



1     **Global mean surface temperature and climate sensitivity of the**  
2                             **EECO, PETM and latest Paleocene**

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26 **Abstract:**

27 Accurate estimates of past global mean surface temperature (GMST) help to contextualise  
28 future climate change and are required to estimate the sensitivity of the climate system to CO<sub>2</sub>  
29 forcing during the geological record. GMST estimates from the latest Paleocene and early  
30 Eocene (~57 to 48 million years ago) span a wide range (~9 to 23°C higher than pre-industrial)  
31 and prevent an accurate assessment of climate sensitivity during this extreme greenhouse  
32 climate interval. Here, we develop a multi-method experimental framework to calculate GMST  
33 during three target intervals: 1) the latest Paleocene (~57 Ma), 2) the Paleocene-Eocene  
34 Thermal Maximum (56 Ma) and 3) the early Eocene Climatic Optimum (EECO; 49.4 to 53.3  
35 Ma). Using six independent methodologies, we find that average GMST estimates during the  
36 latest Paleocene and PETM are 11.7°C (± 0.6°C) and 18.7°C (± 0.8°C) higher than pre-  
37 industrial, respectively. GMST estimates from the EECO are 13.3°C (±0.5°C) warmer than  
38 pre-industrial and comparable to previous IPCC AR5 estimates (12.7°C higher than pre-  
39 industrial). Leveraging the extremely large 'signal' associated with these extreme warm  
40 climates, we combine estimates of GMST and CO<sub>2</sub> from the latest Paleocene, PETM and  
41 EECO to calculate a gross estimate of the average climate sensitivity between the early  
42 Paleogene and today. This yields gross climate sensitivity estimates for the latest Paleocene,  
43 PETM and EECO which range between 2.8 to 4.8°C (66% confidence). These largely fall  
44 within the range predicted by the IPCC (1.5 to 4.5°C per doubling CO<sub>2</sub>), but appear  
45 incompatible with low values (between 1.5 and 2.8°C per doubling CO<sub>2</sub>).

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52 **1. Introduction**

53 Under high growth and low mitigation scenarios, atmospheric carbon dioxide (CO<sub>2</sub>) could  
54 exceed 1000 parts per million (ppm) by the year 2100 (Stocker et al., 2013). The long-term  
55 response of the Earth System under such elevated CO<sub>2</sub> concentrations remains uncertain  
56 (Stevens et al., 2016; Knutti et al., 2017; Hegerl et al., 2007). One way to better constrain these  
57 climate predictions is to examine intervals in the geological past during which greenhouse gas  
58 levels were similar to those predicted under future scenarios. This is the rationale behind the  
59 Deep-time Model Intercomparison Project (DeepMIP) which aims to investigate the behaviour  
60 of the Earth System in three high CO<sub>2</sub> climate states in the latest Paleocene and early Eocene  
61 (~ 57–48 Ma) (Lunt et al., 2017; Hollis et al., 2019).

62 Sea surface temperature (SST) and land air temperature (LAT) proxies indicate that  
63 the latest Paleocene and early Eocene were characterised by global mean surface  
64 temperatures (GMST) much warmer than those of today (Cramwinckel et al., 2018; Farnsworth  
65 et al., 2019; Hansen et al., 2013; Zhu et al., 2019; Caballero and Huber, 2013). Having a robust  
66 quantitative estimate of the magnitude of warming relative to modern is useful for two primary  
67 reasons: (1) it allows us to contextualise future climate change predictions by comparing the  
68 magnitude of future anthropogenic warming with the magnitude of past natural warming; (2)  
69 combined with CO<sub>2</sub> proxy data, it allows us to estimate climate sensitivity, a key metric for  
70 understanding how the climate system responds to CO<sub>2</sub> forcing. The Fifth IPCC Assessment  
71 Report stated that GMST was 9°C to 14°C higher than for pre-industrial conditions during the  
72 early Eocene (~52 to 50 Ma) (Masson-Delmotte et al., 2014). Subsequent studies indicate a  
73 wider range of estimates, from 9 to 23°C warmer than pre-industrial (Cramwinckel et al.,  
74 2018; Farnsworth et al., 2019; Hansen et al., 2013; Zhu et al., 2019; Caballero and Huber, 2013)  
75 (Figure 1). It is an open question whether this range arises from inconsistencies between the  
76 methods used to estimate GMST, such as selection of proxy datasets, treatment of  
77 uncertainty, and/ analysis of different time intervals. This has thwarted a robust assessment  
78 of GMST estimates for the latest Paleocene and early Eocene.



79            Here we calculate GMST estimates within a consistent experimental framework for the  
80 target intervals outlined by the Deep-time Model Intercomparison Project (DeepMIP): i) the  
81 Early Eocene Climatic Optimum (EECO; 53.3 to 49.4 Ma), ii) the Paleocene-Eocene Thermal  
82 Maximum (PETM, ca. 56 Ma) and iii) the latest Paleocene (LP, ca. 57-56 Ma). We use six  
83 independent methods to obtain new GMST estimates for these three time periods, employing  
84 recently compiled datasets of SST and LAT estimates (Hollis et al., 2019) and BWT estimates  
85 (Cramer et al., 2009; Westerhold et al., 2018; Barnet et al., 2019). We also undertake a suite  
86 of additional sensitivity studies to explore the influence of particular proxies on each GMST  
87 estimate. We then combine GMST estimates from all six methods to generate a “best  
88 estimate” GMST for each time slice and use these, with existing estimates of CO<sub>2</sub> (Gutjahr et  
89 al., 2017; Anagnostou et al., 2016) to develop new estimates of ECS during the latest  
90 Paleocene, PETM and EECO.

91

## 92 **2. Methods and Materials**

93 Three different input datasets are used to calculate GMST. Dataset  $D_{surf}$  consists of surface  
94 temperature estimates. Dataset  $D_{deep}$  consists of deep-water temperature estimates. Dataset  
95  $D_{comb}$  consists of a combination of surface- and deep-water temperature estimates. Six  
96 different methodologies make use of these datasets to estimate GMST. Below we describe  
97 these datasets and methods.

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### 99 **2.1. Dataset $D_{surf}$**

100 Dataset  $D_{surf}$  is version 0.1 of the DeepMIP database, as described in Hollis et al (2019). It  
101 consists of SSTs and LATs for the latest Paleocene, PETM and EECO. The SSTs are from  
102 multiple proxies, including foraminiferal  $\delta^{18}\text{O}$ , foraminiferal Mg/Ca, clumped isotopes ( $\Delta 47$ ),  
103 and TEX<sub>86</sub>. Foraminiferal  $\delta^{18}\text{O}$  values are calibrated to SST following Bemis et al. (1998).  
104 Foraminiferal Mg/Ca are calibrated to SST following Evans et al. (2018). TEX<sub>86</sub> values are



105 calibrated to SST using BAYSPAR (Tierney and Tingley, 2014).  $\Delta 47$  values are reported using  
106 the parameters and calibrations of the original publications (Evans et al., 2018; Keating-Bitonti  
107 et al., 2011). LATs are derived from leaf fossils, pollen assemblages, mammal  $\delta^{18}\text{O}$ , paleosol  
108  $\delta^{18}\text{O}$  and branched GDGTs. LAT estimates are calculated using the parameters and  
109 calibrations of the original publication (see Hollis et al., 2019 and ref. therein). The location of  
110 the proxies is shown in Figure 2. For each site, we utilise the uncertainty range reported in  
111 Hollis et al. (2019). We do not explore calibration uncertainty, but instead focus on the  
112 methodologies used to calculate GMST.

113 Four methods ( $D_{surf-1}$ ,  $D_{surf-2}$ ,  $D_{surf-3}$  and  $D_{surf-4}$ ) are employed to calculate GMST from  
114 dataset  $D_{surf}$ . These methods employ parametric ( $D_{surf-1}$ ,  $D_{surf-2}$ ,  $D_{surf-4}$ ) or non-parametric  
115 ( $D_{surf-3}$ ) functions to estimate temperature. Each method conducts a 'baseline' calculation  
116 which uses the SST and LAT data compiled in accordance with the DeepMIP protocols (i.e.  
117 Hollis et al., 2019). Our baseline calculation ( $D_{surf-default}$ ) excludes  $\delta^{18}\text{O}$  values from  
118 recrystallized planktonic foraminifera as these estimates are significantly cooler than  
119 estimates derived from the  $\delta^{18}\text{O}$  value of well-preserved foraminifera, foraminiferal Mg/Ca  
120 ratios and clumped isotope values from larger benthic foraminifera (see Hollis et al., 2019 and  
121 ref. therein). For each method, we also conduct a series of sub-sampling calculations, based  
122 on varying assumptions about the robustness of different proxies (Table 1). The first sensitivity  
123 experiment ( $D_{surf-Frosty}$ ) includes  $\delta^{18}\text{O}$  values from recrystallized planktonic foraminifera. The  
124 second sensitivity experiment ( $D_{surf-NoTEX}$ ) removes  $\text{TEX}_{86}$  values as these give slightly  
125 higher SSTs than other proxies, especially in the mid-to-high latitudes (Bijl et al., 2009; Hollis  
126 et al., 2012; Inglis et al., 2015). The third sensitivity experiment ( $D_{surf-NoMBT}$ ) removes  
127 MBT(')/CBT values derived from marine sediment archives as they may suffer from a cool bias  
128 (Inglis et al., 2017; Hollis et al., 2019). The fourth sensitivity experiment ( $D_{surf-NoMammal}$ )  
129 removes mammal and paleosol  $\delta^{18}\text{O}$  values as these proxies may suffer from a cool bias  
130 (Hollis et al., 2019). For each method, GMST is calculated for: i) the Early Eocene Climatic



131 Optimum (EECO; 53.3 to 49.4 Ma), ii) the Paleocene-Eocene Thermal Maximum (ca. 56 Ma)  
132 and iii) the latest Paleocene (LP; ca. 57-56 Ma).

133

#### 134 2.1.1. $D_{surf-1}$

135 Method  $D_{surf-1}$  was first employed by Caballero and Huber (2013) to estimate GMST from  
136 early Eocene surface temperature proxies in the era after pervasive recrystallization of  
137 foraminiferal  $\delta^{18}O$  values was recognized (e.g. Pearson et al., 2001; Pearson et al., 2007). This  
138 study used data compilations which were the predecessors to the DeepMIP compilation  
139 (Huber and Caballero, 2011, Hollis et al., 2012).

140 Here, the anomalies of individual proxy temperature data points with respect to modern  
141 values at the corresponding paleolocation are first calculated. The calculation involves binning  
142 into low, mid, and high latitudes (30°N to 30°S, 30°N/S to 60°N/S, and 60°N/S to 90°N/S), and  
143 calculating the unweighted mean anomaly within these bins between the median  
144 reconstructed value at a given locality and the temperature at the same location today (from  
145 reanalysis). The geographically binned means are then weighted according to relative  
146 spherical area to calculate a globally weighted mean temperature anomaly between the paleo-  
147 time slice and modern. All samples are treated equally and considered independent. The  
148 associated errors are added in quadrature with the inter-sample standard deviation. These  
149 two sources of error were combined and normalized by the square root of the number of  
150 samples. This method is intended as an unsophisticated, brute force approach to estimating  
151 GMST when dealing with many localities with poorly characterized errors in which there is a  
152 large difference between the reconstructed temperature at a given location and the modern  
153 equivalent. It is not intended to ferret out small differences in GMST nor is it expected to work  
154 well under conditions in which temperature gradients are stronger than today, continents are  
155 far removed from their current configuration, or in situations in which systematic errors are not  
156 readily mitigated by large sample size (i.e. when there are correlations in systematic errors



157 between proxies). It is designed to be relatively straightforward to interpret and simple to  
158 reproduce without relying overly on climate models or sophisticated statistical models.

159         Various sanity checks are performed along the way to determine if the method is likely  
160 to produce useful results for a given sampling distribution and what corrections should be  
161 applied to optimize it. For example, if we sampled the modern temperature field using a  
162 geographic sampling distribution for a given time interval, what would the reconstructed  
163 modern temperature be? If we sampled the modern global, annual average surface  
164 temperature field in the reanalysis product ERA-5 (mean value: 15.1°C) with the geographic  
165 distribution of samples we have in the past, we obtain values of 16.9°C ( $\pm 1.5^\circ\text{C}$ ) in the latest  
166 Paleocene, 14.2°C ( $\pm 1.7^\circ\text{C}$ ) for the PETM, and 15.2°C ( $\pm 1.1^\circ\text{C}$ ) for EECO at the distribution  
167 of localities. For the sampling densities and spatial structure of the latest Paleocene and early  
168 Eocene, this method can approach the true value within  $\sim 1.5^\circ\text{C}$  and the error propagation  
169 adequately characterizes the error, in this 'perfect knowledge' scenario. Seeking precision  
170 beyond that range is probably unwarranted. However, estimating the latest Paleocene and  
171 early Eocene GMST may be somewhat easier than estimating the modern GMST because  
172 temperature gradients are roughly half modern values or less, thus spatial heterogeneity is  
173 much reduced. Indeed, in the limit of a completely flat temperature gradient, only one perfect  
174 sample would be required to estimate GSMT.

175         We can use paleoclimate model results to characterise how well the existing  
176 palaeographic sampling network will impact results. For the latest Paleocene, the  
177 reconstructed GMST is 24.6°C ( $\pm 1.3^\circ\text{C}$ ), compared to the true paleoclimate model mean of  
178 25.8°C. For the PETM, the reconstructed GMST is 27.2°C ( $\pm 1.5^\circ\text{C}$ ), compared to the true  
179 paleoclimate model mean of 29.3°C. For the EECO, the reconstructed GMST is 25.3°C  
180 ( $\pm 0.7^\circ\text{C}$ ), compared to the true paleoclimate model mean of 25.8°C. This method produces  
181 estimates that are within random error given otherwise perfect knowledge. It is also clear that  
182 systematic errors introduced by limited paleogeographic sampling can be alleviated by  
183 incorporating the systematic offset in mean values between the true paleoclimate model  
184 GMST and the sampled paleoclimate model GMST. This is the only component in which



185 paleoclimate model information is included and we utilise this offset to correct for systematic  
186 errors. While this approach could be applied uncritically, it is best applied only within the  
187 context of studying the random and systematic error structure as described above and caution  
188 should be taken in using systematic corrections that are significantly bigger than the estimated  
189 random error.

190 The calculations shown here utilize two utilize two CESM1 simulations, as described  
191 in Cramwinckel et al., (2018; EO3 and EO4). The two cases are chosen to minimize the  
192 magnitude of the correction to GMST and the final result is not sensitivite to the choice of  
193 reference simulation among these two. The magnitude of the global correction could be  
194 sensitive to both using different models or boundary conditions.

195

#### 196 2.1.2. $D_{surf-2}$

197 In this method, GMST estimates are calculated using the method described in Farnsworth et  
198 al. (2019) where a transfer-function is used to calculate global mean temperature from local  
199 proxy temperatures. The transfer function is generated from a pair of Eocene climate model  
200 simulations, carried out at two  $\text{CO}_2$  concentrations. The first simulations are the same 2x  $\text{CO}_2$   
201 and 4x  $\text{CO}_2$  HadCM3L Eocene simulations from Farnsworth et al (2019). The second  
202 simulations are the x 4 $\text{CO}_2$  and 8x  $\text{CO}_2$  CCSM3 simulations of Huber and Caballero (2011),  
203 also discussed in Lunt et al (2012). We then provide a final estimate based on each of our two  
204 models. The two models are configured for the Eocene with different paleogeographies.

205 The principal assumption of this approach is that global temperatures scale linearly  
206 with local temperatures, and that a climate model can represent this scaling correctly. The  
207 resulting GMST estimate is independent of the climate sensitivity of the model but is  
208 dependent on the modelled spatial distribution of temperature. For a single given proxy  
209 location with a local temperature estimate ( $T^{\text{proxy}}$ ) we estimate global GMST ( $\langle T \rangle^{\text{inferred}}$ ) as:

210





211 
$$\langle T \rangle^{inferred} = \langle T^{low} \rangle + (T^{proxy} - T^{low}) \frac{\langle T^{high} \rangle - \langle T^{low} \rangle}{T^{high} - T^{low}} \quad (1)$$

212

213 where  $\langle T^{low} \rangle$  and  $\langle T^{high} \rangle$  are the global means of a low- and high-CO<sub>2</sub> model simulation  
214 respectively, and  $T^{low}$  and  $T^{high}$  are the local temperatures (same location as the proxy) from  
215 the same simulations.  $T^{low}$  and  $T^{high}$  represent local modelled SSTs or local modelled near-  
216 surface LATs (in contrast to Farnsworth et al. 2019 who only used local modelled near-surface  
217 LATs to calculate  $T^{low}$  and  $T^{high}$ , even if  $T^{proxy}$  was SST). If the proxy temperature is greater  
218 than  $T^{high}$  or cooler than  $T^{low}$ , then the inferred global mean is found by extrapolation rather  
219 than by interpolation and is therefore more uncertain (Figure 3). We repeat this process for  
220 each proxy data point (Figure 4) and take an average ( $\pm$  standard error) as our best estimate  
221 of global mean temperature.

222

### 223 2.1.3. $D_{surf-3}$

224 For  $D_{surf-3}$ , GMST estimates are calculated using Gaussian process regression (Figure 5-6;  
225 Bragg et al., Submitted). In this method, temperature is treated as an unknown function of  
226 location,  $f(x)$ . There are many possible functions that can fit the available proxy dataset. By  
227 using a Gaussian process model of the unknown function, we assume that temperature is a  
228 continuous and smoothly varying function of location, and once fitted to the data, the posterior  
229 mean of the model gives the most likely function form for the temperature. We use a Gaussian  
230 process prior and update it using the proxy data to obtain the posterior model which we can  
231 then use to predict the surface temperatures on a global grid. Prior specification of the model  
232 is via a mean function  $E(f(x)) = m(x)$ , and a covariance function  $Cov(f(x), f(x')) = k(x, x')$  (which  
233 tells us how correlated  $f(x)$  is with  $f(x')$ ). We also specify the standard deviation of the  
234 observation uncertainty about each data point ( $\sigma_i^2$ ). If  $\mathbf{f} = (f(x_1), \dots, f(x_n))^T$  is a vector of  
235 temperature observations at each location  $x_i$ , then the model is:

236



237 
$$\mathbf{f} \sim \mathcal{N}(\boldsymbol{\mu}, \boldsymbol{\Sigma}) \quad (2)$$

238

239 where  $\mu_i = m(x_i)$  and  $\Sigma_{ij} = k(x_i, x_j) + \mathbb{I}_{i=j}\sigma_i^2$ . The proxy temperatures are expressed as  
240 anomalies to the present-day zonal mean temperature at the respective paleolatitude. We  
241 subtract the mean temperature anomaly for each time period and core experiment prior to the  
242 analysis and therefore fit the model to the residuals, using a zero-mean prior function. This  
243 means the predicted field will relax towards the mean surface warming in areas of no data  
244 coverage. The covariance function – which considers the clustering of proxy locations -  
245 describes the correlation between  $f(x_i)$  and  $f(x_j)$  in relation to the distance of  $x_i$  and  $x_j$ . We use  
246 a squared-exponential covariance function with Haversine distances replacing Euclidean  
247 distances so that correlation is a function of distance on the sphere. A heteroscedastic noise  
248 model is used to weight the influence of individual proxy data by their associated uncertainty,  
249 i.e. the model will better fit reconstructions with a smaller reported error.

250 Proxy uncertainties are taken from Hollis et al., (2019) or are set to the average of the  
251 respective proxy method where no errors were reported. Standard deviations for TEX<sub>86</sub> and  
252 Mg/Ca records are derived from the reported 90% confidence intervals. A minimum value of  
253 2.5°C for the standard deviation is assumed for all other methods. The output variances of the  
254 covariance function are estimated using their maximum likelihood values, obtained with the  
255 GPy Python package (GPy, 2012). Note that the Gaussian process approach provides  
256 probabilistic predictions of temperature values, i.e., uncertainty estimates of the predicted  
257 field. We apply the method to the marine and terrestrial data separately and combine the  
258 masked fields afterwards in order to prevent mutual interference. The uncertainty reported for  
259 an individual GMST estimate is the standard deviation.

260 Model uncertainty (expressed as standard deviation fields) is typically highest in areas  
261 with sparse data coverage (e.g. the Pacific Ocean and Southern Hemisphere land masses;  
262 Figure S1) and the lower uncertainty for the latest Paleocene relative to the PETM and EECO  
263 is partly related to the smaller reported uncertainties in the training data rather than enhanced



264 data coverage. The large spread in reconstructed terrestrial temperatures for North America  
265 during the PETM (Figure S1d) and EECO (Figure Sf) also increases uncertainties for other  
266 continental areas during both time intervals.

267

#### 268 2.1.4. $D_{surf-4}$

269 For  $D_{surf-4}$ , GMST estimates are calculated using a simple mathematical model, tuned to best  
270 fit the proxy data:

271

$$272 \quad T(\theta) \approx a + b\theta + c \cos \theta \quad (3)$$

273

274 where  $T(\theta)$  is the Eocene zonal-mean temperature, and the coefficients  $a$ ,  $b$ , and  $c$  are chosen  
275 to minimize the sum of the squared residuals relative to  $D_{surf}$  (i.e. the SST and LAT data from  
276 Hollis et al. 2019). This model accurately represents  $T(\theta)$  in the modern climate (Figure S2)  
277 when supplied with similar number of data points as are in the Hollis et al (2019) dataset, and  
278 it ensures a global solution that is consistent with the physical expectation that temperature  
279 should decrease - and the meridional gradient in temperature should increase - from the  
280 tropics toward the poles (Figure S2).

281 For each data point, we account for three types of uncertainty (i.e. temperature,  
282 elevation, latitude). For temperature, we assume a skew-normal probability distribution based  
283 on the stated 90% confidence intervals. Where uncertainty estimates are not given, we  
284 assume a (symmetric) normal distribution with a 90% confidence interval of  $\pm 5K$ . For elevation,  
285 we assume a skew-normal distribution with a 90% confidence interval equal to the lowest and  
286 highest elevations of adjacent grid points in the paleotopography data set of Herold et al.  
287 (2014), with a lower bound of zero. For latitude, we assume a uniform distribution spanning  
288 the stated paleomagnetic and mantle estimates.



289 To estimate  $T(\theta)$ , we randomly sample temperature, elevation, and latitude from their  
290 respective distributions at each location (Figure S3), and apply a lapse-rate adjustment of  
291  $6^\circ\text{K}/\text{km}$ . Then, using a standard Monte Carlo bootstrapping method, we resample the same  
292 number of data points with replacement, and find the coefficients in Equation 3 that best fit the  
293 sub-sampled data. We repeat this procedure 10,000 times to find a probability distribution of  
294  $T(\theta)$ . The uncertainty associated with an individual GMST estimate is the standard deviation.

295

## 296 2.2. Dataset $D_{deep}$

297 Dataset  $D_{deep}$  consists of bottom water temperatures (BWTs) for the latest Paleocene, PETM  
298 and EECO. Benthic foraminifera  $\delta^{18}\text{O}$  values for the latest Paleocene, PETM and EECO come  
299 from previous compilations (Westerhold et al., 2018; Barnett et al., 2019; Cramer et al., 2009),  
300 adjusted to *Cibicidoides* following established methods (Cramer et al., 2009), allowing  
301 temperature to be calculated using Eq. 9 of Marchitto et al (2014):

302

$$303 \quad (\delta_{cp} - \delta_{sw} + 0.27) = -0.245 \pm 0.005t + 0.0011 \pm 0.0002t^2 + 3.58 \pm 0.02 \quad (4)$$

304

305 where  $t$  is bottom water temperature in Celsius,  $\delta_{cp}$  is  $\delta^{18}\text{O}$  of  $\text{CaCO}_3$  on the PeeDee  
306 Belemnite (PDB) scale, and  $\delta_{sw}$  is  $\delta^{18}\text{O}$  of seawater on the Standard Mean Ocean Water  
307 (SMOW).  $\delta_{sw}$  is defined in accordance with the DeepMIP protocols ( $-1.00\text{‰}$ ; see Hollis et al.,  
308 2019). A single method ( $D_{deep-1}$ ) is used to calculate GMST from  $D_{deep}$  following the  
309 methodology outlined in Hansen et al. (2013). For this method, GMST is calculated for: i) the  
310 Early Eocene Climatic Optimum (EECO; 53.3 to 49.4 Ma), ii) the Paleocene-Eocene Thermal  
311 Maximum (ca. 56 Ma) and iii) the latest Paleocene (LP; ca. 57-56 Ma).

312

### 313 2.2.1. $D_{deep-1}$



314 For  $D_{deep-1}$ , GMST estimates are calculated following the method of Hansen et al. (2013),  
315 which utilises only the deep ocean benthic foraminifera  $\delta^{18}\text{O}$  dataset, and we refer the reader  
316 to that study for a detailed justification of the approach. Briefly, GMST is scaled directly to  
317 deep ocean temperature before the Pliocene. Specifically,  $\Delta\text{GMST} = \Delta\text{BWT}$  prior to  $\sim 5.3$  Ma,  
318 where early Pliocene BWT and GMST was calculated following Eq. 3.5, 3.6, and 4.2 of Hansen  
319 et al. (2013). As such, the calculations presented here differ from those of Hansen et al. (2013)  
320 only in that we use a more recent benthic  $\delta^{18}\text{O}$  compilation and a different equation to convert  
321  $\delta^{18}\text{O}$  to temperature in the ice-free Paleogene. For each time-slice, the reported uncertainty  
322 incorporates the mean calibration uncertainty and standard deviation ( $1\sigma$ ) in calculated BWTs.

323

### 324 2.3. Dataset $D_{comb}$

325 Dataset  $D_{comb}$  uses a combination of (tropical) surface- and deep-water temperature  
326 estimates. The deep ocean dataset ( $D_{deep}$ ) is identical to that described in Section 2.2. The  
327 tropical SST dataset utilises all relevant surface ocean proxy data from the DeepMIP  
328 database, i.e. those with a palaeolatitude in the magnetic reference frame within  $30^\circ$  of the  
329 equator. An expanded definition of the tropics is used as tropical SST reconstructions are  
330 relatively sparse;  $30^\circ$  was chosen as it retains tropical SST data from several proxies for all  
331 three intervals whilst SST seasonality remains relatively low within these latitudinal bounds.

332

#### 333 2.3.1. $D_{comb-1}$

334 For  $D_{comb-1}$ , GMST estimates are calculated for each time interval based on the difference  
335 between tropical SSTs and deep-ocean BWTs (Evans et al., 2018), such that:

336

$$337 \quad \text{GMST} = 0.5(\overline{\text{tropical SST}} + \overline{\text{BWT}}) \quad (5)$$

338



339 The fundamental assumptions of this approach are that: 1) GMST can be approximated by  
340 global mean SST, 2) global mean SST is equivalent to the mean of the tropical and high  
341 latitude regions, and 3) benthic temperatures are representative of high latitude surface  
342 temperatures. Applying these assumptions to the modern ocean would generate a GMST  
343 estimate within  $\sim 1^\circ\text{C}$  of measured and a modern latitudinal SST gradient within  $\sim 1^\circ\text{C}$  of the  
344 surface ocean dataset (as discussed in Evans *et al.*, 2018).

345 Probability distributions for each time interval were computed as follows. In the case  
346 of the tropical SST data, 1000 subsamples were taken, following which a random normally  
347 distributed error was added to each data point in the DeepMIP compilation, including both  
348 calibration uncertainty and variance in the data where multiple reconstructions are available  
349 for a given site and time interval. Mean tropical SST was calculated for each of these  
350 subsamples. To provide a BWT dataset of the same size as the subsampled tropical SST  
351 data, 1000 normally distributed values were calculated for each time interval, based on the  
352 mean  $\pm 1\text{SD}$  variation of the pooled benthic  $\delta^{18}\text{O}$  data from all sites including calibration  
353 uncertainty.

354

### 355 **3. Results**

#### 356 3.1. $D_{\text{surf-1 to -4}}$

357 GMST estimates ( $D_{\text{surf-default}}$ ) during the latest Paleocene ( $n = 4$ ) range between  $25.7$  and  
358  $26.8^\circ\text{C}$  (Table 3). GMST estimates ( $D_{\text{surf-default}}$ ) during the PETM ( $n = 4$ ) range between  $31.1$   
359 and  $33.6^\circ\text{C}$  (Table 3). GMST estimates ( $D_{\text{surf-default}}$ ) during the EECO ( $n = 4$ ) range between  
360  $25.4$  and  $29.0^\circ\text{C}$  (Table 3). All four methods indicate that: 1) the PETM is warmer than the  
361 latest Paleocene (by  $\sim 4$  to  $9^\circ\text{C}$ ) and: 2) the PETM is warmer than the EECO (by  $\sim 3$  to  $7^\circ\text{C}$ ).  
362 GMST estimates derived using  $D_{\text{surf-Frosty}}$  (i.e. which include planktonic foraminifera  $\delta^{18}\text{O}$   
363 values) are consistently lower (up to  $3.5^\circ\text{C}$ ) than those derived using  $D_{\text{surf-default}}$ . GMST  
364 estimates derived using  $D_{\text{surf-NoTEX}}$  (i.e. which exclude  $\text{TEX}_{86}$  estimates) are also consistently



365 lower (up to  $\sim 2^{\circ}\text{C}$ ) than those derived using  $D_{surf\_default}$ . GMST estimates derived using  $D_{surf-}$   
366  $NoMBT$  (i.e. which exclude MBT/CBT values from marine sediments) are higher than GMST  
367 estimates derived using  $D_{surf\_default}$  (up to  $1^{\circ}\text{C}$ ). GMST estimates derived using  $D_{surf-}$   
368  $NoMammal$  (i.e. which exclude  $\delta^{18}\text{O}$  mammal or paleosol estimates) are similar to GMST  
369 estimates derived using  $D_{surf\_default}$  ( $\pm 0.5^{\circ}\text{C}$ ), with the exception of  $D_{surf-1}$  during the EECO  
370 which is  $\sim 3^{\circ}\text{C}$  higher when  $\delta^{18}\text{O}$  mammal or paleosol values are excluded.

371

### 372 3.2. $D_{deep-1}$

373 GMST estimates ( $D_{deep}$ ) during the latest Paleocene, PETM and EECO average  $24.3^{\circ}\text{C}$   
374 ( $\pm 1.8^{\circ}\text{C}$ ),  $30.2^{\circ}\text{C}$  ( $\pm 9.2^{\circ}\text{C}$ ) and  $28.0^{\circ}\text{C}$  ( $\pm 2.6^{\circ}\text{C}$ ), respectively (Table 3). This method indicates  
375 that: 1) the PETM is warmer than the latest Paleocene (by  $\sim 6^{\circ}\text{C}$ ) and, 2) the PETM is warmer  
376 than the EECO (by  $\sim 2^{\circ}\text{C}$ ).

377

### 378 3.3. $D_{comb-1}$

379 GMST estimates ( $D_{comb}$ ) during the latest Paleocene, PETM and EECO average  $21.0^{\circ}\text{C}$   
380 ( $\pm 1.7^{\circ}\text{C}$ ),  $26.0^{\circ}\text{C}$  ( $\pm 5.0^{\circ}\text{C}$ ) and  $22.7^{\circ}\text{C}$  ( $\pm 2.3^{\circ}\text{C}$ ), respectively (Table 3). This method indicates  
381 that: 1) the PETM is warmer than the latest Paleocene (by  $\sim 5^{\circ}\text{C}$ ) and, 2) the PETM is warmer  
382 than the EECO (by  $\sim 3^{\circ}\text{C}$ ).

383

## 384 4. Discussion

### 385 4.1. Influence of different proxy datasets upon GMST estimates

386 To explore the importance of other datasets upon our reconstructed latest Paleocene, PETM  
387 and EECO GMST estimates, we conducted a series of subsampling experiments. This was  
388 performed for methods  $D_{surf-1}$ , -2, -3 and -4. In the first subsampling experiment, the inclusion  
389 of  $\delta^{18}\text{O}$  SST estimates from recrystallized planktonic foraminifera yields lower GMST



390 estimates (ca.  $\sim 1$  to  $3^{\circ}\text{C}$ ; e.g. Figure 6b). This is consistent amongst all four methods and  
391 agrees with previous studies which indicate that  $\delta^{18}\text{O}$  values from recrystallized planktonic  
392 foraminifera are significantly colder than estimates derived from the  $\delta^{18}\text{O}$  value of well-  
393 preserved foraminifera, foraminiferal Mg/Ca ratios and clumped isotope values from larger  
394 benthic foraminifera (Hollis et al., 2019). The removal of  $\text{TEX}_{86}$  also results in lower GMST  
395 estimates (ca  $2\text{-}4^{\circ}\text{C}$ ; e.g. Figure 6c) across all methodologies. This is consistent with previous  
396 studies which indicate that  $\text{TEX}_{86}$  gives slightly higher SSTs than other proxies, especially in  
397 the mid-to-high latitudes (e.g. Hollis et al., 2012; Inglis et al. 2015). This implies that the  
398 inclusion of  $\text{TEX}_{86}$  may lead to a slight warm bias in GMST estimates.

399         The input of brGDGTs from archives other than mineral soils or peat can bias LAT  
400 estimates towards lower values (Inglis et al., 2017; Hollis et al., 2019) and the removal of  
401 MBT'/CBT-derived LAT estimates leads to a warm bias in GMST. However, excluding these  
402 proxies has a relatively minor impact on GMST ( $\sim 0.5^{\circ}\text{C}$ ). This is because in regions where  
403 MBT'/CBT values are discarded (e.g. the SW Pacific), there are other proxies (e.g. pollen  
404 assemblages, leaf floral) which yield comparable LAT estimates. The removal of  $\delta^{18}\text{O}$  values  
405 from paleosols or mammals also leads to a small warm bias in GMST estimates ( $\sim 0.5^{\circ}\text{C}$ ).  
406 Intriguingly,  $D_{\text{surf}}-1$  yields much higher GMST estimates ( $\sim 3^{\circ}\text{C}$  higher than  $D_{\text{surf}}\text{-default}$ ) when  
407  $\delta^{18}\text{O}$  values from paleosols or mammals are excluded. This is attributed to the inclusion of two  
408 "cold" LAT estimates from the Salta Basin, NW Argentina (Hyland et al., 2017) which overly  
409 influence GMST (Figure 6e; Figure 7b-c;). These estimates are derived from the salinization  
410 index (SAL) (Sheldon et al., 2002) and the paleosol weathering index (PWI) (Gallagher and  
411 Sheldon, 2013), both of which yield a cold bias in the original DeepMIP database (Hollis et al.  
412 2019).

413

#### 414 **4.2. Intercomparison of methods for calculating GMST**

415 For consistency, the following section discusses 'baseline' GMST estimates only. During the  
416 latest Paleocene and PETM, GMST estimates derived from  $D_{\text{surf}}$  average  $\sim 27$  and  $32^{\circ}\text{C}$ ,





417 respectively (Figure 8). These values agree with previous studies analysing the latest  
418 Paleocene (~27°C; Zhu et al., 2019) and PETM (~32°C; Zhu et al., 2019). During the EECO,  
419 GMST estimates calculated using  $D_{surf}$  range between ~25 and 28°C (Figure 8). These values  
420 are comparable to previous estimates from similar time intervals (ca. 29 to 30°C; Huber and  
421 Caballero, 2011; Caballero and Huber, 2013; Zhu et al., 2019), but are up to 4°C lower. This  
422 cooling can be attributed to two factors. Firstly, our EECO dataset is largely comprised of land  
423 air temperature proxy data (n = 80 LAT estimates; n = 27 SST estimates) which can suffer  
424 from a cold bias (Hollis et al., 2019). To explore whether LAT estimates skew GMST estimates  
425 towards lower values, we derived GMST using only SST or only LAT data. This analysis was  
426 performed using  $D_{surf-1}$ ,  $D_{surf-2}$  and  $D_{surf-4}$  and indicates that the GMST estimate are ~2 to 4°C  
427 lower when calculated using LAT proxies only. This may be less pronounced in previous  
428 studies (i.e. Zhu et al. 2019) because they utilise a different compilation with fewer LAT  
429 estimates (n = 51; Huber and Caballero, 2011). Secondly, the inclusion of  $\delta^{18}\text{O}$  values from  
430 paleosols or mammals leads to a cold bias in GMST estimates. For  $D_{surf-1}$ , a direct comparison  
431 of new and prior estimates (Caballero and Huber, 2013) can be made in which the only change  
432 has been the use of a newer data compilation. For this new method (Figure 7), the EECO is  
433 ~3.5°C colder than previous estimates (29.75°C; Caballero and Huber, 2013). Given that the  
434 floristic LAT estimates are identical between the DeepMIP compilation and the older  
435 compilation, this strongly suggests that the cooling with respect to older estimates is largely  
436 due to the incorporation of paleosol temperature estimates. This suggests that more  
437 investigation of the systematic cold bias introduced by paleosols is warranted.

438 During the latest Paleocene, PETM and EECO, GMST estimates calculated using  
439  $D_{deep}$  average ~24°C ( $\pm 1.8^\circ\text{C}$ ), ~30 ( $\pm 9.2^\circ\text{C}$ ) and ~28°C ( $\pm 2.6^\circ\text{C}$ ), respectively (Figure 8).  
440 These estimates are comparable to those derived via surface temperature proxies (Table 3).  
441 GMST estimates from the EECO are also comparable to previous estimates based on globally  
442 distributed benthic foraminifera data (~28°C; Hansen et al., 2013). This implies that benthic  
443 foraminiferal  $\delta^{18}\text{O}$  values could be used to provide the 'fine temporal structure' of Cenozoic



444 temperature change (Lunt et al., 2016; Hansen et al., 2013). However, we also urge caution  
445 as this approach scales GMST directly to BWT prior to the Pliocene, and therefore assumes  
446 that the characteristics of polar amplification are constant through time or balanced by other  
447 processes. We also note that GMST estimates for the PETM are associated with a large  
448 uncertainty. This is due to differences in  $\delta^{18}\text{O}$  values between sites and an overall lack of  
449 PETM benthic data ( $n = 22$  from 3 sites) rather than an inherent uncertainty in the proxy or  
450 method of calculating GMST.

451 During the latest Paleocene, PETM and EECO, GMST estimates calculated using  
452  $D_{comb}$  average  $\sim 21^\circ\text{C}$  ( $\pm 1.7^\circ\text{C}$ ),  $\sim 26$  ( $\pm 5.0^\circ\text{C}$ ) and  $\sim 23^\circ\text{C}$  ( $\pm 2.3^\circ\text{C}$ ), respectively (Figure 8).  
453 These estimates are consistently lower (by  $\sim 2$  to  $5^\circ\text{C}$ ) than GMST estimates derived using  
454  $D_{surf}$  ( $n = 4$ ) and  $D_{deep}$  ( $n = 1$ ). We suggest this mismatch could be related to two factors. First,  
455 if deep water formation preferentially takes place during the winter months, GMST estimates  
456 will be biased towards lower values. Secondly, there are relatively few tropical SST estimates  
457 during the EECO ( $n = 10$  sites), such that  $D_{comb}$  may not be fully representative of actual  
458 tropical warmth.

459

#### 460 **4.3. A 'best estimate' of GMST during the latest Paleocene, PETM and EECO**

461 To derive the 'best estimate' of GMST during the latest Paleocene, PETM and EECO, we  
462 combine GMST estimates from each 'baseline' experiment (except  $D_{surf-1}$  for the EECO which  
463 uses  $D_{surf-NoMamma}$ ) and calculate a weighted average (Figure 8). This approach is useful  
464 because it assigns lower confidence to GMST estimates associated with larger uncertainties  
465 (e.g.  $D_{deep-1}$  during the PETM). The reported uncertainty is the reciprocal square root of the  
466 sum of all the individual weights. Sequential removal of one time series at a time (jackknife  
467 resampling) was performed to examine the influence of a single method upon the average  
468 GMST estimate. Jackknifing reveals that that no single method overly influences the mean  
469 GMST during the latest Paleocene, PETM or EECO (ca.  $\pm 1.0^\circ\text{C}$ ).



470 We find that the average GMST estimate for the latest Paleocene, PETM and EECO  
471 are 25.7°C ( $\pm 0.6^\circ\text{C}$ ), 32.7°C ( $\pm 0.8^\circ\text{C}$ ) and 27.3°C ( $\pm 0.5^\circ\text{C}$ ), respectively (Figure 8). Assuming  
472 a preindustrial GMST of 14°C, our average GMST estimates indicate that the latest  
473 Paleocene, PETM and EECO are +11.7°C, +18.7°C and +13.3°C warmer than pre-industrial,  
474 respectively. The GMST anomaly for the EECO is skewed to cooler values than previous work  
475 ( $\sim 15^\circ\text{C}$  warmer than pre-industrial; Caballero and Huber, 2013; Zhu et al., 2019) but lies within  
476 the range quoted previously in the IPCC AR5 (12.7°C warmer than pre-industrial). On  
477 average, GMST increases by  $\sim 6$  to 7°C between the latest Paleocene and PETM, in keeping  
478 with previous estimates (Frieling et al., 2019; Dunkley Jones, 2013). The PETM is  
479 approximately 5°C warmer than the EECO. This is higher than previously suggested ( $\sim 3^\circ\text{C}$ ;  
480 Zhu et al., 2019) and may related to a cold bias in EECO GMST estimates (see Section 4.2).

481

#### 482 **4.4. Equilibrium climate sensitivity during the latest Palaeocene, PETM and EECO**

483 Equilibrium climate sensitivity (ECS) can be defined as the equilibrium change in global near  
484 surface air temperature, resulting from a doubling in atmospheric CO<sub>2</sub>. Various “flavours” of  
485 ECS exist, some of which specifically exclude various feedback processes not always included  
486 in climate models, such as those associated with ice sheets, vegetation, or aerosols (Rohling  
487 et al., 2012). ECS may also be state-dependent (Caballero and Huber, 2013) and there is no  
488 reason to expect it has not changed with time. Therefore, direct comparison of ECS in the past  
489 to modern conditions is a fraught enterprise. For our purposes we define a ‘bulk ECS’ as being  
490 a gross estimate of ECS across time between our three intervals and preindustrial. Such  
491 calculations have been performed previously (Shaffer et al., 2016; Anagnostou et al., 2016)  
492 and they provide some constraint on the range of climate sensitivity values that are relevant  
493 for near-modern prediction (Rohling et al., 2012). For example, Anagnostou et al. (2016)  
494 indicated that early Eocene ECS (excluding ice sheet feedbacks) falls within the range 2.1–  
495 4.6 °C per CO<sub>2</sub> doubling with maximum probability for the EECO of 3.8 °C. These values (2.1–  
496 4.6 °C per CO<sub>2</sub> doubling) are similar to the IPCC ECS range (1.5–4.5 °C at 66% confidence).



497 Here we calculate bulk ECS estimates using the change in GMST and CO<sub>2</sub> in the latest  
498 Paleocene, PETM and EECO intervals with reference to the pre-industrial. Following the  
499 approach of Anagnostou et al. (2016) and using the forcing equation of Byrne and Goldblatt  
500 (2014), we first determine the relative change in climate forcing relative to pre-industrial ( $\Delta F_{\text{CO}_2}$ -  
501 vs-PI):

502

$$503 \quad \Delta F_{\text{CO}_2\text{-vs-PI}} = 5.32\ln(C_i/C_{PI}) + (0.39[\ln(C_i/C_{PI})]^2) \quad [6]$$

504

505 where  $C_{PI}$  is the atmospheric CO<sub>2</sub> concentration during pre-industrial (278 ppm) and  $C_i$  refers  
506 to the CO<sub>2</sub> reconstruction at a particular time in the Eocene. The mean proxy estimate of  
507 CO<sub>2</sub> for the PETM is ~2200 ppmv (+1904/-699 ppmv; Gutjahr et al., 2017). The mean proxy  
508 estimate of CO<sub>2</sub> for the LP is ~870 ppmv (Gutjahr et al., 2017; n.b. no published uncertainty  
509 available; here we assign an uncertainty of ±400ppm). The mean proxy estimate of CO<sub>2</sub> for  
510 the EECO is ~1625 ppmv (±750 ppmv) (Anagnostou et al., 2016; Hollis et al., 2019). To  
511 calculate bulk ECS, we then use radiative forcing from a doubling of CO<sub>2</sub> from Byrne and  
512 Goldblatt (2014) to translate CO<sub>2</sub> into forcing relative to preindustrial ( $\Delta F_{\text{CO}_2}$ ):

513

$$514 \quad \text{ECS} = (\Delta \text{GMST}) / \Delta F_{\text{CO}_2\text{-vs-PI}} * 3.875 \quad [7]$$

515

516 Some of the temperature anomaly of the latest Paleocene, PETM, and EECO is caused not  
517 by CO<sub>2</sub> but by the different paleotopography, paleobathymetry, and solar constant compared  
518 with preindustrial. Furthermore, we choose here to calculate an ECS that explicitly excludes  
519 feedbacks associated with vegetation, ice sheets, and aerosols, i.e.  $S_{[\text{CO}_2, \text{LI}, \text{VG}, \text{AE}]}$  in the  
520 nomenclature of Rohling et al (2012). To account for these effects, we subtract a value of 4.5°C  
521 (Caballero and Huber, 2013; Zhu et al. 2019) from the GMST in Table 3. This value of 4.5°C  
522 is based upon a comparison of preindustrial and Eocene simulations (both 1x CO<sub>2</sub>) conducted



523 with CESM1.2 (Zhu et al., 2019), which incorporates the paleogeographic, solar constant, ice  
524 sheet, vegetation, aerosol, and ice sheet changes from preindustrial to Eocene. This value is  
525 similar to previous studies which attribute  $\sim 4$  to  $6^\circ\text{C}$  to the non- $\text{CO}_2$  forcings and feedbacks  
526 (Anagnostou et al., 2016; Caballero and Huber, 2013, Lunt et al., 2012). However, we note  
527 that the sensitivity to these Eocene boundary conditions is likely model-dependant and this  
528 value will likely differ between model simulations. The uncertainties in our estimated ECS are  
529 the products of 10,000 realizations of the latest Paleocene, PETM and EECO  $\text{CO}_2$  values and  
530 the respective  $\Delta\text{GMST}$  estimate (the mean estimate and uncertainty in Table 3) based on  
531 randomly sampling each variable within its 95% confidence interval uncertainty envelope

532 We estimate  $S_{[\text{CO}_2, \text{LI}, \text{VG}, \text{AE}]}$  for the latest Paleocene, EECO and PETM to range between  
533 0.73 and 1.12 (66% confidence; Figure 9). This yields bulk ECS estimates for the latest  
534 Paleocene, EECO and PETM compared to modern which range between 2.8 to  $4.8^\circ\text{C}$  per  
535 doubling  $\text{CO}_2$  (66% confidence). These values are comparable to previous estimates from the  
536 early Eocene which also account for paleogeography and other feedbacks ( $\sim 2.1$  to  $4.6^\circ\text{C}$ ;  
537 Anagnostou et al., 2016) and fall within the modern ECS range predicted by the IPCC (1.5 to  
538  $4.5^\circ\text{C}$  per doubling  $\text{CO}_2$ ). However, care must be exercised when relating geological estimates  
539 to modern climate predictions (e.g. Rohling et al., 2012). In addition, published  $\text{CO}_2$  estimates  
540 remain uncertain (especially during the latest Paleocene and PETM) and new high-fidelity  
541 records are required to accurately constrain ECS during these super warm climates.

542

## 543 **5. Conclusions**

544 Using six different methods, we have quantified global mean surface temperatures (GMST)  
545 during the latest Paleocene, PETM and EECO. GMST was calculated within a coordinated,  
546 experimental framework and utilised three different input datasets. After evaluating the impact  
547 of different proxy datasets upon GMST estimates, we combined all six methodologies to derive  
548 an average GMST value during the latest Paleocene, PETM and EECO. Our results indicate  
549 high GMSTs during the latest Paleocene ( $25.7^\circ\text{C} \pm 0.6^\circ\text{C}$ ), PETM ( $32.7^\circ\text{C} \pm 0.8^\circ\text{C}$ ) and EECO



550 (27.3°C ± 0.5°C). Assuming a preindustrial GMST of 14°C, our average GMST estimates for  
551 the latest Paleocene, PETM and EECO are 11.7°C, 18.7°C and 13.3°C higher than pre-  
552 industrial, respectively. Using our 'combined' GMST estimates, we then estimated a bulk ECS  
553 during the latest Paleocene, PETM and EECO. Our results range between 2.8 to 4.8°C (at  
554 66% confidence) per doubling of atmospheric CO<sub>2</sub> when feedbacks associated with ice  
555 sheets, vegetation, and aerosols are accounted for. Taken together, our study improves our  
556 characterisation of the global mean temperature of these key time periods, allowing future  
557 climate change to be put into the context of past changes, and allowing us to provide a refined  
558 estimate of ECS.

559

#### 560 **Data availability**

561 Data can be accessed via the online supporting information, via [www.pangaea.de/](http://www.pangaea.de/), or from  
562 the author (email: [gordon.inglis@soton.ac.uk](mailto:gordon.inglis@soton.ac.uk)).

563

#### 564 **Authorship tiers and contributions**

565 Authorship of this manuscript is organized into three tiers according to the contributions of  
566 each individual author. Inglis (Tier I) organized the structure and writing of the manuscript,  
567 contributed to all sections of the text and designed the figures. Tier II authors (listed  
568 alphabetically following Inglis) assumed a leading role by contributing methodologies used in  
569 the text. Tier III authors (listed alphabetically following Wilkinson) contributed intellectually to  
570 the text and figure design.

571

#### 572 **Declaration of competing interest**

573 The authors declare that they have no known competing financial interests or personal  
574 relationships that could have appeared to influence the work reported in this paper.

575



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581

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Label in Fig. 1	Source	Time window	GMST (°C)	Uncertainty	Proxy system
1a	Farnsworth et al. (2019)	EE	23.4	±3.2	δ <sup>18</sup> O planktonic
1b	Farnsworth et al. (2019)	EE	37.1	±1.4	δ <sup>18</sup> O planktonic + TEX <sub>86</sub>
2a	Zhu et al. (2019)	LP	27	n/a	Multiple
2b	Zhu et al. (2019)	EEO	29	±3	Multiple
2c	Zhu et al. (2019)	PETM	32	n/a	Multiple
3	Caballero and Huber (2013)	EE	29.5	±2.6	Multiple
4	Hansen et al (2013)	EE	28	n/a	δ <sup>18</sup> O benthic
5	Cramwinckel et al. (2018)	EE	29.3	n/a	Multiple

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740 **Table 1:** Previous studies that have determined GMST for the early Eocene (EE), EEO,  
741 PETM or latest Paleocene (LP). n/a indicates that no error bars were reported in the original  
742 publications.

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Experiment	Description
$D_{surf}^{default}$	All SST and LAT data compiled in Hollis et al. (2019) but excluding recrystallized planktonic foraminifera $\delta^{18}O$ values
$D_{surf}^{Frosty}$	$D_{surf}^{default}$ but including recrystallized planktonic foraminifera $\delta^{18}O$ values
$D_{surf}^{NoTEX}$	$D_{surf}^{default}$ but excluding $TEX_{86}$ values
$D_{surf}^{NoMBT}$	$D_{surf}^{default}$ but excluding MBT(°)/CBT values from marine sediments
$D_{surf}^{NoMammal}$	$D_{surf}^{default}$ but excluding mammal and paleosol $\delta^{18}O$ values

757 **Table 2:** Default and optional subsampling experiments applied to  $D_{surf}$

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GMST (°C)							
	D <sub>surf-1</sub>	D <sub>surf-2</sub>	D <sub>surf-3</sub>	D <sub>surf-4</sub>	D <sub>deep-1</sub>	D <sub>comb-1</sub>	Average
LP	25.9 (±1.0)	26.8 (±1.2)	25.7 (±6.0)	27.6 (±1.3)	24.3 (±1.1)	21.0 (±1.7)	25.7 (±0.6)
PETM	33.6 (±1.2)	33.4 (±1.6)	31.2 (±7.6)	31.3 (±1.6)	30.2 (±9.2)	26.0 (±5.0)	32.7 (±0.8)
EECO	26.3 (±0.7)	26.7 (±0.9)	27.9 (±7.0)	25.4 (±1.1)	28.0 (±2.6)	22.7 (±2.3)	27.3 (±0.5)

774

775 **Table 3:** GMST for latest Paleocene (LP), PETM and EECO. Reported GMST estimates utilise  
776 'baseline' experiments except  $D_{surf-1}$  during the EECO which uses  $D_{surf-NoMammal}$ .

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	ECS (°C) (66% confidence)	ECS (°C) (95% confidence)
Latest Paleocene	3.9 – 4.8	3.6 – 5.5
PETM	3.5 – 4.4	3.2 – 5.5
EECO	2.8 – 3.8	2.6 – 5.2

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792 **Table 4:** Estimates of ECS (66% and 95% confidence) during the latest Paleocene, PETM  
793 and EECO.

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811 **Figure captions:**

812 **Figure 1:** Published GMST estimates during the early Paleogene (57 to 48 Ma). Dots  
813 represent average values. The horizontal limits on the individual dots represent the reported  
814 error. y-Axis labels refer to previous estimates (see Table 1).

815

816 **Figure 2:** Location of proxies within the surface temperature dataset ( $D_{surf}$ ). A) SST proxies  
817 with time intervals indicated as followed: black circles, all three-time intervals represented.  
818 Red circles: PETM  $\pm$  latest Paleocene intervals; orange circles, EECO interval (b) Terrestrial  
819 sites with time intervals indicated as in (a) and green circles, LP only.

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821 **Figure 3:** An illustration of Method  $D_{surf-2}$  for 2 sites: (a) Tanzania in the EECO as diagnosed  
822 using HadCM3L, and (b) Mid Waipara in the PETM as diagnosed using CCSM3. The vertical  
823 dashed line shows  $\langle T \rangle^{inferred}$  and the horizontal dashed line shows  $T^{proxy}$ , which intercept at  
824 the orange dot. The dark blue dots show the intercept of  $T^{low}$  with  $\langle T^{low} \rangle$ , and the red dots  
825 show the intercept of  $T^{high}$  with  $\langle T^{high} \rangle$ .

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827 **Figure 4:** Inferred global mean temperature ( $\langle T \rangle^{inferred}$ ) for each EECO-aged proxy in the  
828 DeepMIP database using  $D_{surf-2}$ , as diagnosed using CCSM3. The final estimate of global  
829 mean temperature is the average of all the individual sites.

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831 **Figure 5:** Predicted surface warming by Gaussian process regression using  $D_{surf-3}$  for the (a)  
832 latest Paleocene, (b) PETM and (c) EECO. Anomalies are relative to the present-day zonal  
833 mean surface temperature. Circles indicate all available SST and LAT proxy data for the  
834 respective time slice that were used to train the model. Circles for locations where multiple  
835 proxy reconstructions are available are slightly shifted in latitude for improved visibility.



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837 **Figure 6:** Predicted surface warming by Gaussian process regression using  $D_{surf-3}$  for the  
838 EECO for the five core experiments (see Table 2). Anomalies are relative to the present-day  
839 zonal mean surface temperature. Circles indicate all available SST and LAT proxy data for the  
840 respective time slice and experiment that were used to train the model. Circles for locations  
841 where multiple proxy reconstructions are available are slightly shifted in latitude for improved  
842 visibility.

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844 **Figure 7:** An illustration of Method  $D_{surf-1}$  during the EECO. (a) Modelled early Eocene (2240  
845 ppm) temperatures utilising CCSM3 (b) Interpolated absolute SST reconstructions, (c) Data-  
846 model difference between (a) and (b).

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848 **Figure 8:** Summary of GMST estimates for the (a) latest Paleocene, (b) Paleocene-Eocene  
849 Thermal Maximum and (c) early Eocene Climatic Optimum. Error bars on each individual  
850 method are the standard deviation, except  $D_{surf-1}$  and  $D_{surf-2}$  which use the standard error.  
851 Error bar on weighted average is the reciprocal square root of the sum of all the individual  
852 weights.

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854 **Figure 9:** Probability density function of bulk ECS during the latest Paleocene, PETM and  
855 EECO that explicitly accounts for non-CO<sub>2</sub> forcings of palaeography and solar constant, and  
856 feedbacks associated with land ice, vegetation, and aerosols (Zhu et al., 2019), i.e.  
857  $S_{[CO_2,LI,VG,AE]}$  in the nomenclature of Rohling et al (2012).

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Figure 1

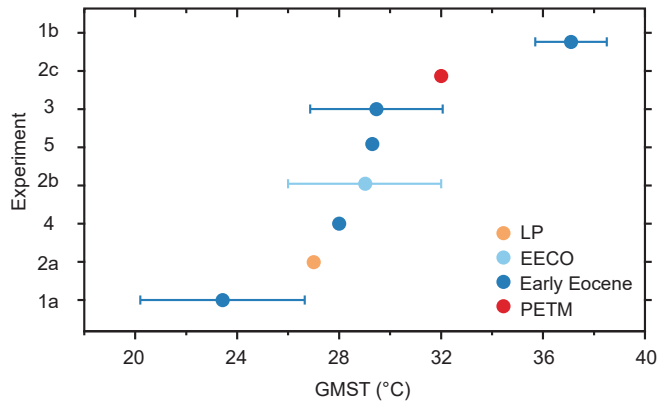




Figure 2

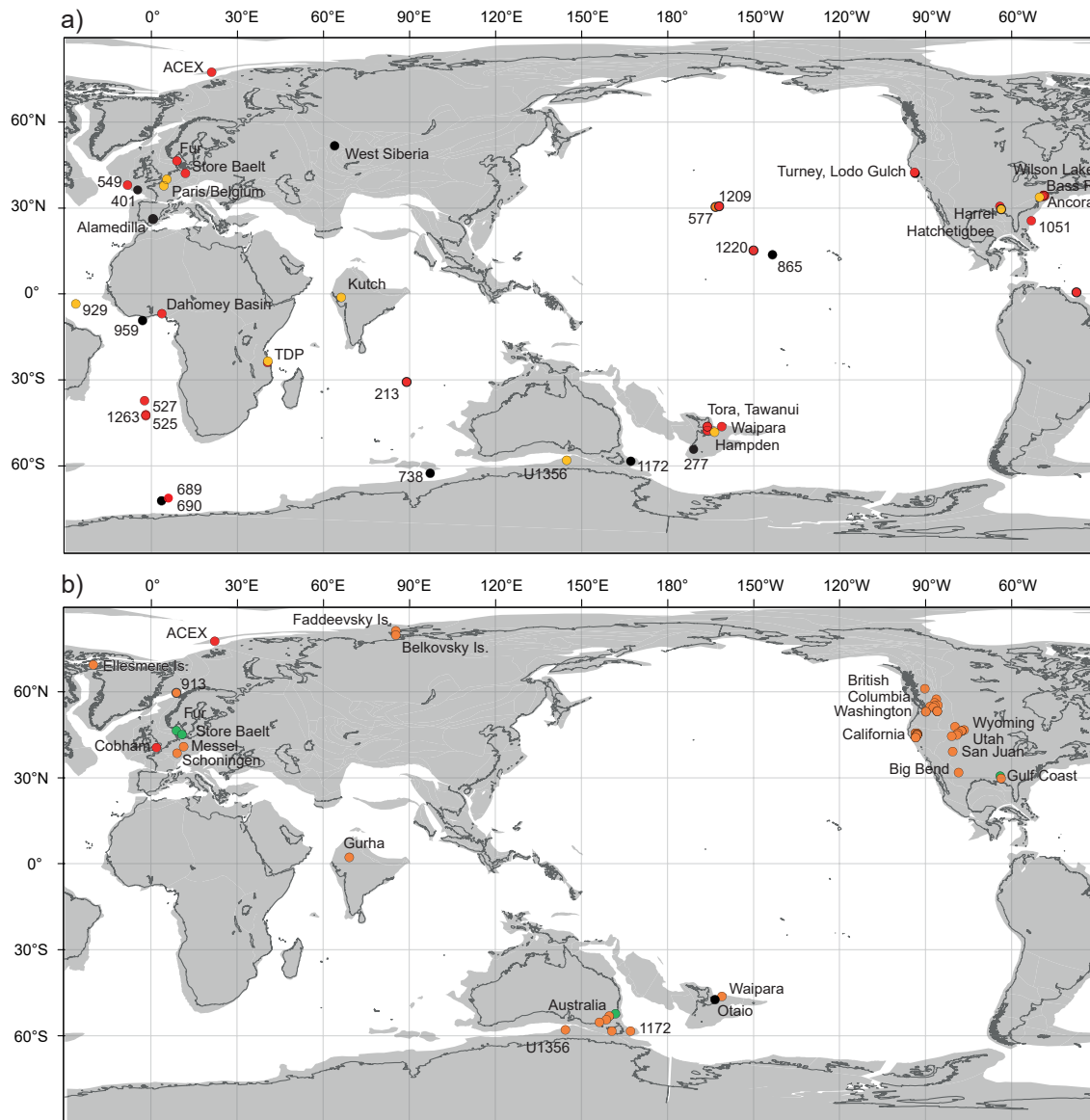




Figure 3

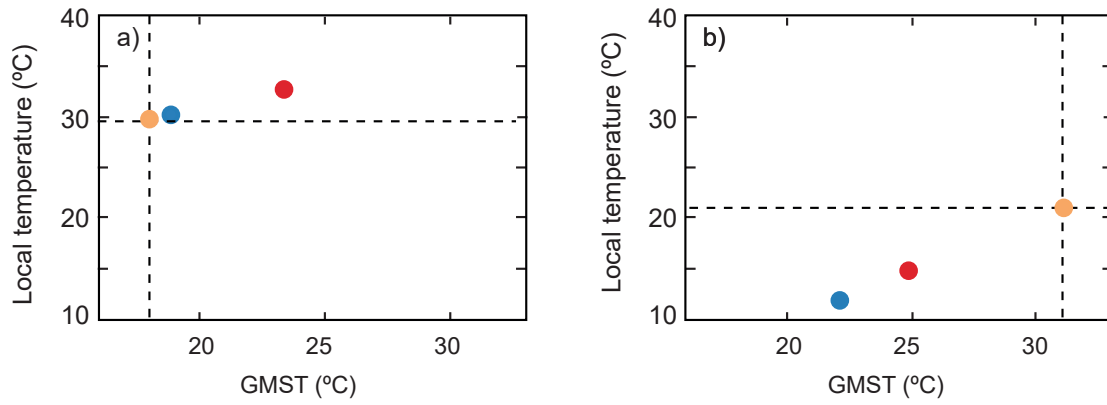




Figure 4

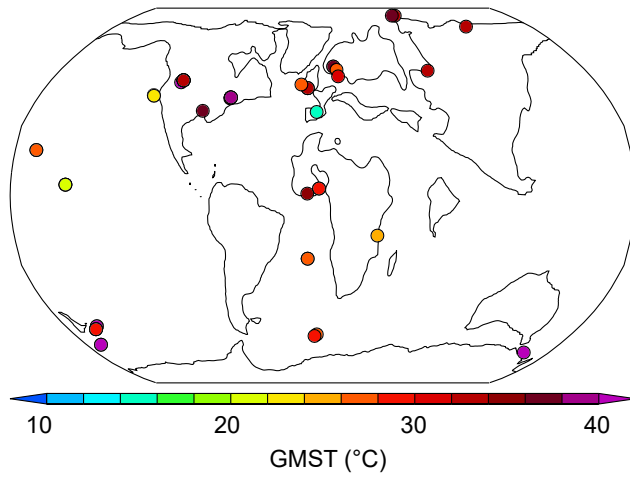




Figure 5

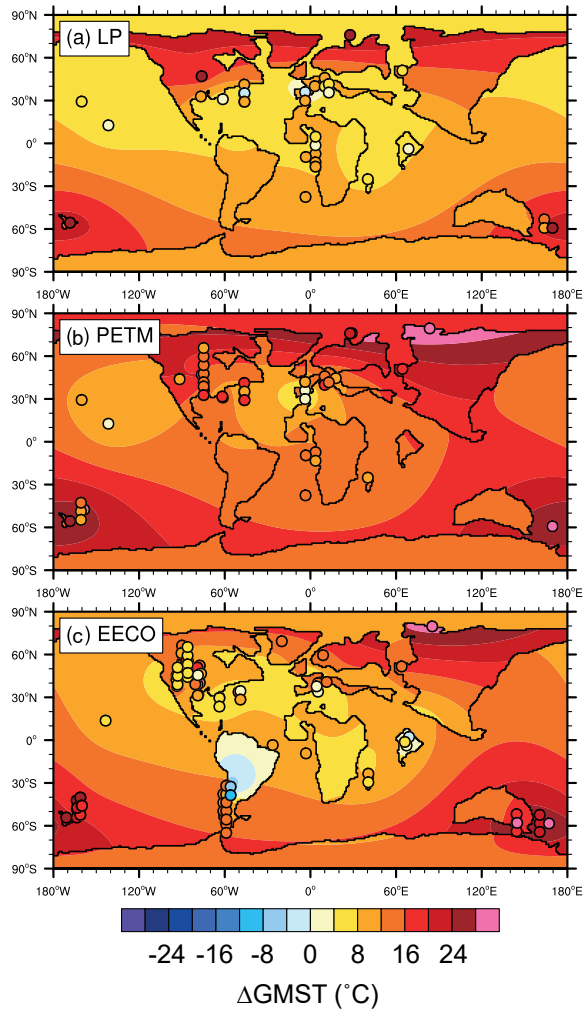




Figure 6

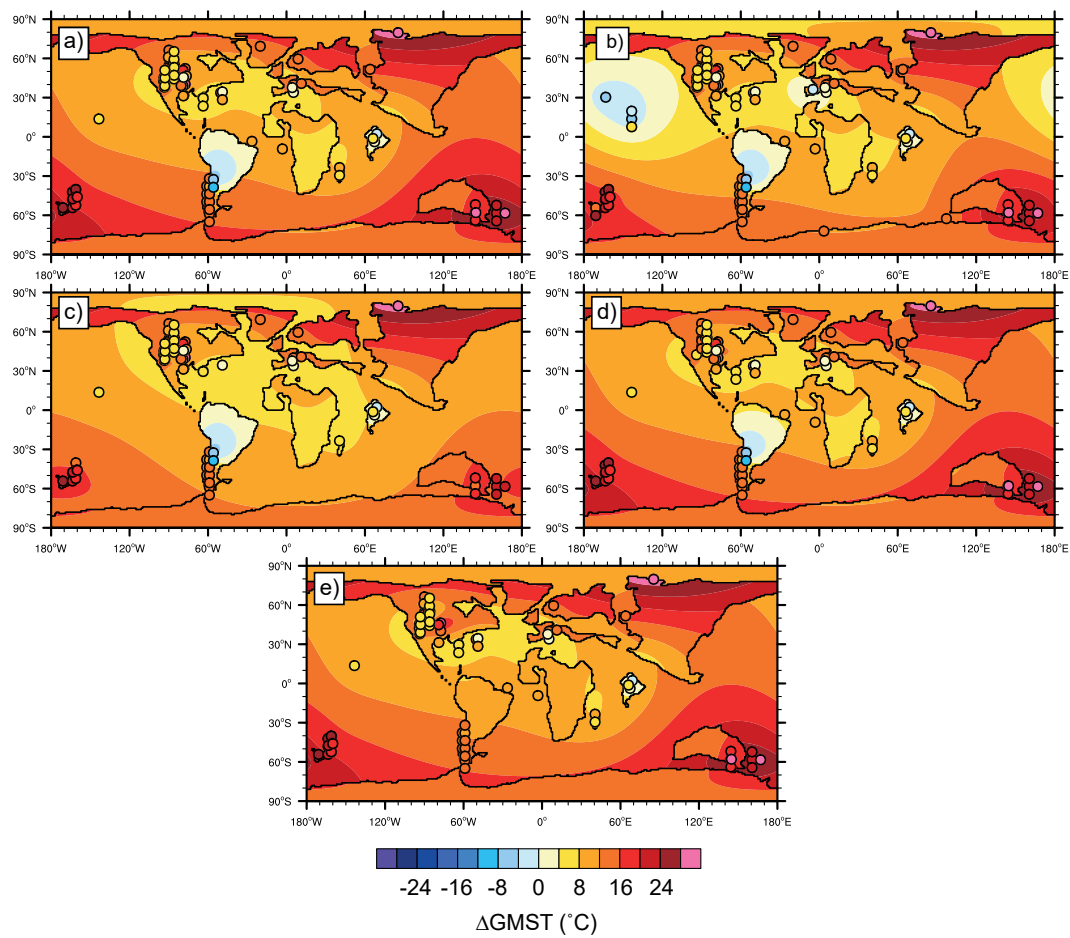






Figure 7

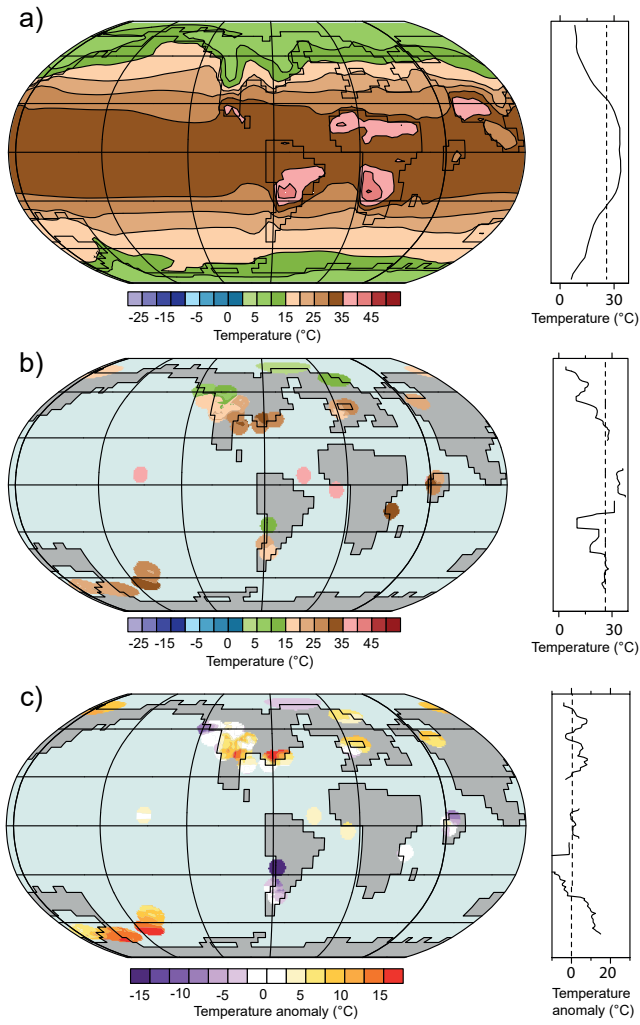




Figure 8

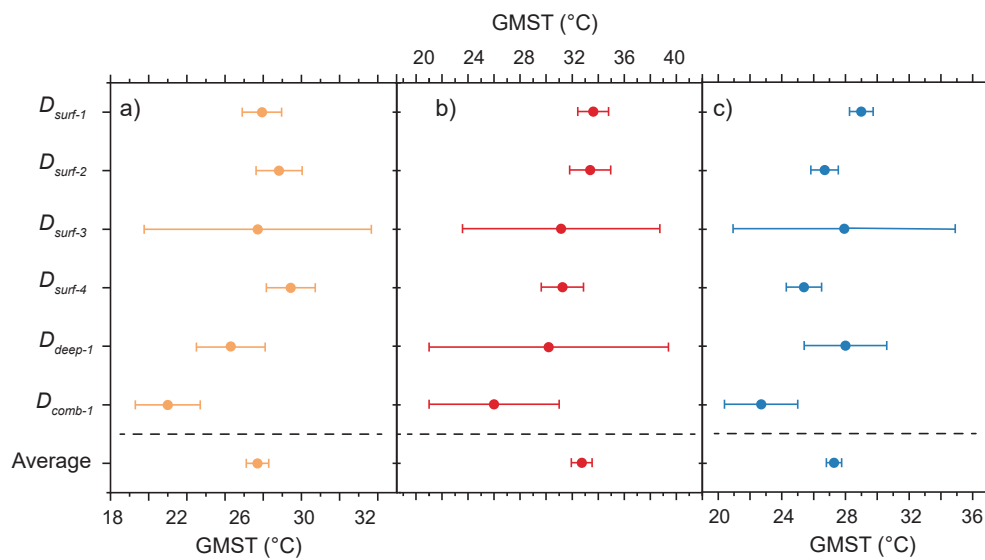




Figure 9

