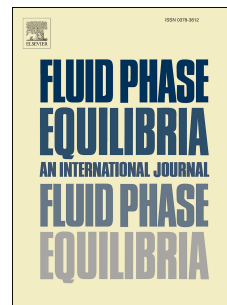


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Experimental and modelling study of the densities of the hydrogen sulphide + methane mixtures at 253, 273 and 293 K and pressures up to 30 MPa.

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ABSTRACT

Densities of three binary mixtures of hydrogen sulphide and methane ($x\text{H}_2\text{S} + (1-x)\text{CH}_4$), with mole fractions of 0.1315, 0.1803 and 0.2860 of acid gas, were determined experimentally at three temperatures (253, 273 and 293) K and at pressures up to 30 MPa. Densities were measured continuously using a high temperature and high pressure Vibrating Tube densitometer (VTD), Anton Paar DMA 512. The SAFT-VR Mie, PR and GERG2008 equations of state (EoS) are used to describe the experimental data with different levels of success.

Keywords: CH₄, H₂S, Thermophysical properties, Acid gas injection

1. Introduction

Many sour natural gases reservoirs and sour gas condensates fields have been discovered in the last thirty years. This kind of natural hydrocarbon gas reservoirs represent about half of the known total worldwide resources (270 trillion m³) [1]. Acid gases are those raw natural

gases which contain significant amounts of carbon dioxide (CO_2) and hydrogen sulphide (H_2S), with compositions around of 0-80% moles CO_2 and 0-30% H_2S [2]. For this gas with high acid gas content carbon capture storage (CCS) technologies, such as oxy-fuel combustion, have the potential to become economically competitive with other zero-carbon and renewal sources of energy [3]. Thus, CCS may allow continuing to burn fossil fuels in power stations preventing CO_2 emissions to the atmosphere. CCS refers to a large number of technologies and processes, such as combustion methods (pre-combustion, post-combustion and oxy-fuel), transport pipelines or injection systems in geological basins [4]. Pressure-Volume-Temperature (PVT) data and thermophysical property models are of principal importance to the design of process involved in the capture, transport and storage of CO_2 .

Since hydrogen sulphide is a toxic and corrosive compound, it is necessary to process sour gases in order to remove acid gases before their uses [5]. Different regulations require that H_2S contain of sweet gases must be less than 4 ppm. The sweetening and desulphurisation of acid gases, such as the SPREX process [6] or physical and chemical absorption with solvents, are costly processes that require accurate thermodynamic models to design natural gas processing plants. The methane- H_2S binary system is of interest to the oil and gas industry [7] because CH_4 and H_2S are important components of reservoir fluids.

There are limited references available in the literature concerning single phase density (ρ - PTx) of methane and hydrogen sulphide systems (Table 1). In 1951, Reamer et al [8] did a thorough study of this binary mixture, they were the first to measure vapour-liquid equilibria (VLE) and densities of several $\text{H}_2\text{S} + \text{CH}_4$ systems [9]. Reamer's density measurements cover a wide range of compositions (0.1-0.9 mol fraction H_2S), temperatures (277-411 K) and pressures (up to 69 MPa) with 1140 data. Bailey et al. [10] studied the system 49% mol of CH_4 and 51% mol of H_2S at higher temperature (501 K) The main goal of the new measurements presented in this work is to complete the literature data at low temperature.

In this paper, new density data of $\text{H}_2\text{S} + \text{CH}_4$ mixtures are presented for the following compositions (mole fractions): 0.1315 $\text{H}_2\text{S} + 0.8685 \text{CH}_4$, 0.1803 $\text{H}_2\text{S} + 0.8197 \text{CH}_4$ and 0.286 $\text{H}_2\text{S} + 0.714 \text{CH}_4$. The density of each system has been measured at three isotherms, 253, 273 and 293 K, and at pressures up to 30 MPa. The data of the three measured systems are compared to density calculations using three types of equation of state: the Peng-Robinson EoS [11], the SAFT-VR Mie EoS [12] and the multiparameter GERG-2008 EoS [13] for

natural gas). Finally, all the literature data were modelled using the three EoS proposed, in order to evaluate these models in a wider range of temperature, pressure and compositions.

2. Experimental

2.1 Sample preparation

The specification and sources of the chemicals used in this work are summarized in Table 2. Three mixtures of CH₄ and H₂S were prepared volumetrically at laboratory temperature in 300 cm³ cylinder with its own pressure transducer to track the pressure of the sample. The final pressure target of the mixture in the vessel was approximately 40MPa in order to avoid any phase change and possible variations of composition during the injection of mixture into the densitometer set-up. To prepare the mixture, a volume of H₂S is first injected into the cylinder; thereby the injected volume will contain the number of moles calculated by an EoS to reach the expected final composition. Second, the methane is pumped in the cylinder until it the final pressure is reached. Finally, the composition of each mixture was validated by gas chromatography analysis (Varian model CP-3800). The resulting compositions of the prepared mixtures have been 0.1315, 0.1803 and 0.2860 mole fractions of H₂S.

2.2 Equipment description

A full description of the experimental set-up and procedures are available in Bouchot and Richon [14], Coquelet et al. [15] and Nazeri et al. [16]. The density of the studied mixture have been measured in a Hastelloy Vibrating Tube Densitometer (VTD), Anton Paar model DMA 512, using the one fluid reference calibration method [17].

2.3 Experimental procedure

Three isotherms of each binary system were measured at 253, 273 and 293 K. The mixture was gradually charged from the cylinder in the experimental set-up while the vibrating period, the temperature and the pressure were recorded continuously during the slow-increasing pressure up to 30 MPa and the slow decompression (the pressure in the vessel containing the mixture was maintained at pressure higher than 30 MPa during all the measurements). During the depressurisation, the acid outlet gas was neutralised by bubbling it through a column with a basic solution of sodium hydroxide.

2.4 Uncertainty of measurements

Uncertainties of the properties measured have been evaluated as standard uncertainties of type A and type B [18]. Type A of uncertainties is based on the statistical treatment of experimental data. The uncertainty of the composition measurements was evaluated as type A and it was calculated as [19]:

$$u(x_{H_2S}) = \sqrt{\frac{\sigma^2(x)}{N}} \quad (1)$$

where σ^2 is the variance of the values measured and N is the number of measurements. The expanded uncertainties ($k=2$, in order to increase the confidence level up to 95% [19]) of the composition of the three systems are 0.0006 for 0.1315 H₂S mole fraction system, 0.0008 for 0.1803 H₂S mole fraction system and 0.0011 for 0.2860 H₂S mole fraction system.

The uncertainties type B are evaluated by other means (not purely statistical), such as literature, manufacturer information, previous experience or, as in our case, calibrations. Then, uncertainty on temperature and pressure measurements was estimated as type B.

The temperature of the system in the set-up is regulated by two liquid thermoregulated baths, which temperatures are measured with two Pt100 (100 Ω platinum resistance) probes. The probes calibration is done against a 25 Ω reference thermometer (Tinsley Precision Instrument). From the calibrations, the expanded uncertainty ($k=2$) in temperatures measurements was estimated to be 0.03 K.

The pressure was measured by two pressure transducers at two complementary ranges, one between 0-5 MPa and other from 5 up to 30 MPa. The calibration of the transducers was done using a dead weight balance (Desgranges & Huot, model 5202S). The expanded uncertainties ($k=2$) of the pressure measurements from the calibration are estimated to be less than 0.003 MPa for low pressure (up to 5 MPa) and 0.005 MPa for higher pressures than 5 MPa (up to 30 MPa).

Density uncertainty was evaluated as combined standard uncertainty, because density is expressed through the combination of two sources of expanded standard uncertainty: calibration and densitometer information. There is a mathematical relation ($\rho=a\tau+b$) between these standard uncertainties, therefore applying the law of propagation of uncertainty [20], density uncertainty was obtained by:

$$u(\rho) = \sqrt{\left(\frac{\partial \rho}{\partial \tau}\right)_{a,b}^2 u(\tau)^2 + \left(\frac{\partial \rho}{\partial a}\right)_{\tau,b}^2 u(a)^2 + \left(\frac{\partial \rho}{\partial b}\right)_{\tau,a}^2 u(b)^2}, \quad (2)$$

where τ is the vibrating period and ‘a’ and ‘b’ are the calibration parameters. From manufacturer’s specifications, the standard uncertainty on the period of oscillation is 10^{-8} s. Uncertainty on the parameters of the calibration has been estimated to be 0.5% over the investigated range of pressures; however, it is worth highlighting that, due to the used technique, average uncertainty at low pressure (below 0.5 MPa) was 8.6%. The combined standard uncertainties of the measurements are reported accompanying the density data in Tables 6-14.

The calculation of the compressibility factor (Z) is function of the 3 measured properties ($Z=P/\rho RT$): temperature, pressure and density. Therefore, $u(Z)$ gives an idea of the overall uncertainty of our experimental data because includes the uncertainty of every measurement. Then, following the same approach, the uncertainty of the Z was calculated using the law of propagation of uncertainty as:

$$u(Z) = \sqrt{\left(\frac{\partial Z}{\partial P}\right)_{\rho,T}^2 u(P)^2 + \left(\frac{\partial Z}{\partial \rho}\right)_{P,T}^2 u(\rho)^2 + \left(\frac{\partial Z}{\partial T}\right)_{P,\rho}^2 u(T)^2} \quad (3)$$

Further information about calculations of the combined uncertainties of our measurements is provided in Appendix A.

3. Modelling

3.1 Peng and Robinson

The critical properties (T_c and P_c) and acentric factors (ω) of methane and hydrogen sulphide are given in Table 3. The pure component parameters have been used to model the system with the Peng and Robinson (PR) EoS [11], which is one of the most used cubic EoS due its simplicity and reasonable accuracy to correlate phase equilibria for components involved in this study such as carbon dioxide [21] or hydrogen sulphide [7]. In this work the van der Waals (classical) mixing rules are used, i.e.:

$$b = \sum_i x_i b_i \quad (4)$$

$$a = \sum_i \sum_j x_i x_j \sqrt{a_i a_j} (1 - k_{ij}) \quad (5)$$

where a and b are the parameters in the PR-EoS and k_{ij} the binary interaction parameter (BIP).

The BIPs are coefficients introduced to describe the experimental phase behaviour. Thus, the binary parameters avoid wrong predictions of the two phase region during density calculations. A temperature independent k_{ij} has been regressed by minimizing the objective function given in Equation 6, which is based on calculated bubble point pressures and experimental VLE data from the literature [7] [8] [22]. The regressed BIP is reported in Table 5.

$$\min F = \frac{100}{N} \sum_1^N \left(\frac{P_{bubble}^{exp} - P_{bubble}^{cal}}{P_{bubble}^{exp}} \right) \quad (6)$$

The PR-EoS tends to underestimate experimental densities [23]. Volume translations can be used in order to improve the density calculations of liquid and dense fluid phases. The Peneloux volume correction [24] has been implemented here (Equation 7) and the results with and without Peneloux shift parameters are discussed in Section 4.

$$V = V^{PR} + \sum_i^{N_{Comp}} x_i V_i^c \quad (7)$$

where V^{PR} is the molar volume calculated by the PR EoS, x_i the mole fraction of each pure component i , and V_i^c the volume correction parameter. The values of the parameters are reported in Table 3.

3.2 SAFT-VR Mie

The SAFT-VR Mie EoS proposed by Lafitte et al [12] is one of the latest updates of the SAFT family of EoS. In this equation of state, the attractive and repulsive interactions between the segments that build the molecules are described by the Mie potential that is defined as:

$$u^{Mie}(r) = \frac{\lambda_r}{\lambda_r - \lambda_a} \left(\frac{\lambda_r}{\lambda_a} \right)^{\frac{\lambda_r}{\lambda_r - \lambda_a}} \varepsilon \left(\left(\frac{\sigma}{r} \right)^{\lambda_r} - \left(\frac{\sigma}{r} \right)^{\lambda_a} \right) \quad (8)$$

where r is the intersegment distance, σ the temperature-independent segment diameter, and ε the potential depth; λ_r and λ_a are the repulsive and attractive ranges, respectively.

The SAFT-VR Mie EoS can be expressed in terms of the reduced Helmholtz energy as the sum of several contributions:

$$a = \frac{A}{nRT} = a^{IDEAL} + a^{MONOMER} + a^{CHAIN} + a^{ASSOCIATION} \quad (9)$$

The molecular parameters for CH₄ and H₂S are presented in Table 4. Hydrogen sulphide parameters were regressed using experimental saturation pressures (P_{sat}) and liquid densities (ρ_{sat}), thereby the fitting consisted in the minimization of the following objective function [12]:

$$\min_{\theta} F = \frac{1}{N_{P_{sat}}} \sum_{i=1}^{N_{P_{sat}}} \left[\frac{P_{sat,i}^{exp}(T_i) - P_{sat,i}^{calc}(T_i; \theta)}{P_{sat,i}^{exp}(T_i)} \right]^2 + \frac{1}{N_{\rho_{sat}}} \sum_{i=1}^{N_{\rho_{sat}}} \left[\frac{\rho_{sat,i}^{exp}(T_i) - \rho_{sat,i}^{calc}(T_i; \theta)}{\rho_{sat,i}^{exp}(T_i)} \right]^2 \quad (10)$$

A temperature independent binary interaction parameter was regressed following the same approach and VLE data as for the PR-EoS. The resulting k_{ij} is also reported in Table 5.

3.3 GERG

GERG-2008 is a wide-range EoS for natural gases and other similar mixtures of gases [13]. It is an empirical equation of state based on pure component EoS and correlations for the binary systems [25]. Like the SAFT EoS, GERG is expressed in terms of the Helmholtz free energy, as the sum of an ideal gas contribution and a residual part.

In this work, the PR, SAFT-VR Mie and GERG-2008 [13] EoSs were employed to predict the densities of mixtures and were implemented into the thermodynamic package HWPVT [16] [26] [27] [28] [29].

4. Result and discussion

Densities of three binary systems of CH₄ and H₂S with 0.1315, 0.1803 and 0.2860 mol fractions of hydrogen sulphide have been measured continuously using a high temperature and high pressure VTD Anton Paar. First, the densitometer calibration was done using pure ethane with a first-order polynomial calibration at 253, 273 and 293 K and pressures up to 31 MPa. Previous to the measurements, the phase envelopes of the three binary systems have been studied in order to forecast at which pressure the two phase behaviour is found. The phase diagrams of the three measured systems calculated by the PR-EoS and other three systems comparing calculations against literature data [22] are shown in the Figure 1. According to Scott and van Konynenburg, the phase diagram of this system is classified as type III [7]. This

means that the curves presented in the phase envelopes of Figure 1 are dew lines, therefore no density was measured in the liquid region. The studied binary mixtures are systems with no critical point [30] [31], thus all our ρ - PTx measurements have been done in the gas phase. The P-T envelopes show that there is no phase change for any of the studied isotherms for the 0.1315 mol fraction of H₂S system. However, it is possible to enter the two phase region at 253K for the 0.1803 mol fraction of H₂S system and at 253 and 273K in the 0.2860 mol fraction of H₂S system.

The experimental density data for the measured systems are presented in Table 6 to Table 14. The compressibility factors derived from the measured temperature, pressure and density data, as well as their uncertainty, are also reported in the Tables 6-14.

The PR, SAFT-VR Mie and GERG-2008 equations of state have been used to model the density of the methane and hydrogen sulphide binary systems. The modelling results are presented by comparing the average deviations (%AAD) between the models and the experimental data. The AAD is the absolute average deviation and is defined as:

$$ADD (\%) = \frac{1}{N} \sum_{i=1}^N \left(\left| \rho_{\text{exp}} - \rho_{\text{EoS}} \right| / \rho_{\text{exp}} \right) \cdot 100 \quad (11)$$

The resulting SAFT-VR Mie parameters for pure hydrogen sulphide w_i are reported in Table 4, as well as the AAD(%) of the equation of state from the experimental vapour pressure P_{sat} , saturated-liquid densities ρ_{sat} (Figure 2) and enthalpy of vaporization ΔH_v [32]. The pure H₂S densities in the gas, liquid and supercritical regions have been evaluated at 13 temperatures between 200 to 500 K and pressures up to 100 MPa, reporting an %AAD of 2.3%. However, considering the H₂S single phase densities at the pressure and temperature ranges of our measurements, the absolute average deviation is 0.9% (Figure 3).

BIPs for the CH₄-H₂S system have been regressed for both the SAFT-VR Mie EoS ($k_{ij}=0.0314$) and the PR EoS ($k_{ij}=0.0807$) models using VLE data from the literature [7] [8] [22] (Figure 4). Using these BIPs, the PR EoS is slightly more accurate to correlate the phase behaviour of the CH₄-H₂S system than the SAFT-VR Mie EoS, with bubble point pressure AADs of 4.4% and 4.8%, respectively.

The deviations of the PR, SAFT-VR Mie and GERG-2008 models for the three measured systems at each temperature are reported in Table 15. Generally, the SAFT-VR Mie EoS

shows lower overall deviations (AAD=2.5%) than the other two models, PR EoS (3.0%) and GERG-2008 (3.4%). The experimental densities measured in this work and the predicted densities for the system 0.2860 H₂S mol fraction systems by using the GERG-2008 and SAFT-VR Mie are illustrated in Figures 5. As the GERG EoS is an empirical model developed for natural gases whose parameters for the CH₄+H₂S binary system have been fitted to experimental data over wide ranges of temperature (189 to 501 K), pressure (0.048 to 68.9 MPa) and methane mol fraction (0.1 to 0.9993) [13], it was unexpected that the GERG-2008 EoS reported the highest deviations for these systems, particularly for the 0.2860 mol fraction of H₂S system (Figure 5) with an AAD of 4.9%. However, the GERG-2008 EoS presents better results than SAFT and PR EoSs for the binary mixture with smaller amount of H₂S.

Density data available in the literature (1748 points) and those measured in this work have been modelled with the PR, PR + Peneloux volume correction, SAFT-VR Mie and GERG-2008 equations of state, and the deviations are listed in Table 16. As can be observed, the SAFT-VR Mie EoS reports the lower deviation between experimental and calculated densities with an AAD of 4.3%, while GERG-2008 shows similar level of agreement (4.6%). The experimental densities of 50 mol% H₂S + 50 mol% CH₄ and the predicted densities using the PR + Peneloux, GERG-2008 and SAFT-VR Mie EoSs are presented in Figure 6, as an example of the modelling result of this system at high pressure (up to 70MPa).

The PR-EoS is the studied model that has reported the largest total deviation (AAD=7.8%), especially when PR calculations are compared against Reamer et al. [8] data at pressures over 30 MPa. The results of the PR –EoS with volume correction (VC) have not been presented in Table 6 because no better density predictions were observed after applying the Peneloux VC to model our measured densities. However, remarkable improvements in the density calculations with the PR-EoS can be noticed in the results of modelling the full Reamer's data set using the PR-Peneloux, decreasing by half the ADD. The AAD reduces from 7.8% to 5.4% when the complete density data set is modelled using the PR with Peneloux shift model. Figure 7 shows the comparison of PR and PR-Peneloux calculations against literature data of the 0.3 mol fraction H₂S system, in order to illustrate the large deviations of PR EoS at high pressure.

The uncertainties for each measured density are reported in Tables 6-14. The uncertainties were evaluated as combined standard uncertainty with 95% level of confidence. Despite the

low average uncertainty (0.5%), the uncertainty of the density measurements below 0.5MPa is 8.3% with a maximum value of 10.1%. This high uncertainty was expected due to the fact that the vibrating tube densitometer is not the most appropriate technique for the determination of the densities of gases at low pressure (i.e. low mass in the VTD) [33]. The elevated uncertainty of density at low pressure is propagated to compressibility factor calculations (Figure 8).

The volumetric behaviour of the CH₄ + H₂S binary mixture at low pressure has been studied with the virial expansion truncated after the second coefficient. A virial equation provides a simple way to describe thermodynamic properties, and the virial coefficients can be determined by different experimental methods or correlations [34]. The form for our virial expansion is given by:

$$Z = 1 + \rho B(T, x_1) \quad (12)$$

where B is the second virial coefficient which is calculated as a function of temperature and mol fraction of methane (x_1) as:

$$B(T, x_1) = a + \frac{b}{T} + \frac{c}{T^3} + dx_1 \quad (13)$$

where a , b , c and d are the parameters reported in Table 17. These parameters have been correlated using our density measurements and the low pressure ρ - PTx data sets from the literature [8] [10]. The correlated virial equation of state has an AAD of 1.5% with a maximum deviation of 5.7% in a wide range of compositions, pressures up to 1.9 MPa and temperatures between 253 and 500 K (Figure 9). Several isotherms calculated with our CH₄+H₂S virial equation of state are illustrated in Figure 10.

5. Conclusion

Density data measurements for the three binary mixtures of methane with 0.1315, 0.1803 and 0.286 mol fraction of hydrogen sulphide were performed at three temperatures between 253 and 293 K and pressures up to 30 MPa by using a vibrating tube Anton Paar densitometer. The average uncertainty of the measurements at the 95% confidence level is 0.5%, reporting the highest average uncertainty of 8.3% at low pressures (below 0.5 MPa).

The measured experimental data were compared with the densities predicted with the PR, SAFT-VR Mie and GERG-2008 equations of state. For these measurements the SAFT-VR Mie EoS has the lowest absolute average deviation (2.5%) among the three investigated models. However deviations for all models are of the same order (3.4 % for the GERG EoS and for 3.0 % the PR EoS without volume correction 3.0%). However, the GERG-2008 is slightly superior to describe the density of the 0.1315 mol fraction of H₂S system (AAD=2.8%) than the SAFT-VR Mie (AAD=3.0%) and PR (AAD=2.9%) EoSs.

Furthermore, the literature data have been studied with the different models. When compared against the full density dataset, the lowest deviations are observed for the SAFT-VR Mie (4.3 %). The deviations with GERG-2008, PR, PR-Peneloux EoSs were 4.6, 7.8 and 5.4 %, respectively. Significant improvement in density predictions are observed when volume correction are used with the PR-EoS, due to the overestimated densities predicted by the PR EoS at pressures over 30MPa.

Finally, the measured densities and the ρ - PTx data from the literature at low pressure were used to correlate the second virial coefficient as a function of temperature and CH₄ mol fraction. The absolute average deviation of the compressibility factor calculated from our virial EoS in a wide range of compositions and at pressures up to 1.9 MPa and temperatures between 253 and 500 K is 1.5% with a maximum deviation of 5.7%.

Appendix A. Uncertainty in density measurements and compressibility factors

Density uncertainty was evaluated as combined standard uncertainty [18] [20]. Density measurement uncertainty can be expressed through the combination of two sources of expanded standard uncertainty, calibration and densitometer information, due to the mathematical relation used to do the calibration:

$$\rho = a\tau + b \quad (\text{A1})$$

Therefore, applying the law of propagation of uncertainty [20], density uncertainty was obtained by:

$$u(\rho) = \sqrt{\left(\frac{\partial\rho}{\partial\tau}\right)_{a,b}^2 u(\tau)^2 + \left(\frac{\partial\rho}{\partial a}\right)_{\tau,b}^2 u(a)^2 + \left(\frac{\partial\rho}{\partial b}\right)_{\tau,a}^2 u(b)^2}, \quad (\text{A2})$$

where τ is the time of oscillation and both 'a' and 'b' are the calibration parameters. Subsequently, the partial derivatives required for calculating $u(\rho)$ are derived from equation A1 as:

$$\left(\frac{\partial \rho}{\partial \tau}\right)_{a,b} = a \quad \left(\frac{\partial \rho}{\partial a}\right)_{\tau,b} = \tau \quad \left(\frac{\partial \rho}{\partial b}\right)_{a,\tau} = 1 \quad (\text{A3})$$

Finally, the combined standard uncertainty of our density measurements can be expressed by

$$u(\rho) = \sqrt{a^2 u(\tau)^2 + \tau^2 u(a)^2 + u(b)^2} \quad (\text{A4})$$

$u(a)$ and $u(b)$ are the standard deviations calculated after linear regression between reference fluid density values and measured period of vibration at the corresponding temperature of calibration. The calculation of the compressibility factor (Z) is function of the 3 properties measured: temperature, pressure and density. The compressibility factor can be formulated as

$$Z = \frac{P}{\rho RT} \quad (\text{A5})$$

Consequently, uncertainty in compressibility factor calculation, $u(Z)$, gives an idea of the overall uncertainty of our experimental data due to the consideration of the uncertainties of every measurement. Thus, following the same approach for the propagation of the uncertainty, the uncertainties of the compressibility factors were calculated using the law of propagation as:

$$u(Z) = \sqrt{\left(\frac{\partial Z}{\partial P}\right)_{\rho,T}^2 u(P)^2 + \left(\frac{\partial Z}{\partial \rho}\right)_{P,T}^2 u(\rho)^2 + \left(\frac{\partial Z}{\partial T}\right)_{P,\rho}^2 u(T)^2} \quad (\text{A6})$$

where the partial derivatives are obtained from deriving the equation A5 as follows:

$$\left(\frac{\partial Z}{\partial P}\right)_{\rho,T} = \frac{1}{\rho RT} \quad \left(\frac{\partial Z}{\partial \rho}\right)_{P,T} = -\frac{P}{\rho^2 RT} \quad \left(\frac{\partial Z}{\partial T}\right)_{\rho,P} = -\frac{P}{\rho RT^2} \quad (\text{A7})$$

Table 1 - Available experimental ρ - PTx data in the literature with their uncertainties for the methane and hydrogen sulphide system.

Reference	Year	No of Data	H ₂ S mol fraction		Pressure		Temperature		Density	
			Range (%)	$u(x_{H_2S})$ (%)	Range (MPa)	$u(P)$ (MPa)	Range (K)	$u(T)$ (K)	Range (kg·m ⁻³)	$u(\rho)$ (%)
Reamer et al. [8]	1951	1140	10-90	0.3	1-69	0.001	277-411	0.01	1-69	0.5
Bailey et al. [10]	1987	80	50.7	0.01	0.2-38	0.003	299-501	0.01	1-230	1

Table 2 - Details of the chemicals, suppliers and purities of the components used in this study.

Chemical Name	Source	Initial Purity ^a	Certification	Analysis Method ^b
Hydrogen sulphide	Air Liquide	0.995 vol	Air Liquide Certified	SM
Methane	Air Liquide	0.99995 vol	Air Liquide Certified	SM

^a No additional purification is carried out.

^b SM: Supplier method

Table 3 - Critical parameters, acentric factors and volume correction parameters for methane and hydrogen sulphide.

Compound	T_c/K	P_c/MPa	ω	$V_c^C/m^3 \cdot m^{-1}$
CH ₄	190.58	4.604	0.01083	-5.02
H ₂ S	373.20	8.963	0.081	-4.02

Table 4 –Mie molecular parameters for pure methane and hydrogen sulphide, and average absolute deviation (%AAD)from pure experimental data [32] for the vapour pressure (P_{sat}), the saturated-liquid density (ρ_{sat}) and the enthalpy of vaporization (ΔH_v).

Compound	m_s	$\sigma/\text{\AA}$	$(\varepsilon/k)/\text{K}$	λ_r	λ_a	AAD (%)		
						P_{sat}	ρ_{sat}	ΔH_v
H₂S (this work)	1	3.7783	387.28	22.451	6	2.2	0.4	3.7
CH₄ [12]	1	3.7412	153.36	12.650	6	0.7	0.8	2.9

Table 5 - Regressed k_{ij} values for PR and SAFT-VR Mie EoSs and their absolute average deviations (%AAD) in bubble point pressure and vapour phase composition calculations for the methane + hydrogen sulphide binary system.

	k_{ij}	%AAD P^{bubble}	%AAD y_1
PR	0.0807	4.4	1.9
SAFT-VR Mie	0.0314	4.8	2.0

Table 8 – Experimental results of the 0.8685 mole CH₄ + 0.1315 mole H₂S system at 293K, $u(x_{H_2S})= 0.0006$, $u(T)= 0.03$ K, $u(P)= 0.003$ MPa for pressures up to 5 MPa and $u(P)= 0.005$ MPa for pressures from 5 to 30 MPa.

No	T	P	ρ	$u(\rho)$		Z	u(Z)	No	T	P	ρ	$u(\rho)$		Z	u(Z)
				$\left[\frac{kg}{m^3}\right]$	$\left[\frac{kg}{m^3}\right]$							%	$\left[\frac{kg}{m^3}\right]$		
	[K]	[MPa]					10^{-2}		[K]	[MPa]					10^{-2}
1	293.18	0.239	1.86	0.18	9.5	0.97	9.2	31	293.19	13.230	140.02	0.71	0.5	0.71	0.4
2	293.18	0.469	3.71	0.19	5.3	0.96	5.0	32	293.18	13.726	145.96	0.74	0.5	0.71	0.4
3	293.19	0.792	6.46	0.22	3.4	0.93	3.2	33	293.20	14.242	152.42	0.76	0.5	0.71	0.4
4	293.21	1.117	9.20	0.24	2.7	0.92	2.4	34	293.20	14.579	156.48	0.78	0.5	0.70	0.4
5	293.19	1.341	11.22	0.26	2.3	0.90	2.1	35	293.20	14.924	160.62	0.81	0.5	0.70	0.4
6	293.20	1.820	15.41	0.29	1.9	0.89	1.7	36	293.20	15.365	165.51	0.83	0.5	0.70	0.4
7	293.19	2.300	20.14	0.32	1.6	0.86	1.4	37	293.20	15.806	170.31	0.86	0.5	0.70	0.4
8	293.18	2.890	25.81	0.36	1.4	0.85	1.2	38	293.19	16.228	174.96	0.89	0.5	0.70	0.4
9	293.19	3.396	30.35	0.38	1.3	0.85	1.1	39	293.19	16.699	180.07	0.92	0.5	0.70	0.4
10	293.19	3.988	35.82	0.41	1.1	0.84	1.0	40	293.20	17.183	185.14	0.95	0.5	0.70	0.4
11	293.19	4.428	40.25	0.42	1.0	0.83	0.9	41	293.19	17.682	190.29	0.98	0.5	0.70	0.4
12	293.20	4.887	44.78	0.44	1.0	0.82	0.8	42	293.20	18.163	195.16	1.01	0.5	0.70	0.4
13	293.20	5.494	50.99	0.45	0.9	0.81	0.7	43	293.23	18.686	200.27	0.99	0.5	0.71	0.3
14	293.20	5.964	55.59	0.46	0.8	0.81	0.7	44	293.29	19.219	205.31	0.87	0.4	0.71	0.3
15	293.20	6.411	60.21	0.46	0.8	0.80	0.6	45	293.23	19.770	210.30	0.73	0.3	0.71	0.2
16	293.19	6.909	65.40	0.47	0.7	0.80	0.6	46	293.22	20.355	215.54	0.58	0.3	0.71	0.2
17	293.19	7.335	70.05	0.48	0.7	0.79	0.5	47	293.20	20.932	220.42	0.43	0.2	0.72	0.1
18	293.19	7.786	74.96	0.49	0.7	0.79	0.5	48	293.20	21.495	224.99	0.39	0.2	0.72	0.1
19	293.18	8.263	79.99	0.50	0.6	0.78	0.5	49	293.23	22.173	230.34	0.37	0.2	0.73	0.1
20	293.18	8.722	85.68	0.51	0.6	0.77	0.5	50	293.23	22.860	235.56	0.34	0.1	0.73	0.1
21	293.19	9.097	90.09	0.53	0.6	0.76	0.4	51	293.21	23.505	240.20	0.32	0.1	0.74	0.1
22	293.19	9.534	95.16	0.54	0.6	0.76	0.4	52	293.22	24.254	245.19	0.30	0.1	0.75	0.1
23	293.18	9.972	100.39	0.56	0.6	0.75	0.4	53	293.22	25.052	250.52	0.28	0.1	0.76	0.1
24	293.19	10.368	105.20	0.57	0.5	0.74	0.4	54	293.21	25.865	255.77	0.26	0.1	0.76	0.1
25	293.19	10.794	110.28	0.59	0.5	0.74	0.4	55	293.21	26.669	260.49	0.24	0.1	0.77	0.1
26	293.19	11.183	115.06	0.61	0.5	0.73	0.4	56	293.20	27.629	265.96	0.22	0.1	0.79	0.1
27	293.19	11.608	120.16	0.63	0.5	0.73	0.4	57	293.20	28.496	270.59	0.21	0.1	0.80	0.1
28	293.18	12.003	124.94	0.65	0.5	0.73	0.4	58	293.21	29.415	275.27	0.20	0.1	0.81	0.1
29	293.18	12.415	130.08	0.67	0.5	0.72	0.4	59	293.21	29.995	278.16	0.20	0.1	0.81	0.1
30	293.18	12.830	135.13	0.69	0.5	0.72	0.4	60	293.21	30.419	280.17	0.19	0.1	0.82	0.1

Table 9 – Experimental results of 0.8197 mole CH₄ + 0.1803 mole H₂S system at 253K, $u(x_{H_2S})= 0.0008$, $u(T)= 0.03$ K, $u(P)= 0.003$ MPa for pressures up to 5 MPa and $u(P)= 0.005$ MPa for pressures from 5 to 30 MPa.

No	T [K]	P [MPa]	ρ $\left[\frac{kg}{m^3}\right]$	$u(\rho)$		Z	$u(Z)$ 10^{-2}	No	T [K]	P [MPa]	ρ $\left[\frac{kg}{m^3}\right]$	$u(\rho)$		Z	$u(Z)$ 10^{-2}
				$\left[\frac{kg}{m^3}\right]$	%							$\left[\frac{kg}{m^3}\right]$	%		
1	253.03	0.225	2.10	0.18	8.7	0.98	8.6	31	252.98	16.314	285.18	1.32	0.5	0.53	0.2
2	253.05	0.472	4.43	0.22	4.9	0.97	4.8	32	252.99	16.702	288.37	1.32	0.5	0.53	0.2
3	253.07	1.105	10.58	0.31	2.9	0.96	2.8	33	253.01	17.275	293.02	1.24	0.4	0.54	0.2
4	253.08	1.496	14.53	0.36	2.5	0.94	2.4	34	253.02	17.701	296.11	1.19	0.4	0.55	0.2
5	253.08	2.006	20.39	0.43	2.1	0.90	1.9	35	253.03	18.070	299.00	1.15	0.4	0.55	0.2
6	253.25	2.607	28.21	0.50	1.8	0.85	1.5	36	253.02	18.537	302.29	1.10	0.4	0.56	0.2
7	253.21	2.947	32.50	0.51	1.6	0.83	1.3	37	253.02	19.009	305.49	1.04	0.3	0.57	0.2
8	253.16	3.517	38.95	0.52	1.3	0.83	1.1	38	253.02	19.564	309.06	0.99	0.3	0.58	0.2
9	253.19	4.054	46.42	0.54	1.2	0.80	0.9	39	253.01	20.084	312.27	0.93	0.3	0.59	0.2
10	253.18	4.507	52.31	0.55	1.1	0.79	0.8	40	253.01	20.574	315.19	0.89	0.3	0.60	0.2
11	253.12	4.809	59.33	0.56	0.9	0.74	0.7	41	253.00	21.010	317.91	0.85	0.3	0.61	0.2
12	253.13	5.304	67.27	0.58	0.9	0.72	0.6	42	253.00	21.473	320.52	0.81	0.3	0.61	0.2
13	252.91	9.089	146.00	0.75	0.5	0.57	0.3	43	253.00	21.973	323.20	0.77	0.2	0.62	0.1
14	252.91	9.296	153.90	0.77	0.5	0.55	0.3	44	253.00	22.531	326.01	0.73	0.2	0.63	0.1
15	252.91	9.508	162.60	0.78	0.5	0.54	0.3	45	253.00	22.822	327.46	0.71	0.2	0.64	0.1
16	252.91	9.727	172.12	0.79	0.5	0.52	0.2	46	253.00	23.125	329.05	0.69	0.2	0.64	0.1
17	252.90	9.948	181.75	0.81	0.4	0.50	0.2	47	253.01	23.774	332.07	0.64	0.2	0.66	0.1
18	252.90	10.181	191.68	0.82	0.4	0.49	0.2	48	253.01	24.145	333.77	0.62	0.2	0.66	0.1
19	252.90	10.440	200.58	0.84	0.4	0.48	0.2	49	253.02	24.553	335.64	0.60	0.2	0.67	0.1
20	252.89	10.727	209.51	0.86	0.4	0.47	0.2	50	253.02	25.031	337.77	0.58	0.2	0.68	0.1
21	252.89	11.063	217.25	0.88	0.4	0.47	0.2	51	253.03	25.582	340.15	0.55	0.2	0.69	0.1
22	252.89	11.429	224.63	0.91	0.4	0.47	0.2	52	253.04	26.249	342.94	0.52	0.2	0.70	0.1
23	252.90	11.825	231.88	0.93	0.4	0.47	0.2	53	253.07	26.760	345.19	0.51	0.1	0.71	0.1
24	252.90	12.251	239.02	0.97	0.4	0.47	0.2	54	253.07	27.152	346.63	0.50	0.1	0.72	0.1
25	252.91	12.717	246.10	1.00	0.4	0.47	0.2	55	253.06	27.510	348.27	0.49	0.1	0.72	0.1
26	252.92	13.223	253.09	1.04	0.4	0.48	0.2	56	253.07	28.062	350.41	0.48	0.1	0.73	0.1
27	252.92	13.782	260.02	1.09	0.4	0.49	0.2	57	253.08	28.543	352.25	0.47	0.1	0.74	0.1
28	252.94	14.392	266.89	1.14	0.4	0.50	0.2	58	253.08	28.966	353.85	0.46	0.1	0.75	0.1
29	252.95	15.070	273.89	1.20	0.4	0.51	0.2	59	253.08	29.496	355.79	0.46	0.1	0.76	0.1
30	252.97	15.829	280.91	1.28	0.5	0.52	0.2	60	253.08	30.039	357.73	0.46	0.1	0.77	0.1

Table 12 – Experimental results of the 0.714 mole CH₄ + 0.286 mole H₂S system at 253K, $u(x_{H_2S})= 0.0011$, $u(T)= 0.03$ K, $u(P)= 0.003$ MPa for pressures up to 5 MPa and $u(P)= 0.005$ MPa for pressures from 5 to 30 MPa.

No	T	P	ρ	$u(\rho)$		Z	u(Z)	No	T	P	ρ	$u(\rho)$		Z	u(Z)
				$\left[\frac{kg}{m^3}\right]$	$\left[\frac{kg}{m^3}\right]$							%	$\left[\frac{kg}{m^3}\right]$		
	[K]	[MPa]					10^{-2}		[K]	[MPa]					10^{-2}
1	252.96	0.508	5.18	0.23	4.4	0.99	4.3	21	253.11	20.550	389.58	0.89	0.2	0.53	0.1
2	252.94	1.010	10.45	0.30	2.9	0.97	2.7	22	253.10	21.049	391.70	0.85	0.2	0.54	0.1
3	252.95	1.513	16.11	0.37	2.3	0.95	2.2	23	253.15	21.583	393.97	0.80	0.2	0.55	0.1
4	253.00	2.008	22.87	0.43	1.9	0.88	1.7	24	253.17	22.039	395.89	0.76	0.2	0.56	0.1
5	253.02	2.407	28.16	0.48	1.7	0.86	1.5	25	253.15	22.523	397.90	0.73	0.2	0.57	0.1
6	253.27	13.000	342.99	1.03	0.3	0.38	0.2	26	253.09	23.043	399.91	0.69	0.2	0.58	0.1
7	253.23	13.535	348.43	1.07	0.3	0.39	0.2	27	253.07	23.585	402.01	0.66	0.2	0.59	0.1
8	253.17	14.005	352.44	1.11	0.3	0.40	0.2	28	253.09	24.033	403.73	0.63	0.2	0.60	0.1
9	253.25	14.514	356.43	1.15	0.3	0.41	0.2	29	253.12	24.495	405.58	0.60	0.1	0.61	0.1
10	253.16	15.038	360.04	1.20	0.3	0.42	0.2	30	253.14	25.004	407.49	0.58	0.1	0.62	0.1
11	253.22	15.498	363.19	1.25	0.3	0.43	0.2	31	253.11	25.528	409.34	0.55	0.1	0.63	0.1
12	253.14	16.004	366.38	1.29	0.4	0.44	0.3	32	253.09	25.963	410.91	0.54	0.1	0.64	0.1
13	253.21	16.513	369.43	1.34	0.4	0.45	0.3	33	253.06	26.459	412.74	0.52	0.1	0.65	0.1
14	253.18	17.054	372.46	1.27	0.3	0.46	0.2	34	253.05	26.980	414.51	0.50	0.1	0.66	0.1
15	253.13	17.511	374.95	1.22	0.3	0.47	0.2	35	253.07	27.494	416.29	0.49	0.1	0.67	0.1
16	253.19	18.047	377.75	1.15	0.3	0.48	0.2	36	253.10	28.034	418.14	0.48	0.1	0.68	0.1
17	253.16	18.491	380.05	1.10	0.3	0.49	0.2	37	253.13	28.568	420.00	0.47	0.1	0.69	0.1
18	253.12	19.058	382.70	1.04	0.3	0.50	0.2	38	253.16	29.087	421.82	0.46	0.1	0.69	0.1
19	253.15	19.521	384.91	0.99	0.3	0.51	0.2	39	253.16	29.450	423.08	0.46	0.1	0.70	0.1
20	253.16	20.070	387.42	0.94	0.2	0.52	0.1	40	253.16	30.025	425.02	0.46	0.1	0.71	0.1

Table 13 – Experimental results of the 0.714 mole CH₄ + 0.286 mole H₂S system at 273K, $u(x_{H_2S})= 0.0011$, $u(T)= 0.03$ K, $u(P)= 0.003$ MPa for pressures up to 5 MPa and $u(P)= 0.005$ MPa for pressures from 5 to 30 MPa.

No	T	P	ρ	$u(\rho)$		Z	u(Z)	No	T	P	ρ	$u(\rho)$		Z	u(Z)
				$\left[\frac{kg}{m^3}\right]$	$\left[\frac{kg}{m^3}\right]$							%	$\left[\frac{kg}{m^3}\right]$		
	[K]	[MPa]					10^{-2}		[K]	[MPa]					10^{-2}
1	272.97	0.448	4.32	0.22	5.1	0.97	5.0	25	273.10	18.931	331.97	1.16	0.3	0.53	0.2
2	272.98	0.925	9.10	0.25	2.7	0.95	2.5	26	273.16	19.608	336.94	0.94	0.3	0.54	0.2
3	272.99	1.499	15.62	0.29	1.8	0.89	1.6	27	273.23	20.100	340.42	0.81	0.2	0.55	0.1
4	272.98	1.959	21.08	0.32	1.5	0.86	1.4	28	273.20	20.623	344.02	0.69	0.2	0.56	0.1
5	272.99	2.470	27.39	0.35	1.3	0.84	1.2	29	273.19	21.199	347.78	0.57	0.2	0.57	0.1
6	273.07	2.991	34.29	0.38	1.1	0.81	1.0	30	273.21	21.506	349.84	0.52	0.1	0.57	0.1
7	273.06	3.515	41.26	0.41	1.0	0.80	0.9	31	273.14	21.825	351.99	0.47	0.1	0.58	0.1
8	273.02	4.006	49.21	0.43	0.9	0.76	0.7	32	273.16	22.152	354.18	0.42	0.1	0.58	0.1
9	273.02	4.495	57.70	0.45	0.8	0.73	0.6	33	273.16	22.483	356.27	0.38	0.1	0.59	0.1
10	273.00	5.009	66.37	0.46	0.7	0.71	0.6	34	273.18	22.828	358.14	0.37	0.1	0.60	0.1
11	273.03	5.418	73.50	0.47	0.6	0.69	0.5	35	273.20	23.590	362.19	0.34	0.1	0.61	0.1
12	273.01	12.511	252.68	0.73	0.3	0.46	0.2	36	273.37	24.085	364.70	0.32	0.1	0.62	0.1
13	273.00	13.055	265.48	0.76	0.3	0.46	0.2	37	273.25	24.591	367.01	0.31	0.1	0.63	0.1
14	273.00	13.551	273.70	0.79	0.3	0.46	0.2	38	273.19	24.981	368.95	0.30	0.1	0.63	0.1
15	273.00	14.019	280.64	0.82	0.3	0.47	0.2	39	273.23	25.533	371.48	0.28	0.1	0.64	0.1
16	273.00	14.532	287.50	0.85	0.3	0.47	0.2	40	273.25	26.031	373.67	0.27	0.1	0.65	0.1
17	273.01	14.977	293.17	0.88	0.3	0.48	0.2	41	273.22	26.410	375.25	0.26	0.1	0.66	0.1
18	273.00	15.457	298.99	0.91	0.3	0.48	0.2	42	273.24	27.020	377.85	0.25	0.1	0.67	0.1
19	272.99	15.974	304.94	0.95	0.3	0.49	0.2	43	273.05	27.474	379.67	0.24	0.1	0.68	0.1
20	272.99	16.531	310.78	0.98	0.3	0.50	0.2	44	273.06	27.956	381.54	0.23	0.1	0.68	0.1
21	273.03	16.977	315.19	1.02	0.3	0.50	0.2	45	273.10	28.471	383.53	0.23	0.1	0.69	0.1
22	273.08	17.450	319.61	1.05	0.3	0.51	0.2	46	273.05	29.015	385.58	0.22	0.1	0.70	0.1
23	273.11	17.956	324.07	1.09	0.3	0.52	0.2	47	273.03	29.571	387.72	0.21	0.1	0.71	0.1
24	273.09	18.521	328.70	1.13	0.3	0.53	0.2	48	273.03	30.070	389.49	0.21	0.1	0.72	0.1

Table 14 – Experimental results of the 0.714 mole CH₄ + 0.286 mole H₂S system at 293K, $u(x_{H_2S})= 0.0011$, $u(T)= 0.03$ K, $u(P)= 0.003$ MPa for pressures up to 5 MPa and $u(P)= 0.005$ MPa for pressures from 5 to 30 MPa.

No	T	P	ρ	$u(\rho)$			Z	$u(Z)$	No	T	P	ρ	$u(\rho)$			Z	$u(Z)$
				$\left[\frac{kg}{m^3}\right]$	$\left[\frac{kg}{m^3}\right]$	%							$\left[\frac{kg}{m^3}\right]$	$\left[\frac{kg}{m^3}\right]$	%		
	[K]	[MPa]					10^{-2}		[K]	[MPa]						10^{-2}	
1	293.27	0.227	1.99	0.19	9.5	0.99	9.3	34	293.30	15.503	239.94	0.84	0.4	0.56	0.3		
2	293.27	0.560	4.92	0.21	4.3	0.99	4.2	35	293.31	16.108	249.28	0.88	0.4	0.56	0.3		
3	293.28	1.101	9.72	0.25	2.6	0.98	2.5	36	293.34	16.524	253.44	0.91	0.4	0.57	0.3		
4	293.28	1.547	14.1	0.29	2.1	0.95	2.0	37	293.34	17.035	260.09	0.94	0.4	0.57	0.3		
5	293.28	2.065	19.16	0.31	1.6	0.94	1.5	38	293.35	17.740	267.95	0.99	0.4	0.57	0.3		
6	293.30	2.511	23.63	0.34	1.4	0.92	1.2	39	293.33	18.012	271.26	1.00	0.4	0.58	0.3		
7	293.29	2.976	28.53	0.37	1.3	0.91	1.1	40	293.33	18.543	276.99	1.02	0.4	0.58	0.3		
8	293.29	3.489	33.95	0.40	1.2	0.89	1.0	41	293.33	19.012	281.75	0.92	0.3	0.59	0.2		
9	293.42	3.851	38.01	0.41	1.1	0.88	1.0	42	293.33	19.476	286.23	0.80	0.3	0.59	0.2		
10	293.43	4.386	46.59	0.42	0.9	0.82	0.8	43	293.34	20.081	291.58	0.65	0.2	0.60	0.1		
11	293.44	4.823	51.27	0.43	0.8	0.82	0.7	44	293.34	20.504	295.67	0.54	0.2	0.60	0.1		
12	293.39	5.407	58.83	0.45	0.8	0.80	0.7	45	293.31	21.026	300.53	0.41	0.1	0.61	0.1		
13	293.32	5.943	66.82	0.46	0.7	0.77	0.6	46	293.33	21.863	306.80	0.38	0.1	0.62	0.1		
14	293.33	6.464	75.29	0.46	0.6	0.75	0.4	47	293.32	22.053	308.34	0.37	0.1	0.62	0.1		
15	293.31	6.885	80.49	0.47	0.6	0.74	0.4	48	293.31	22.118	308.67	0.37	0.1	0.62	0.1		
16	293.27	7.261	85.92	0.48	0.6	0.74	0.4	49	293.31	22.512	311.24	0.36	0.1	0.63	0.1		
17	293.27	7.749	94.83	0.49	0.5	0.71	0.4	50	293.30	22.979	314.55	0.34	0.1	0.64	0.1		
18	293.28	8.092	103.64	0.50	0.5	0.68	0.4	51	293.30	23.460	317.83	0.32	0.1	0.64	0.1		
19	293.29	8.523	108.80	0.51	0.5	0.68	0.4	52	293.31	23.712	319.93	0.32	0.1	0.64	0.1		
20	293.30	9.149	119.96	0.53	0.4	0.66	0.3	53	293.29	23.988	321.16	0.31	0.1	0.65	0.1		
21	293.30	9.741	129.36	0.55	0.4	0.66	0.3	54	293.30	24.512	324.48	0.29	0.1	0.66	0.1		
22	293.33	10.169	136.99	0.57	0.4	0.65	0.3	55	293.29	25.012	327.50	0.28	0.1	0.66	0.1		
23	293.29	10.516	145.41	0.58	0.4	0.63	0.3	56	293.30	25.515	330.43	0.27	0.1	0.67	0.1		
24	293.29	11.236	161.66	0.61	0.4	0.60	0.3	57	293.30	25.988	333.07	0.26	0.1	0.68	0.1		
25	293.30	11.789	174.33	0.64	0.4	0.59	0.3	58	293.31	26.506	335.86	0.24	0.1	0.69	0.1		
26	293.32	12.220	183.56	0.66	0.4	0.58	0.3	59	293.33	26.879	337.31	0.24	0.1	0.69	0.1		
27	293.32	12.521	189.88	0.67	0.4	0.57	0.3	60	293.64	27.145	339.08	0.23	0.1	0.70	0.1		
28	293.31	12.964	198.31	0.69	0.4	0.57	0.3	61	293.53	27.520	340.85	0.23	0.1	0.70	0.1		
29	293.30	13.528	208.17	0.72	0.3	0.57	0.2	62	293.43	28.085	343.33	0.22	0.1	0.71	0.1		
30	293.29	13.780	213.21	0.74	0.3	0.56	0.2	63	293.42	28.586	345.52	0.21	0.1	0.72	0.1		
31	293.30	14.426	223.09	0.78	0.3	0.56	0.2	64	293.40	29.019	347.54	0.21	0.1	0.73	0.1		
32	293.31	14.523	224.65	0.78	0.3	0.56	0.2	65	293.33	29.517	349.82	0.20	0.1	0.73	0.1		
33	293.30	15.049	233.30	0.81	0.3	0.56	0.2	66	293.33	29.998	352.02	0.20	0.1	0.74	0.1		

Table 15 - Absolute average deviations (%AAD) between the studied models and the densities measured in this work.

x_{H_2S}	T/K	SAFT-VR Mie	PR	GERG 2008
x=0.1315	253	3.3	4.8	2.1
	273	1.6	1.4	2.0
	293	3.9	2.2	4.3
	Total	3.0	2.9	2.8
x=0.1801	253	1.6	3.4	2.5
	273	1.5	2.0	2.6
	293	2.5	2.0	3.3
	Total	1.9	2.5	2.8
x=0.2860	253	1.8	4.1	4.6
	273	3.2	3.8	5.3
	293	3.1	3.1	4.8
	Total	2.8	3.6	4.9

Table 16 – Absolute average deviation (%AAD) between the available experimental data and the studied models.

Author	No Data	PR	PR+Peneloux	SAFT-VR Mie	GERG 2008
Bailey et al.	80	5.1	3.9	4.6	3.3
Reamer et al.	1140	10.2	5.5	5.0	5.3
This work	526	3.0	5.2	2.5	3.4
Total	1748	7.8	5.4	4.3	4.6

Table 17 – Regressed parameters for the calculation of the second virial coefficient B , condition ranges and AAD deviations between the correlation and experimental compressibility factors.

Parameters	a ($\text{m}^3\cdot\text{mol}^{-1}$)	b ($\text{m}^3\cdot\text{K}\cdot\text{mol}^{-1}$)	c ($\text{m}^3\cdot\text{K}^3\cdot\text{mol}^{-1}$)	d ($\text{m}^3\cdot\text{mol}^{-1}$)
	1.5385×10^{-4}	-6.6201×10^{-2}	-1.5017×10^2	9.1010×10^{-5}
Range	CH₄ mole fraction	Pressure (MPa)	Temperature (K)	
	0.1 - 0.9	0.17 – 1.88	253 - 500	
Deviation	%AAD		Max.Dev.	
	1.5%		5.7%	

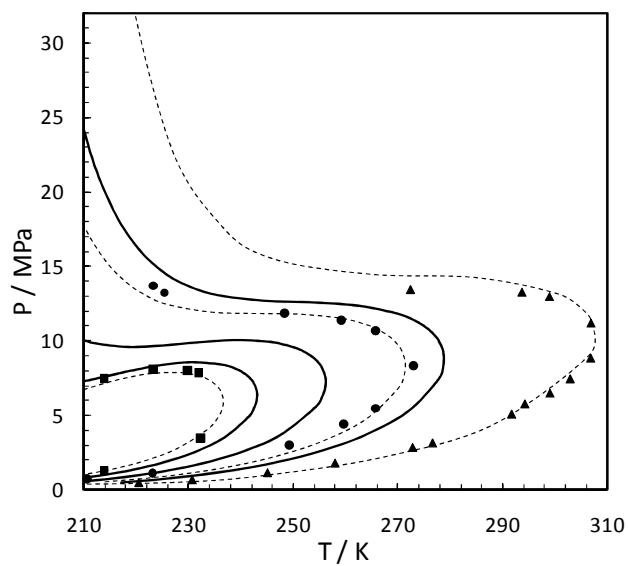


Figure 1. Predicted phases envelopes with the PR EoS of the methane + hydrogen sulphide system with 0.1101, 0.1315, 0.1803, 0.248, 0.286 and 0.458 mol fractions of H₂S. The solid lines are the compositions studied in this work and the dashe lines are other phase diagrams compared against Kohn and Kurata data [22]: (■) 0.1101, (●) 0.248 and (▲) 0.458 mol fractions of H₂S.

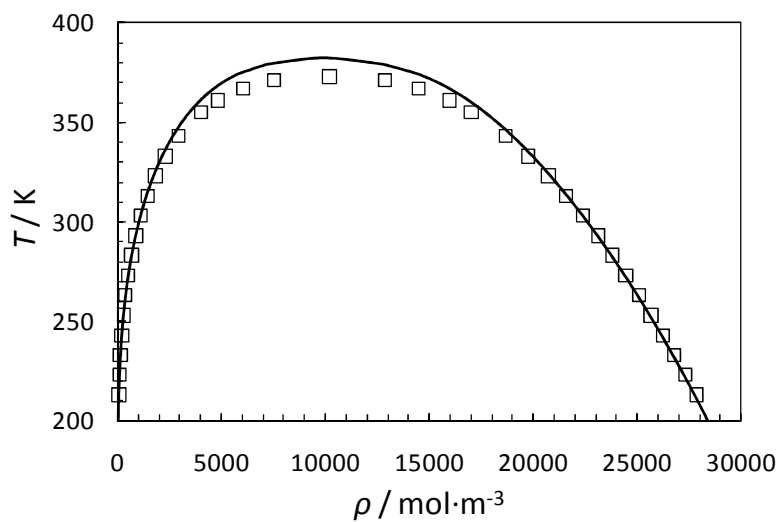


Figure 2. Temperature-density coexistence envelop for pure H_2S . Comparison between experimental data (\square) [32] and SAFT-VR Mie calculation.

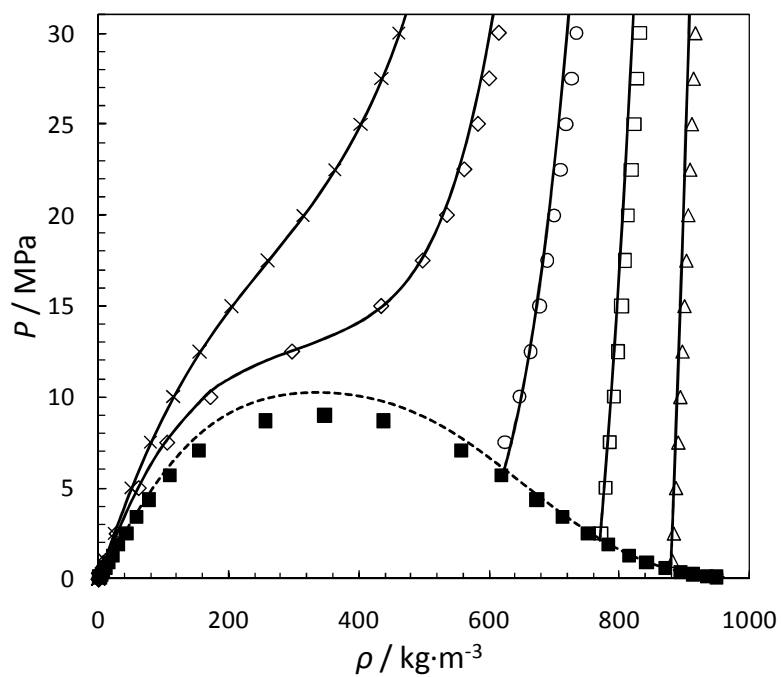


Figure 3. Predicted and experimental densities of pure H₂S. The solid lines are isotherms calculated with the SAFT-VR Mie and the dashed line is the calculated coexistence curve. The symbols denote experimental data: from the literature [32] at T=250K (Δ), T=300K (\square), T=350K (\circ), T=400K (\diamond) and T=450K (\times) and at saturation (\blacksquare).

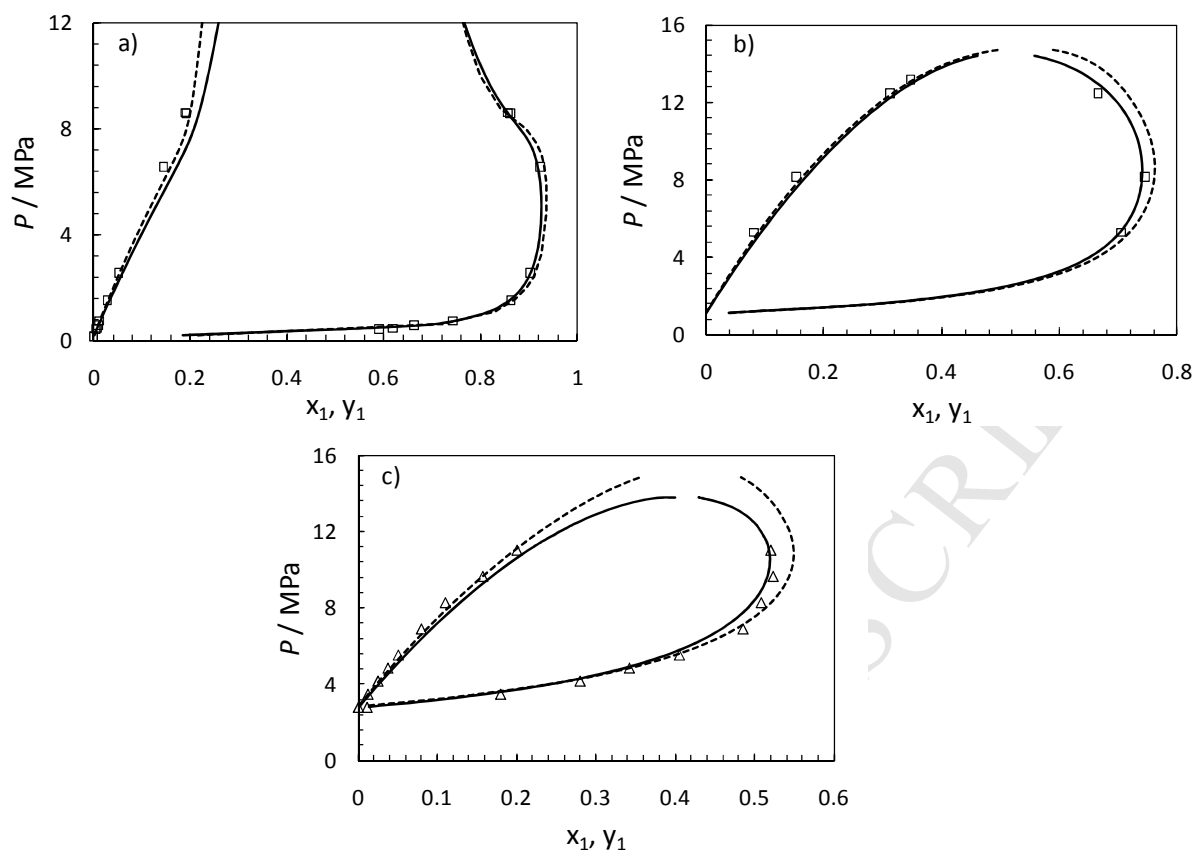


Figure 4. P-x diagrams of CH_4 (1) + H_2S (2) system at a) $T = 223.17\text{K}$, b) $T = 273.54\text{K}$ and c) $T = 310.93\text{K}$. Symbols: (\square) Coquelet et al. [7] and (\triangle) Kohn and Kurata [22]. Solid line: calculated bubble and dew lines using PR model with $k_{ij} = 0.0807$. Dashed line: calculated bubble and dew lines using SAFT-VR Mie EoS with $k_{ij} = 0.0314$.

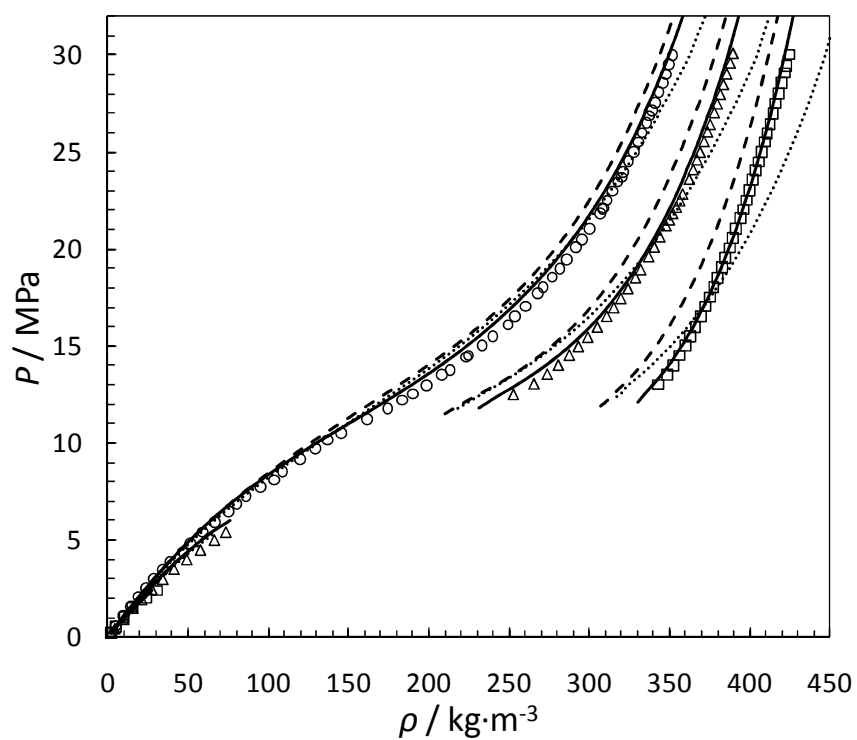


Figure 5. Experimental and predicted densities of the 0.714 mole CH_2 + 0.286 mole H_2S system. Experimental results: (\square) 253 K, (\circ) 273 K, (\triangle) 293 K. Lines: Predictions using the SAFT-VR Mie EoS. Dashed lines: Predictions using the GERG-2008 EoS. Dotted lines: Predictions using the PR EoS.

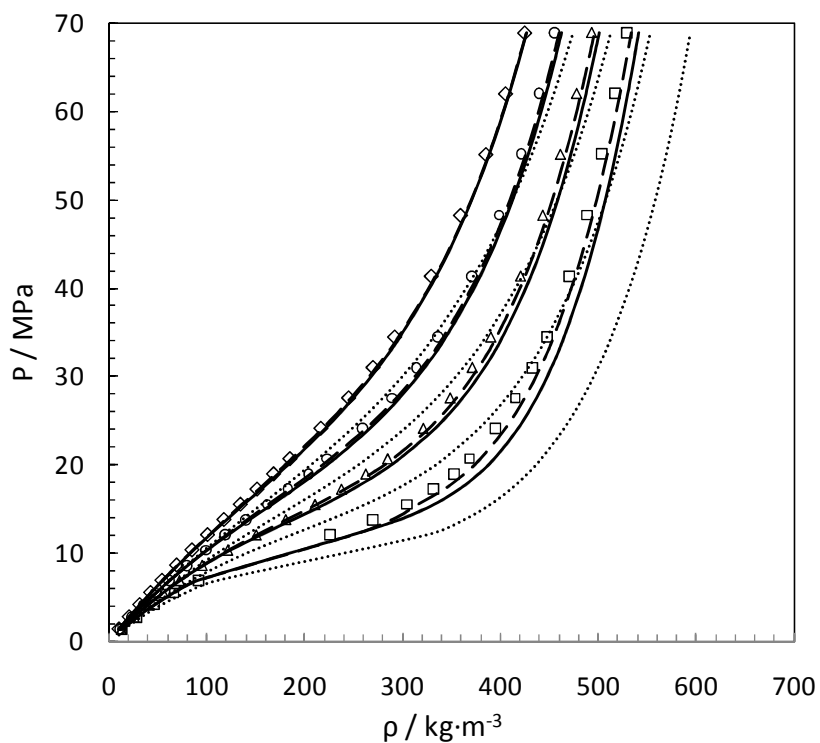


Figure 6. Experimental and predicted densities of the 0.5 mole CH_4 + 0.5 mole H_2S system. Experimental results: (\square) 311 K, (\triangle) 344 K, (\circ) 377 K and (\diamond) 411 K [8]. Lines: Predictions using the SAFT-VR Mie EoS. Dashed lines: Predictions using the GERG-2008 EoS. Dotted lines: Predictions using the PR+Peneloux EoS.

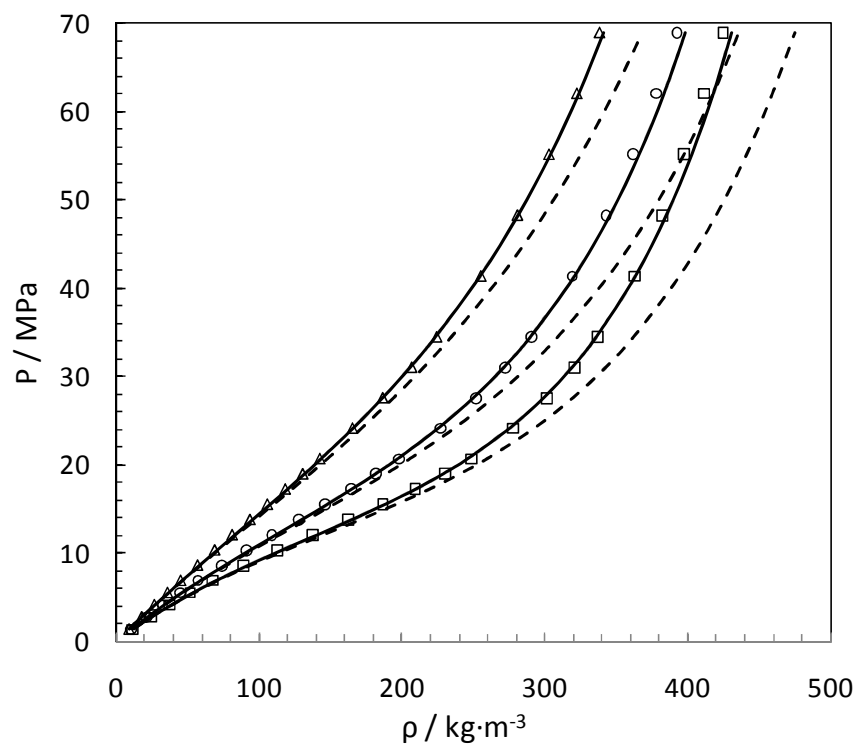


Figure 7. Experimental and predicted densities of the 0.7 mole CH_4 + 0.3 mole H_2S system. Comparison of PR+Peneloux (continuous curve), PR (dashes) and literature data at $T=311\text{K}$ (\square), $T=344\text{K}$ (\circ) and $T=411\text{K}$ (\triangle) [8].

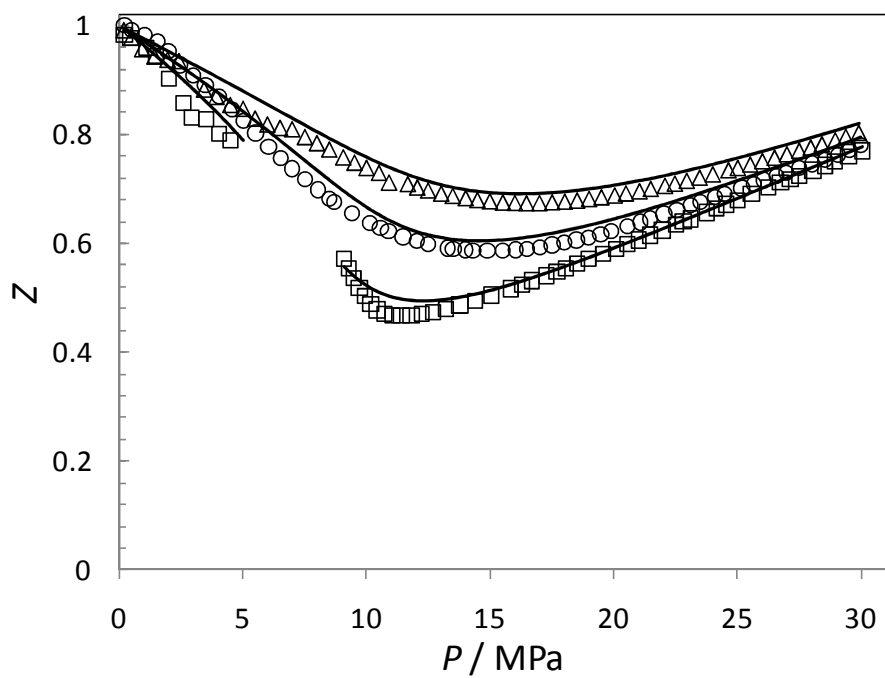


Figure 8. Compressibility factor of the 0.8197 mol CH₄ + 0.1803 mol H₂S system. Comparison between the SAFT-VR Mie calculation and experimental data measured in this work: T=253K (□), T=273K (○) and T=293K (△).

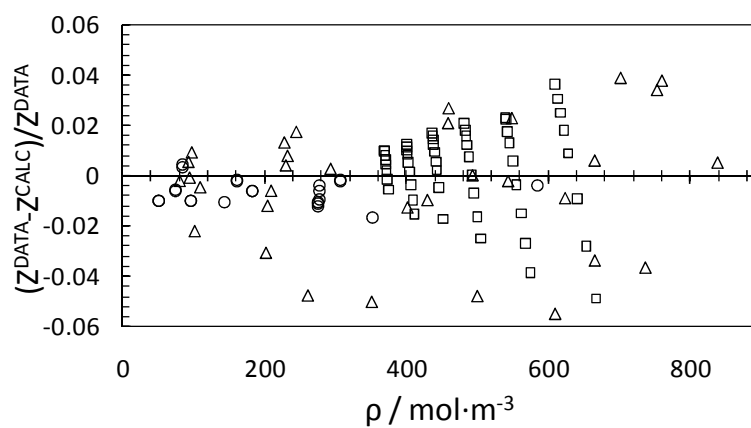


Figure 9. Deviations between this work (Δ), Reamer et al. data (\square) [8] and Bailey et al. data (\circ) [10] and predictions using low pressure virial EoS from

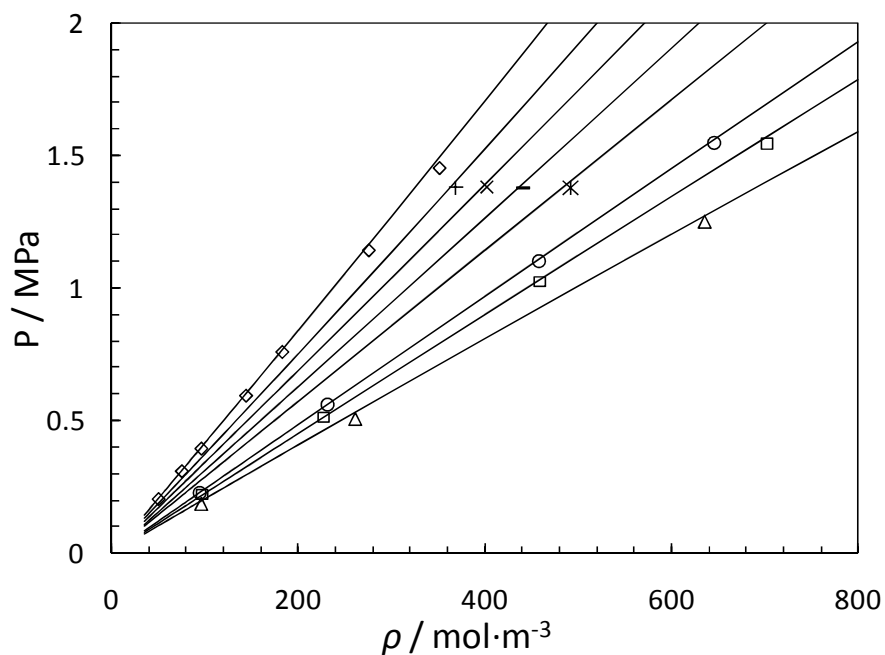


Figure 10. P - ρ diagram of several systems of $\text{H}_2\text{S} + \text{CH}_4$ at 8 isotherms. Comparison of predictions with low pressure virial EoS and experimental data: $T=253\text{K}$ and $x_{\text{CH}_4}=0.87$ (Δ), $T=273\text{K}$ and $x_{\text{CH}_4}=0.82$ (\square), $T=293\text{K}$ and $x_{\text{CH}_4}=0.71$ (\circ), $T=344\text{K}$ and $x_{\text{CH}_4}=0.4$ ($*$), $T=377\text{K}$ and $x_{\text{CH}_4}=0.5$ ($-$), $T=411\text{K}$ and $x_{\text{CH}_4}=0.6$ ($+$), $T=444\text{K}$ and $x_{\text{CH}_4}=0.8$ (\times) and $T=500\text{K}$ and $x_{\text{CH}_4}=0.5$ (\diamond) [8] [10].

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