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# Automated and Objective Removal of Bifurcation Aneurysms: Incremental Improvements, and Validation Against Healthy Controls

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## Abstract

*Abnormal hemodynamic stresses are thought to correlate with aneurysm initiation, growth, and rupture. We have previously investigated the role of wall shear stress (WSS) and WSS gradients (WSSG) in search for a mechanistic link to formation of sidewall aneurysms using an automated and objective tool for aneurysm removal and arterial reconstruction in combination with computational fluid dynamics (CFD). However, we warned against the use of the tool for bifurcation type aneurysms because of a potential unrealistic reconstruction of the apex. We hypothesized that inclusion of additional morphological features from the surrounding vasculature could overcome these constraints. We extended the previously published method for removal and reconstruction of the bifurcation vasculature based on diverging and converging points of the parent and daughter artery centerlines, to also include two new centerlines between the daughter vessels, one of them passed through the bifurcation center. Validation was performed by comparing the efficacy of the two algorithms, using ten healthy models of the internal carotid artery terminus as ground truth. Qualitative results showed that the bifurcation apexes became smoother relative to the original algorithm; more consistent with the reference models. This was reflected quantitatively by a reduced maximum distance between the reference and reconstructed surfaces, although not statistically significant. Furthermore, the modified algorithm also quantitatively improved CFD derived WSS and WSSG, especially the latter. In conclusion, the modified algorithm does not perfectly reconstruct the bifurcation apex, but provides an incremental improvement, especially important for the derived hemodynamic metrics of interest in vascular pathobiology.*

*Keywords:* Mechanobiology, Wall Shear Stress, Wall Shear Stress Gradients, Aneurysm Pathogenesis, Subarachnoid Hemorrhage

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## 29 1. Introduction

30 Rupture of an intracranial aneurysm is the most common cause of subarachnoid hemorrhage (Wiebers et  
31 al., 2003). The vast majority of aneurysms are asymptomatic and incidentally detected when patients undergo  
32 neuroimaging for unrelated reasons. However, risk of clinical intervention can exceed the natural risk of rupture,  
33 which is as low as 1% annually (Rinkel et al., 1998) making optimal patient-specific treatment decisions difficult.  
34 Morphological indices have historically been used clinically for risk of rupture stratification (Raghavan et al.,  
35 2005), but aneurysm morphology and size are ultimately surrogates for hemodynamically induced wall shear  
36 stress (WSS) that contribute to vessel wall adaptation, remodeling, and vascular pathogenesis (Malek et al.,  
37 1999; Morbiducci et al., 2016). Medical image-based computational fluid dynamics (CFD) (Taylor and  
38 Steinman, 2010) has been extensively used in the investigation of vascular pathology, e.g., retrospectively  
39 correlating flow phenotypes and stresses with aneurysm rupture status in search for prospective clinical  
40 use (Xiang et al., 2011; Cebal et al., 2011).

41 However, 'predicting' aneurysm rupture status in large databases with a retrospectively known clinical  
42 outcome can be problematic for a number of reasons. Aneurysm rupture is an event that may change  
43 both morphology and size (Schneiders et al., 2014; Skodvin et al., 2017), only certain aneurysms have  
44 endothelial cells (Frösen et al., 2004), and the aneurysm wall has a different structure compared to healthy  
45 arteries (Canham et al., 1999). Additionally, there are uncertainties related to modeling of aneurysm flows,  
46 like neck size overestimation with 3D rotational angiography (Schneiders et al., 2013), image segmentation,  
47 which is both laborious and operator-dependent (Valen-Sendstad et al., 2018), and numerical solution  
48 strategies (Valen-Sendstad and Steinman, 2014; Khan et al., 2015). Therefore, studying the fundamental role  
49 of hemodynamics in aneurysms might be more intricate than originally anticipated. However, since the same  
50 stimuli (WSS/WSSG) are believed to be involved in aneurysm initiation (Gao et al., 2008; Kulcsár et al.,  
51 2011), growth (Sugiyama et al., 2012; Francis et al., 2013), and rupture (Cebal et al., 2005; Xiang et al.,  
52 2011), one can investigate the hemodynamic stimulus and vascular response before aneurysms have formed,  
53 without the aforementioned limitations. Hence, studying aneurysm initiation can provide mechanistic links  
54 that are paramount for understanding fundamental vascular remodeling.

55 Ford et al. (Ford et al., 2009) developed a tool for objective aneurysm removal and arterial reconstruction  
56 for investigating the plausible hemodynamic stimulus prior to sidewall aneurysm formation. They also warned  
57 about the application to bifurcation aneurysms, and clearly stated that the tool 'remains to be verified'. The  
58 latter is difficult because medical images of the pre-aneurysmal vasculature are rarely available. Secondly, the  
59 high-resolution contrast-based computed tomography images needed to adequately reconstruct a bifurcation  
60 apex, can naturally not be obtained from healthy individuals to limit potentially harmful radiation (Hendee  
61 and O'Connor, 2012). From previous usage of the tool developed by Ford et al., for instance applied to  
62 sidewall aneurysms Valen-Sendstad et al. (2014) we hypothesized that the bifurcation apex was occasionally  
63 reconstructed with an artificial "notch" at the apex. We, therefore, proposed a technical improvement to the  
64 original algorithm. We also acquired access to segmentation of intracranial blood vessels in ten patients that

65 underwent neurointensive care where no vascular abnormalities were found, which enabled validation. The  
66 latter is indeed the only possible solution since the vasculature is unknown in the presence of an aneurysm,  
67 which the algorithm actually is independent of. The aim of the study was to reconstruct an artificially  
68 removed bifurcation, and compare the results of the two reconstruction algorithms to the reference and *a*  
69 *priori* known bifurcation surface, especially focusing on relevant CFD derived stresses. In the following, we  
70 will refer to the bifurcation surfaces as *reference*, *Ford*, and *modified* corresponding to the unmodified healthy  
71 surface, the reconstructed surface from Ford et al., and our modified algorithm, respectively.

## 72 **2. Methods**

### 73 *2.1. Parent artery and bifurcation reconstruction*

74 We acquired access to 3D angiograms from ten patients that underwent neurointensive care where no  
75 vascular abnormalities were found, originally collected for the open-source Aneurisk database, and subsequently  
76 made publicly available (Aneurisk-Team, 2012). Figure 1 is adapted from Ford et al. and outlines the  
77 algorithm for intracranial aneurysm removal and parent artery reconstruction. Note that we here illustrate  
78 the algorithm using the same model as in Ford et al., but that we here apply the algorithm to models without  
79 aneurysms only. Briefly, the algorithm is based on manipulating the Voronoi diagram, which is an alternative  
80 representation of a surface (Piccinelli et al., 2009), and associated centerlines, to both remove and reconstruct  
81 the bifurcation. Details are provided in the caption of Figure 1. The main difference between the original  
82 and the modified algorithm is that the Voronoi diagram is interpolated onto two new centerlines between the  
83 daughter vessels, these changes are colored purple in Figure 1.

### 84 *2.2. CFD, wall shear stress, and wall shear stress gradients*

85 CFD simulations were performed to investigate the effects of the reconstruction algorithms on hemodynamic  
86 stresses. The Vascular Modelling ToolKit (Antiga et al., 2008) was used to extend the inlet and outlets five  
87 times the local radius, and create meshes that on average consisted of three million tetrahedron cells with  
88 four boundary layers, previously demonstrated to be sufficient to resolve WSS (Khan et al., 2015). Pulsatile  
89 CFD simulations were performed assuming blood to behave as a Newtonian fluid (Khan et al., 2017) using  
90 the *Oasis* solver (Mortensen and Valen-Sendstad, 2015), designed to obtain a solution that preserves kinetic  
91 energy while minimizing numerical dispersion and diffusion errors, taking 10,000 time steps per cycle with a  
92 period of 0.951s using an older adult waveform (Hoi et al., 2010). We specified a fully developed Womersley  
93 velocity profile at the inlet and a time-averaged cross-sectional mean velocity of 0.27 *m/s* (Valen-Sendstad  
94 et al., 2015) with a flow splitting approach for the outflow boundary as detailed in (Chnafa et al., 2018).

95 The efficacy of the reconstruction algorithms was quantified with respect to the mean and maximum  
96 distance, curvature, WSS, and WSSG; measured relatively to the reference surface or associated CFD  
97 simulations. All metrics were computed along the intersection between the objectively defined bifurcation  
98 plane (Piccinelli et al., 2011) and surface, see white lines in Figure 3A, now referred to as *bifurcation lines*.

99 To quantitatively measure the differences, we sampled WSS and WSSG along the normalized bifurcation line,  
100 and used a spline representation to compute the maximum curvature, a metric describing the bifurcation  
101 apex "notch". A one-sided paired t-test was used to check if the modified method performed significantly  
102 better, setting the level of significance to  $p\text{-value} < 0.05$ , not adjusting for multiple tests.

### 103 3. Results

#### 104 3.1. Parent artery and bifurcation reconstruction

105 Figure 2 shows models 1-5 of the reference surface in white with the results of the original and modified  
106 surface reconstruction algorithms colored in red in sub-plots A and B, respectively, all in opaque. We have  
107 zoomed into model 1 to better highlight the differences. These qualitative results arguably show that the  
108 modified algorithm produce reconstructed surfaces closer to the reference surface, most importantly at the  
109 apex of the bifurcation. That is, the modified algorithm does not produce the same artificial "notch",  
110 especially apparent in the models 1, 2, 4, and 5 shown in Figure 2A. The remaining five models are shown in  
111 the Appendix with broadly consistent results.

#### 112 3.2. Hemodynamic metrics: Wall shear stress and wall shear stress gradients

113 Focusing now on qualitative CFD derived results, Figure 3A shows bifurcation WSS maps obtained on  
114 the modified, reference, and Ford surfaces, respectively. The WSS maps show largely similar global trends,  
115 but with clearly visible differences at the bifurcation apex. This is further highlighted by the corresponding  
116 WSS and WSSG values along the bifurcation lines shown in Figure 3B; especially WSSG is overestimated by  
117 the original algorithm. The remaining five models are shown in the Appendix with broadly consistent results.

118 Table 1 shows quantitative results and demonstrates that both the curvature, WSS, and WSSG were  
119 significantly closer to the reference values, with  $p\text{-values} < 0.05$  marked in bold. The maximum distance  
120 between the reference and reconstructed surfaces was also reduced with the modified algorithm, although not  
121 statistically significant.

### 122 4. Discussion

123 We have shown that a minor modification of Ford et al.'s algorithm can reconstruct arterial bifurcations  
124 that are more consistent with the reference bifurcation obtained from state-of-the-art medical images. As a  
125 result, the computed WSS and WSSG from the reconstructed surfaces are statistically and phenotypically  
126 improved compared to the original algorithm. Since the vast majority of aneurysms are located in bifurcations,  
127 the modified algorithm could increase the number of subjects, increase the rigor of aneurysm initiation  
128 research, and accelerate our understanding of fundamental vascular pathobiology. The latter can ultimately  
129 contribute to further advances in research on aneurysm risk of rupture.

130 We have previously shown that there is relatively high intra- and interlaboratory uncertainty in segmenta-  
131 tion of intracranial arteries (Valen-Sendstad et al., 2018). To reduce the uncertainty in the segmentation

132 we chose to focus on the ICA terminus since it is the largest intracranial artery, and is therefore the least  
133 sensitive to segmentation errors because of the high voxel-to-vessel ratio. However, we have also compared  
134 the geometrical metrics of middle- and anterior cerebral artery bifurcations and obtained equivalent results  
135 for the maximum curvature (average absolute errors of 2.09 and 0.52 [ $\frac{1}{mm}$ ] using the Ford and modified  
136 algorithm, respectively, p-value < 0.001). These results, however, are associated with higher uncertainties  
137 due to the smaller voxel-to-vessel ratio. Hence, a limitation is that validation has just been performed  
138 on ten models. Another "feature" associated with the current methods is namely that neither algorithms  
139 were designed or capable to reproduce a proximal stenosis, as observed in model 7, see Figure 5 of the  
140 Appendix. Both algorithms produced a too wide arterial segment at the stenosis location, which resulted in a  
141 lowered WSS/WSSG, relative to the reference model. The quantitative results are admittedly sensitive to the  
142 bifurcation plane, as is obvious from Figures 3 and 5, however, they are objectively defined (Piccinelli et al.,  
143 2011).

144 Relative to previous studies, our WSS/WSSG figures/lines appear to be noisier since we used human  
145 "patient-specific" models instead of idealized (Kono et al., 2013; Lauric et al., 2018) or animal models (Meng  
146 et al., 2010). We do not consider this a limitation, but rather a result of controlling numerical viscosity, and  
147 the use of potentially "irregular" human models from the Aneurisk database. Smoothing the surfaces is  
148 indeed possible, but we consider the current approach the most sensitive, and consequently the most rigorous  
149 one.

150 Although we have shown that the modified algorithm better reconstructs the bifurcation, it still re-  
151 mains to quote Ford et al., namely that users must still "exercise their judgment if a particular case  
152 is a good candidate for similar studies". The code and associated tutorials are provided online, see  
153 <https://github.com/KVSlab/morphMan>, which also includes other methods for objectively altering ad-  
154 ditional morphological features of anatomically plausible vascular geometries.

## 155 5. Conclusion

156 We have shown that an incremental modification of Ford et al.'s aneurysm removal tools plausibly give  
157 better agreement with the reference surface and the corresponding stresses on the arterial wall. The modified  
158 algorithm can accelerate and broaden research on the hemodynamic stresses associated with aneurysm  
159 initiation, with the ultimate extrapolation to rupture prediction.

## 160 6. Conflict of interest statement

161 The authors have no conflicts of interest to declare.

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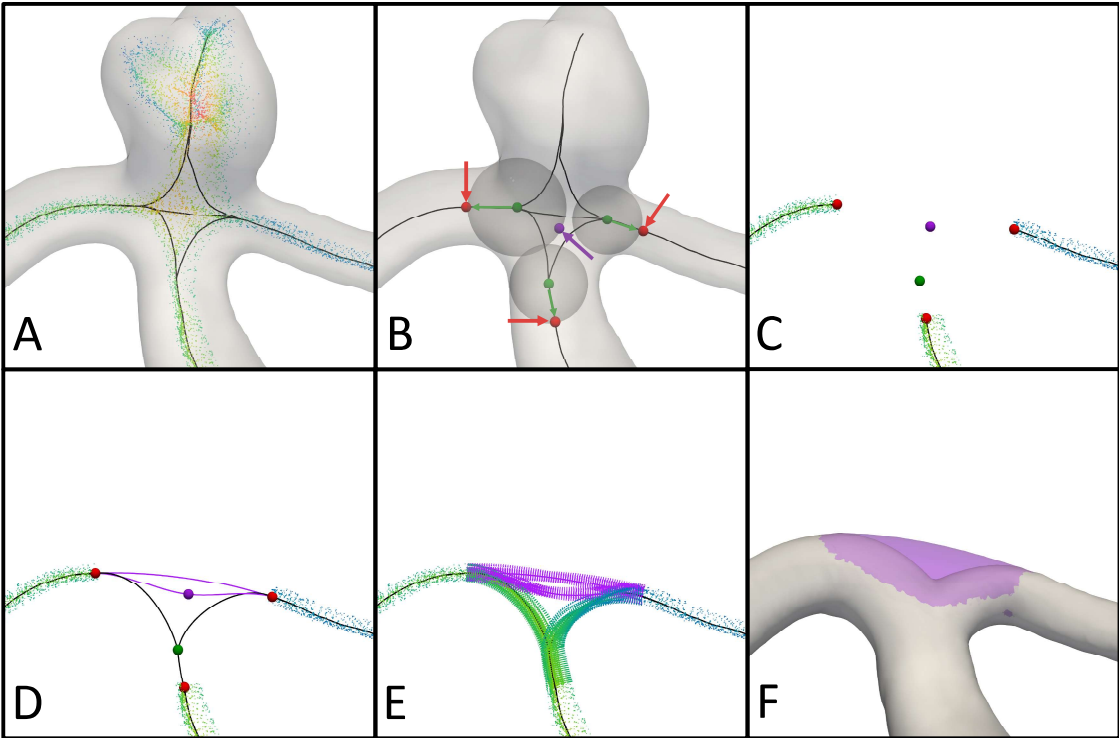


Figure 1: Illustration of the algorithm for removing a bifurcation aneurysm. The additions to the algorithm, relative to Ford et al., is highlighted in purple. Note that to ease comparison with Ford et al. we here illustrate the algorithm on the same model, but for the remainder of the paper we are applying the algorithm to bifurcations without aneurysms for validation purposes. **Step A**, compute the Voronoi diagram and five centerlines; two from the parent artery to each daughter branch, two from each daughter branch to the aneurysm sac, and one between the two daughter branches. **Step B**, the green dots are located where the centerlines coordinates diverge; referred to as diverging points, and the arithmetic mean of the coordinates of these is defined as the bifurcation center location, shown in purple. The diverging points are then moved one radius of the local minimal inscribed sphere away from the bifurcation center along the centerlines, as indicated by the green arrows; now referred to as clipping points. **Step C**, subtract the centerlines and Voronoi diagram that are located in between the clipping points. **Step D**, create a total of four new centerlines, two of which are passed through the diverging point from the parent artery to the daughter branches using third order splines. The remaining two start and end at the daughter branches, where one of them is passed through the bifurcation center. **Step E**, extrapolate the old Voronoi diagram along the new centerlines. **Step F**, envelope the Voronoi diagram to create a new surface.

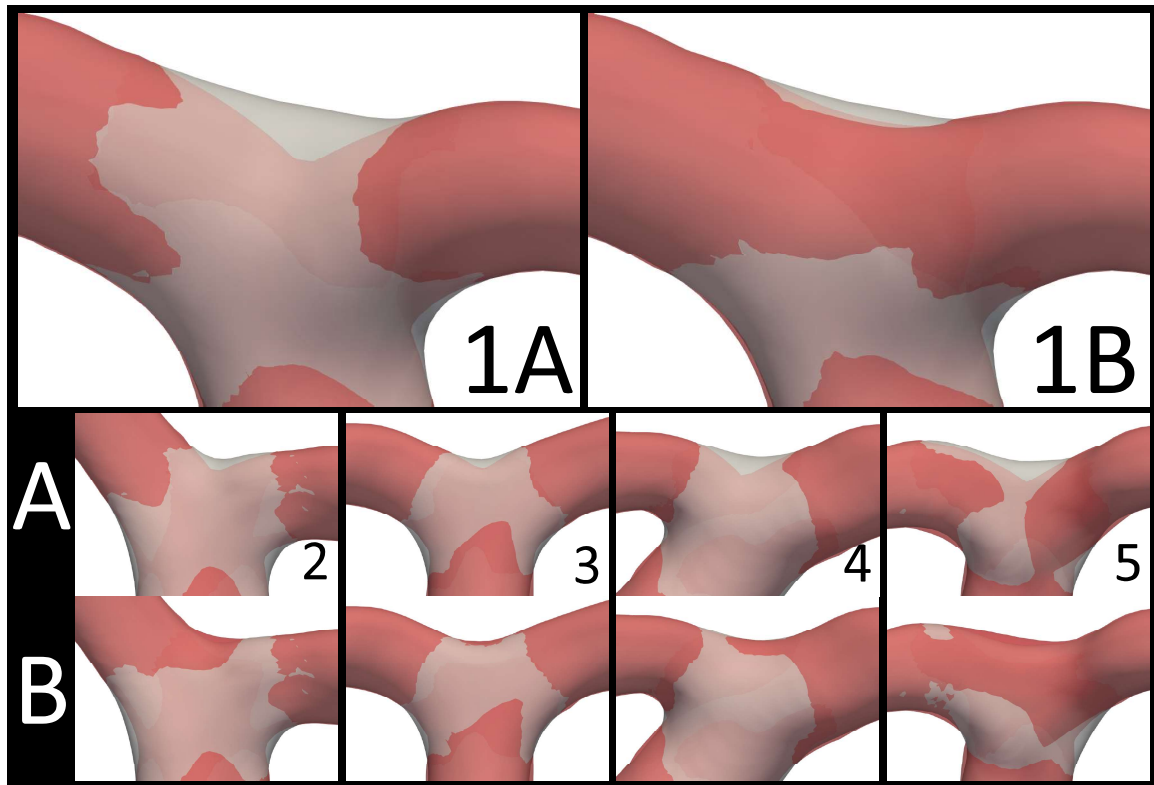


Figure 2: The figure shows the reference surface in opaque, with the results from the original and modified surface reconstruction algorithms colored in red in sub-plots A and B, respectively.

Figure3

[Click here to access/download;Figure;Figure3.pdf](#)

Figure 3 consists of two main panels, A and B. Panel A, labeled 'A', shows five rows of WSS maps for three models: Modified, Reference, and Ford. The rows are numbered 1 to 5. Each row contains three maps corresponding to the models. White lines indicate bifurcation lines. Panel B, labeled 'B', shows a 5x2 grid of line graphs. The columns are labeled 'WSS' and 'WSSG'. The rows correspond to the five bifurcation lines in panel A. The y-axis for the 'WSS' column is labeled '[Pa]' and the y-axis for the 'WSSG' column is labeled '[Pa/mm]'. The x-axis for both columns is labeled from 0.0 to 1.0. A legend in the top right of panel B identifies the lines: Modified (blue), Reference (black), and Ford (orange).

Figure 3: **A** Wall shear stress (WSS) maps from computational fluid dynamic simulations of the modified, reference, and Ford models, from left to right, respectively, and bifurcation lines shown in white. The absolute values of the WSS are indicated in the panel to the right. **B** WSS and WSS gradients along the bifurcation lines where the colors black, orange, and blue refers to the modified, reference, and Ford models, respectively.

12

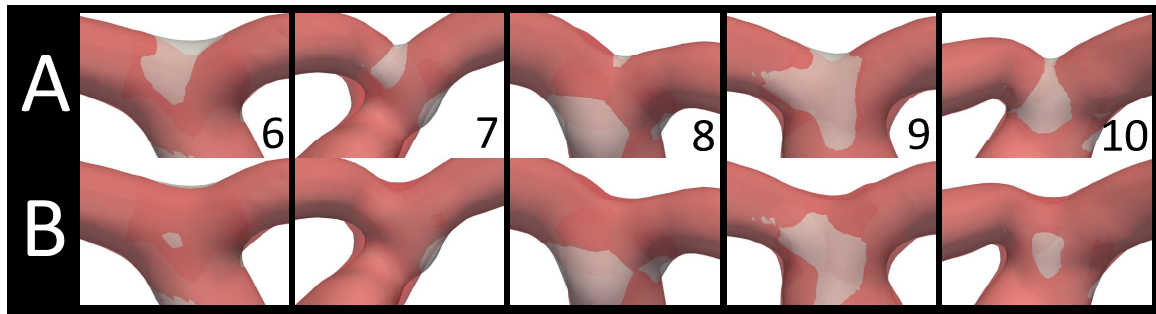


Figure 4: The figure shows the reference surface in opaque, with the results of the original and modified surface reconstruction algorithms colored in red in sub-plots A and B, respectively.

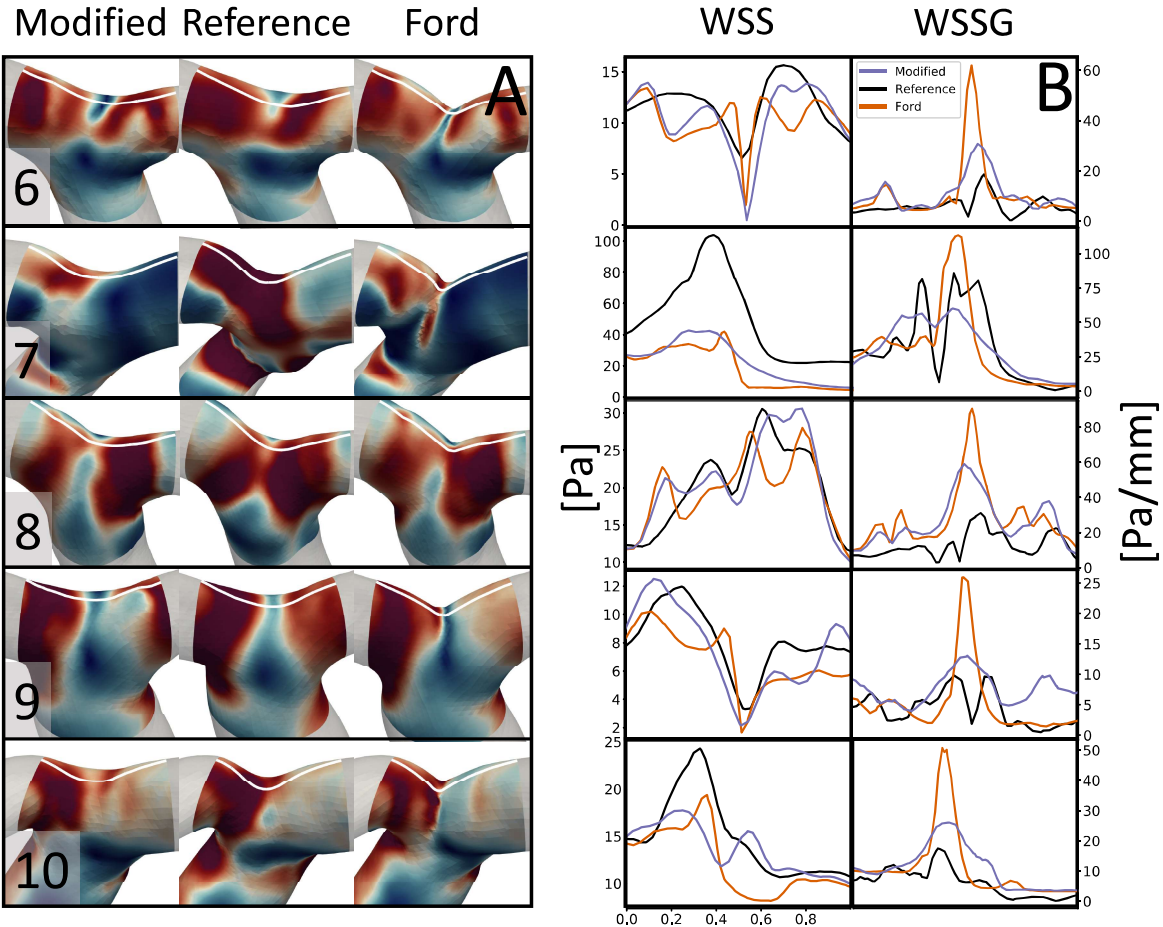


Figure 5: **A** Wall shear stress (WSS) maps from computational fluid dynamic simulations of the modified, reference, and Ford models, from left to right, respectively, and bifurcation lines shown in white. The absolute values of the WSS are indicated in the panel to the right. **B** WSS and WSS gradients along the bifurcation lines where the colors black, orange, and blue refers to the modified, reference, and Ford models, respectively.

Table1

Metric	Measure	Mean absolute error (SD)		p-value
		Ford	Modified	
Distance [ $mm$ ]	Average	0.06 (0.03)	0.06 (0.04)	0.408
	Max	0.30 (0.15)	0.19 (0.11)	0.076
Curvature [ $\frac{1}{mm}$ ]	Max	2.03 (0.48)	0.24 (0.26)	<b>&lt;0.001</b>
WSS [Pa]	Average	7.27 (11.02)	5.63 (8.73)	<b>0.037</b>
	Max	17.57 (22.33)	12.90 (16.66)	0.081
WSSG [Pa/mm]	Average	12.54 (8.23)	9.41 (5.49)	<b>0.012</b>
	Max	50.22 (29.40)	26.82 (17.47)	<b>0.001</b>

Table 1: The table shows quantitative result based on the error measurements between the reference surface versus those obtained from the original and modified algorithms, respectively. P-values below 0.05 % are marked in bold.