

# 1     **The Performance Evaluation and Design Optimisation of Multiple Fractured** 2                                     **Horizontal Wells in Tight Reservoirs**

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## 4 5     **Abstract**

6     Multiple fractured horizontal wells (MFHWs) are recognised as the most efficient stimulation  
7     technique to improve recovery from unconventional gas assets. Although multistage fracture  
8     treatment has been very successful in stimulating these reservoirs, very little work has been done  
9     on multi-stage design optimisation.

10    In most of the published works, the improved MFHWs design is recommended to be determined  
11    by sensitivity analysis of one variable while keeping all the other variables fixed. Several  
12    researches suggested that this optimisation should be typically performed based on economic  
13    objectives such as Net Present Value (NPV).

14    This paper initially describes the results of an exercise that uses statistical algorithms coupled with  
15    numerical reservoir simulations to evaluate the simultaneous impacts of important pertinent  
16    parameters on the performances of different MFHW designs at various production periods. It is  
17    shown that the impact of the individual parameter, quantified by Spearman's rank correlation  
18    coefficients technique, on different objective functions e.g. total gas production during the  
19    production period, varies depending on the governing flow regimes. For example, it is  
20    demonstrated that the impact of fracture length on the performance of MFHWs decreases over the  
21    production time while the number of fractures exhibits almost a fixed effect. It was also shown  
22    that the general trend of the importance of parameters on productivity index (PI) is similar to those  
23    observed for some of other objective functions including total gas production and NPV.

24    In addition, these results confirm the applicability of available well productivity models developed  
25    for the early, middle and boundary dominated flow conditions to optimise the design of MFHWs  
26    in tight reservoirs. The result of the study confirms provided maximising a desired objective in the  
27    long term (longer than the time to reaching the compound linear flow) is targeted; the pseudo-  
28    steady state productivity indices models are appropriate to be used for the design optimisation of  
29    MFHWs. Otherwise, if a shorter-term objective is targeted, this optimisation could be performed  
30    based on appropriate productivity index models available for the early or middle production

31 periods. These results are also confirmed by performing reservoir simulation-based optimisation  
32 of the MFHWs design using the genetic algorithm approach for various cases.  
33 This work provides a general, fit for purpose set of guidelines, suitable for an improved well design  
34 of MFHWs in tight reservoirs. In addition, a new and easily to use workflow based on the  
35 productivity index equations is developed to optimise MFHWs design in tight gas reservoirs for a  
36 chosen targeted time while considering the practical limits and economics.

37

### 38 **Keywords:**

39 Performance evaluation, productivity index, design optimisation, multiple fractured horizontal  
40 wells, tight reservoirs, statistical analysis.

41

### 42 **1. Introduction**

43 Conventionally the formations with permeability varying between  $1\mu\text{D}$  and  $0.1\text{ mD}$  are classified  
44 as tight reservoirs. In these reservoirs, enlarged drainage area by the horizontal well with multiple  
45 transvers fractures increases the well productivity significantly. Therefore, multiple fractured  
46 horizontal wells (MFHWs) have been considered as the most efficient stimulation technique to  
47 improve recovery from such low permeability reservoirs. Fig 1 shows that the folds of PI increase  
48 due to enlarged drainage area by MFHWs with respect to conventional horizontal wells could be  
49 as large as about 12 in tight reservoirs ( $K_m < 0.1\text{ mD}$ ) provided that each fracture is properly cleaned  
50 up and has infinite conductivity [1, 2].

51 Several parameters such as formation permeability, well completion and fracture properties could  
52 affect the benefits obtained from installing MFHWs. The optimisation of the parameters such as  
53 fracture spacing, number, half-length and conductivity is necessary to ensure determining the  
54 optimum MFHWs design that delivers the maximum added-value possible. Therefore, the  
55 development of a workflow to optimise production in an efficient and practical manner is clearly  
56 desirable.

57 Many researchers used dimensionless fracture conductivity measure [3-5] to design hydraulically  
58 fractured vertical wells usually installed in conventional reservoirs.

59 In the case of unconventional reservoirs, despite the success of MFHW stimulation techniques in  
60 increasing productivity of the reservoirs and efforts directed toward their modelling and  
61 performance prediction, there is no general agreement on how their designs should be optimised

62 particularly in tight formations. The reasons are that any decisions regarding optimum designs of  
63 MFHWs in such low permeability formations should include; 1) the impacts of mutual parameters  
64 such as fracture number, length, spacing etc., 2) the impact of existence of a relatively long  
65 transient flow, 3) the important economic considerations for potentially such as the low total  
66 production capability of the reservoirs.

67 In most of the published works, the MFHW's optimum design is determined by performing  
68 sensitivity analysis on one variable while keeping all other variables fixed [6-10]. Several  
69 researches suggested that this optimisation should be performed based on common economic  
70 objectives such as Net Present Value (NPV) [10-17]. This includes production forecasting by either  
71 numerical reservoir simulations, or analytical/semi-analytical models or proxy models and  
72 fracturing cost estimation.

73 Numerical simulation of all plausible scenarios is time-consuming, especially noting that each case  
74 requires employing a massive local grid refinement for explicit modelling of the fractures.

75 The problem with analytical forecasting models of MFHWs in tight reservoirs is that they do not  
76 capture all of the flow regimes (as will be discussed in Section 2) and/or requires information about  
77 the expected flow regimes during production time [7, 14, 18-20]. For instance, the methodology  
78 proposed by Meyer et al. [14] neither included any equations for capturing the compound linear  
79 flow regime around MFHWs nor considered the impacts of interference between fractures (i.e.  
80 considering complex flow regimes around MFHWs). Several of these equations have been  
81 developed based on various assumptions mainly valid in either conventional or ultra-tight  
82 formation, which are not applicable for tight reservoirs. For instance, Moradi et al. [20, 21]  
83 addressed the deficiencies of the widely-used models and developed a new flow equation to model  
84 the compound linear flow regime, the most important flow regime for characterising the fractured  
85 well and formation. In addition, it should be noted that many of the equations used are borrowed  
86 from well testing (i.e. rate constant solution) which may not necessarily be accurate for the constant  
87 pressure production strategy, which is commonly employed by the industry in these reservoirs.

88 Proxy models have recently been used to correlate the objective functions such as NPV to pertinent  
89 parameters for estimating their values in unconventional reservoirs [15, 16, 22]. Apart from the  
90 issues related to the accuracy of these models in predicting the performance of such complex well  
91 geometries, these approaches still require a certain number of reservoir simulations or information  
92 about the already drilled wells in the field to create the proxy models.

93 The more adopted trend in the industry for optimising MFHWs design is towards installing the  
94 longest possible fractures with more stages/clusters and tighter spacing in unconventional  
95 reservoirs or applying learnings from the previous successful operations in the field. This approach  
96 commonly results in higher initial production rates and a much higher decline rate later, which is  
97 easy to justify if only the short-term production objectives were considered [6, 23]. Closely spaced  
98 fractures also have some other practical disadvantages [24, 25] such as the fractures do not remain  
99 planar and influence propagation of each other [26]. These cause the final fracture configuration  
100 to be suboptimal.

101 Traditionally, for conventional reservoirs, the optimum design of a fractured vertical well is chosen  
102 based on the PI index at pseudo-steady (steady) state (PSS) flow conditions because of the very  
103 short transient flow regime. In the case of unconventional reservoirs, some researchers also  
104 proposed that an optimum design at PSS condition is the optimum design for the transient flow  
105 period too. Nevertheless, there is no proof to confirm whether this approach can be applicable in  
106 tight reservoirs with MFHWs, where transient flow period lasts much longer (months or years).

107 Here, a new approach, shown in Fig 2, is followed by applying statistical algorithms to evaluate  
108 various MFHWs design strategies while considering various objective functions at different times  
109 during a production period. Based on the results of the cases investigated, it is shown that, for  
110 example, the PSS based PI model could be used to optimise the overall performance of MFHWs  
111 provided long-term objectives are considered. In other words, the design that optimised the well  
112 performance at PSS conditions provided the best performance for the well lifetime. However, it  
113 should be noted that this design would not be the best design for any individual transient flow  
114 conditions.

115 Accordingly, a new workflow has been proposed to optimise MFHWs completion design in tight  
116 reservoirs. The proposed workflow replaces the commonly used economic objective functions (e.g.  
117 NPV), which are cumbersome to be calculated for individual MFHW design, by a new objective  
118 function (e.g. PI at PSS condition) that can be calculated and optimised easily. This eliminates or  
119 drastically reduces the requirement of production forecasting by reservoir simulation. In other  
120 words, this workflow can be simply implemented by well engineers in their optimum design  
121 practices, which leads to enhancing well performance while considering economic and/or the  
122 practical constraints. Below the tools, used to achieve the objectives, are briefly described first  
123 before presenting the details of this workflow.

124 **2. Numerical Simulation**

125 The performance of MFHWs in tight reservoirs can be explained by series of very complex flow  
126 regimes developed during the production time as shown in Fig 3. Assuming a perfect clean-up is  
127 performed [2], after passing the fracture linear flow regime, at the early times, linear flow from  
128 formation to each fracture corresponding to formation linear flow develops. If constant finite  
129 conductivity within the fracture is assumed, this flow regime could be represented in the form of  
130 bi-linear flow regime. The subsequent flow regime is early formation radial flow regime. It is most  
131 likely that the expected early formation radial flow regime will not follow due to the fracture  
132 interference effect. The fracture interference effect leads to a compound linear flow regime. At this  
133 stage, the pressure gradually shifts its orientation such that the bulk flow is linear toward the set of  
134 fractures. Eventually, pseudo elliptical flow regime may be observed. Finally, as pressure profiles  
135 reach the boundaries, pseudo-steady state or boundary dominated flow regime develops to  
136 represent the flow from further reservoir. The duration of these flow regimes would be different  
137 based on the fracture spacing, half-length and the diffusivity of the tight formation.

138 It should be noted that there are long transition periods between the mentioned flow regimes that  
139 produce the significant bulk of the total production. In addition, considering the practical fracture  
140 spacing, half-length and the diffusivity of the tight formation, some of the flow regimes before the  
141 PSS conditions may not be observed for all cases.

142 As already mentioned, the available analytical, semi-analytical models have not adequately  
143 addressed development of such complex flow regimes as they require information when each of  
144 these flow regimes develops over any production period. In other words, the starting and finishing  
145 times of each flow regimes and appropriate expressions describing the production during the long  
146 transition periods between the flow regimes are not well defined.

147 In this study, the numerical simulation approach was used to investigate the flow behaviour around  
148 the MFHWs. In these simulations, the pertinent parameters [fracture permeability ( $K_f$ ), fracture  
149 width ( $W_f$ ), fracture half-length ( $X_f$ ), number of fractures ( $N_f$ ) and fracture spacing ( $S_f$ )] were varied  
150 over wide practical ranges based on the Latin Hypercube sampling (LHS) method. In this exercise,  
151 a programming code, which automatically creates the required include files and stores relevant  
152 output data for each simulation, was coupled with a 3D reservoir model, developed by a  
153 commercially available reservoir simulator, to generate the required data bank.

154

## 155 2.1 Base Case Model Description

156 In this study, a 3D Cartesian grid model has been set-up in a black oil simulator which applies  
157 finite difference method to simulate a tight gas reservoir. As it is shown in Fig 4, the model has  
158 151\*151\*10 grid cells with a dimension of 40\*40\*10 ft in the X, Y and Z directions, respectively.

159 The gridding was selected based on a sensitivity analysis on the global grid size to avoid numerical  
160 dispersion while keeping the run time reasonable. Due to a much more complex flow behaviour  
161 around a MFHW compared to that around a conventional well, the local grid refinement (LGR),  
162 which explicitly defines hydraulic fractures in the simulation, is required to properly capture the  
163 variation of flow parameters as fluid travels from the matrix to the fractures and then to the  
164 wellbore. Another sensitivity analysis on the grid refinement was carried out to determine the  
165 optimum number of grids around each fracture. The optimum LGR around each fracture used in  
166 this study divided each parent grid into 9 subgrids in X, 4 sub-grids in Y and 1 grid in Z directions.  
167 The hypothetical tight gas reservoir produces from a horizontal well, which is placed in the centre  
168 of the model. The dry gas flows within a reservoir with an initial reservoir pressure of 7,500 psi,  
169 the average effective reservoir permeability ( $K_m$ ) and porosity of 0.15. Table 1 and Table 2 provide  
170 more information on the model's properties and investigated parameters. To establish the  
171 scenarios, the following additional assumptions have been made, unless otherwise stated:

- 172 1) The reservoir formation is homogeneous.
- 173 2) The fluid is single-phase and slightly compressible.
- 174 3) Darcy Law governs the flow of fluid towards fractures and within the matrix.
- 175 4) Pressure loss along the horizontal section of the wells is assumed negligible.
- 176 5) The fractures are identical in term of physical properties such as conductivity and have been  
177 positioned vertically with constant spacing along the well and penetrating the whole  
178 reservoir thickness.
- 179 6) Considering MFHWs with cased/perforated completion has been used in this study, the flow  
180 to the wellbore is only through hydraulic fractures.
- 181 7) No geomechanics model is included in this study as it is expected that the impact not to be  
182 significant for the considered range of permeability. In other words, the formation and  
183 fracture properties do not change throughout a simulation.

184 It should be noted that the well length is not limited to a specific value to investigate the  
185 performance of installing a different number of fractures at various spacing.

### 186 **3. Statistical Analysis of Effective Parameters**

#### 187 **3.1 Latin Hypercube Sampling**

188 Sampling (Experimental design) methods are widely used to efficiently sample among all the  
189 possibilities to identify the impact of important parameters. Latin Hypercube sampling is a  
190 statistical method for creating a sample of feasible collections of parameter values [27, 28], from  
191 a multi-dimensional distribution randomly, but systematically. In the context of statistical  
192 sampling, a square grid containing sample positions is a Latin square if (and only if) there is only  
193 one sample in each row and each column, as shown in Fig 5 (Right). A Latin Hypercube is the  
194 generalisation of this concept to an arbitrary number of dimensions, whereby each sample is the  
195 only one in each axis-aligned hyperplane containing it. This method ensures that the whole  
196 parameter range, considering its corresponding distribution, is represented in the sampling as it  
197 uses stratified sampling without a replacement technique. More information about this technique  
198 can be found in the work by McKay, Beckman and Conover [27].

199 Table 2 shows that distributions of the variables have been assumed uniform.  $N_f$ ,  $S_f$  and  $X_f$  have  
200 been varied within the ranges of (1-15), (80-650 ft) and (100-1020 ft) while  $K_f$  and  $W_f$  have been  
201 changed from 2 to 8 mm and from 10 to 200 D, respectively. In this study, 1000 simulations with  
202 various MFHWs designs were generated by applying the LHS method to investigate the impact of  
203 the pertinent parameters fully. A pre-processor, i.e. a programming code, was developed to  
204 generate includes file, required for modelling different cases. Another programming code was also  
205 developed as a post processor to extract the required data and calculate appropriate outputs that  
206 cannot be provided by the reservoir simulators, for instance, calculation of cost and NPV described  
207 later in section 4.

208

#### 209 **3.2 Spearman's Rank Correlation Coefficient**

210 The spearman's rank correlation coefficient ( $\rho$ ) is a quantitative measure to assess how well the  
211 dependence of two variables can be described with an either linear or non-linear monotonic  
212 relationship. In other words, if non-linear but monotonic relationships between the output and input  
213 variables are expected, the Spearman's rank is the most suitable technique to analysis such a  
214 dependency. It ranks the variables based on their values (e.g. from low to high) and measures the  
215 statistical dependency between two ranked variables as follows:

$$\rho = \frac{\sum_{i=1}^n (X_i - \bar{X}) \cdot (Y_i - \bar{Y})}{\sqrt{\sum_{i=1}^n (X_i - \bar{X})^2 \cdot \sum_{i=1}^n (Y_i - \bar{Y})^2}} \quad \text{Equation 1}$$

216 where X is the ranked input variable and Y is the ranked output. If Y tends to increase or decrease  
 217 when X increases, the coefficients are positive or negative, respectively, and higher value means  
 218 a stronger correlation, (Fig 6). The Spearman's rank technique provides values between -1 and +1  
 219 where +1 is the perfect positive correlation and -1 is the perfect negative correlation. In addition,  
 220 zero value shows that either increasing or decreasing X does not change Y. Fig 7 shows the  
 221 corresponding field total gas production (FGPT) after 20 years of production for different fracture  
 222 spacing (Sf) while other parameters change simultaneously by LHS. It is to note that for all these  
 223 simulation the rho value was calculated as 0.485 (the last bar in Fig 9).

224  
225

#### 226 4. Results and Discussion

227 In this study, the variation of five relevant parameters ( $N_f$ ,  $S_f$ ,  $X_f$ ,  $K_f$  and  $W_f$ ) in reservoirs with  
 228 various permeability values were examined. For each case, 1000 simulations with different  
 229 MFHWs designs were generated by LHS to investigate the impact of these parameters fully. It  
 230 should be noted this number of simulations was the optimum number based on a separate  
 231 sensitivity analysis performed to make sure a full investigation of the search space. Also, the well  
 232 length is not limited to a specific value to investigate the performance of installing a different  
 233 number of fractures at various spacing.

234 Fig 8 shows the Spearman correlation coefficients between the five pertinent parameters and total  
 235 gas production of the field (FGPT) values for the case with  $K_m=0.01$  mD at different times during  
 236 the 20-year production period where the minimum bottom hole pressure was limited to 4000 psi.  
 237 The results illustrate that  $N_f$  is the most important parameter affecting FGPT during the entire well  
 238 lifetime with almost a constant impact (rho value). As production continues, the rho value of  $N_f$   
 239 reduces from 0.76 to 0.71, when the fracture interference begins (mostly after a week for these  
 240 cases). However, the value then increases to 0.73, when the compound flow condition is fully  
 241 developed and becomes constant (at 0.74), when the boundary dominated flow regime is developed  
 242 at the late production time. The results also show that the  $X_f$  effect reduces with time from 0.57 to  
 243 0.31, while the impact of fracture spacing is increasing from zero at the early production time of 1



244 day up to 0.46 at the late production time of 20 years. The graph also shows that the impacts of  
245 fracture permeability and width are small.

246 Fig 9 shows the Spearman correlation coefficients between the five pertinent parameters and PI  
247 values for the case with  $K_m=0.01$  mD at different times during the 20-year production period. As  
248 Fig 9 shows, the general trend of the importance of parameters (rho coefficients) on PI is similar  
249 to those observed in the previous case for FGPT in Fig 8. That is, this Figure shows that the  $X_f$   
250 effect decreases from 0.54 to 0.28, almost half of its initial value, over the entire 20-year production  
251 period while the impact of fracture spacing has increased from zero at the early time of 1 day of  
252 production to over 0.43 after approximately 1 year of the production and has reached to 0.47 during  
253 the boundary dominated flow period.

254 Fig 10 and Fig 11 show examples of delivered PI and field total gas production (FGPT) profiles  
255 over the 20-year of the well lifetime for four MFHW designs with  $N_f=10$ ,  $W_f=0.025$  ft and  $K_f=200$   
256 D in the reservoir with  $K_m=0.01$  mD. Fig 10 shows that the PI is a monotonic function and the  
257 values reduce from initial high values during the transition period of the system and stabilise at  
258 constant values during the boundary dominated flow regime at the late time of the production  
259 period (after 5 years in these cases). Fig 11 illustrates the monotonically increasing profile of the  
260 FGPT function and shows that the long-term performance of two designs with 10 properly spaced  
261 fractures ( $S_f=600$ ft) are much better than those closely spaced even with much higher half-length  
262 for the cases considered.

263 In general, the Figures confirms the difference between short-term and long-term performances of  
264 the wells. The results show that the long-term performances (their rankings) of all the considered  
265 cases became unique after fracture interferences time, which is around 100 days in these cases. To  
266 best knowledge of the authors, there is no equation that calculates this time. However, the start  
267 time of compound linear flow regime that follows can be approximated by the following Equation:

$$t = 237 \frac{\phi \mu C_t S_f^2}{K_m} \quad \text{Equation 2}$$

268 where  $\phi$ ,  $\mu$ ,  $C_t$  and  $t$  are the porosity, viscosity, total compressibility and the start time of fracture  
269 interference respectively.

270 It should be noted that the start time of the fracture interference is always earlier than the start time  
271 of compound linear, and during the lengthy transition period in between the linear and compound  
272 flow regimes in such low permeability reservoirs.

273 In other words, for instance, the case with ( $X_f=100$  ft and  $S_f=600$  ft) is the design with better  
 274 performance at PSS conditions, started performing better after the end of compound linear flow  
 275 than the design ( $X_f=1020$  ft and  $S_f=80$  ft) which had performed better at the earlier time of  
 276 production.

277 In addition to technical, economic considerations were included and the above graphs were  
 278 regenerated based on Discounted Cumulative Gas Production (DCGP), Net Present Revenue  
 279 (NPR) and NPV calculated by Equation 3, Equation 4 and Equation 5, respectively.

$$DCGP = \sum_{j=1}^n \frac{(Q_g)}{(1+i)^j} \quad \text{Equation 3}$$

$$NPR = \sum_{j=1}^n \frac{(Q_g)R_g}{(1+i)^j} \quad \text{Equation 4}$$

$$NPV = NPR - \left( \sum_{k=1}^M (C_{well} + C_{frac}) \right) \quad \text{Equation 5}$$

280 where  $i$ ,  $n$ ,  $R_g$  and  $Q_g$  are the interest rate, number of years of production, the estimated gas price  
 281 and gas production (Mscf). NPR is the revenue from the fractured well and  $M$  is the number of  
 282 wells, which is one in this study.  $C_{well}$  and  $C_{frac}$  are the cost of drilling a horizontal well and the  
 283 fracturing operation respectively and obtained based on the example cost listed in Table 3.

284 Fig 12 and Fig 13 show the rho values when DCGP and NPR with typical interest ratio of 0.1 and  
 285 \$3 per Mscf gas were used for 20 years of the production. In both cases, almost similar trends (i.e.  
 286 rho coefficients) to those obtained in previous cases are observed. The same trends were observed  
 287 when interest ratios of 0.2 and 0.3 were also applied.

288 Fig 14 shows the rho values between the five pertinent parameters and NPV values at different  
 289 times during the 20-year production period in the reservoir with  $K_m=0.01$  mD. It is noted that the  
 290 rho values at the early time of production (less than 1-year production) are influenced by the cost  
 291 of the operation, but the later trends are like those observed for the previous indicators already  
 292 discussed. For example, the rho value of 0.70 and higher for  $N_f$  during most of the production time  
 293 (after 1 year of production) indicates that the number of fractures is the most important parameter  
 294 for maximising NPV.

295 It should be noted that here there was no limit on the production in this study, whereas, in reality,  
 296 the rate of production in the early times of production is often limited by surface facility

297 capabilities. This would suggest that the impacts of placing longer fractures at the early days of  
298 the production would be even less when such constraints are applied.

299 This exercise was repeated for other cases under different conditions at the range of considered  
300 parameters in Table 1, for instance, the reservoir with lowest formation permeability ( $K_m=0.001$   
301 mD) in tight formation category.

302 Fig 15 shows the rho values between the pertinent parameters and FGPT values at different  
303 production times during 50 years well lifetime when formation permeability is 0.001 mD. The  
304 results again show that  $N_f$  is the most important parameter affecting FGPT regardless of the various  
305 flow regimes occurring throughout a well lifetime. Similar to the case of  $K_m=0.01$  mD, the impact  
306 of  $X_f$  (and  $S_f$ ) reduces (increases) with time, albeit to a different extent. That is, the effect of  $X_f$   
307 decreases from 0.61 at the early time of 1 week of production to 0.38 at the late time of 20 years  
308 of production while the impact of  $S_f$  increases from zero at the early days up to 0.44 at the late time  
309 of production. Compared with the results of the case with  $K_m=0.01$  mD, the impact of increasing  
310 fracture half-length has increased by about 20%, on average, for the entire well lifetime of the  
311 reservoir with  $K_m=0.001$  mD. Also, the time that  $S_f$  becomes more important than  $X_f$  is about 5  
312 years for  $K_m=0.001$  mD, while it is 1 year for  $K_m=0.01$  mD due to a longer period of the formation  
313 linear flow regime.

314 It should be noted that if the permeability of the formation decreases, the boundary-dominated  
315 flow will develop later assuming same drainage area for the well. However, in practice, as the  
316 common development strategy in lower permeability reservoirs is to increase the number of wells;  
317 i.e. decreasing drainage area of a well, this results in a reduction of the transient flow regime time.

318 Fig 16 shows the performances of two MFHWs completion designs with the same number of  
319 infinite conductivity fractures ( $N_f=15$ ), but different configuration, stimulated over a fixed contact  
320 area of 52.5 acres in a reservoir with  $K_m=0.001$  mD. For the first case, 15 fractures were placed  
321 with  $X_f=1020$  ft and  $S_f=80$  ft (the largest  $X_f$  and the lowest  $S_f$  used in this study). For the second  
322 case, the 15 fractures with fracture half-length of  $X_f=260$  ft (a quarter of the previous case) were  
323 placed four times further ( $S_f=320$  ft) compared to the previous case. The Figure shows that  
324 although the early production is accelerated by installing longer fractures, the case with bigger  $S_f$   
325 and much shorter fractures delivers 30% more total gas production over 20 years of production.

326 Two other MFHWs designs (case 1:  $N_f=10$ ,  $X_f=1960$  and  $S_f=320$  and case 2:  $N_f=25$ ,  $X_f=760$  and  
327  $S_f=120$ ), induced with a constant volume of proppant and well length, were also considered for the

328 same reservoir and  $K_m=0.001$  mD with results shown in Fig 17. The Figure indicates that the case  
329 with more  $N_f$ , even with much shorter fractures, produce 45% more total gas production than the  
330 case with larger  $X_f$  and more spaced fractures. All these results contradict the more common  
331 industry practice of placing longer fracture length, which is based on short-term production period  
332 objectives.

333

## 334 **5. Optimisation of Design of MFHWs in Tight Reservoirs**

### 335 **5.1 Simulation Based Optimisation of MFHWs Design**

336 In addition to the above analyses, Level-set optimiser that is a version of Genetic Algorithm (GA)  
337 was applied to determine the optimum MFHW design. The optimisation of MFHWs design was  
338 performed to maximise the NPV value of the well after 20 years of production in the reservoir with  
339  $K_m=0.01$  mD. As shown in Fig 18, a sufficient number of iterations (340 runs) were attempted by  
340 the optimiser to allow the algorithm to determine the optimum design. Fig 19 shows the PI values,  
341 corresponding to the PSS conditions, of the attempted runs by the optimiser. It shows the same  
342 trend as that illustrated for NPV in Fig 18. In other words, where the PI value increases, its  
343 corresponding NPV value is increased too and vice versa. The optimum MFHW design with  
344  $N_f=15$ ,  $X_f=1020$  ft and  $S_f=600$  ft deliveries NPV of 14.8 Million\$ and PI of 1.457 (Mscf/D.psi).

345 In summary, similar trends as those of the Spearman correlation coefficients for the objective  
346 functions (PI, FGPT, DCGP, NPR and NPV) are observed. This similarity and the monotonic  
347 relationships between the input and output parameters of MFHWs in tight reservoirs confirm that  
348 if a MFHW design maximises PI of the boundary dominated flow regime, it maximises the  
349 objective functions over a long enough production time in a tight reservoir for the range of  
350 conditions considered. However, this approach may not deliver the optimum design if very short-  
351 term objectives (before the start of compound linear flow) are considered. For such scenarios, an  
352 appropriate PI model for a transient flow period should be used to optimise the MFHW design for  
353 maximising a chosen objective function at the targeted time.

354 The results of these analyses confirm that calculating cumbersome economic objectives such as  
355 NPV is not necessary and using PI models is appropriate to optimise the MFHWs design in tight  
356 reservoirs. The selection of PI model depends on the targeted time to maximise any common  
357 objective functions.

358

359

## 360 **5.2 PI-Based Optimisation Workflow**

361 As already mentioned, it is statistically proven that PI at PSS conditions could be used to optimise  
362 the performance of MFHWs for the whole production period even though transient flow regimes  
363 may last for a considerable, long period provided the targeted time for maximising the desired  
364 objective is long enough (i.e. after fracture interference).

365 Applying the learning of the previous analyses, a workflow is developed to optimise PI values.  
366 Although there are several equations to calculate PI of MFHWs at PSS conditions in tight  
367 reservoirs, they have drawbacks. In this study, as maximising long-term objectives was considered,  
368 the empirical PI equation proposed by authors [29] which can predict PI of MFHWs under pseudo-  
369 steady state conditions in tight reservoirs, was used. This workflow uses GA as optimisation  
370 algorithm to optimise the variables ( $N_f$ ,  $S_f$ ,  $X_f$ ,  $K_f$  and  $W_f$ ) related to the design of MFHWs while  
371 maximising PI. The workflow considers constraints such as maximum proppant volume and/or  
372 budget etc. to deliver a practical, optimum MFHW design.

373 An optimisation study for a case with assumed maximum proppant volume of 15000 ft<sup>3</sup> and budget  
374 of 2.5 MM\$ was performed while maximum length of the well was constrained to 4500 ft in the  
375 reservoir with  $K_m=0.1$  mD. The well and fracking cost were calculated based on the data in Table  
376 3. The spacing and half-length were limited to maximum 1000 ft and 2000 ft and minimum 10 ft  
377 and 40 ft respectively in this case. The other parameters were restricted to the range defined in  
378 Table 2. The costs were calculated based on the prices listed in Table 3.

379 The optimum design was found to be the MFHW with  $N_f=8$ ,  $X_f=1172$  ft,  $S_f=583$  ft,  $W_f=0.008$  ft  
380 and  $K_f=200$  D. The maximum delivered PI was 11.233 MScf/Day.psi in this case.

381

382

## 383 **6. Summary and Conclusions**

384 **In this study, results of numerous numerical simulations have been combined with statistical**  
385 **approaches to provide a better understanding of the performance of MFHWs. It specifically**  
386 **examines the applicability of PI to optimise the design of MFHWs in tight reservoirs under the**  
387 **considered prevailing conditions. Accordingly, a practically attractive workflow for determining**  
388 **optimum MFHWs design in tight reservoirs is proposed.** The followings key findings can also  
389 be pointed out:

- 390 1. There were similarities in the trends of the Spearman correlation coefficients for various  
 391 cases and objective functions (PI, FGPT, DCGP, NPR and NPV) **considered here. That**  
 392 **is:**
- 393 a. the number of fractures was the most important parameter influencing these  
 394 objective functions over the entire well lifetime with an almost constant impact.
  - 395 b. the fracture spacing had bigger impact on the late time of production while the  
 396 half-length impact was more effective at the early time of production. The  
 397 impacts of  $K_f$  and  $W_f$  were small throughout the production period.
- 398 2. These similarities, as well as the monotonic relationships between the inputs and outputs  
 399 parameters for **the studied cases**, suggested that if a MFHW design maximises PI at PSS  
 400 conditions, it would maximise any objective functions in the tight reservoirs provided  
 401 the targeted time for maximising the desired objective is long enough (i.e. after the start  
 402 of compound linear flow).
- 403 3. The optimum design determined based on the PI at PSS condition may not achieve the  
 404 best possible performance at the transient flow conditions, but it would exhibit the best  
 405 overall performance over the whole well lifetime.
- 406 4. The results of this study eliminate necessities of performing the lifetime performance  
 407 prediction of the MFHWs by either numerical simulation or analytical modelling for  
 408 determining the optimum MFHWs design in tight reservoirs.
- 409 5. A new workflow that uses PI equations was developed to optimise MFHW designs while  
 410 considering the practical limits and economics.

411  
 412

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419  
 420

## 421 Nomenclature:

h	Formation thickness	PI	Productivity index
HWS	Horizontal wells	$P_{wf}$	Flowing Bottom-hole pressure

$K_m$	Matrix permeability	$Q_g$	Gas production rate
$K_f$	Fracture permeability	$S_f$	Fracture spacing
LGR	Local grid refinement	$W_f$	Fracture width
LHS	Latin Hyperbolic sampling	$X_e$	Drainage half-length in X direction
$K_m$	Matrix permeability	$Y_e$	Drainage half-length in Y direction
MFHWs	Multiple fractured horizontal wells	$\mu$	Viscosity of the fluid

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## REFERENCES

- [1] M.J. H.R. Nasriani, E. Alajmi and P. Ghahri A Study of Hydraulic Fracturing Clean-up Efficiency in Unconventional Gas Reservoirs Using Statistical Approaches, in: ECMOR XIV - 14th European Conference on the Mathematics of Oil Recovery EAGE, Sicily, Italy, 2014.
- [2] M. Jamiolahmady, E. Alajmi, H.R. Nasriani, P. Ghahri, K. Pichestapong, A Thorough Investigation of Clean-up Efficiency of Hydraulic Fractured Wells Using Statistical Approaches, in, Society of Petroleum Engineers, 2014.
- [3] H. Cinco-Ley, F. Samaniego-V, Transient Pressure Analysis for Fractured Wells, (1981).
- [4] M. Prats, Effect of Vertical Fractures on Reservoir Behavior-Incompressible Fluid Case, (1961).
- [5] M.J.a.E.A. H.R. Nasriani, An Integrated Study of Cleanup Efficiency of Short Hydraulic Fractured Vertical Wells Using Response Surface Methodology, in: 76th EAGE Conference and Exhibition EAGE, Amsterdam, 2014.
- [6] L.K. Britt, M.B. Smith, Horizontal Well Completion, Stimulation Optimization, and Risk Mitigation, in: SPE Eastern Regional Meeting, Society of Petroleum Engineers, Charleston, West Virginia, 2009.
- [7] M. Marongiu-Porcu, X. Wang, M.J. Economides, Delineation of Application and Physical and Economic Optimization of Fractured Gas Wells, in: SPE Production and Operations Symposium, Society of Petroleum Engineers, Oklahoma City, 2009.
- [8] X. Zhang, C. Du, F. Deimbacher, M. Crick, A. Harikesavanallur, Sensitivity Studies of Horizontal Wells with Hydraulic Fractures in Shale Gas Reservoirs, in: International Petroleum Technology Conference, International Petroleum Technology Conference, Doha, Qatar, 2009.
- [9] S. Bhattacharya, M. Nikolaou, Optimal Fracture Spacing And Stimulation Design For Horizontal Wells In Unconventional Gas Reservoirs, in: SPE Annual Technical Conference and Exhibition, Society of Petroleum Engineers, Denver, Colorado, USA, 2011.
- [10] R. Schweitzer, H.I. Bilgesu, The Role of Economics on Well and Fracture Design Completions of Marcellus Shale Wells, in: SPE Eastern Regional Meeting, Society of Petroleum Engineers, West Virginia, USA, 2009.
- [11] M.Y. Soliman, J.L. Hunt, A.M. El Rabaa, Fracturing Aspects of Horizontal Wells, Journal of Petroleum Technology, 42 (1990).
- [12] E.A. ElRafie, R.A. Wattenbarger, Comprehensive Evaluation of Horizontal Wells with Transverse Hydraulic Fractures in the Upper Bahariya Reservoirs, in: Middle East Oil Show and Conference, Society of Petroleum Engineers, Bahrain, 1997.
- [13] E. Lolon, J.R. Shaoul, M.J. Mayerhofer, Application of 3-D Reservoir Simulator for Hydraulically Fractured Wells, in: Asia Pacific Oil and Gas Conference and Exhibition, Society of Petroleum Engineers, Jakarta, Indonesia, 2007.
- [14] B.R. Meyer, L.W. Bazan, R.H. Jacot, M.G. Lattibeaudiere, Optimization of Multiple Transverse Hydraulic Fractures in Horizontal Wellbores, in: SPE Unconventional Gas Conference, Society of Petroleum Engineers, Pittsburgh, Pennsylvania, 2010.
- [15] K. Sepehrnoori, W. Yu, An Efficient Reservoir Simulation Approach to Design and Optimize Unconventional Gas Production, in, Society of Petroleum Engineers, 2013.
- [16] S.E. Gorucu, T. Ertekin, Optimization Of The Design Of Transverse Hydraulic Fractures In Horizontal Wells Placed In Dual Porosity Tight Gas Reservoirs, in: SPE Middle East Unconventional Gas Conference and Exhibition, Society of Petroleum Engineers, Muscat, Oman, 2011.
- [17] R.D. Barree, S.A. Cox, J.L. Miskimins, J.V. Gilbert, M.W. Conway, Economic Optimization of Horizontal-Well Completions in Unconventional Reservoirs, SPE Production & Operations, Preprint (2015).
- [18] S. Gao, J. Yao, R. Lu, Y. Wang, Z. Sun, L. Li, Optimal Design of Nonuniform Multiple Transverse Fractures for Horizontal Wells in Tight Gas Reservoirs, in: SPE Unconventional Gas Conference and Exhibition, Society of Petroleum Engineers, Muscat, Oman, 2013.



- [19] R.D. Barree, S.A. Cox, J.L. Miskimins, J.V. Gilbert, M.W. Conway, Economic Optimization of Horizontal-Well Completions in Unconventional Reservoirs, *SPE Production & Operations*, 30 (2015) 293 - 311.
- [20] M. MoradiDowlatabad, M. Jamiolahmady, The lifetime performance prediction of fractured horizontal wells in tight reservoirs, *Journal of Natural Gas Science and Engineering*, 42 (2017) 142-156.
- [21] M.M. Dowlatabad, Novel Integrated Approach Simultaneously Optimising AFI Locations Plus Number and (A)ICD Sizes, in: *SPE EUROPEC 2015*, Society of Petroleum Engineers, Madrid, Spain, 2015.
- [22] A. Kalantari-Dahaghi, S. Mohaghegh, S. Esmaili, Coupling numerical simulation and machine learning to model shale gas production at different time resolutions, *Journal of Natural Gas Science and Engineering*, 25 (2015) 380-392.
- [23] B. Bagherian, A. Ghalambor, M. Sarmadivaleh, V. Rasouli, A. Nabipour, M.M. Eshkaftaki, Optimization of Multiple-Fractured Horizontal Tight Gas Well, in: *SPE International Symposium and Exhibiton on Formation Damage Control*, Society of Petroleum Engineers, Louisiana, USA, 2010.
- [24] A.P. Bungler, X. Zhang, R.G. Jeffrey, Parameters Affecting the Interaction Among Closely Spaced Hydraulic Fractures, *SPE Journal*, 17 (2012) 292 - 306.
- [25] W. El Rabaa, Experimental Study of Hydraulic Fracture Geometry Initiated From Horizontal Wells, in: *SPE Annual Technical Conference and Exhibition*, Society of Petroleum Engineers, San Antonio, Texas, 1989.
- [26] D.G. Crosby, Z. Yang, S.S. Rahman, Methodology to Predict the Initiation of Multiple Transverse Fractures from Horizontal Wellbores, *J Can Petrol Technol*, 40 (2001).
- [27] M.D. McKay, R.J. Beckman, W.J. Conover, A Comparison of Three Methods for Selecting Values of Input Variables in the Analysis of Output from a Computer Code, *Technometrics*, 21 (1979) 239-245.
- [28] M. MoradiDowlatabad, F. Zarei, M. Akbari, The Improvement of Production Profile While Managing Reservoir Uncertainties with Inflow Control Devices Completions, in: *SPE Bergen One Day Seminar*, Society of Petroleum Engineers, Bergen, Norway, 2015.
- [29] M. MoradiDowlatabad, M. Jamiolahmady, Novel Approach for Predicting Multiple Fractured Horizontal Wells Performance in Tight Reservoirs, in: *SPE Offshore Europe Conference and Exhibition*, Society of Petroleum Engineers, Aberdeen, UK, 2015.

Table 1: Reservoir Parameters.

Parameter	Value	Unit
Initial Reservoir Pressure	7500	psi
<b>Min Bottom hole Flowing Pressure</b>	<b>3000-5000</b>	<b>psi</b>
<b>Reservoir Permeability</b>	<b>0.001-0.1</b>	<b>mD</b>
Reservoir Temperature	200	°F
Reservoir Porosity	0.15	
Rock Compressibility	3.82E-6	psi
Reservoir Depth	14800	ft
Well Diameter	4.5	inch

Table 2: Fracture parameters and their variation ranges.

Parameter	Min	Max	Distribution	Unit
Number of Fractures ( $N_f$ )	1	15	Uniform	
Fracture Spacing ( $S_f$ )	80	650	Uniform	ft
Fracture Half-Length ( $X_f$ )	100	1020	Uniform	ft
Fracture Width ( $W_f$ )	2	8	Uniform	mm
Fracture Permeability ( $K_f$ )	10	200	Uniform	Darcy

Table 3: Fracture and operating costs [10].

		$X_f < 250$ ft	$X_f > 250$ ft
$C_{frac}$	Fixed cost (\$)	25,000	100,000
	Fracture Cost (\$)	300	+100\$ per extra ft
		$L_w < 1000$ ft	$L_w > 1000$ ft
$C_{well}$	Fixed cost (\$)	1,500,000	2,000,000
	Drilling Cost (\$)	500	+100\$ per extra ft

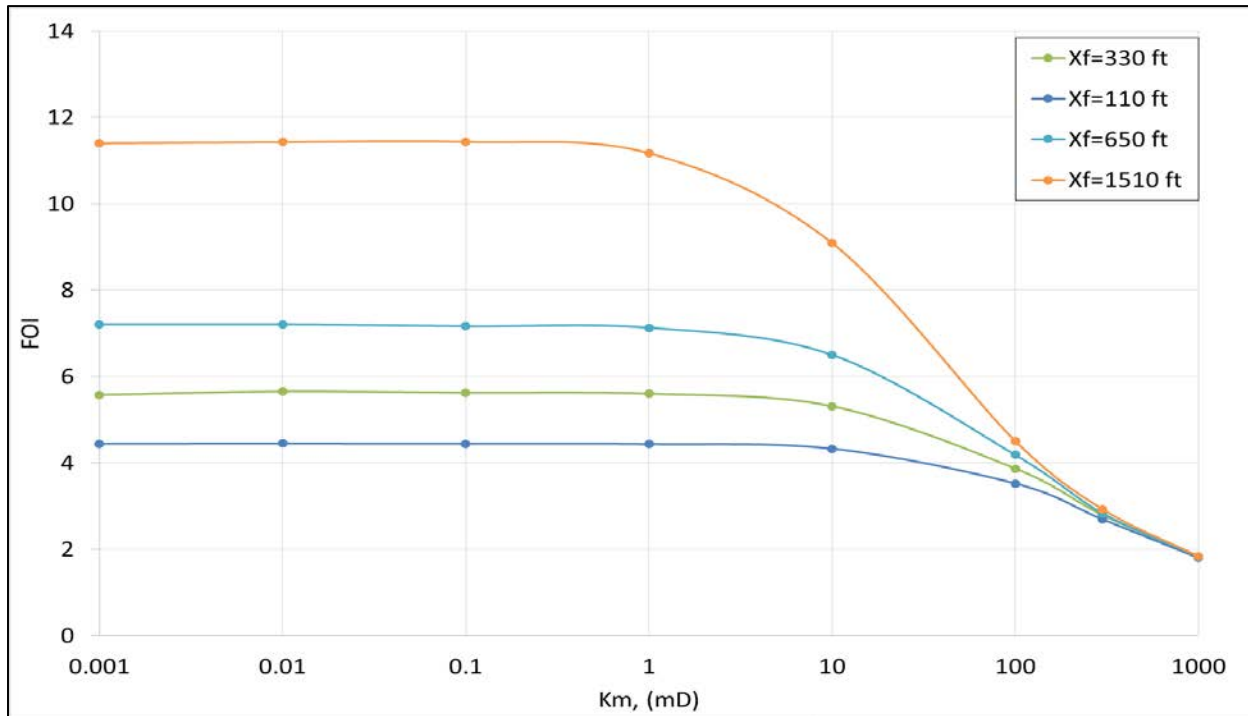


Fig 1: Folds of PI increase (FOI) versus matrix permeability for various Open-hole MFHWs completion with infinite conductivity and  $N_f=5$  in an anisotropic formation ( $K_v/K_h=0.1$ ).

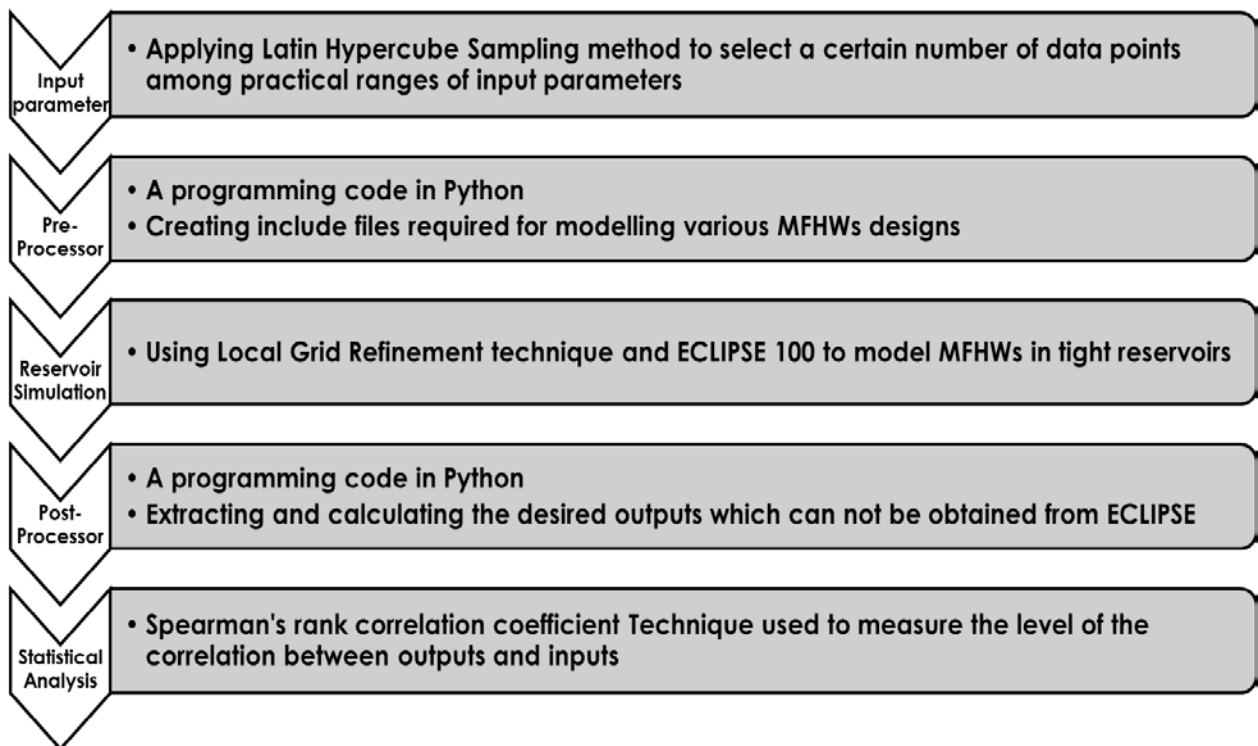


Fig 2: The sequence of steps followed to produce the sample experiments

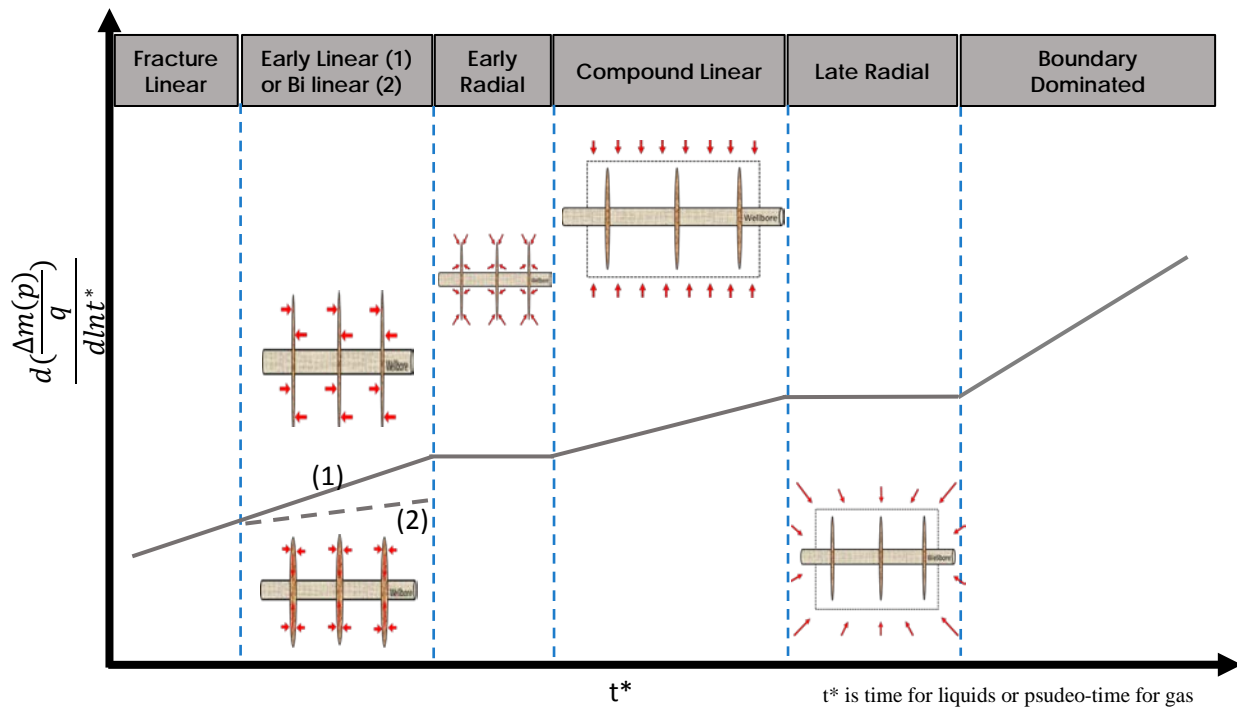


Fig 3: Schematic diagram illustrating the theoretical flow regimes sequence for a MFHW.

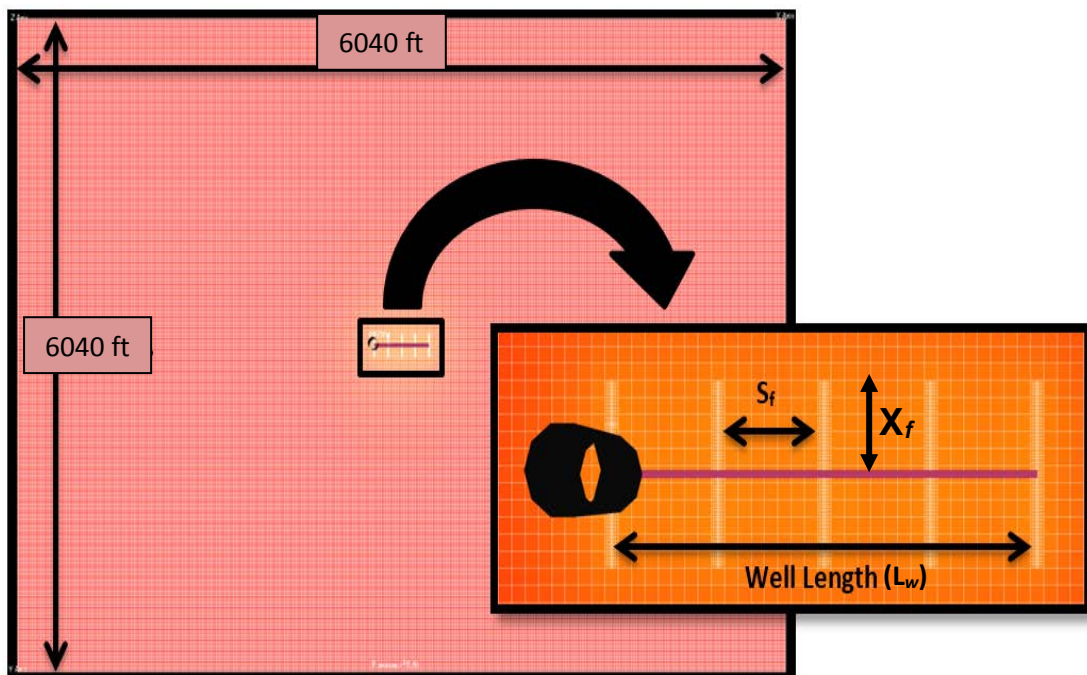


Fig 4: The simulation model used in this study.

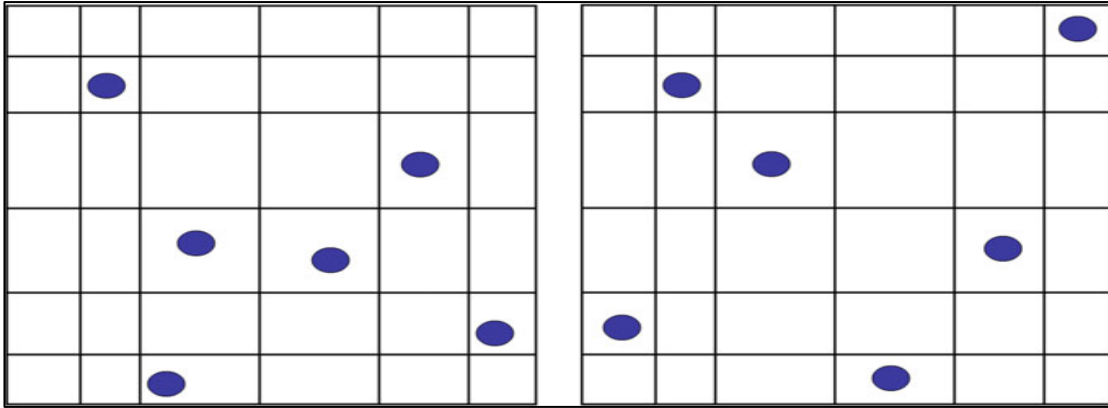


Fig 5: Examples of a square grid containing sample positions generated at random without any constraint (left) and of a Latin square where only one sample is contained in each row and each column (right).

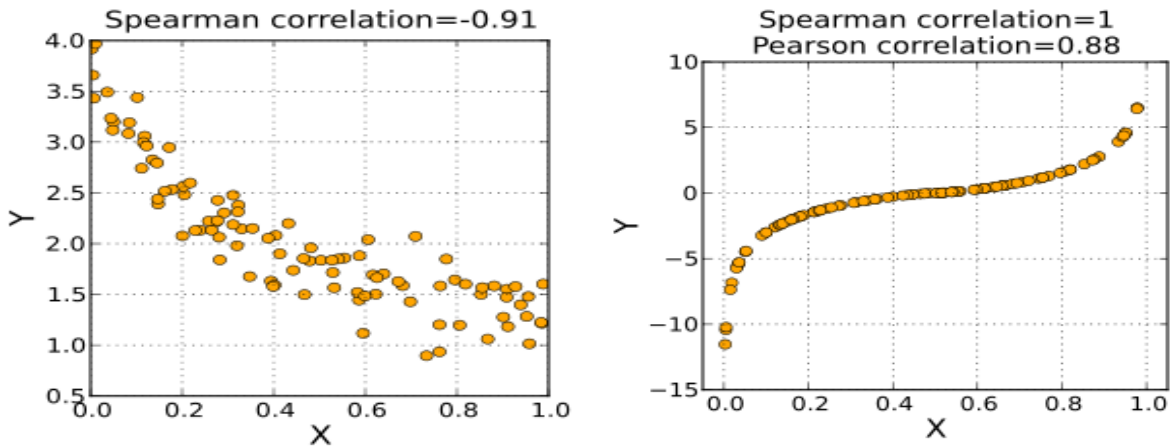


Fig 6: Examples of Spearman correlation coefficients.

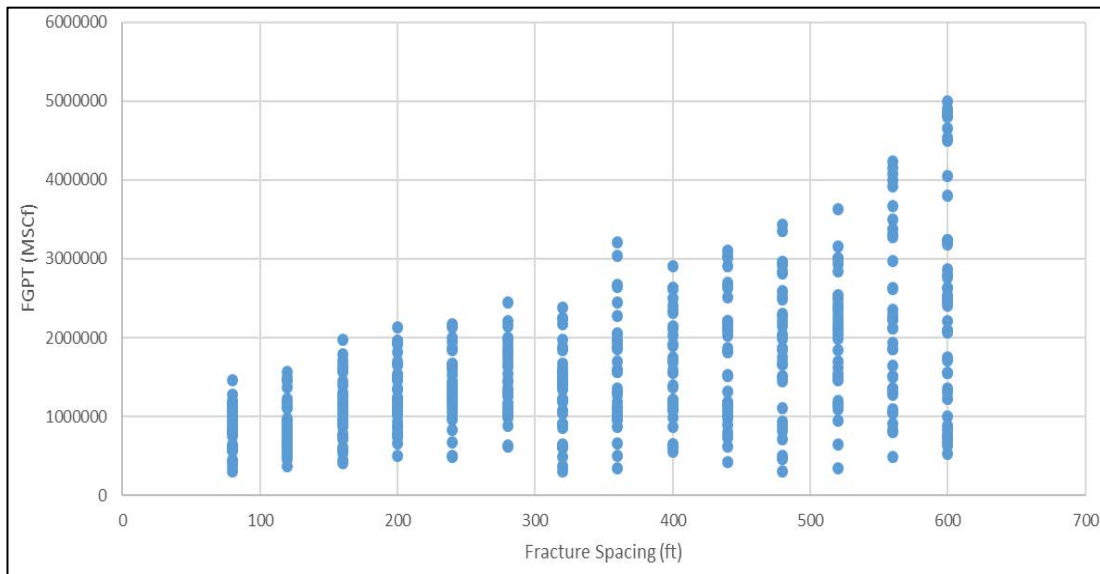


Fig 7: The total gas production (FGPT after 20 years of production) for different fracture spacing ( $S_f$ ) while other parameters changed simultaneously,  $K_m=0.01$  mD.

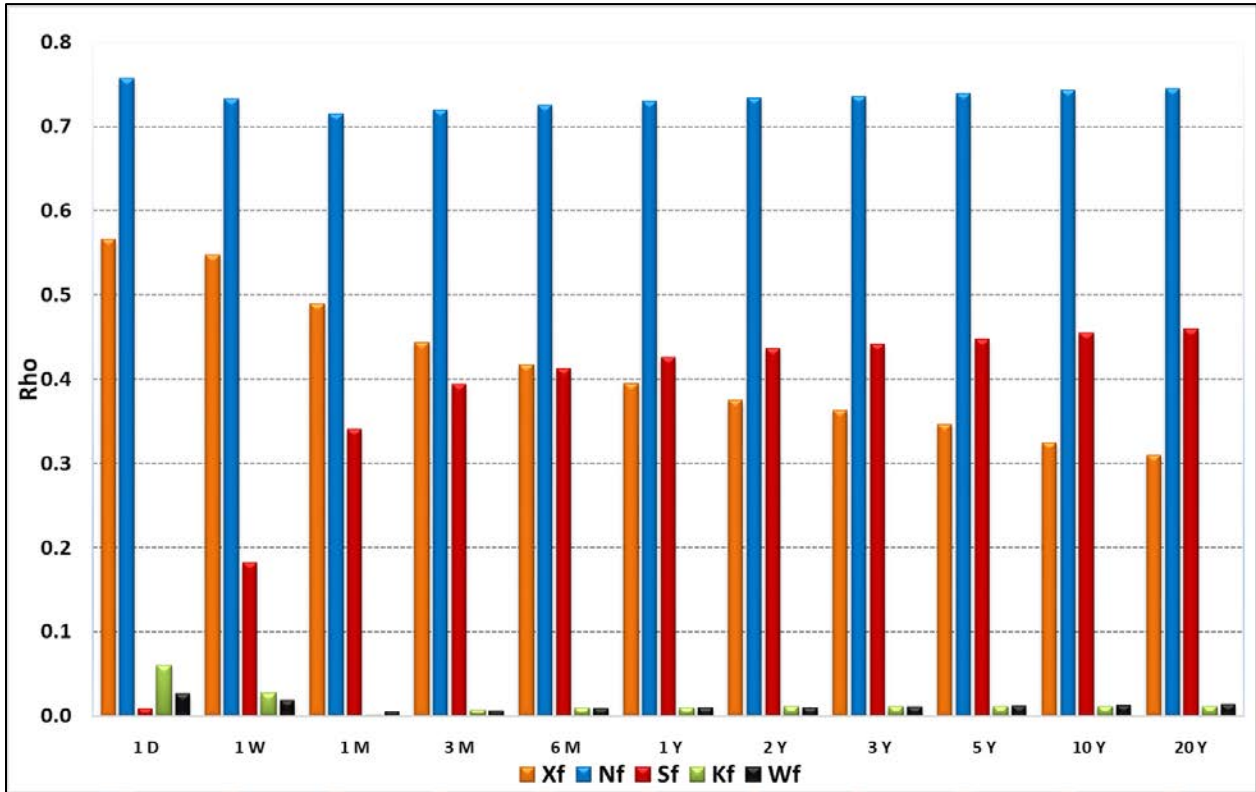


Fig 8: The impact of five pertinent parameters on FGPT values over the 20-year well lifetime ( $K_m=0.01$  mD).

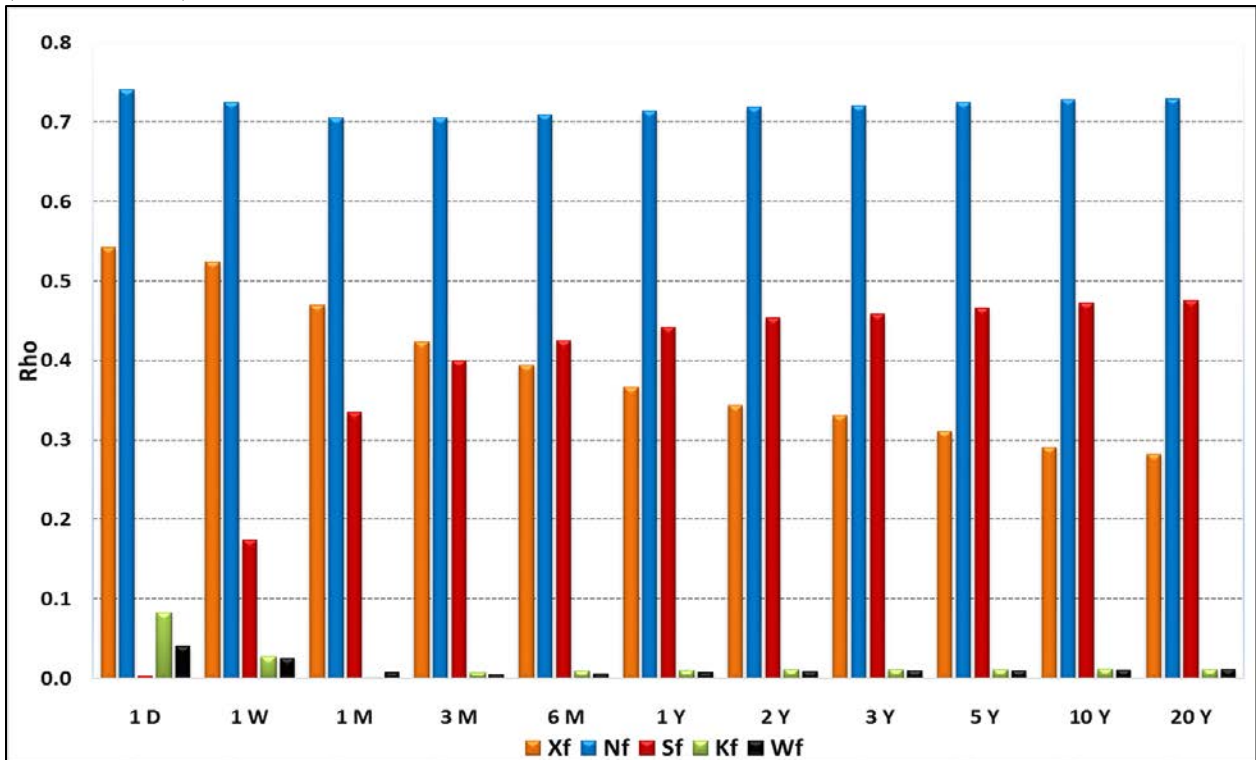


Fig 9: The impact of five pertinent parameters on PI values over the 20-year well lifetime ( $K_m=0.01$  mD).

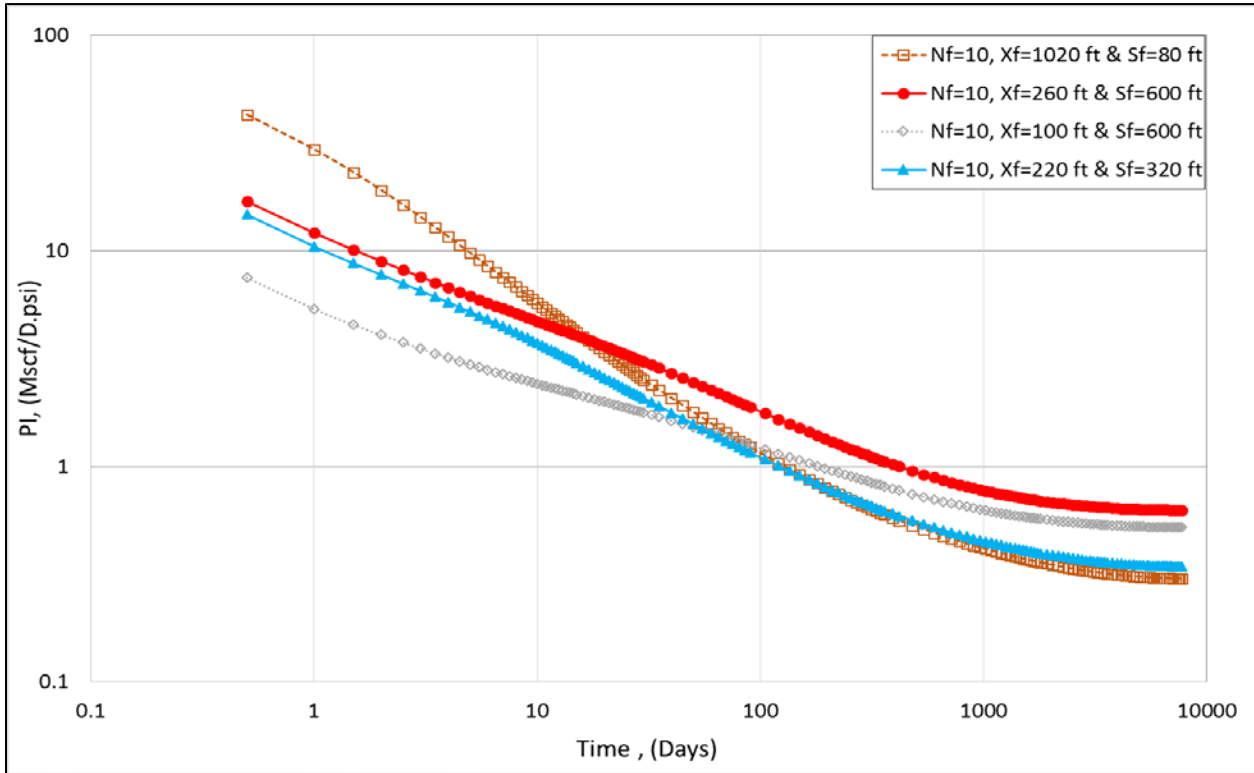


Fig 10: PI values of four MFHW completion designs over the 20-year well lifetime ( $K_m=0.01$  mD,  $K_f=200$  D,  $W_f=0.025$  ft).

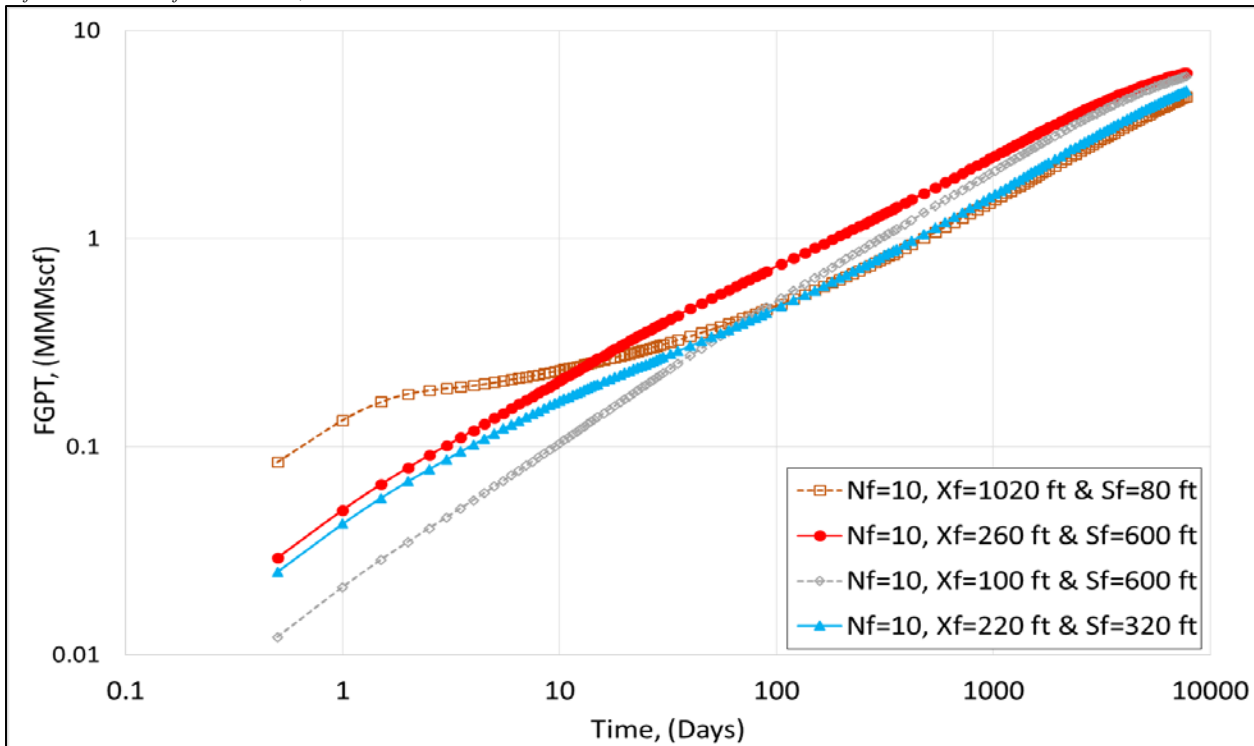


Fig 11: FGPT values of four MFHW completion designs over the 20-year well lifetime ( $K_m=0.01$  mD,  $K_f=200$  D,  $W_f=0.025$  ft).



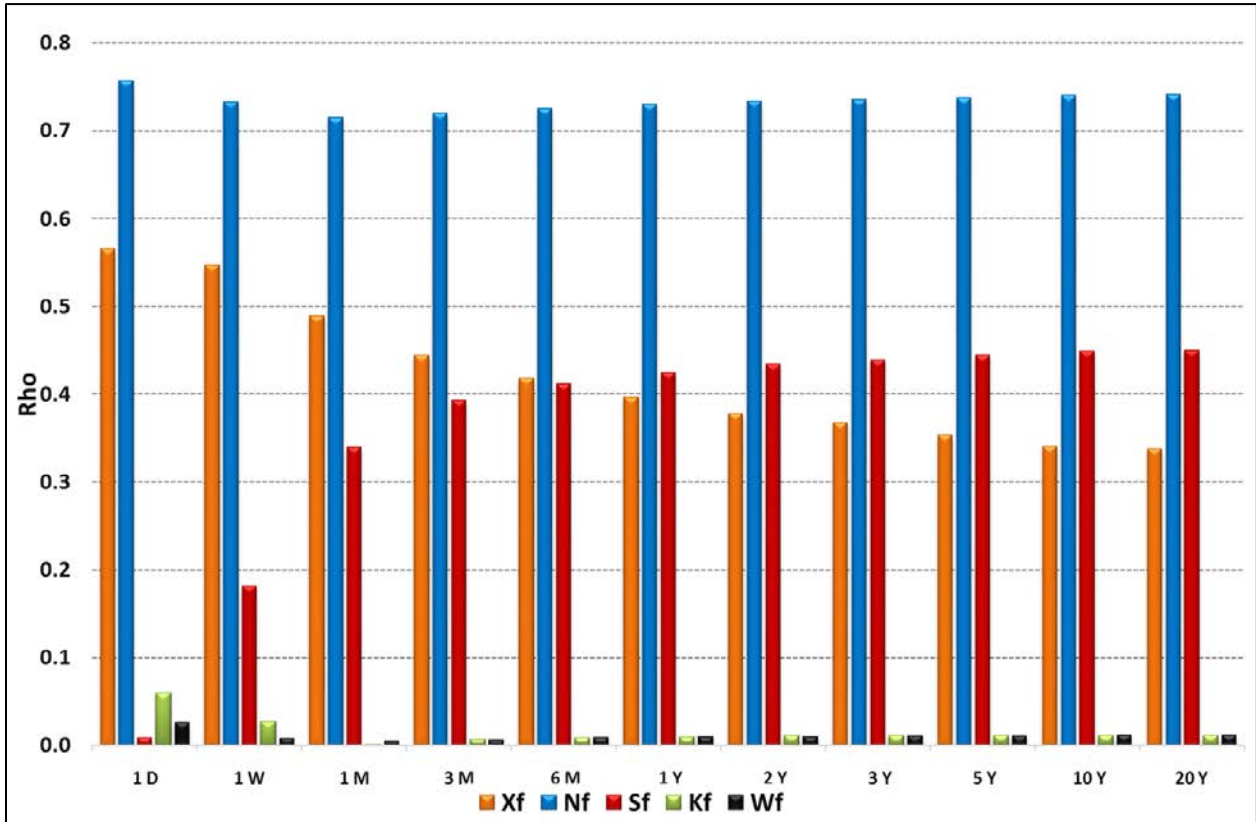


Fig 12: The impact of five pertinent parameters on DCGP values over the 20-year well lifetime ( $K_m=0.01$  mD).

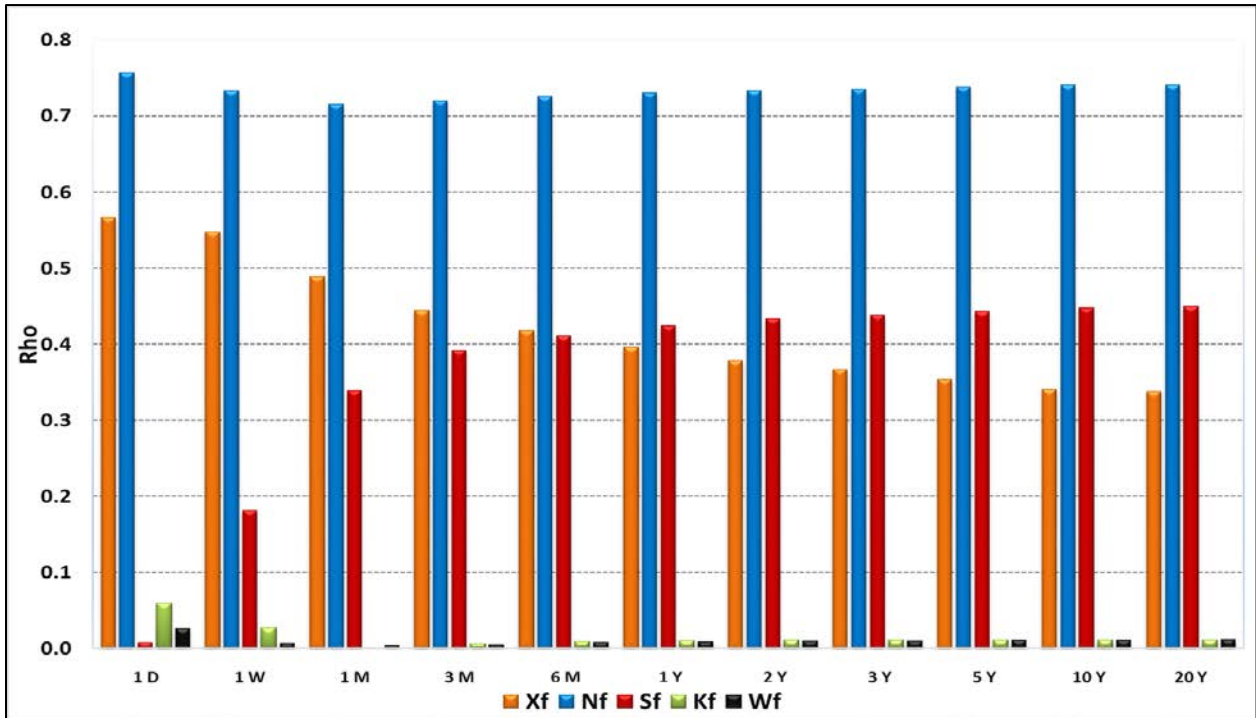


Fig 13: The impact of five pertinent parameters on NPR values over the 20-year well lifetime ( $K_m=0.01$  mD).



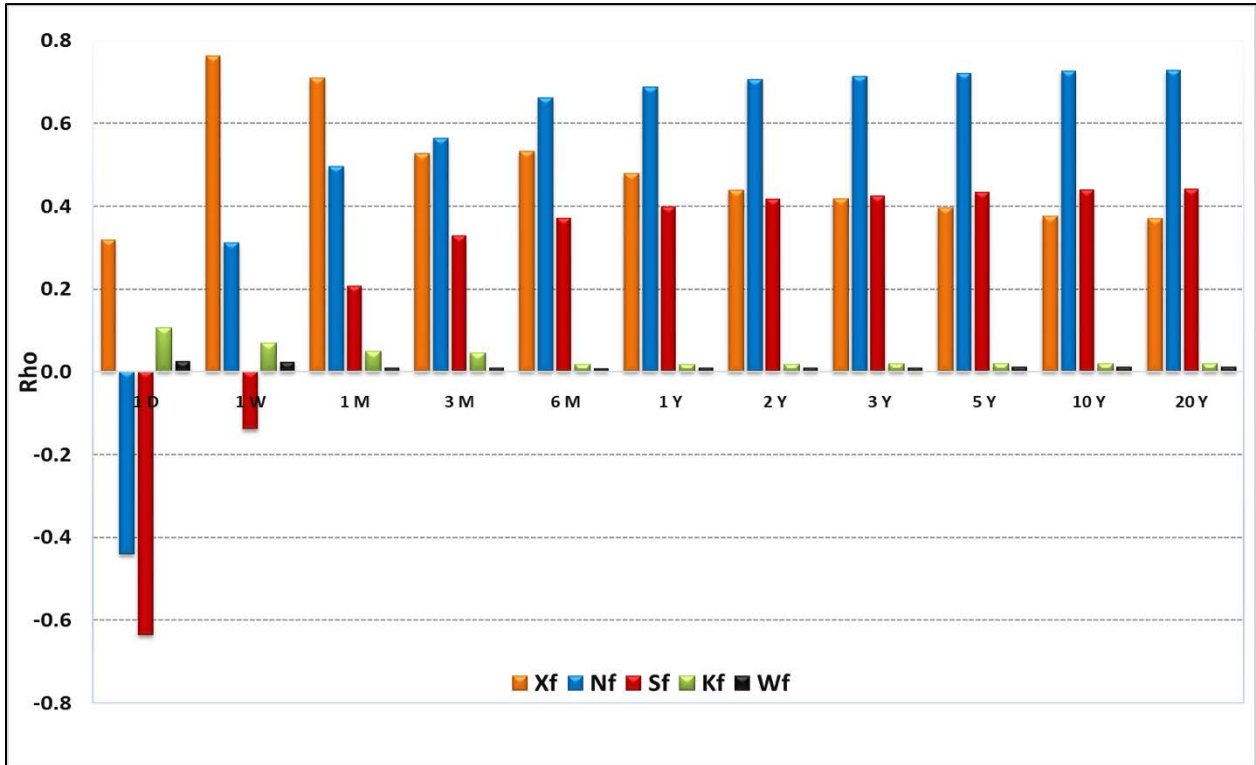


Fig 14: The impact of five pertinent parameters on NPV values for the 20-year well lifetime ( $K_m=0.01$  mD).

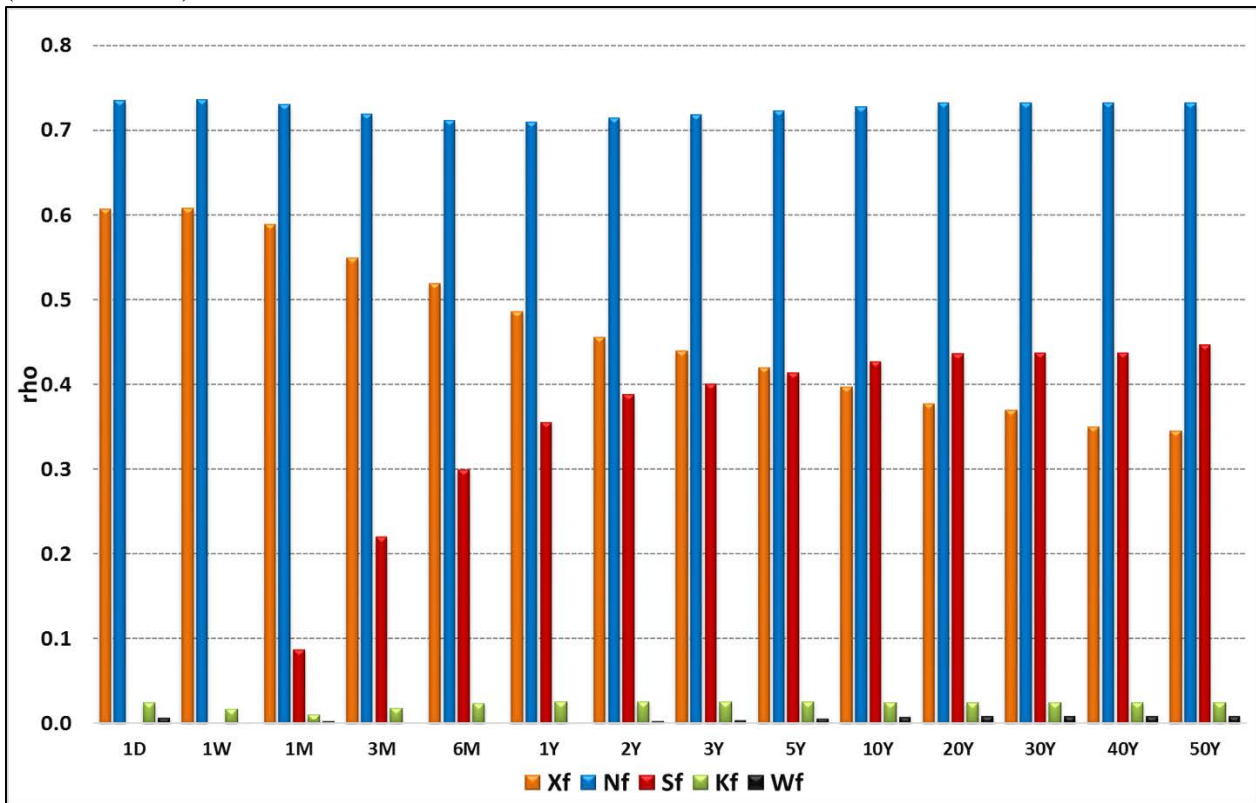


Fig 15: The impact of five pertinent parameters on FGPT over the 50-year well lifetime ( $K_m=0.001$  mD).

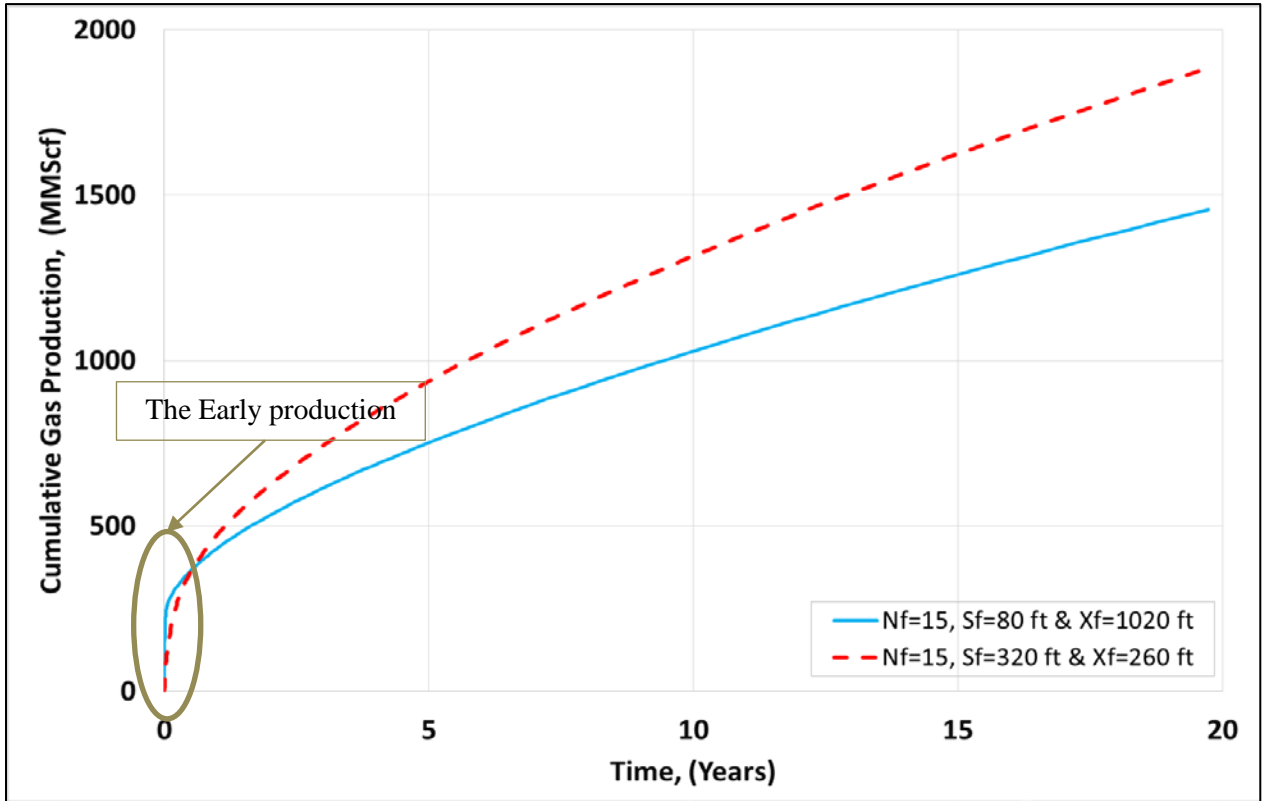


Fig 16: Cumulative Gas Production for two different MFHWs designs at  $K_m=0.001$  mD.

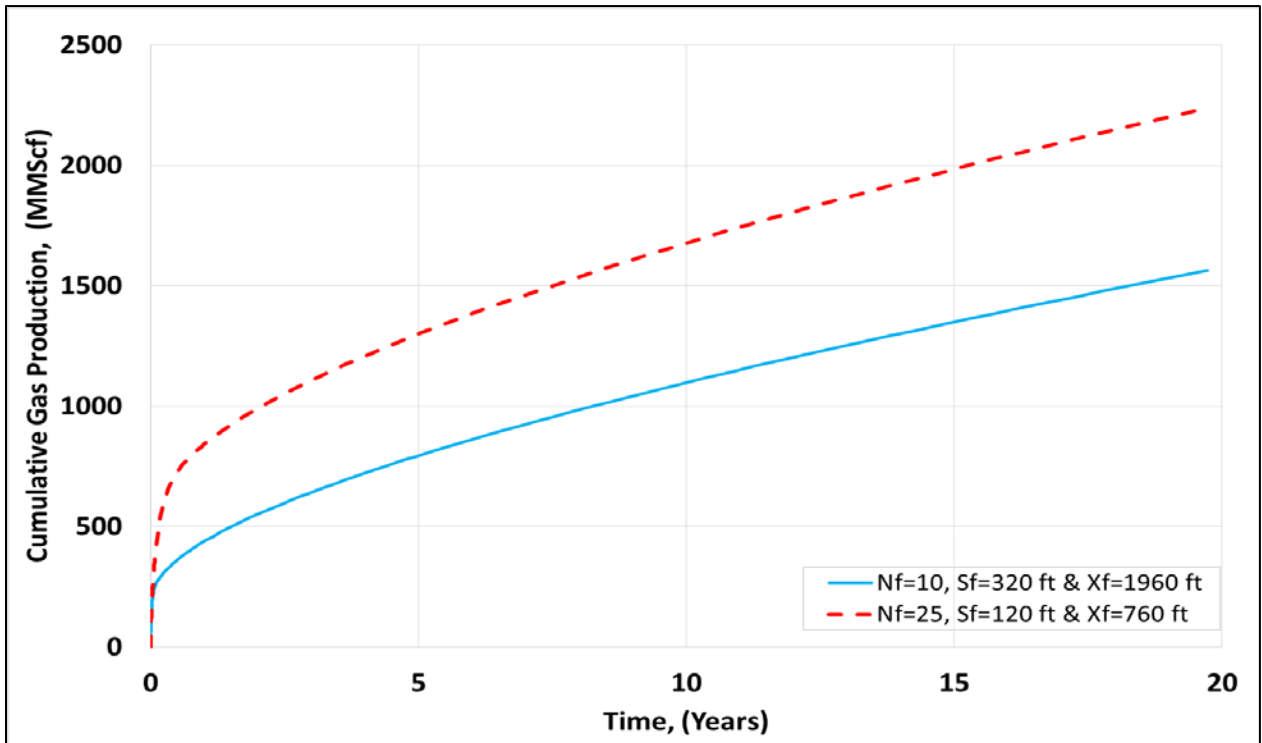


Fig 17: Cumulative Gas Production for two different MFHWs designs at  $K_m=0.001$  mD.

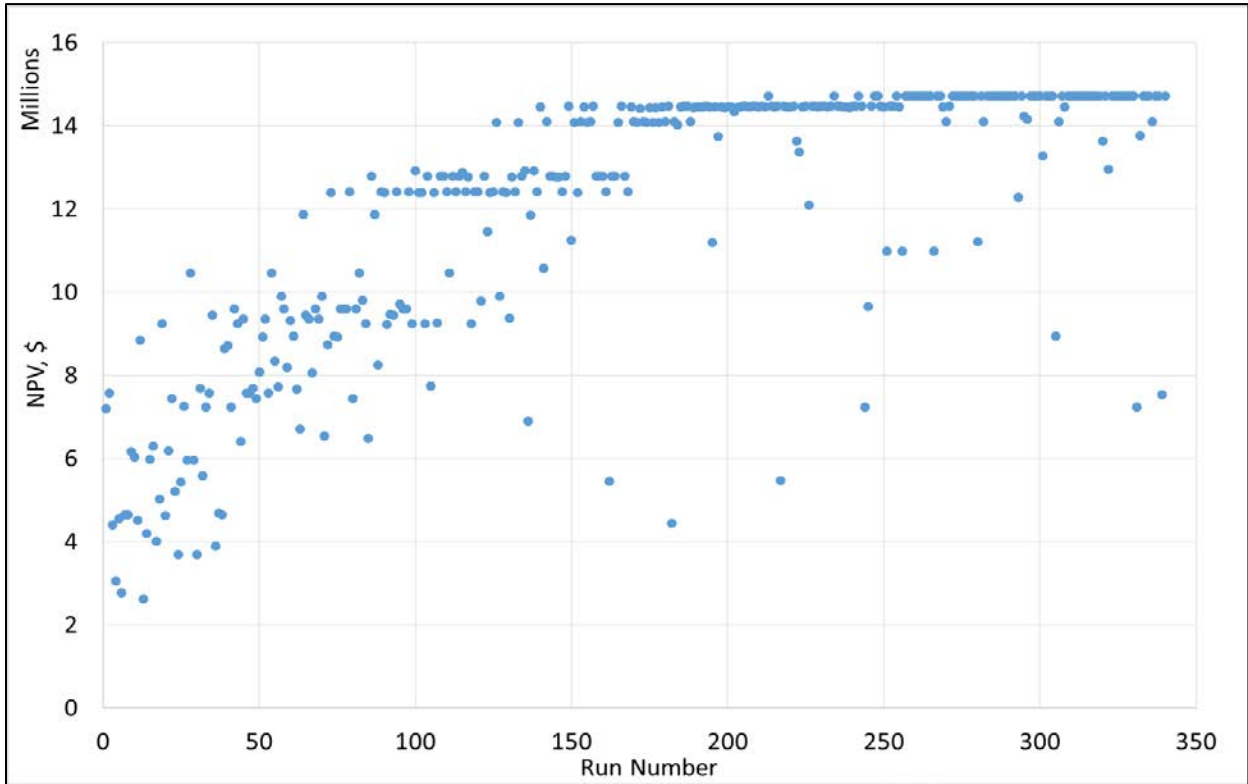


Fig 18: NPV values for 340 cases, performed by the optimizer to determine the optimum MFHW design, in the reservoir with  $K_m=0.01$  mD.

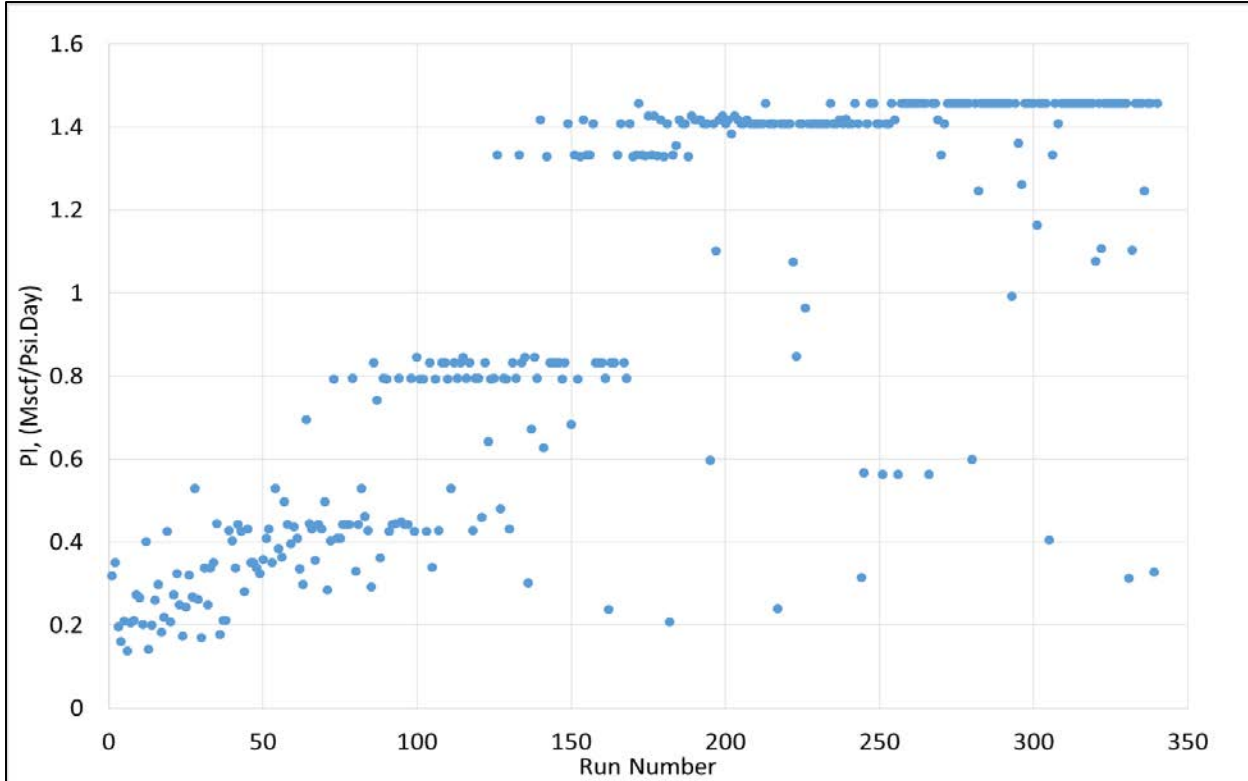


Fig 19: PI values for 340 cases, performed by the optimizer to determine the optimum MFHW design, in the reservoir with  $K_m=0.01$  mD.