

1 **Contingent Convergence: The ability to detect convergent genomic**
2 **evolution is dependent on population size and migration**

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21 **ABSTRACT**

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Outlier scans, in which the genome is scanned for signatures of selection, have become a prominent tool in studies of local adaptation, and more recently studies of genetic convergence in natural populations. However, such methods have the potential to be confounded by features of demographic history, such as population size and migration, which are considerably varied across natural populations. In this study, we use forward-simulations to investigate and illustrate how several measures of genetic differentiation commonly used in outlier scans (F_{ST} , D_{XY} and $\Delta\pi$) are influenced by demographic variation across multiple sampling generations. In a factorial design with 16 treatments, we manipulate the presence/absence of founding bottlenecks (N of founding individuals), prolonged bottlenecks (proportional size of diverging population) and migration rate between two populations with ancestral and diverged phenotypic optima. Our results illustrate known constraints of individual measures associated with reduced population size and a lack of migration; but notably we demonstrate how relationships between measures are similarly dependent on these features of demography. We find that false-positive signals of convergent evolution (the same simulated outliers detected in independent treatments) are attainable as a product of similar population size and migration treatments (particularly for D_{XY}), and that outliers across different measures (for e.g. F_{ST} and D_{XY}) can occur with little influence of selection. Taken together, we show how underappreciated, yet quantifiable measures of demographic history can influence commonly employed methods for detecting selection.

44 **INTRODUCTION**

45 Studies assessing adaptation and evolution across the genome are increasing in popularity
46 with the availability of modern sequencing technologies. These studies often centre around
47 quantifying patterns of variation in genome-wide SNPs, which can be used to highlight
48 regions or genes having experienced selection relative to the neutral backdrop of the rest of
49 the genome. These analyses, which we refer to here as outlier scans, have become a
50 common tool in population genetics and have been useful across diverse, natural systems in
51 identifying candidate genes associated with the evolution of a range of adaptive traits
52 (reviewed recently by (Ahrens *et al.* 2018)). More recently, the method of overlapping
53 outlier scans across independent lineages has been employed to test whether the same
54 regions are involved in independent adaptation events (i.e. genetic convergent evolution)
55 (reviewed by (Fraser and Whiting 2019)). This study seeks to investigate how different
56 outlier scan methods are influenced by demographic variation in natural populations, and
57 how this may lead to overlapping false-positives.

58

59 Recent discussions have highlighted the propensity of outlier scans to yield false-positives,
60 given that outliers caused by heterogeneous genomic landscapes are commonplace
61 irrespective of selection (Ellegren and Wolf 2017). For example, background selection (BGS),
62 whereby linkage between neutral and deleterious variants reduces local diversity
63 (Charlesworth *et al.* 1993; Bank *et al.* 2014; Burri 2017), has been invoked to offer
64 alternative explanations for patterns at first attributed to directional selection (Cruickshank
65 and Hahn 2014). Furthermore, the influence of neutral processes such as genetic drift
66 (Charlesworth 2009) can similarly produce elevated genetic divergence and false-positive
67 signatures of selection.

68

69 The strength of these processes is dependent on demography. For example, the influence of
70 neutral processes and BGS should be more pronounced in smaller populations (low N_e)
71 (Charlesworth *et al.* 1995; Charlesworth 2009; Yeaman and Otto 2011; Cutter and Payseur
72 2013); as has been demonstrated in humans (Torres *et al.* 2018) and *Drosophila*
73 (Charlesworth 1996; Sella *et al.* 2009). This relationship, however, may not be simply linear,
74 with additional simulation evidence suggesting the effects of BGS are strongest at
75 intermediate-low N_e , and weaker at very low or high N_e (Zeng 2013).

76

77 Lack of connectivity among populations may also elevate measures of genetic
78 differentiation, if a large global population is composed of smaller, isolated, sub-divided
79 populations that each experience the effects of reduced N_e (Charlesworth *et al.* 1997;
80 Hoban *et al.* 2016). In an attempt to mitigate the likelihood of false-positives, some have
81 advocated using multiple measures of population differentiation and divergence to identify
82 regions of the genome likely to be under selection (Charlesworth 1998; Cruickshank and
83 Hahn 2014). However, how these measures are correlated with each other, and with
84 selection under different demographic scenarios, has not been explored.

85

86 A diverse array of measures of genetic differentiation and divergence have been employed
87 for outlier scans, but here we focus on two of the most common measures of relative
88 differentiation (F_{ST} and changes in nucleotide diversity [$\Delta\pi$]) and a measure of absolute
89 divergence (D_{XY}). The fixation-index F_{ST} (Weir and Cockerham 1984; Hudson *et al.* 1992),
90 which measures the relative amount of within- and between-population variance. This
91 measure is therefore maximised when genomic regions exhibit the lowest within- and
92 highest between-population variance. F_{ST} outliers at the right-tail of the distribution are

93 considered candidates for adaptation because they reflect regions with large differences in
94 allele frequency or high substitution rate (large between-population variance) and/or low
95 nucleotide variation (low within-population variance) relative to the rest of the genome.
96 Changes in nucleotide diversity ($\Delta\pi$) are another indicator of adaptation, as selection on a
97 beneficial allele limits variation within a population resulting in selective sweeps (Smith and
98 Haigh 1974). Comparisons of the ratio of π between diverging populations reveal regions
99 under selection, as local π is reduced in one population in comparison to the other. Whilst
100 similar to F_{ST} , $\Delta\pi$ does not discriminate between which copy of a polymorphism is fixed,
101 such that a substitution between populations is equivalent to a common non-polymorphic
102 site. $\Delta\pi$ outliers therefore represent regions of the genome with reduced π in either
103 population relative to the rest of the genome. As a measure of absolute genetic divergence,
104 D_{XY} (Nei 1987) does not consider the relative frequencies of polymorphisms within
105 populations (Charlesworth 1998; Cruickshank and Hahn 2014). D_{XY} can be quantified as the
106 average number of pairwise differences between sequence comparisons between two
107 populations. This measure is therefore influenced by ancestral π and the substitution rate,
108 so D_{XY} outliers highlight regions that are highly variable ancestrally, or in either population
109 (large π), or exhibit many substitutions and thus increased sequence divergence.

110

111 Because each measure of differentiation/divergence (hereafter referred to collectively as
112 measures of divergence) quantifies genetic variation between populations in a slightly
113 different way, each has a unique relationship with demography. Whilst we can predict how
114 individual measures are influenced by demography, and subsequently neutral processes, we
115 know little about how different relationships between measures of divergence and

116 demography affect their combined usage. We expect then that the utility of using multiple
117 measures of divergence to detect selection may vary with demography.

118

119 This complex interplay between divergence measures and demography may be further
120 exacerbated in studies that compare scans from multiple populations to identify convergent
121 genomic evolution. Here, researchers use measures of population divergence across
122 independent pairs of evolutionary replicates with outlier loci compared across results. This
123 strategy has been employed extensively across diverse taxa, including: birds (Cooper and Uy
124 2017), fish (Hohenlohe *et al.* 2010; Jones *et al.* 2012a; Fraser *et al.* 2015; Reid *et al.* 2016;
125 Rougemont *et al.* 2017; Meier *et al.* 2018), insects (Soria-Carrasco *et al.* 2014; Van
126 Belleghem *et al.* 2018), mammals (Waterhouse *et al.* 2018), molluscs (Westram *et al.* 2014;
127 Ravinet *et al.* 2016) and plants (Roda *et al.* 2013; Trucchi *et al.* 2017). For the sake of
128 consistency, it is common to infer outlier loci within each replicate pair through a common
129 method, but if replicates differ in their demographic histories then the applicability/power
130 of that common method will also vary accordingly. This begs the question, can demographic
131 variation among replicates alone explain signals of, or lack of, convergence?

132

133 Here, we used forward-simulations to investigate the effects of different demographic
134 histories on the relationships between measures of divergence with selection. We varied
135 demography through manipulating the number of founding individuals (founding
136 bottlenecks), the population size of the diverging population (prolonged bottlenecks) and
137 the presence/absence of migration. We simulated the effects of selection on 25kb regions,
138 each with a gene designed from features taken from the guppy (*Poecilia reticulata*) genome
139 assembly, a prominent model system for studies of convergent evolution (Reznick and

140 Endler 1982; Fraser *et al.* 2015). Moreover, we measured genetic divergence at 12 set time
141 points through F_{ST} , D_{XY} and $\Delta\pi$ between diverging populations to examine temporal
142 relationships. Our aim was to investigate the significance of founding/prolonged bottlenecks
143 and migration between populations when employing outlier scans, and highlight
144 demographic scenarios that are susceptible to false-positives. We also aimed to test the
145 occurrence of common outliers across measures, and whether overlapping outliers are
146 consistently good indicators of selection. We sought to answer the following questions: 1)
147 How do these demographic factors influence measures of divergence through time? 2) How
148 well do measures of divergence identify regions of the genome under strong selection
149 through time and across demographic factors? 3) How are the different measures of
150 divergence related through time and across demographic factors? 4) Where do we detect
151 the strongest signals of convergence (i.e. overlapping outliers using single or multiple
152 measures), and are these consistent with selection?

153

154 **METHODS**

155 The forward-simulation software SLiM 3.0 (Haller and Messer 2019) was used to simulate
156 population divergence under contrasting demographic treatments in a fully factorial design
157 between a population with an ancestral phenotype (AP) of $N = 1000$ and population with a
158 diverged phenotype (DP), with a mutation rate based on the guppy genome ($4.89e^{-8}$)
159 (Künstner *et al.* 2016) and scaled 100-fold over three raw mutation rates ($4.89e^{-5}$, $4.89e^{-6}$,
160 $4.89e^{-7}$) to ensure robustness of results across different, more realistic values of θ ($4N_e\mu$).
161 These scaled mutation rates therefore represent effective population sizes of 10-, 100-, and
162 1000-times greater than the number of individuals in our simulations ($N = 1000$), in line with
163 estimates from other species (Charlesworth 2009). The main text reflects results for the

164 intermediate mutation rate $4.89e^{-6}$, with others presented in supplementary figures. SLiM
165 employs a classic Wright-Fisher model to simulate populations, in which a population of
166 diploid hermaphrodites proceeds through generations such that an individual's contribution
167 towards the next generation is proportional to its relative fitness.

168

169 Demographic treatments included reducing DP size (prolonged bottlenecks) relative to the
170 AP size ($N = 1000$) (0.01, 0.1, 0.5, 1.0), migration as a proportion of individuals exchanged
171 between populations (0.0, 0.002) and founding bottlenecks as the number of individuals
172 sampled from the burn-in population to construct DP genomes ($N = 100$ or 1000). For
173 example, a demographic history with founding bottleneck = 100 individuals, DP size = 0.01,
174 and migration = 0.002 would represent the following scenario: 1) At generation 1, following
175 a burn-in period of 10,000 generations to reach mutation-selection balance, populations
176 split as 100 genomes are sampled from the burn-in population of 1000 to form DP, whilst AP
177 is formed by sampling all 1000 burn-in genomes; 2) At the next generation (and for the
178 remainder of the simulation), DP size reflects the prolonged bottleneck treatment, in this
179 case 10 (0.01 of 1000); 3) AP and DP experience migration in both directions for the
180 remainder of the simulation. Thus, each of our treatments can be thought of as a
181 manipulation of the following: Founding bottlenecks limit the amount of variation within
182 the burn-in population that is available to found DP; Prolonged bottlenecks limit the size of
183 DP, reducing mutational input and moderating the strength of neutral evolution and efficacy
184 of selection; and migration dictates the presence of migration between AP and DP (Figure
185 1). The total N of individuals (AP + DP) within simulations varies between 1010 and 2000
186 depending on DP size parameter, however this potential expansion does not impact our
187 results (Supporting Information).

188

189 Combining these treatment levels in a fully factorial experimental design generated a total
190 of 16 different, independent demographic histories that all 25kb gene regions (see below
191 for architecture) experienced. This factorial design allows us to examine the relative
192 influence of founding bottlenecks, prolonged bottlenecks and migration, but our study is
193 limited to these features of demographic history and does not extend to population
194 expansions, more complex cases of migration, or demographic fluctuations through time. In
195 some cases, the influence of prolonged bottlenecks renders the effects of founding
196 bottlenecks unnecessary. However, when DP size is greater than 100, the inclusion of the
197 founding bottleneck allows us to compare populations with equivalent mutational input but
198 different standing variation.

199

200 SLiM runs were performed independently over 25kb genomic regions with a central 'gene'
201 that functioned as a QTL and varied in length and exon content (Figure 1E); with exon
202 number, lengths, and intron lengths drawn at random from the guppy genome gene
203 annotation file (gff). In total, we simulated a dataset of 100 25kb regions (Figure 1F).

204 Recombination rate was scaled alongside mutation rate from a human-derived $r = 1e^{-8}$ to $1e^{-6}$.
205

206

207 Selection (S) in our model was represented as the fitness consequences incurred through
208 distance from a phenotypic optimum in a one-dimensional fitness landscape. Selection in
209 Wright-Fisher models is soft, in that low fitness individuals are not removed but have a
210 lower likelihood of contributing to the next generation. Phenotypic optima were maintained
211 over the course of simulations; thus, selection was constant throughout. This setup can be

212 considered as analogous to two environments with contrasting optimum trait values for a
213 single trait. Intensity of selection was manipulated by modifying the standard deviation (S_σ)
214 of the normal distribution curve from which the density distribution was calculated through
215 the “dnorm” function in SLiM. Values for S were drawn from a continuous distribution
216 between -1.00 and 1.00 and transformed such that $S_\sigma = 10^{-S}$, yielding values between 0.1
217 and 10, with 0.1 representing the steepest fitness peak ($S = 1$) and 10 the shallowest ($S = -1$)
218 (Figure 1A). Phenotypes were calculated per individual, per region, as the additive
219 phenotypic effects of exonic non-synonymous mutations, which appeared at a rate of 7/3
220 relative to synonymous mutations (assuming that most mutations in the third base of a
221 codon do not alter the amino acid). Additive genetic variance was assessed due to its
222 prevalence in complex traits in nature (Hill *et al.* 2008). Effect sizes for mutations with
223 phenotypic effects were drawn from a Gaussian distribution with mean = 0 and $\sigma = 1$. The
224 remaining synonymous exon mutations, and mutations in introns and outside of genes, had
225 no effect on fitness.

226

227 For each simulation, populations were seeded with 1000 individuals and allowed to proceed
228 for a burn-in period of $5 \times 2N$ (10,000) generations to reach mutation-selection-migration
229 balance. During this period, burn-in populations evolved towards the ancestral phenotypic
230 optimum of 0, defined as a normal distribution with mean = 0 and $\sigma = 1.0$ (Figure 1A). Burn-
231 in populations were then subjected to each demographic treatment to simulate the
232 founding of multiple populations from a shared ancestral state. During this ‘divergence
233 period’, AP continued to evolve around the ancestral optimum of 0, whilst DP’s phenotypic
234 optimum was centred around 10, with fitness consequences defined according to S_σ .
235 Individuals also experienced fitness costs associated with phenotypic proximity to other

236 individuals within the population as a proxy for competition and to ensure a realistic
 237 amount of phenotypic variation persisted within populations. Fitness costs due to
 238 competitive proximity were scaled to a maximum value of 1 with $\sigma = 0.4$ and occurred
 239 reciprocally between local individuals with phenotypes with a difference of ≤ 1.2 ($3 * 0.4$).
 240
 241 Simulations were sampled at 100, 500, 1000, and then every 1000 generations up to 10,000
 242 (Figure 1C). F_{ST} was calculated across the 25kb region based on the proportion of
 243 subpopulation heterozygosity (H_S) relative to total heterozygosity (H_T) (according to Hudson,
 244 Slatkin and Maddison (1992)): $F_{ST} = 1 - \frac{H_S}{H_T}$. D_{XY} was calculated as the sum of nucleotide
 245 differences (d_{ij}) between the i^{th} haplotype from AP and the j^{th} haplotype from DP (according
 246 to Nei (1987)): $D_{XY} = \sum_{ij} AP_i DP_j d_{ij}$. Mean heterozygosity (π) for each population was
 247 calculated as a single measure across the 25kb region. At each sampling point, each
 248 measure was calculated and averaged across the preceding 20 generations. Averaging was
 249 performed such that measures would not be dramatically biased by events occurring within
 250 individual generations. The change in mean heterozygosity between AP and DP ($\Delta\pi$) was
 251 calculated as the ratio of π_{AP} to π_{DP} , such that reduced diversity in the DP population
 252 increases the value of $\Delta\pi$: $\Delta\pi = \log_{10} \frac{\pi_{AP}}{\pi_{DP}}$. Statistics were calculated over all monomorphic
 253 and polymorphic sites of 25kb regions. This has been designed to replicate genome scans
 254 that use window-approaches, with each 25kb region analogous to an independent window.
 255 In total, 100 unique 25kb regions were simulated across 16 demographic treatments across
 256 three mutation rates, with results for the intermediate mutation rate presented in the main
 257 text. To account for stochastic noise in the simulation, each 25kb region was iterated 20
 258 times for each demographic treatment. Simulations with divergent AP and DP phenotypes

259 are referred to as “Pheno_{Div}” simulations. Additional simulations were performed in which
260 both populations shared the ancestral phenotype (“Pheno_{Null}” simulations) and in which all
261 sites were neutral with no selection imposed (“Neutral” simulations). The former of these
262 was used to assess whether patterns associated with selection were driven by phenotypic
263 divergence or variable stabilising selection within populations, whilst the latter was used to
264 disentangle effects of selection and neutral processes such as drift. A common set of 100
265 25kb regions were used for all simulations. Outliers for simulations were taken as upper
266 95% quantiles.

267

268 All data analysis was performed in R (3.5) (R Core Team 2016). To assess relationships
269 between divergence measures and selection, data were grouped by sampling generation
270 within each treatment group (N = 16) and Pearson’s correlation coefficients were calculated
271 between measures of divergence and selection (S) at each sampling point for all regions (N =
272 100). Correlation coefficients were then grouped within specific treatment levels (e.g. DP
273 size = 0.5, or migration = 0.002) and averaged to give a coefficient reflecting each specific
274 treatment level. These correlation coefficients were calculated for each iteration (N = 20)
275 and averaged over to give final values.

276

277 To assess the effects of treatments on detecting outliers, we compared distributions and
278 95% cut-offs within each treatment for each measure of divergence for Pheno_{Div}, Pheno_{Null},
279 and Neutral simulations. We limited this analysis to early (100, 500), intermediate (3000)
280 and late (10,000) sampling generations. Here, data from all iterations of each 25kb region
281 were pooled. To calculate false positive (FPR) and false negative rates (FNR), we pooled
282 Neutral simulation data within treatment groups (20 iterations of 100 genes, N = 2000),

283 removed a random set of iterations ($N = 100$), and replaced it with an assortment of random
284 iterations of each gene (e.g. Gene 1/Iteration 2, Gene 2/Iteration 14... Gene 100/Iteration 4)
285 from Pheno_{Div} data. We calculated FPR as the proportion of data above the 95% quantile for
286 each measure of divergence/differentiation that came from neutral simulations. For single
287 measures, FPR = FNR as 5% of data in each permutation comes from Pheno_{Div}. We combined
288 outlier sets across all combinations of F_{ST} , D_{XY} and $\Delta\pi$ and examined neutral proportions
289 within outlier sets to determine FPR. FNR for combined outlier sets corresponded to the
290 proportion of Pheno_{Div} data not recovered in the combined outlier sets. These permutations
291 were performed 100 times with results averaged. Proportional overlap of outlier sets was
292 also calculated and compared across demographic treatment groups to examine
293 convergence of results across treatments. Overlap was calculated within each permutation,
294 averaged over, and visualised using heatmaps with hierarchical clustering of axes.

295

296 To examine how simulated gene features influenced patterns of genetic divergence, we
297 used a linear mixed modelling (LMM) approach with gene ID and treatment group as
298 random factors. Gene features modelled as independent factors were: number of exons
299 (Exon N), gene size, the proportion of gene that is coding (selection target %), selection
300 applied to each gene (S), and the generation at which the optimum phenotype was reached
301 (Pheno Gen).

302

303 **DATA AVAILABILITY**

304 A full set of scripts including all bash, Eidos and R scripts necessary to repeat this analysis
305 can be downloaded from Github
306 (https://github.com/JimWhiting91/Contingent_Convergence_Pipeline). Supplementary

307 figures (S1-49) have been uploaded through the GSA figshare portal. Supplementary figures
308 include results for different mutation/recombination rates, $\text{Pheno}_{\text{Null}}$ and neutral data
309 across sampling generations along with additional figures.

310

311 **RESULTS**

312 *Demography modifies measures of divergence*

313 Founding bottlenecks, simulated by reducing the number of possible founding genomes to a
314 random 10% of the ancestral population, had little measurable effect on F_{ST} , D_{XY} or $\Delta\pi$,
315 producing minimal variance between treatments over all sampling points (Figure 2A).

316

317 Prolonged bottlenecks, simulated by modifying the stable number of individuals within DP,
318 had pronounced and variable effects on all measures. F_{ST} increased with reductions in DP
319 size. This effect was generally consistent through time, although variance between
320 treatments increased gradually through time (Figure 2B). A similar effect was observed for
321 $\Delta\pi$; however, this measure was particularly susceptible to inflation under the most extreme
322 reductions in DP size, with substantially more elevated values observed between DP size
323 proportions of 0.01 and 0.1 compared with 0.1 and either 0.5 or 1.0. This pattern was
324 broadly consistent through sampling points. Such observations are unsurprising given that
325 both F_{ST} and $\Delta\pi$ increase with processes that reduce within-population genetic variance. D_{XY}
326 was generally robust to prolonged bottlenecks, but in contrast to F_{ST} and $\Delta\pi$, D_{XY} decreased
327 when DP sizes were reduced (Figure 2B).

328

329 The inclusion of migration reduced absolute values of all measures of divergence. For F_{ST}
330 and D_{XY} , variance between migration treatments increased across the simulation, however

331 D_{XY} was generally more consistent across migration treatments. $\Delta\pi$ was also reduced in the
332 presence of migration, although the effect of migration on $\Delta\pi$ was generally consistent
333 across all generations and did not increase through time, as was the case for F_{ST} and D_{XY} .
334
335 Whilst F_{ST} and D_{XY} increased generally over time, $\Delta\pi$ peaked around generation 500 and
336 declined thereafter. This peak corresponded to the median generation that DP replicates
337 reached their optimum phenotype (median across all data = 493), suggesting this peak
338 reflects selective sweeps. The majority of these patterns were apparent in the $Pheno_{Null}$
339 (Figure S1) and neutral (Figure S2) simulations, however divergence for all measures was
340 reduced and ultimately negligible by the removal of divergent phenotypes when migration
341 was present.

342

343 ***Demography moderates the association between measures of divergence and selection***

344 Again, founding bottlenecks had a minimal effect on the correlations observed between
345 strength of selection and measures of divergence with minimal variance observed between
346 bottleneck treatments in all comparisons (Figure 3A).

347

348 Prolonged bottlenecks had substantial effects on relative (F_{ST} and $\Delta\pi$) measures and
349 marginal effects on absolute (D_{XY}) measures of divergence (Figure 3B). F_{ST} correlations with
350 selection became consistently weaker as DP size reduced. There was minimal difference
351 between $\Delta\pi$ correlations with selection except for the most extreme reductions in DP size.
352 Effects for both were generally consistent through time. For D_{XY} , correlations with selection
353 were broadly consistent with minimal variance across DP size reductions (Figure 3B).

354

355 Expectedly, the absence of migration largely precluded the ability of measures of divergence
356 to predict strength of selection, with notable variance observed between no migration (0.0)
357 and minimal migration (0.002) treatments emerging rapidly for all divergence measures
358 (Figure 3C). Both F_{ST} and D_{XY} variance between migration treatments was greatest at the
359 10,000 generations sampling point, whereas similar variance was observed between
360 migration treatments for $\Delta\pi$ across simulations. This observation again highlights the
361 significance of temporal differences between measures. Interestingly, correlations between
362 $\Delta\pi$ and selection persisted, albeit weakly, in the absence of migration, which was not the
363 case for F_{ST} and D_{XY} . Further, at larger population scaling ($\mu = 4.89e^{-5}$, $r = 1e^{-5}$) D_{XY}
364 correlations with selection were negative (although became more positive over time with
365 migration) (Figure S6), most likely due to a stronger influence of mutational input. In larger
366 populations, positive correlations were observed between F_{ST} and selection without
367 migration, but were weaker than with migration (Figure S6).

368

369 Prolonged bottlenecks had a minimal effect on how measures of divergence correlated with
370 selection in $Pheno_{Null}$ data (Figure S5). Both F_{ST} and D_{XY} became negatively correlated with
371 selection over time without divergent selection, likely due to stronger selection on common
372 alleles shared between AP and DP. Negative correlations were stronger for D_{XY} , consistent
373 with reductions in DP_{π} with stronger selection. This suggests positive associations between
374 selection and D_{XY} in $Pheno_{Div}$ simulations are likely more dependent on adaptive
375 substitutions in order to overcome this effect. $\Delta\pi$ was generally positively associated with
376 selection in $Pheno_{Null}$ simulations regardless of migration, but was slightly reduced when
377 migration was absent.

378

379 By examining the correlation coefficients of all 16 unique demographic histories, we can
380 investigate the combined effect of migration and prolonged bottlenecks and directly
381 compare effectiveness of individual measures across time (Figure 4). F_{ST} consistently
382 outperforms D_{XY} in terms of associating with selection under most demographic treatments,
383 particularly when DP sizes are larger and migration is present. By 10,000 generations
384 however, the relative dominance of F_{ST} appears to subside, with the trend through time
385 suggesting a relative improvement in D_{XY} in treatments with migration (Figure 4). $\Delta\pi$ is
386 similarly more informative than D_{XY} across sampling generations under most demographic
387 treatments. Interestingly at sampling generation 10,000, reductions in prolonged
388 bottlenecks produce the biggest bias towards $\Delta\pi$ (Figure 4). The resilience of $\Delta\pi$ under no-
389 migration treatments is also apparent in F_{ST} - $\Delta\pi$ comparisons, such that at 3,000
390 generations $\Delta\pi$ is more informative than F_{ST} in the absence of migration. Consistent with its
391 rapid response to sweeps around 500 generation, $\Delta\pi$ slightly outperforms F_{ST} under most
392 demographic scenarios in early generations. By 10,000 generations, however, F_{ST} performs
393 as well as $\Delta\pi$ without migration and outperforms $\Delta\pi$ with migration.

394

395 ***Demography moderates the shape and tail end of divergence distributions***

396 By comparing distributions across simulations with divergent ($Pheno_{Div}$) and stabilising
397 ($Pheno_{Null}$) selection with neutral runs, we can examine the effect of demographic
398 treatments on the ability of each measure of divergence to discriminate between them
399 (Figure S11-13; Figure 5). There are few differences between distributions of F_{ST} for the
400 three simulation types when migration is absent between AP and DP replicates, highlighting
401 an increased likelihood of false-positives. The exceptions occur in early sampling points at
402 100 and 500 generations (Figure S12) when sweeps are most common. With migration,

403 $F_{ST}^{Pheno_{Null}}$ is marginally elevated compared with neutral F_{ST} , but distributions are broadly
404 similar. $F_{ST}^{Pheno_{Div}}$ distributions however become more positive and flattened, according to
405 variable selection, with the majority of $F_{ST}^{Pheno_{Div}}$ above the 95% quantiles of $F_{ST}^{Pheno_{Div}}$ and
406 neutral F_{ST} by 10,000 generations (Figure 5).

407

408 Similar patterns were observed for D_{XY} distributions (Figure S14-17), with little to
409 discriminate between in treatments without migration. However, without migration, neutral
410 D_{XY} was generally reduced relative to $F_{ST}^{Pheno_{Null}}$ and $F_{ST}^{Pheno_{Div}}$ at earlier sampling points.
411 With migration, like F_{ST} , $D_{XY}^{Pheno_{Div}}$ was readily distinguishable from $F_{ST}^{Pheno_{Null}}$ and neutral
412 distributions, but $F_{ST}^{Pheno_{Null}}$ D_{XY} was also generally more positive than neutral D_{XY} . These
413 patterns also emerged more slowly than for F_{ST} . In contrast, $\Delta\pi^{Pheno_{Div}}$ (Figure S18-21) was
414 elevated according to DP size, such that at 500 generations the majority of 25kb regions
415 under divergent selection exhibited $\Delta\pi$ above neutral and $F_{ST}^{Pheno_{Null}}$ 95% cut-offs for all
416 treatments with DP size ≥ 0.5 .

417

418 We quantified false-positive rates (FPR) by permuting over merged data comprised of
419 randomly sampled 5% $F_{ST}^{Pheno_{Div}}$ regions and 95% neutral regions and observing the upper
420 5% quantile (Table S1). By 100 generations, F_{ST} FPR ranged between 0.06 and 0.91, and was
421 lower with increased DP size and lower in treatments without migration (Table S1). By 500
422 generations (Table 2), FPR rates were lower with migration and higher without, but only for
423 treatments with DP sizes of 0.5 and 1.0. F_{ST} FPR remained high (> 0.81) for all treatments
424 with smaller DP sizes. By 3,000 generations, migration was the most important demographic
425 factor for F_{ST} FPR. With migration, FPR ranged from 0.15 – 0.61, and decreased with
426 increasing DP size. Without migration, FPR were high (0.88 - 0.97), close to the random

427 proportion of neutral (0.95) data. By the end of simulations, F_{ST} FPR was as low as 0.13, and
428 was no greater than 0.27 with migration and DP size ≥ 0.1 . Without migration, FPR was >
429 0.94.

430

431 Initial D_{XY} FPR were generally high irrespective of demographic treatment, ranging between
432 0.78 and 0.93. FPR were largely similar after 500 generations, but by 3,000 generations
433 there was a distinction between treatments with ($0.07 \leq FPR \leq 0.71$) and without ($0.85 \leq$
434 $FPR \leq 0.88$) migration. Interestingly, here FPR rates were lower ($0.07 \leq FPR \leq 0.24$) when DP
435 were smaller (size = 0.01, 0.1) rather than larger ($0.47 \leq FPR \leq 0.71$). This pattern was also
436 observed at the end of simulations, with FPR lower without migration ($0.01 \leq FPR \leq 0.34$)
437 and lowest with DP size = 0.1.

438

439 $\Delta\pi$ FPR rates were generally higher across all sampling generations, with FPR not falling
440 below 0.28. There was a clear distinction based on DP size in earlier (100 and 500) sampling
441 points, with FPR lower with larger DP size. However, at later sampling generations (3,000
442 and 10,000), FPR were generally high (≥ 0.68) regardless of treatment.

443

444 Taken together, there are clear effects of DP size and migration on distributions of genetic
445 variation and upper quantiles of interest. DP size appears initially most important in the first
446 few hundred generations for F_{ST} and $\Delta\pi$, but these effects are later swamped by the effect
447 of migration for F_{ST} and are simply eroded for $\Delta\pi$. D_{XY} exhibits similar patterns to F_{ST} , but
448 these develop after many more generations, and whilst gene flow increases the
449 informativeness of D_{XY} for detecting divergent selection, as it does for F_{ST} , D_{XY} and F_{ST}
450 experience opposing effects of increases to DP size.

451

452 ***Demography moderates relationships between measures of divergence***

453 Given F_{ST} , D_{XY} and $\Delta\pi$ are all measures of population genetic divergence, there is an
454 assumption that positive correlations should exist between them. We employed the same
455 analysis as above for correlations with selection, but instead examined correlations between
456 individual measures. Founding bottlenecks had minimal effects on the correlations observed
457 between all measures of divergence (Figure 6A).

458

459 Positive correlations between F_{ST} and D_{XY} emerged rapidly irrespective of DP size, but
460 smaller DP sizes generally increased the correlation (Figure 6B), with variance between
461 treatments generally decreasing over time. Similarly, F_{ST} and $\Delta\pi$ were generally positively
462 correlated, however reductions in DP size reduced correlation coefficients. By 4,000
463 generations, F_{ST} - $\Delta\pi$ correlations for DP sizes ≥ 0.1 stabilised around 0.4, but correlations
464 under extreme prolonged bottlenecks continued to decline to a low of 0.19 (Figure 6B). D_{XY} -
465 $\Delta\pi$ correlations were generally weaker than other comparisons across the course of
466 simulations, but were minimally affected by prolonged bottlenecks.

467

468 Migration induced substantial variance between correlations of divergence measures, with
469 effects dependent on sampling point (Figure 6C). In the absence of migration, F_{ST} and D_{XY}
470 were more strongly correlated for the first 4,000 generations than in treatments with
471 migration. However, from here until 10,000 generations this pattern reversed and F_{ST} - D_{XY}
472 correlations increased with migration and deteriorated in allopatry. F_{ST} - $\Delta\pi$ correlations
473 were strong initially, but a lack of migration weakened the correlation over time until

474 measures were uncorrelated by around 4,000 generations. In contrast, in the presence of
475 migration, positive correlations between F_{ST} and $\Delta\pi$ were strong and relatively stable ($R^2 =$
476 $0.75 - 0.61$ over the whole simulation period). Interestingly, without migration, D_{XY} and $\Delta\pi$
477 were largely uncorrelated, but migration induced a positive correlation between D_{XY} and $\Delta\pi$
478 that emerged after 2,000 generations and continued to increase through time.

479

480 Contextualised by our previous demonstrations of associations with selection, these results
481 highlight that selection can induce positive correlations between measures. By 10,000
482 generations, all pairwise comparisons of divergence measures become positively correlated
483 with migration, which we know is when variation is most strongly associated with selection.
484 Crucially however, this relationship only emerges after several thousand generations, before
485 which we observe positive correlations in migration-absent treatments when associations
486 with selection are weak for all measures ($F_{ST} - D_{XY}$ in particular). Extreme reductions in DP
487 size also increase positive correlations between F_{ST} and D_{XY} despite poor associations with
488 selection in these treatments. These results highlight that positive correlations between
489 statistics are also achievable in the absence of divergent selection. It is also interesting to
490 note the decay of correlations with $\Delta\pi$ and both F_{ST} and D_{XY} in the absence of migration.
491 These observations are most likely driven by the substitution rate. Substitutions that are not
492 linked to selection (drift with ineffective selection) likely drive increased F_{ST} and D_{XY} but not
493 $\Delta\pi$.

494

495 In $\text{Pheno}_{\text{Null}}$ simulations, F_{ST} and D_{XY} were positively correlated in all treatments, but stronger
496 associations linked with demographic treatments with effective selection did not emerge

497 (Figure S22). This was also true for neutral simulations (Figure S23), but $F_{ST} - D_{XY}$ correlations
498 were slightly larger than for $Pheno_{Div}$ and $Pheno_{Null}$ when selection was ineffective, reaching
499 a maximum of $R^2 = 0.81$ without migration (Figure S23C). This demonstrates that the
500 positive correlations in $Pheno_{Div}$ simulations are driven in part by divergently adaptive allele
501 frequency shifts and substitutions when selection is effective, but these correlations can
502 also emerge under stabilising selection or neutrality. Specifically, strong positive correlations
503 with $\Delta\pi$ were dependent on divergent selection, and $F_{ST} - \Delta\pi$ correlations became negative
504 over time in treatments without migration under neutrality. $D_{XY} - \Delta\pi$ correlations became
505 negative in $Pheno_{Null}$ data with migration and were unassociated without. Thus, these
506 results highlight that the relationships between measures of divergence are highly
507 dependent on migration, population size, time, and selection experienced over a genomic
508 region.

509

510 We then examined FPR and false negative rates (FNR) when combining outliers across F_{ST} ,
511 D_{XY} and $\Delta\pi$ (Table S1; summaries from 500 and 10,000 generations in Table 2). Combined F_{ST}
512 - D_{XY} outliers exhibited FPR rates that were highly variable (0.00 - 0.95) and similar to or
513 slightly lower than F_{ST} alone at generations 100 and 500, suggesting some improvement in
514 reducing FPR. During this period, FNRs were also high (≥ 0.78), suggesting most regions with
515 divergent selection could not be detected on a neutral backdrop. Combined $F_{ST} - D_{XY}$ outlier
516 sets performed well at generations 3,000 and 10,000 for treatments with migration, in some
517 cases dropping to 0 although FNR were highly variable ($0.26 \leq FNR \leq 1.00$). High FPR ($0.84 \leq$
518 $FPR \leq 0.99$) and high FNR ($0.93 \leq FNR \leq 1.00$) were observed without migration,
519 highlighting most common outliers between F_{ST} and D_{XY} to be neutral, and a failure to detect
520 almost all divergent regions.

521

522 Combined $F_{ST} - \Delta\pi$ outliers tended to outperform F_{ST} and $\Delta\pi$ outliers according to FPR with
523 DP sizes of 0.5 or 1.0 and in earlier (100 and 500) sampling generations. Here, FPR dropped
524 to a low of 0 but FNR were reasonable through this time (≥ 0.35). Beyond this (sampling
525 generations 3,000 and 10,000), FPR again dropped to 0, however these were generally
526 alongside high FNR of up to 1.0 without migration, highlighting a failure to detect any
527 common outliers at all. A good example of improvement over singular measures was
528 observed at generation 500, with a founding bottleneck, equal sized populations, and
529 migration. Here, an average of ~66% of divergent regions were detected with an average
530 FPR of 0. This is compared with: singular F_{ST} , where $FPR/FNR = 0.18$; and singular $\Delta\pi$ where
531 $FPR/FNR = 0.29$. By 10,000 generations, combined outlier sets of $F_{ST} - \Delta\pi$ performed poorer
532 than singular F_{ST} with migration present, but generally returned low numbers of false
533 positives when migration was absent, unlike $F_{ST} - D_{XY}$.

534

535 Combined $D_{XY} - \Delta\pi$ outliers performed poorly across all treatments and all sampling
536 generations, with FNR failing to fall below 0.71. There were, however, some benefits in
537 terms of low FPR for treatments with larger DP sizes (0.5 and 1.0) across all sampling points,
538 suggesting high confidence in outliers (although most divergent regions are missed). This
539 discordance between D_{XY} and $\Delta\pi$ and large FNR also limited the combined usage of all three
540 measures together, with similarly high FNR largely precluding their combined usage. All
541 three statistics did exhibit low FPR with larger DP populations at 100, and 500 generations
542 despite migration. However, at later sampling generations performance of all three
543 combined outlier sets was poor (high FPR/FNR) if migration was absent.

544

545 These results therefore highlight that combining measures can help reduce FPR, but usually
546 at the cost of increased FNR (expectedly), and only under certain demographics. Our
547 observation that high FPR are prevalent among combined outlier sets from statistics,
548 particularly in the absence of migration, suggests their usage must be dependent on a
549 knowledge of disparity in population size and connectivity of populations. These findings
550 also highlight that the strong correlations that emerge between measures of divergence
551 under scenarios with ineffective selection or even under neutrality do extend to the tail-
552 ends of distributions.

553

554 ***Demography drives signals of convergence irrespective of selection***

555 Clusters of overlapping outliers developed steadily over time (Figure S26-28). By sampling
556 generation 10,000, significant proportions of overlapping outliers were recovered across
557 different demographic treatment groups (Figure 7). For F_{ST} and D_{XY} , clustering of treatments
558 was driven by the presence/absence of migration, with the highest proportions of
559 convergent outliers observed between treatments with migration.

560

561 Interestingly, for D_{XY} reasonable proportions of convergent outliers were also recovered
562 across no migration treatments, and the same was true of F_{ST} by 3,000 generations (Figure
563 S28), and for both measures at 10,000 generations in 'smaller' populations with reduced
564 scaling ($\mu = 4.89e^{-7}$, $r = 1e^{-7}$; Figure S37). This is despite these treatment groups lacking
565 effective selection. Importantly, there was little overlap between migration and no-
566 migration clusters, suggesting different convergent outliers within each. Combining outliers
567 from F_{ST} and D_{XY} reduced overlap among no-migration treatments, but did not remove
568 overlapping outliers altogether.

569

570 There were minimal convergent outliers observed for $\Delta\pi$ outliers, however combining $\Delta\pi$
571 with F_{ST} and D_{XY} did appear somewhat effective in removing convergent outliers found
572 between no-migration treatments. However, for both combination of $\Delta\pi$ with F_{ST} and D_{XY} ,
573 the highest proportional overlap was observed for treatments with the smallest DP size.

574

575 Interestingly, the clustering of $F_{ST} - D_{XY}$ outliers in the presence of migration was greatly
576 reduced when divergent selection was removed in both $Pheno_{Null}$ (Figure S29-32) and
577 neutral data (Figure S33-36), but clusters of outliers in the absence of migration were still
578 apparent.

579

580 Because migration was the dominant factor in clustering of treatments with convergent
581 outlier overlap, we sought to investigate what features of simulated genes drove variance in
582 measures of divergence with treatments separated by migration factor using linear mixed
583 models at the final sampling generation. With migration between AP and DP, selection had
584 by far the strongest effect on F_{ST} (Table 3) in the expected positive direction. We also
585 observed a weaker positive association with selection target (% coding) of gene (Table 3),
586 and weaker negative associations with Pheno Gen (generation DP optimum reached) (Table
587 3). These fixed effects explained 48.96% of variance in F_{ST} with migration.

588

589 Conversely, fixed effects explained minimal variance (1.10%) of F_{ST} in treatments without
590 migration. These fixed effects were significant, but had weak positive associations with
591 selection, exon N and selection target %, and a weak negative association with Pheno Gen.

592

593 D_{XY} was similarly most strongly positively associated with selection in treatments with
594 migration (Table 3), but the strength of this effect relative to the other model effects was
595 not as large as observed for F_{ST} . D_{XY} was also negatively associated with Pheno Gen (Table
596 3), as was F_{ST} , but negatively associated with Exon N (Table 3). This model however
597 explained less variance of D_{XY} with migration (9.53%) than F_{ST} with migration. In treatments
598 without migration, selection target % was strongly negatively associated with D_{XY} (Table 3),
599 and this fixed effect explained 30.70% of D_{XY} variance without migration.

600

601 Selection was the most important fixed effect for $\Delta\pi$ regardless of migration (Table 3),
602 however both models explained minimal variance (8.27% with migration, 0.59% without
603 migration). This is consistent with the previous demonstration of the erosion of $\Delta\pi$ over
604 time (Figure 1).

605

606 Removing divergent selection (i.e. in Pheno_{Null} simulations) modified models for F_{ST} and D_{XY}
607 for treatments with migration. Selection and selection target remained the most important
608 model effects, but had more similar sized effects, and ultimately variance explained
609 dropped from 48.96% to 3.60%. Conversely, the model for Pheno_{Null} D_{XY} with migration
610 increased variance explained from 9.53% to 13.10% compared with Pheno_{Div} D_{XY} . Selection
611 target had a strongly significant negative association alongside strength of selection in this
612 model. $\Delta\pi$ models were largely unchanged. Together, these results confirm that divergent
613 selection, and not stabilising selection within DP, drive F_{ST} and D_{XY} variation in Pheno_{Div}
614 simulations.

615

616 **DISCUSSION**

617 **Summary of results**

618 Here, we show that features of demography can have dramatic effects on how measures of
619 population divergence identify regions of the genome under selection. Effects are also
620 strongly time-dependent. Using simulated populations, we have demonstrated the relative
621 influences of founding bottlenecks, prolonged bottlenecks, and migration on three
622 commonly used measures of genetic divergence (F_{ST} , D_{XY} , $\Delta\pi$), whilst demonstrating the
623 relative usefulness of each measure for informing on selection when population sizes and
624 connectivity vary.

625

626 We find that founding bottlenecks have little effect on population divergence measures,
627 potentially either because populations quickly recover (before first sampling after 100
628 generations), or founding bottlenecks of 10% (100 individuals) were not extreme enough.
629 Prolonged bottlenecks (reductions in DP size) however, artificially inflate F_{ST} and $\Delta\pi$ but
630 reduce D_{XY} , and can erase the relationship of F_{ST} and D_{XY} with selection under the most
631 extreme reductions in population size. Relative measures are, in part, driven by intra-
632 population changes in allele frequency, which become exaggerated in smaller populations
633 as a product of drift (Charlesworth 2009; Ellegren and Galtier 2016). As a consequence, we
634 observe inflated measures of relative divergence as allele frequencies drift in smaller DP
635 replicates.

636

637 In contrast, D_{XY} increases with larger DP size, as a product of the relationship between the
638 number of segregating sites and the population-level mutation rate ($4N_e\mu$) (Hartl *et al.*
639 1997). D_{XY} is a measure of sequence divergence and is averaged across all sites (although
640 similar statistics limit averaging to segregating sites only), which results in higher D_{XY} as

641 segregating sites are introduced into either population at a rate of $4N_e\mu$. This relationship
642 with the number of segregating sites can be observed by examining the positive
643 relationships between D_{XY} and DP_π (Figure S38). Overall, the relationship between D_{XY} and
644 selection is less affected by prolonged bottlenecks than F_{ST} and $\Delta\pi$, likely due to the lack of
645 allele frequency relevance. Consider for example, two SNPs with minor allele frequencies of
646 0/0.5 (SNP 1) and 0.5/0.5 (SNP 2) in AP/DP. Each locus contributes equally towards D_{xy} (SNP
647 1 = $[0 \times 0.5] + [1 \times 0.5] = 0.5$; SNP 2 = $[0.5 \times 0.5] + [0.5 \times 0.5] = 0.5$), whereas the reduction of
648 within-population variance observed for SNP 1 inflates F_{ST} and $\Delta\pi$. However, we also see
649 evidence of D_{XY} FPR increasing with increased DP size (Table 2), suggesting this relationship
650 with increased acquisition of segregating sites may conflict with increased efficacy of
651 selection.

652

653 Migration, even at the relatively modest rate of 0.2% employed here, substantially reduced
654 absolute values for all measures of divergence. However, whilst absolute values were
655 reduced, their informativeness of selection coefficients increased dramatically (both in
656 terms of their overall relationship with selection and in identifying outliers). Such a result is
657 expected given the role of gene flow in homogenising neutral loci (reducing measures of
658 divergence), whilst retaining population divergence around adaptive loci (increasing
659 informativeness). The well-known 'genomic islands of divergence' model is often invoked to
660 explain this pattern of heterogenous genomic divergence in studies of speciation-with-gene-
661 flow (Turner *et al.* 2005; Nosil *et al.* 2009).

662

663 Migration also exhibited interesting temporal patterns that are useful for discussing the
664 discrepancies observed between $\Delta\pi$ and both F_{ST} and D_{XY} . Of the measures considered here,

665 $\Delta\pi$ uniquely disregards SNP substitutions in its calculation, as fixed substitutions have no
666 influence on intra-population heterozygosity beyond reducing the heterozygosity of
667 proximate SNPs in the aftermath of a hard sweep. This characteristic explains why $\Delta\pi$
668 responds to selection more rapidly than F_{ST} and D_{xy} and is influenced by migration in a
669 constant manner across time. In addition, the inability of $\Delta\pi$ to account for adaptive
670 substitutions is likely why the informativeness of $\Delta\pi$ peaked at around 500 generations
671 (approximate median for sweeps), decayed, and then stabilised. In contrast, the
672 contributions of adaptive substitutions to F_{ST} and D_{xy} over time increases their predictive
673 power. This characteristic of $\Delta\pi$, however, also makes it unable to differentiate between
674 divergent and stabilising selection. This temporal observation has important implications for
675 studies of rapid adaptation on the scale of 10s to 100s of generations, in which our
676 simulations suggest $\Delta\pi$ may be the most informative measure of divergence, whilst D_{xy} is
677 initially uninformative for several thousand generations.

678

679 Examining the effects of bottlenecks and migration on the associations between measures
680 of divergence themselves is a novel element to this study. The relative weaknesses of
681 individual measures of divergences has prompted a recent movement within the literature
682 to employ multiple measures of divergence to avoid false-positives (for e.g. Tine et al. 2014;
683 Malinsky et al. 2015; Hämälä and Savolainen 2019). Our results provide some support for
684 this strategy, with reductions in FPR in treatments with gene flow generally, and low FPR
685 when combining either F_{ST} or D_{xy} with $\Delta\pi$ (albeit at a reasonably high FNR). However, we
686 also find large numbers of overlapping outliers across combined $F_{ST} - D_{xy}$ with a large FPR
687 across treatments without migration. Further, these false-positives persisted in $Pheno_{Null}$
688 and neutral data, whereas clusters of treatments with overlapping outliers (Figure 7) and

689 with low FPR were restricted to simulations with divergent phenotypes. It is clear then that
690 combining outlier sets of F_{ST} and D_{XY} only improves analyses under certain demographic
691 histories, in particular when populations are connected by migration.

692

693 Cruickshank and Hahn (2014) suggested that a disagreement between F_{ST} and D_{XY} outliers in
694 genomic-islands-of-divergence tests highlights a particular susceptibility of F_{ST} to BGS
695 (although see (Matthey-Doret and Whitlock 2019)). Our results are in line with the notion
696 that D_{XY} may be more resistant to false positives due to BGS, given that reductions in DP size
697 resulted in minimal variance in D_{XY} (assuming reductions in population size are analogous to
698 different rates of BGS across the genome exhibit reduced N_e). However, BGS was not
699 specifically manipulated in these simulations, and results are difficult to disentangle with
700 variation in efficacy of removing deleterious mutations. Further, this minimal variance may
701 be explained by the opposing forces of selection efficacy and acquisition of segregating sites
702 discussed previously. We also found that a greater proportion of variance could be
703 explained by the size of selection target for D_{XY} (30.7%) in the absence of migration than for
704 F_{ST} (1.1%). We found that F_{ST} and D_{XY} are positively correlated under several demographic
705 scenarios, but this strong association only reflects selection when gene flow is present and
706 only after several thousand generations, consistent with previous simulation work (Ravinet
707 *et al.* 2017). When migration is absent, and selection ineffective, F_{ST} and D_{XY} are also
708 positively correlated; but this relationship decays over time (Figure 6C), with empirical
709 evidence (see below) suggesting a negative relationship is likely to emerge without gene
710 flow. No-migration treatments are consistent with Isolation-By-Distance demographic
711 histories and, similarly, comparisons between reproductively-isolated populations or
712 species. Indeed, negative correlations between F_{ST} and D_{XY} within and between clades of

713 birds (Irwin *et al.* 2016; Vijay *et al.* 2017), within a radiation event of monkeyflowers
714 (Stankowski *et al.* 2019) and between speciating orca populations (Foote *et al.* 2016)
715 support a declining relationship between these measures over long periods of time in
716 isolation. In agreement, we find that without migration F_{ST} and D_{XY} exhibit opposite
717 associations with the proportion of regions made up of coding elements. Mechanistically, a
718 larger selection target increases the rate of deleterious mutation, reducing local π directly
719 through loss of polymorphic deleterious sites, or indirectly through the loss of linked neutral
720 variants under a BGS model. Reductions in local π increase F_{ST} and decrease D_{XY} . Over time,
721 associations between F_{ST} and D_{XY} should stabilise, given π is generally well-conserved in
722 stable populations even across long time periods (Romiguier *et al.* 2014; Dutoit *et al.* 2017;
723 Van Doren *et al.* 2017).

724

725 By comparing our results to a second dataset that lacked divergent selection (Pheno_{Null}), we
726 found consistent support that positive associations between D_{XY} and selection are strongly
727 dependent on the inclusion of a divergent phenotype. Positive associations with F_{ST} are
728 attainable only in the absence of migration, and are weakly negative without, and $\Delta\pi$
729 patterns are primarily driven by variable stabilising selection and made weaker by the
730 inclusion of phenotypic divergence. These comparisons are useful in highlighting the relative
731 roles of adaptive allele frequency changes and substitutions in driving patterns of genetic
732 differentiation. It is also of interest to note that overlapping outliers are readily attainable
733 (most strongly for D_{XY}) across no-migration treatments in Pheno_{Null} (Figure S32) and neutral
734 simulations (Figure S36), but not for treatments with migration. This confirms that
735 overlapping outliers in no-migration treatments occur due to common non-divergent
736 processes within genomic regions, whereas overlapping outliers in treatments with

737 migration are driven by the effects of divergent selection. The discrepancies between our
738 $\text{Pheno}_{\text{Div}}$ and other simulated datasets highlight the necessity in quantifying phenotypic
739 differences or environmental selection pressure when interpreting patterns of variation
740 across the genome.

741

742 ***Detecting genetic convergence***

743 In addition to understanding how outlier detection in individual pairs were affected by
744 bottlenecks and migration, we wanted to explore how studies looking at overlapping
745 outliers in multiple pairs (i.e. detecting genetic convergence) were affected by these aspects
746 of demography. Our simulation design, in which an ancestral burn-in population is used to
747 found 16 independent AP-DP pairs is analogous to replicated ecotype population pairs in
748 model systems, such as various ecotype pairs of the three-spined stickleback, *Gasterosteus*
749 *aculeatus* (Hohenlohe *et al.* 2010; Jones *et al.* 2012a); high/low predation Trinidadian
750 guppies, *Poecilia reticulata* (Fraser *et al.* 2015); crab/wave ecotype periwinkles, *Littorina*
751 *saxitilis* (Westram *et al.* 2014; Ravinet *et al.* 2016; Kess *et al.* 2018), and alpine/montane
752 ecotypes of *Heliosperma pusillum* (Trucchi *et al.* 2017). We found overlapping outliers
753 between demographic treatments and thus, that signals of convergent outliers are
754 attainable for singularly used F_{ST} and D_{XY} , and combined outlier sets for $F_{\text{ST}} - \Delta\pi$, $D_{\text{XY}} - \Delta\pi$
755 and $F_{\text{ST}} - D_{\text{XY}}$. Clustering of outliers was predominantly driven by the presence or absence of
756 migration (with minimal overlap between clusters) (Figure 7).

757

758 The overlap of quantile-based outliers between demographic treatments without migration
759 and ineffective selection may be explained in part probabilistically. With migration
760 restricted, AP and DP exhibit significantly elevated measures of divergence, as seen in Figure

761 1. This increase results in a normal distribution of F_{ST} and D_{XY} across neutral simulations
762 without migration. In contrast, with migration, drift is limited and random recombination
763 influences gene flow and subsequently variation in divergence. Distributions of divergence
764 with migration under neutrality are therefore are heavily right tail-skewed (Figure S39).
765 Spread of data increases with longer right tails, and density of data in each overlapping
766 distribution is limited to the median and lower quantiles.

767

768 We also expect some effect of different amounts of starting variation among genome
769 regions following burn-ins. With gene flow restricted, this variation may promote overlap
770 under neutral conditions given all demographic treatments are founded from a common
771 burn-in. However, this feature of our simulations is analogous to the conserved landscapes
772 of variation observed in natural genomes (Burri 2017; Vijay *et al.* 2017; Stankowski *et al.*
773 2019).

774

775 Empirically, the influence of migration on outlier overlap has been observed in replicate
776 pairs of parasitic and non-parasitic lampreys. As we show here, when comparing outliers
777 from disconnected and connected parasitic/non-parasitic pairs, Rougemont *et al.* (2017)
778 recover greater numbers of overlapping outliers among comparisons of disconnected pairs
779 than connected pairs. Overlapping outliers among connected pairs are however better
780 correlated, which the authors suggest reflects selection.

781

782 ***Limitations of simulations***

783 In our analyses, we grouped genomic regions within 16 unique demographic treatments,
784 assuming the effects of reductions in population size and migration are equivalent for all

785 regions. This may be unrepresentative of genomes sampled from the wild, in which gene
786 flow and effective population size can vary across genomic regions through structural
787 variation, variable recombination rate and BGS (Gossmann *et al.* 2011). A prominent
788 example of such a mechanism is the well-characterised consequence of reduced gene flow
789 within inversions that carry locally adapted alleles. Assuming inversion variants are fixed
790 between populations, gene flow across the locus is limited by the prevention of
791 recombinant haplotypes and resistance to introgression (Kirkpatrick and Barton 2006;
792 Ravinet *et al.* 2017). Recent genome scan studies have highlighted convergent outliers
793 within inversions (Jones *et al.* 2012b; Nishikawa *et al.* 2015; Morales *et al.* 2019), confirming
794 theoretical models regarding their role in shielding adaptive haplotypes from introgression
795 during the adaptation process. Our simulations suggest that genes with reduced migration,
796 and reduced N_e as a consequence, will have inflated measures of divergence and
797 differentiation relative to other genomic regions. Therefore, we predict this may have led to
798 their over-representation in genome scan outliers, and increased potential to overlap across
799 replicate populations. Thus, caution should be taken regarding the adaptive significance of
800 these outliers relative to absolutely lower values of genetic divergence attained from
801 regions outside of chromosomal rearrangements.

802

803 By choosing to use a factorial design here, we have increased our understanding of the
804 interplay between specific features of demographic history and multiple measures of
805 population divergence. However, computational limitations constrained absolute
806 population sizes to a maximum of 1,000 individuals and generations to a maximum of
807 10,000 (with 10,000 generation burn-in). To mitigate these constraints, we repeated the
808 analysis over multiple mutation rates (and scaled recombination rate) to illustrate patterns

809 over 100-fold variation of θ . In general, most trends were consistent, suggesting that results
810 should be consistent across taxa of variable effective population size. However, certain
811 patterns were exaggerated or dampened with increased or decreased mutation rate
812 respectively. For instance, the overlap of outliers between no-migration treatments was
813 exaggerated at our smallest level of population scaling (Figure S37), suggesting false-positive
814 signals of convergence may be more likely with reduced N_e . Further, patterns associated
815 with D_{XY} and selection vary according to population size, appearing delayed in smaller
816 populations (Figure S7) and swamped by mutational input in larger populations (Figure S6).
817 This latter effect can induce negative associations between selection and D_{XY} with effective
818 selection, as selection reduces local genetic variation that would otherwise increase D_{XY} . It is
819 well-documented that both N_e (Frankham 1995) and mutation rate (μ) (Hodgkinson and
820 Eyre-Walker 2011) are highly variable across taxa, which suggests that applying knowledge
821 of the relationships between measures of population differentiation will vary in nature.

822

823 In addition, temporal variation within our simulations is confounded by the time at which
824 there was a major shift in the DP population phenotype (Figure S40), and by extension when
825 selective sweeps occur. This variation in timing is random with respect to adaptive
826 mutations arising *de novo*, but is also influenced by demographic treatment. For example,
827 treatments that experience founding bottlenecks are less likely to evolve using variation in
828 the founder, increasing dependence on *de novo* mutations for adaptation. Additionally,
829 variation in our DP size parameter modifies the per population number of new mutations
830 per generation. This is also true for features of simulated genes, such as size of selection
831 target. Predictable temporal variation in the time at which adaptation is likely to occur is a

832 probable source of variance between measures of divergence and is particularly clear for
833 $\Delta\pi$, but this was controlled for in later modelling analyses as a fixed effect.
834
835 A further consideration for these simulations concerns the architecture of the phenotype.
836 Results reported here pertain to mutation effect sizes drawn from a distribution centred at
837 0 with $\sigma = 1$. This produces mutations of typically large effect, but was selected on the basis
838 of phenotypic optima being reasonably distant, with a difference of 10. Thus, 99% of
839 mutations in simulations produce phenotypic differences of less than a third the divergence
840 distance of AP and DP phenotypes. There are numerous factors that influence the
841 distribution of mutation effect sizes in nature, including: selection, mutation, drift, gene
842 flow, extent of pleiotropy and distance to phenotypic optima (Dittmar *et al.* 2016), with no
843 single expectation for natural systems as a result. The relatively large distance between
844 optima in our simulations, as well as the rapid change in optima implemented in simulations
845 (Collins and De Meaux 2009), likely gives increased importance to mutations of large effect.
846 The interactions between mutation effect size and the results presented here are beyond
847 the scope of the current study, but we did investigate the effect of reducing μ_e of mutation
848 effect distributions to 0.1 (Supporting Information; Figures S40-45). Briefly, we see
849 reductions in the strength of correlations and associations with selection with decreasing
850 phenotypic effects of mutation, consistent with the notion of softer sweeps on small-effect
851 loci. We also see increased variance in the amount of time taken for simulations to reach
852 the $\text{Pheno}_{\text{Div}}$ optimum, which agrees with the probable importance of large effect loci in our
853 standard dataset. We, however, retain strong positive associations between measures such
854 as F_{ST} and D_{XY} , as we see in neutral simulations, as well as overlapping outliers linked to
855 selection at the tail ends of $\text{Pheno}_{\text{Div}}$ distributions. Running the simulations in this way

856 suggests that many of the patterns described here may be robust to scenarios with reduced
857 mutation effect sizes.

858

859 It is also important when translating these results to genomic data to consider how
860 correlations between measures of divergence depend on the selection type used in
861 simulations. For example, F_{ST} and D_{XY} are strongly positively correlated under neutrality
862 without migration, but under the same demographic scenarios we observe a decay in the
863 relationship between F_{ST} and D_{XY} when divergent selection is involved. Genomes of natural
864 populations will include regions that are neutral or nearly neutral, under stabilising selection
865 around a common phenotypic optimum, or divergent between populations. Thus, the
866 patterns described here may not apply to all genomic regions pooled together.

867

868 ***Concluding remarks***

869 We have used forward-in-time simulations to perform a factorial experiment in which we
870 explored the relationships between three measures of genetic divergence, selection, and
871 features of demographic history that are commonly variable in natural populations. In
872 agreement with previous theoretical work, we found the reliance of measures of genetic
873 divergence to identify loci under selection are dependent on population size and migration,
874 and variable through time, with a notable lag in D_{XY} . Furthermore, we provided novel
875 comparisons between measures of genetic divergence that call into question the use of
876 multiple measures to rule out false-positives. We also demonstrated that signals of
877 convergent evolution across independent replicates can be driven by similar features of
878 demographic history with minimal influences of selection, specifically, across replicate
879 populations pairs that lack migration. Therefore, we strongly advise those using overlapping

880 outlier scans to carefully consider the demographic context of their system to avoid false-
881 positives. In particular, the presence or absence of migration between diverging populations
882 is a key factor determining the informativeness of genetic variation for selection, and
883 importantly shapes our expectations of outlier overlap among replicate population pairs. It
884 is tempting to assume that replication in study design or analysis in the form of taking
885 multiple measures of genetic divergence can reduce the risk of attaining false-positives. We
886 hope to emphasise in this study that this is not always the case, as false-positives (i.e.
887 genome scan outliers that are not associated with regions under divergent selection) can be
888 driven by non-random genomic or common demographic features that cannot be bypassed
889 through replication. Moreover, many of the patterns we observe are variable through time,
890 such that the relevant pitfalls of analyses will depend on the age of the populations being
891 considered. It should thus also be important to estimate population splits, as a young
892 replicate pair and older replicate pair with similar demographic histories should be expected
893 to exhibit potentially different patterns of genetic variation.

894

895 Recent simulation work by Quilodrán et al. (2019), has also emphasised the influence of
896 genomic features and demography, and includes simulation software for estimating the
897 distribution of genetic variation over user-defined chromosomes. Such an approach is
898 particularly useful for systems with chromosome-level genome assemblies in order to gain a
899 sense for how features such as recombination, gene density, and selection targets may
900 produce false-positives under certain demographies. The software employed here, SLiM
901 (Haller and Messer 2019), may also be used to this end, and the scripts accompanying this
902 study will facilitate similar analyses over system-specific genome regions. Further, recent
903 work on genomic landscapes of linked selection (Stankowski *et al.* 2019) has highlighted that

904 much of the total variance of genetic divergence such as F_{ST} , D_{XY} , and π can be explained by
905 the major principal component (PC1) over numerous pairwise comparisons. These
906 population comparisons need not reflect divergent phenotypes, as PC1 reflects genomic
907 features associated with diversity landscapes. Adopting this approach may be useful for
908 systems lacking a chromosome-level genome assembly by estimating SNPs or regions with
909 non-random elevated measures of divergence associated with genome features. Such SNPs
910 or regions may be particularly prone to false-positives under certain demographic histories.

911

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920

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1089

1090

1091 **FIGURE LEGENDS**

1092

1093 **Figure 1:** Experimental design for simulations. **A)** Examples of selection treatments
1094 experienced by genes from across the range, illustrated as the relationship between relative
1095 fitness of an individual and its phenotype. Each facet represents a different fitness
1096 landscape modified through editing the standard deviation of the normal distribution of
1097 fitness consequences in DP (blue, dashed). Facet labels constitute S , which were
1098 transformed as 10^{-5} to give fitness function standard deviations (S_{σ}) The x-axes represent
1099 phenotype as calculated through non-synonymous mutations and the y-axes represent
1100 relative fitness of individuals. The ancestral phenotype of AP (red, solid) is the same in all
1101 treatments (mean = 0, $\sigma = 1$), whilst DPs have a diverged phenotypic optimum (mean = 10, σ
1102 = S_{σ}). **B)** Distribution of S values applied to genes (1 per gene) **C)** Demographic
1103 representation of treatment factors. **D)** Representation of simulation timeline for
1104 treatments, illustrating that all treatments share an ancestral burn-in population before
1105 splitting into 16 replicated “AP” (solid) and “DP” (dotted) population pairs. Red, dashed lines
1106 denote sampling generations at which F_{ST} , D_{XY} and $\Delta\pi$ are calculated and averaged across
1107 the preceding 20 generations. The purpose of this averaging was to achieve a general sense
1108 of population differentiation at sampling points, such that values represent stable patterns
1109 rather than stochastic generation to generation variation. **E)** Examples of two simulated
1110 25kb regions, showing central genes that function as QTL, and illustrating how regions vary
1111 in gene length, exon N and selection target (%). **F)** Representation of 100 simulated 25kb
1112 regions dataset per iteration ($N = 20$) per treatment group ($N = 16$).

1113

1114 **Figure 2:** Effects of demographic treatments on measures of genetic divergence across all
1115 sampling generations. Point colour and shape denote treatment groups for founding
1116 bottlenecks **(A)**, prolonged bottlenecks **(B)** and migration **(C)**. Each point represents values
1117 of divergence averaged across all genes within individual treatments groups, averaged
1118 within treatment levels, and averaged over 20 iterations.

1119

1120 **Figure 3:** Effects of demographic treatments on the relationship between selection and
1121 measures of genetic divergence across all sampling generations. Point colour and shape
1122 denote treatment groups for founding bottlenecks (A), prolonged bottlenecks (B) and
1123 migration (C). Each point represents correlation coefficients calculated across all genes
1124 within individual treatments groups, averaged within treatment levels, and averaged over
1125 20 iterations.

1126
1127 **Figure 4:** Pairwise comparisons between the correlation coefficients of selection with F_{ST} , D_{XY} and $\Delta\pi$
1128 across four sampling points. Each data point represents a unique demographic treatment with
1129 points coloured according to DP population size and shaped according to migration level. Correlation
1130 1 refers to the first measure listed in the comparison and Correlation 2 to the second. The $y=x$ line is
1131 plotted within each facet to illustrate biases towards one measure. Points below the line are biased
1132 towards Correlation 1, whilst points above the line are biased towards Correlation 2. Each point
1133 represents correlation coefficients calculated across all genes within individual treatments groups
1134 and averaged over 20 iterations.

1135
1136 **Figure 5:** Distributions of F_{ST} under each of the 16 unique demographic treatments under three
1137 selection regimes: Pheno_{Div} (divergent selection), Pheno_{Null} (stabilising selection) and Neutral, after
1138 10,000 generations. Upper 5% quantiles are highlighted for each distribution, with linetype
1139 corresponding to selection: Solid = Divergent, Dashed = Stabilising, Dotted = Neutral. Each
1140 distribution represents data pooled from 20 iterations of 100 25kb regions (N = 2000).

1141
1142 **Figure 6:** Effects of demographic treatments on the relationship between measures of genetic
1143 divergence across all sampling generations. Point colour and shape denote treatment groups for
1144 founding bottlenecks (A), prolonged bottlenecks (B) and migration (C). Each point represents
1145 correlation coefficients calculated across all genes within individual treatments groups, averaged
1146 within treatment levels, and averaged over 20 iterations.

1147
1148 **Figure 7:** The proportional overlap of outliers above the 95% quantile, averaged across 100
1149 downsampled datasets consisting of 95% Neutral and 5% Pheno_{Div} data for each of the 16
1150 demographic treatments after 10,000 generations. Axis orderings were determined through
1151 hierarchical clustering. Heatmaps are shown for single measures of F_{ST} , D_{XY} and $\Delta\pi$ in the first
1152 column, and combined measures in the second column. Heatmaps are coloured according to a
1153 common scale of 0 to 1. Treatments are labelled with founding bottleneck (Bot), DP population size
1154 (Pop2), and migration (Mig) values.

TABLE 1: SIMULATION PARAMETERS

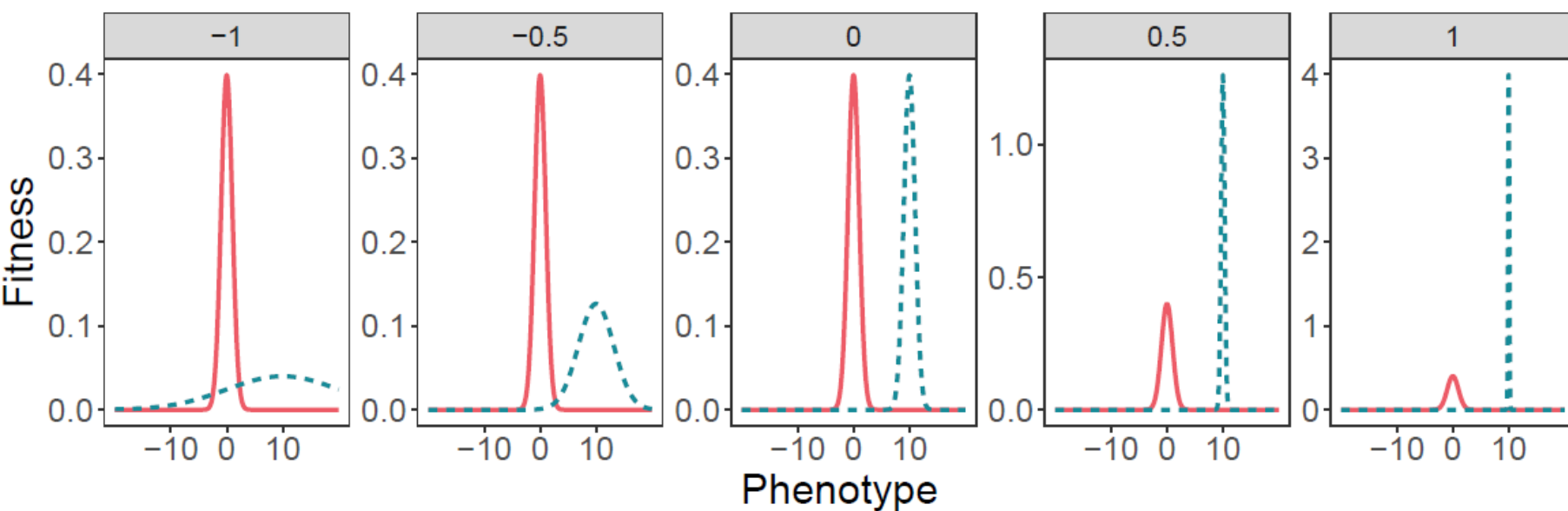
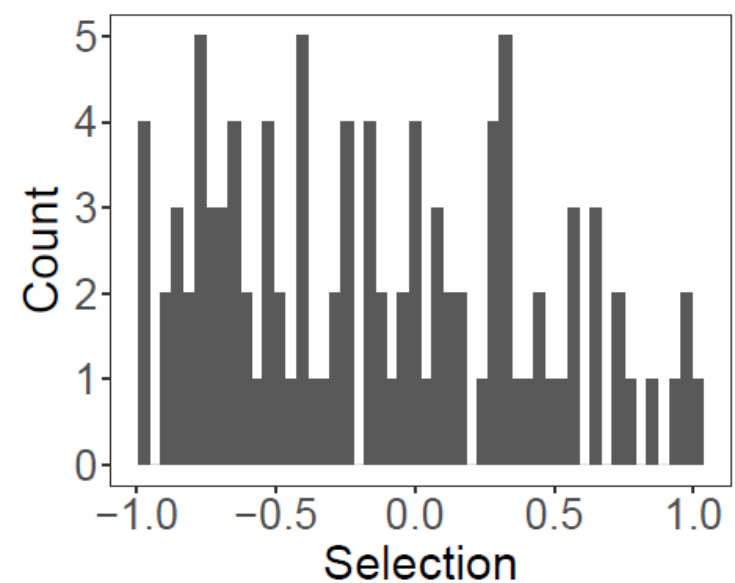
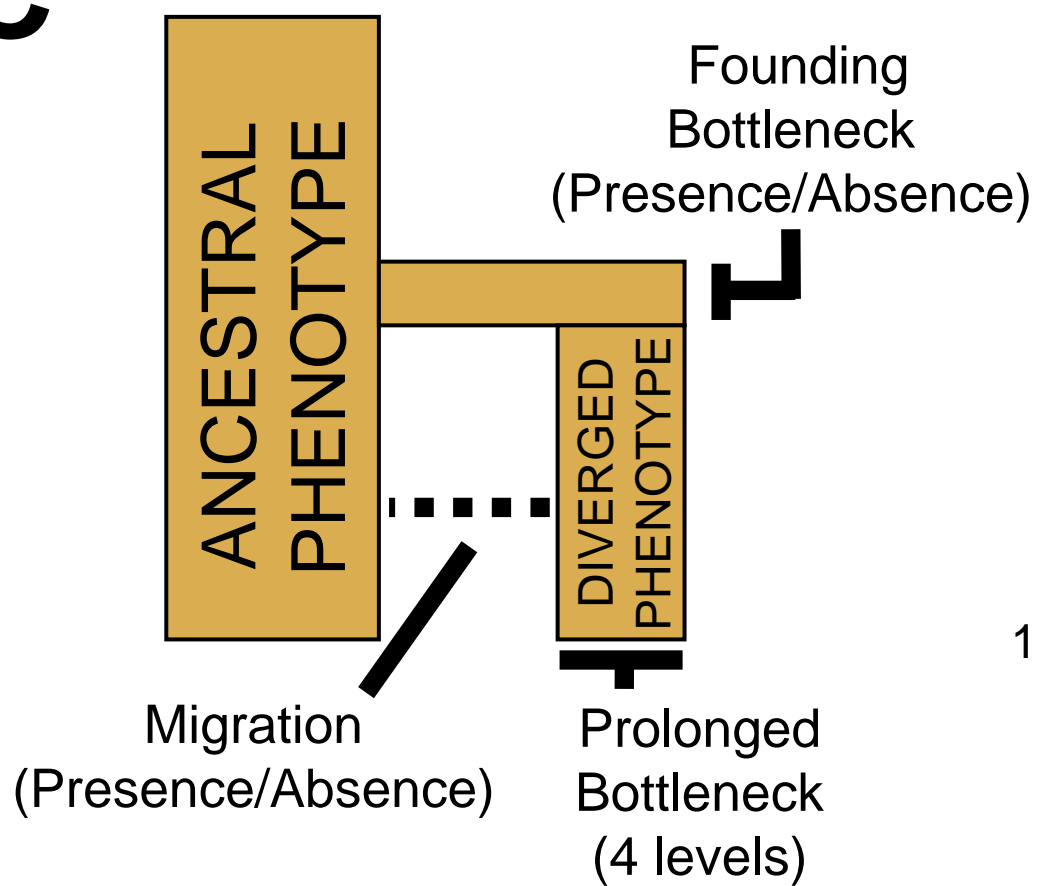
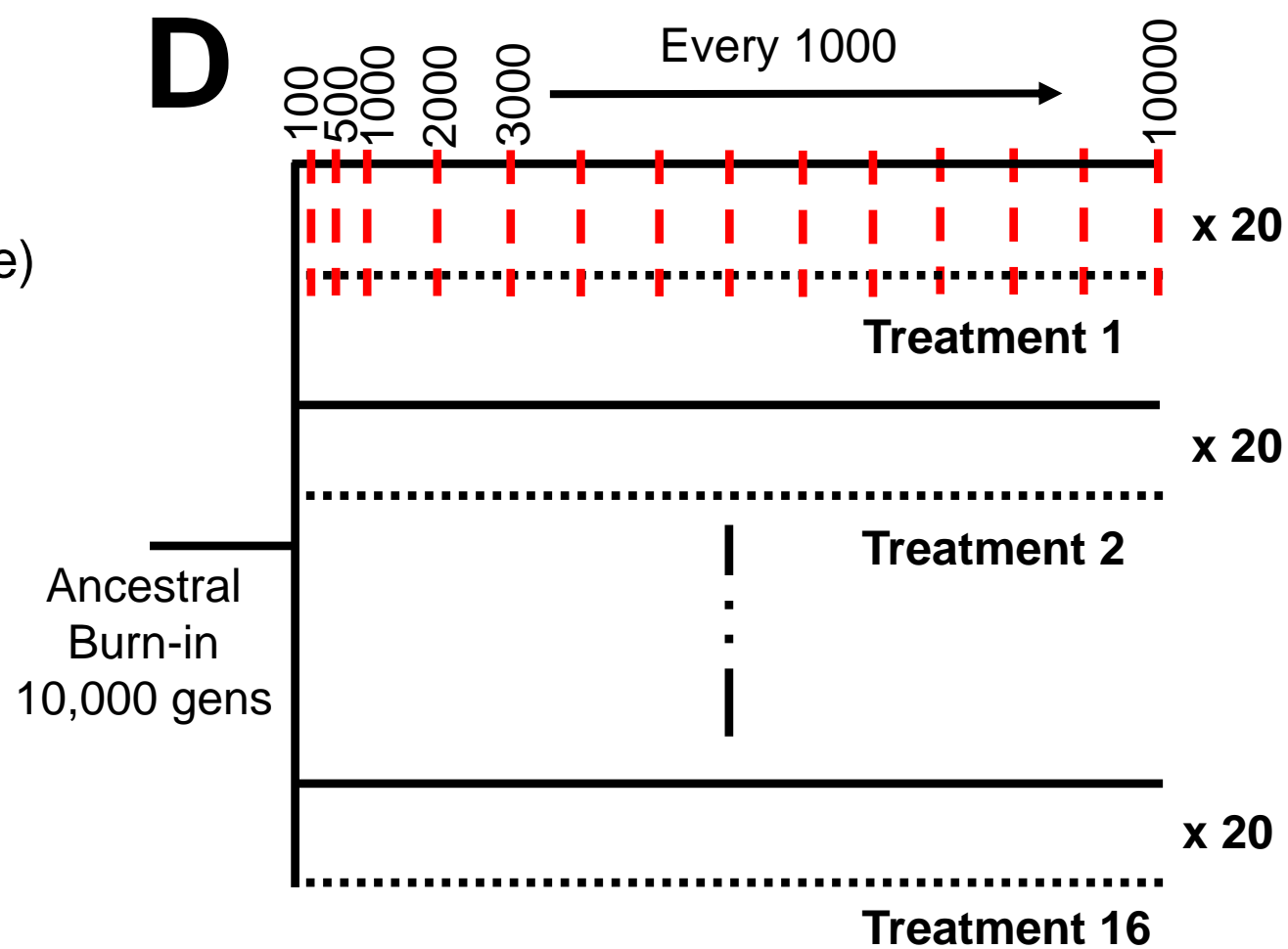
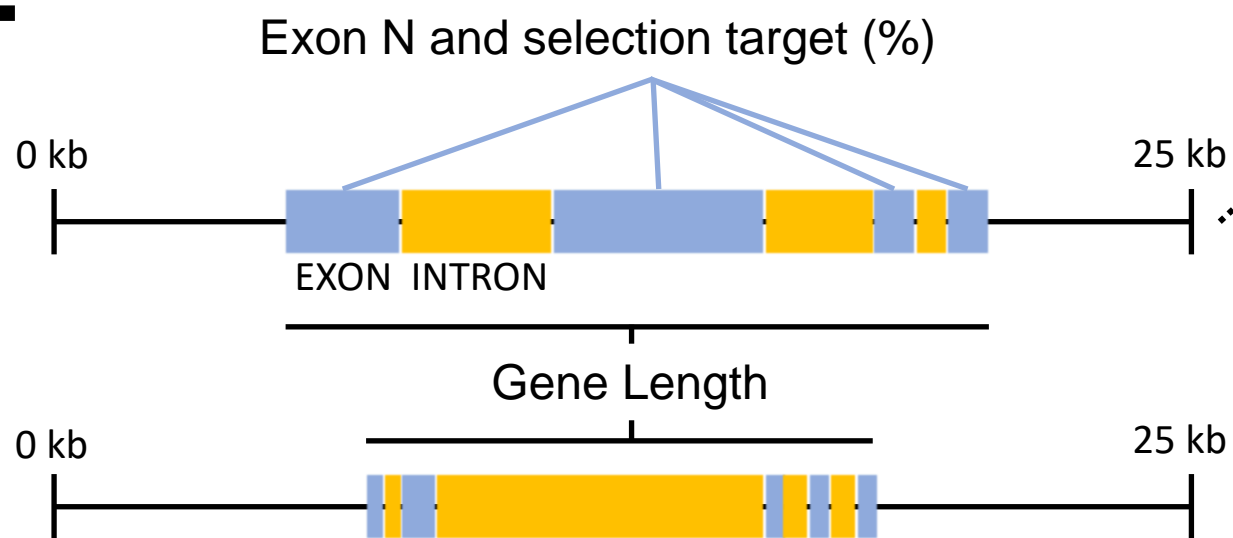
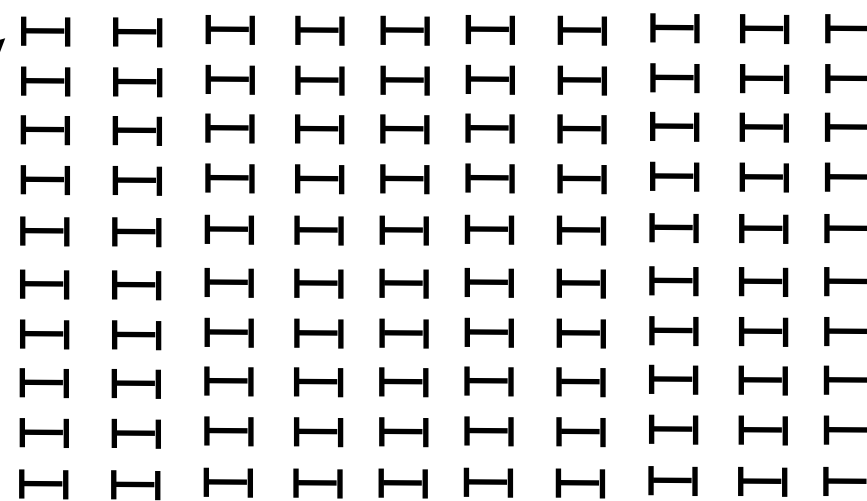
| Variable | Value | Description |
|-----------------|--|--|
| AP | 0 | Ancestral phenotypic optimum |
| AP- S_σ | 1 | AP Selection (σ of fitness around phenotypic optimum, after transforming) |
| AP _N | 1000 | AP population size |
| DP | 10 | Diverged phenotypic optimum |
| DP- S_σ | 0.1-10.00 | DP Selection (σ of fitness around phenotypic optimum, after transforming) |
| DP _N | (10, 100, 500, 1000) | DP population size |
| BN | (100, 1000) | Founding bottleneck (N burn-in genomes sampled to populate DP) |
| m | (0, 0.002) | Migration (Percentage gene flow in both directions) |
| μ | $4.89e^{-6}$ ($4.89e^{-5}$, $4.89e^{-7}$) | Mutation rate (bp^{-1}) (additional rates for higher/lower scaling) |
| μ_σ | 1.00 | Mutation effect size (σ of distribution of effect sizes) |
| r | $1.00e^{-6}$ ($1.00e^{-5}$, $1.00e^{-7}$) | Recombination rate (bp^{-1}) (additional rates for higher/lower scaling) |
| C_{max} | 1.00 | Maximum fitness cost through competition |
| C_σ | 0.40 | Local phenotypic competition (σ of fitness reductions between individuals) |
| C_{Dist} | 1.20 | Maximum phenotypic distance between competitive individuals |

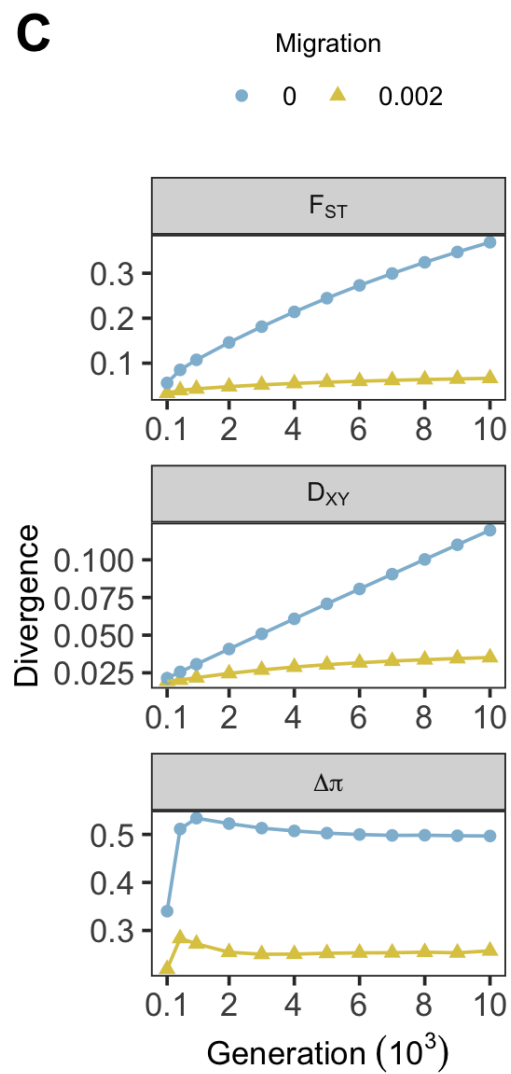
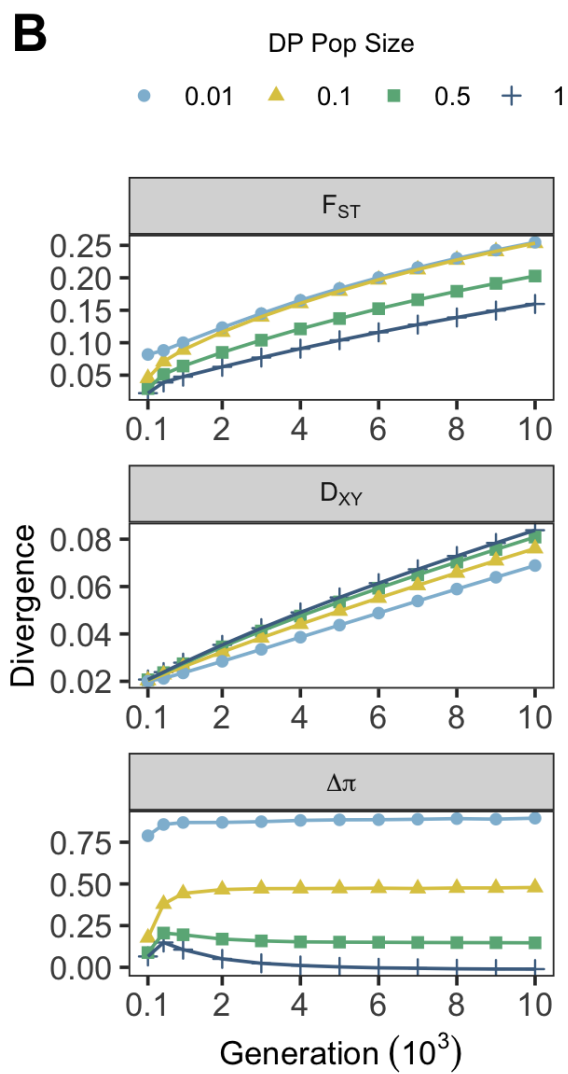
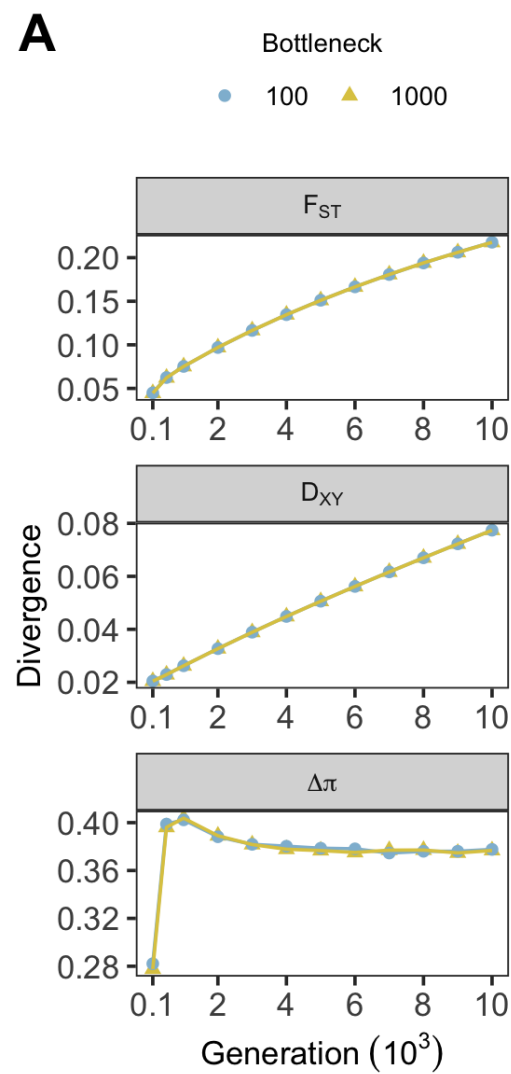
TABLE 2: FALSE POSITIVE (FPR) AND FALSE NEGATIVE RATES (FNR) CALCULATED ACROSS ALL MEASURES OF DIVERGENCE AND THEIR COMBINED USE. ESTIMATES WERE CALCULATED BY COMBINING 5% OF DATA UNDER DIVERGENT SELECTION WITH 95% NEUTRAL DATA AND TAKING UPPER 5% CUT-OFFS. FOR SINGLE MEASURES, OUTLIER N IS ALWAYS 100 (5% OF 2,000) AND FNR = FPR.

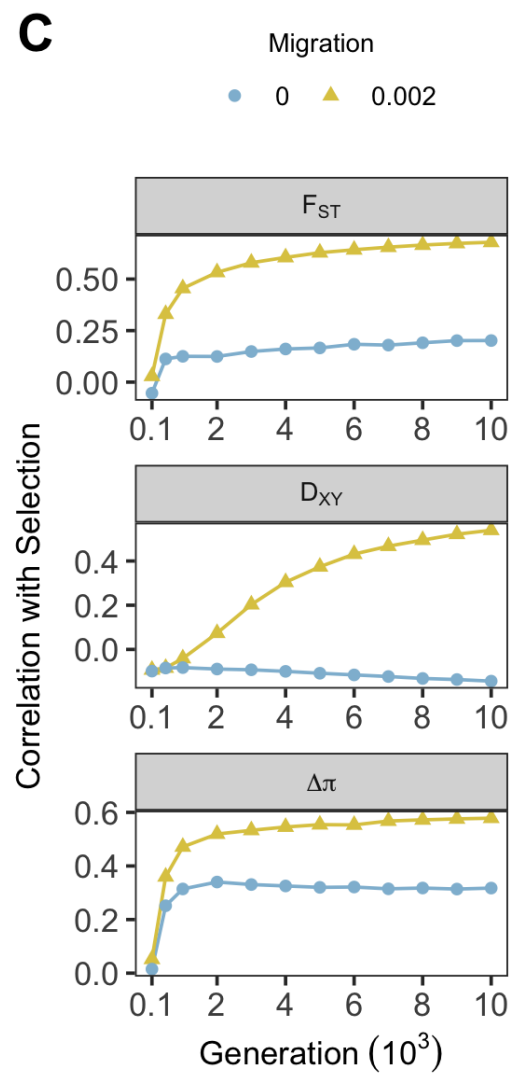
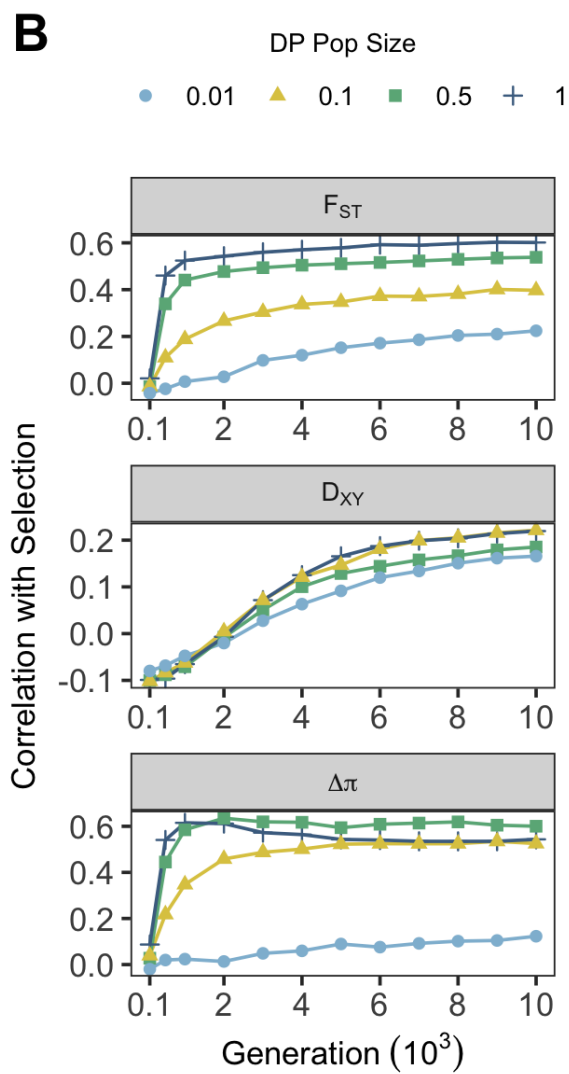
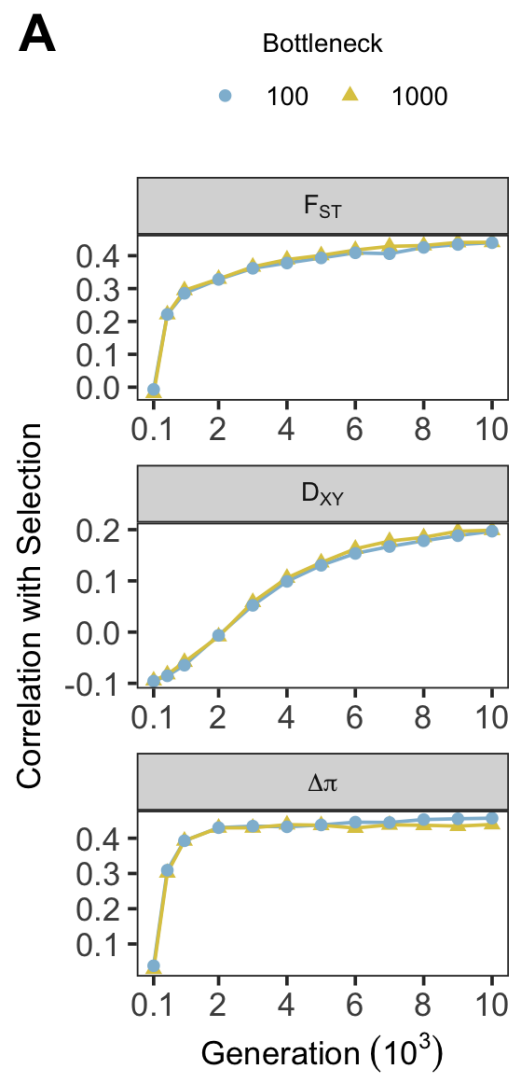
| Gen | Demographic Treatments | | Single Measures | | | Combined Measures | | | | | | | | | | | |
|-------|------------------------|---------|-----------------|----------|-------------|--------------------|------|------|-----------------------|------|------|-----------------------|------|------|-----------|------|------|
| | Migration | DP Size | F_{ST} | D_{XY} | $\Delta\pi$ | $F_{ST} \& D_{XY}$ | | | $F_{ST} \& \Delta\pi$ | | | $D_{XY} \& \Delta\pi$ | | | All 3 | | |
| | | | FPR | FPR | FPR | Outlier N | FPR | FNR | Outlier N | FPR | FNR | Outlier N | FPR | FNR | Outlier N | FPR | FNR |
| 500 | 0 | 0.01 | 0.87 | 0.87 | 0.99 | 62.21 | 0.87 | 0.92 | 9.64 | 0.98 | 1.00 | 26.21 | 0.98 | 1.00 | 9.64 | 0.98 | 1.00 |
| 500 | | 0.1 | 0.91 | 0.86 | 0.99 | 54.79 | 0.89 | 0.94 | 14.77 | 0.98 | 1.00 | 13.63 | 0.99 | 1.00 | 7.89 | 0.98 | 1.00 |
| 500 | | 0.5 | 0.50 | 0.81 | 0.47 | 31.56 | 0.49 | 0.84 | 41.54 | 0.19 | 0.66 | 12.11 | 0.37 | 0.92 | 10.01 | 0.24 | 0.92 |
| 500 | | 1 | 0.28 | 0.80 | 0.28 | 26.84 | 0.28 | 0.81 | 59.81 | 0.04 | 0.43 | 14.99 | 0.00 | 0.85 | 14.75 | 0.00 | 0.85 |
| 500 | 0.002 | 0.01 | 0.93 | 0.76 | 0.98 | 60.15 | 0.92 | 0.95 | 19.57 | 0.97 | 0.99 | 17.07 | 0.96 | 0.99 | 15.21 | 0.96 | 0.99 |
| 500 | | 0.1 | 0.85 | 0.81 | 0.96 | 14.83 | 0.78 | 0.97 | 29.09 | 0.89 | 0.97 | 1.48 | 0.72 | 0.99 | 1.48 | 0.72 | 0.99 |
| 500 | | 0.5 | 0.35 | 0.90 | 0.47 | 10.56 | 0.37 | 0.93 | 58.81 | 0.17 | 0.51 | 5.20 | 0.21 | 0.96 | 5.20 | 0.21 | 0.96 |
| 500 | | 1 | 0.18 | 0.90 | 0.30 | 11.37 | 0.29 | 0.92 | 66.35 | 0.02 | 0.35 | 6.61 | 0.12 | 0.94 | 5.67 | 0.00 | 0.94 |
| 10000 | 0 | 0.01 | 0.95 | 0.89 | 0.97 | 27.86 | 0.96 | 0.99 | 0.00 | 0.00 | 1.00 | 7.57 | 0.96 | 1.00 | 0.00 | 0.00 | 1.00 |
| 10000 | | 0.1 | 0.98 | 0.89 | 1.00 | 31.29 | 0.99 | 1.00 | 0.73 | 0.73 | 1.00 | 1.53 | 0.98 | 1.00 | 0.00 | 0.00 | 1.00 |
| 10000 | | 0.5 | 0.98 | 0.88 | 0.98 | 31.21 | 0.99 | 1.00 | 7.60 | 0.99 | 1.00 | 4.98 | 0.95 | 1.00 | 3.79 | 0.99 | 1.00 |
| 10000 | | 1 | 0.94 | 0.88 | 0.95 | 31.47 | 0.95 | 0.98 | 5.25 | 0.82 | 0.99 | 5.15 | 0.87 | 0.99 | 2.80 | 0.89 | 1.00 |
| 10000 | 0.002 | 0.01 | 0.53 | 0.17 | 0.79 | 56.84 | 0.21 | 0.55 | 34.41 | 0.44 | 0.81 | 22.76 | 0.17 | 0.81 | 22.56 | 0.17 | 0.81 |
| 10000 | | 0.1 | 0.27 | 0.04 | 0.89 | 72.06 | 0.00 | 0.28 | 24.08 | 0.54 | 0.89 | 11.12 | 0.00 | 0.89 | 11.12 | 0.00 | 0.89 |
| 10000 | | 0.5 | 0.17 | 0.17 | 0.70 | 74.68 | 0.02 | 0.27 | 32.26 | 0.09 | 0.70 | 28.57 | 0.00 | 0.71 | 28.57 | 0.00 | 0.71 |
| 10000 | | 1 | 0.14 | 0.34 | 0.78 | 67.03 | 0.07 | 0.37 | 25.33 | 0.11 | 0.78 | 20.70 | 0.05 | 0.80 | 20.70 | 0.05 | 0.80 |

TABLE 3: LMM RESULTS FOR MODELS OF MEASURES OF DIVERGENCE EXPLAINED BY FEATURES OF SIMULATED REGIONS. FOR ALL MODELS, RANDOM VARIABLES INCLUDED GENE ID AND DEMOGRAPHIC TREATMENT.

| Measure | Migration | Var. explained (%) | | Fixed Effect | Estimate | Std. Error | df | <i>t</i> | <i>P</i> |
|-----------------|-----------|--------------------|-------|------------------|----------|------------|-------|----------|-----------|
| | | Fixed | Total | | | | | | |
| F _{ST} | 0.002 | 48.96 | 69.12 | Selection | 0.044 | 0.002 | 98 | 27.27 | <2.00E-16 |
| | | | | Selection Target | 0.009 | 0.001 | 103 | 9.32 | 2.47E-15 |
| | | | | Pheno Gen | -0.002 | 0.000 | 14530 | -7.55 | 4.60E-14 |
| F _{ST} | 0 | 1.10 | 96.84 | Selection | 0.005 | 0.001 | 96 | 4.32 | 3.78E-05 |
| | | | | Pheno Gen | 0.000 | 0.000 | 14480 | -2.58 | 0.010* |
| | | | | Exon N | 0.005 | 0.002 | 96 | 2.51 | 0.014* |
| | | | | Selection Target | 0.004 | 0.002 | 97 | 2.46 | 0.015* |
| D _{XY} | 0.002 | 9.53 | 84.25 | Selection | 0.007 | 0.000 | 98 | 16.97 | <2.00E-16 |
| | | | | Pheno Gen | -0.001 | 0.000 | 14560 | -10.49 | <2.00E-16 |
| | | | | Exon N | -0.001 | 0.000 | 101 | -4.15 | 6.89E-05 |
| D _{XY} | 0 | 30.70 | 53.94 | Selection Target | -0.003 | 0.000 | 98 | -11.57 | <2.00E-16 |
| Δπ | 0.002 | 8.27 | 76.20 | Selection | 0.184 | 0.006 | 99 | 29.82 | <2.00E-16 |
| | | | | Selection Target | 0.018 | 0.004 | 120 | 4.71 | 6.84E-06 |
| | | | | Pheno Gen | 0.006 | 0.002 | 14250 | 2.92 | 0.004 |
| Δπ | 0 | 0.59 | 95.84 | Selection | 0.066 | 0.004 | 99 | 16.14 | <2.00E-16 |
| | | | | Exon N | -0.018 | 0.003 | 111 | -6.15 | 1.24E-08 |
| | | | | Pheno Gen | -0.004 | 0.001 | 13900 | -3.33 | 8.67E-04 |

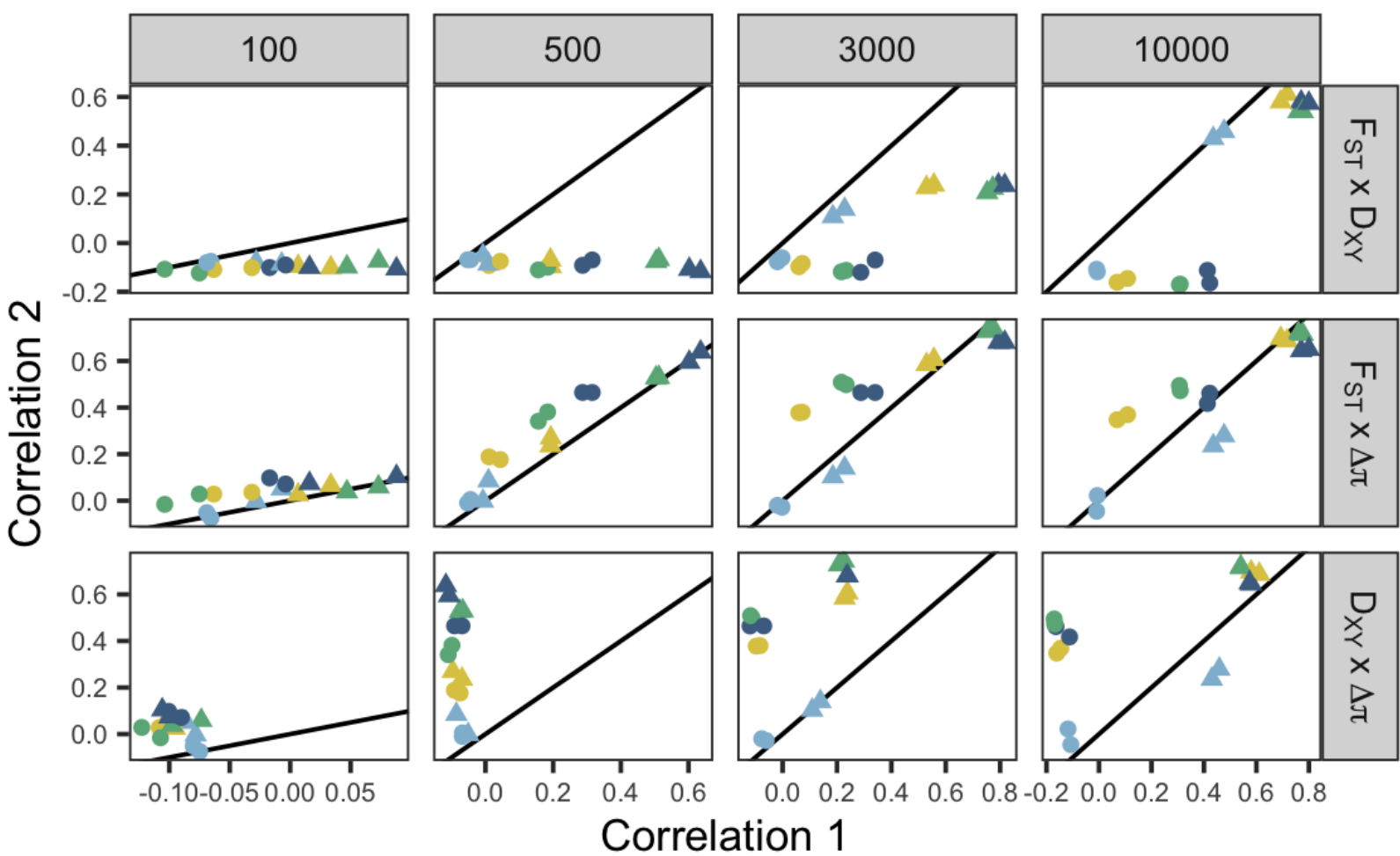
A**B****C****D****E****F**



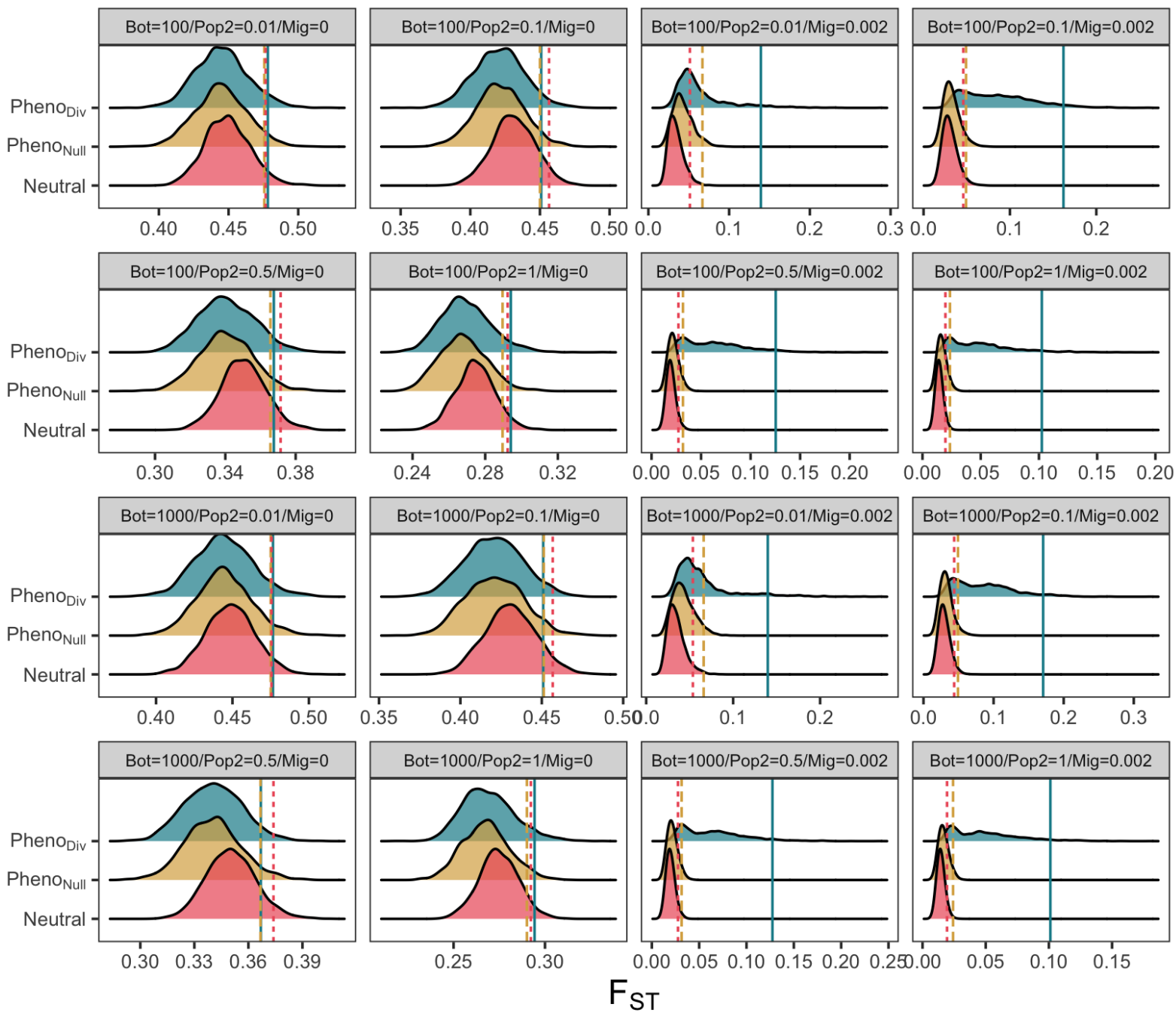


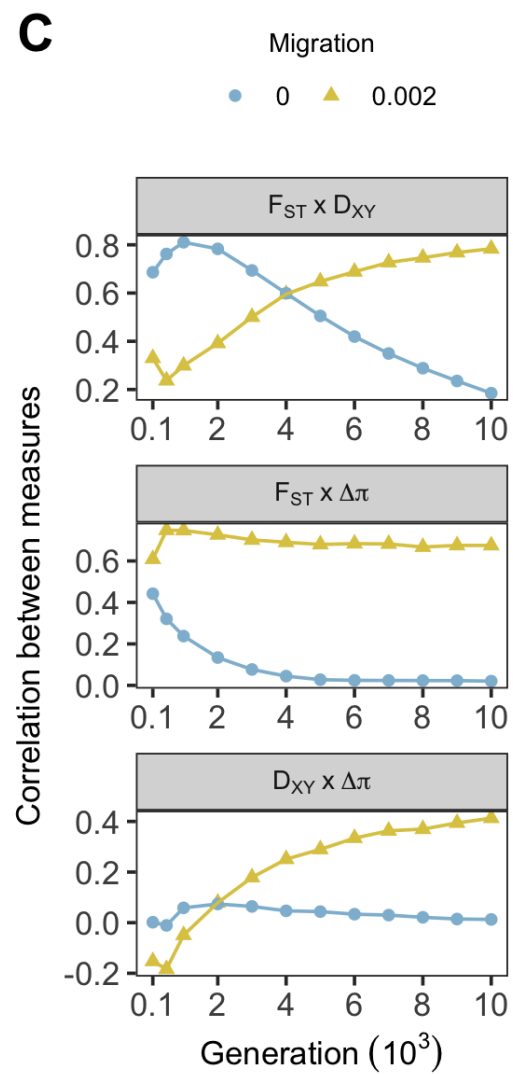
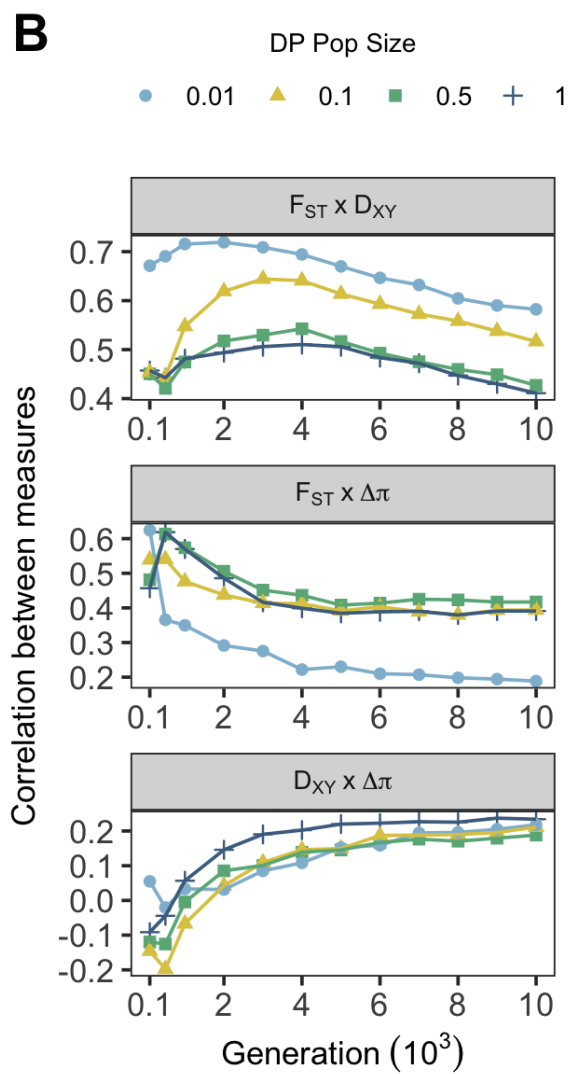
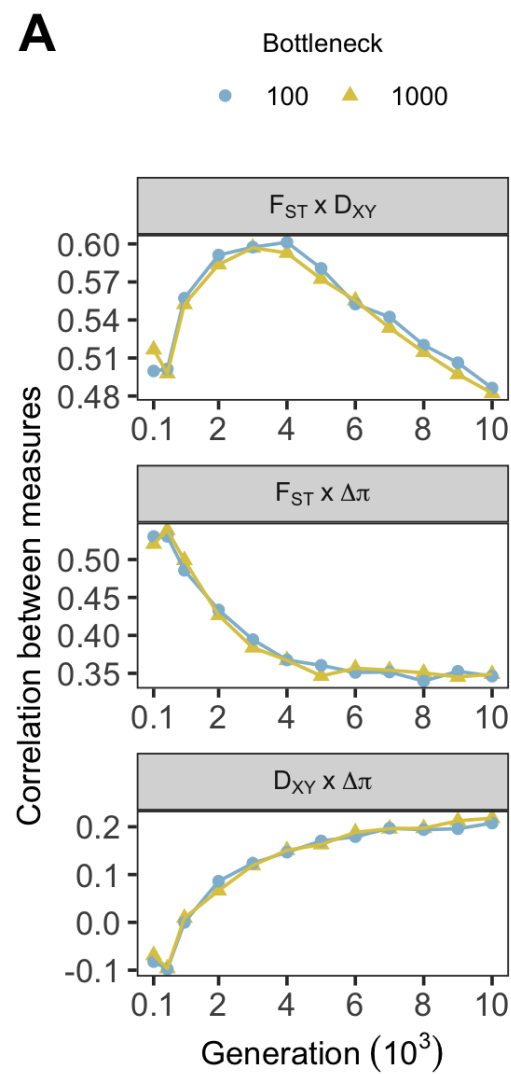
Migration DP Pop Size

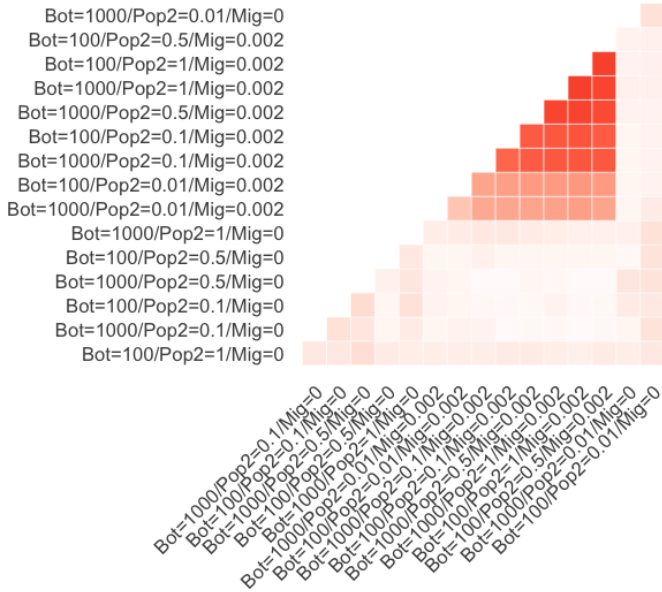
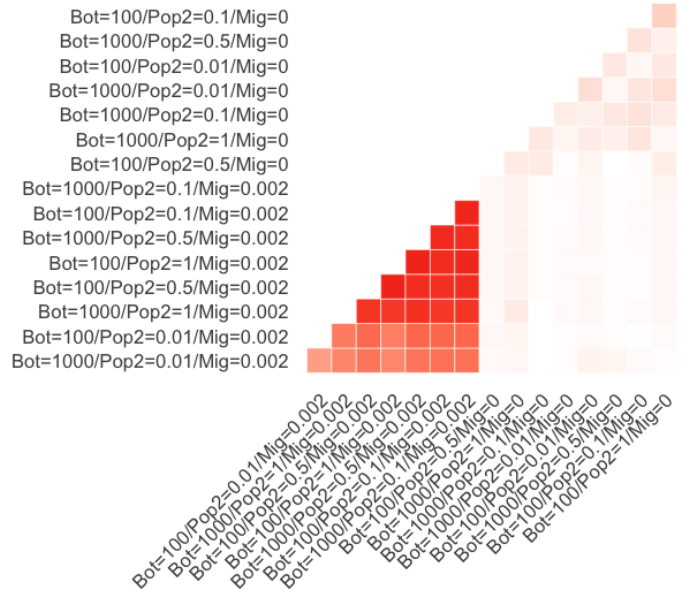
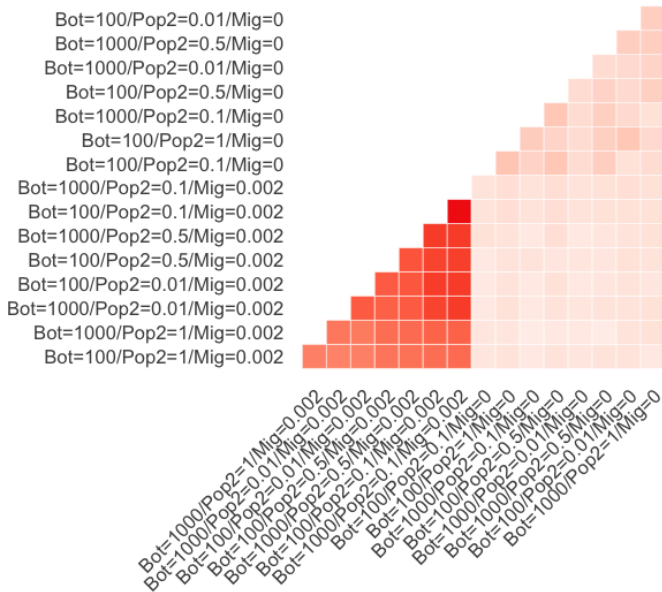
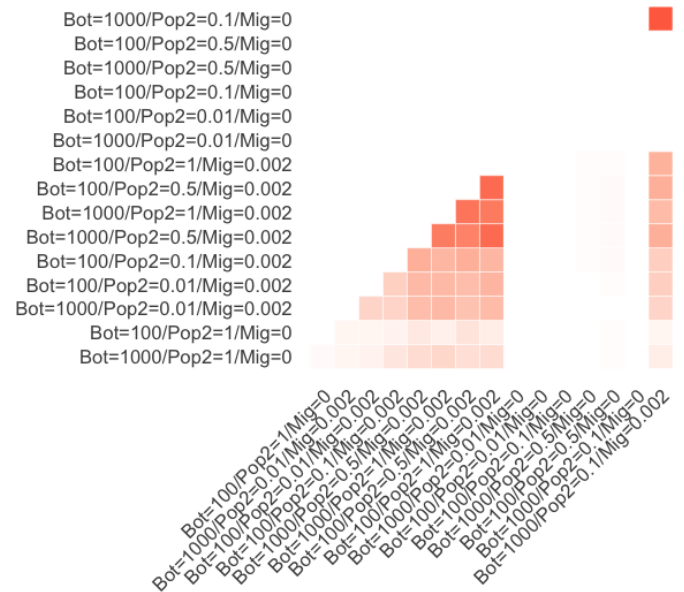
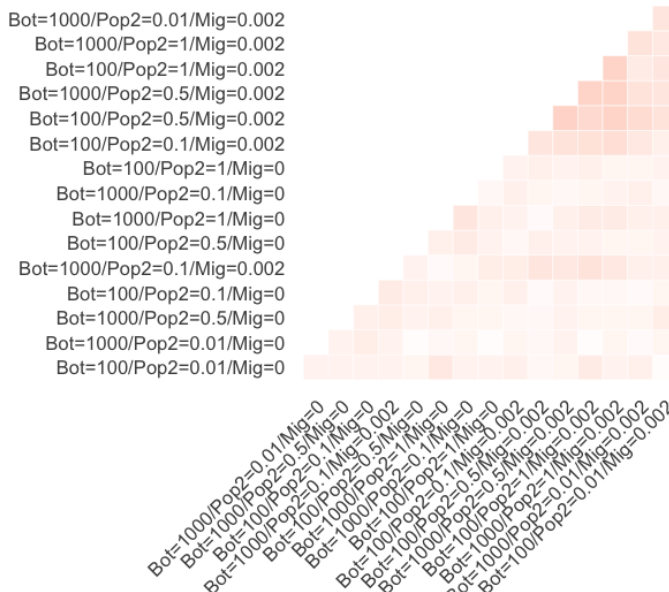
● 0 ▲ 0.002 ● 0.01 ● 0.1 ● 0.5 ● 1



Simulation Type





F_{ST}  $F_{ST} + D_{XY}$  D_{XY}  $F_{ST} + \Delta \pi$  $\Delta \pi$  $D_{XY} + \Delta \pi$ 