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The muon g-2: retrospective and future

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Abstract. Soon, new experiments at FNAL and J-PARC will measure the muon anomalous magnetic moments with better accuracy than before. From theoretical side, the uncertainty of the standard model prediction is dominated by the hadronic contributions. Current status of the experimental data and theoretical calculations are briefly discussed.

1 Introduction

Cosmology tell us that about 95% of matter is not detected by modern measurements. We think that the dark matter surround us, however, we don't see it. There are two strategies to search for the physics beyond the standard matter: high energy and low energy experiments. In the first case, due to high energy we attempt to excite the heavy degrees of freedom. There are no firm evidences on the deviation of measured cross sections from the predictions of the standard model. In the case of the low energy experiments, it is possible to reach very high precision of the measured quantities because of huge statistics. And within this kind of experiments there are some rough redges of the standard model. The most famous deviation is observed for the muon anomalous magnetic moment and it remains stable for many years.

The anomalous magnetic moment (AMM) of charged leptons $(l = e, \mu, \tau)$ is defined as

$$a_l = \frac{g_l - 2}{2},\tag{1}$$

with the gyromagnetic ratio g_l of the lepton magnetic moment to its spin, in Bohr magneton units. The Dirac equation g = 2 predicts for a free point-like fermion with spin 1/2 and thus there is no anomaly at tree level (Fig. 1a). However, deviations appear when taking into account the interactions leading to fermion substructure and thus to nonzero a_l . In the standard model it appears from the radiative corrections to the tree fermion-photon vertex (Fig. 1) due to the coupling of the lepton spin to virtual fields, which in the SM are induced by QED, weak and strong (hadronic) interactions (Fig. 1)

$$a^{\rm SM} = a^{\rm QED} + a^{\rm weak} + a^{\rm hadr}.$$
 (2)

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Figure 1. Representative diagrams for the SM contributions to a_{μ} . Here, H is for the hadronic block.

2 The electron g - 2 and the fine coupling constant

The electron AMM was experimentally discovered by Kush and Foley from Columbia University, New York (USA) in 1947 [1, 2] with the result [3]

$$a_{e}^{\text{Columbia}} = 0.00118 \pm 0.00003. \tag{3}$$

This was immediately confirmed by Schwinger in the framework of quantum electrodynamics as a result of the radiative correction (Fig. 1b)

$$a_e^{\text{Schwinger}} = \frac{\alpha}{2\pi} = 0.001161. \tag{4}$$

Since that time, enormous progress has been reached in experiment and theory. The latest measurement by the Gabrielse' group from Harvard university (USA) provides the result with fantastic accuracy [4]

 $a_e^{\text{Harvard}} = 1\ 159\ 652\ 180.73\ (0.28) \times 10^{-12}$ [0.24 ppb]. (5)

Within the standard mode (1), the electron AMM is almost completely dominated by QED contribution calculated with 5-loop accuracy

$$a_l^{\text{QED}} = \sum_{n=1}^{5} C_{2n}^l (\frac{\alpha}{\pi})^n + \dots,$$
(6)

where the value of coefficients are given in Table 1.

The result (6) allows to determine the fine structure constant α with the extraordinary precision [6, 7]

 $\alpha^{-1}(a_e) = 137.035\ 999\ 1570\ (29)(27)(18)(331)$ [0.25 ppb], (7)

where the first two uncertainties are due to errors in $C_{8,10}^{l}$, the third one is uncertainty from hadronic and weak corrections, and the last one is due to experimental error in the measurement of $a_{e}^{Harvard}$.

Table 1. The coefficients in the QED contribution to the lepton AMM (6). The first three coefficients are known analytically. The errors in $C_{4,6}^{\mu}$ are due to the experimental uncertainties in m_{μ}/m_e ratio. The errors in $C_{8,10}^{l}$ are due to numerical simulations.

	l=e	l=μ	source
C_2^l	0.5	0.5	Schwinger[3]
$C_4^{\overline{l}}$	-0.328 478 444 00	0.765 857 425(17)	Laporta, Remiddi [5]
C_6^l	1.181 234 017	24.050 509 96(32)	Laporta, Remiddi [5]
C_8^{ℓ}	-1.912 06(84)	130.879 6(63)	Kinoshita, Nio, et.al. [6]
$C_{10}^{l^{\circ}}$	7.791(336)	753.29(1.04)	Kinoshita, Nio, et.al. [6]

This determination became possible after the complete QED contribution to the electron AMM up to tenth order in the coupling constant were achieved numerically by the Prof. T. Kinoshita group [6] (for recent review see [7]).

In 2010, the direct determination of the fine coupling constant became possible from measurement of the ratio \hbar/m_{Rb} [8]

$$\alpha^{-1}(Rb) = 137.035\ 999\ 049\ (90) \quad [0.66\ \text{ppb}].$$
 (8)

With this α , the the SM prediction for the electron AMM becomes

$$a_{\rho}^{\text{SM,Rb}} = 1\ 159\ 652\ 181.643\ (764) \times 10^{-12}$$
 [0.24 ppb]. (9)

Both determination of the electron AMM (5) and (9) are consistent within the errors.

$$a_e^{\exp} - a_e^{SM,Rb} = -0.91 \ (81) \times 10^{-12}.$$
 (10)

Thus the experimental and SM results for the electron AMM are in perfect agreement.

3 The muon *g* – 2: experiment vs standard model. Electroweak contributions.

In 2006, there were published the results obtained by the E821 collaboration at Brookhaven National Laboratory [9] on measurements of the muon $AMMa_u$

$$a_{\mu}^{\text{BNL}} = 116\ 592\ 08.0\ (6.3) \times 10^{-10} \quad [0.54\ \text{ppm}].$$
 (11)

Later on, this value was corrected [10, 11] for a small shift in the ratio of the magnetic moments of the muon and the proton as

$$a_{\mu}^{\text{BNL,CODATA}} = 116\ 592\ 09.1\ (6.3) \times 10^{-10}.$$
 (12)

It is well-known that the effect of the second-order contribution, due to exchange by the particle with mass M, to the AMM of the lepton with mass m_l is proportional to $a_l \propto (m_l/M)^2$. It means, that sensitivity for the muon to the interaction with scale M is by factor $m_{\mu}^2/m_e^2 \propto 40000$ higher than for the electron. This fact compensates a less experimental accuracy of the muon AMM measurements (11) relatively to the electron one (5), and make the study of the muon AMM more perspective in search for new physics.

Another exciting point is that soon the new data on the muon AMM will be available from experiments proposed at Fermilab (USA) [12] and J-PARC (Japan) [13]. These experiments plan to reduce the present experimental error by factor 4, to a precision of 0.14 ppm. In SM, the contributions to the muon AMM from QED (Fig. 1b) [14] and weak (Fig. 1c) [15, 16] interactions (Fig. 1c) are known with high accuracy

$$a_{\mu}^{\text{QED,Rb}} = 11\ 658\ 471.8951\ (0.0080) \times 10^{-10},$$
 (13)

$$a_{\mu}^{\text{QED},a_{e}} = 11\ 658\ 471.8846\ (0.0037) \times 10^{-10},$$
 (14)

$$a_{\mu}^{\text{weak}} = 15.36 \ (0.10) \times 10^{-10},$$
 (15)

The most important feature of new estimate for the weak sector, that significantly increases the theoretical precision, is to use precise Higgs-boson mass value measured at LHC. The remaining theory error comes from unknown three-loop contributions and dominantly from light hadronic uncertainties in the second-order electroweak diagrams with quark triangle loops. The accuracy of these calculations is enough for any planed experiments in new future.

Subtracting from the experimental result the well-defined contributions from QED and weak interactions one gets

$$a_{\mu}^{\text{BNL}} - a_{\mu}^{\text{QED,Rb}} - a_{\mu}^{\text{weak}} = 721.65 \ (6.38) \times 10^{-10},$$
 (16)

where the error is only due to the experiment. We can treat this number as an experimental result for the rest contributions, i.e. of the strong interaction of SM and of the hypothetical interactions beyond SM.

4 Hadronic contributions to the muon g - 2. Vacuum polarization effect.

Strong (hadronic) interaction produces relatively small contributions to a_{μ} , however they are known with an accuracy comparable to the experimental uncertainty in (11). In the leading in α orders, these contributions can be separated into three terms

$$a_{\mu}^{\text{hadr}} = a_{\mu}^{\text{HVP,LO}} + a_{\mu}^{\text{HVP,HO}} + a_{\mu}^{\text{HLbL}}.$$
 (17)

In (17), a_{μ}^{HVP} is the leading in α contribution due to the hadron vacuum polarization (HVP) effect in the internal photon propagator of the one-loop diagram (Fig. 1d), a_{μ}^{ho} is the next-to-leading order contribution related to iteration of HVP (Fig. 1e). The last term is not reduced to HVP iteration and it is due to the hadronic light-by-light (HLbL) scattering mechanism (Fig. 1g).

Hadronic contributions in (17) are determined by effects dominated by long distance dynamics, the region where the methods of perturbation theory of Quantum Chromodynamics (QCD) do not applicable and one must use less reliable nonperturbative approaches. However, in case of HVP, using analyticity and unitarity (the optical theorem) a_{μ}^{HVP} can be expressed as the spectral representation integral [17, 18]

$$a_{\mu}^{\rm HVP} = \frac{\alpha}{\pi} \int_{4m_{\pi}^2}^{\infty} \frac{dt}{t} K(t) \rho_{\rm V}^{\rm (H)}(t) \,, \tag{18}$$

which is a convolution of the hadronic spectral function

$$\rho_V^{(\rm H)}(t) = \frac{1}{\pi} \text{Im}\Pi^{(\rm H)}(t)$$
(19)

with the known from QED kinematical factor

$$K(t) = \int_0^1 dx \frac{x^2(1-x)}{x^2 + (1-x)t/m_{\mu}^2},$$
(20)

where m_{μ} is the muon mass. The QED factor is sharply peaked at low invariant masses t and decreases monotonically with increasing t. Thus, the integral defining a_{μ}^{HVP} is sensitive to the details of the spectral function $\rho_{V}^{(\text{H})}(t)$ at low t. At present there is no direct theoretical tools that allow to calculate the spectral function at low t with required accuracy. Fortunately, $\rho_{V}^{(\text{H})}(t)$ is related to the total $e^+e^- \rightarrow \gamma^* \rightarrow$ hadrons cross-section $\sigma(t)$ at center-of-mass energy squared t by

$$\sigma^{e^+e^- \to \text{hadrons}}(t) = \frac{4\pi\alpha}{t} \rho_{\text{V}}^{(\text{H})}(t), \qquad (21)$$

and this fact is used to get quite accurate estimate of a_{μ}^{HVP} . The most precise recent phenomenological evaluations of a_{μ}^{HVP} , using recent $e^+e^- \rightarrow$ hadrons data, provide the results

$$a_{\mu}^{\text{HVP,LO},e^+e^-} = \begin{cases} 692.3 \ (4.2) \times 10^{-10}, \quad [19]\\ 694.91 \ (4.27) \times 10^{-10}. \quad [20] \end{cases}$$
(22)

In addition, data on inclusive decays of the τ -lepton into hadrons are used to replace the e^+e^- data in certain energy regions. This is possible, since the vector current conservation law relates the I = 1 part of the electromagnetic spectral function to the charged current vector spectral function measured in $\tau \rightarrow \nu$ +non-strange hadrons (see, i.e. [21]). All these allows to reach during the last decade a substantial improvement in the accuracy of the contribution from the HVP.

Similar dispersion relation approach and the same phenomenological input lead to the estimate of the next-to-leading hadronic contribution (Fig. 1e) [20, 22]

$$a_{\mu}^{\text{HVP,NLO}} = -9.84 \ (0.07) \times 10^{-10},$$
 (23)

$$a_{\mu}^{\text{HVP,NNLO}} = 1.24 \ (0.01) \times 10^{-10}$$
 (24)

Thus, the HVP and next-to-leading order contribution related to HVP are known with an accuracy better than 1 per cent.

In near future it is expected that new and precise measurements from CMD3 and SND at VEPP-2000 in Novosibirsk, BES III in Beijing and KLOE-2 at DAFNE in Frascati allow to significantly increase accuracy of predictions for a_{μ}^{HVP} and a_{μ}^{ho} and resolve some inconsistency problems between different set of data.

Subtracting from the experimental result the contributions from electroweak interaction and hadronic vacuum effect one gets

$$a_{\mu}^{\text{BNL}} - a_{\mu}^{\text{QED,Rb}} - a_{\mu}^{\text{weak}} - a_{\mu}^{\text{HVP}} = 37.95 \ (7.64) \times 10^{-10},$$
 (25)

where one can treat this number as an experimental result for the rest contributions, i.e. of the strong interaction of due to the light-by-light mechanism and of the hypothetical interactions beyond SM.

5 Hadronic contributions to the muon *g* – 2. Light-by-light scattering mechanism.

The basic element for calculations of the hadronic LbL contribution to the muon AMM (Fig. 1g) is the fourth-rank light quark hadronic vacuum polarization tensor

$$\Pi_{\mu\nu\lambda\rho}(q_1, q_2, q_3) = \int d^4 x_1 \int d^4 x_2 \int d^4 x_3 e^{i(q_1x_1 + q_2x_2 + q_3x_3)} \times \langle 0|T(j_\mu(x_1)j_\nu(x_2)j_\lambda(x_3)j_\rho(0))|0\rangle,$$
(26)

where $j_{\mu}(x)$ are light quark electromagnetic currents and $|0\rangle$ is the QCD vacuum state.

The muon AMM can be extracted by using the projection [23]

$$a_{\mu}^{\text{LbL}} = \frac{1}{48m_{\mu}} \text{Tr}\left((\hat{p} + m_{\mu})[\gamma^{\rho}, \gamma^{\sigma}](\hat{p} + m_{\mu})\Pi_{\rho\sigma}(p, p)\right),$$

where

$$\Pi_{\rho\sigma}(p',p) = -ie^{6} \int \frac{d^{4}q_{1}}{(2\pi)^{4}} \int \frac{d^{4}q_{2}}{(2\pi)^{4}} \frac{1}{q_{1}^{2}q_{2}^{2}(q_{1}+q_{2}-k)^{2}} \times \\ \times \gamma^{\mu} \frac{\hat{p}' - \hat{q}_{1} + m_{\mu}}{(p'-q_{1})^{2} - m_{\mu}^{2}} \gamma^{\nu} \frac{\hat{p} - \hat{q}_{1} - \hat{q}_{2} + m_{\mu}}{(p-q_{1}-q_{2})^{2} - m_{\mu}^{2}} \gamma^{\lambda} \times \\ \times \frac{\partial}{\partial k^{\rho}} \Pi_{\mu\nu\lambda\sigma}(q_{1},q_{2},k-q_{1}-q_{2}),$$
(27)

 m_{μ} is the muon mass, $k_{\mu} = (p' - p)_{\mu}$ and it is necessary to consider the limit $k_{\mu} \rightarrow 0$.

In general, the HLbL scattering amplitude is a complicated object for calculations. It is a sum of different diagrams including the dynamical quark loop, the meson exchanges, the meson loops and the iterations of these processes. Fortunately, already in the first papers devoted to the calculation of the HLbL contributions [24–26], it has been recognized that these numerous terms show a hierarchy. This is related to existence of two small parameters: the inverse number of colors $1/N_c$ and the ratio of the characteristic internal momentum to the chiral symmetry parameter $m_{\mu}/(4\pi f_{\pi}) \sim 0.1$. The former suppresses the multiloop contributions, so that the leading contribution is due to the quark loop diagram and the two-loop diagrams with mesons in the intermediate state. In latter case, the contribution of the diagram with intermediate pion is enhanced by small pion mass in the meson propagator. The leading in $1/N_c$ diagrams are drawn in Fig. 2. They are the box diagram with dynamical quarks (Fig. 3) and the meson exchange diagrams in pseudoscalar, scalar and axial-vector channels.



Figure 2. A schematic illustration for the diagrams contributing to the four-rank polarization tensor to the leading in $1/N_c$ order. The four-fermion interaction is introduced through (28). The nonlocal multi-photon vertices are not shown for simplicity, see Fig. 3.

For explicit calculations of the hadronic contributions to the muon AMM due to the light-by-light scattering mechanism [27–31] we use the $SU(3) \times SU(3)$ chiral quark model with nonlocal Lagrangian (N χ QM)

$$\mathcal{L} = \bar{q}(x)(i\hat{\partial} - m_c)q(x) + \frac{G}{2}[J_S^a(x)J_S^a(x) + J_{PS}^a(x)J_{PS}^a(x)] - \frac{H}{4}T_{abc}[J_S^a(x)J_S^b(x)J_S^c(x) - 3J_S^a(x)J_{PS}^b(x)J_{PS}^c(x)],$$
(28)



Figure 3. Contact terms which are gave contribution to $\Pi_{\mu\nu\lambda\rho}(q_1, q_2, q_3)$. Numbers in front of diagrams are the degeneracy factors.

where q(x) are the quark fields, $m_c (m_u = m_d \neq m_s)$ is the diagonal matrix of the quark current masses, *G* and *H* are the four- and six-quark coupling constants. Second line in the Lagrangian represents the Kobayashi–Maskawa–t'Hooft determinant vertex with the structural constant

$$T_{abc} = \frac{1}{6} \epsilon_{ijk} \epsilon_{mnl}(\lambda_a)_{im}(\lambda_b)_{jn}(\lambda_c)_{kl},$$

where λ_a are the Gell-Mann matrices for a = 1, ..., 8 and $\lambda_0 = \sqrt{2/3}I$. The nonlocal structure of the model is introduced via the nonlocal quark currents

$$J_M^a(x) = \int d^4 x_1 d^4 x_2 f(x_1) f(x_2) \bar{Q}(x - x_1, x) \Gamma_M^a Q(x, x + x_2),$$
(29)

where M = S for the scalar and M = PS for the pseudoscalar channels, $\Gamma_S^a = \lambda^a$, $\Gamma_{PS}^a = i\gamma^5 \lambda^a$ and f(x) is a form factor with the nonlocality parameter Λ reflecting the nonlocal properties of the QCD vacuum. In (29), the gauge-invariant interaction with an external photon field V_{μ}^a is introduced through the Schwinger phase factor

$$Q(x,y) = \mathcal{P}\exp\left\{i\int_{x}^{y} dz^{\mu}V_{\mu}^{a}(z)T^{a}\right\}q(y).$$
(30)

In order to guarantee the Ward-Takahashi identities, it induces the quark-antiquark–*n*-photon vertices. Additionally, there appear the meson–quark-anti-quark–*n*-photon vertices.

The numerical results for the value of a_{μ}^{HLbL} are presented in Fig. 4 for the SU(2) and SU(3) models. The estimates for the partial contributions to a_{μ}^{HLbL} (in 10^{-10}) are the π^0 contribution 5.01(0.37) [28], the sum of the contributions from π^0 , η and η' mesons 5.85(0.87) [28], the scalar σ , $a_0(980)$ and $f_0(980)$ mesons contribution 0.34(0.48) [29, 30], and the quark loop contribution is 11.0(0.9) [30]. The total contribution obtained in the leading order in the $1/N_c$ expansion is (see also [30])

$$a_{\mu}^{\text{HLbL},N_{\chi}\text{QM}} = 16.8(1.25) \cdot 10^{-10}.$$
 (31)

The error bar accounts for the spread of the results depending on the model parameterizations. Comparing with other model calculations, we conclude that our results are quite close to the recent results obtained in [32, 33].

If we add the result (31) to all other known contributions of the standard model to a_{μ} , (14),(22) and (23), we get that the difference between experiment (12) and theory is

$$a_{\mu}^{\text{BNL,CODATA}} - a_{\mu}^{\text{SM}} = 18.73 \times 10^{-10},$$
 (32)

which corresponds to 2.43σ . If one uses the hadronic vacuum polarization contribution from the τ hadronic decays instead of e^+e^- data

$$a_{\mu}^{\text{HVP,LO}-\tau} = 701.5(4.7) \times 10^{-10}$$
 [19], (33)

the difference decreases to $12.14 \times 10^{-10} (1.53\sigma)$ in the N χ QM model (31).



Figure 4. (Left) The results for a_{μ}^{HLbL} in the SU(2) model: the red dashed line is the total result, the green dotted line is the quark loop contribution and the magenta dash-dot-dot line is the $\pi + \sigma$ contribution. Thin vertical line indicates the region for estimation of a_{μ}^{HLbL} error band. (Right) The results for a_{μ}^{HLbL} : the black solid line is the SU(3)-result, the red dash line corresponds to the SU(2)-result, the blue dash-dotted line is the $C_{\chi}QM$ result [32], hatched region correspond to DSE result [33].

6 Conclusions

Clearly, a further reduction of both the experimental and theoretical uncertainties is necessary. On the theoretical side, the calculation of the still badly known hadronic light-by-light contributions in the next-to-leading order in the $1/N_c$ expansion (the pion and kaon loops) and extension of the model by including heavier vector and axial-vector mesons is the next goal. The contribution of these effects and the model error induced by them are not included in the result (31). Preliminary studies [25, 34] show that these contributions are one order smaller than the pseudoscalar exchanges and the quark loop contribution. However, the interesting point that inclusion of vector channel can strongly suppress contribution from the quark loop due photon–vector meson exchange which lead to appearance in each photon vertex additional VMD-like factor. This was found in local NJL model [26] and should be carefully investigated in the nonlocal one.

New experiments at FNAL and J-PARC have to resolve the muon g - 2 problem, increasing effect or leading to its disappearance.

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