACS is at present the deepest wide-area survey at low frequency. By comparison, the VLA Low-frequency Sky Survey (VLSS Cohen et al. 2007) has a typical rms noise level of $\langle \sigma \rangle \approx 0.1$ Jy beam⁻¹. The VLSS blazar detection rate reported by Massaro et al. (2013b) was only ~26%, so that the sample presented in Table 5 becomes the deepest low-frequency blazar sample ever assembled. Moreover, this sample has simultaneous spectral information by construction, which is extremely valuable for studying core-dominated sources like blazars.

In the widely accepted unified scheme of radio-loud AGNs (Urry & Padovani 1995), blazars are the aligned counterparts of radio galaxies; in particular, BL Lacs are the aligned counterparts of low-power, edge-dimmed FR1 radio galaxies, and FSRQs are the aligned versions of high radio power, edgebrightened FR2 radio galaxies. This scheme has met with success, and Doppler boosting of radiation emitted from relativistic jets closely aligned to our line of sight (within ~5°) successfully explains most observational properties of blazars. However, Doppler boosting itself makes the blazar flat-spectrum cores apparently much brighter than the extended radio lobes, which then become very hard to study unless high-sensitivity images with high angular resolution are taken. For this reason, the opening of the low radio frequency window is of great value to the study of the extended emission in blazars (Massaro et al. 2013a,b, 2014; Nori et al. 2014; Trüstedt et al. 2014), and ultimately for the full validation of the unified schemes.

Our work has shown that the MWACS spectra of the blazars in our catalogues are on average (1) flatter (by about $\Delta \alpha \sim 0.3$) than those of the entire MWACS population and (2) steeper (by about $\Delta \alpha \sim -0.2$) than those of the same blazar population when considered between 180 MHz and ~1 GHz. The first fact shows that the core component still contributes significantly to the total emission. The second result is direct proof that extended, steep spectrum emission is also present in blazars.

The (mildly) significant correlation between the lowfrequency flux density and the gamma-ray energy flux, which is produced in the vicinity of the jet base, is also consistent with this scenario. Various works considering higher frequency radio observations have revealed a stronger and more significant correlation between the GHz-domain and gamma-ray data, for instance for the 1LAC samples (Ackermann et al. 2011a; Mahony et al. 2010; Ghirlanda et al. 2010, 2011). The fact that the MWACS data still provide a correlation, but weaker, agrees with additional, but not overwhelming, extended emission that is not beamed and therefore not correlated with the gamma rays.

Our spectral index measurements allowed us to estimate the intensity ratio between the emission from the flat-spectrum core and the steep-spectrum lobes. We assumed that the mean spectral index of the MWACS catalogue describes the extended emission component and that the α_{1-20} measured for our blazar population is a good approximation of the flat spectrum core spectral index. We decomposed the total flux density $S(\nu)$ as

$$S(\nu) = k_{\rm c}\nu^{-\alpha_{\rm c}} + k_{\rm l}\nu^{-\alpha_{\rm l}}$$

where k_c and α_c indicate the normalization and spectral index of the core component, and k_1 and α_1 are the same quantities for the lobes. By substituting $\alpha_c = 0.096$ and $\alpha_1 = 0.866$ and requiring that the average index between 120 and 180 MHz is $\alpha_{low} = 0.57$, we determined that $k_1/k_c \sim 75$.

Although k_1 and k_c , as well as their simple ratio, have little physical meaning by themselves, they are useful since they allow us to estimate the core-to-lobe flux density ratio at any frequency. For instance, the core-to-lobe flux density ratio is ~0.53 at 120 MHz and ~0.73 at 180 MHz, indicating that the core still contributes at low frequency, but the majority of the flux density is emitted in the lobes. With increasing frequency, the core becomes the dominant component, with $S_c/S_1 \sim 3.5$ at 1 GHz, and as large as ~27 at 20 GHz.

Clearly, these values are based on the mean indices and therefore are only suggestive of the average behaviour of the population. Moreover, the MWACS detected sources only constitute about 36% of the blazar population; about one half of the remaining blazars certainly have flat or inverted spectra, while we can say little about the other half. In general, these results will need to be complemented with deeper low-frequency surveys. Each single source can have wildly different contributions; in particular, the amount of Doppler beaming at the base of the jet can dramatically change the core flux and, accordingly, the component ratio. This is certainly the case for the sources with the flattest (or even inverted) MWACS spectral indices. We can directly test this by comparing the gamma-ray luminosity L_{γ} (which is affected by Doppler beaming) to α_{low} . In Fig. 5 we show the plot of these two quantities. While the points are scattered, the plot shows that the most inverted sources have generally a high gamma-ray luminosity (above $10^{46} \text{ erg s}^{-1}$), whereas the steeper sources span the entire range in luminosity, down to 5.4×10^{42} erg s⁻¹. Of course, the situation is also complicated by several other factors, such as luminosity distance and source type.

A larger luminosity distance corresponds to higher redshift so that the observed radiation is emitted at higher frequency in the rest frame, where the spectra are flatter; this has a qualitatively similar behaviour to the one produced by the core dominance: more luminous sources have flatter spectra both because they are more beamed and because their rest-frame spectra are intrinsically flatter. In this context, we have noted in Sect. 3.1 that most sources in the BZCat-MWACS sample also have a high radio frequency counterpart in AT20G. Of the few that do not, most are typically below the AT20G sensitivity if we extrapolate from low-frequency flux density and $\alpha_{0.18-1}$. Interestingly,

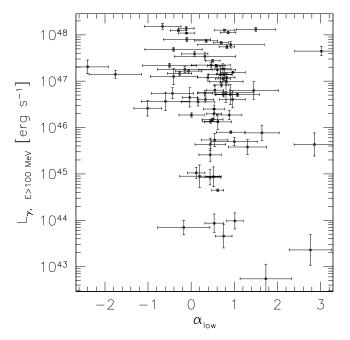


Fig. 5. Gamma-ray luminosity vs. low-frequency spectral index for the 3LAC-MWACS sample.

there are just two sources that have an extrapolated 20 GHz flux density higher than 100 mJy and they are both FSRQs at high redshift: 5BZQJ2300-2644 (z = 1.476) and 5BZQJ2327-1447 (z = 2.465), while the mean z in this sub-sample is z = 0.9 (in particular, they are the second and fourth most distant in the 16 source subsample). This could suggest that the rest-frame spectrum of blazars shows a rather complex behaviour, with a new steepening at even higher frequency (>20 GHz) after the flattening between the MWA band and the few GHz domain. A similar high-frequency spectral behaviour for compact sources has been reported by Chhetri et al. (2012) and Massardi et al. (2016).

We note that the gamma-ray luminosity is generally dependent on the source type (Ackermann et al. 2011b, 2015), with FSRQs more luminous than BL Lacs. By the peak of the synchrotron component of their SED, blazars are further classified into low-, intermediate-, or high-synchrotron peaked (LSP, ISP, HSP, respectively) sources that are characterized by a synchrotron peak frequency v_{peak} (Hz) such that $\log v_{\text{peak}} < 14$, $14 < \log v_{\text{peak}} < 15$, and $\log v_{\text{peak}} > 15$, respectively. The gamma-ray luminosity decreases from LSP to HSP blazars, similar to what has already been suggested for the blazar sequence by Fossati et al. (1998). While this scenario is the subject of a lively and long-lasting debate (e.g. Giommi & Padovani 2015; Potter & Cotter 2013; Meyer et al. 2011), we note that our sample is mainly composed of FSRO (which are typically LSP blazars). The reason for this composition lies in the still somewhat limited sensitivity of the MWACS. As we have noted, the present sample is the deepest available at present; however, faint sources like BL Lacs, and HSP blazars in particular, have lower flux density, and deeper catalogues are necessary to study the blazar population in greater depth.

In the very near future, significant resources are expected to become available, such as the recently released LOw Frequency Array (LOFAR) Multifrequency Snapshot Sky Survey (MSSS, e.g. Heald et al. 2015) and the GaLactic and Extragalactic All-Sky MWA Survey (GLEAM, Wayth et al. 2015). On the path towards the Square Kilometer Array, it will be possible to greatly extend the current picture of the connection between high-energy and radio emission in blazars (Giroletti et al. 2015) and more generally between the core and extended emission in radio-loud AGNs. The new catalogues will indeed allow us to characterize the low-frequency spectral properties of the still significant population of blazars that are missed in the present work. MSSS and GLEAM, which also partly overlap, will provide a combined dataset that is ideal for studying the low-frequency properties of *Fermi*-LAT blazars (1) simultaneously and (2) for the full sky. Moreover, because the new surveys will also cover the Galactic plane, important results might be obtained in the study of pulsars and other astrophysical accelerators such as supernovae.

For UGS sources, the situation is more complicated. The spatial density of low-frequency sources is already too high to claim associations only based on the spatial coincidence, and this is bound to increase at lower flux density limits. It will be necessary to take additional features into account to recognize sources of known gamma-ray emitters. This includes for example a flat spectrum (for core-dominated blazars) or pulsed emission.

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