



Low Earth Orbiter



LAGEOS 1/2

## Realization of reference frames based on integrated SLR measurements to LEO and LAGEOS satellites

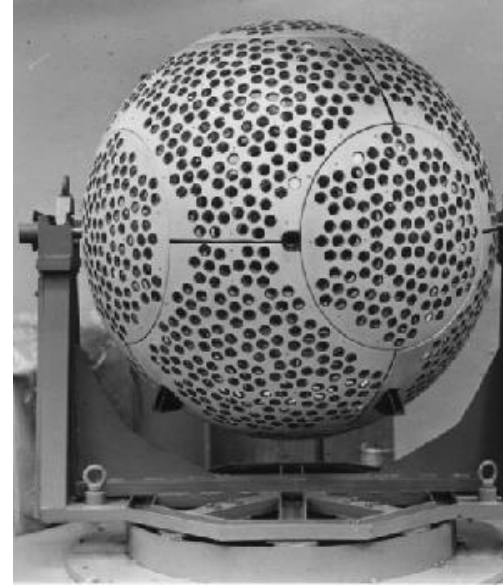
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# Motivation



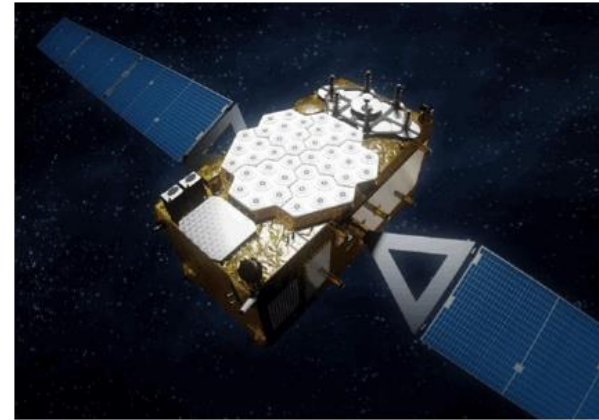
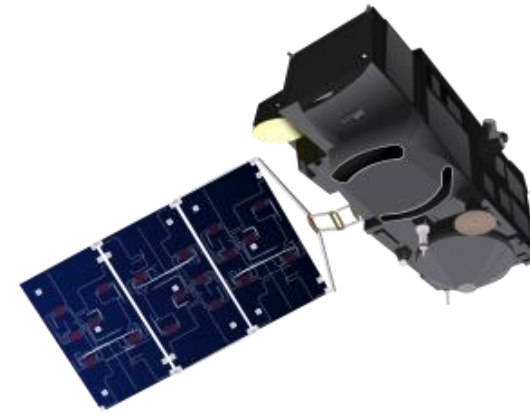
**LAGEOS1/2**



**Etalon 1/2**

**Satellite Laser Ranging (SLR) measurements to passive geodetic satellites (LAGEOS & Etalon) are used for the realization of reference frames (e.g. ITRF2014)**

# Motivation



**retroreflectors**

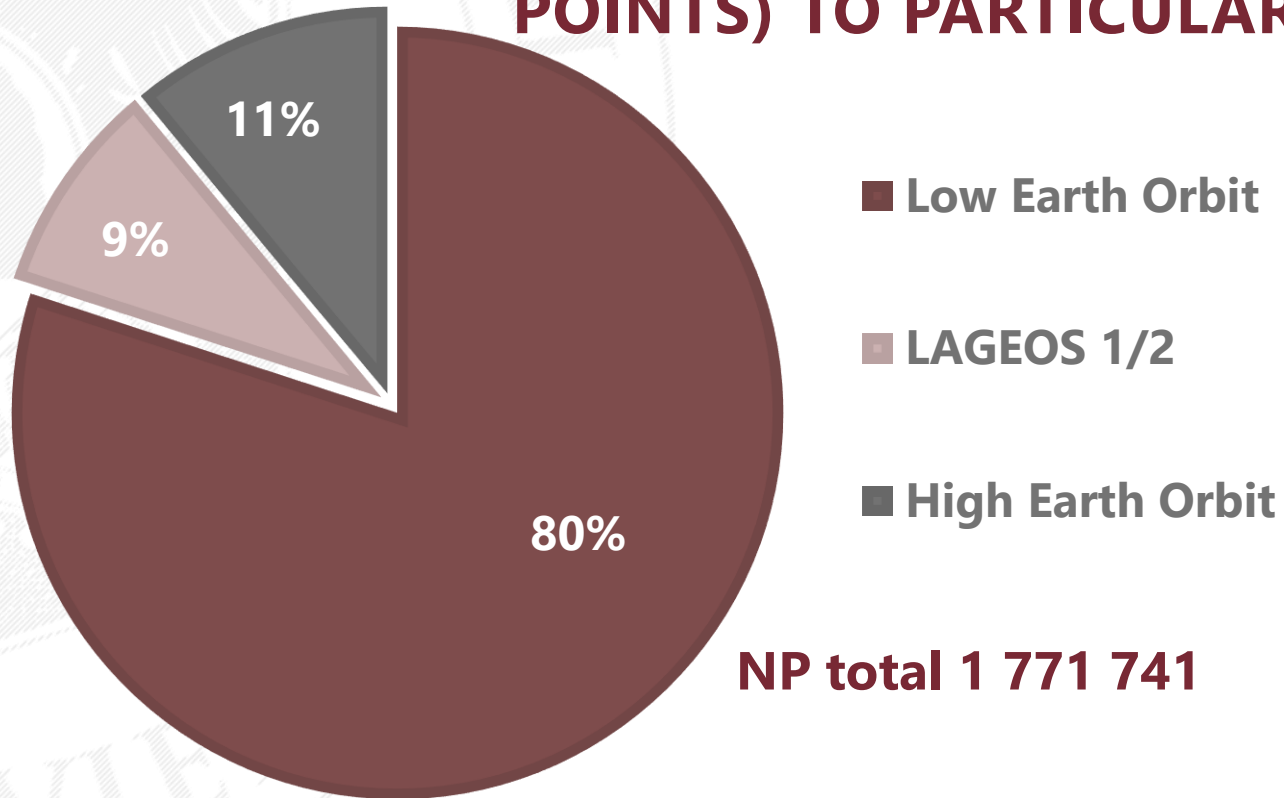
**GNSS or active Low Earth orbit (LEO) satellites are equipped with retroreflectors, which allow for SLR measurements**

# Motivation



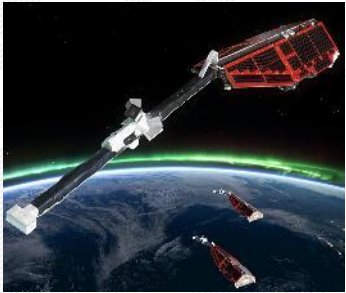
**International Laser Ranging Service (ILRS) initiates a series of intense tracking campaigns for GNSS and LEO satellites**

## **PERCENTAGE OF SLR OBSERVATIONS (NORMAL POINTS) TO PARTICULAR SATELLITE TYPES IN 2017**

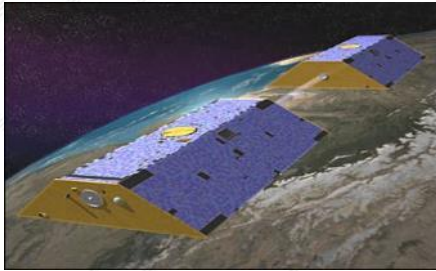


**Only 9%** of all SLR measurements are used currently for the reference frames realization, determination of Earth rotation parameters (ERP), and geocenter coordinates

# SLR measurements



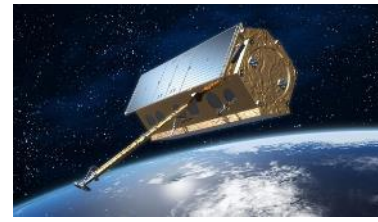
SWARM-A/B/C



GRACE-A/B



Jason-2



TerraSAR-X



SENTINEL-3A

- *ESA, NASA, EUMETSAT, GFZ DLR, CNES*
- *active Low Earth Orbit satellites*
- *GNSS receivers onboard*
- *satellites with different weight, shape, equipment, orbit parameters*
- *precise GPS-based orbits and attitude data*

**Active satellites**

SLR



orbit validation

*LAGEOS-1, LAGEOS-2*

- *NASA and ASI*
- *used for relativistic effects, gravity field, geodynamics, ERP, geocenter coordinates research by SLR measurements*
- *passive, spherical, geodetic satellites, with low area-to-mass ratio*
- *equipped with 426 retroreflectors dedicated for SLR technique*

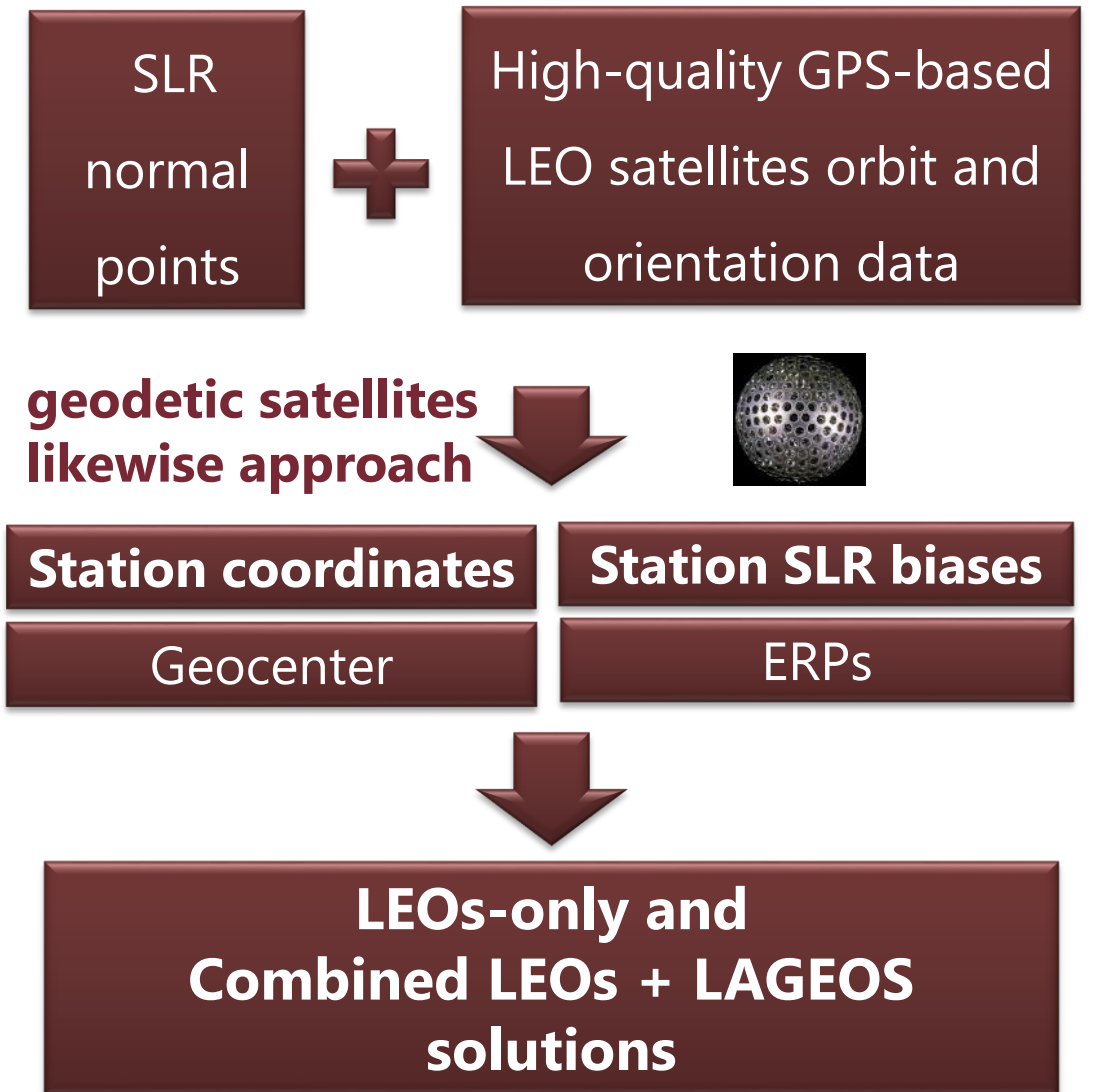
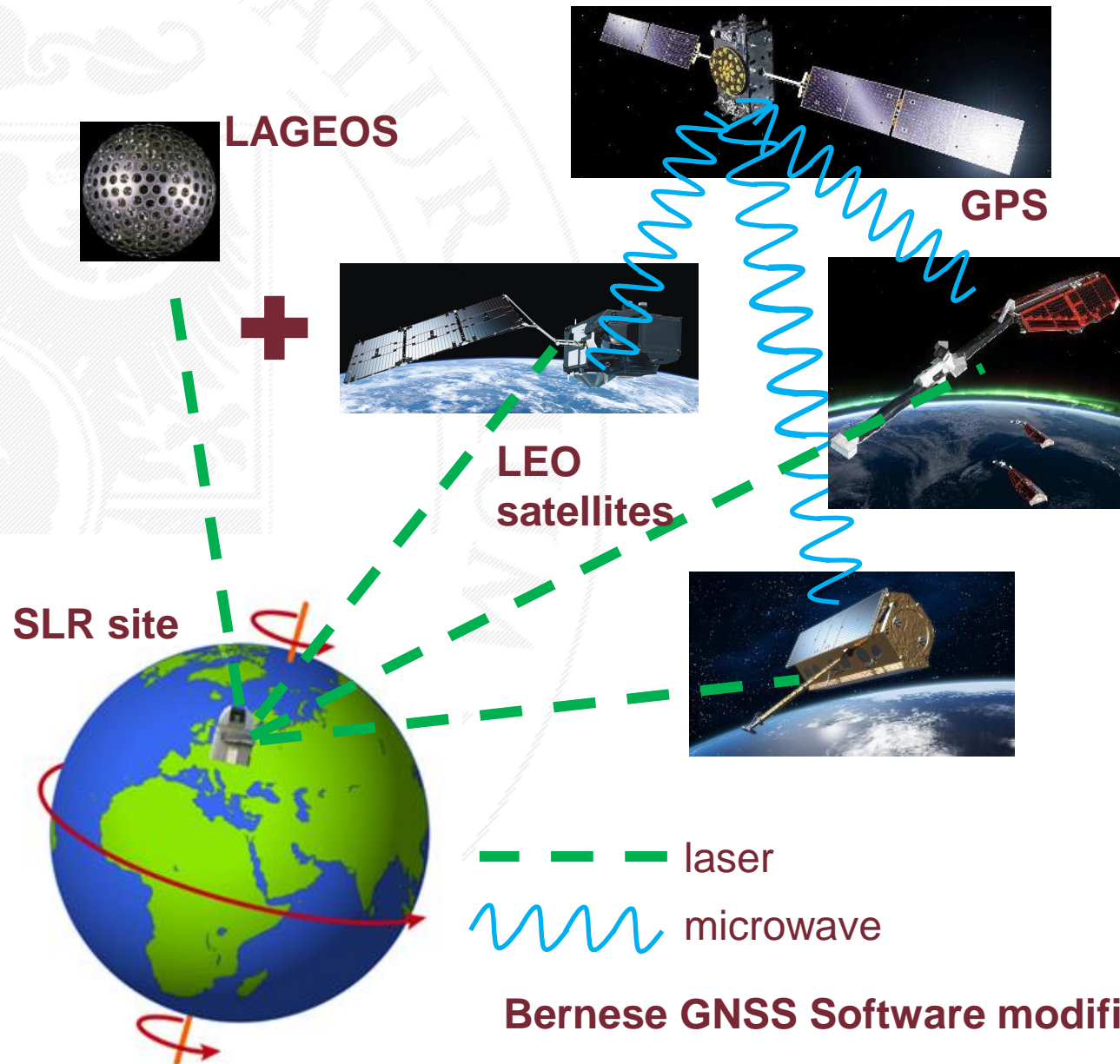
**Passive satellites**

SLR



station coordinates, geocenter coordinates, ERP, scale, relativistic effects validation

# LEOs GNSS- and SLR- based analysis



Bernese GNSS Software modified 5.3 Version

# Solution tests– SLR to LEOs

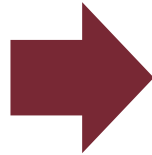
## Solution tests: different network and parameters constraining and a different number of accumulated 1-day orbit combination

**Test1:** network constraining: no-net-translation (NNT) no-net-rotation (NNR) with estimation of parameters



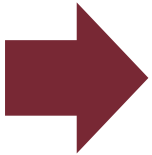
SLR station coordinates, geocenter, ERPs

**Test2:** network constraining: no-net-translation (NNT) no-net-rotation (NNR) without estimation of parameters



SLR station coordinates

**Test3:** no network constraining and without estimation of parameters



SLR station coordinates

**Time span: 2016-2017**

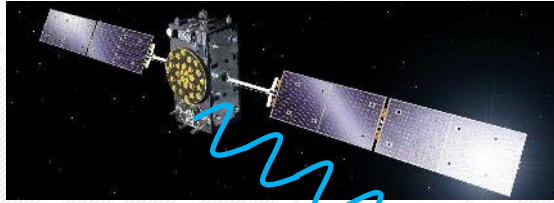
**LEO satellites  
(fixed GPS-based orbits)**



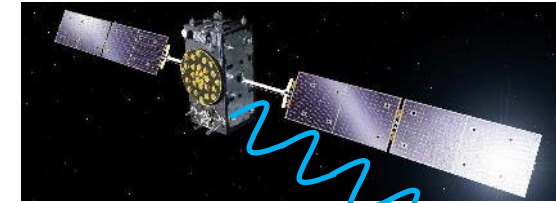
# The issue of the reference frame differences

## Test 3 no network constraints

### Test 1 with NNT/NNR constraints



**GNSS – IGS14**  
integrated around  
Center-of-Figure (CoF)



**GNSS – IGS14**  
integrated around  
Center-of-Figure (CoF)

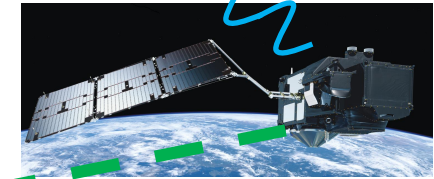


**SLR sites in SLRF2014**  
(CoF by NNT/NNR)

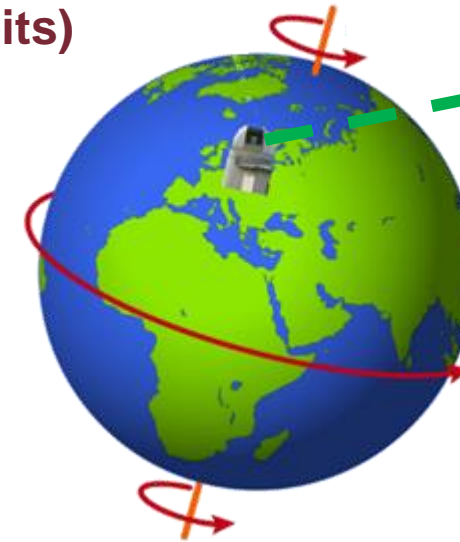


**LEO – IGS14**, but pseudo-stochastic orbit parameters are estimated → larger flexibility, close representation of the Earth's Center-of-Mass (CoM)

**SLR sites IGS14**  
(reference frame transferred through LEO orbits)



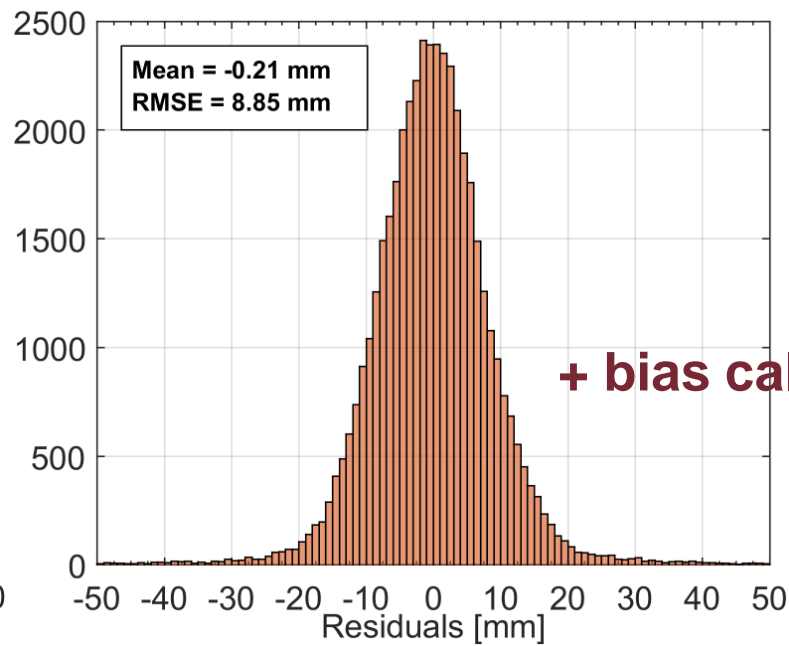
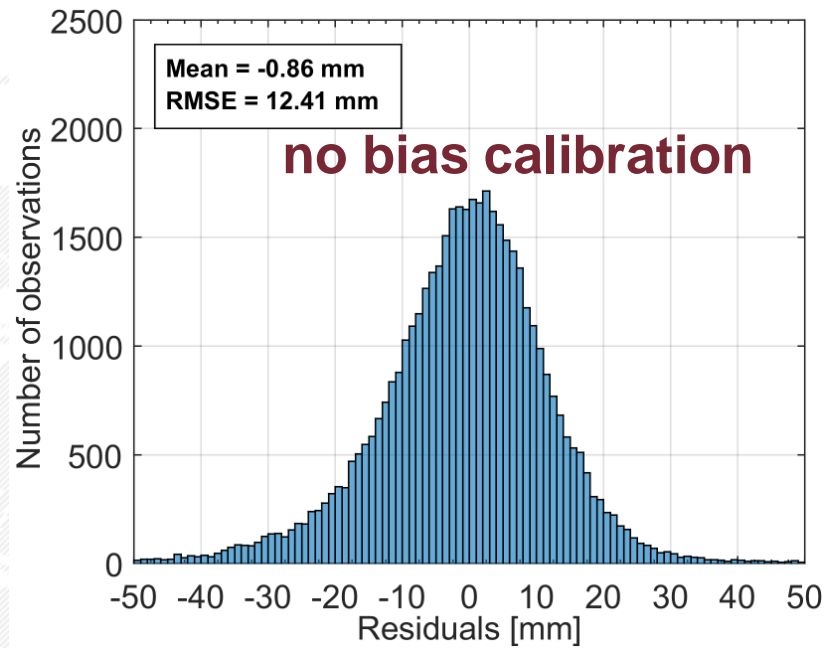
**LEO – IGS14**,  
reduced



**In SLR-PPP (test3)**  
SLR station coord.  
are in IGS14

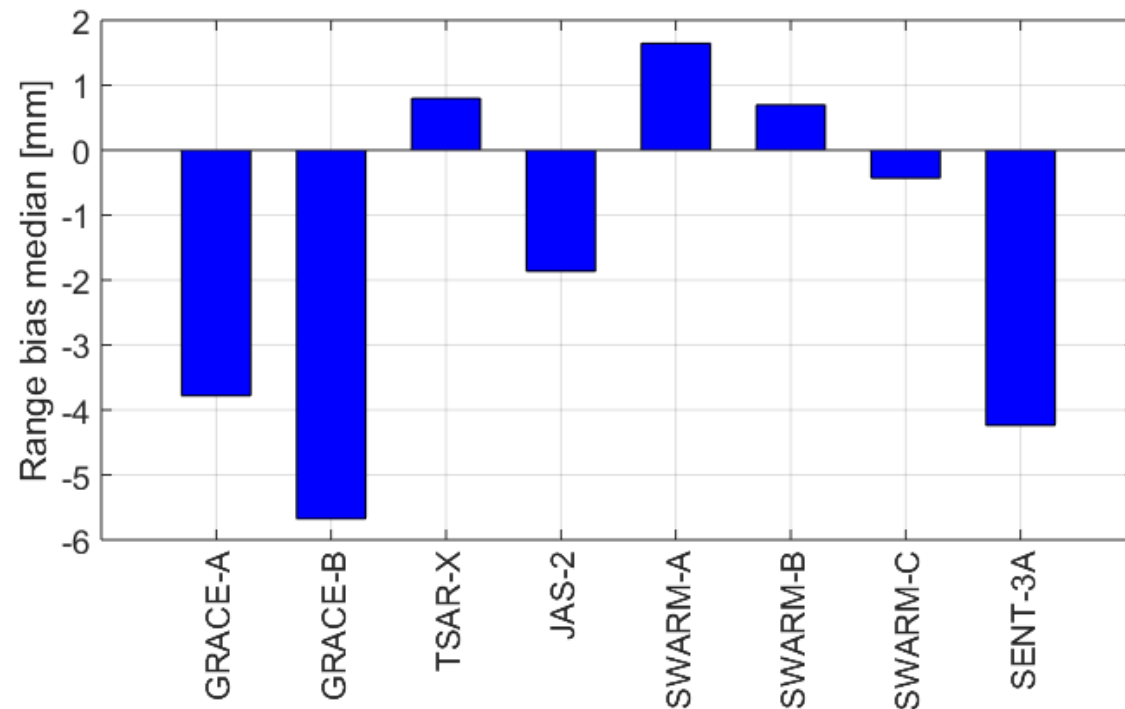
**CoM vector w.r.t. CoF represents geocenter motion, but to what extent IGS14 and SLRF2014 are consistent**





## Importance of proper SLR station bias calibration for LEOs

Example of SLR residuals to Sentinel-3A GPS based orbits without and with bias calibration



Each satellite requires different bias correction

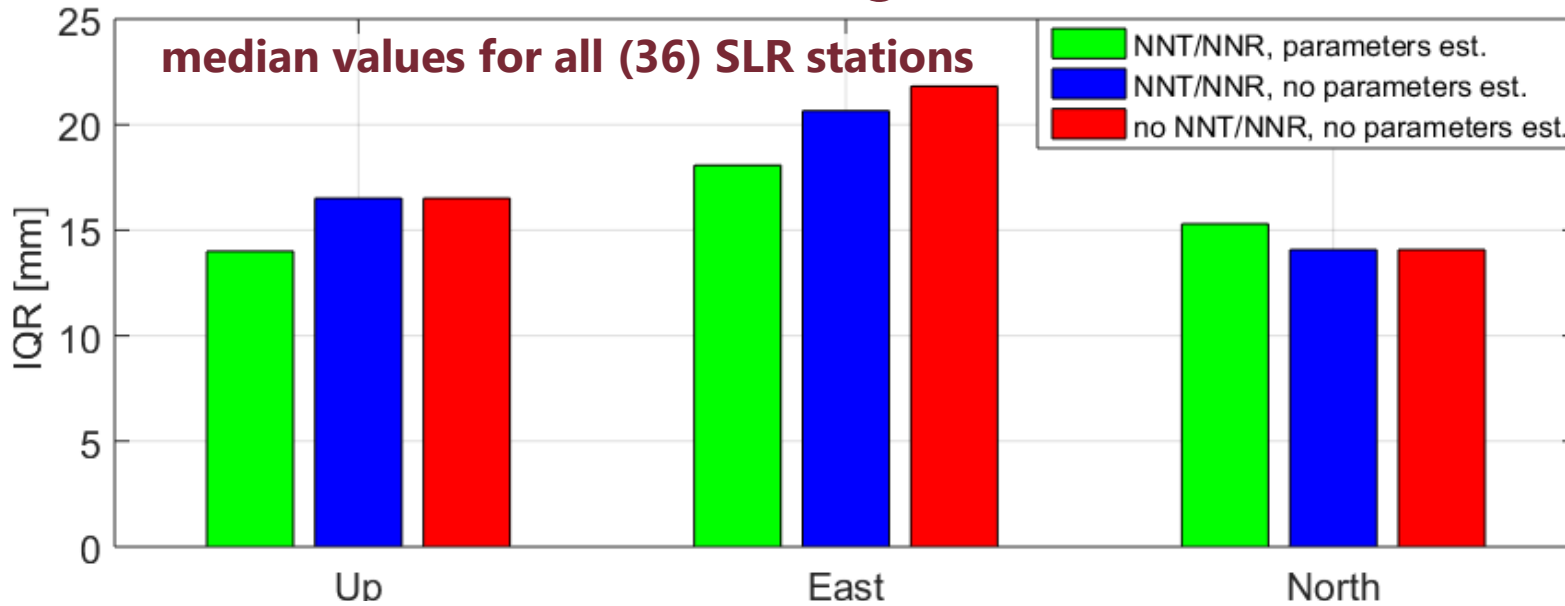


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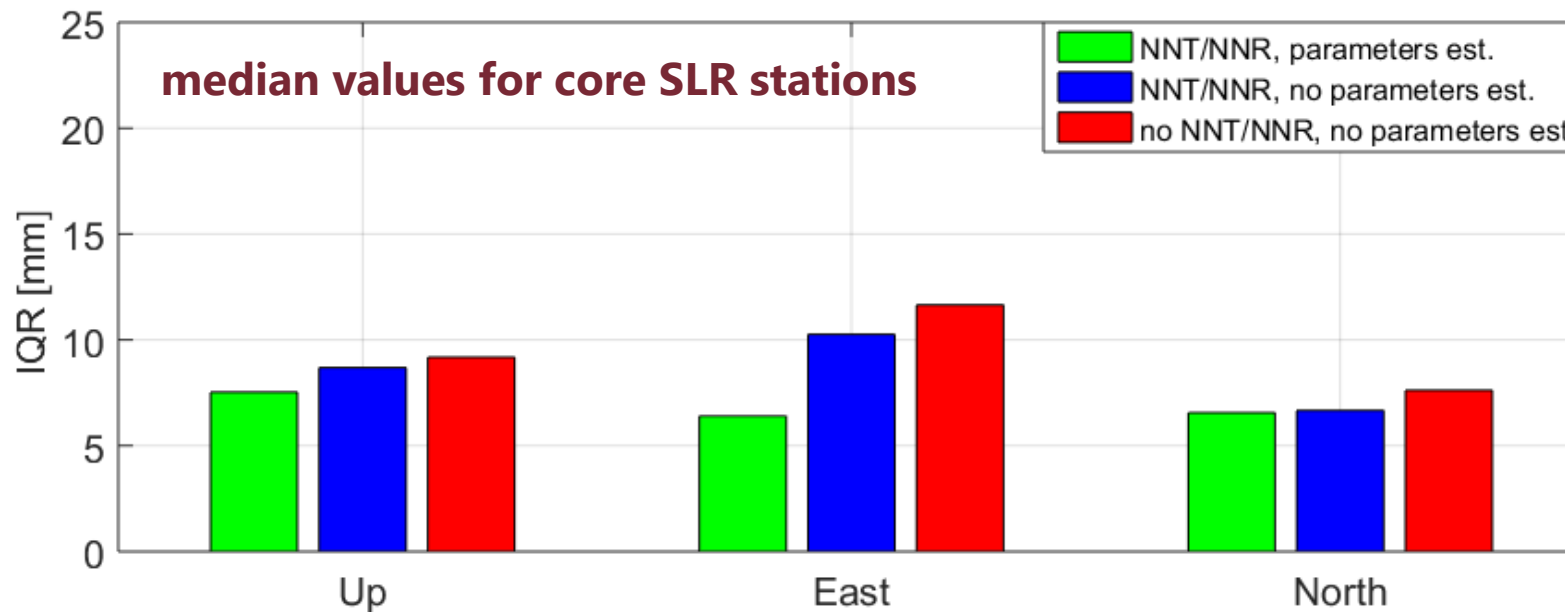
RESULTS

# TEST 1: A different constraining for LEOs

Station coordinates  
(w.r.t ITRF2014)



The positioning of **all SLR stations** with the accuracy at the level of **less than 22 mm**, even without network constraining

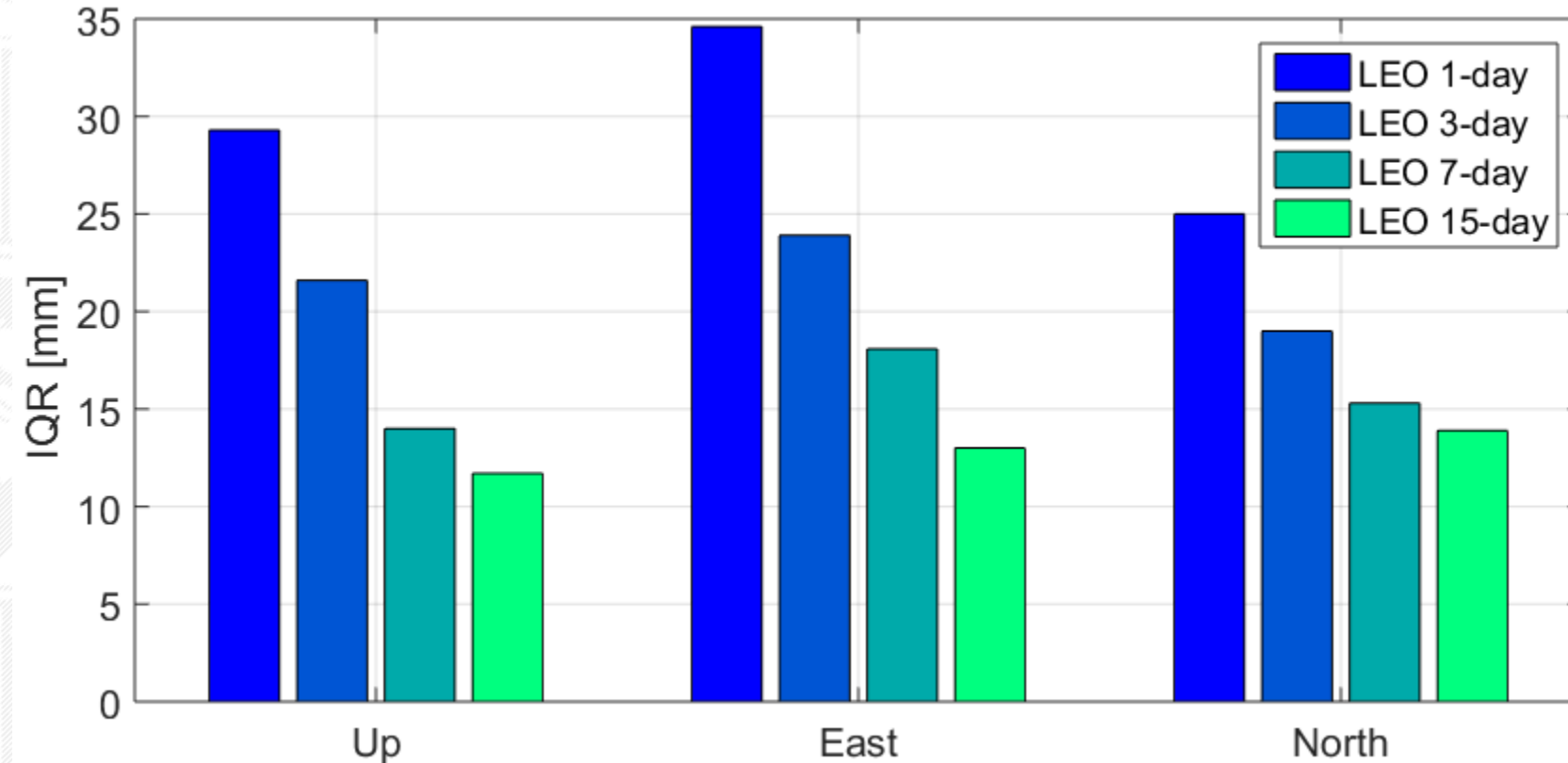


The positioning of **core SLR stations** with the accuracy at the level of **10 mm is possible!**

Even without network constraining (blue) provides proper station coordinates (8-12mm-top sites)

Core stations: Yarragadee, Greenbelt, Matera, Hartebeesthoek, Haleakala, Zimmerwald, Mt Stromlo, Graz, Herstmonceux, Potsdam

## TEST 2: A different number of accumulated 1-day orbits- LEO



### Statistics for all SLR sites

1-day, 3-day LEO solutions are insufficient for high-quality coordinates

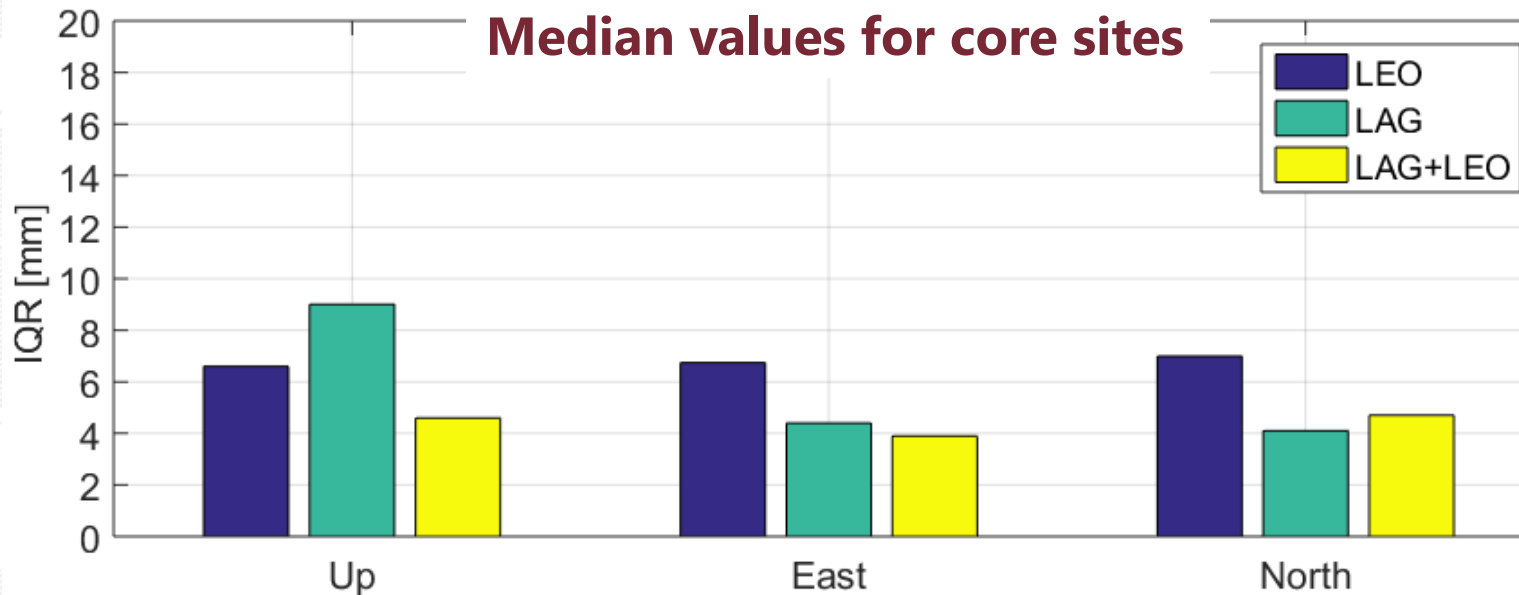
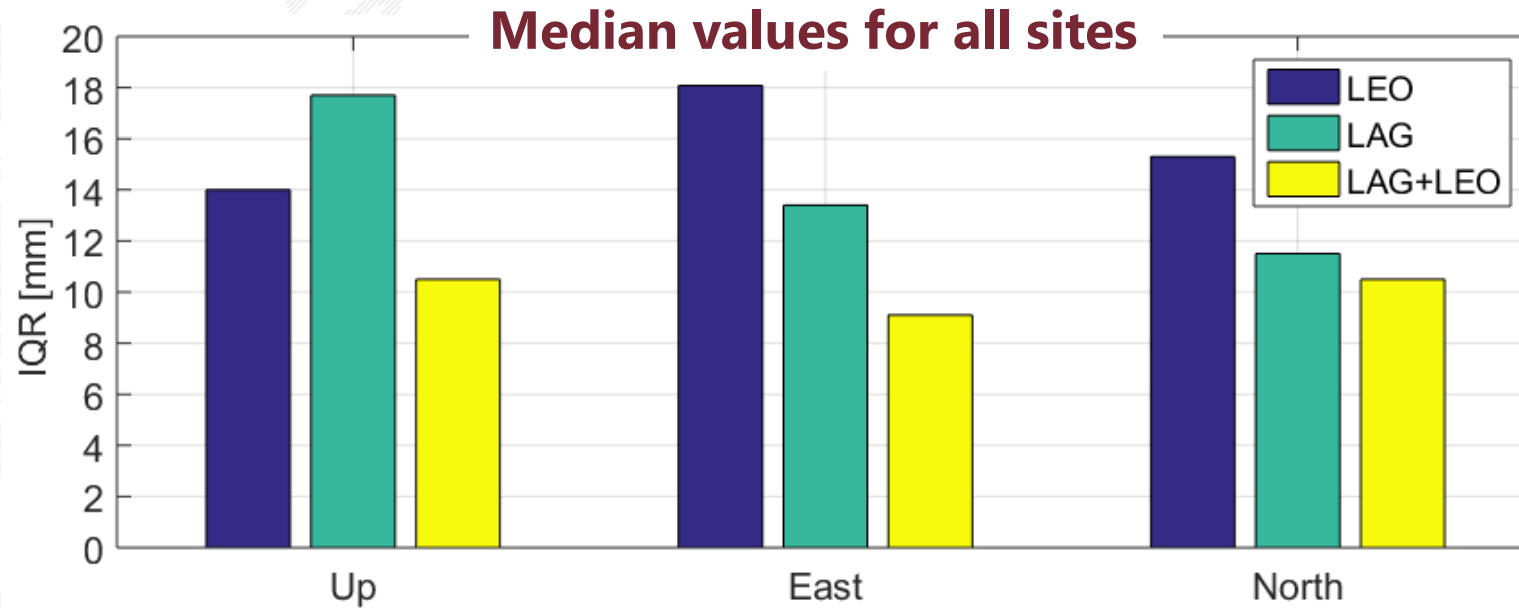
Good global coverage can be achieved in **7-day solutions**

**Different number of accumulated orbits  
median values for all (36) stations**

Station coordinates  
(w.r.t ITRF2014)

# Combined solution results and comparison

Station coordinates  
(w.r.t ITRF2014)



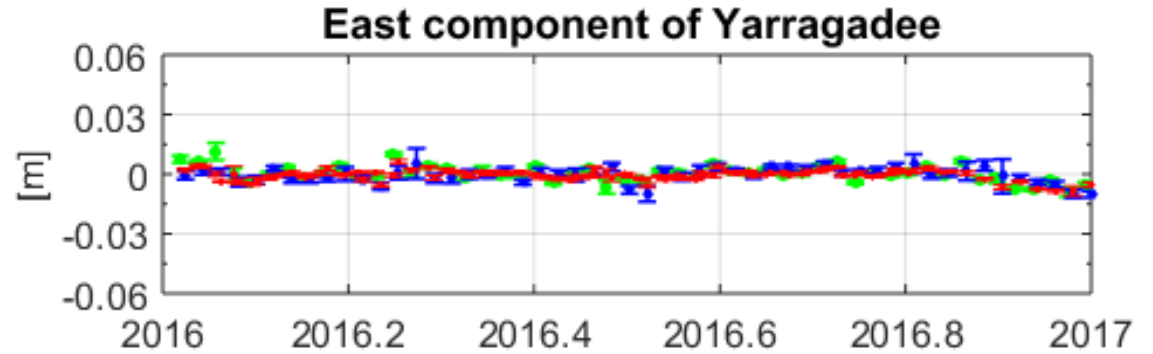
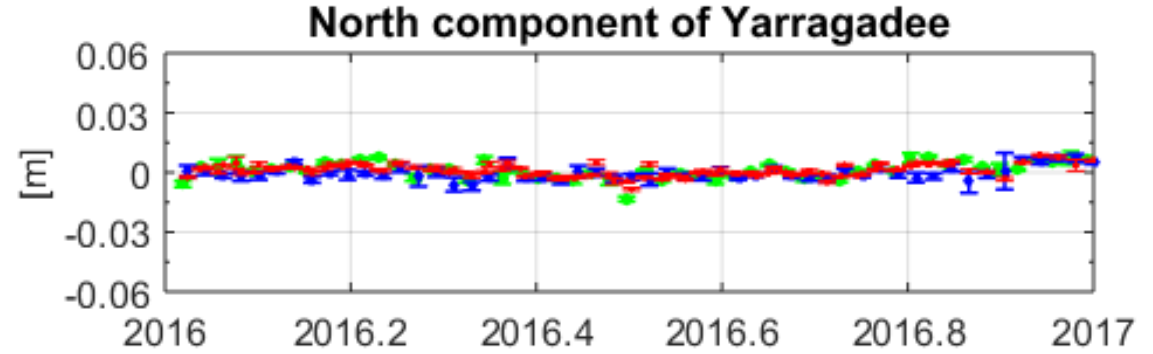
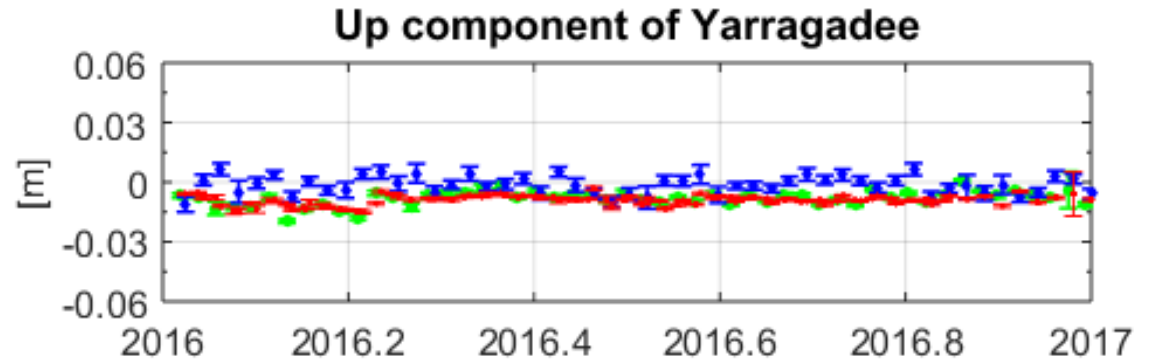
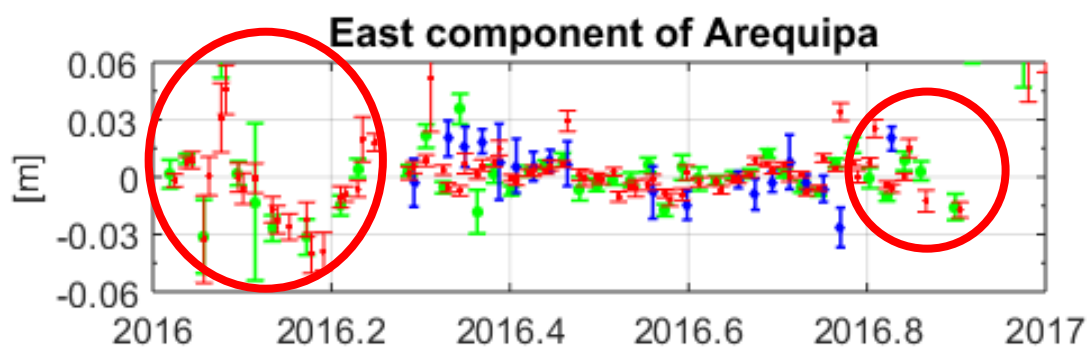
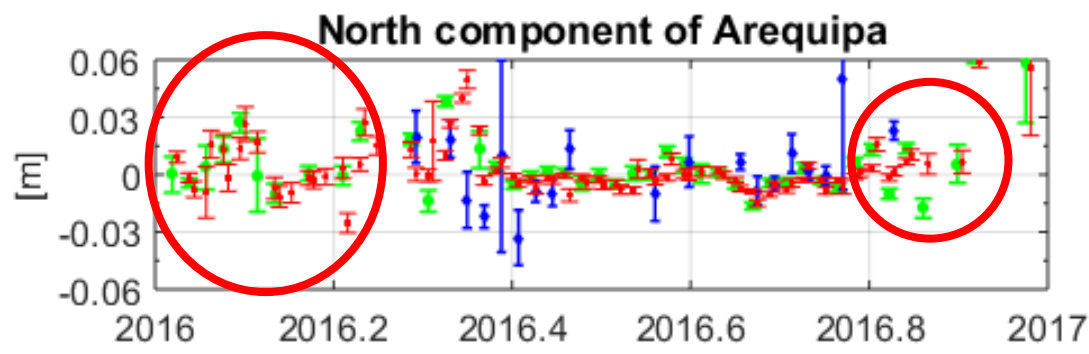
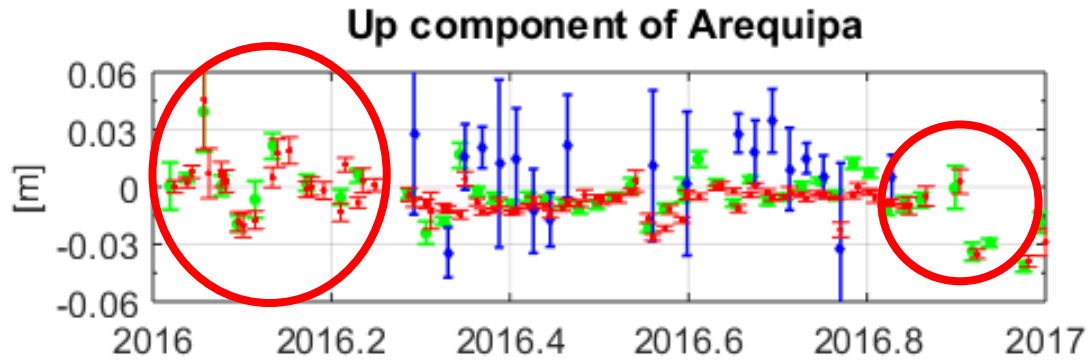
## Determination strategy:

- NNT/NNR with estimation of parameters
- 7-day accumulated orbits
- Introduction of annual range bias for LEOs in all solutions
- Weighting of observations in LAG+LEO solution ( $\sigma=10\text{mm}$  for LAG,  $\sigma=20\text{mm}$  for LEOs)

## SLR sites statistics

- LEOs are slightly better for the Up component
- LAGEOS is better for the horizontal components
- **Best results** for all components in the **combined solution**

# Number of obs. increase



LEOs-only solutions when LAGEOS not tracked-  
number of obs. increase

Station coordinate repeatability for Yarragadee falls  
between 5 and 11 (IQR) mm for individual components.

## Summary

SLR stations have been providing **observations to a large number** of new active **LEOs and GNSS**

SLR observations to active LEO satellite require a **proper station bias calibration**

SLR data and high-quality GPS-based orbits of LEOs allow for the determination of **station coordinates with the accuracy of 10 mm** (core sites), even without network constraining

**Reference frame realization based on SLR measurements to LEOs is possible**

Best results are obtained from the combined LAGEOS+LEOs solution

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