PUBLISHED FOR SISSA BY 2 SPRINGER

Received: October 3, 2018 Accepted: November 9, 2018 PUBLISHED: November 22, 2018

The dS swampland conjecture with the electroweak symmetry and QCD chiral symmetry breaking

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ABSTRACT: The dS swampland conjecture $|\nabla V|/V \geq c$, where c is presumed to be a positive constant of order unity, implies that the dark energy density of our Universe can not be a cosmological constant, but mostly the potential energy of an evolving quintessence scalar field. As the dark energy includes the effects of the electroweak symmetry breaking and the QCD chiral symmetry breaking, if the dS swampland conjecture is applicable for the low energy quintessence potential, it can be applied for the Higgs and pion potential also. On the other hand, the Higgs and pion potential has the well-known dS extrema, and applying the dS swampland conjecture to those dS extrema may provide stringent constraints on the viable quintessence, as well as on the conjecture itself. We examine this issue and find that the pion dS extremum at $\cos(\pi_0/f_\pi) = -1$ implies $c \lesssim \mathcal{O}(10^{-2}-10^{-5})$ for arbitrary form of the quintessence potential and couplings, where the weaker bound (10^{-2}) is available *only* for a specific type of quintessence whose couplings respect the equivalence principle, while the stronger bound (10^{-5}) applies for generic quintessence violating the equivalence principle. We also discuss the possibility to relax this bound with an additional scalar field, e.g. a light modulus which has a runaway behavior at the pion dS extremum. We argue that such possibility is severely constrained by a variety of observational constraints which do not leave a room to significantly relax the bound. We make a similar analysis for the Higgs dS extremum at $H = 0$, which results in a weaker bound on c.

Keywords: Effective Field Theories, Cosmology of Theories beyond the SM

ArXiv ePrint: [1809.01475](https://arxiv.org/abs/1809.01475)

Contents

1 Introduction

Motivated by the difficulty of constructing dS vacuum in string theory, recently the authors of [\[1\]](#page-17-0) proposed a conjecture that the scalar potential in low energy effective theory which has a UV completion consistent with quantum gravity satisfies

$$
M_{\rm Pl} \frac{|\nabla V|}{V} \equiv \frac{\sqrt{G^{ij} \partial_i V \partial_j V}}{V} \ge c \tag{1.1}
$$

over a certain range of scalar fields which can be of $\mathcal{O}(M_{\rm Pl})$, where G_{ij} is the metric of the scalar field kinetic terms in the Einstein frame, $M_{\rm Pl} \simeq 2.4 \times 10^{18} \,\mathrm{GeV}$ is the reduced Planck mass, and c is a positive constant of $\mathcal{O}(1)$. Obviously this conjecture constrains the possible form of (approximate) stationary points or flat directions of the scalar potential with a positive energy density. For instance, once applied for the dark energy density of the present Universe [\[2\]](#page-17-1), it implies that the dark energy can not be a cosmological constant, but mostly the potential energy of a very light evolving scalar field ϕ which is often dubbed quintessence [\[3](#page-17-2)[–5\]](#page-17-3).

If the dS swampland conjecture is applicable for the low energy quintessence potential, it can be applied for the Higgs and QCD pseudo-scalar meson potential also, since the quintessence potential which is identified as the dark energy density includes the effects of the electroweak symmetry and QCD chiral symmetry breaking. On the other hand, the Higgs and pseudo-scalar meson potential involve the well-known dS extrema, e.g. at $H = 0$ or $\cos(\pi_0/f_\pi) = -1$, where H is the Higgs doublet and π_0 is the neutral pion field with the periodicity $\pi_0 \equiv \pi_0 + 2\pi f_\pi$, whose present vacuum values are given by $\langle H \rangle = v = 174 \,\text{GeV}$ and $\langle \pi_0 \rangle = 0$. The existence of such dS extrema may impose strong constraints on the quintessence which can be compatible with the dS swampland conjecture,

as well as on the parameter c defining the conjecture.^{[1](#page-2-0)} Indeed, it has been pointed out recently [\[6\]](#page-17-4) that if the Standard Model (SM) sector is completely decoupled from the quintessence field ϕ , applying the dS swampland conjecture to the Higgs extremum results in $c \lesssim V(H = v)/V(H = 0)$ ~ 10⁻⁵⁵, which is smaller than the conjectured value $c = \mathcal{O}(1)$ by many orders of magnitude. Yet, one can avoid this bizarre conclusion by assuming proper (fine-tuned) couplings of ϕ to the Higgs sector [\[6\]](#page-17-4), which may allow $c = \mathcal{O}(1)$ and therefore rescue the conjecture.[2](#page-2-1)

Motivated by this observation, in this paper we wish to examine the implications of the pion or Higgs dS extrema for the dS swampland conjecture, while focusing on the possible (model-independent or model-dependent) bound on the parameter c. Here we do not question how much plausible it is to have a viable quintessence in the context of string theory, which is an issue extensively discussed in [\[29,](#page-18-0) [30\]](#page-18-1) a long time ago, and more recently in [\[31–](#page-18-2)[33\]](#page-18-3). Instead, we take the most general quintessence potential and couplings at low energy scales, and examine what would be the maximal value of the parameter c allowed by the observational constraints. We then find that the most stringent bound comes from the pion extremum at $\cos(\pi_0/f_\pi) = -1$, yielding

$$
c \le \text{Max} \left[d_q + 3d_g, \, V_{\text{eff}} / f_\pi^2 m_\pi^2 \sim 10^{-43} \right],\tag{1.2}
$$

where d_q and d_g are the low energy quintessence couplings to the light quarks and gluons defined in [\(2.7\)](#page-5-0), $V_{\text{eff}} \sim (2 \times 10^{-3} \text{ eV})^4$ is the quintessence potential energy in the present Universe, and m_{π} and f_{π} are the pion mass and decay constant, respectively. The observational bounds on the quintessence couplings d_q and d_q depend on whether they respect or violate the equivalence principle. For a specific type of quintessence whose couplings respect the equivalence principle, e.g. a quintessence which couples to the SM sector only through the trace of the energy momentum tensor, we have $d_q = d_q$. In such case, the quintessence couplings are constrained mainly by the observational bound on the deviation from the general relativity by the quintessence-mediated force in relativistic limit [\[34\]](#page-18-4), which results $in³$ $in³$ $in³$

$$
c < 1.4 \times 10^{-2} \tag{1.3}
$$

for arbitrary form of the quintessence potential. We call such quintessence a metrical quintessence [\[30\]](#page-18-1) as such a specific form of couplings which respect the equivalence principle may arise through the mixing with the conformal factor of the spacetime metric. However, for more generic quintessence with $(d_g - d_q)/(d_g + d_q) = \mathcal{O}(1)$, the quintessence couplings are bounded by the non-observation of the violation of the equivalence principle in nonrelativistic limit [\[36,](#page-18-5) [37\]](#page-18-6), yielding a much stronger bound

$$
c < 2 \times 10^{-5} \tag{1.4}
$$

¹The dS swampland conjecture might be modified, for instance as in $[7, 8]$ $[7, 8]$ $[7, 8]$ and $[9]$, in such a way that the dS extrema that we are discussing are manifestly compatible with the conjecture.

²For recent discussions of various implications of the dS swampland conjecture, see [\[10–](#page-17-8)[28\]](#page-18-7).

³All experimental bounds used in this paper are the 95% confidence level bounds.

again for *arbitrary* form of the quintessence potential. The bounds on c from the Higgs extremum is weaker than those from the pion extremum, but yet significantly stronger than the results obtained in $[6]$.

In fact, the above bounds on c are obtained while assuming that other scalar fields in the underlying theory can be integrated out without affecting the low energy dynamics around the pion dS extremum. One can then contemplate the possibility that those bounds are relaxed by an additional scalar field, e.g. a light modulus-like scalar, which has a large tadpole or a runaway behavior when the pion field is at the dS extremum. We examine this possibility also, and find that such a light scalar is severely constrained by a variety of observational constraints which practically close the room to significantly relax the above bounds on c.

Our bounds on c from the pion extremum appear to have a significant tension with the dS swampland conjecture [\(1.1\)](#page-1-1) which assumes $c = \mathcal{O}(1)$. We note that the conjecture (1.1) can be modified or refined, for instance as in $[7, 8]$ $[7, 8]$ $[7, 8]$ and $[9]$, in such a way to avoid the bounds from the Higgs and pion extrema. Then our results can be interpreted as providing additional motivation for such refinement of the conjecture.

The organization of this paper is as follows. In the next section, we discuss the possible couplings of quintessence to the SM sector and summarize the relevant observational constraints on the quintessence couplings. In section [3,](#page-7-0) we apply the dS swampland conjecture for the pion and Higgs extrema, and examine what would be the maximal value of c allowed by the observational constraints in the context of the most general form of the low energy quintessence potential and couplings. In section [4,](#page-10-0) we examine if an additional scalar which has a sizable tadpole or runaway behavior at the pion dS extremum can relax the bound on c obtained in section [3.](#page-7-0) Section 5 is the conclusion.

2 Quintessence couplings to the standard model

In this section we briefly discuss the possible couplings of the quintessence scalar field ϕ to the SM sector, as well as the observational constraints on the couplings. Without loss of generality, using appropriate field redefinitions, one can always move to the Einstein frame and make the kinetic terms of the SM fermions and the Higgs boson to take the ϕ -independent canonical form. We are interested in the possible non-derivative couplings of ϕ to the SM fields in this field basis, which can be encoded in the ϕ -dependent SM parameters. Then the lagrangian density at some scale μ above the weak scale can be written as^{[4](#page-3-1)}

$$
\mathcal{L} = \frac{1}{2} \partial_{\mu} \phi \partial^{\mu} \phi + |D_{\mu} H|^{2} + \bar{\psi}_{L} i \mathcal{D} \psi_{L} + \bar{\psi}_{R} i \mathcal{D} \psi_{R} - \frac{1}{4g_{a}^{2}(\phi)} F^{a\mu\nu} F^{a}_{\mu\nu} - (y_{\psi}(\phi) H \bar{\psi}_{L} \psi_{R} + h.c.) - \lambda(\phi) |H|^{4} + m_{H}^{2}(\phi) |H|^{2} - V_{b}(\phi),
$$
\n(2.1)

⁴For simplicity, here we do not consider the quintessence couplings such as $\theta(\phi)F^{a\mu\nu}\tilde{F}^a_{\mu\nu}$, $\partial_\mu\phi H^{\dagger}D^{\mu}H$ and $\partial_\mu \phi \bar{\psi} \gamma^\mu \psi$ as they do not affect our subsequent discussion. Note that the derivative couplings of ϕ to H and ψ can affect the scalar field metric G_{ij} that appears in the dS swampland conjecture, but their effects are suppressed by $v/M_{\rm Pl} \sim 10^{-16}$ or $f_\pi/M_{\rm Pl} \sim 10^{-19}$ and therefore can be safely ignored.

where V_b is the H-independent bare potential of ϕ , and $g_a(\phi)$, $\lambda(\phi)$ and $y_{\psi}(\phi)$ are generically φ-dependent gauge, Higgs quartic, and Yukawa couplings, respectively.

From the above lagrangian density, one can calculate the low energy consequences of the model, including the effective potential of ϕ at cosmic scales and also the low energy couplings of ϕ which are constrained by a variety of laboratory, astrophysical and cosmological observations [\[34–](#page-18-4)[36,](#page-18-5) [38\]](#page-19-0). For instance, the low energy quintessence potential can be obtained by integrating out all SM fields, which would result in

$$
V_{\text{eff}}(\phi) = V_b(\phi) + \left\langle \lambda |H|^4 - m_H^2 |H|^2 - \left(y_\psi H \bar{\psi}_L \psi_R + h.c \right) + \frac{1}{4g_a^2} F^{a\mu\nu} F^a_{\mu\nu} \right\rangle + \dots
$$

$$
= V_b(\phi) - \frac{m_H^4(\phi)}{4\lambda(\phi)} - \sum_{q=u,d,s} m_q(\phi) \langle \bar{q}q \rangle + \mathcal{O}(\Lambda_{\text{QCD}}^4) + \dots,
$$
 (2.2)

where $\langle \ldots \rangle$ are the expectation values of the SM fields, $\mathcal{O}(\Lambda_{\rm QCD}^4)$ denotes the contribution from the gluon condensation including the contributions from the heavy quark thresholds effects, and the ellipsis stands for additional contributions including a variety of additional quantum corrections. If ϕ is identified as the quintessence scalar field explaining the dark energy of the present Universe, its low energy potential should satisfy [\[2,](#page-17-1) [39\]](#page-19-1)

$$
V_{\text{eff}}(\phi) \sim (2 \times 10^{-3} \text{eV})^4, \qquad M_{\text{Pl}} \frac{V_{\text{eff}}'(\phi)}{V_{\text{eff}}(\phi)} \lesssim 0.6 \tag{2.3}
$$

over a field range $\Delta \phi \sim M_{\text{Pl}}$, where the prime denotes the derivative w.r.t. ϕ , and also

$$
V''_{\text{eff}}(\phi_0) \lesssim H_0^2 \sim (10^{-33} \,\text{eV})^2,\tag{2.4}
$$

where ϕ_0 and H_0 are the quintessence field value and the Hubble expansion rate of the present Universe, respectively.

As for the couplings of ϕ defined at high energy scale μ , one finds

$$
\mathcal{L}_{\phi}(\mu) = \frac{g_a'}{2g_a^3} \phi F^{a\mu\nu} F_{\mu\nu}^a - \left(m_{\psi} \left(\frac{y_{\psi}'}{y_{\psi}} + \frac{v'}{v} \right) \phi \bar{\psi}_L \psi_R + h.c \right) - m_h^2 \left(\frac{\lambda'}{\lambda} + \frac{2v'}{v} \right) \phi h^2 + \dots,
$$
\n(2.5)

where v denotes the ϕ -dependent Higgs vacuum value given by

$$
v^2(\phi) = \frac{m_H^2(\phi)}{2\lambda(\phi)},\tag{2.6}
$$

 h is the canonically normalized Higgs boson fluctuation, and again the prime denotes the derivative w.r.t. ϕ . Here the field ϕ corresponds to the fluctuation around ϕ_0 , and the ellipsis stands for additional couplings which are not relevant for our subsequent discussion.

As they are even weaker than the gravitational coupling, the quintessence couplings are constrained mostly by the macroscopic observations such as the violation of the equivalence principle in non-relativistic limit, the deviation from the general relativity in relativistic limit, or the variation of the fundamental constants, e.g. the fine structure constant [\[35\]](#page-18-8).

However, those constraints apply for the low energy effective couplings of ϕ defined at lower energy scale μ_{eff} , which may be parametrized as

$$
\mathcal{L}_{\phi}(\mu_{\text{eff}}) = d_{\gamma} \frac{\phi}{M_{\text{Pl}}} \frac{1}{4e^2} F^{\mu\nu} F_{\mu\nu} - d_g \frac{\phi}{M_{\text{Pl}}} (T^{\mu}_{\mu})_{\text{QCD}} - \sum_{q=u,d,s} (d_q - d_g) m_q \frac{\phi}{M_{\text{Pl}}} \bar{q} q
$$

= $d_{\gamma} \frac{\phi}{M_{\text{Pl}}} \frac{1}{4e^2} F^{\mu\nu} F_{\mu\nu} - d_g \frac{\phi}{M_{\text{Pl}}} \frac{\beta_s}{2g_s} G^{i\mu\nu} G^i_{\mu\nu} - \sum_{q=u,d,s} (d_q + \gamma_m d_g) m_q \frac{\phi}{M_{\text{Pl}}} \bar{q} q,$ (2.7)

where $(T^{\mu}_{\mu})_{\text{QCD}}$ is the trace of the energy momentum tensor for the low energy QCD of the light quark flavors $q = (u, d, s)$, and therefore β_s and γ_m are the QCD beta function and the mass anomalous dimension, respectively. Here the gluon fields $G^i_{\mu\nu}$ are rescaled to have the standard canonical kinetic term as $-\frac{1}{4}G^{i\mu\nu}G^{i}_{\mu\nu}$. Note that d_g and d_q are defined to be independent of the renormalization scale μ_{eff} . Also, they can be defined as

$$
\frac{d_g}{M_{\rm Pl}} = \frac{\Lambda'_{\rm QCD}(\phi)}{\Lambda_{\rm QCD}(\phi)}, \qquad \frac{d_q}{M_{\rm Pl}} = \frac{m'_q(\phi, \Lambda_{\rm QCD}(\phi))}{m_q(\phi, \Lambda_{\rm QCD}(\phi))},\tag{2.8}
$$

where $\Lambda_{\text{QCD}}(\phi)$ is the ϕ -dependent physical QCD scale and $m_q(\phi, \Lambda_{\text{QCD}}(\phi))$ is the ϕ -dependent light quark mass renormalized at Λ_{QCD} .

Although the low energy couplings d_q and d_q are defined to be independent of μ_{eff} , perturbative calculation of those couplings in terms of the high energy couplings in [\(2.5\)](#page-4-0) can be done only for μ_{eff} where the perturbation theory applies. For later use, let us briefly discuss the perturbative corrections that d_g receives from the high energy couplings in (2.5) . At one-loop order, the dominant corrections to d_q come from the one-loop thresholds of heavy quarks which couple to ϕ . There can be also a potentially important two loop correction induced by the $\phi - h - h$ coupling in [\(2.5\)](#page-4-0) and the top quark Yukawa coupling of the Higgs boson h. Putting those radiative corrections with the tree level contribution, we find that the low energy coupling d_g at μ_{eff} just below the charm quark mass is determined by the high energy couplings in (2.5) as follows:

$$
\frac{d_g}{M_{\text{Pl}}} \simeq \frac{(16\pi^2)}{9} \frac{g_s'(\mu)}{g_s^3(\mu)} + \frac{2}{27} \sum_{q=t,b,c} \left(\frac{y_q'}{y_q} + \frac{v'}{v} \right) - \frac{y_t^2 f(\tau)}{288\pi^2} \left(\frac{\lambda'}{\lambda} + 2\frac{v'}{v} \right),\tag{2.9}
$$

where $\tau \equiv 4m_t^2/m_h^2$. Here the second term in the RHS represents the one-loop threshold of heavy quarks, while the third term corresponds to the two-loop threshold involving the Higgs boson and the top quark. We obtained the analytic form of the function $f(\tau)$ for a generic τ from full two-loop calculations. For $m_t = 173$ GeV and $m_h = 125$ GeV, it yields $f(4m_t^2/m_h^2) = 0.21.$

For generic low energy quintessence couplings, the most stringent constraint comes from the violation of the weak equivalence principle (EPV) by the quintessence-mediated force in non-relativistic limit. For instance, using the results of [\[37,](#page-18-6) [40,](#page-19-2) [41\]](#page-19-3), we find that non-observation of EPV implies

$$
(d_g + 0.093(d_{\tilde{q}} - d_g) + 0.00027d_\gamma) (3.3(d_{\tilde{q}} - d_g) + 1.9d_\gamma) < 2.7 \times 10^{-11},\tag{2.10}
$$

where

$$
d_{\tilde{q}} = \frac{m_u d_u + m_d d_d}{m_u + m_d}.\tag{2.11}
$$

If we assume that there is no significant cancellation among the different quintessence couplings, e.g.

$$
\frac{d_{\alpha} - d_{\beta}}{d_{\alpha} + d_{\beta}} = \mathcal{O}(1) \quad (\alpha, \beta = g, q, \gamma)
$$
\n(2.12)

which would be the case for generic forms of low energy couplings, this implies

$$
d_g < 3 \times 10^{-6}, \quad d_{\tilde{q}} < 10^{-5}, \quad d_{\gamma} < 2 \times 10^{-4}.\tag{2.13}
$$

The quintessence coupling to the photon can be constrained by the observational bound on the time-varying fine structure constant also [\[35\]](#page-18-8), which would result in

$$
d_{\gamma} < 3 \times 10^{-7} \frac{M_{\rm Pl} H_0}{\dot{\phi}},\tag{2.14}
$$

where H_0 is the Hubble expansion rate today and $\dot{\phi} = d\phi/dt$.

In fact, there is a specific type of quintessence which automatically satisfies the above constraints from EPV and time-varying fine structure constant. If ϕ couples to the SM only through the trace of the energy momentum tensor, i.e.

$$
\mathcal{L}_{\phi} = d_T \frac{\phi}{M_{\text{Pl}}} T^{\mu}_{\mu},\tag{2.15}
$$

we have

$$
d_T = d_g = d_q, \quad d_\gamma = 0,\tag{2.16}
$$

therefore the observational bounds [\(2.10\)](#page-5-1) and [\(2.14\)](#page-6-0) are automatically satisfied. Note that the quintessence coupling to T^{μ}_{μ} does not violate the equivalence principle, and also the time-varying fine structure constant applies for the low energy electromagnetic coupling which has a vanishing beta function, and therefore the corresponding $d_{\gamma} = 0$ when the quintessence couplings take the form [\(2.15\)](#page-6-1).

One may call the above type of quintessence a "metrical quintessence" since the specific coupling (2.15) can arise from the mixing of ϕ with the conformal factor of the spacetime metric $g_{\mu\nu}$ [\[30\]](#page-18-1). A specific such example is a theory which does not have any coupling between ϕ and the SM fields in an appropriate field basis, while having non-trivial couplings between ϕ and $g_{\mu\nu}$ through the ϕ -dependent Planck mass. One can then move to the Einstein frame by making an appropriate Weyl transformation:

$$
g_{\mu\nu} \to \Omega(\phi) g_{\mu\nu} \tag{2.17}
$$

which would result in the quintessence coupling (2.15) in the Einstein frame. Yet, the coupling of metrical quintessence is constrained by the observational bounds on the deviation from the general relativity by the quintessence-mediated force in relativistic limit. For instance, from the measurement of the gravitational time delay effect to the Cassini spacecraft, one finds [\[34\]](#page-18-4)

$$
d_T = d_g = d_q < 3.4 \times 10^{-3}.\tag{2.18}
$$

3 De Sitter swampland conjecture for the pion and Higgs extrema

As we have stressed, if the dS swampland conjecture (1.1) applies for the low energy quintessence potential (2.2) including the contributions from the electroweak symmetry and QCD chiral symmetry breaking, it is applicable also for the Higgs and QCD pseudoscalar meson potentials. In this section, we apply the dS swampland conjecture to some of the dS extrema of the pseudo-scalar meson or Higgs potential and examine its implications. For simplicity, we will take the simple effective field theory approach, assuming that all other degrees of freedom can be integrated out in such a way that the resulting effective theory is good enough over a field range including both the vacuum configuration and the relevant dS extrema, e.g. the entire field range of the pion field $\pi_0/f_\pi \in [0, 2\pi]$ and also the Higgs field range $\Delta H \sim v$.

Because we are considering both the vacuum solution and a dS extremum together, generically our results can receive corrections from the tadpoles or runaway behavior of the integrated scalar fields, which can be induced at the dS extremum point. We will see in the next section that those corrections do not significantly affect the results of this section when the observational constraints on the underlying dynamics are properly taken into account.

3.1 Pion extremum

To proceed, let us first consider the field configuration where the Higgs field is frozen at its vacuum value, $H = v(\phi) = m_H(\phi)/\sqrt{2\lambda(\phi)}$, and integrate out all SM fields heavier than the QCD scale $\Lambda_{\rm QCD}$. The remained light scalar degrees of freedom are the quintessence field ϕ and the pseudo-scalar meson octet $\pi_a = (\pi, K, \eta)$ which correspond to the pseudo-Nambu-Goldstone bosons associated with the spontaneous breakdown of the QCD chiral symmetry:

$$
SU(3)_L \times SU(3)_R \to SU(3)_V. \tag{3.1}
$$

The corresponding field manifold $SU(3)_L \times SU(3)_R / SU(3)_V$ is compact and can be parametrized as

$$
U = \exp\left[i\frac{\pi_a}{f_\pi}\lambda_a\right],\tag{3.2}
$$

where λ_a are the Gell-Mann matrices and f_π is the pion decay constant. At leading order in chiral perturbation theory, the effective lagrangian of U is given by

$$
\frac{f_{\pi}^2}{4} \text{Tr} \left[\partial_{\mu} U^{\dagger} \partial^{\mu} U \right] + \frac{\Lambda^3}{2} \text{Tr} \left[M_q (U + U^{\dagger}) \right], \tag{3.3}
$$

where Λ can be identified as the condensation scale of the light quark fields, i.e. $\langle \bar{q}_i q_j \rangle = \Lambda^3 \delta_{ij}$ for $q_i = (u, d, s)$, and $M_q = \text{diag}(m_u, m_d, m_s)$ is the light quark mass matrix which is chosen to be real, diagonal and positive.

Because the meson field manifold $SU(3)_L \times SU(3)_R / SU(3)_V$ is compact, there can be multiple dS extrema of the meson potential. Here, for simplicity we focus on the neutral

pion π_0 , while fixing all other mesons at their vacuum values. Then the effective potential of the pion and quintessence is given by

$$
V(\phi, \pi_0/f_\pi) = V_{\text{eff}}(\phi) + (m_u(\phi) + m_d(\phi))\Lambda^3(\phi) \left[1 - \cos\left(\frac{\pi_0}{f_\pi(\phi)}\right)\right],\tag{3.4}
$$

where we choose the convention that $\langle \pi_0 \rangle = 0$ in the true vacuum, and the low energy QCD parameters $m_{u,d}$, f_{π} and Λ are understood to be generic functions of the quintessence field φ. This potential is valid over the full range of the pion field $\pi_0/f_\pi \in [0, 2\pi]$ and has a dS local maximum along the pion direction at

$$
\frac{\pi_0}{f_\pi} = \pi.
$$
\n(3.5)

Note that although we consider a leading order approximation in chiral perturbation theory, the periodicity of the pion field $\pi_0 \equiv \pi_0 + 2\pi f_\pi$ and the CP invariance under $\pi_0 \to -\pi_0$ assure that this configuration is a dS local maximum of the exact pion potential up to negligible corrections due to the CP violating weak interactions. We then find

$$
V(\phi, \pi_0/f_\pi = \pi) = V_{\text{eff}}(\phi) + 2(m_u(\phi) + m_d(\phi))\Lambda^3(\phi)
$$

$$
\nabla V(\phi, \pi_0/f_\pi = \pi) = V'_{\text{eff}}(\phi) + 2\left(\frac{m'_u + m'_d}{m_u + m_d} + 3\frac{\Lambda'}{\Lambda}\right)(m_u + m_d)\Lambda^3,
$$
 (3.6)

which results in

$$
M_{\rm Pl} \frac{|\nabla V(\phi, \pi_0/f_\pi = \pi)|}{V(\phi, \pi_0/f_\pi = \pi)} = \left| M_{\rm Pl} \left(\frac{m_u' + m_d'}{m_u + m_d} + \frac{3\Lambda'}{\Lambda} \right) + \mathcal{O}(10^{-43}) \right| \ge c, \qquad (3.7)
$$

where we used the properties (2.3) of $V_{\text{eff}}(\phi)$ yielding

$$
M_{\rm Pl} \frac{V'_{\rm eff}}{(m_u + m_d)\Lambda^3} \lesssim \frac{V_{\rm eff}}{(m_u + m_d)\Lambda^3} = \frac{V_{\rm eff}}{m_\pi^2 f_\pi^2} \sim 10^{-43},\tag{3.8}
$$

and applied the dS swampland conjecture [\(1.1\)](#page-1-1) in the last step.

For us, it is most convenient to choose the renormalization scale of the light quark mass m_q and the quark bilinear operator $\bar{q}q$ to be $\Lambda_{\rm QCD}$, for which

$$
\frac{\Lambda'}{\Lambda} = \frac{\Lambda'_{\text{QCD}}}{\Lambda_{\text{QCD}}} = \frac{d_g}{M_{\text{Pl}}}, \qquad \frac{m'_q}{m_q} = \frac{d_q}{M_{\text{Pl}}},\tag{3.9}
$$

where d_g and d_g are the low energy quintessence couplings defined in [\(2.7\)](#page-5-0). Then the dS swampland conjecture applied for the pion and quintessence potential at the pion dS extremum results in

$$
c \lesssim \text{Max} \left[d_{\tilde{q}} + 3d_g, \mathcal{O}(10^{-43}) \right], \tag{3.10}
$$

where

$$
d_{\tilde{q}} = \frac{m_u d_u + m_d d_d}{m_u + m_d}.\tag{3.11}
$$

We stress that the above bound is valid for *arbitrary* form of the quintessence potential and couplings.

Similarly to the case of the Higgs extremum discussed in [\[6\]](#page-17-4), if ϕ is completely decoupled from the QCD sector, so that $d_q = d_q = 0$, the parameter c is required to be smaller than $V_{\text{eff}}/f_{\pi}^2 m_{\pi}^2 \sim 10^{-43}$, which is smaller than the conjectured value $c = \mathcal{O}(1)$ by many orders of magnitude. Again, by assuming appropriate form of couplings between the quintessence and the QCD sector, one can alleviate this bound on c up to the value allowed by observational constraints. Then, for generic quintessence with $(d_q-d_q)/(d_q+d_q) = \mathcal{O}(1)$, the observational bound (2.10) on the violation of the equivalence principle (EP) can be applied to get

$$
c < 2 \times 10^{-5} \quad \text{for quintessence violating the EP.} \tag{3.12}
$$

On the other hand, for a metrical quintessence which couples to the SM only through the trace of energy momentum tensor and therefore has $d_q = d_q$, the bound on c can be significantly relaxed. In such case, we can use the observational bound [\(2.18\)](#page-6-2) on the deviation from the general relativity in the solar system to get

$$
c < 1.4 \times 10^{-2} \quad \text{for quintessence, the EP.} \tag{3.13}
$$

3.2 Higgs extremum

Let us now consider the Higgs dS extremum at $H = 0$, which was discussed also in [\[6\]](#page-17-4). Here we will elaborate the discussion of $[6]$ and examine if any useful bound on c can be obtained from the consideration of the Higgs dS extremum. In the scalar field space near $H = 0$, the effective potential can be written as

$$
V(H,\phi) = V_{\text{eff}}(\phi) + \lambda(\phi)v^4(\phi) - \sum_{\psi} \left(y_{\psi}(\phi)H\langle \bar{\psi}_L \psi_R \rangle + h.c \right) - \frac{1}{2}m_H^2(\phi)|H|^2 + \dots,
$$
\n(3.14)

where we include the contribution from the quark condensations in the limit $H = 0$ where all quarks are massless. To proceed, we can take the gauge that H is identified as a real scalar field, and also choose the field basis where the Yukawa couplings y_{ψ} are real, positive and diagonal.^{[5](#page-9-1)} To avoid unnecessary complication due to nonzero tadpoles of the fields other than ϕ , we then focus on the field configuration with

$$
\tilde{\pi}_{\psi} = \frac{\pi}{2} \tag{3.15}
$$

where $\tilde{\pi}_{\psi}$ denotes the phase of the quark condensation for $H = 0$, i.e.

$$
\langle \bar{\psi}_L \psi_R \rangle_{H=0} = \tilde{\Lambda}^3 e^{i\tilde{\pi}_{\psi}} \tag{3.16}
$$

for $\tilde{\Lambda}$ which corresponds to the QCD condensation scale for $H = 0$, which is about an half of the QCD scale for $H = v$. For such field configuration, one immediately finds

$$
\partial_H V(H = 0, \tilde{\pi}_{\psi} = \pi/2) = \partial_{\tilde{\pi}_{\psi}} V(H = 0, \tilde{\pi}_{\psi} = \pi/2) = 0, \tag{3.17}
$$

 5 The flavor changing weak interactions mediated by the W-boson in this field basis can be safely ignored.

which results in [\[6\]](#page-17-4):

$$
M_{\rm Pl} \frac{|\nabla V|}{V} = M_{\rm Pl} \frac{|V'_{\rm eff} + (\lambda'/\lambda + 4v'/v) \lambda v^4|}{V_{\rm eff}(\phi) + \lambda(\phi)v(\phi)^4} = \left| M_{\rm Pl} \left(\frac{\lambda'}{\lambda} + \frac{4v'}{v} \right) + \mathcal{O}(10^{-55}) \right| \gtrsim c. \tag{3.18}
$$

Translating the above result to an observational bound on c is more complicated and model-dependent than the case of the pion extremum. Yet, with the matching condition (2.9) on d_g including the relevant radiative corrections and also the tree level matching condition $d_q/M_{\rm Pl} = m'_q/m_q = y'_q/y_q + v'/v$, we can estimate the maximal value of c compatible with the observational constraints on the low energy quintessence couplings. Given the observational bounds on d_g and d_q , the maximal value of c can be achieved when $|\lambda'/\lambda| \gg |v'/v|, |y'_q/y_q|$ and λ'/λ saturates the bound on d_g through the two loop contribution represented by the last term of (2.9) . In fact, the model discussed in $[6]$ corresponds to such case as it assumes $v' = y'_q = 0$ with $\lambda' \neq 0$. Inserting all the involved numerical factors, we find that the corresponding bound on c is given by

$$
c \le \text{Max} \left[1.5 \times 10^4 \cdot d_g, \, 10^{-55} \right] \lesssim 4.4 \times 10^{-2} \tag{3.19}
$$

which is significantly weaker than the bound (3.12) from the pion extremum. Note that for a metrical quintessence, we have $|\lambda'/\lambda| \ll |v'/v|$ and the bound on c from the Higgs extremum is same as the one from the pion extremum, i.e. $c < 1.4 \times 10^{-2}$.

4 Effects of the tadpole or runaway of additional scalar fields

In the previous section, we discussed the implications of the pion or Higgs extremum for the dS swampland conjecture within an effective theory while assuming that other scalar degrees of freedom can be integrated out in such a way that the resulting effective theory can describe well the relevant low energy physics over the entire field range of the pion field, i.e. $\pi_0/f_\pi \in [0, 2\pi]$, and also over the Higgs field range $\Delta H \sim v$. Here we examine possible effects of the tadpole or runaway behavior of the integrated scalar fields, which can be induced at the pion or Higgs dS extremum. As it provides the most stringent bound on c , we will focus on the case of the pion extremum. As we will see, the bounds on c obtained in section [3](#page-7-0) can not be significantly relaxed by additional scalar fields when the observational constraints are properly taken into account.

Let Φ denote a generic scalar field which is integrated out in the effective potential (3.4) . As the quintessence is the only rolling field in the present Universe, Φ should be properly stabilized at least when the pion field is at the vacuum with $\pi_0/f_\pi = 0$. Then, one can always choose $\langle \Phi \rangle_{\pi_0=0} = 0$ and expand the full potential of ϕ, π_0 and Φ as follows:

$$
V(\phi, \pi_0, \Phi) = V_{\text{eff}}(\phi) + V_{\text{up}}(\phi, \pi_0) + \frac{1}{2} m_{\Phi}^2(\phi) \Phi^2 + \left(\frac{\Phi}{2\Lambda_{\Phi}(\phi)} + \cdots\right) V_{\text{up}}(\phi, \pi_0), \quad (4.1)
$$

where

$$
V_{\rm up}(\phi, \pi_0) \equiv V(\phi, \pi_0, \Phi = 0) - V(\phi, \pi_0 = 0, \Phi = 0)
$$

\n
$$
\simeq (m_u(\phi) + m_d(\phi))\Lambda^3(\phi) \left(1 - \cos \frac{\pi_0}{f_\pi(\phi)}\right) = m_\pi^2(\phi) f_\pi^2(\phi) \left(1 - \cos \frac{\pi_0}{f_\pi(\phi)}\right) \quad (4.2)
$$

and the ellipsis denotes the terms higher order in Φ . Obviously, here m_{Φ} is the mass of Φ when $\pi_0/f_\pi = 0$, and Λ_{Φ} is a mass scale parametrizing the coupling of Φ to the pions or more generically to the low energy QCD sector.

If $m_{\Phi} \Lambda_{\Phi} > m_{\pi} f_{\pi}$, Φ is stabilized with a small field shift even when the pion field is at $\pi_0/f_\pi = \pi$. The corresponding tadpole is determined by

$$
\partial_{\pi_0} V(\phi, \pi_0/f_\pi = \pi, \Phi = \delta \Phi) = \partial_{\Phi} V(\phi, \pi_0/f_\pi = \pi, \Phi = \delta \Phi) = 0,\tag{4.3}
$$

yielding

$$
\frac{\delta\Phi}{\Lambda_{\Phi}} \simeq \frac{m_{\pi}^2 f_{\pi}^2}{m_{\Phi}^2 \Lambda_{\Phi}^2}.
$$
\n(4.4)

One may then apply the dS swampland conjecture for the shifted extremum point, which would result in

$$
M_{\rm Pl} \frac{|\nabla V(\phi, \pi_0/f_\pi = \pi, \Phi = \delta \Phi)|}{V(\phi, \pi_0/f_\pi = \pi, \Phi = \delta \Phi)} = M_{\rm Pl} \frac{|\partial_\phi V(\phi, \pi_0/f_\pi = \pi, \Phi = \delta \Phi)|}{V(\phi, \pi_0/f_\pi = \pi, \Phi = \delta \Phi)}
$$

\n
$$
\simeq M_{\rm Pl} \left| \partial_\phi \ln V_{\rm up}(\phi, \pi_0/f_\pi = \pi) - \frac{m_\pi^2 f_\pi^2}{m_\Phi^2 \Lambda_\Phi^2} \partial_\phi \ln \left(\frac{V_{\rm up}(\phi, \pi_0/f_\pi = \pi)}{m_\Phi^2 (\phi) \Lambda_\Phi^2 (\phi)} \right) \right|
$$

\n
$$
= M_{\rm Pl} \left| \left(\frac{m_u' + m_d'}{m_u + m_d} + 3 \frac{\Lambda'}{\Lambda} \right) - \frac{m_\pi^2 f_\pi^2}{m_\Phi^2 \Lambda_\Phi^2} \left(\frac{m_u' + m_d'}{m_u + m_d} + 3 \frac{\Lambda'}{\Lambda} - \partial_\phi \ln(m_\Phi^2 \Lambda_\Phi^2) \right) \right|
$$

\n
$$
= \left| (d_{\tilde{q}} + 3d_g) \left(1 - \frac{m_\pi^2 f_\pi^2}{m_\Phi^2 \Lambda_\Phi^2} \right) + \frac{m_\pi^2 f_\pi^2}{m_\Phi^2 \Lambda_\Phi^2} M_{\rm Pl} \partial_\phi \ln(m_\Phi^2 \Lambda_\Phi^2) \right| \geq c. \tag{4.5}
$$

Note that the terms suppressed by $m_{\pi}^2 f_{\pi}^2 / m_{\Phi}^2 \Lambda_{\Phi}^2$ correspond to the corrections to eq. [\(3.7\)](#page-8-1) in section [3,](#page-7-0) which arise from the tadpole of Φ induced at $\pi_0/f_\pi = \pi$.

Let us apply the above results for the SM scalar degrees of freedom which are either elementary or composite. Fist of all, for Φ being the pseudo-scalar mesons such as K and η , P or CP symmetry assures that the linear coupling of Φ to V_{up} is highly suppressed, e.g. $\Lambda_{\Phi} \gg v$, and therefore $f_{\pi}^2 m_{\pi}^2/m_{\Phi}^2 \Lambda_{\Phi}^2 \ll 10^{-5}$. For Φ being the SM Higgs boson, we have $\Lambda_{\Phi} \sim v$ and again $m_{\pi}^2 f_{\pi}/m_{\Phi}^2 \Lambda_{\Phi}^2 \sim m_{\pi}^2 f_{\pi}^2/m_h^2 v^2 \ll 10^{-5}$. This assures the possible corrections due to the tadpole of the pseudo-scalar mesons and Higgs boson are much smaller than the observational bound on d_g and d_q , and therefore can be safely ignored. In fact, the only scalar degree of freedom of the SM which can have a non-negligible value of $f_{\pi}^2 m_{\pi}^2 / m_{\Phi}^2 \Lambda_{\Phi}^2$ is the quark-antiquark composite scalar σ which controls the size of the light quark condensation:[6](#page-11-0)

$$
\langle \bar{q}q \rangle \propto e^{-\sigma/\Lambda_{\sigma}},\tag{4.6}
$$

for which

$$
m_{\sigma} \sim \Lambda_{\sigma} \sim \Lambda_{\text{QCD}}.\tag{4.7}
$$

⁶In real QCD, σ has a too broad decay width, so there is no corresponding particle state. However, yet σ can be relevant for the dS swampland conjecture as the potential energy varies as a function of σ.

In this case, the corresponding suppression factor $m_{\pi}^2 f_{\pi}^2/m_{\sigma}^2 \Lambda_{\sigma}^2 \sim m_q/\Lambda_{\rm QCD}$ is not small enough. However the accompanying factor which is given by

$$
M_{\rm Pl}\partial_{\phi}\ln(m_{\sigma}^2\Lambda_{\sigma}^2) = 4M_{\rm Pl}\frac{\Lambda'_{\rm QCD}}{\Lambda_{\rm QCD}} = 4d_g \tag{4.8}
$$

provides additional suppression, so that again the tadpole of σ at the pion extremum does not alter the result (3.7) .

Our discussion above suggests that the upper bound on c can be relaxed if there exists some scalar field Φ (other than those in the SM) with $\frac{m_{\pi}^2 f_{\pi}^2}{m_{\Phi}^2 \Lambda_{\Phi}^2} M_{\text{Pl}} \partial_{\phi} \ln(m_{\Phi}^2 \Lambda_{\Phi}^2) \gg \mathcal{O}(10^{-5} -$ 10⁻²) at $\pi_0/f_\pi = \pi$, i.e. a light scalar which has a sizable tadpole or runaway behavior at the pion extremum. In string theory, the most promising candidate for such scalar field is a light modulus χ. Even when χ has a sizable tadpole or runaway behavior at $\pi_0/f_\pi = \pi$, it has to be stabilized at certain vacuum value $\langle \chi \rangle$ with a mass $m_{\chi} > H_0 \sim 10^{-33}$ eV at $\pi_0/f_\pi = 0$. Again one can choose a field basis for which $\langle \chi \rangle = 0$ at $\pi_0/f_\pi = 0$, and then the potential can be expanded as

$$
V(\phi, \pi_0, \chi) = V_{\text{eff}}(\phi) + V_{\text{up}}(\phi, \pi_0) + \frac{1}{2} m_{\chi}^2(\phi) \chi^2 + \left(c_{\chi} \frac{\chi}{2M_{\text{Pl}}} + \cdots\right) V_{\text{up}}(\phi, \pi_0), \quad (4.9)
$$

where we introduce a dimensionless parameter c_{χ} to parametrize the coupling of χ to the low energy QCD sector. Here the coupling c_x should be the low energy consequence of the modulus couplings to the QCD sector, which can be parametrized as

$$
\mathcal{L}_{\chi} = -\tilde{d}_{g} \frac{\chi}{M_{\text{Pl}}} \frac{\beta_{s}}{2g_{s}} G^{i\mu\nu} G^{i}_{\mu\nu} - \sum_{q=u,d,s} (\tilde{d}_{q} + \gamma_{m} \tilde{d}_{g}) m_{q} \frac{\chi}{M_{\text{Pl}}} \bar{q} q, \tag{4.10}
$$

and then

$$
c_{\chi} = \frac{m_u \tilde{d}_u + m_d \tilde{d}_d}{m_u + m_d} + 3\tilde{d}_g \equiv \tilde{d}_{\tilde{q}} + 3\tilde{d}_g.
$$
\n(4.11)

There are some range of m_{χ} for which the modulus χ is obviously in conflict with the observational constraints or not useful for relaxing the bound on c. For instance, for a relatively massive χ with

$$
m_{\chi} \gtrsim 1.5 \times 10^{-9} c_{\chi} \,\text{eV},\tag{4.12}
$$

one can apply [\(4.5\)](#page-11-1) with $m_{\Phi} = m_{\chi}$ and $\Lambda_{\Phi} = M_{\rm Pl}/c_{\chi}$ to ensure that the modulus tadpole $\delta \chi$ is small enough to keep the bound [\(3.10\)](#page-8-2) unaffected. Also, the following mass regions are excluded by the blackhole superradiance [\[46\]](#page-19-4):

$$
5 \times 10^{-13} \text{ eV} \lesssim m_{\chi} \lesssim 2 \times 10^{-11} \text{ eV},
$$

\n
$$
10^{-17} \text{ eV} \lesssim m_{\chi} \lesssim 6 \times 10^{-17} \text{ eV},
$$

\n
$$
8 \times 10^{-19} \text{ eV} \lesssim m_{\chi} \lesssim 10^{-18} \text{ eV}.
$$
 (4.13)

If χ is light enough, e.g.

$$
m_{\chi} < 5 \times 10^{-12} c_{\chi}^{1/2} \,\text{eV},\tag{4.14}
$$

the resulting modulus tadpole $\delta \chi$ is of $\mathcal{O}(M_{\text{Pl}})$, so a nearby stationary point is not guaranteed to exist. In such case, one can apply the dS swampland conjecture to the field configuration with $\pi_0/f_\pi = \pi$ and $\chi = 0$, rather than the configuration with $\pi_0/f_\pi = \pi$ and $\chi = \delta \chi$. This then leads to a new upper bound on c as

$$
M_{\rm Pl} \frac{|\nabla V(\phi, \pi_0/f_\pi = \pi, \chi = 0)|}{V(\phi, \pi_0/f_\pi = \pi, \chi = 0)} = M_{\rm Pl} \frac{\sqrt{(\partial_\phi V)^2 + (\partial_\chi V)^2}}{V}
$$

$$
\simeq \sqrt{(d_{\tilde{q}} + 3d_g)^2 + c_\chi^2} \geq c.
$$
 (4.15)

For $m_{\chi} < 10^{-18}$ eV, the modulus couplings \tilde{d}_q and \tilde{d}_q are constrained as the quintessence couplings d_q and d_g by both the non-observation of the violation of the equivalence principle [\[36\]](#page-18-5) and tests of general relativity in the solar system [\[34,](#page-18-4) [42](#page-19-5)[–45\]](#page-19-6). Then the above new bound is essentially equivalent to the bound [\(3.10\)](#page-8-2), which means that a ultralight modulus with $m_\chi < 10^{-18}$ eV is not useful for relaxing the bound [\(3.10\)](#page-8-2). If $(\tilde{d}_g - \tilde{d}_q)/(\tilde{d}_g + \tilde{d}_q) = \mathcal{O}(1)$, so that the modulus couplings violate the equivalence principle, one can use the corresponding bounds on \ddot{d}_q and \ddot{d}_q to get the following bound on c from [\(4.15\)](#page-13-0):

$$
c < 2 \times 10^{-5} \quad \text{for} \quad m_\chi < 10^{-13} \text{ eV}.\tag{4.16}
$$

This means that a modulus with $m_{\chi} < 10^{-13}$ eV and $(\tilde{d}_g - \tilde{d}_q)/(\tilde{d}_g + \tilde{d}_q) = \mathcal{O}(1)$ is again not useful for relaxing the bound (3.10) .

The light modulus χ which may have a sizable tadpole or runaway behavior at the pion extremum is constrained also by the cosmological modulus mass density generated by the modulus misalignment $\Delta \chi$ in the early Universe which is induced by the coupling c_{χ} . Note that a nonzero c_x means that χ couples to the gluons and/or the light quarks, so the thermal free energy of gluons and light quarks in the early Universe depends on χ . Such modulusdependent free energy induces a modulus misalignment, which eventually produces the modulus dark matter. To examine this issue, let us consider the finite temperature effective potential before the QCD phase transition, which is given by

$$
V(\chi,T) = -\frac{\pi^2}{90} g_*(T) T^4 + \frac{2T^2}{3} \left(3 + \frac{N_f}{2}\right) \frac{g_s^2(\chi) T^2}{6} + \sum_{m_q < T} \frac{T^2}{4} \left(m_q^2(\chi) + \frac{g_s^2(\chi) T^2}{6}\right), \tag{4.17}
$$

where g_* is the number of degrees of freedom contributing to the free energy and N_f is the number of quark flavors lighter than T. This potential provides a slope to the modulus χ as

$$
\frac{\partial V}{\partial \chi} = \frac{2\alpha_s^2 T^4}{9} \left(3 + \frac{7}{8} N_f \right) \left(b_3 \frac{\tilde{d}_g}{M_{\text{Pl}}} - \sum_{\Lambda_{\text{QCD}} < m_q < T} \frac{2}{3} \partial_\chi \ln(y_q v) \right) + \sum_{m_q < T} \frac{\tilde{d}_q m_q^2 T^2}{2M_{\text{Pl}}},\tag{4.18}
$$

which induces a modulus misalignment

$$
\frac{\Delta \chi}{M_{\rm Pl}} \simeq \frac{\partial_\chi V}{M_{\rm Pl} H^2}.\tag{4.19}
$$

Figure 1. Observational upper bound on the modulus coupling $c_{\chi} = \tilde{d}_{\tilde{q}} + 3\tilde{d}_{g}$ as a function of the modulus mass m_{χ} . The gray regions are excluded by the blackhole superradiance (BH-SR) [\[46\]](#page-19-4). The cyan region and the red region are excluded, respectively, by the composition-dependent [\[37,](#page-18-6) [47\]](#page-19-7) and composition-independent [\[48,](#page-19-8) [49\]](#page-19-9) equivalence principle (CD-EP and CI-EP) tests. Constraints on the parametrized post-Newtonian (PPN) parameters [\[34,](#page-18-4) [42–](#page-19-5)[45\]](#page-19-6) exclude the blue region, which applies not only for a generic modulus, but also for a metrical modulus respecting the equivalence principle. The dark matter relic abundance constrains the modulus misalignment, excluding the brown region.

We estimate such modulus misalignment at $T = T_{\chi} \simeq \sqrt{m_{\chi} M_{\text{Pl}}}$ and find

$$
\frac{\Delta \chi}{M_{\rm Pl}} \gtrsim 0.5 \frac{\left(3 + \frac{7}{8} N_f\right) \left(11 - \frac{2}{3} N_f\right)}{g_*(T_\chi)} \alpha_s^2(T_\chi) c_\chi + \sum_{m_q > T_\chi} \frac{0.4}{\sqrt{g_*(m_q)}} c_\chi \quad \text{for} \quad m_\chi > 10^{-11} \text{eV},
$$
\n
$$
\frac{\Delta \chi}{M_{\rm Pl}} \gtrsim 0.4 \, c_\chi \quad \text{for} \quad m_\chi \ll 10^{-11} \text{eV}, \tag{4.20}
$$

where for simplicity \tilde{d}_q and \tilde{d}_g are assumed to have a similar value. Requiring that the resulting modulus mass density does not exceed the observed dark matter mass density, i.e.

$$
\Omega_{\chi}h^2 < 0.12,\tag{4.21}
$$

we obtain the following bounds on the modulus coupling:

$$
c_{\chi} \lesssim \frac{2.2 \times 10^{-6}}{\alpha_s^2 (T_{\chi}) g_*^{-1} (T_{\chi}) + \sum_{m_q > T_{\chi}} 0.015 g_*^{-1/2} (m_q)} \left(\frac{10^{-12} \text{eV}}{m_{\chi}}\right)^{\frac{1}{4}} \quad \text{for} \quad m_{\chi} > 10^{-11} \text{eV},
$$

$$
c_{\chi} \lesssim 1.4 \times 10^{-4} \left(\frac{10^{-12} \text{eV}}{m_{\chi}}\right)^{\frac{1}{4}} \quad \text{for} \quad m_{\chi} \ll 10^{-11} \text{eV}.
$$
 (4.22)

In figure [1,](#page-14-0) we summarize the available constraints on the modulus coupling c_{χ} as a function of m_X . The blackhole superradiance (BH-SR) [\[46\]](#page-19-4) excludes the modulus mass

Figure 2. The refined upper bound on the parameter c as a function of the mass m_x of a moduluslike scalar field χ introduced to relax the original bounds [\(3.12\)](#page-9-2) and [\(3.13\)](#page-9-3). This shows that the original bounds are not significantly relaxed by additional light scalar once the observational constraints on such light scalar are properly taken into account.

range [\(4.13\)](#page-12-0) which corresponds to the gray region in figure [1.](#page-14-0) The cyan region bounded by a dotted line for $m_\chi < 10^{-12} \, {\rm eV}$ is excluded by the MICROSCOPE test of the composition-dependent equivalence principle (CD-EP) [\[37\]](#page-18-6), while the region above 10^{-12} eV is excluded by the short range test of the CD-EP [\[47\]](#page-19-7). If χ respects the equivalence principle, e.g. a metrical modulus χ with $d_q = d_q$, the CD-EP bounds do not apply anymore. Yet, for certain range of m_x , such metrical modulus can result in an observable deviation of the gravitational potential from $1/r$, which is bounded by the composition-independent equivalence principle (CI-EP) test. The red region of figure [1](#page-14-0) is excluded by such experiments testing the CI-EP [\[48,](#page-19-8) [49\]](#page-19-9). The blue region of figure [1](#page-14-0) is excluded by the measurement of the gravitational time delay to photons from the Cassini spacecraft in the parametrized post-Newtonian (PPN) formalism [\[34,](#page-18-4) [42](#page-19-5)[–45\]](#page-19-6), which applies not only for generic modulus, but also for a metrical modulus which respects the equivalence principle. Finally, the brown region is excluded by the bound on the relic modulus dark matter produced by the modulus misalignment induced by the coupling c_{χ} .

Since its coupling c_x is severely constrained as above, the modulus-like scalar χ can not significantly relax the bounds (3.12) and (3.13) which were obtained in the effective theory where χ is integrated out. In figure [2,](#page-15-0) we depict the refined bound on c taking into account the effects of χ for three different cases. The blue line is the bound for the case that both the quintessence ϕ and the additional modulus χ have generic couplings violating the equivalence principle, while the black (red) line corresponds to the case that $\phi(\chi)$ respects the equivalence principle. The results of figure [2](#page-15-0) can be extrapolated to $m_{\chi} \ll 10^{-21}$ eV in a straightforward manner. On the other hand, for $m_{\chi} > 10^{-6}$ eV, one can use [\(4.4\)](#page-11-2) and (4.5) to assure that the bounds (3.12) and (3.13) can not be relaxed by introducing χ .

With the above results, let us now regard (3.12) as the bound on c when both ϕ and χ have generic couplings to violate the equivalence principle, while (3.12) corresponds to the bound when any of ϕ and χ respects the equivalence principle. Then our results imply that those bounds on c can not be significantly relaxed by additional modulus-like light scalar field once the observational constraints on such scalar field are properly taken into account.[7](#page-16-1)

5 Conclusion

In this paper we examined the implications of the pion or Higgs dS extrema for the dS swampland conjecture, while focusing on the possible (model-independent or modeldependent) bound on the parameter c. Applying the dS swampland conjecture to the pion extremum at $\cos(\pi_0/f_\pi) = -1$, we could derive a model-independent upper bound on c given in terms of the low energy quintessence couplings.

If the quintessence couplings take a rather specific form to respect the equivalence principle, which would be the case when the quintessence couples to the SM sector only through the trace of the energy momentum tensor, c is bounded essentially by the observational bound on the deviation from the general relativity by the quintessence-mediated force in relativistic limit, yielding $c < 1.4 \times 10^{-2}$. However, for generic quintessence whose couplings violate the equivalence principle, the parameter c is more strongly bounded as $c < 2 \times 10^{-5}$ by the non-observation of the violation of the equivalence principle in nonrelativistic limit. These bounds on c are rather robust as (i) they are obtained within the framework of the most general quintessence potential and couplings and (ii) they can not be significantly relaxed by an additional light scalar field which may have a nonzero tadpole or runaway behavior at the pion dS extremum, if the observational constraints on such light scalar field are properly taken into account. One can do a similar analysis for the Higgs extremum at $H = 0$, but the resulting bound $c \lesssim 4.4 \times 10^{-2}$ is weaker than those from the pion extremum as the quintessence couplings to the Higgs sector is more weakly constrained than those to the low energy QCD sector.

Our bounds on c from the pion extremum appear to have a significant tension with the dS swampland conjecture [\(1.1\)](#page-1-1) which assumes $c = \mathcal{O}(1)$. Yet the conjecture (1.1) can be modified or refined, for instance as in $[7, 8]$ $[7, 8]$ $[7, 8]$ and $[9]$, which would allow us to avoid the bounds from the Higgs and pion extrema. If it is the right direction to pursue, our results provide additional motivation for such refinement of the conjecture.

Acknowledgments

This work was supported by IBS under the project code IBS-R018-D1. K.C. thanks A. Hebecker for useful discussions. C.S.S. thanks Deog Ki Hong for valuable discussions during the CERN-Korea TH Institute, and also the CERN Theory Group for the hospitality.

⁷Our result suggests that the stronger bound (3.12) can be relaxed by about one order of magnitude by a modulus χ with $m_{\chi} = \mathcal{O}(10^{-13})$ eV. However this minor point does not change the main message of our results.

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