



21 Such non-uniform inflow and pre-mature breakthrough of unwanted fluids can have a negative impact  
22 on well productivity, well life and hydrocarbon recovery (Dilib et al., 2012).

23 Engineers may use inflow control devices to try to counteract the negative consequences of this  
24 non-uniform inflow. In this case, the outer annulus of the well is subdivided into a number of isolated  
25 zones using packers, and the inner annulus is then similarly subdivided into isolated completion joints,  
26 because early breakthrough of unwanted fluids at the well is likely to be restricted to just one or a few  
27 completion joints (Mathiesen et al., 2011; Ouyang, 2009). Inflow control devices are then installed in  
28 each isolated completion joint to passively or actively control inflow from the reservoir, by restricting  
29 flow from the annulus into the production tubing (Birchenko et al., 2011; Dilib and Jackson, 2013).

30 Passive inflow control devices (ICDs) impose a fixed additional pressure drop from the reservoir  
31 into the tubing to counteract the heel-toe effect however they suppress the flow of all fluid phases,  
32 including the oil (Dilib and Jackson, 2013; Ouyang, 2009). Furthermore, the sizing of these devices is  
33 usually based on the initial conditions along the production well, which may be significantly different  
34 from the time-varying behaviour during long-term operation (Dilib et al., 2012; Dilib and Jackson,  
35 2013; Ouyang, 2009).

36 Alternatively autonomous inflow control devices (AICDs) provide active inflow control that can  
37 respond to the time-varying behaviour of the reservoir-well system. They are designed to introduce a  
38 pressure drop that varies depending on the volume fraction and flow rate of the different fluid phases  
39 entering the device. Typically, a larger pressure drop is applied to unwanted phases such as water or  
40 gas. AICDs are thus able to selectively choke unwanted fluid phases at the locations along the wellbore  
41 where they break through and their performance changes in response to time-varying reservoir  
42 behaviour. (Eltaher et al., 2014; Halvorsen et al., 2012; Mathiesen et al., 2011; Prebeau-Menezes et al.,

43 2013).

44 The additional pressure drop imposed by a single AICD valve is measured typically in laboratory  
45 experiments for a range of fluid properties, total flow rates, and individual fluid phase flow rates or  
46 volume fractions. These data are then used to derive empirical relationships for the pressure drop using  
47 adjustable variables that are fitted to the measurements (Halvorsen et al., 2012; Mathiesen et al., 2011).  
48 These experimentally derived mathematical expressions are then implemented into a reservoir simulator  
49 to capture the effect of AICD valves on inflow to the well and evaluate the overall recovery efficiency  
50 and production performance (e.g. Eltaher et al., 2019). For example, Halvorsen et al. (2012)  
51 implemented the empirical equations into the reservoir simulation software Eclipse™ and predicted that  
52 a significant increase of oil production can be achieved by installing AICDs at the Troll field. Leitao  
53 Junior and Negrescu (2013) employed the similar approach to assess the oil production at the Peregrino  
54 field. Aakre et al. (2018) used the well completion simulation tool NETool, which assumes steady-  
55 state one-dimensional (1-D) flow and incorporates the experimentally based empirical equations, for  
56 analysing the performance of oil recovery at the Midale field. Eltaher et al. (2019) proposed a  
57 simplified formula fitting to experimental data and applied it for optimising the inflow control design.

58 These laboratory experiments are expensive, as they require specialist equipment and staff, occupy  
59 significant space in a laboratory and are time consuming to perform. Consequently some researchers  
60 have attempted to derive the additional pressure drop based on direct numerical simulation of fluid flow  
61 through a single AICD device (Zeng et al., 2015). These simulations can be computationally very  
62 expensive and still need to be properly validated by comparison with experiments.

63 In many cases, it may be necessary to install two or more AICDs in a single completion joint (Luo  
64 et al., 2015; Ostrowski et al., 2010; Youngs et al., 2009) in order to achieve desired inflow performance,

65 however multiple AICDs can change the flow patterns (i.e. different from those for a single AICD) in  
66 the annulus. This means that the empirical relationships determined by fitting to experimental data for  
67 a single AICD, may no longer properly capture the total pressure drop from the annulus into the tubing.  
68 Direct use of these experimentally-derived equations for a single AICD to calculate the pressure drop  
69 imposed by multiple AICDs could cause significant inaccuracies in the predictions of reservoir  
70 simulation models. Thus, it is practically useful to develop an approach to extend the predictability of  
71 these formulations (e.g. by including a prefactor) for analysing production systems with multiple AICDs  
72 installed in each single completion joint.

73 This paper investigates the flow patterns resulting from two interacting AICDs and develops a  
74 modified pressure versus water cut relationship for these cases. We use state-of-the-art, high resolution  
75 numerical modelling techniques to capture the detailed physics and dynamics of multiphase flow in the  
76 inner annulus of a completion joint mounted with one or two AICD(s). Earlier work has shown that  
77 our numerical modelling techniques can capture the dynamics of multiphase flow in thin annuli, through  
78 comparison with experiments (Lei et al., 2018). The model is used to explore a range of relevant flow  
79 conditions with different flow rates and phase volume fractions and allows us to determine the pressure  
80 drop from the annulus to the tubing across one or two AICD(s). We focus here on oil-water flow, but  
81 the methods are equally applicable to oil-gas and gas-water flows; they are also equally applicable to  
82 study joints with three or more AICDs installed.

## 83 **2. Wellbore configuration and autonomous inflow control devices**

84 We study a typical wellbore configuration with inflow control (Fig. 1). The production well is  
85 divided into a number of isolated completion joints so that annular flow between neighbouring joints is  
86 eliminated. Each joint (12 m long) includes an outer, gravel-packed annulus, a mesh screen for sand

87 control and a pipe section (Fig. 2). The pipe section has an inner annulus region (5 m long) through  
 88 which fluids are transported into the tubing, and a closed region (7 m long) encapsulating the tubing but  
 89 having no communication with the surrounding gravel pack. The inner annulus is enclosed by a sand  
 90 screen, and part of it (4.5 m long) is partitioned into 48 parallel, narrow channels which restrict radial  
 91 flow around the inner annulus. The rest of the inner annulus (0.5 m long) has no partitions and hosts  
 92 the AICD(s). Table 1 summarises the geometric parameters of each component of the wellbore system.  
 93 During production, oil and water flow from the surrounding reservoir rock into the outer annulus, across  
 94 the sand screen, into the inner annulus and enter the tubing via the AICD(s) (see arrows in Fig. 2).

95 We focus on the two-phase flow of oil and water. The fluid properties are given in Table 2. We  
 96 assume that the AICD valve imposes an additional pressure drop  $\Delta p_{\text{AICD}}$  on the oil-water mixture as it  
 97 flows through the device, given by the empirical formula (Aakre et al., 2018; Eltahir et al., 2014;  
 98 Halvorsen et al., 2012; Mathiesen et al., 2011):

$$99 \quad \Delta p_{\text{AICD}} = \left( \frac{\rho^2}{\rho_{\text{cal}}} \right) \left( \frac{\mu_{\text{cal}}}{\mu} \right)^n a_{\text{AICD}} q_{\text{AICD}}^m, \quad (1)$$

100 where  $a_{\text{AICD}}$  is the strength parameter of the AICD,  $q_{\text{AICD}}$  is the total flow rate into the AICD,  $m$  is the  
 101 volume exponent, and  $n$  is the viscosity ratio exponent,  $\rho_{\text{cal}}$  and  $\mu_{\text{cal}}$  are the calibration density and  
 102 calibration dynamic viscosity, respectively, while  $\rho$  and  $\mu$  are the density and dynamic viscosity of the  
 103 oil-water mixture, respectively, given as (Aakre et al., 2018; Halvorsen et al., 2012; Mathiesen et al.,  
 104 2011):

$$105 \quad \rho = \alpha_o \rho_o + \alpha_w \rho_w, \quad (2)$$

$$106 \quad \mu = \alpha_o \mu_o + \alpha_w \mu_w, \quad (3)$$

107 where  $\alpha_o$  and  $\alpha_w$  are the volume fractions of oil and water, respectively;  $\rho_o$  and  $\rho_w$  are the densities of  
 108 oil and water, respectively. The parameters of a typical AICD valve obtained by fitting to laboratory

109 data (modified based on (Aakre et al., 2018) and used in this study) are given in Table 3.

### 110 **3. Numerical modelling methodology**

#### 111 **3.1 Modelling of the inner annulus**

112 To elucidate the impact of more than one AICD per completion joint on oil-water flow in the  
113 production system, we explicitly modelled the complex multiphase flow dynamics in a 2D model of the  
114 horizontally placed inner annulus with two AICD valves.

115 The 3-D problem was reduced to a two-dimensional (2-D) model (Fig. 3) associated with a  
116 distorted gravity field (Fig. 3c) (see (Lei et al., 2018) for the derivation details) by averaging across the  
117 annulus gap. Fig. 3a, shows the full, three dimensional (3-D), curvilinear coordinate system  $(x, y, z)$ .  
118 The  $x$  coordinate was defined to be along the pipe length ( $0 \leq x \leq L_i$ ), whilst  $y$  was around the perimeter  
119 ( $-\pi D_i/2 \leq y \leq \pi D_i/2$  with  $y = 0$  and  $y = \pm \pi D_i/2$  corresponding to the top and bottom of the annulus,  
120 respectively, and  $D_i$  being the mean diameter of the pipe). The  $z$  coordinate thus measures the distance  
121 across the annulus, where the origin for the  $z$  coordinate was along the mid-plane of the inner annulus.  
122 The thickness of the annulus was  $h$  so the distance of this mid-plane from both the outer and inner walls  
123 was  $h_i/2$ . We assumed that the flow velocity in the  $z$  direction was negligible ( $u_z = 0$ ). The annulus  
124 surfaces were assumed to be neutrally wetting for oil and water phases (i.e. not strongly wetted by either  
125 fluid with a contact angle of  $90^\circ$ ), and laminar flow was assumed through the annulus meaning that the  
126 velocity profile was parabolic in the  $z$  direction (Gondret and Rabaud, 1997).

127 The derived gap-averaged governing equations are presented in the following subsection. The  
128 validity of this 2-D representation was determined by comparing the flow patterns it predicts with those  
129 seen in experiments (Lei et al. 2018). More details can also be found in the supplementary material.

### 130 3.2 Governing equations

131 The gap-averaged governing equations (Lei et al., 2018) for compressible two-phase, oil-water  
 132 flow are given below. By conservation of volume, the sum of the volume fractions must sum to 1:

$$133 \quad \alpha_o + \alpha_w = 1. \quad (4)$$

134 The equations for the conservation of mass for oil and water phases are:

$$135 \quad \frac{\partial}{\partial t}(\alpha_o \rho_o) + \nabla \cdot (\alpha_o \rho_o \mathbf{u}) = 0, \quad (5)$$

136 and

$$137 \quad \frac{\partial}{\partial t}(\alpha_w \rho_w) + \nabla \cdot (\alpha_w \rho_w \mathbf{u}) = 0, \quad (6)$$

138 respectively. The equation of motion is

$$139 \quad \frac{\partial}{\partial t}(\rho \mathbf{u}) + \frac{6}{5} \nabla \cdot (\rho \mathbf{u} \otimes \mathbf{u}) = -\nabla p + \nabla \cdot \mu \left[ \nabla \mathbf{u} + (\nabla \mathbf{u})^T \right] - f \mathbf{u} + \rho \mathbf{g} + \sigma \kappa \delta \mathbf{n}. \quad (7)$$

140 Here,  $\mathbf{u} = [u_x, u_y]$  is the gap-averaged velocity vector,  $\nabla = [\partial/\partial x, \partial/\partial y]$  is the 2-D gradient,  $t$  is the time,  
 141 the bulk density is  $\rho = \alpha_o \rho_o + \alpha_w \rho_w$ ,  $p$  is the pressure, the bulk dynamic viscosity is  $\mu = \alpha_o \mu_o + \alpha_w \mu_w$ , the  
 142 gravitational acceleration vector is  $\mathbf{g} = [0, g \sin(2y/D_i)]$ ,  $f$  is the coefficient of frictional pressure loss  
 143 (equal to  $12\mu/h_i^2$  for the flow in the non-partitioned inner annulus and  $32\mu/d_c^2$  for the flow in the narrow  
 144 channels),  $\sigma$  is the surface tension,  $\kappa$  is the interface curvature,  $\delta$  is the Dirac delta function, and  $\mathbf{n}$  is the  
 145 interface outward-pointing unit normal. Surface tension is treated as a continuous surface force  
 146 (Brackbill et al., 1992). The densities of compressible oil and water are calculated respectively using:

$$147 \quad \rho_o = \frac{\rho_{o0}}{1 - c_o(p - p_0)}, \quad (8)$$

148 and

$$149 \quad \rho_w = \frac{\rho_{w0}}{1 - c_w(p - p_0)}, \quad (9)$$

150 where  $c_o$  and  $c_w$  are the compressibility coefficients of oil and water, respectively, and  $\rho_{o0}$  and  $\rho_{w0}$  are  
 151 their densities at the reference tubing pressure  $p_0$ .

### 152 3.3 Initial and boundary conditions on flow into the inner annulus

153 Fig. 4 shows the 2D geometry used to simulate the fluid flow in the inner annulus with one or two  
154 AICD valves. The fluids enter the model via 48 narrow, parallel channels and are produced from one  
155 or two model AICDs placed within the annulus.

156 We assume that the flow through each channel is approximately 1D due to the high aspect ratio  
157 of the channels and approximate the flow entering these channels from the outer annulus as distributed  
158 inflow along the length of each channel. The velocity of the imposed distributed inflow varied linearly  
159 along each boundary from zero at the end furthest from the AICD to a maximum at the end of the  
160 channel nearest to the AICD (Figs. 4a and b). We further assume that the oil and water are completely  
161 segregated by gravity as they approach the sand-screen from the outer annulus so that there is single-  
162 phase flow within each channel i.e. each channel contains only water or only oil. As water is denser  
163 than oil, the default condition is that water enters through channels closest to the base, and oil enters  
164 through channels nearest the top. We investigated the sensitivity of the results to this by testing the  
165 opposite end-member scenario, in which oil entered at the base, and water entered at the top. This did  
166 not materially alter the results. The inflow rates from the reservoir are assumed to be steady because  
167 the timescales over which multiphase flow evolves in the annulus and the reservoir are very different.  
168 Steady flow for a given inflow and AICD configuration occurs over the timescale of seconds, compared  
169 to hours to years in the reservoir.

170 We explored two inflow rate cases of  $Q_{\text{tot}} = 20$  and  $30 \text{ m}^3/\text{day}$  per completion joint, which  
171 correspond to approximately 125 bbl/day/joint and 187.5 bbl/day/joint, respectively, or approximately  
172 10,000 – 15,000 bbl/day for a total well completion length of 1 km. The Reynolds numbers of the flow  
173 in the annulus for these two inflow rate cases were  $\rho_{w0}Q_{\text{tot}}(2h_i)/\mu_w/(\pi D_i h_i) = 21.9$  and 32.8, confirming



174 that the flow is laminar (Beavers et al., 1970). We also examined a range of water cuts between 0 and  
175 1 by adjusting the inlet boundary condition such that water flowed into more channels to yield a higher  
176 water cut, and fewer channels to yield a lower water cut, while oil flowed into the remaining channels.

177 We defined the initial volume fraction of fluids inside the annulus based on the corresponding  
178 water cut value. A free-slip condition was used for the two longitudinal sides of the (unrolled) domain.

179 We did not include an explicit model of the flow through each AICD valve in the simulation but  
180 instead represented their effect on the flow via an outlet pressure boundary in the shape of a square. The  
181 pressure around the border of each square varied depending upon the amount of water and oil flowing  
182 across that boundary and was calculated as the sum of the reference tubing pressure  $p_0$  (constant) and  
183 the pressure drop imposed by the AICD,  $\Delta p_{\text{AICD}}$ , (Eq. 1). The first AICD was always located in the  
184 middle of the inner annulus domain (Fig. 4a) whilst the second AICD, if present, was located across the  
185 free slip boundary (see Fig. 4b). This meant it was decomposed into two parts, located on opposing  
186 lateral boundaries of the domain (Fig. 4b). An identical pressure for the two parts was enforced based  
187 on the overall flow across this AICD. The remaining boundaries of the domain were no-flow  
188 perpendicular to the boundary.

### 189 **3.4 Numerical methods**

190 The governing equations were solved using a mixed control-volume finite-element method, which  
191 has been validated against a series of benchmark cases of single rising bubbles, coalescence of two  
192 bubbles and droplet impacts (Xie et al., 2017, 2016, 2014). The computational domain was discretised  
193 using an unstructured grid of triangular  $P_1$ DG- $P_2$  elements (Cotter et al., 2009). A finite volume  
194 discretisation of the mass conservation equation and a linear discontinuous Galerkin discretisation of  
195 the momentum equation were used with an adaptive implicit/explicit time stepping scheme (Xie et al.,

2016). Within each time step, the equations were iterated using a pressure projection method until all equations are simultaneously balanced (Pavlidis et al., 2014; Xie et al., 2014). The interface dynamics were captured through a compressive advection-based volume-of-fluid approach, which uses a novel and mathematically rigorous nonlinear Petrov-Galerkin method for maintaining sharp interfaces (Pavlidis et al., 2016). Surface tension was modelled using a diffused-interface formulation based on the volume fraction field (Xie et al., 2016). The numerical algorithm is summarised in Fig. 6.

The simulation used a fixed mesh with different discretisation settings for different subdomains (Fig. 5b). In the narrow channels, a structured mesh was used with element edge lengths in the tangential and longitudinal directions of 0.002 m and 0.1 m, respectively (a much larger element size was used for the longitudinal direction to reduce computational costs without violating the model accuracy). Our numerical solver is sufficiently robust that it can converge to a solution when such high aspect ratio elements are used (Xie et al., 2014). For the inner annulus hosting the AICD(s), an average element size of 0.002 m was used to build an unstructured mesh and a local refinement with average element sizes of 0.001 m was applied in the vicinity of the AICD(s). These values were chosen following a mesh sensitivity analysis (see the supplementary material for the details). The total number of elements was almost 60,000. An adaptive time stepping scheme was used that ensured all time-steps conformed to the Courant–Friedrichs–Lewy (CFL) condition with the CFL number being set to 1, i.e. time step  $\Delta t \leq h/u$ , where  $h$  is the local element size and  $u$  is the local fluid velocity. The run time for each simulation was about 600 hours on a desktop computer equipped with an Intel(R) Xeon(R) CPU E5-2697@2.30 GHz.

### 3.5 Model validation and verification

The flow dynamics in a cylindrical annulus for both oil-water and gas-water flow predicted by the

218 numerical model have been previously validated by comparison against experimental results (Lei et al.  
219 2018). A summary of the experimental setup and model validation results is also provided in the  
220 supplementary material.

221 In addition, we verified that the numerical model gave the same average pressure drops across the  
222 AICD as predicted by Eq. (1) for single-phase flow (water or oil) and two-phase oil-water flow (with a  
223 fixed water cut of 0.5) through a single AICD, for a range of flow rates. We measured the pressure  
224 drop averaged around the boundary of the AICD and the tubing, and then compared this with that  
225 predicted using Eq. (1). The very close match (Fig. 7) confirmed that the chosen outlet boundary  
226 conditions mimicked the flow rate and pressure drop behaviour as observed in a real AICD. There was  
227 a much higher pressure drop when water was flowing compared to oil, because the AICD was designed  
228 to choke-back the flow of water.

## 229 **4. Simulation results**

### 230 **4.1 Single AICD**

231 We first studied the fluid patterns obtained in a system with a single AICD together with the  
232 pressure drops across the AICD and the total flow rate and the oil and water flow rates through it, for a  
233 flow rate of  $Q_{\text{tot}} = 20 \text{ m}^3/\text{day}$  and a range of water cuts (Fig. 8). Water entered the annulus from the base  
234 while oil entered from the top.

235 Fig. 8 shows the pressure drop measured across the AICD and the flow rates through it as a function  
236 of time. Steady-state flow was reached within 1.5 seconds in all cases (a very short timescale compared  
237 to the evolution of flow in the reservoir, which evolves over hours to years). Note that the total outflow  
238 rate across the AICD exhibited slight fluctuations because of the fluid compressibility and the choking-  
239 induced pressure variation.

240 Fig. 9 shows distribution of oil and water over time on the channels and the annulus at different  
241 times and water cuts. For low water cuts (e.g. 0.1), water that entered the annulus via the lower channels  
242 coned upwards to reach the AICD located at the top of the annulus (Fig. 9a). For intermediate water  
243 cuts (e.g. 0.5), the water cone became much wider, and approximately equal volumes of water and oil  
244 exited the annulus via the AICD (Fig. 9b). At high water cuts (e.g. 0.9), the water phase dominated  
245 the flow into the AICD (Fig.9c).

246 Fig. 10 gives the pressure drops across the AICD and flowrates through it for an injection rate of  
247  $30 \text{ m}^3/\text{day}$ . There is a larger pressure drop across the AICD compared to that seen for  $Q_{\text{tot}} = 20 \text{ m}^3/\text{day}$   
248 (as expected) and again steady state is reached very quickly ( $\sim 1 \text{ s}$ ). The flow patterns obtained for  $Q_{\text{tot}}$   
249  $= 30 \text{ m}^3/\text{day}$  and the different water cuts were very similar to those for  $Q_{\text{tot}} = 20 \text{ m}^3/\text{day}$  and are not  
250 shown here to avoid redundancy.

251 Fig. 11 compares the AICD pressure drops as a function of water cut obtained from simulation  
252 with those predicted by Eq. (1) when the AICD was located at the top or bottom of the annulus for the  
253 case when water entered the annulus from the bottom as well as the case when water entered from the  
254 top. Fig 11a shows the results for  $20 \text{ m}^3/\text{day}$  when water entered the annulus from the top and bottom.  
255 Fig. 11b show the results for the  $30 \text{ m}^3/\text{day}$  flow rate case. All pressure drops were obtained after a  
256 simulation time of 1.5 s, when it was assumed that steady state had been achieved. The AICD pressure  
257 drop increased as the water cut increased, demonstrating its selective choking effect as expected. More  
258 importantly, there is good agreement between the numerical predictions and those obtained from the  
259 AICD formula (Eq. 1), irrespective of the position of the AICD and whether water entered the annulus  
260 from the base or top. The results confirm that the exact details of how water enters the inner annulus  
261 and the position of a single AICD have negligible effect on flow through, and the pressure drop across

262 the AICD.

## 263 **4.2 Two AICDs**

264 We next investigated the oil-water flow in an annulus with two AICDs, one located at the top of  
265 the annulus and one at the base.

266 Fig. 12 shows the simulation results of flow rate and pressure drop for the case of  $Q_{\text{tot}} = 20 \text{ m}^3/\text{day}$ ,  
267 Again, steady state was reached after around 0.2-1.5 seconds. As expected, the pressure drops imposed  
268 by each AICD increases with water cut. At the lowest water cut the pressure drop across the lower  
269 AICD is slightly higher than that of the upper AICD suggesting there is more water flowing into the  
270 lower AICD while the total outflow rate from the upper AICD was higher than that of the lower AICD.  
271 This difference in pressure drops across the AICDs increases for the intermediate water cut case (0.5)  
272 and then decreases again for the highest water cut case (0.9).

273 Fig. 13 shows the oil and water distribution seen around the top and bottom AICDs as a function  
274 of time for different water cuts. When the water cut was low (e.g. 0.1), the water phase, which occupied  
275 the lower part of the annulus, left the annulus only via the lower AICD (Fig. 13a). The upper AICD is  
276 surrounded by oil and the lower AICD is also mostly surrounded by oil. This is consistent with the  
277 lower pressure drops measured across both AICDs and the slightly higher pressure drop seen across the  
278 lower AICD (Fig 12a). For intermediate water cuts (0.5), the lower AICD is surrounded by water. The  
279 water also cones up to partially outflow via the upper AICD (Fig. 13b). Again this is consistent with  
280 the increased pressure drop seen across both AICDs for this case, together with the larger difference in  
281 pressure drop seen across the lower AICD (Fig. 12b). For the highest water cut (0.9), the water phase  
282 completely surrounds the lower AICD and is also the dominant phase around the upper AICD (Fig.13c).  
283 Again, this is consistent with the pressure drops measured across each AICD (Fig. 12c)

284 Fig. 14 gives the simulation results for flow rate and pressure drop for the case of  $Q_{\text{tot}} = 30 \text{ m}^3/\text{day}$ .  
285 As expected the pressure drops across the AICDs are higher than those obtained when  $Q_{\text{tot}} = 20 \text{ m}^3/\text{day}$ .  
286 The flow pattern evolution for  $Q_{\text{tot}} = 30 \text{ m}^3/\text{day}$  was very similar to that for  $Q_{\text{tot}} = 20 \text{ m}^3/\text{day}$  and is not  
287 shown to avoid redundancy.

288 We analysed the variation of the absolute pressure in the annulus by plotting a polar diagram for  
289 the cross-section containing the two AICDs (Fig. 15). The pressure around the annulus is  
290 approximately uniform apart from close to the AICDs however, the magnitude of the pressure increases  
291 with water cut due to pressure around the boundary of both the AICDs increasing with water cut. There  
292 is a greater drawdown of pressure around the upper AICD for both the 0.5 and 0.9 water cut cases,  
293 because there is a higher flow rate of oil into this AICD (e.g. the top AICD in Fig. 12) so the pressure  
294 around the boundary of this AICD is lower. This indicates a self-organisation of the flow partitioning  
295 between the two AICDs resulting in the oil-water flow pattern in the annulus tending towards a steady  
296 state.

297 Fig. 16 compares the simulated pressure drops across each AICD (calculated after 1.5 s when  
298 steady-state flow was achieved) with the predictions of Eq. 1 as a function of water cut for two different  
299 total flow rates. The results obtained when water enters the inner annulus from the top rather than the  
300 bottom are also shown. Unlike the single AICD case (Fig. 11) there is a marked difference between the  
301 results of the numerical simulation and the AICD equation, especially when the water cut is larger than  
302 0.2. Not only are the pressure drops across both AICDs higher, there is a different pressure drop across  
303 each AICD. This is because there are different flows and water cuts into each AICD and the flow  
304 patterns of oil and water for the two AICD case (Fig. 13) are different from those seen in the single  
305 AICD case (Fig. 11). The simple mathematical calculation using Eq. (1) assumes that the flows into

306 and around the two AICDs are identical and the flow pattern within the inner annulus is not altered by  
307 the presence of 2 AICDs. This difference is particularly noticeable when water cut is high. The  
308 results are very similar whether water enters the inner annulus from the top or bottom channels.

309 We calculated the average pressure drop between the annulus and the tubing and then computed  
310 the ratio  $\eta$  of this pressure drop derived from numerical simulation to the solution of the AICD formula  
311 for two different flow rates (Fig. 17). It can be seen that  $\eta$  is close to 1 when the water cut is smaller  
312 than 0.2, but abruptly increases to a maximum value of approximately 2.4 when the water cut is  
313 increased to around 0.3-0.4, beyond which  $\eta$  gradually decreases to 1 as the water cut approaches unity.  
314 The peak value of  $\eta$  tends to shift slightly to the left in Fig. 17 as the total flow rate increases, but the  
315 general variation of  $\eta$  seems to be reasonably independent of the total flow rate, at least for the two  
316 cases examined here. Importantly, the location of the AICD, and whether the water enters the annulus  
317 from the top or bottom, have a relatively small impact on the  $\eta$  value, as indicated by the shaded areas  
318 in Fig. 17. We suggest that the coefficient  $\eta$  may be used as a “correction factor” to the AICD formula  
319 to improve its predictability and assess the uncertainty when dealing with a completion joint with two  
320 AICDs.

## 321 **5. Discussion**

322 The correction factor, shown in Fig. 17, was derived assuming fully segregated inflow of water  
323 and oil into the completion joint. In reality, there may also be unsegregated flow occurring. Further  
324 detailed simulation work is needed to investigate the impact of these different inflow conditions, but  
325 capturing the dynamics of the oil-water interfaces in these complex flows would be very  
326 computationally expensive. We speculate that the behaviour of the completion system with  
327 unsegregated inflow will be bounded by the results of our numerical simulation assuming fully

328 segregated inflow and the direct calculation by the AICD formula assuming fully mixed inflow. We  
329 suggest that the possible impact of these non-segregated flows on reservoir performance could be  
330 evaluated approximately by performing a sensitivity analysis using our simulation approach to derive  
331 the upper bound and the original AICD equation to calculate the lower bound.

332 It should be noted that the characteristic correction factor curve reported here will probably be  
333 affected by the intrinsic properties of the fluids and completion system, such as fluid viscosity, fluid  
334 density, the AICD design, number of AICDs and possibly the geometry of the inner annulus. Further  
335 simulation studies are needed to evaluate the impact of these factors on the shape and magnitude of the  
336 correction factor curve.

337 In the absence of these quantitative studies, our results indicate that the installation of 2 AICDs in  
338 a completion joint will significantly increase the pressure drop between the inner annulus and tubing at  
339 intermediate water cuts (between 0.3 and 0.6). This increase does not seem to depend on total flow rate  
340 into the joint. The possible impact of this pressure drop could be estimated by comparing simulation  
341 results using the single AICD formula with one in which the pressure drop is doubled for these  
342 intermediate water cuts.

## 343 **6. Conclusions**

344 In this paper, we have investigated, using detailed simulation of the flow in the annulus, how the  
345 oil-water flow pattern and associated pressure drop change when there are two AICDs in a completion  
346 joint rather than one. Our model has provided new insights into the flow interactions between the two  
347 AICDs. There is a different flow pattern around each AICD when there is two-phase flow in the annulus  
348 mounted with more than one AICDs. The interaction between the AICDs results in self-organised  
349 behaviour. It also results in a different average different pressure drop between the annulus and the



350 tubing at intermediate water cuts when there are two AICDs in the annulus rather than one. This average  
351 pressure drop is higher than would be predicted, assuming the flow with two AICDs is identical to when  
352 there is a single AICD. We have quantified this discrepancy as a water cut-dependent correction to the  
353 AICD equation (derived in the literature for the case of single AICD) extending its predictability for  
354 the case of two AICDs. This correction could be used in reservoir simulation models to better capture  
355 the pressure drop across a single completion containing two AICDs.

356 Our modelling method also provides a generalised framework for exploring further scenarios, e.g.  
357 with even more AICDs mounted in a completion joint or different AICD types. Our investigations  
358 have shown that the detailed flow dynamics within the annulus can affect the well performance.  
359 Further research is needed to better understand these impacts.

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370 (<http://www.imperial.ac.uk/matar-fluids-group>).

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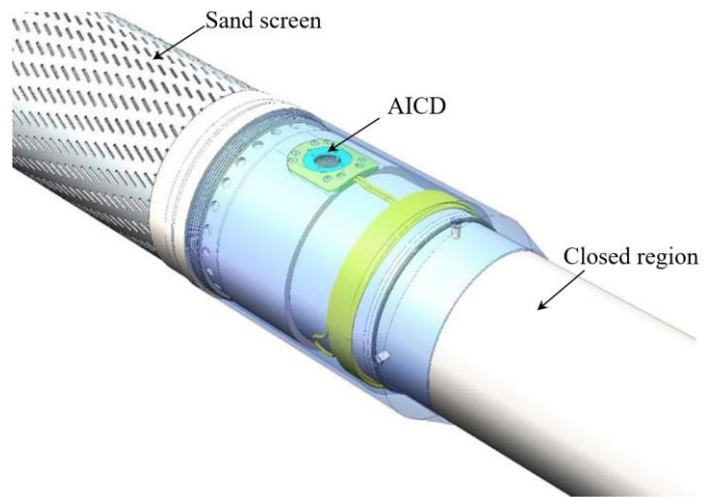
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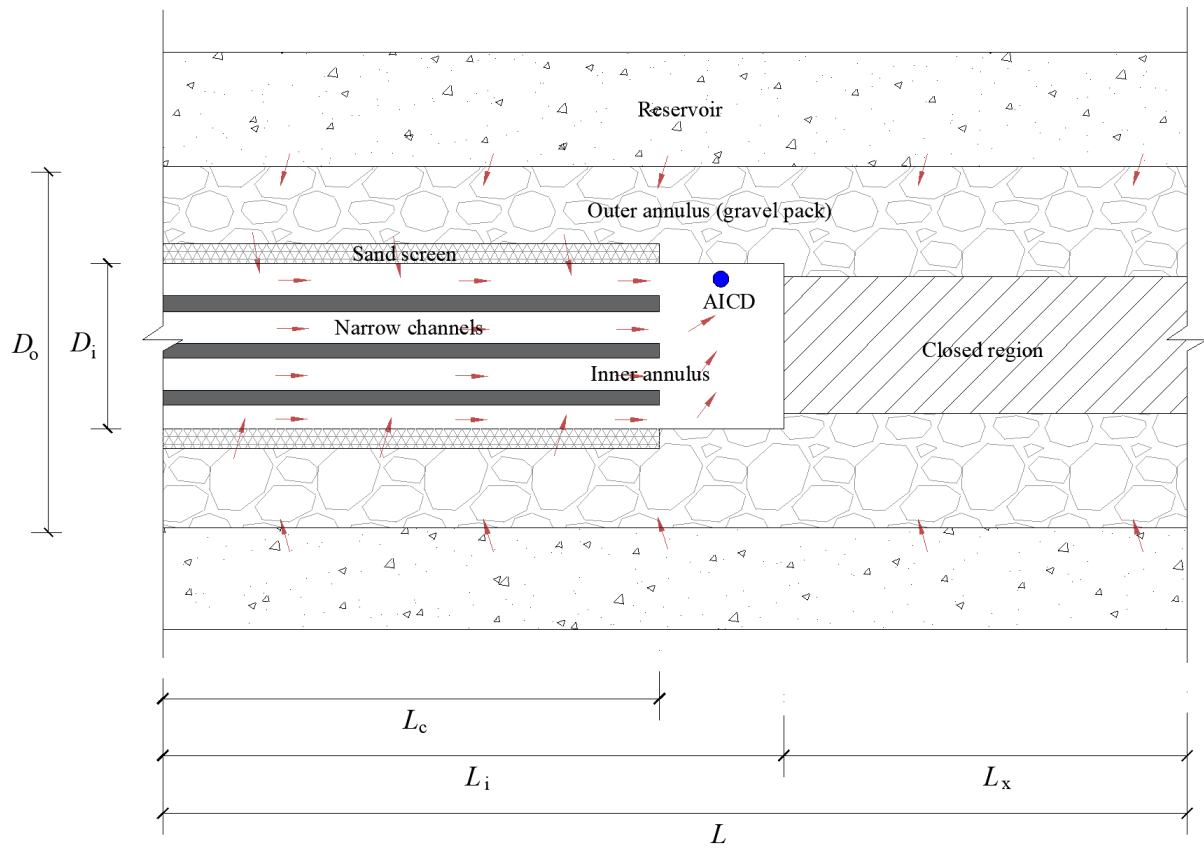


452

453 **Fig. 1.** A typical wellbore configuration, in which the AICD is mounted on the base pipe associated with a sand

454

screen mesh (after Aakre et al., 2018).

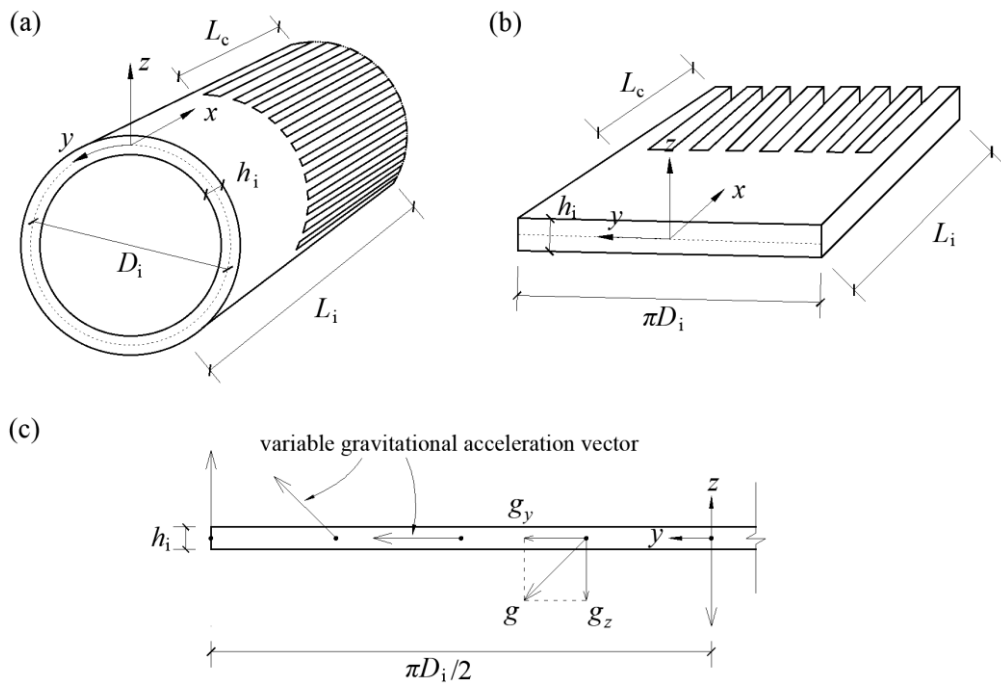


455

456 **Fig. 2.** Schematic showing the configuration of a completion joint for oil production in a hydrocarbon reservoir.

457 The arrows indicate the direction of flow from the reservoir into the wellbore system, successively passing

458 through the outer annulus (gravel pack), sand screen, inner annulus and AICD.



459

460

**Fig. 3.** Schematic of (a) the inner annulus and (b) the equivalent Hele-Shaw cell. (c) An illustration showing

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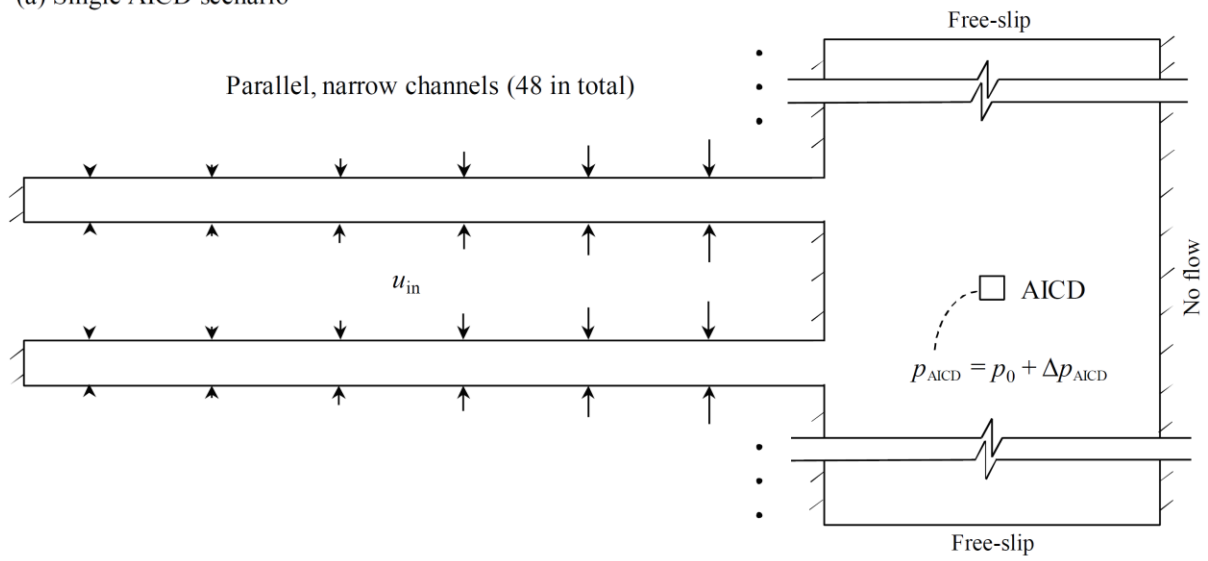
how the direction of gravitational acceleration changes along the equivalent Hele-Shaw cell to ensure the flow

462

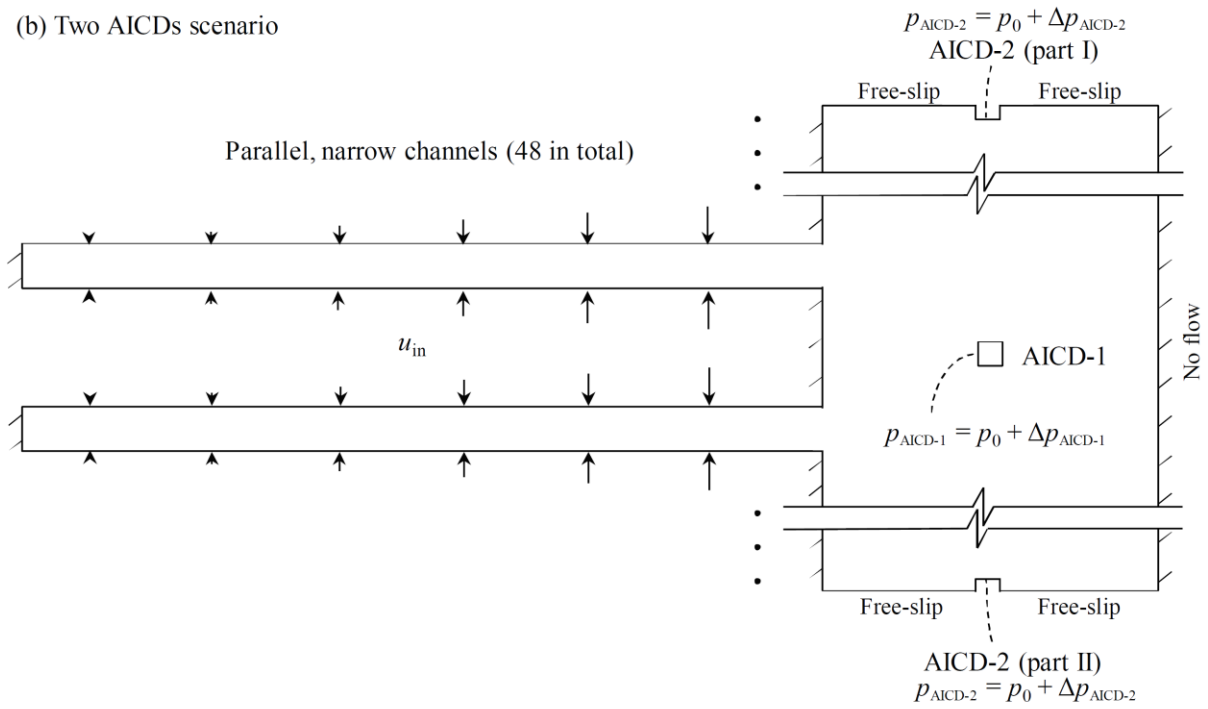
replicates that seen in the actual annulus.



(a) Single AICD scenario



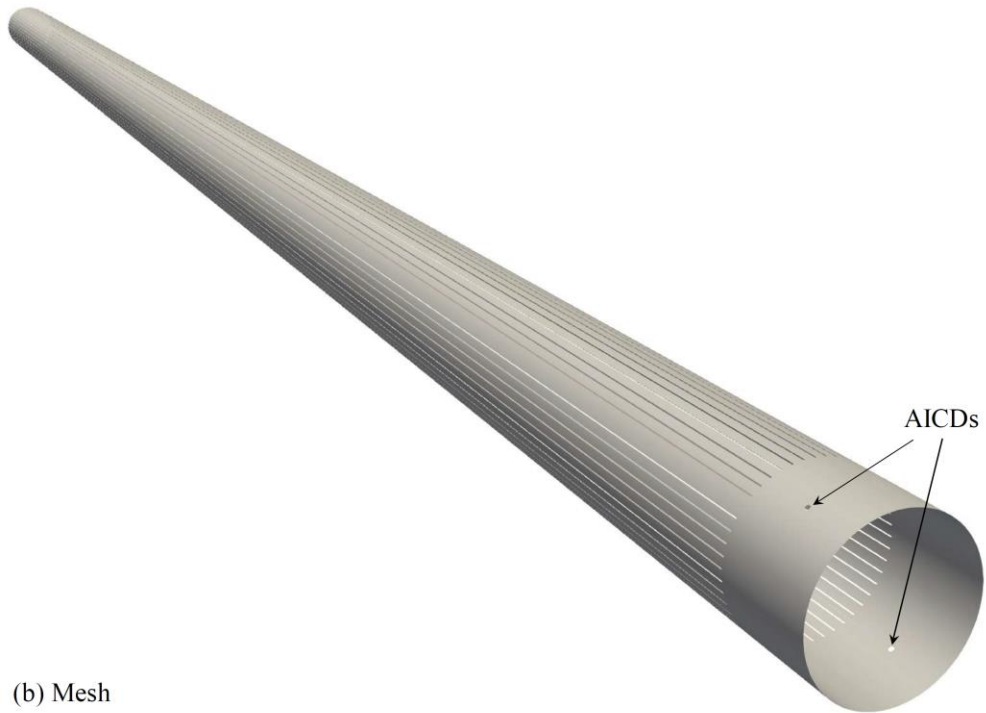
(b) Two AICDs scenario



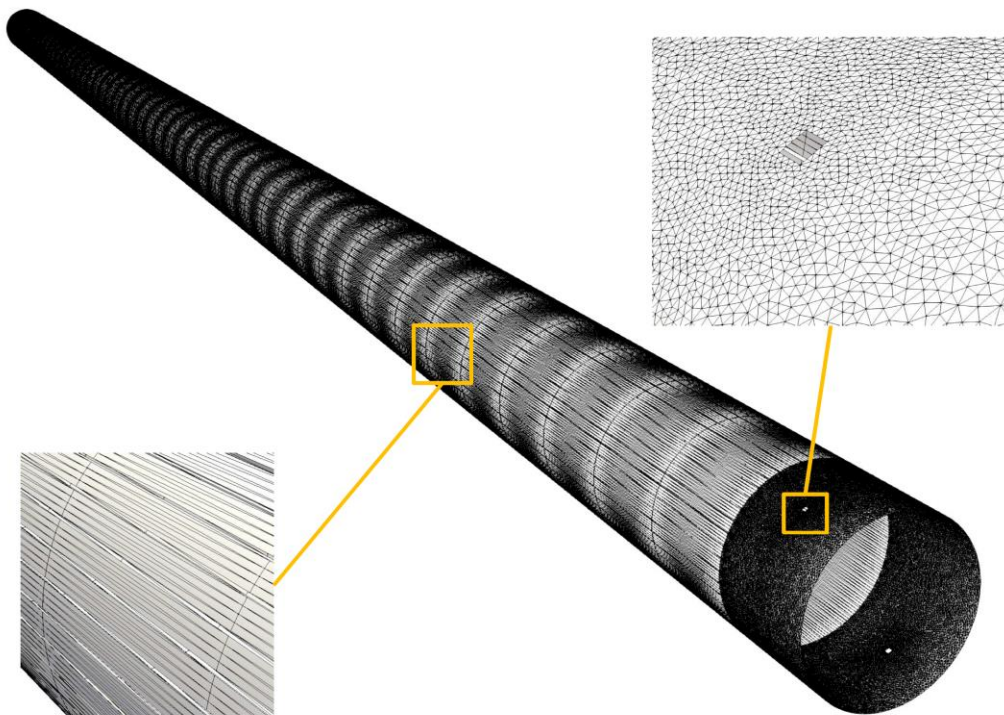
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464 **Fig. 4.** Model representation and set-up for the inner annulus mounted with (a) a single AICD or (b) two AICDs.

(a) Geometry



(b) Mesh

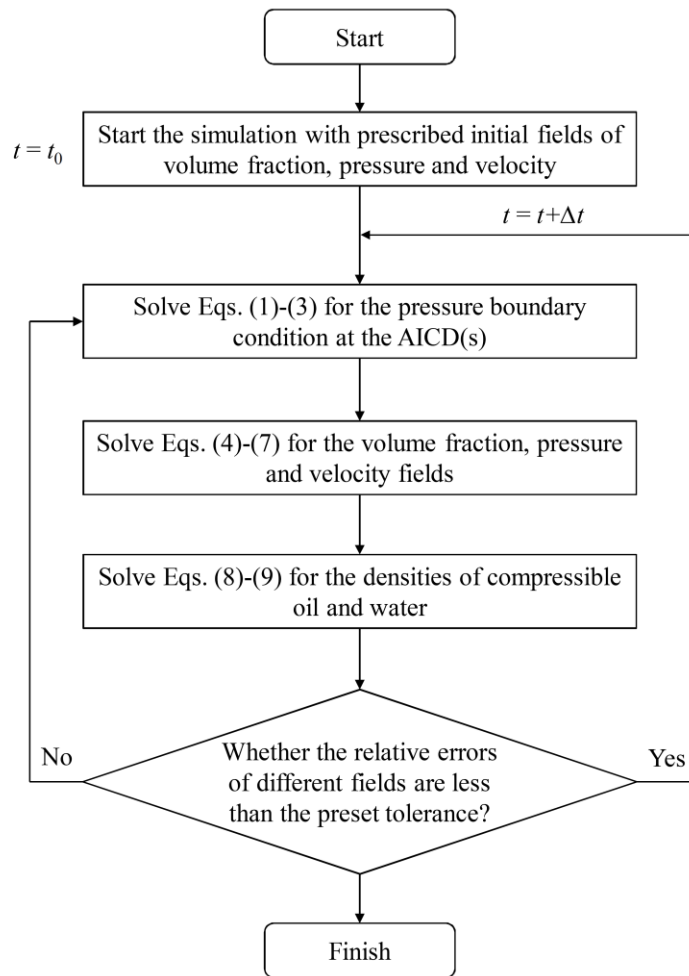


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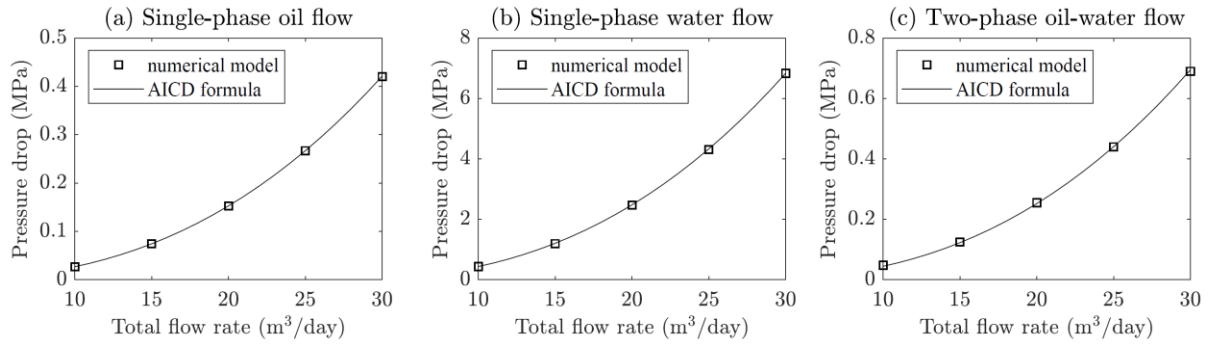
**Fig. 5.** (a) Geometry and (b) mesh of the 2-D numerical model projected onto the 3-D Cartesian coordinate system for visualisation.



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469

**Fig. 6.** Flowchart for the numerical calculation.

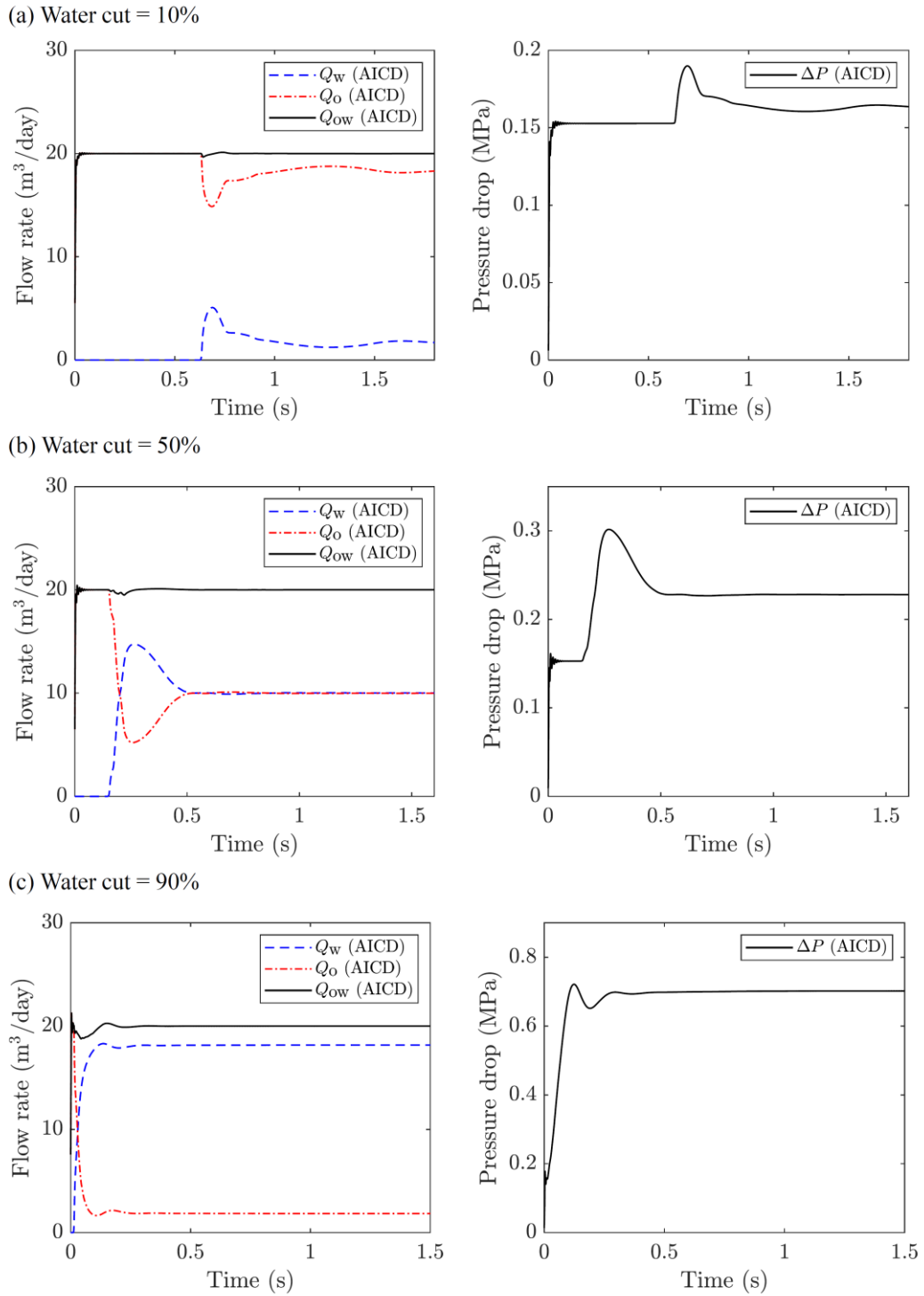


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471 **Fig. 7.** Pressure drop imposed by the AICD for single-phase (a) oil or (b) water flow and (c) two-phase oil-water

472

flow (with a water cut of 0.5) of different total flow rates.



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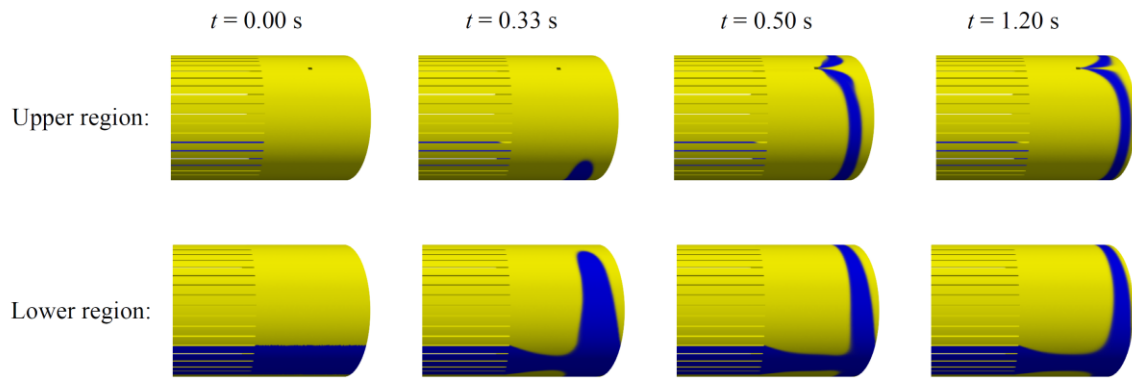
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**Fig. 8.** Variation of flow rate (left) and pressure drop (right) at the AICD for different water cut cases with the

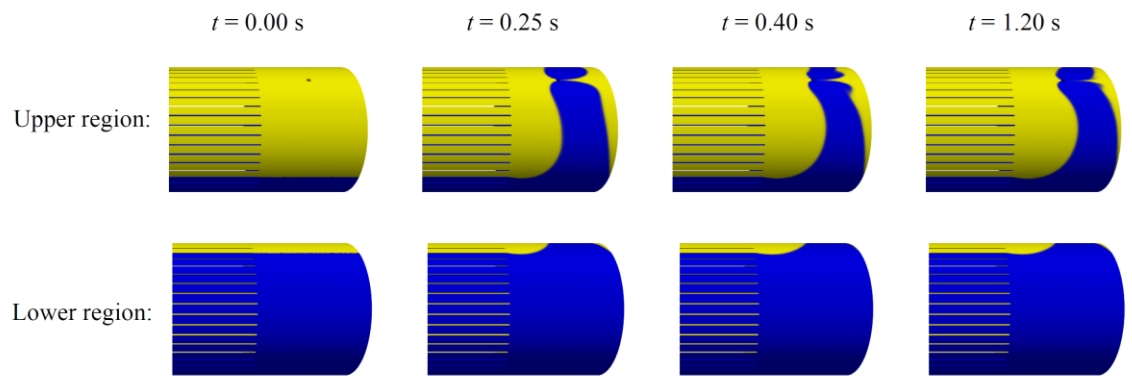
475

total flow rate  $Q_{\text{tot}} = 20 \text{ m}^3/\text{day}$ .

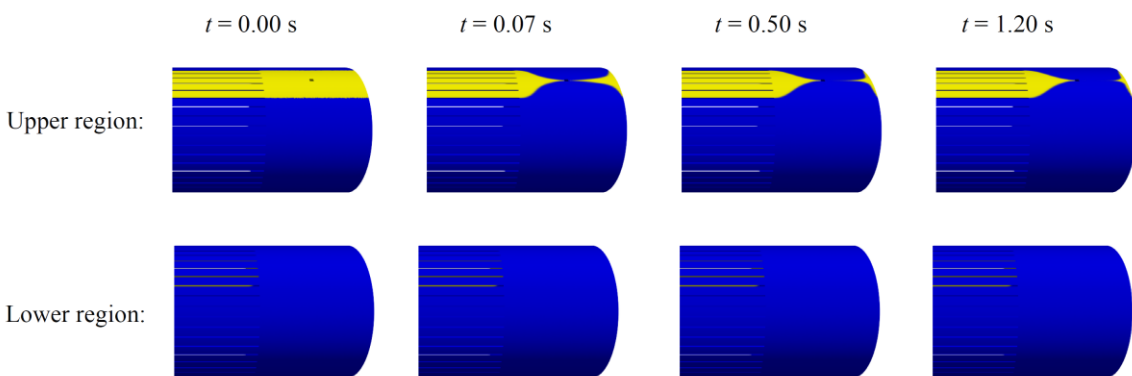
(a) Water cut = 10%



(b) Water cut = 50%



(c) Water cut = 90%



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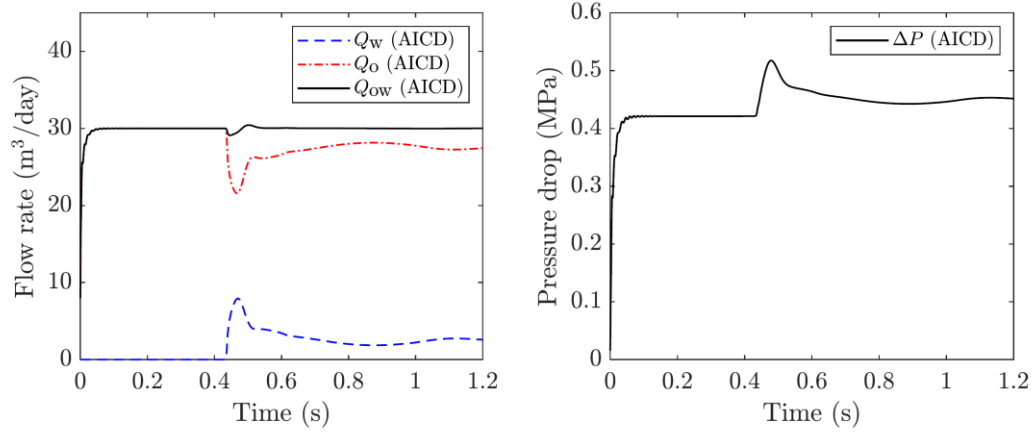
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**Fig. 9.** Variation of flow pattern at the AICD for different water cut cases with the total flow rate  $Q_{\text{tot}} = 20$

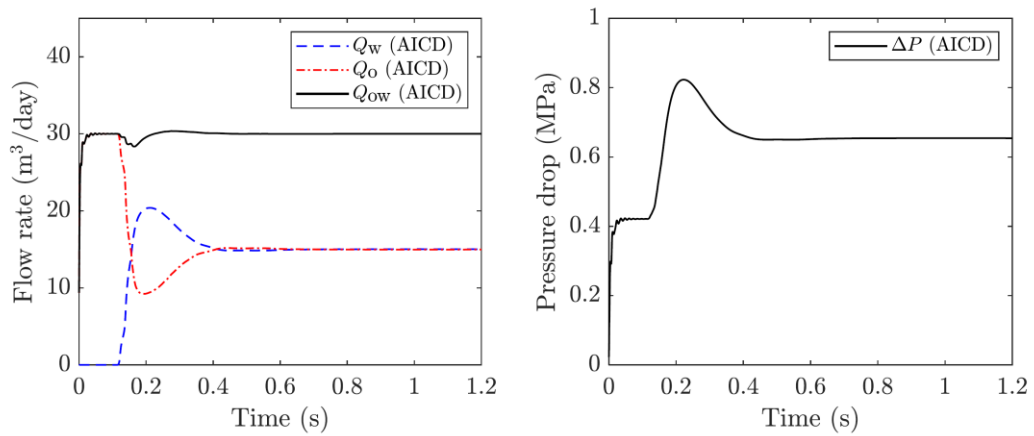
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$\text{m}^3/\text{day}$ .

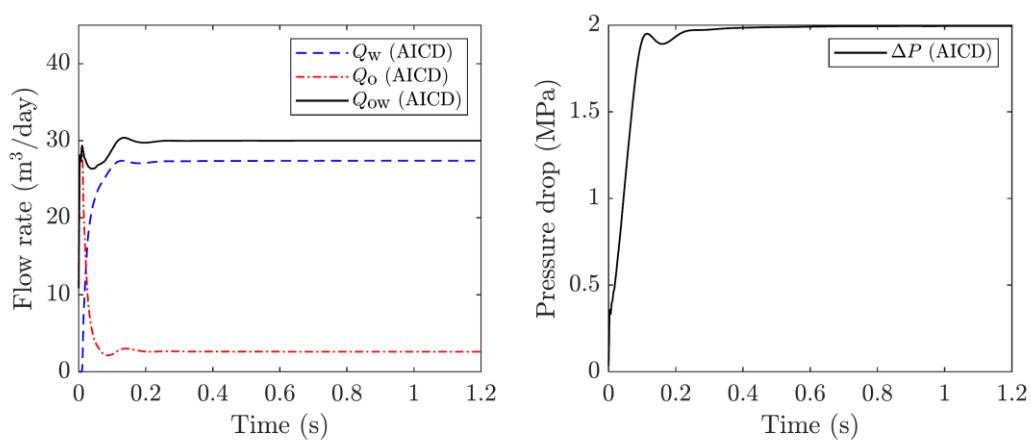
(a) Water cut = 10%



(b) Water cut = 50%



(c) Water cut = 90%



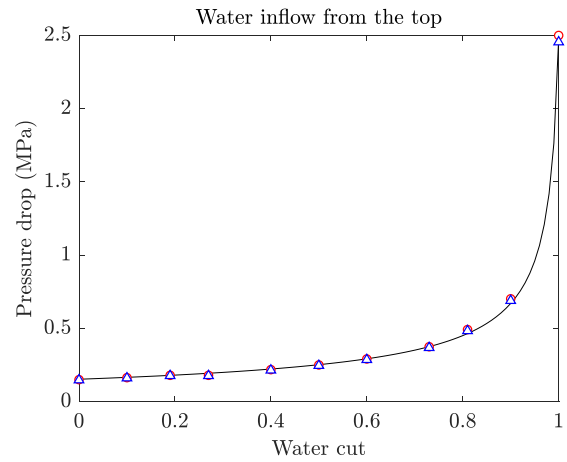
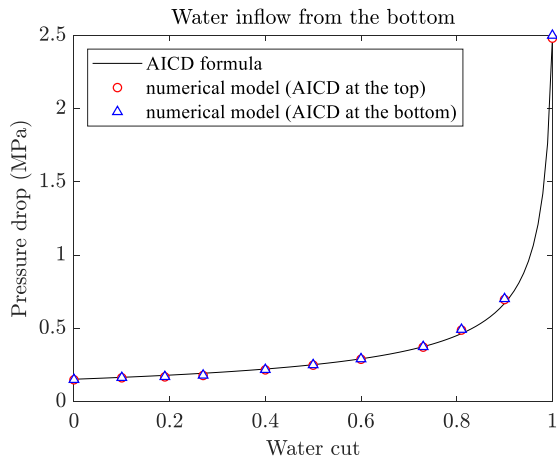
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480 **Fig. 10.** Variation of flow rate (left) and pressure drop (right) at the AICD for different water cut cases with the

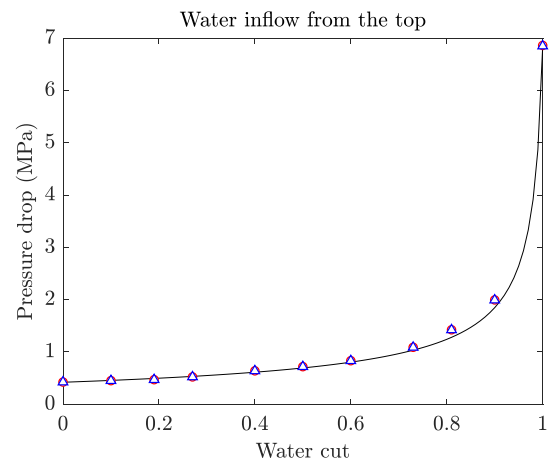
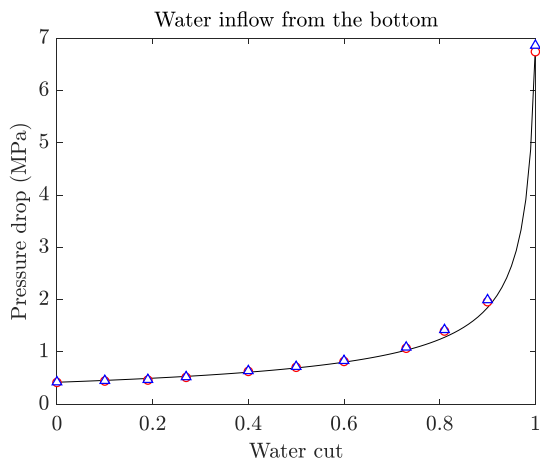
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total flow rate  $Q_{tot} = 30 \text{ m}^3/\text{day}$ .

(a)  $Q_{\text{tot}} = 20 \text{ m}^3/\text{day}$



(b)  $Q_{\text{tot}} = 30 \text{ m}^3/\text{day}$



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483

**Fig. 11.** Pressure drop imposed by the single AICD (either located at the top or the bottom of the annulus) for

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different water cut inflow scenarios with a total flow rate of  $Q_{\text{tot}} =$  (a) 20 or (b) 30  $\text{m}^3/\text{day}$ . The left panel

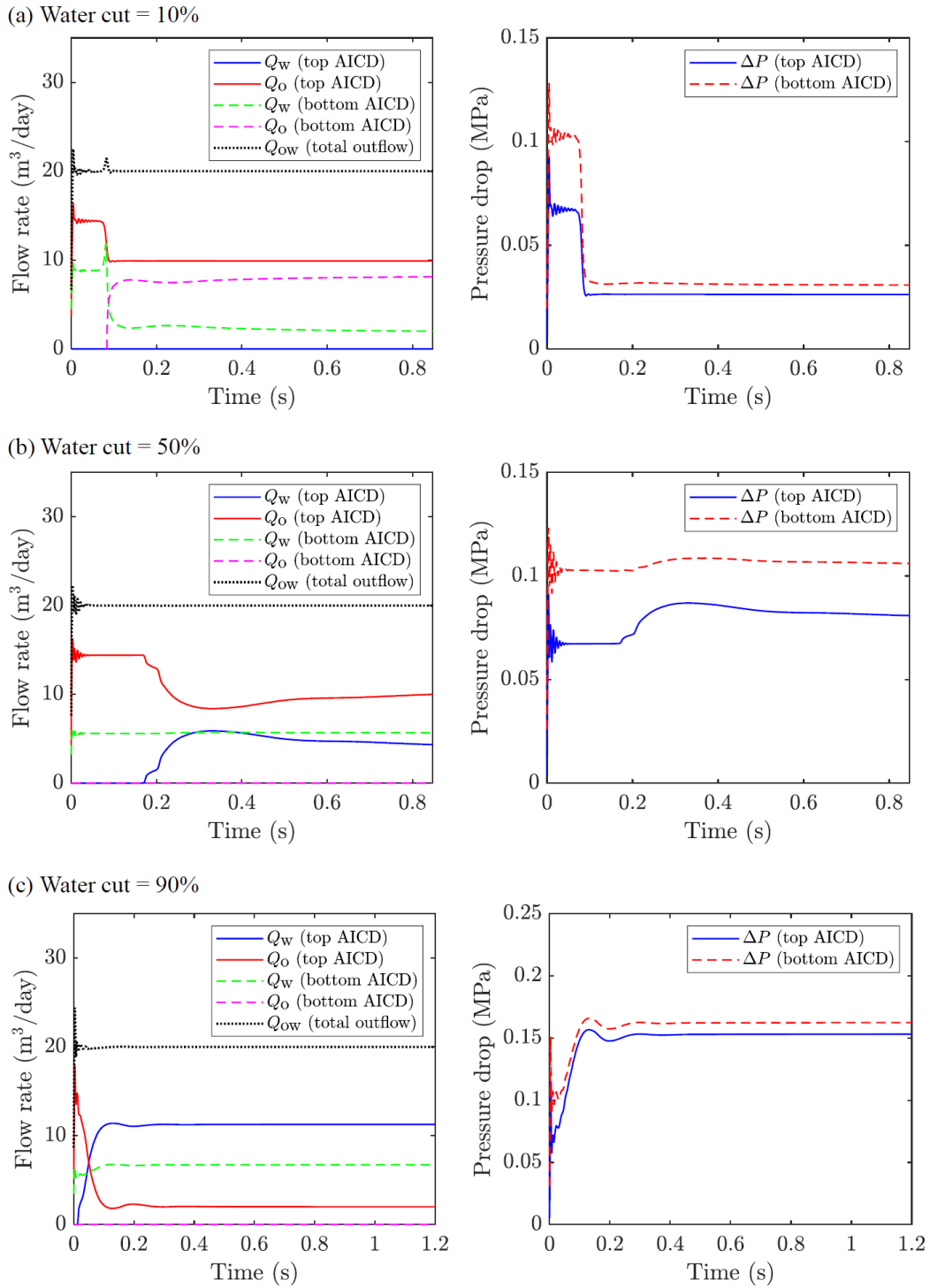
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corresponds to the case that water inflows from the lower region of the annulus, while the right panel

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corresponds to the case that water inflows from the upper region of the annulus.





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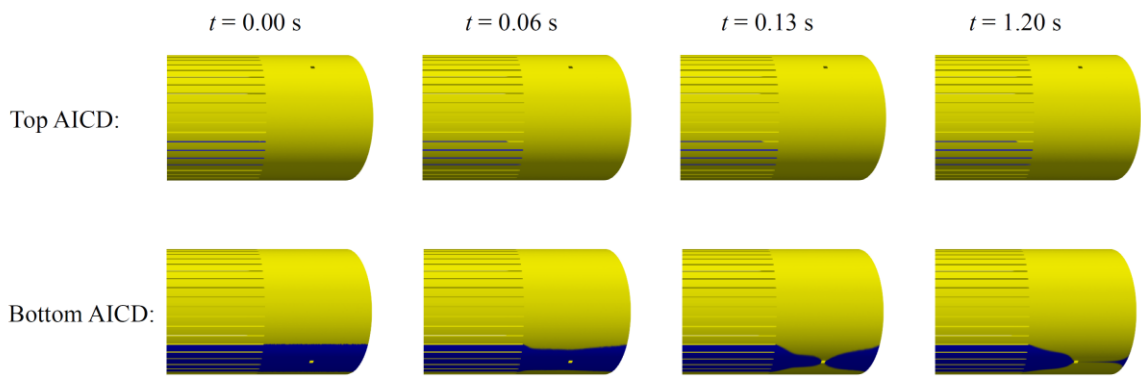
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**Fig. 12.** Variation of flow rate (left) and pressure drop (right) at the two AICDs for different water cut cases

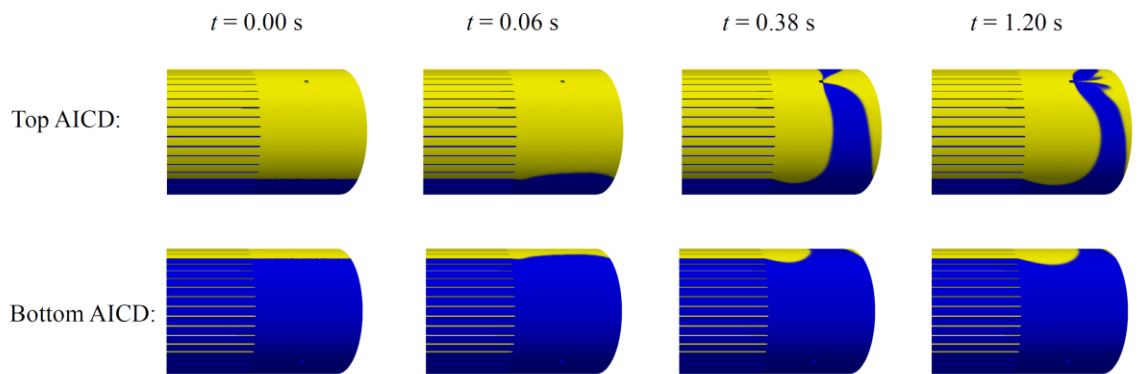
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with the total flow rate  $Q_{\text{tot}} = 20 \text{ m}^3/\text{day}$ .

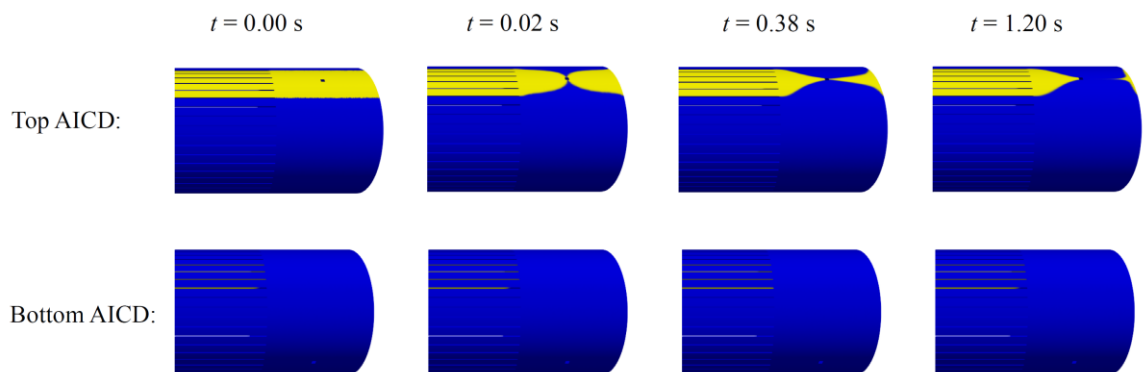
(a) Water cut = 10%



(b) Water cut = 50%



(c) Water cut = 90%

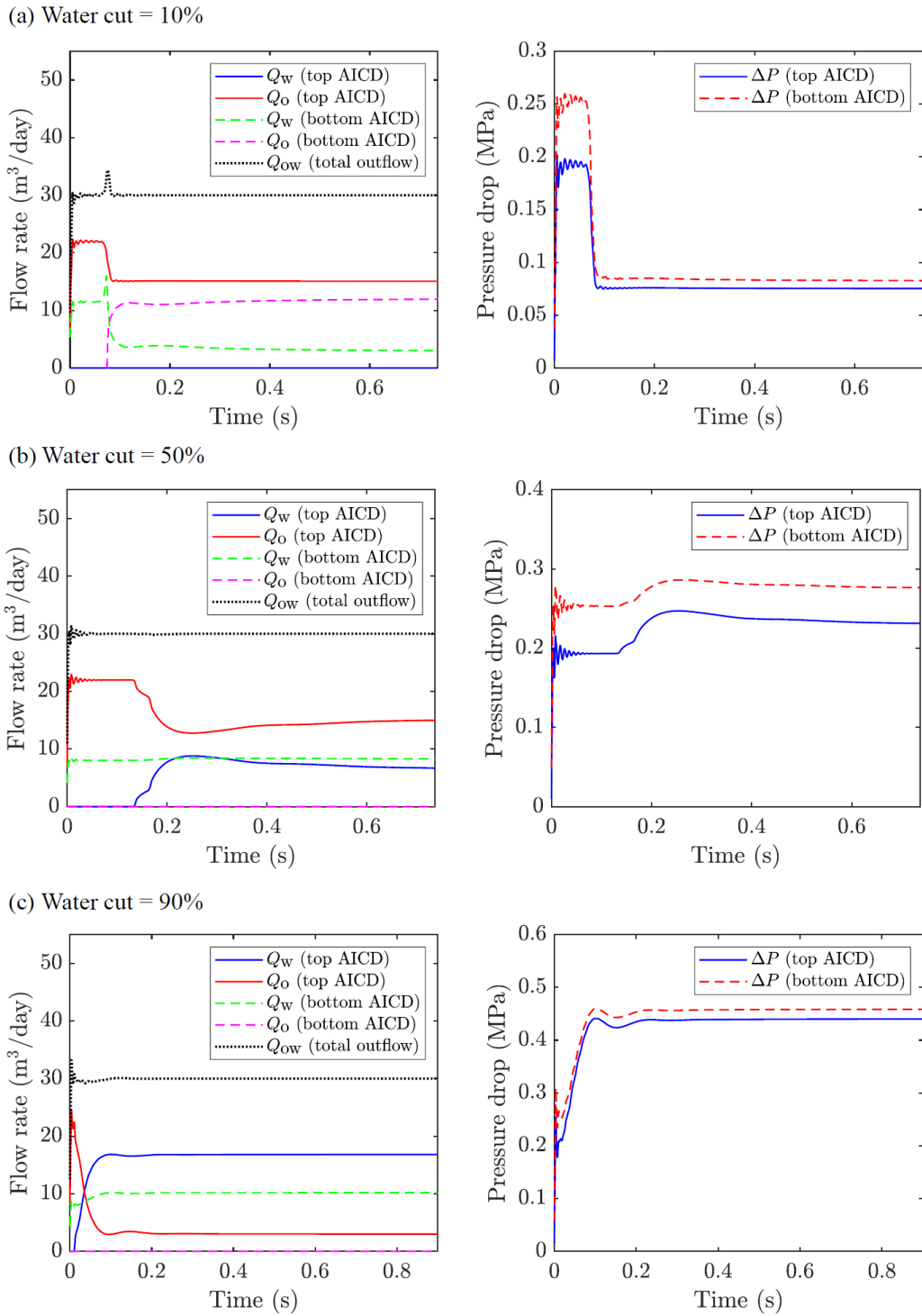


490

491 **Fig. 13.** Variation of flow pattern at the two AICDs for different water cut cases with the total flow rate  $Q_{\text{tot}} = 20$

492

$\text{m}^3/\text{day}$ .



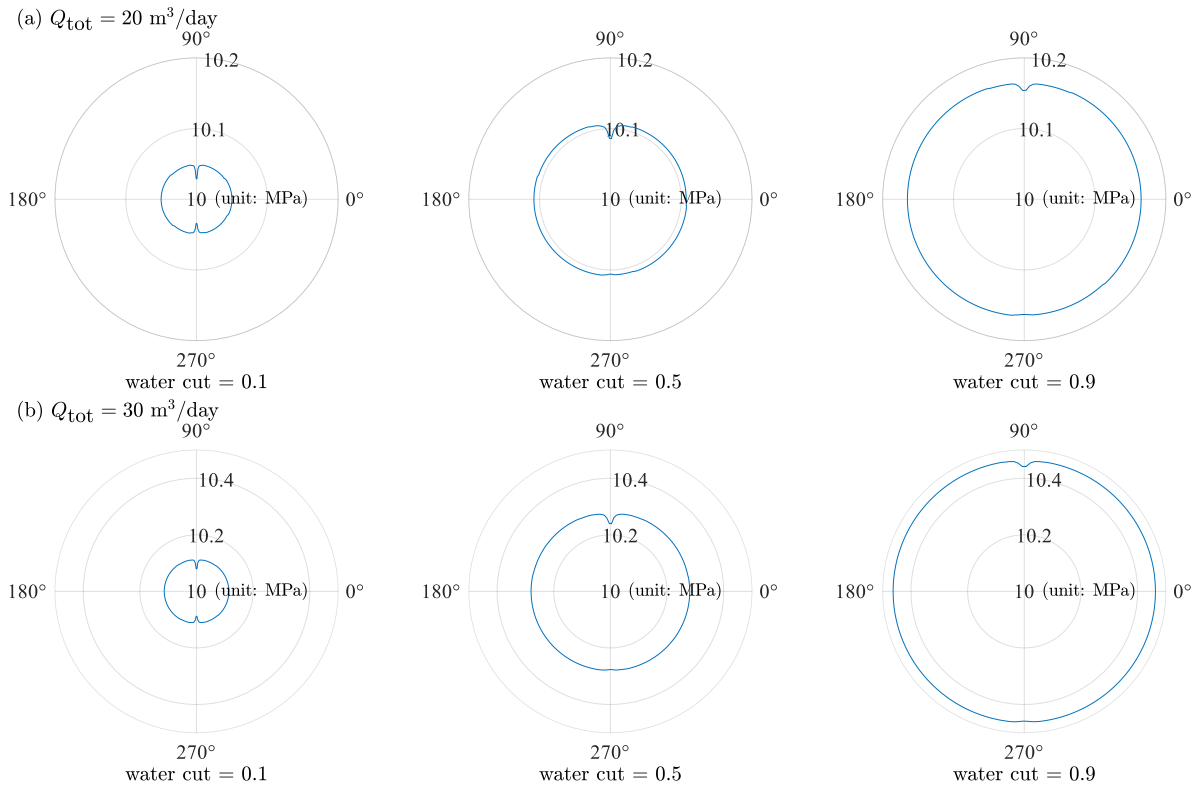
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494

**Fig. 14.** Variation of flow rate (left) and pressure drop (right) at the two AICDs for different water cut cases

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with the total flow rate  $Q_{tot} = 30 \text{ m}^3/\text{day}$ .

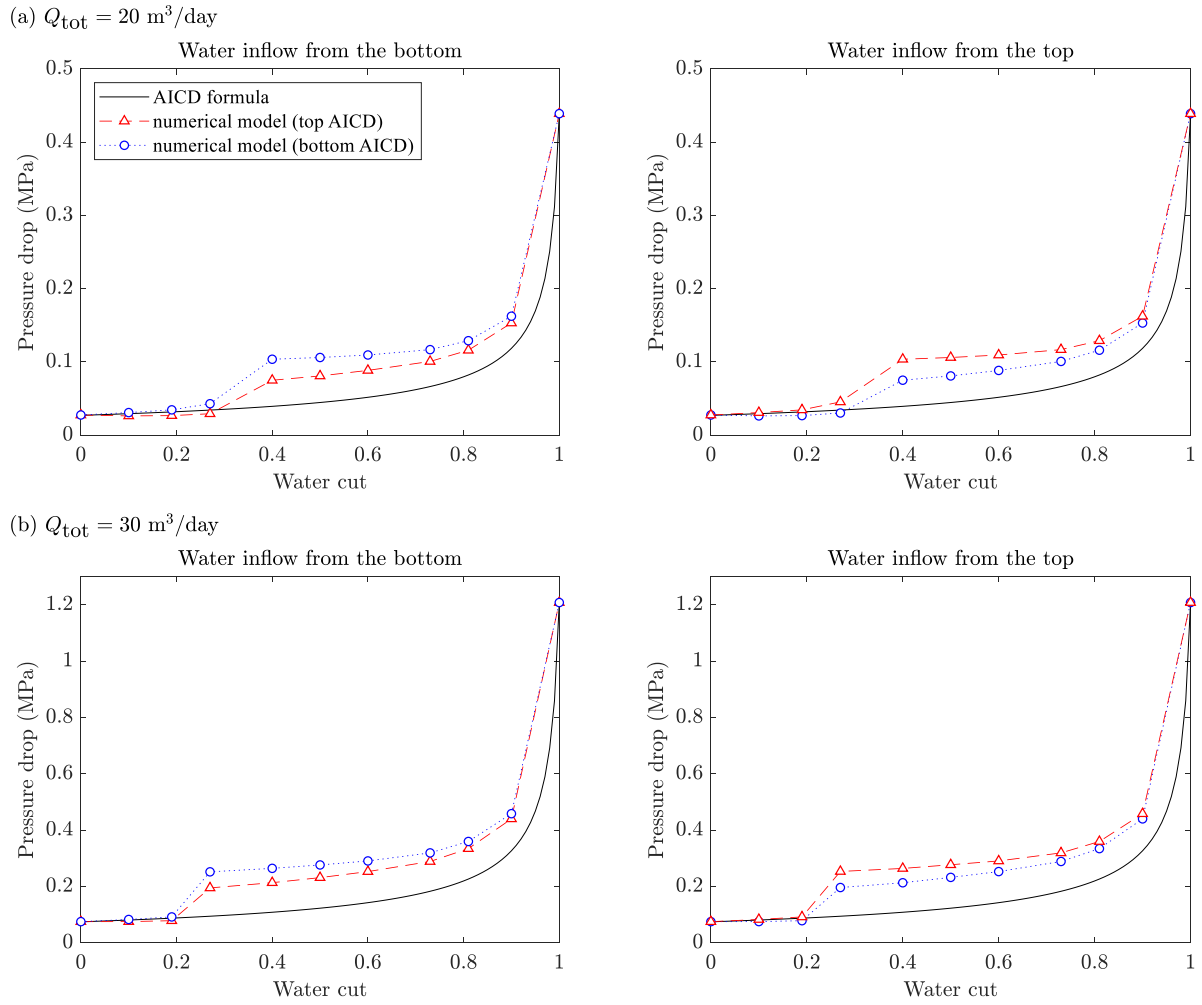


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497 **Fig. 15.** Polar diagrams showing the variation of absolute pressure in the cross-section across the two AICDs.

498 The values at 90° and 270° indicate the absolute pressure in the vicinity of the top and bottom AICDs,

499 respectively. The absolute pressure in the tubing is 10 MPa.



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501

**Fig. 16.** Pressure drop imposed by the two AICDs (one is installed at the top and the other is installed at the

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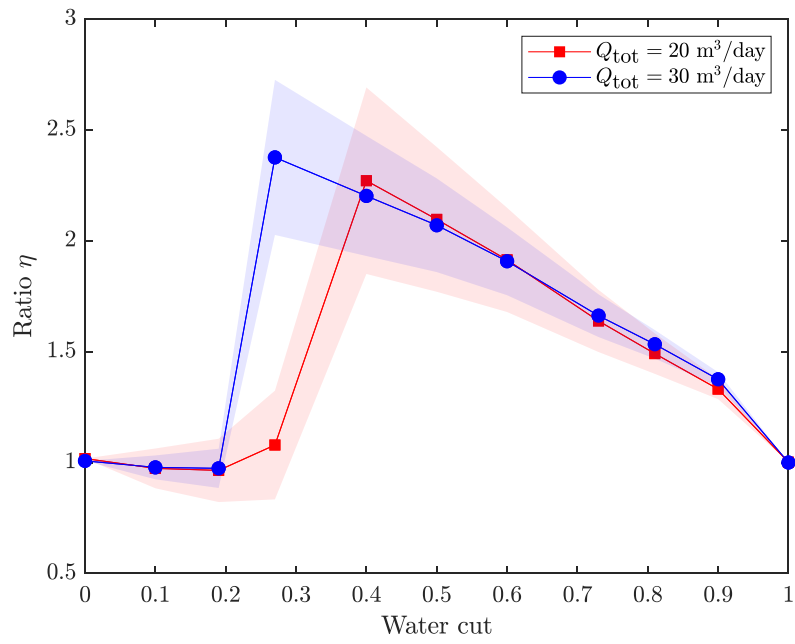
bottom of the annulus) for different water cut inflow scenarios with a total flow rate of  $Q_{\text{tot}} =$  (a) 20 or (b) 30

503

$\text{m}^3/\text{day}$ . The left panel corresponds to the case that water inflows from the lower region of the annulus, while the

504

right panel corresponds to the case that water inflows from the upper region of the annulus.



505

506

**Fig. 17.** Variation of the ratio  $\eta$  of the pressure drop derived from numerical simulation to that predicted from

507

the AICD formula with respect to different water cut inflow conditions; the shaded areas indicate the variation

508

induced by the location of the AICD and the condition that water enters the annulus from the top or bottom.

509 **Table 1.** Parameters of the completion joint.

Parameters	Value	Unit
Total length of the completion joint $L$	12.0	m
Diameter of the outer annulus $D_o$	0.24	m
Length of the inner annulus $L_i$	5.0	m
Mean diameter of the inner annulus $D_i$	0.14	m
Length of the narrow channel $L_c$	4.5	m
Cross-sectional area of the narrow channel $A_c$	$4.8 \times 10^{-5}$	$m^2$
Hydraulic diameter of the narrow channel $d_c$	0.0046	m
Gap thickness of the inner annulus $h_i$	0.0027	m
Length of the closed region of the joint $L_x$	7.0	m
Reference fluid pressure inside the tubing $p_0$	$1.0 \times 10^7$	Pa
Gravitational acceleration $g$	9.8	$m/s^2$

510

511 **Table 2.** Parameters of the fluids (based on the reference pressure  $p_0 = 1.0 \times 10^7$  Pa).

Parameters	Value	Unit
Dynamic viscosity of oil $\mu_o$	0.05	Pa·s
Density of oil $\rho_{o0}$	950.0	kg/m <sup>3</sup>
Compressibility coefficient of oil $c_o$	$7.25 \times 10^{-10}$	1/Pa
Dynamic viscosity of water $\mu_w$	$6.5 \times 10^{-4}$	Pa·s
Density of water $\rho_{w0}$	1040.0	kg/m <sup>3</sup>
Compressibility coefficient of water $c_w$	$3.55 \times 10^{-10}$	1/Pa
Interfacial tension $\sigma$	0.03	N/m
Total inflow rate at a single completion joint $Q_{tot}$	20.0 or 30.0	m <sup>3</sup> /day
Water cut of the inflow $Q_w/Q_{tot}$	between 0.0 and 1.0	-

512



513 **Table 3.** Parameters of the AICD valve.

Parameters	Value	Unit
Strength parameter $a_{\text{AICD}}$	$1.5 \times 10^{-5}$	-
Volume exponent $m$	2.5	-
Viscosity exponent $n$	0.6	-
Calibration density $\rho_{\text{cal}}$	1000	kg/m <sup>3</sup>
Calibration dynamic viscosity $\mu_{\text{cal}}$	$5.0 \times 10^{-4}$	Pa·s
Cross-sectional area $A_{\text{AICD}}$	$1.6 \times 10^{-5}$	m <sup>2</sup>

514