# Simulations for the Test Flight of an Experimental HALE Aircraft 

Brooke E. Kaszynski

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# SIMULATIONS FOR THE TEST FLIGHT OF AN EXPERIMENTAL HALE AIRCRAFT 

THESIS

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# SIMULATIONS FOR THE TEST FLIGHT OF AN EXPERIMENTAL HALE AIRCRAFT 

## THESIS

Presented to the Faculty<br>Department of Aeronautics and Astronautics Graduate School of Engineering and Management<br>Air Force Institute of Technology<br>Air University<br>Air Education and Training Command<br>In Partial Fulfillment of the Requirements for the Degree of Master of Science in Aeronautical Engineering

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June 2011

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#### Abstract

Recent events, such as the crash of NASA's Helios aircraft during a test flight, show that more must be known about the nonlinear control of HALE aircraft. Shearer, Cesnik and their co-workers have developed a code that is a practical solution to the coupled nonlinear aeroelasticity and flight dynamics of very flexible aircraft called the University of Michigan's Nonlinear Aeroelastic Simulation Toolbox (UM/NAST). They are also in the process of developing a model HALE aircraft called X-HALE which will be used to validate this code experimentally. This research performs flight simulations with UM/NAST so as to make predictions about X-HALE's future test flights and subsequently uncover the strengths and weaknesses of UM/NAST when X-HALE is finally flown. These simulations include simulations of straight and level flight and rolling flight. Rolling simulations involve periodic changes in the angle of the ailerons. Both the 6 meter and the 8 meter models of X-HALE are studied. Two control models are compared. These include the linear and non-linear models of UM/NAST.


## Acknowledgements

I would like to say thank you to my loving husband and our beautiful son; both of whom have been with me the whole way on this journey, and to God for all the wonderful blessings He has given me in life.

Brooke E. Kaszynski

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## List of Symbols

Symbol

| $a$ | An arbitrary point in the vehicle with respect to the origin of the inertial frame $G$ |
| :---: | :---: |
| B | The body-fixed reference frame |
| $b$ | Displacements and rotations as the time integral of $\beta$ |
| C | A generalized damping matrix |
| F | An externally applied state-dependent force |
| $f(\cdot)$ | Generic function |
| $f$ | A vector used to trim the aircraft |
| $f_{d s t}, f_{p t}$ | Distributed and point forces |
| G | The inertial reference frame |
| $g^{B}$ | $B$ reference frame resolved gravity vector |
| $g_{0}$ | Gravity column vector |
| $h$ | The position and orientation vector of the flexible structure |
| $I_{B}$ | Inertia matrix |
| $J$ | Jacobian matrix |
| $J_{\text {trim }}$ | Trim cost function |
| K | A generalized stiffness matrix |
| M | An externally applied state-dependent moment or a generalized mass matrix |
| $m$ | Mass per unit span |
| O | The origin of the $B$ reference frame |
| $p_{a}$ | Position of an arbitrary point in the vehicle with respect to the origin of the inertial frame $G$ |
| $p_{B}$ | Inertial position vector of the $B$ reference frame |
| $p_{r}$ | Position from the $B$ reference frame origin $t$ the local $w$ reference frame |
| $p_{r_{c m}}$ | Vector from the $B$ reference frame origin to the center of mass |
| $q$ | Generalized displacement column vector |


| $R$ | Either the a generalized force column vector, or the residual value computed at each subiteration when UM/NAST is run |
| :---: | :---: |
| $R_{B}$ | Generalized force applied to the B reference frame states |
| $R_{F}$ | Generalize force applied to elastic states |
| $S$ | Search variable column vector |
| $s$ | Undeformed beam spatial dimension |
| $t$ | Time |
| $u$ | Control surface and external inputs for a function |
| $v_{B}$ | Linear velocity vector of the $B$ reference frame |
| w | Local elastic reference frame |
| $\delta W$ | The total virtual work |
| $x, y, z$ | The $x, y$ and $z$ directions |
| $\alpha$ | Angle of attack |
| $\beta$ | Column vector of the $B$ reference frame linear and angular velocities |
| $\delta_{e}$ | Elevator deflection angle |
| $\delta_{t}$ | Thrust |
| $\epsilon$ | Column vector of the elastic strain state |
| $\zeta$ | Quaternion column vector used for the $B$ reference frame orientation |
| $\Theta_{B}$ | Generalized B reference frame rotation vector |
| $\lambda$ | Column vector of inflow states |
| $\bar{\Omega}_{\zeta}$ | The finite element discretization of the $\omega_{B}$ matrix |
| $\omega_{B}$ | Angular velocity vector of the $B$ reference frame |
| $(\stackrel{\sim}{*})$ | Skew-symmetric matrix operator |
| ( ${ }_{\text {( }}$ ) | Transpose of the skew-symmetric matrix operator |

Subscript or superscript
aero $\quad$ Related to aerodynamic effects
$B \quad$ A reference to the body-fixed reference frame $B$
$B B, B F \quad$ Contributions of a particular matrix to the body and body/flexible differential equations of motion
dst Distributed

| (e) | Element number |
| :--- | :--- |
| ext | External |
| $F$ | A reference to the flexible degree of freedom |
| $F F, F B$ | Contributions of a particular matrix to the body and flexible/body <br> differential equations of motion |
| $G$ | A reference to the global matrix |
| $k$ | A member, which is a collection of elements, index |
| $p t$ | Point |
| $T$ | Transpose operator |

## List of Abbreviations

Abbreviation

| AFIT | Air Force Institute of Technology |
| :--- | :--- |
| AVL | Athena Vortex Lattice |
| CFD | Computational Fluid Dynamics |
| ESC | Electronic Speed Controller |
| GPS | Global Positioning System |
| HALE | High Altitude Long Endurance |
| INS | Inertial Navigating System |
| ISR | Intelligence, Surveillance and Reconnaissance |
| MC | Phoenix Integration's Model Center Software |
| NASA | National Aeronautics and Space Administration |
| NATASHA | Nonlinear Aeroelastic Trim and Stability for HALE aircraft |
| Nastran | NASA Stress Analysis Program |
| NPRF | Navy Pacific Range Facility |
| ONERA | Office National d'Etudes et Recherches Aérospatiales |
| SBC | Single Board Computer |
| SSC | Servo Switch Controller |
| RCAS | Rotorcraft Comprehensive Analysis System |
| RPA | Remotely Piloted Aircraft |
| THWIL | True Hardware in the Loop |
| UM/NAST | University of Michigan's Nonlinear Aeroelastic Simulation Toolbox |
| X-HALE | Experimental High Altitude Long Endurance |

## SIMULATIONS FOR THE TEST FLIGHT OF A HALE AIRCRAFT

## I. Introduction

High Altitude Long Endurance (HALE) aircraft have great potential as Intelligence, Surveillance and Reconnaissance (ISR) platforms [35]. Additionally, they can also be used as network communication nodes for military or civilian purposes, or perform general atmospheric research [39]. The US Air Force has been developing a new type of ISR aircraft called "SensorCraft", which are large HALE aircraft with wings spans in excess of 60 meters. These highly flexible aircraft ideally have high-aspectratio wings, slender fuselages and high aircraft performance to handle long loiter times and heavy payloads [22]. SensorCraft generally have high structural performance, high aerodynamic efficiencies and low structural weight fractions. As a result, they also generally have low frequency natural structural vibration modes, and geometricallynonlinear structural and flight dynamics. The three platform shapes that have been considered for SensorCraft are wing-body-tail (Figure 1), single-wing (Figure 2) and joined-wing (Figure 3) configurations [34]. Because very flexible aircraft have very low frequencies for their natural vibration modes, the structural dynamics and the rigid-body characteristics of these aircraft are strongly coupled [4].


Figure 1. Wing-Body-Tail Configuration [4]


Figure 2. Single-Wing Configuration [4]


Figure 3. Joined-Wing Configuration [4]

Aurora Flight Sciences, Boeing Co. and Lockheed-Martin Co. have developed very long duration HALE aircraft concepts for the DARPA's Vulture Program [40]. However, recent events show that more must be known about the nonlinear control of HALE aircraft. For example, NASA developed the Helios aircraft (Figure 4) as a forerunning HALE Remotely Piloted Aircraft (RPA).


Figure 4. Aerovironment's Helios [4]

During a flight test on 26 June 2003, Helios experienced turbulence on a test flight at the Navy Pacific Missile Range Facility (PMRF) near Kauai, Hawaii, and developed high wing dihedral which resulted in an unstable pitching mode. The resulting high speed caused parts of the aircraft wing and solar cells to rip off. The aircraft then crashed in to the ocean. One of the primary causes of the accident was that Helios' engineers did not fully understand the nonlinear flight dynamics of the aircraft [14]. Several codes, such as NATASHA (Nonlinear Aeroelastic Trim and Stability for HALE
aircraft), RCAS (Rotorcraft Comprehensive Analysis System) and ASWING have been developed for the use of modeling nonlinear aeroelastic and flight dynamics of an aircraft but none have been completely validated with real flight data from a HALE aircraft [4].

Shearer, Cesnik and their co-workers [4] have developed a Matlab program that is a practical solution to the coupled nonlinear aeroelasticity and flight dynamics of very flexible aircraft called the University of Michigan's Nonlinear Aeroelastic Simulation Toolbox (UM/NAST). This code serves as a plant representation for HALE aircraft control design. It focuses on a reduced number of states to represent the complex nonlinear problem. This code addresses the following issues: nonlinear aeroelastic modeling, integral wing actuation for generating maneuver loads, flutter boundary enhancement, gust load alleviation and overall nonlinear vehicle optimization of unconventional high aspect ratio aircraft. Shearer, Cesnik and their co-workers are also in the process of developing a scaled test HALE aircraft called X-HALE which will be used to validate UM/NAST. The goal of this research is to perform flight simulations with UM/NAST so as to make predictions about X-HALE's future test flights and subsequently uncover the strengths and weaknesses of UM/NAST when X-HALE is finally flown.

## II. Theoretical Development

## II. 1 Previous Research and Motivation

Recent events such as the crash of NASA's Helios aircraft show that more must be known about the nonlinear control of HALE aircraft. This is the motivation of this research. Nonlinear aeroelastic solvers have been under development since the 1990's; however, the problem of nonlinear aeroelasticity coupled with nonlinear flight dynamics is still not completely understood. Several codes, such as UM/NAST, NATASHA, ASWING and RCAS, have been developed for the use of modeling nonlinear aeroelastic and flight dynamics of an aircraft but none have been completely validated with real flight test data from a HALE aircraft; they have been validated in a piecemeal fashion against beam models such as a simple cantilevered beam model and wind tunnel data. This is because there currently is no aircraft flight data available for validation [4]. A history of progress made on the problem of nonlinear aeroelasticity coupled with nonlinear flight dynamics will be explored.

## II. 2 The Early Work of Van Schoor, Von Flotow and Jones

Van Schoor and von Flotow were two of the first to study nonlinear aeroelasticity for very flexible aircraft in the 1990's. They demonstrated that when flexible structural modeling is included the classic rigid-body modes change significantly by using linearized analysis about nonlinear equilibrium points. Their work confirmed the importance of taking aircraft structural dynamics, as well as other aeroelastic effects such as gust response and flutter instability, into account when analyzing the flight dynamics of very flexible aircraft [36]. Jones and his co-workers [11] have worked on the approach of designing HALE aircraft. Their work describes some of the challenges with the design
approach of HALE aircraft and demonstrates that standard aircraft control design methods are not valid for the high-aspect-ratio and low Reynolds number wings of HALE aircraft. They concluded that this is because of the lack of data and methods that allow the prediction of a HALE aircraft's structure mass, engine performance at high altitudes and aerodynamic parameters. They explained that the high-aspect-ratio and low Reynolds number wings of HALE aircraft are associated with nonlinear structural dynamics and are frequently subject to aeroelastic phenomena such as flutter making typical design approaches unreliable.

## II. 3 The Development and Use of ASWING

Drela [6] was the first to begin developing the ASWING code and is currently working to improve its design. ASWING models an entire flexible aircraft as a structure of joined nonlinear beams. ASWING uses a compressible vortex type source-lattice with wind-aligned trailing vorticity. It also uses the full Newton method to solve the nonlinear equation.

Love et al. [13] used ASWING to model the aeroelastic effects on a swept flying wing SensorCraft. The aeroelastic analysis focused on body freedom flutter. A Nastran finite element model of the aircraft was used to provide an initial aeroelastic flutter analysis. Love explored tradeoffs with wing stiffness, altitude and center of gravity locations in order to better understand whether passive means can increase flutter speed to acceptable levels.

González [9] modeled the Unmanned Airplane for Ecological Conservation as a flexible-body using the ASWING code and compared it with results from an analyticalempirical method and potential flow codes. The goal was to evaluate the aerodynamic
and static stability of the aircraft. The results show that the flexible-body and rigid-body results show slight differences.

## II. 4 The Development of UM/NAST

Patil et al. [16] studied the aeroelasticity and flight dynamics of HALE aircraft. Their work showed that the behavior of HALE aircraft can vary dramatically due to the flexible nature of the wings. They also showed that modeling a HALE aircraft using a linear aeroelastic analysis in which the structure is assumed to be rigid can lead to significant errors. Furthermore, there is a significant difference between rigid body, linear aeroelastic and nonlinear aeroelastic dynamics when it comes to the short period and the phugoid modes of very flexible aircraft. The short period and phugoid modes were acquired by linearizing the nonlinear dynamics about a nonlinear equilibrium.

Cesnik and Brown [3] started the strain-based approach for modeling the dynamics of highly flexible aircraft. This method is solved in the time domain and was validated against the Goland wing [2]. Cesnik and Brown [3] modeled a HALE aircraft using a rigid fuselage and a highly flexible high-aspect-ratio composite wing. They analyzed the time-marching aeroelastic and aeroservoelastic behavior of HALE aircraft and cantilevered wings under constrained reference frame motion with imbedded actuation. They used the finite state two-dimensional strip theory developed by Peters et al. [19] for unsteady aerodynamics.

By adding a flexible fuselage and developing a split beam formulation, Cesnik and Su [5] continued the work of Cesnik and Brown. They emphasized roll performance and nonlinear-flutter during their study. Patil and Hodges [17], Su and Cesnik [31], and Patil and Taylor [18] all used 1-D beam modeling for slender structures to study the
nonlinear structural flight dynamics of a flying wing type aircraft. They also used the finite state two-dimensional strip theory developed by Peters et al. [19] for unsteady aerodynamics just as Cesnik and Brown did [3]. Su and Cesnik also studied how the wrinkling of the skin of a flying wing type aircraft affected its torsional stiffness. Wang et al. [37] used the unsteady vortex lattice method and the geometrically exact beam modeling method to study a flying wing type aircraft.

Palacios and Cesnik [15] developed nonlinear aeroelastic tools. Their highfidelity code used 3-D Euler equations to model the air flow. They used a split 1-D and 2-D model to model the 3-D structural deformation. The 1-D model follows traditional 1-D beam bending theory where the cross section of the beam remains undeformed. The 2-D model allows for changes in the cross section of the beam as the beam undergoes various internal and external loads. Palacios and Cesnik's high-fidelity code can only produce results for steady-state solutions because of the large computational size and the coupled structure of the CFD solution; the code is not suitable to run full aircraft simulations. Garcia [8] added to Palacios and Cesnik's code and created a nonlinear finite element model which includes the full Euler/Navier-Stokes solution. Garcia's results are significant because he showed that there are significant differences between the results of the linear and the nonlinear structural modeling of a swept cantilevered wing.

Shearer and Cesnik [22] developed a method for the characterization of the response of a very flexible aircraft that is used in the UM/NAST code. The geometrically nonlinear structural response of the aircraft was modeled using six-degree of freedom equations of motion. They used a low-order strain-based nonlinear structural analysis
method and an unsteady finite state potential-flow aerodynamics analysis method to formulate their aerodynamic model. Shearer and Cesnik used their modified Generalized- $\alpha$ Method for integrating the governing equations of a very flexible aircraft. Su and Cesnik [32] used the UM/NAST code to model the nonlinear aeroelasticity of a flapping wing Micro Air Vehicle (MAV), however, the code has not been validated by any experimental means at this time.

Shearer, Cesnik and their co-workers have begun the development of a very flexible RPV aircraft called X-HALE for this purpose. This aircraft has two configurations: the 6 meter and 8 meter span configurations. Cesnik et al. [4] have performed gust and roll simulations for the 8 meter model of X-HALE. Their results suggest that when a 1 -cosine gust is symmetrically applied to the 8 meter model X-HALE with a maximum gust speed of $4 \mathrm{~m} / \mathrm{s}$, while the nominal flight speed is $14 \mathrm{~m} / \mathrm{s}$ at 30 m altitude, the aircraft is stable. Also, when a single period of a left-wing-down sinusoidal aileron input is applied the aircraft is stable for aileron inputs with a 2 degree amplitude, but not for inputs with a 5 degree amplitude or greater.

## II. 5 RCAS

Saberi et al. [21] of the Aeroflightdynamics Directorate of the U.S. Army developed an integrated computational fluid and non-linear structural dynamics software system called RCAS for comprehensive rotorcraft analysis and simulation. The software uses computational fluid dynamics, rotorcraft comprehensive analysis and computational structural dynamics on parallel high performance computer systems. According to Strawn et al. [30], RCAS was validated with data taken from full-scale helicopters. The results of the validation showed that the computational fluid approach provides an
accurate model for the non-linear aerodynamics and dynamic forces experienced by a rotorcraft. No validation has been done using fixed-wing aircraft [4].

## II. 6 NATASHA

NATASHA is a software system that analyzes the nonlinear aerodynamics and nonlinear structural dynamics of HALE aircraft. NATASHA is based on geometrically exact, fully intrinsic beam equations. Sotoudeh and Hodges [26] updated NATASHA so that it is capable of analyzing joined-wing aircraft configurations. This was done using fully intrinsic equations and an incremental form of kinematical equations. This updated version of the NATASHA code was validated using a joined-wing structure. The program can also now provide trim and stability analyses. Sotoudeh and Hodges [27] also studied the effects of joint position and sweep angle of the aft wing of a joined-wing aircraft. Sotoudeh et al. [28] validated NATASHA with a range of results from well known solutions of beam stability and vibration problems, experimental data from scaled wind tunnel tests and results from RCAS. NATASHA uses 2-D aerodynamics and the finite state induced flow model of Peters and Johnson [19] to analyze the nonlinear aeroelastic characteristics of flying wings. Sotoudeh and Hodges have stated that they hope that NATASHA's results can be used as benchmarks for their own codes since the NATASHA model is limited in its capabilities.

## II. 7 Other Recent Work on Nonlinear Aeroelastic Solvers

Blair and Canfield [1] created a method for estimating the weight of a joined-wing HALE aircraft. Their method is based on the nonlinear static aeroelastic formulations and structural constraints of a given joined-wing HALE aircraft. It also incorporates the structures, aerodynamics and aeroelasticity of the aircraft. The static aerodynamics are
modeled using vortex lattice formulations. Recently, Richards, et al. [20] began designing a scaled joined-wing SensorCraft model for the purpose of validating an existing analytical nonlinear aeroelastic model which is based on the Matlab Aerospace Blockset and the Unmanned Dynamics Aerosim v1.2 Blockset. The simulator uses a set of first order terms and multi-dimensional lookup tables, which allow for the input of different angles of attack and sideslip angles, to model nonlinear aerodynamics. The simulator also uses vortex lattice software called AVL and a parametric model based on the software Phoenix Integration's Model Center Software (MC). The data is then outputted into a Matlab m-file. The model can very quickly produce a flight simulation using the flight simulator FlightGear for visualization. An optional aircraft autopilot was also integrated into the model using the Micropilot 2128 THWIL system.

Weishaar and Lee [38] studied how the weight and center of gravity of a high-aspect-ratio joined-wing HALE aircraft affect body-freedom flutter. Additionally, Tang et al. [33] used the finite state aerodynamic model to experimentally validate linear structural modeling when nonlinear trailing-edge flap deflections occur. Their results showed a strong correlation between their model and their experimental results; therefore, their results validated their model well. Tang and Dowell [34] experimentally validated an ONERA unsteady aerodynamic model using nonlinear structural modeling. Their results also validated their model well for cantilevered wings similar to HALE wings when the wings are exposed to limit-cycle oscillations. Dowell and Tang [7] also created a review of cantilevered structures with nonlinear aeroelasticity in which they discuss HALE aircraft.

## II. 8 Present Motivation and Problem

While all of the previous research discussed contributes to the problem of nonlinear aeroelasticity coupled with nonlinear flight dynamics, the problem is still not completely understood. Several codes have been developed for the use of modeling nonlinear aeroelastic and flight dynamics of an aircraft but none have been completely validated with real flight data from a fixed-wing aircraft [4]. This research will continue the work of Shearer, Cesnik and their co-workers and perform flight simulations with UM/NAST in order to make predictions about X-HALE's future test flights. This is all done with the hope of eventually experimentally validating the UM/NAST code with the X-HALE aircraft.

## III. Model Development

This research involved running various simulations with UM/NAST in order to predict the behavior of the X-HALE test vehicle. Initial simulations have been run by Shearer and are described in [23]. These initial simulations predicted that X-HALE will show instabilities in flight under certain conditions; further simulations need to be run in order to explore what other conditions will cause unstable flight. Also, more simulations are necessary in order to potentially validate the UM/NAST code. These simulations will include straight and level flight, and rolling flight performed by simulating aileron deflections.

## III. 1 The X-HALE Aircraft

Shearer, Cesnik and their co-workers have are developing a very flexible RPV aircraft called X-HALE, shown in Figure 5, at the University of Michigan in order to experimentally validate the UM/NAST code. X-HALE can be converted from a 6 meter test vehicle to an 8 meter test vehicle. This is done by removing two wing segments from the aircraft. During flight, X-HALE's middle elevator can rotate 90 degrees to become a vertical stabilizer. This will be done in order to observe the vertical stabilizer's effects on the aircraft's stability [25].


Figure 5. X-HALE: 6 Meter Model (Top) and 8 Meter Model (Bottom) [25]

This aircraft will collect data of its geometrically nonlinear aeroelastic response when it is test flown in the hope of validating the UM/NAST code. The aircraft has rigid and elastic body instabilities with large deflections during gusts. The airframe will be designed so that its elastic, inertial and geometric properties correlate well with its

UM/NAST model [4]. The aircraft can be configured either as a 6 m flight test vehicle (FTV) or an 8 m aeroelastic test vehicle (ATV) [25].

Both the 6 meter and the 8 meter models include five fuselages, which are each mounted to a joiner block that connects two wing modules. The wing modules are all 1 meter long. Each fuselage is composed of a fairing pod, a tail boom, and an elevon. Remote control aircraft propellers attach to the motors for propulsion. Each fairing pod has a carbon spine which holds an electric motor with two batteries and other components such as a GPS/INS, a GPS antenna, a transmitter, electronic speed controllers (ESC's), a glitch buster, a servo switch controller, an Ethernet hub and landing gear. The first battery powers the motor and the second powers the electronics contained in the fuselage. These electronics include a single board computer (SBC), an analog to digital converter module, and several scientific sensors such as strain gauges, accelerometers, a pitot probe and a tail potentiometer. These sensors vary in number and type depending on the wing module and the aircraft configuration [12].

The majority of the X-HALE flight components have been manufactured by the X-HALE program. Currently, the X-HALE program is integrating these components at the University of Michigan and is developing software for the networking of the onboard computers. Table 1 summarizes X-HALE's characteristics [12].

Table 1. X-HALE's Characteristics [12]

| Wing Span | 6 m or 8 m |
| :---: | :---: |
| Chord | 0.2 m |
| Planform Area | $1.2 \mathrm{~m}^{2}$ |
| Aspect Ratio | 30 or 40 |
| Length | 0.96 m |
| Propeller Diameter | 12 in |
| Gross Takeoff Weight | 11 kg or 12 kg |
| Power/Weight | $30 \mathrm{~W} / \mathrm{kg}$ |
| Airspeed | $12-18 \mathrm{~m} / \mathrm{s}$ |
| Max Range | 3 km |
| Endurance | 45 min |

## III. 2 The Coordinate Systems of UM/NAST

The UM/NAST controller was developed based on the known physics of the situation that is being modeled; that is, how a very flexible aircraft flies. The controller uses closed-loop reference tracking of a body fixed reference frame $B$ (Figure 6) at a point $O$ while also including the properties of nonlinear aeroelasticity. This point $O$ is typically is not the aircraft's center of mass but may be at some points in time during a simulation. The point $O$ is chosen to be at a convenient location on the aircraft so that both linear and angular velocities can be tracked. Usually, the x -axis is chosen to be out the right wing and the $y$-axis is tangent to the undeformed fuselage's longitudinal axis and extends in the direction of the front of the aircraft. As a result, the $x-y$ plane of the $B$ reference frame is parallel to the x-y plane of the inertial frame $G$ when the aircraft is undeformed. The $z$-axis extends out the top of the aircraft and is the cross product of the x -axis and y -axis. The flexible members of the aircraft are modeled as beams that propagate from the origin $O$ or that are rigidly offset from the point $O$. In order to determine the orientation of the $B$ reference frame, one of three methods is used: an Euler
angle transformation using three nonorthogonal Euler angles, a transformation using a four-parameter quaternion, or a transformation using a nine-parameter set of the unit vectors that define the $\mathrm{x}-, \mathrm{y}$ - and z -axes of the $B$ reference frame [23].


Figure 6. Body Fixed Reference Frame B [23]

Here $p_{B}$ is the inertial position of the $B$ reference frame. Also, $v_{B}$ and $\omega_{B}$ are the linear and angular velocity variables of the $B$ reference frame and can be represented by the vector shown in Equation (1.

$$
\beta=\left\{\begin{array}{l}
v_{B}  \tag{1}\\
\omega_{B}
\end{array}\right\}
$$

Figure 7 depicts the $B$ reference frame if the aircraft is assumed to be a rigid-body. For this case, the elastic members are modeled as beams that propagate from the $B$ reference
frame origin or with rigid offsets from the origin. The position vector $p_{r_{c m}}$ extends from the body-fixed $B$ reference frame to the center of mass of a rigid fuselage piece. Note that the origin $O$ of the $B$ reference frame is not the center of mass of the fuselage piece [23].


Figure 7. The Rigid-body Reference Frame [23]

During a simulation, the $B$ reference frame moves forward with the aircraft, allowing the movement of the aircraft to be modeled. This is done by deriving and integrating a set of first-order differential equations. These equations are of the form of Equation (2) below.

$$
\begin{equation*}
\dot{x}=f(x, u) \tag{2}
\end{equation*}
$$

These nonlinear differential equations are time-invariant and nonlinear. When the aircraft is assumed to be a rigid-body, the first-order equations take the form of Equation (3).

$$
\begin{gather*}
\dot{v}_{B}=f_{v_{B}}\left(v_{B}, \omega_{B}, \zeta, p_{B}, g_{0}, m, F_{\text {ext }}\right) \\
\dot{\omega}_{B}=f_{\omega_{B}}\left(\omega_{B}, I_{B}, \zeta, p_{B}, M_{e x t}\right) \\
\dot{\zeta}_{B}=f_{\zeta_{B}}\left(\omega_{B}, \zeta\right)  \tag{3}\\
\dot{p}_{B}=f_{p_{B}}\left(\zeta, v_{B}\right)
\end{gather*}
$$

The forces $F_{\text {ext }}$ and the moments $M_{\text {ext }}$ are state-dependent externally applied. Additionally, $I_{B}$ is the inertia matrix of the aircraft about the origin $O$ of the $B$ reference frame, $\zeta$ is the quaternion vector containing the four quaternion elements used to find the orientation of the $B$ reference frame with respect to the inertial reference frame $G$ and $g_{0}$ represents the gravitational field effects on the aircraft [23].

Figure 8 shows the $B$ reference frame and the coordinates of the flexible aircraft wing.


Figure 8. The Body Reference Frame B and the Vehicle Coordinates [23]

Here $w$ represents the local elastic reference frame, $p_{r}$ is the position of the $B$ reference frame origin to the local $w$ reference frame, $s$ represents the undeformed beam spatial dimension, $a$ represents an arbitrary point in the vehicle with respect to the origin of the inertial frame $G$ and $t$ represents time [23].

The position and the orientation vector $h$ at a point in the flexible body is given in Equation (4 below.

$$
h=\left\{\begin{array}{llll}
p^{T} & w_{x}^{T} & w_{y}^{T} & w_{z}^{T} \tag{4}
\end{array}\right\}^{T}
$$

The vector function $h$ is a function of only $\epsilon$, the column vector of the elastic strain state and $b$, displacements and rotations as time integral of $\beta$, the $B$ reference frame linear and angular velocities. Equation (5 gives expressions that relate $h$ to $\epsilon$ and $b$.

$$
\begin{align*}
& \delta h=J_{h \epsilon} \delta \epsilon+J_{h b} \delta b \\
& d h=J_{h \epsilon} \delta \epsilon+J_{h b} d b \tag{5}
\end{align*}
$$

In these equations, $\mathrm{J}_{\mathrm{h} \epsilon}$ and $\mathrm{J}_{\mathrm{hb}}$, which are given in Equation (6, are Jacobian matrices which link the flexible position and orientation vectors and the independent coordinates of $\epsilon$ and $\beta$.

$$
\begin{align*}
& J_{h \epsilon}=\frac{\partial h}{\partial \epsilon} \\
& J_{h b}=\frac{\partial h}{\partial b} \tag{6}
\end{align*}
$$

Equation (7 gives the value of $\dot{h}$, which further explains the connection between the vectors $\epsilon$ and $\beta$.

$$
\begin{equation*}
\dot{h}=J_{h \epsilon} \dot{\epsilon}+J_{h b} \dot{b}=J_{h \epsilon} \dot{\epsilon}+J_{h b} \beta \tag{7}
\end{equation*}
$$

The relative acceleration of $h$ due to the vectors $\epsilon$ and its first and second derivatives with respect to time is given in Equation (8 [23].

$$
\ddot{p}_{a}=\ddot{p}+x \ddot{w}_{x}+y \ddot{w}_{y}+z \ddot{w}_{z}=\left\{\begin{array}{l}
1  \tag{8}\\
x \\
y \\
z
\end{array}\right\}^{T}\left[\dot{J}_{h \epsilon} \dot{\epsilon}+J_{h \epsilon} \ddot{\epsilon}\right]
$$

## III. 3 A Study of the Governing Differential Equations of Motion

By assuming that an aircraft is a rigid body when creating a controller, three things are assumed:

1. The inertia properties of the aircraft are either constant or time-varying.
2. The inertial force caused by a rotating coordinate frame in conjunction with the relative velocity of the aircraft's flexible members can be neglected.
3. Any external forces, such as $F_{\text {ext }}$ and $M_{\text {ext }}$, or moments are founded on a constant aircraft geometry.

These assumptions are invalid for vey flexible aircraft because of the changing geometry of the aircraft. Instead, for a flexible aircraft a set of differential equations of motion that allow for changing aircraft geometry are used. These equations are shown in Equation (9) and Equation (10).

$$
\begin{gather*}
M \ddot{q}+C \dot{q}+K q=R(q, \dot{q}, \lambda)  \tag{9}\\
q=\left\{\begin{array}{c}
\epsilon \\
p_{B} \\
\Theta_{B}
\end{array}\right\} \quad \dot{q}=\left\{\begin{array}{c}
\dot{\epsilon} \\
v_{B} \\
\omega_{B}
\end{array}\right\} \quad \ddot{q}=\left\{\begin{array}{c}
\ddot{\epsilon} \\
\dot{v}_{B} \\
\dot{\omega}_{B}
\end{array}\right\} \tag{10}
\end{gather*}
$$

In these equations, $M$ represents the mass properties of the aircraft and $C$ represents the structural damping and the nonlinear terms created by a rotating coordinate frame and its effects on relative position and velocity, such as $v_{B}$ and $\omega_{B}$. Additionally, $K$ represents the stiffness matrix of the aircraft, and $q$ represents a set of coordinates which contain both strain $\epsilon$, which is linked with the inertial position $p_{B}$, and an orientation vector $\Theta_{B}$. The function $R(q, \dot{q}, \lambda)$ represents forces, such as aerodynamic forces, that are a function
of finite state flow velocities $\lambda$. This function is further described in [19]. Because the variables $M, C$ and $R$ are dependent on each other, the rigid-body and flexible structural dynamics are also dependent on each other. The program UM/NAST uses a constant strain-based approach to predict the movement of the aircraft. This approach, which is further described in [2, 3], allows for nonlinear geometric changes and changes to the inertia matrix $I_{B}$, and the matrices $M, C$ and $R[23]$.

## III.3.1 The Equations of Motion

The equations of motion are further derived from Equation (9) and Equation (10) using unsteady aeroelastic modeling. This is done by applying the principle of virtual work to the $B$ reference frame while assuming the aircraft wings are flexible beams and the body of the aircraft is composed of rigid bodies. Equation (11 below is the total virtual work expression based on both the $B$ reference frame, and the flexible beams and the rigid bodies of the aircraft.

$$
\begin{align*}
& \delta W=\left[\begin{array}{ll}
\delta \epsilon^{T} & \delta b^{T}
\end{array}\right]^{T}\left(-\left[\begin{array}{ll}
M_{F F} & M_{F B} \\
M_{B F} & M_{B B}
\end{array}\right]\left[\begin{array}{c}
\ddot{\epsilon} \\
\dot{\beta}
\end{array}\right]-\left[\begin{array}{cc}
C_{F F} & C_{F B} \\
C_{B F} & C_{B B}
\end{array}\right]\left[\begin{array}{l}
\dot{\epsilon} \\
\beta
\end{array}\right]\right. \\
&\left.-\left[\begin{array}{ll}
K_{F F} & K_{F B} \\
K_{B F} & K_{B B}
\end{array}\right]\left[\begin{array}{l}
\epsilon \\
b
\end{array}\right]+R\right) \tag{11}
\end{align*}
$$

In this equation, $R$ is the vector described below in Equation (12) where $R_{F}$ is the force vector component pertaining to the flexible body degree of freedom and $R_{B}$ is the force vector component pertaining to the fixed-body degree of freedom.

$$
R=\left\{\begin{array}{l}
R_{F}  \tag{12}\\
R_{B}
\end{array}\right\}
$$

Equation (13) provides the mass and damping matrices that apply to Equation (11 [23].

$$
\begin{gather*}
\mathrm{M}_{\mathrm{FF}}=\mathrm{J}_{\mathrm{h} \epsilon}^{\mathrm{T}} \mathrm{M}_{\mathrm{G}} \mathrm{~J}_{\mathrm{h} \epsilon} \\
\mathrm{M}_{\mathrm{FB}}=\mathrm{J}_{\mathrm{h} \epsilon}^{\mathrm{T}} \mathrm{M}_{\mathrm{G}} \mathrm{~J}_{\mathrm{hb}} \\
\mathrm{M}_{\mathrm{BF}}=\mathrm{J}_{\mathrm{hb}}^{\mathrm{T}} \mathrm{M}_{\mathrm{G}} \mathrm{~J}_{\mathrm{h} \epsilon} \\
\mathrm{M}_{\mathrm{BB}}=\mathrm{J}_{\mathrm{hb}}^{\mathrm{T}} \mathrm{M}_{\mathrm{G}} \mathrm{~J}_{\mathrm{hb}}+M_{\mathrm{B}} \\
\mathrm{C}_{\mathrm{FF}}=\mathrm{J}_{\mathrm{h} \epsilon}^{\mathrm{T}} \mathrm{M}_{\mathrm{G}} \dot{\mathrm{~J}}_{\mathrm{h} \epsilon}+\mathrm{C}_{\mathrm{G}} \\
\mathrm{C}_{\mathrm{FB}}=\mathrm{J}_{\mathrm{he}}^{\mathrm{T}} \mathrm{M}_{\mathrm{G}} \mathrm{H}_{\mathrm{hb}}+2 \mathrm{~J}_{\mathrm{h} \epsilon}^{\mathrm{T}} \mathrm{M}_{\mathrm{G}} \mathrm{H}_{\mathrm{h} \dot{\mathrm{e}}} \mathrm{~b}  \tag{13}\\
\mathrm{C}_{\mathrm{BF}}=\mathrm{J}_{\mathrm{hb}}^{\mathrm{T}} \mathrm{M}_{\mathrm{G}} \dot{\mathrm{~J}}_{\mathrm{h} \epsilon} \\
\mathrm{C}_{\mathrm{BB}}=\mathrm{J}_{\mathrm{hb}}^{\mathrm{T}} \mathrm{M}_{\mathrm{G}} \mathrm{H}_{\mathrm{hb}}+2 \mathrm{~J}_{\mathrm{hb}}^{\mathrm{T}} \mathrm{M}_{\mathrm{G}} \mathrm{H}_{\mathrm{h} \dot{\beta} \dot{\beta}}+\mathrm{C}_{\mathrm{B}} \\
\mathrm{~K}_{\mathrm{FF}}=\mathrm{K}_{\mathrm{G}} \\
\mathrm{~K}_{\mathrm{FB}}=\mathrm{K}_{\mathrm{BF}}=\mathrm{K}_{\mathrm{BB}}=0
\end{gather*}
$$

Here $\mathrm{M}_{\mathrm{G}}, \mathrm{C}_{\mathrm{G}}$ and $\mathrm{K}_{\mathrm{G}}$ are the generalized flexible-element mass, damping and stiffness matrices about the $G$ reference frame, while $M_{\mathrm{B}}$ and $\mathrm{C}_{\mathrm{B}}$ are the generalized rigid-element mass and damping matrices associated with the $B$ reference frame rigidelement portion. Also, $\mathrm{H}_{\mathrm{hb}}$ and $\mathrm{H}_{\mathrm{h} \dot{\mathrm{\epsilon}} \boldsymbol{\beta}}$ incorporate the effects of a rotating coordinate frame. $\mathrm{M}_{\mathrm{G}}, \mathrm{C}_{\mathrm{G}}$ and $\mathrm{K}_{\mathrm{G}}$ are the assembled flexible-element generalized mass, damping and stiffness matrices. They are of the form of Equation (14.

$$
\begin{align*}
\mathrm{M}_{\mathrm{G}} & =\left[\begin{array}{cccc}
M_{(1)} & 0 & \cdots & 0 \\
0 & M_{(2)} & \cdots & 0 \\
0 & 0 & \ddots & 0 \\
0 & 0 & \cdots & M_{(e)}
\end{array}\right] \\
\mathrm{C}_{\mathrm{G}} & =\left[\begin{array}{cccc}
C_{(1)} & 0 & \cdots & 0 \\
0 & C_{(2)} & \cdots & 0 \\
0 & 0 & \ddots & 0 \\
0 & 0 & \cdots & C_{(e)}
\end{array}\right] \tag{14}
\end{align*}
$$

$M_{B}$ and $C_{B}$ are the mass and damping matrices associated with the $B$ reference frame element portion. They are given in Equation (15).

$$
\begin{gather*}
M_{B}=\left[\begin{array}{cc}
m & m \tilde{\tilde{p}}_{r_{c m}} \\
m \tilde{p}_{r_{c m}} & I_{B}
\end{array}\right] \\
C_{B}=\left[\begin{array}{cc}
m \widetilde{\omega}_{B} & m \widetilde{\omega}_{B} \tilde{\tilde{p}}_{c m} \\
m \tilde{p}_{r_{c m}} \widetilde{\omega}_{B} & \widetilde{\omega}_{B} I_{B}
\end{array}\right] \tag{15}
\end{gather*}
$$

Here $m$ represents mass per unit span and $p_{r_{c m}}$ represents the position vector from the $B$ reference frame origin to the center of mass. Additionally, $(\because)$ is a skew-symmetric matrix operator on the given matrix and $(\tilde{\sim})$ is the transpose of the given matrix's skewsymmetric matrix [23].

Equation (16 below can be derived from Equation (11, the total virtual work expression and the principle of virtual work.

$$
\left[\begin{array}{ll}
M_{F F} & M_{F B}  \tag{16}\\
M_{B F} & M_{B B}
\end{array}\right]\left[\begin{array}{c}
\ddot{\ddot{c}} \\
\dot{\beta}
\end{array}\right]+\left[\begin{array}{ll}
C_{F F} & C_{F B} \\
C_{B F} & C_{B B}
\end{array}\right]\left[\begin{array}{c}
\dot{\epsilon} \\
\beta
\end{array}\right]+\left[\begin{array}{ll}
K_{F F} & K_{F B} \\
K_{B F} & K_{B B}
\end{array}\right]\left[\begin{array}{l}
\epsilon \\
b
\end{array}\right]=\left\{\begin{array}{l}
R_{F} \\
R_{B}
\end{array}\right\}
$$

This equation comprises the set of elastic equations of motion and could be written in the form of Equation (9) where the mass matrix is a function of strain, $M=f_{M}(\epsilon)$, the damping matrix is a function of strain, strain rate and the $B$ reference frame velocity, $C=f_{C}(\epsilon, \dot{\epsilon}, \beta)$, the stiffness matrix $K$ is constant and $R$ contains all other nonlinearities. Equation (17 provides the expanded form of Equation (16 and the complete set of governing differential equations.

$$
\begin{gather*}
M_{F F} \ddot{\epsilon}=-M_{F B} \dot{\beta}-C_{F F} \dot{\epsilon}-C_{F B} \beta-K_{F F} \epsilon+R_{F} \\
M_{B B} \dot{\beta}=-M_{B F} \ddot{\epsilon}-C_{B B} \beta-C_{B F} \dot{\epsilon}+R_{B} \\
\dot{\zeta}=-\frac{1}{2} \bar{\Omega}_{\zeta} \zeta  \tag{17}\\
\dot{p}_{B}=\left[\begin{array}{ll}
C^{B G} & 0
\end{array}\right] \beta \\
\dot{\lambda}=F_{1} \ddot{q}+F_{2} \dot{q}+F_{3} \lambda
\end{gather*}
$$

Here $\zeta$ is a vector of four quaternion parameters used to determine the orientation of the $B$ reference frame, $\bar{\Omega}_{\zeta}$ is the finite element discretization of the $\omega_{B}$ matrix, $\dot{p}_{B}$ is the time rate of change of the inertial position vector of the $B$ reference frame, $C^{B G}$ is a transformation matrix between the $B$ reference frame and the inertial $G$ reference frame, and $\lambda$ is a set of unsteady aerodynamic inflow velocities. $F_{1}, F_{2}$ and $F_{3}$ are differential equation matrices associated with $\lambda$ [23].

## III.3.2 A Retrieval of the Rigid-Body Equations of Motion

It is valuable to identify that the standard rigid-body equations of motion for an aircraft can be retrieved from the total virtual work expression, Equation (11, by holding the elastic degrees of freedom constant. This results in the expression for $R$ in Equation (18).

$$
\begin{align*}
R=\left\{\begin{array}{l}
R_{F} \\
R_{B}
\end{array}\right\}= & {\left[\begin{array}{l}
K_{F F} \\
K_{B F}
\end{array}\right] \epsilon_{\text {initial }}+\left[\begin{array}{c}
B_{g F} \\
B_{g B}
\end{array}\right] g^{B}+\left[\begin{array}{l}
B_{d s t_{F}}^{F} \\
B_{d s t_{B}}^{F}
\end{array}\right] F^{d s t}+\left[\begin{array}{l}
B_{d s t_{F}}^{M} \\
B_{d s t_{B}}^{M}
\end{array}\right] M^{d s t} }  \tag{18}\\
& +\left[\begin{array}{c}
B_{p t_{F}}^{F} \\
B_{p t_{B}}^{F}
\end{array}\right] F^{p t}+\left[\begin{array}{c}
B_{p t_{F}}^{M} \\
B_{p t_{B}}^{M}
\end{array}\right] M^{p t}
\end{align*}
$$

In this equation, $\epsilon_{\text {initial }}$ is the initial strain vector and $g^{B}$ is the body-fixed reference frame $B$ resolved gravity vector. Also, $F^{d s t}, M^{d s t}, F^{p t}$ and $M^{p t}$ are the body-resolved
distributed and point forces and moments. $F^{\text {aero }}$ and $M^{\text {aero }}$ are functions of control surface inputs $u$ and are included in $F^{d s t}$ and $M^{d s t}$. Any propulsion related forces such as propeller forces or motor forces are modeled as if they were evenly distributed along the vehicle and are included in $F^{p t}$ and $M^{p t}$. The values for the influence matrices are explained further in [2] and are given in Equation (19).

$$
\begin{align*}
B_{d s t_{F}}^{F} & =J_{p \epsilon}^{T} B_{F} \\
B_{d s t_{B}}^{F} & =J_{p \beta}^{T} B_{F} \\
B_{d s t_{F}}^{M} & =J_{\theta \epsilon}^{T} B_{M} \\
B_{d s t_{B}}^{M} & =J_{\theta \beta}^{T} B_{M}  \tag{19}\\
B_{p_{F}}^{F} & =J_{p \epsilon}^{T} \\
B_{p_{B}}^{F} & =J_{p \beta}^{T} \\
B_{p_{F}}^{M} & =J_{\theta \epsilon}^{T} \\
B_{p_{B}}^{M} & =J_{\theta \beta}^{T}
\end{align*}
$$

Here $B_{F}$ and $B_{M}$ are constant matrices characterized by an elastic element's undeformed mass [23]. If $\epsilon_{\text {initial }}$ and $M^{p t}$ are assumed to be zero, and the finite strain formulation given in [19] for any aerodynamic forces and moments is assumed to be linear in the discrete trailing edge surface deflections, Equation (18) can be simplified to Equation (20) [3].

$$
\begin{align*}
R=\left[B_{g}\right] g^{B}+ & B_{d s t}^{F} F^{\text {aero }}+\left[B_{d s t}^{M}\right] M^{\text {aero }}+\left[B_{d s t}^{M}\right] \frac{\delta F^{\text {aero }}}{\delta u_{\text {flap }}} u_{\text {flap }}  \tag{20}\\
& +\left[B_{p}^{F}\right] u_{\text {thrust }}
\end{align*}
$$

## III. 4 Numerical Integration and the Trim Solution

For both the zero thrust and the thrust required for $1-\mathrm{g}$ level flight cases, trimming is performed in UM/NAST and is based upon techniques described in [23]. A cost function given in Equation (21 is used.

$$
\begin{equation*}
J_{\text {trim }}=f^{T} \cdot f \tag{21}
\end{equation*}
$$

Equation (22 gives the zero thrust or gliding cases value for $f$, the vector used to trim the aircraft.

$$
\begin{equation*}
f=\{\text { pitching moment about the origin of the } B \text { frame lift weight }\} \tag{22}
\end{equation*}
$$

Equation ( 23 gives the thrust required for $1-\mathrm{g}$ level flight case value for $f$. Here the longitudinal $B$ reference frame linear and angular accelerations are used for $f$.

$$
f=\left\{\begin{array}{c}
\dot{v}_{B_{y}}  \tag{23}\\
\dot{v}_{B_{z}} \\
\dot{v}_{x}
\end{array}\right\}
$$

UM/NAST minimizes the cost function $J$ over the solution space using the elevator deflection angle $\delta_{e}$, the body angle of attack $\alpha$ and the thrust $\delta_{t}$. The local minimum of the search variable is discovered using a basic numerical Newton-Raphson method, which is given in Equation (24.

$$
\begin{equation*}
\Delta S_{k}=-{\frac{\delta f^{-1}}{\delta S_{k}}}_{k} f_{k} \tag{24}
\end{equation*}
$$

Here $S_{k}$ is given in Equation (25.

$$
S_{k}=\left\{\begin{array}{l}
\delta_{e}  \tag{25}\\
\alpha \\
\delta_{t}
\end{array}\right\}_{k}
$$

The search variable $S_{k}$ is recomputed using Equation (26.

$$
\begin{equation*}
S_{k+1}=S_{k}+\Delta S \tag{26}
\end{equation*}
$$

Furthermore, $f_{k+1}$ and

$$
\left[\frac{\partial f}{\partial S}\right]_{k+1}^{-1}
$$

are recomputed at each iteration using $S_{k+1}$. This minimization process continues until a desired tolerance is met. Divergence of the solution is avoided by checking $S_{k+1}$ at each iteration step and is limited to prescribed bounds. Equation (27 provides the Jacobian matrix which is computed numerically through finite differences.

$$
\begin{equation*}
J_{t r i m}=\frac{\delta f}{\delta S} \tag{27}
\end{equation*}
$$

Figure 9 outlines this entire trimming solution procedure [23].


Figure 9. Trim Solution Flow Chart [23]

## III. 5 Solution of the Governing Equations of Motion

A high-frequency dissipative time-stepping approach is used to solve the governing nonlinear differential equations given in Equation (17. This involves a modified Newark method, which is further described in [23]. The modified Newark method was selected because it can integrate large systems of equations, including ones
with repeated eigenvalues, its ease of use with the equations of motion used, and means by which its first-order and second-order methods were derived [10].

UM/NAST can produce three different types of solutions: a reduced order solution, a linear solution and a nonlinear solution. For a reduced order solution, all elastic degrees of freedom are removed once the vehicle flexes into a steady-state deflection. For this type of simulation the inertia matrices is fixed but the Jacobian matrices change at each subiteration. For a linear solution, the elastic degrees of freedom remain intact and the inertia matrices change at each subiteration, but the Jacobian matrices obtained from the steady-state solution that UM/NAST computes at the beginning of each simulation are used; therefore, they are fixed. For a nonlinear solution, the elastic degrees of freedom remain intact, the inertia matrices change at each subiteration and the Jacobian matrices are updated at each subiteration, resulting in a full time-marching simulation based on Equation (17.

A few issues with UMNAST should be noted: UM/NAST begins a simulation by first going through a routine that determines the steady-state solution. It then continues into a time-marching simulation. The code is also sensitive to the time step selected, how long the simulation is run for and how big the tolerance for the $R$, or the residual, value is. Additionally, the predictor-corrector method used to find the $S$ values can create a problem where certain matrices have values that are very large or very small, making it difficult to invert these matrices. The simulation may fail before it is complete because the values selected are inappropriate. In general, smaller time steps work better, but often a smaller time step means the simulation may take longer to finish. A time step that is too large can also cause the simulation to take a longer amount of time to finish. Also, a
larger residual value tolerance helps the simulation to finish sooner, although a residual value that is too large may cause the simulation to diverge from the actual solution. The longer the simulation time, the more difficult it is for the simulation to complete without issues. If these values are selected properly, a complete simulation can be accomplished. The ease at which a simulation will complete depends on the simulation type selected; the reduced-order type simulation is the least sensitive to selected values and is the most likely to complete, while the linear type is less likely to complete and the nonlinear type is the least likely to complete because it is the least sensitive to the selected values.

## IV. Results

## IV. 1 The Assumptions Made

This research performed a set of simulations using the UM/NAST code to predict the flight behavior of the 6 meter and 8 meter models of X-HALE. The UM/NAST code was provided by Shearer, Cesnik and their co-workers. In order to model the X-HALE aircraft using UM/NAST, several assumptions were made. These assumptions involve how X-HALE is modeled in the UM/NAST code. For example, the NACA 4415 airfoil used for the main wing segments in these simulations is not identical to the EMX-07 airfoil used for the physical X-HALE aircraft, but it is similar enough to the EMX-07 airfoil for the purposes of this research because it has similar lifting and moment characteristics. The NACA 0012 airfoil used to model the tail elevons is the actual airfoil used on the physical X-HALE. The fairing pods are modeled with a NACA 0018 airfoil. The fairings are also modeled with applied follower concentrated forces to simulate motor thrust.

Each motor is simulated with a constant force. The tails are modeled as allmovable horizontal surfaces. All booms, tails and fairings are modeled as rigid members with inertias placed at points best suitable to model the two physical X-HALE aircrafts. Furthermore, the outer 1 meter long members are modeled with a dihedral of 10 degrees just like the physical X-HALE aircrafts. The ailerons are modeled on the outer dihedral members and occupy $25 \%$ of the chord also just like the physical X-HALE aircrafts. The inertias of the spine and the pod covers are neglected and instead the concentrated inertias are placed inside the pods. This is done primarily to model the electronic equipment inside the pods. The masses of aircraft models are programmed to be the estimated
completed 6 meter and 8 meter X-HALE weights. Figure 10 illustrates the UM/NAST model of the 8 meter X-HALE [4].

The actual X-HALE aircraft has a center tail and elevon, as seen in Figure 5. The UM/NAST model does not include a center tail and elevon, as seen in Figure 10. However, because the tail is in the center and it is a symmetric airfoil, its absence is unlikely to make a difference in the results of the simulations. Also, the actual X-HALE can flip the center tail 90 degrees so that it becomes a vertical stabilizer. However, this is not done in any of the simulations performed for this research.


Figure 10. UM/NAST Model of the 8 Meter X-HALE Aircraft [4]

The X-HALE aircraft is trimmed for equal lift and weight, and also for a zero pitching moment about its center of gravity at level flight at 30 meters altitude. The normal flight velocity for the aircraft ranges from 12 to $20 \mathrm{~m} / \mathrm{s}$. Figure 11 shows the deformed shape at the trimmed condition for the 8 meter X-HALE model. The 8 meter X-HALE trims at $14 \mathrm{~m} / \mathrm{s}$ and its tip deflection is about $37 \%$ its half span [4]. The XHALE aircraft's starting speed is its trim speed, the flights are assumed to be gust free and the starting altitude is assumed to be 30 meters above sea level.


Figure 11. Deformed Shape at the Trim Condition for the 8 Meter X-HALE [4]

## IV. 2 Running the Simulations and Initial Complications

This research was performed by altering pre-existing input files for the UM/NAST code in order to meet the specified simulation parameters. Initial complications arose when completing the simulations because the code is sensitive to the simulation type selected (the reduced-order, linear or nonlinear cases), the time step selected, how long the simulation flight is and how big the tolerance for the $R$ (the residual) value is. Many simulations failed before they completed because the values selected were inappropriate and calculations became very difficult for the computer to perform.

This research ran two types of simulations: the linear and nonlinear solution types. Initially the simulations were set for the 6 meter aircraft and a 15 second flight time involving constant thrust flight with no other inputs such as an aileron or control surface input. However, problems occurred completing the simulation after approximately the 9.6 second point, no matter what time step or maximum residual value was selected. After repeatedly failing simulations, a linear type simulation with a time
step of 0.0025 seconds and a maximum residual value of 0.1 completed. The simulation took approximately a week to complete using 64-bit Matlab on a dual core 2.6 GHz personal computer. The results of this simulation revealed why the simulations struggled to complete after approximately 9.6 seconds: the flight of the 6 meter X-HALE model had become highly unstable at that point in time as seen in Figure 12. No nonlinear type simulation attempted for the 6 meter X-HALE would run to completion after approximately the 9.7 second mark because all of these simulations resulted in unstable flight. This will be further discussed in Section IV.4.1.


Figure 12. Case 1 Longitudinal Velocity $v_{y}$ versus Time
The simulation flight time was shortened to 10 seconds in order to ensure the 6 meter X-HALE simulations completed. Several more 6 meter X-HALE simulations were run until a nonlinear simulation involving constant thrust flight with no other inputs, such as an aileron or control surface input, completed a 10 second flight with a time step of
0.0001 seconds and a maximum residual value of 10 . All other 6 meter X-HALE simulations and several 8 meter X-HALE simulations were run using this time step and maximum residual value from this point on so that all the simulations run from this point onward would have this time step and maximum residual value in common. Next one linear type simulation involving constant thrust flight with no other inputs was run for the 6 meter X-HALE. After that three linear type simulations involving sinusoidal aileron inputs on both wings were run for the 6 meter X-HALE.

Next the 8 meter X-HALE simulations were run. First, four 8 meter X-HALE model linear type simulations with a 10 second flight time and sinusoidal aileron inputs on both wings were run. Each 10 second flight time simulation took anywhere from three to five days to complete using 64-bit Matlab on a dual core 2.6 GHz personal computer. These simulations had the same time step ( 0.0001 seconds) and maximum residual value (10) as the 6 meter X-HALE simulations. They ran much smoother than the 6 meter XHALE simulations because the aircraft did not become extremely unstable by the end of the 10 second runs. However, these 10 second simulations did not provide enough data in order to find what sinusoidal aileron inputs on both wings would make the aircraft unstable, so thirteen more simulations were run for the 8 meter X-HALE using a 0.001 second time step, a maximum residual value of 10 and a time duration of 15 seconds. Therefore, the 10 second 8 meter X-HALE simulations are not discussed in this research because the 15 second simulations provide all of the data needed. The time step was then increased by an order of magnitude for the latter simulations in order to get the simulations to run faster. Two of the 15 second simulations failed because the
amplitudes of the sinusoidal aileron inputs applied to both wings were too large (20 and 25degrees) and caused the aircraft to become unstable.

In general, smaller time steps worked better for the simulations, but often a smaller time step meant the simulation took longer to finish. Also, a larger maximum residual value helped the simulation to finish sooner. However, a maximum residual value that is too large could cause a simulation to diverge from the actual solution. The ease at which a simulation would complete also depended on the simulation type selected; the nonlinear type simulation was more likely to fail than the linear type simulation was. This research first aimed for a time step of 0.05 seconds and a maximum residual value of 0.1 for the 6 meter X-HALE simulations, but these values were changed since the simulations would fail before finishing a 10 second flight with these values. A time step of 0.0001 and a maximum residual value of 10 were used in order to ensure a nonlinear type 6 meter simulation finished the 10 second flight. However, a time step this small caused the simulations to take approximately 3 to 5 days to complete a 6 meter X-HALE simulation, which was much longer than initially anticipated.

In comparison, the 8 meter X-HALE simulations run with a 15 second time duration and a time step of 0.001 seconds each took approximately 7 to 10 hours to complete. These were a mix of linear and nonlinear type simulations. The time step and time duration were changed for these additional 8 meter model X-HALE simulations to allow the simulations to provide more data since the flight was longer but also so that the simulation could run faster. A 10 second 8 meter X-HALE simulation with a time step of 0.0001 seconds took approximately ten times longer than a 10 second simulation with a
time step 0.001 since this large time step still allowed the simulation to run quite smoothly.

## IV. 3 The Chosen Simulations

The 6 meter model of the aircraft was based off the pre-existing input file 6_meter_baseline_case0.nin which uses a NACA 4415 airfoil. The 8 meter model of the aircraft was based off the pre-existing input file 8_meter_ailerons_case0.nin, which also uses a NACA 4415 airfoil. Examples of these input files can be found in Appendix B and Appendix C. Of all the simulations run, seventeen were chosen to be discussed in detail in this research. The first six simulations, Cases 1 through 6, were simulations for the 6 meter model of X-HALE. The first simulation, Case 1 , used a 0.0025 second time step, a maximum residual value of 0.1 and a 15 second time duration. It had no inputs, such as an aileron or control surface input, and had a constant thrust. This was a linear type simulation. The rest of the 6 meter X-HALE simulations used a 0.0001 time step, a maximum residual value of 10 and a 10 second time duration. Except for one nonlinear type simulation, they were all linear type simulations which either used no inputs or they had sinusoidal aileron inputs on both wings. The 8 meter X-HALE simulations had a time duration of 15 seconds, a time step of 0.001 seconds and a maximum residual value of 10. These all had sinusoidal aileron inputs on both wings. These were part linear type and part nonlinear type simulations.

Each of the simulations that used a sinusoidal aileron input on both wings were given an aileron input with a period of 5 seconds on both the left and right ailerons. The input started at 0.1 seconds and finished after 10 seconds. The inputs had amplitudes of $2,5,10,15,20$ or 25 degrees. The aileron input completes approximately two periods
before terminating. An example of a sinusoidal aileron input can be seen in Figure 13. A summary of the simulations discussed in this research is provided in Table 2.


Figure 13. Case 6 Aileron Input versus Time

Table 2. A Summary of Discussed Simulations

| Case | Simulation Type | Input | Duration (sec) | Time Step (sec) | MaxResidualValue | Sinusoidal Aileron Input Data |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  | Period (sec) | Start/ <br> End <br> Time <br> (sec) | Amplitude (deg) |
| 1 | 6 Meter Linear | None | 15 | 0.0025 | 0.1 | N/A | N/A | N/A |
| 2 | 6 Meter Linear | None | 10 | 0.0001 | 10 | N/A | N/A | N/A |
| 3 | 6 Meter Nonlinear | None | 10 | 0.0001 | 10 | N/A | N/A | N/A |
| 4 | 6 Meter Linear | Aileron | 10 | 0.0001 | 10 | 5 | 0.1/10 | 2 |
| 5 | 6 Meter Linear | Aileron | 10 | 0.0001 | 10 | 5 | 0.1/10 | 5 |
| 6 | 6 Meter Linear | Aileron | 10 | 0.0001 | 10 | 5 | 0.1/10 | 10 |
| 7 | 8 Meter Linear | None | 15 | 0.001 | 10 | N/A | N/A | N/A |
| 8 | 8 Meter Linear | Aileron | 15 | 0.001 | 10 | 5 | 0.1/10 | 2 |
| 9 | 8 Meter Nonlinear | Aileron | 15 | 0.001 | 10 | 5 | 0.1/10 | 2 |
| 10 | 8 Meter Linear | Aileron | 15 | 0.001 | 10 | 5 | 0.1/10 | 5 |
| 11 | 8 Meter Nonlinear | Aileron | 15 | 0.001 | 10 | 5 | 0.1/10 | 5 |
| 12 | 8 Meter Linear | Aileron | 15 | 0.001 | 10 | 5 | 0.1/10 | 10 |
| 13 | 8 Meter Nonlinear | Aileron | 15 | 0.001 | 10 | 5 | 0.1/10 | 10 |
| 14 | 8 Meter Linear | Aileron | 15 | 0.001 | 10 | 5 | 0.1/10 | 15 |
| 15 | 8 Meter <br> Nonlinear | Aileron | 15 | 0.001 | 10 | 5 | 0.1/10 | 15 |
| 16 | 8 Meter Linear | Aileron | 15 | 0.001 | 10 | 5 | 0.1/10 | 20 |
| 17 | 8 Meter Linear | Aileron | 15 | 0.001 | 10 | 5 | 0.1/10 | 25 |

This research was performed to predict the in flight behavior of both the 6 meter model and the 8 meter models of X-HALE. The two baseline 6 meter model simulations performed with no inputs were performed using the linear and nonlinear simulation types. This was done in order to compare the linear and nonlinear simulation types and to gain knowledge of their differences. This was also done in order to see how well the 6 meter X-HALE model can fly straight and level. The three sinusoidal aileron input linear type simulations were performed for the 6 meter model in order further understand the aircraft's response to an aileron input. Only the linear type solution was used in order to better compare the simulations performed while also minimizing the time it took to compute the solutions. The one 8 meter model linear type simulation was run with no inputs in order to form an understanding of how well the 8 meter aircraft can fly straight and level. Finally, the ten 8 meter model sinusoidal aileron input simulations were performed in order to understand aircraft's response to an aileron input on both wings. These simulations were a mix of linear and nonlinear type simulations so that the two simulation types could be compared.

Again, for a linear solution, the elastic degrees of freedom remain intact and the inertia matrices change at each subiteration, but the Jacobian matrices obtained from the steady-state solution computed at the beginning of each simulation are used; therefore, they are fixed. For a nonlinear solution, the elastic degrees of freedom remain intact, the inertia matrices change at each subiteration and the Jacobian matrices are updated at each subiteration, resulting in a full time-marching simulation based on Equation (17.

While the Case 1 simulation has a different time step ( 0.0025 seconds) and maximum residual value (0.1) than the other 6 meter X-HALE simulations, it is included
in the data because it is the only 6 meter X-HALE simulation that runs for 15 seconds; the other simulations only run for 10 seconds. For the rest of the 6 meter X-HALE simulations the time step, maximum residual value, and time duration were chosen based on the limitations of the UM/NAST code and the simulation parameters, as mentioned in Section IV.1. The time step for these simulations, 0.0001 seconds, was the largest time step that actually allowed a 6 meter X-HALE nonlinear type simulation to complete a 10 second run. The residual value tolerance of 10 was chosen because a value smaller than that would cause a simulation to take significantly longer to finish but a value larger than would potentially cause a nonlinear simulation to fail. The time duration of 10 seconds was chosen because after approximately the 9.6 second point, a simulation would struggle to finish, so this time duration value was chosen to make sure simulations could finish. For the 8 meter X-HALE simulations, the time step was changed to 0.001 and the time duration was changed to 15 seconds in order to allow for a longer flight but also so that the simulations could finish more quickly.

For simulations that involved a sinusoidal aileron input on both wings, the period of the input, 5 seconds, and the start and stop time of the input, 0.1 seconds and 10 seconds, were chosen because this periodic input would be similar to the kind of aileron input X-HALE would normally receive in flight. Several different sinusoidal aileron input amplitudes were used: $2,5,10,15,20$ and 25 degrees. These values were chosen in order to find the maximum aileron input amplitude that could be used without the aircraft's flight becoming unstable. These values were also chosen based on the results of Cesnik et al. [4] who, when performing UM/NAST simulations for the 8 -meter X -

HALE, discovered that a left aileron input (a rolling maneuver) resulted in unstable flight when a sinusoidal input of 5 degrees or more was used.

## IV. 4 The Completed Simulations and Their Results

The results of all seventeen chosen simulations are discussed in detail in this section of the research. The results are broken down into results for the 6 meter aircraft and the 8 meter aircraft. Six to seven plots per simulation were generated. Some of them are used in this section and all of them are included in the Appendix.

## IV.4.1 The 6 Meter X-HALE Results

All six 6 meter X-HALE simulations had the same primary result; the aircraft over speeds up to approximately $40 \mathrm{~m} / \mathrm{s}$ and stalls after approximately 9 seconds in all six simulations. After the stall, the aircraft enters highly unstable flight. As stated previously, 12 to $20 \mathrm{~m} / \mathrm{s}$ is considered the normal flight speed range for X-HALE [4]. This leads to two possible conclusions: Either UM/NAST did not properly model the flight of the 6 meter X-HALE or the 6 meter X-HALE is an unstable aircraft and can be expected to crash soon after takeoff.

Case 1 is a linear type no aileron input simulation run for 15 seconds. The time step was 0.0025 seconds and the residual tolerance value was 0.1 . Again, this was the first completed simulation and is the case that has a different time step and residual tolerance value then the other simulations. Figure 14 shows the aircraft's longitudinal velocity $v_{y}$ versus time. Note that the $B$ reference frame is used for all plots. The x -axis is out the right wing and the $y$-axis is tangent to the undeformed fuselage's longitudinal axis and extends in the direction of the front of the aircraft. As a result, the $x-y$ plane of
the $B$ reference frame is parallel to the $x-y$ plane of the inertial frame $G$ when the aircraft is undeformed. The z-axis extends out the top of the aircraft and is the cross product of the x -axis and y -axis.


Figure 14. Case 1 Longitudinal Velocity $v_{y}$ versus Time

This plot shows that the aircraft begins to over speed at approximately 2.5 seconds when its velocity goes over $20 \mathrm{~m} / \mathrm{s}$ and stalls at approximately 9 seconds. At this point the aircraft becomes highly unstable. Figure 15 and Figure 16 show the velocity of the aircraft in the x and z directions. Figure 17, Figure 18 and Figure 19 show the angular velocity of the aircraft about the x -, y - and z -axes versus time.


Figure 15. Case 1 Lateral Velocity $v_{x}$ versus Time


Figure 16. Case 1 Vertical Velocity $v_{z}$ versus Time


Figure 17. Case 1 Pitch Rate $\omega_{x}$ versus Time


Figure 18. Case 1 Roll Rate $\omega_{y}$ versus Time


Figure 19. Case 1 Yaw Rate $\omega_{z}$ versus Time

These plots also show that the 6 meter X-HALE becomes highly unstable after approximately 9 seconds. These angular velocity plots show that the 6 meter X-HALE is rotationally stable for approximately the first 9 seconds of the simulation. However, Figure 14 which shows the aircraft's longitudinal velocity $v_{y}$, suggests that the aircraft was unstable from the start of the simulation since the aircraft begins to speed up and then over speeds at the beginning of the simulation. Note that many of the results of the simulations run for this research show initial instabilities that quickly dampen out, such as in Figure 17. This is not due to an actual instability of the aircraft but is due to numerical errors caused by the UM/NAST program.

Case 2 is another linear type no aileron input simulation, just like Case 1 , but is run for 10 seconds instead of 15 seconds. Also, Cases 2 through 6 have a different time
step ( 0.0001 seconds), residual tolerance value (10) and time duration (10 seconds) than Case 1. Besides the fact that Case 2 is a shorter simulation than Case 1, there are no apparent differences between the results of the two simulations. Case 3 is a nonlinear version of Case 2 and its results can be viewed in Figure 20, Figure 21, Figure 22, Figure 23, Figure 24 and Figure 25. The Case 2 simulations can be viewed in the Appendix.


Figure 20. Case 3 Lateral Velocity $v_{x}$ versus Time


Figure 21. Case 3 Longitudinal Velocity $v_{y}$ versus Time


Figure 22. Case 3 Vertical Velocity $v_{z}$ versus Time

Pitch Rate vs. Time, 0 deg Aileron Input, 6 m Nonlinear Case


Figure 23. Case 3 Pitch Rate $\omega_{x}$ versus Time


Figure 24. Case 3 Roll Rate $\omega_{y}$ versus Time


Figure 25. Case 3 Yaw Rate $\omega_{z}$ versus Time

These plots show that there is little difference between the linear and nonlinear simulation types because they are very similar to the results from Case 1 and Case 2 .

Case 4, Case 5 and Case 6 are the same linear type 6 meter X-HALE simulation except for the fact that they have different sinusoidal aileron input amplitudes. The input amplitudes are 2,5 and 10 degrees, respectively. These three cases also show that the 6 meter X-HALE aircraft begins to over speed at approximately 2.5 seconds when its velocity goes over $20 \mathrm{~m} / \mathrm{s}$ and stalls at approximately 9 seconds. The aileron input for Case 6 can be seen in Figure 26, while the results for Case 6 can be seen in Figure 27, Figure 28, Figure 29, Figure 30, Figure 31 and Figure 32. The aileron inputs and the results for Cases 4 and 5 can be viewed in the Appendix.


Figure 26. Case 6 Aileron Input versus Time


Figure 27. Case 6 Lateral Velocity $v_{x}$ versus Time


Figure 28. Case 6 Longitudinal Velocity $v_{y}$ versus Time


Figure 29. Case 6 Vertical Velocity $v_{z}$ versus Time


Figure 30. Case 6 Pitch Rate $\omega_{x}$ versus Time


Figure 31. Case 6 Roll Rate $\omega_{y}$ versus Time


Figure 32. Case 6 Yaw Rate $\omega_{z}$ versus Time

It is clear when comparing the figures from Cases 4, 5 and 6 that the sinusoidal aileron inputs did have an impact on the flight behavior of the aircraft. However, the aileron inputs did not prevent the aircraft from over speeding and stalling. The results from Cases 4,5 and 6 show that the larger the aileron input amplitude is, the more effect the aileron input has on the flight behavior of the aircraft. The results for Cases 1 through 6 all show that the flight behavior of the 6 meter X-HALE is unstable from the start of the simulations.

## IV.4.2 The 8 Meter X-HALE Results

Cases 7 through 17 are the 8 meter X-HALE model simulations preformed. These cases have a 15 second flight time, a 0.0001 second time step and a maximum residual value of 10 . They are a mix of the linear and nonlinear solution types. Case 7 is
a linear type simulation and has no inputs, while Cases 8 through 17 have sinusoidal aileron inputs with amplitudes of $2,5,10,15,20$ and 25 degrees. The results for Case 7 can be viewed in Figure 33, Figure 34, Figure 35, Figure 36, Figure 37 and Figure 38.


Figure 33. Case 7 Lateral Velocity $v_{x}$ versus Time


Figure 34. Case 7 Longitudinal Velocity $v_{y}$ versus Time


Figure 35. Case 7 Vertical Velocity $v_{z}$ versus Time


Figure 36. Case 7 Pitch Rate $\omega_{x}$ versus Time


Figure 37. Case 7 Roll Rate $\omega_{y}$ versus Time


Figure 38. Case 7 Yaw Rate $\omega_{z}$ versus Time
These results show that the 8 meter X-HALE is stable for no aileron inputs. While the plots of the aircraft's velocities in the $\mathrm{x}, \mathrm{y}$, and z directions show a sinusoidal pattern, the amplitudes of the peaks and troughs get progressively smaller as the flight progresses. This suggests that the aircraft is approaching a constant velocity in all three directions. For the x direction, this value is near zero. For the z direction, this value appears to be approximately 0.095 , which is very close to zero. For the $y$ direction, this value appears to be approximately $13.8 \mathrm{~m} / \mathrm{s}$. Additionally, the plot of the angular velocity about the x -axis shows a sinusoidal pattern with the amplitude of the peaks and troughs get progressively smaller as the flight progresses. The plots of the angular velocities about the $y$ - and $z$ - axes also show sinusoidal patterns but their amplitudes are near zero. The aircraft appears to be approaching an angular velocity of zero in all three directions. Combined, this data suggests that the aircraft is stable when no inputs, such as
an aileron input, are given. Again, many of the results of the simulations run for this research show initial instabilities that quickly dampen out, such as in Figure 38. This is not due to an actual instability of the aircraft but is due to numerical errors caused by the UM/NAST program.

Case 8 is a linear simulation run with a sinusoidal aileron input on both wings with an amplitude of 2 degrees. The aileron input for Case 8 can be viewed in Figure 39, and the results for Case 8 can be viewed in Figure 40, Figure 41, Figure 42, Figure 43, Figure 44 and Figure 45.


Figure 39. Case 8 Aileron Input versus Time


Figure 40. Case 8 Lateral Velocity $v_{x}$ versus Time


Figure 41. Case 8 Longitudinal Velocity $v_{y}$ versus Time


Figure 42. Case 8 Lateral Velocity $v_{z}$ versus Time


Figure 43. Case 8 Pitch Rate $\omega_{x}$ versus Time


Figure 44. Case 8 Roll Rate $\omega_{y}$ versus Time


Figure 45. Case 8 Yaw Rate $\omega_{z}$ versus Time

These figures show that the 8 meter X-HALE is stable when a sinusoidal aileron input is performed on both wings with a 2 degree amplitude. For example, while the plot for the longitudinal velocity, the velocity in the y direction, shows a sinusoidal pattern, and the peaks and troughs become smaller after 10 seconds because the aileron input ends after 10 seconds. Also, the plot of the angular velocity about the x -axis, the pitch rate, shows peaks and troughs that also become smaller once the aileron input ends. This suggests that the aircraft is stable with this input. The plot of the velocity in the vertical direction, the $z$ direction, shows a sinusoidal pattern that terminates very quickly once the aileron input ends, meaning that the aircraft is stable in the vertical direction. The plot for the velocity in the x direction, the lateral direction, shows a very small sinusoidal pattern. However the amplitude of this pattern is very small and shows no signs of increasing once the aileron input ends. The aircraft also rotates slightly in a sinusoidal pattern about the $y$ - and z-axes, but this amplitude of these patterns are very small and show no signs of increasing. Case 9 is the same simulation as Case 8 , but it is the nonlinear case. The plots from the results of Case 9 can be viewed in the Appendix. There are no significant differences between the results for Cases 8 and 9 . The aircraft is stable for both cases and the two cases' plots are very similar.

Case 10 is a linear type simulation with a sinusoidal aileron input performed on both wings with a 5 degree amplitude. Case 11 is a nonlinear version of Case 10. The aileron input and the results for Cases 10 and 11 can be viewed in the Appendix. There are no significant differences between the plots for Cases 10 and 11. Both cases suggest that the 8 meter X-HALE is stable for a sinusoidal aileron input with a 5 degree amplitude applied to both wings. The results for these cases are very similar to those of

Cases 8 and 9, which showed that the aircraft is stable for an aileron input of 2 degrees, except that plots show that the aileron input has a slightly more significant affect on the flight of the aircraft.

Cases 12 and 13 involve a 10 degree sinusoidal aileron input. The linear case, Case 12 , suggests that the 8 meter X-HALE is stable for a sinusoidal aileron input with a 10 degree amplitude applied to both wings, while the nonlinear case, Case 13, suggests that the 8 meter X-HALE is unstable for this aileron input. The results for Case 12 are in Figure 46, Figure 47, Figure 48, Figure 49, Figure 50, Figure 51 and Figure 52, and the results for case 13 are in Figure 53, Figure 54, Figure 55, Figure 56, Figure 57, Figure 58 and Figure 59.


Figure 46. Case 12 Aileron Input versus Time


Figure 47. Case 12 Lateral Velocity $v_{x}$ versus Time


Figure 48. Case 12 Longitudinal Velocity $v_{y}$ versus Time


Figure 49. Case 12 Vertical Velocity $v_{z}$ versus Time


Figure 50. Case 12 Pitch Rate $\omega_{x}$ versus Time


Figure 51. Case 12 Roll Rate $\omega_{y}$ versus Time


Figure 52. Case 12 Yaw Rate $\omega_{z}$ versus Time


Figure 53. Case 13 Aileron Input versus Time


Figure 54. Case 13 Lateral Velocity $v_{x}$ versus Time


Figure 55. Case 13 Longitudinal Velocity $v_{y}$ versus Time


Figure 56. Case 13 Vertical Velocity $v_{z}$ versus Time


Figure 57. Case 13 Pitch Rate $\omega_{x}$ versus Time


Figure 58. Case 13 Roll Rate $\omega_{y}$ versus Time


Figure 59. Case 13 Yaw Rate $\omega_{z}$ versus Time
The results for Case 12, a linear type simulation, show similar results to the cases for the 2 and 5 degree aileron input simulations; the aircraft shows minimal movement in the lateral direction, and recovers well from the aileron input in the longitudinal and vertical directions. Rotationally, the aircraft rotates slightly in a sinusoidal pattern about the x -axis but begins to recover after the input ends. The aircraft rotates slightly in a sinusoidal pattern about the $y$ - and z-axes but these movements are very small. These results show stable flight.

However, the results for Case 13, a nonlinear type simulation and Case 12's nonlinear counterpart, suggest that the aircraft is unstable for an aileron input with a 10 degree amplitude. The results for Case 13 are similar to Case 12 except instead of recovering from the input in the longitudinal direction, the amplitude of the aircraft's sinusoidal longitudinal velocity continues to increase over time even though the aileron
input has terminated. This suggests unstable flight for an aileron input with a 10 degree amplitude. Therefore, while the linear case suggests stability, the nonlinear case suggests instability. Because the nonlinear simulation type models the nonlinear aeroelasticity and flight dynamics of an aircraft better than the linear simulation type does, the nonlinear simulation probably provides a more accurate depiction of the flight behavior of XHALE.

Cases 14 and 15 involve a 15 degree sinusoidal aileron input. The results for Cases 14 can be viewed in Figure 60, Figure 61, Figure 62, Figure 63, Figure 64, Figure 65 and Figure 66, and the results for Case 15 can be viewed in Figure 67, Figure 68, Figure 69, Figure 70, Figure 71, Figure 71, Figure 72 and Figure 73. The linear case, Case 14 , suggests that the 8 meter X-HALE is stable for this input, while the nonlinear case, Case 15 , suggests that the 8 meter X-HALE is unstable for this aileron input.


Figure 60. Case 14 Aileron Input versus Time


Figure 61. Case 14 Lateral Velocity $v_{x}$ versus Time


Figure 62. Case 14 Longitudinal Velocity $v_{y}$ versus Time


Figure 63. Case 14 Vertical Velocity $v_{z}$ versus Time


Figure 64. Case 14 Pitch Rate $\omega_{x}$ versus Time


Figure 65. Case 14 Roll Rate $\omega_{y}$ versus Time


Figure 66. Case 14 Yaw Rate $\omega_{z}$ versus Time


Figure 67. Case 15 Aileron Input versus Time


Figure 68. Case 15 Lateral Velocity $v_{x}$ versus Time


Figure 69. Case 15 Longitudinal Velocity $v_{y}$ versus Time


Figure 70. Case 15 Vertical Velocity $v_{z}$ versus Time


Figure 71. Case 15 Pitch Rate $\omega_{x}$ versus Time


Figure 72. Case 15 Roll Rate $\omega_{y}$ versus Time


Figure 73. Case 15 Yaw Rate $\omega_{z}$ versus Time
For Case 14, the linear case, the plot for the longitudinal velocity, the velocity in the $y$ direction, shows a sinusoidal pattern, and the peaks and troughs become smaller after 10 seconds because the aileron input ends after 10 seconds. Also, the plot of the angular velocity about the x -axis, the pitch rate, shows a very rough sinusoidal pattern, with peaks and troughs that also become smaller once the aileron input ends. The plot of the velocity in the vertical direction, the z direction, shows a sinusoidal pattern that terminates very quickly once the aileron input ends, meaning that the aircraft is stable in the vertical direction. The plot for the velocity in the x direction, the lateral direction, shows a vaguely sinusoidal pattern. However the amplitude of this pattern is very small and shows no signs of increasing once the aileron input ends. The aircraft also rotates slightly in vaguely sinusoidal patterns about the $y$ - and z-axes, but this amplitude of these
patterns are very small. This all suggests that the aircraft is stable for a 15 degree aileron input.

However, Case 15, the nonlinear 15 degree amplitude aileron input case, suggests that the aircraft is unstable for this input. The aircraft shows minimal movement in the lateral direction until approximately 8 seconds, but this motion is still stable. The aircraft recovers from the aileron input in the vertical direction well. The longitudinal velocity plot suggests that aircraft does not recover from the aileron input in the longitudinal direction once the input ends after 10 seconds. This suggests that the aircraft is unstable for a 15 degree amplitude sinusoidal aileron input applied to both wings. Instead, the amplitude of the longitudinal velocity's sinusoidal pattern continues to grow larger. Rotationally, the aircraft recovers from the aileron input for all three axes. Note that several plots show some high frequency instabilities after approximately 8 seconds; however, this is not due to an actual instability of the aircraft but is due to numerical errors caused by the UM/NAST program.

Case 16 and 17 involve 20 and 25 degree amplitude sinusoidal aileron inputs, respectively. These are both linear type simulations. Both simulations suggest that the 8 meter X-HALE is unstable with these inputs. The nonlinear type versions of these simulations were attempted but these simulations failed most likely because the aircraft flight went extremely unstable. These attempts had the same time step ( 0.001 seconds), residual value (10) and time duration (15 seconds) as the other 8 meter X-HALE simulations. The results of Cases 16 and 17 can be viewed in the Appendix.

Case 16's results show minimal movement in the lateral direction. The aircraft recovers from the aileron input in the vertical direction, but the longitudinal velocity plot
suggests that aircraft does not recover from the aileron input in the longitudinal direction once the input ends after 10 seconds. Instead, the amplitude of the longitudinal velocity's sinusoidal pattern continues to grow larger. This suggests that the 8 meter X-HALE will be unstable for a 20 degree amplitude sinusoidal aileron input applied to both wings when test flown. The aircraft does show some small rotational movement about the x -axis, but this lessens once the aileron input ends. The aircraft also shows some rotational movement about the $y$ - and z-axes; however, this movement is very small.

Case 17's results show minimal movement in the lateral direction. The aircraft recovers from the aileron input in the vertical direction, but the longitudinal velocity plot suggests that aircraft does not recover from the aileron input in the longitudinal direction once the input ends after 10 seconds. This suggests that the 8 meter X-HALE is unstable for a 25 degree amplitude sinusoidal aileron input applied to both wings. Instead, the amplitude of the longitudinal velocity's sinusoidal pattern continues to grow larger. Rotationally, the aircraft is stable and is minimally affected by the aileron input. Note that several plots for Case 17 show some high frequency instabilities after approximately 8 seconds; however, this is not due to an actual instability of the aircraft but is due to numerical errors caused by the UM/NAST program.

## V. Conclusions and Recommendations

## V. 1 Conclusions

The results of the six 6 meter X-HALE simulations discussed suggest that the 6 meter X-HALE model is either unstable or that the simulations were set up incorrectly. Because Shearer, Cesnik and their co-workers designed both the 6 meter and the 8 meter models of X-HALE to be stable, it is unlikely that the actual 6 meter X-HALE aircraft is unstable. The most likely cause of the instabilities that the simulations show is that the trim conditions for the 6 meter simulations were poorly configured. More research must be done in order to determine the actual cause of the perceived instability of the aircraft. For now, no conclusion can be drawn about the stability of the aircraft. A summary of the results of the 6 meter X-HALE simulations discussed is given in Table 3.

Table 3. A Summary of Discussed 6 Meter X-HALE Simulations

| Case | Simulation Type | Input | Duration (sec)/ <br> Time Step (sec)/ Max <br> Residual Value | Sinusoidal Aileron Input Data |  |  | Stability |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | Period (sec) | Start/ <br> End <br> Time <br> (sec) | Amplitude (deg) |  |
| 1 | 6 Meter Linear | None | $\begin{gathered} 15 / \\ 0.0025 / \\ 0.1 \end{gathered}$ | N/A | N/A | N/A | Unstable |
| 2 | 6 Meter Linear | None | $\begin{gathered} 10 / \\ 0.0001 / \\ 10 \end{gathered}$ | N/A | N/A | N/A | Unstable |
| 3 | 6 Meter <br> Nonlinear | None | $\begin{gathered} 10 / \\ 0.0001 / \\ 10 \end{gathered}$ | N/A | N/A | N/A | Unstable |
| 4 | 6 Meter Linear | Aileron | $\begin{gathered} 10 / \\ 0.0001 / \\ 10 \end{gathered}$ | 5 | 0.1/10 | 2 | Unstable |
| 5 | 6 Meter Linear | Aileron | $\begin{gathered} 10 / \\ 0.0001 / \\ 10 \end{gathered}$ | 5 | 0.1/10 | 5 | Unstable |
| 6 | 6 Meter Linear | Aileron | $\begin{gathered} 10 / \\ 0.0001 / \\ 10 \end{gathered}$ | 5 | 0.1/10 | 10 | Unstable |

The results of the 8 meter X -HALE simulations suggest that 8 meter X-HALE is stable for sinusoidal aileron inputs performed on both wings with 5 degrees of amplitude or less, and the aircraft is unstable for amplitudes of 10 degrees or more. The results also suggest that the aircraft is stable when no inputs are applied. Cesnik et al.'s results when performing UM/NAST simulations for the 8 -meter X-HALE [4] suggest that when a single period of a left-wing-down sinusoidal aileron input is applied, the aircraft is stable for aileron inputs with a 2 degree amplitude, but not for inputs with a 5 degree amplitude or greater. Their results suggest that when a 1-cosine gust is symmetrically applied to the 8 meter X-HALE with a maximum gust speed of $4 \mathrm{~m} / \mathrm{s}$, while the nominal flight speed is
$14 \mathrm{~m} / \mathrm{s}$ at 30 m altitude, the aircraft is stable. This research build's off of Cesnik et al.'s results and predicts that, when test flown, the 8 meter X-HALE can be expected to be stable as long as any sinusoidal aileron inputs commanded on both wings has no more than 5 degrees of amplitude. A summary of the results of the 8 meter X-HALE simulations discussed is given in Table 4.

Table 4. A Summary of Discussed 8 Meter X-HALE Simulations

| Case | Simulation Type | Input | Duration (sec)/ <br> Time Step (sec)/ Max <br> Residual Value | Sinusoidal Aileron Input Data |  |  | Stability |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | Period (sec) | Start/ <br> End <br> Time <br> (sec) | Amplitude (deg) |  |
| 7 | 8 Meter Linear | None | $\begin{gathered} 15 / \\ 0.001 / \\ 10 \end{gathered}$ | N/A | N/A | N/A | Stable |
| 8 | 8 Meter Linear | Aileron | $\begin{gathered} 15 / \\ 0.001 / \\ 10 \end{gathered}$ | 5 | 0.1/10 | 2 | Stable |
| 9 | 8 Meter Nonlinear | Aileron | $\begin{gathered} 15 / \\ 0.001 / \\ 10 \end{gathered}$ | 5 | 0.1/10 | 2 | Stable |
| 10 | 8 Meter Linear | Aileron | $\begin{gathered} 15 / \\ 0.001 / \\ 10 \end{gathered}$ | 5 | 0.1/10 | 5 | Stable |
| 11 | 8 Meter Nonlinear | Aileron | $\begin{gathered} 15 / \\ 0.001 / \\ 10 \end{gathered}$ | 5 | 0.1/10 | 5 | Stable |
| 12 | 8 Meter Linear | Aileron | $\begin{gathered} 15 / \\ 0.001 / \\ 10 \end{gathered}$ | 5 | 0.1/10 | 10 | Stable |
| 13 | 8 Meter <br> Nonlinear | Aileron | $\begin{gathered} 15 / \\ 0.001 / \\ 10 \\ \hline \end{gathered}$ | 5 | 0.1/10 | 10 | Unstable |
| 14 | 8 Meter Linear | Aileron | $\begin{gathered} \hline 15 / \\ 0.001 / \\ 10 \end{gathered}$ | 5 | 0.1/10 | 15 | Stable |
| 15 | 8 Meter Nonlinear | Aileron | $\begin{gathered} 15 / \\ 0.001 / \\ 10 \end{gathered}$ | 5 | 0.1/10 | 15 | Unstable |
| 16 | 8 Meter Linear | Aileron | $\begin{gathered} \hline 15 / \\ 0.001 / \\ 10 \end{gathered}$ | 5 | 0.1/10 | 20 | Unstable |
| 17 | 8 Meter Linear | Aileron | $\begin{gathered} 15 / \\ 0.001 / \\ 10 \\ \hline \end{gathered}$ | 5 | 0.1/10 | 25 | Unstable |

## V. 2 Recommendations for Future Research

This research provides another step forward in the process of predicting the flight behavior of the X-HALE aircrafts when they are test flown for the purpose of potentially validating the UM/NAST code; however, more research is necessary to expand on the findings of this research. Unfortunately, the 6 meter X-HALE simulations run are probably not accurate models of the flight of the 6 meter X-HALE. More simulations should be done for the 6 meter model of X-HALE but this time the trim conditions should be properly configured. Ideally simulations would be run for at least a 15 second flight time. Simulations should be run using both the linear and nonlinear solution types. These simulations should include sinusoidal aileron inputs on both wings with various amplitudes, gust inputs of various speeds, and no inputs at all. Other simulations that may be helpful include turning simulations and climb and descent simulations. Additionally, simulations need to be run in order to predict the effect of flipping XHALE's vertical tail on the 6 meter X-HALE. It is possible that the vertical tail may provide more stability, especially in the lateral direction. The 8 meter aircraft has more wing dihedral when the wings are flexed than the 6 meter aircraft because the aircraft is longer. This provides more lateral stability for the 8 meter aircraft. This may be why the 6 meter X-HALE appears to be less stable than the 8 meter X-HALE according to the results of this research.

Thankfully, the 8 meter X-HALE simulations performed in this research are more helpful. However, this research only performed simulations involving either sinusoidal aileron inputs on both wings or no inputs. Shearer, Cesnik and their co-workers performed simulations for the 8 meter X-HALE involving single period, left-wing-down
sinusoidal aileron inputs, and simulations with a 1-cosine gust symmetrically applied with a maximum gust speed of $4 \mathrm{~m} / \mathrm{s}$. There are plenty more simulations that can be run for the 8 meter version of X-HALE in order to help predict the aircraft's flight behavior such as turning simulations, and climb and descend simulations, and gust inputs of various speeds. Additionally, it may be helpful to run nonlinear type simulations for aileron inputs between 5 and 10 degrees of amplitude to pinpoint exactly what sinusoidal aileron input amplitude causes the aircraft to become unstable. Simulations also need to be run in order to predict the effect of flipping the 8 meter X-HALE's vertical tail.

Much of the initial difficulties experienced are due to the fact that the 6 meter simulations were probably improperly set up. However, future research can benefit from the findings of this research when it comes to the balance of the time step, the maximum residual value and the flight time. Future research should set up simulations with a time step of no more than 0.05 seconds (but at least 0.0001 seconds), a maximum residual value of no more than 10 (but at least 0.1 ) and a flight time of at least 15 seconds. A time step of no more than 0.05 seconds and a maximum residual value of no more than 10 will help to the simulations complete easily and to provide accurate results. A flight time of at least 15 seconds will help to ensure that enough information can be drawn from the results.

## V. 3 General Remarks

The recent crash of NASA's Helios aircraft (Figure 4), a forerunning HALE Remotely Piloted Aircraft (RPA), demonstrates that while previous research has been done on the problem of nonlinear aeroelasticity coupled with nonlinear flight dynamics, the problem is still not completely understood. Several codes have been developed for
the use of modeling nonlinear aeroelastic and flight dynamics of an aircraft, such as UM/NAST, NATASHA, ASWING and RCAS, but none have been completely validated with real flight data from a fixed-wing aircraft [4]. The goal of this research was to perform flight simulations with UM/NAST so as to make predictions about X-HALE's future test flights and subsequently uncover the strengths and weaknesses of UM/NAST when X-HALE is finally flown. Indeed, this research managed to make predictions about X-HALE's future test flights and is a step forward in potentially validating UM/NAST. This research, in conjunction with the UM/NAST code and the test flights of the XHALE aircrafts should provide more information on the problem of nonlinear aeroelasticity coupled with nonlinear flight dynamics. Hopefully this knowledge can be put to use in the development of HALE aircraft. These HALE aircraft may include ISR platforms, such as US Air Force SensorCraft, network communication nodes for military or civilian purposes, or aircraft that will perform general atmospheric research.

## Appendix A. Additional Figures

Case 1: 6 m Linear Type 15 sec Simulation, No Aileron Input


Figure 74. Case 1 Lateral Velocity $v_{x}$ versus Time


Figure 75. Case 1 Longitudinal Velocity $v_{y}$ versus Time


Figure 76. Case 1 Vertical Velocity $v_{z}$ versus Time


Figure 77. Case 1 Pitch Rate $\omega_{x}$ versus Time


Figure 78. Case 1 Roll Rate $\omega_{y}$ versus Time


Figure 79. Case 1 Yaw Rate $\omega_{z}$ versus Time

## Case 2: 6 m Linear Type 10 sec Simulation, No Aileron Input



Figure 80. Case 2 Lateral Velocity $v_{x}$ versus Time


Figure 81. Case 2 Longitudinal Velocity $v_{y}$ versus Time


Figure 82. Case 2 Vertical Velocity $v_{z}$ versus Time


Figure 83. Case 2 Pitch Rate $\omega_{x}$ versus Time


Figure 84. Case 2 Roll Rate $\omega_{y}$ versus Time


Figure 85. Case 2 Yaw Rate $\omega_{z}$ versus Time

Case 3: 6 m Nonlinear Type 10 sec Simulation, No Aileron Input


Figure 86. Case 3 Lateral Velocity $v_{x}$ versus Time


Figure 87. Case 3 Longitudinal Velocity $v_{y}$ versus Time


Figure 88. Case 3 Vertical Velocity $v_{z}$ versus Time

Pitch Rate vs. Time, 0 deg Aileron Input, 6 m Nonlinear Case


Figure 89. Case 3 Pitch Rate $\omega_{x}$ versus Time


Figure 90. Case 3 Roll Rate $\omega_{y}$ versus Time


Figure 91. Case 3 Yaw Rate $\omega_{z}$ versus Time

Case 4: 6 m Linear Type 10 sec Simulation, 2 deg Aileron Input


Figure 92. Case 4 Aileron Input versus Time


Figure 93. Case 4 Lateral Velocity $v_{x}$ versus Time


Figure 94. Case 4 Longitudinal Velocity $v_{y}$ versus Time


Figure 95. Case 4 Vertical Velocity $v_{z}$ versus Time


Figure 96. Case 4 Pitch Rate $\omega_{x}$ versus Time


Figure 97. Case 4 Roll Rate $\omega_{y}$ versus Time


Figure 98. Case 4 Yaw Rate $\omega_{z}$ versus Time

Case 5: 6 m Linear Type 10 sec Simulation, 5 deg Aileron Input


Figure 99. Case 5 Aileron Input versus Time


Figure 100. Case 5 Lateral Velocity $v_{x}$ versus Time


Figure 101. Case 5 Longitudinal Velocity $v_{y}$ versus Time


Figure 102. Case 5 Vertical Velocity $v_{z}$ versus Time


Figure 103. Case 5 Pitch Rate $\omega_{x}$ versus Time


Figure 104. Case 5 Roll Rate $\omega_{y}$ versus Time


Figure 105. Case 5 Yaw Rate $\omega_{z}$ versus Time

Case 6: 6 m Linear Type 10 sec Simulation, 10 deg Aileron Input


Figure 106. Case 6 Aileron Input versus Time


Figure 107. Case 6 Lateral Velocity $v_{x}$ versus Time


Figure 108. Case 6 Longitudinal Velocity $v_{y}$ versus Time


Figure 109. Case 6 Vertical Velocity $v_{z}$ versus Time


Figure 110. Case 6 Pitch Rate $\omega_{x}$ versus Time


Figure 111. Case 6 Roll Rate $\omega_{y}$ versus Time


Figure 112. Case 6 Yaw Rate $\omega_{z}$ versus Time

## Case 7: 8 m Linear Type 15 sec Simulation, No Aileron Input



Figure 113. Case 7 Lateral Velocity $v_{x}$ versus Time


Figure 114. Case 7 Longitudinal Velocity $v_{y}$ versus Time


Figure 115. Case 7 Vertical Velocity $v_{z}$ versus Time


Figure 116. Case 7 Pitch Rate $\omega_{x}$ versus Time


Figure 117. Case 7 Roll Rate $\omega_{y}$ versus Time


Figure 118. Case 7 Yaw Rate $\omega_{z}$ versus Time

Case 8: 8 m Linear Type 15 sec Simulation, 2 deg Aileron Input


Figure 119. Case 8 Aileron Input versus Time


Figure 120. Case 8 Lateral Velocity $v_{x}$ versus Time


Figure 121. Case 8 Longitudinal Velocity $v_{y}$ versus Time


Figure 122. Case 8 Vertical Velocity $v_{z}$ versus Time


Figure 123. Case 8 Pitch Rate $\omega_{x}$ versus Time


Figure 124. Case 8 Roll Rate $\omega_{y}$ versus Time


Figure 125. Case 8 Yaw Rate $\omega_{z}$ versus Time

Case 9: 8 m Nonlinear Type 15 sec Simulation, 2 deg Aileron Input


Figure 126. Case 9 Aileron Input versus Time


Figure 127. Case 9 Lateral Velocity $v_{x}$ versus Time


Figure 128. Case 9 Longitudinal Velocity $v_{y}$ versus Time


Figure 129. Case 9 Vertical Velocity $v_{z}$ versus Time


Figure 130. Case 9 Pitch Rate $\omega_{x}$ versus Time


Figure 131. Case 9 Roll Rate $\omega_{y}$ versus Time


Figure 132. Case 9 Yaw Rate $\omega_{z}$ versus Time

## Case 10: 8 m Linear Type 15 sec Simulation, 5 deg Aileron Input



Figure 133. Case 10 Aileron Input versus Time


Figure 134. Case 10 Lateral Velocity $v_{x}$ versus Time


Figure 135. Case 10 Longitudinal Velocity $v_{y}$ versus Time


Figure 136. Case 10 Vertical Velocity $v_{z}$ versus Time


Figure 137. Case 10 Pitch Rate $\omega_{x}$ versus Time


Figure 138. Case 10 Roll Rate $\omega_{y}$ versus Time


Figure 139. Case 10 Yaw Rate $\omega_{z}$ versus Time

Case 11: 8 m Nonlinear Type 15 sec Simulation, 5 deg Aileron Input


Figure 140. Case 11 Aileron Input versus Time


Figure 141. Case 11 Lateral Velocity $v_{x}$ versus Time


Figure 142. Case 11 Longitudinal Velocity $v_{y}$ versus Time


Figure 143. Case 11 Vertical Velocity $v_{z}$ versus Time


Figure 144. Case 11 Pitch Rate $\omega_{x}$ versus Time


Figure 145. Case 11 Roll Rate $\omega_{y}$ versus Time


Figure 146. Case 11 Yaw Rate $\omega_{z}$ versus Time

Case 12: 8 m Linear Type 15 sec Simulation, 10 deg Aileron Input


Figure 147. Case 12 Aileron Input versus Time


Figure 148. Case 12 Lateral Velocity $v_{x}$ versus Time


Figure 149. Case 12 Longitudinal Velocity $v_{y}$ versus Time


Figure 150. Case 12 Vertical Velocity $v_{z}$ versus Time


Figure 151. Case 12 Pitch Rate $\omega_{x}$ versus Time


Figure 152. Case 12 Roll Rate $\omega_{y}$ versus Time


Figure 153. Case 12 Yaw Rate $\omega_{z}$ versus Time

Case 13: 8 m Nonlinear Type 15 sec Simulation, 10 deg Aileron Input


Figure 154. Case 13 Aileron Input versus Time


Figure 155. Case 13 Lateral Velocity $v_{x}$ versus Time


Figure 156. Case 13 Longitudinal Velocity $v_{y}$ versus Time


Figure 157. Case 13 Vertical Velocity $v_{z}$ versus Time


Figure 158. Case 13 Pitch Rate $\omega_{x}$ versus Time


Figure 159. Case 13 Roll Rate $\omega_{y}$ versus Time


Figure 160. Case 13 Yaw Rate $\omega_{z}$ versus Time

Case 14: 8 m Linear Type 15 sec Simulation, 15 deg Aileron Input


Figure 161. Case 14 Aileron Input versus Time


Figure 162. Case 14 Lateral Velocity $v_{x}$ versus Time


Figure 163. Case 14 Longitudinal Velocity $v_{y}$ versus Time


Figure 164. Case 14 Vertical Velocity $v_{z}$ versus Time


Figure 165. Case 14 Pitch Rate $\omega_{x}$ versus Time


Figure 166. Case 14 Roll Rate $\omega_{y}$ versus Time


Figure 167. Case 14 Yaw Rate $\omega_{z}$ versus Time

Case 15: 8 m Nonlinear Type 15 sec Simulation, 15 deg Aileron Input


Figure 168. Case 15 Aileron Input versus Time


Figure 169. Case 15 Lateral Velocity $v_{x}$ versus Time


Figure 170. Case 15 Longitudinal Velocity $v_{y}$ versus Time


Figure 171. Case 15 Vertical Velocity $v_{z}$ versus Time


Figure 172. Case 15 Pitch Rate $\omega_{x}$ versus Time

Roll Rate vs. Time, 15 deg Aileron Input, 8 m Nonlinear Case


Figure 173. Case 15 Roll Rate $\omega_{y}$ versus Time


Figure 174. Case 15 Yaw Rate $\omega_{z}$ versus Time

Case 16: 8 m Linear Type 15 sec Simulation, 20 deg Aileron Input


Figure 175. Case 16 Aileron Input versus Time


Figure 176. Case 16 Lateral Velocity $v_{x}$ versus Time


Figure 177. Case 16 Longitudinal Velocity $v_{y}$ versus Time


Figure 178. Case 16 Vertical Velocity $v_{z}$ versus Time


Figure 179. Case 16 Pitch Rate $\omega_{x}$ versus Time


Figure 180. Case 16 Roll Rate $\omega_{y}$ versus Time


Figure 181. Case 16 Yaw Rate $\omega_{z}$ versus Time

Case 17: 8 m Linear Type 15 sec Simulation, 25 deg Aileron Input


Figure 182. Case 17 Aileron Input versus Time


Figure 183. Case 17 Lateral Velocity $v_{x}$ versus Time


Figure 184. Case 17 Longitudinal Velocity $v_{y}$ versus Time


Figure 185. Case 17 Vertical Velocity $v_{z}$ versus Time


Figure 186. Case 17 Pitch Rate $\omega_{x}$ versus Time


Figure 187. Case 17 Roll Rate $\omega_{y}$ versus Time


Figure 188. Case 17 Yaw Rate $\omega_{z}$ versus Time

## Appendix B. Input File for the 6 Meter, 5 Degree Aileron Input Linear

## Case, Case 5

```
%This is from the input flie 6_meter_baseline_case0.nin
title="XHALE_Dec2009_TEST"
filename="xHALE_dec_2009_test"
Aerodynamics {
    drag
    drag_derivatives
    inflow_forces
    inflow_expansion
% stall_model
    load_factor
    pg_correction
    nominal_mach
    vertical_aero_load
    stall_on
    stall_model_type
    reynolds_number
}
Flight Conditions {
    altitude = 30
    pressure =
    load_factor = 1 % gravmult
    density
    velocity = 12
    gustx =
    gusty =
    gustz =
}
    Pilot Input {
}
    Structure {
    baoa = 7.828875834563730%7.828876272969460%7.828493098845625
    fuel_mass = 0;
    keypoints {
\begin{tabular}{rllll}
0 & 0 & 0 & \%1 & Center \\
1 & 0 & 0 & \(\% 2\) & kpt 1 on the right \\
-1 & 0 & 0 & \(\% 3\) & kpt 1 on the left \\
2 & 0 & 0 & \(\% 4\) & kpt-extension on the right \\
-2 & 0 & 0 & \(\% 5\) & kpt-extension on the right \\
3.037 & 0 & 0.174 & \(\% 6\) & kpt-extension on the right \\
-3.037 & 0 & 0.174 & \(\% 7\) & kpt-extension on the right \\
1 & 0 & -0.184 & \(\% 8\) & R1 Pod down
\end{tabular}
```

```
        -0.7625 -0.650 0 %16 L1 Tail inner tip
        -1.2375-0.650 0 %17 L1 Tail outer tip
        2 -0.650 0 %18 R2 Tailboom
        1.7625-0.650 0 %19 R2 Tail inner tip
        2.2375 -0.650 0 %20 R2 Tail outer tip
        -2 -0.650 0 %21 L2 Tailboom
        -1.7625 -0.650 0 %22 L2 Tail inner tip
        -2.2375 -0.650 0 %23 L2 Tail outer tip
        0 0 -0.184 %24 Center pod down
        2.052 0 0 %25 kpt-extension on the right
        -2.052 0 0 %26 kpt-extension on the right
    }
    members{
        % [memb name, (key points ...), propertiy]
        PODC 1 24 fairing_center %1
        WR1 1 2 main_wing %2
        P0D1up 2 8 fairing_up_right%3
        BR1 2 12 boom %4
        TR1in 12 13 tail_in_right %5
        TR1ou 12 14 tail_out_right %6
        WR2 2 4 main_wing %7
        POD3up 4 10 fairing_up_right%8
        BR2 4 18 boom %9
        TR2in 18 19 tail_in_right %10
        TR2ou 18 20 tail_out_right %11
        WR3 4 25 6 main_wing_dih %12
        WL1 1 3 main_wing %13
        POD2up 3 9 fairing_up_left %14
        BL1 3 15 boom %15
        TL1in 15 16 tail_in_left %16
        TL1ou 15 17 tail_out_left %17
        WL2 3 5 main_wing %18
        POD4up 5 11 fairing_up_left %19
        BL2 5 21 boom %20
        TL2in 21 22 tail_in_left %21
        TL2ou 21 23 tail_out_left %22
        WL3 5 26 7
    }
    integration_direction= 1 1 1 1 -1 -1 1 1 1 1 1 - 1 - -1 1 1 1 -1 1 1 -1 1 1 - 1 - - 
1 -1 1 -1 -1
    group{
    grp1{
        1
        }
    grp2{
            2 3
            24
            4
            4
            2 7
            7
            7 9
            910
            911
            712
        }
```

```
    grp3{
        13 14
        13 15
        1516
        15 17
        13 18
        18}1
        18}2
        20 21
        20 22
        18 23
        }
    }
    inter member constraint{
    }
    member properties {
        boom {
            type = "fuselage"
            diameter = 0.024 0.013
            number of elements = 1
            rigid_element = 1
            crosssection {
                    reference axis = 0.5 0 % location of ra from LE
                        % User may choose following
                        % type of input for varible
                                    % reference axis locations
            mass_distribution = 0.119339623
                                    % (mass units)/(unit span)
                    center_of_gravity{ % Empty inputs means cg is
                }
                inertia {
                    Ixx= 2.914E-09
                    Ixy= 0
                    Ixz= 0
                    Iyy= 1.457E-09
                    Iyz= 0
                Izz= 1.457E-09
                }
            stiffness { % Be Set to rigid. These numbers
are dummy
                K11= 5.390E+07 % extension stiffness [E*A]
                    K12= 0 % extension twist coupling
                    K13= 0 % extension bend y coupling
                    K14= 0 % extension bend z coupling
                    K22= 5.390E+07 % twist stiffness [G*J]
                    K23= 0 % twist / bend y coupling
                    K24= 0 % twist / bend z coupling
                K33= 5.390E+07 % bend y stiffness [E*I]
                    K34= 0 % bend y / bend z coupling
                    K44= 5.390E+07 % bend z stiffness
            }
        }
    }
    main_wing {
        type = "wing"
        number of elements = 2
        control surface{
```

```
    }
    airfoil = NACA4415
    aero_coefficient = datatable
values
    crosssection {
        reference axis = 0.2878 0
                                    % location of ra from LE
                                    % User may choose following
                                    % type of input for varible
                                    % reference axis locations
        mass_distribution = 0.319
        center_of_gravity{
            cgx = 0.0
            cgy = 0.00756 % @ c/4
            cgz = 0.0
    }
        inertia {
            IxX= 8.089765E-04
            Ixy= -0.000000E+00
            Ixz= 0.000000E+00
            Iyy= 1.221712E-05
            Iyz= -6.493531E-06
            Izz= 7.967593E-04
        }
        stiffness {
            K11= 2.140827E+06 % extension stiffness [E*A]
            K12= 0.000000E+00 % extension twist coupling
            K13= 1.544115E+03 % extension bend y coupling
            K14= -4.905651E+04 % extension bend z coupling
            K22= 7.224739E+01 % twist stiffness [G*J]
            K23= -0.000000E+00 % twist / bend y coupling
            K24= 0.000000E+00 % twist / bend z coupling
            K33= 1.195708E+02 % bend y stiffness [E*I]
            K34= -4.634442E+01 % bend y / bend z coupling
            K44= 6.350796E+03 % bend z stiffness
        }
    }
    }
    main_wing_dih {
        type = "wing"
        number of elements = 1 2
        control surface{
            AilR = trail 0.25 2 3 WR3 % [name, percent of chord,
start element, end element]
            AilL = trail 0.25 2 3 WL3 % [name, percent of chord,
start element, end element]
    }
```

```
    airfoil = NACA4415
    aero_coefficient = datatable
    airfoilfile = EMX07.dat
    AoA = 0 0 0
    rigid_element =
    aerodynamic_spanwise_distribution = 40
    fuel_percentage =
    chord = 0.2 % Single value is used for
                                    % constant chord length
                                    % The user may specify
values
```

```
    crosssection {
```

    crosssection {
        reference axis = 0.2878 0
        reference axis = 0.2878 0
                                    % location of ra from LE
                                    % location of ra from LE
                                    % User may choose following
                                    % User may choose following
                                    % type of input for varible
                                    % type of input for varible
                                    % reference axis locations
                                    % reference axis locations
        mass_distribution = 0.319
        mass_distribution = 0.319
        center_of_gravity{
        center_of_gravity{
            cgx = 0.0
            cgx = 0.0
            cgy = 0.00756 % @ c/4
            cgy = 0.00756 % @ c/4
            cgz = 0.0
            cgz = 0.0
    }
    }
    inertia {
    inertia {
            Ixx= 8.089765E-04
            Ixx= 8.089765E-04
            Ixy= -0.000000E+00
            Ixy= -0.000000E+00
            Ixz= 0.000000E+00
            Ixz= 0.000000E+00
            Iyy= 1.221712E-05
            Iyy= 1.221712E-05
            Iyz= -6.493531E-06
            Iyz= -6.493531E-06
            Izz= 7.967593E-04
            Izz= 7.967593E-04
    }
    }
    stiffness {
    stiffness {
        K11= 2.140827E+06 % extension stiffness [E*A]
        K11= 2.140827E+06 % extension stiffness [E*A]
        K12= 0.000000E+00 % extension twist coupling
        K12= 0.000000E+00 % extension twist coupling
        K13= 1.544115E+03 % extension bend y coupling
        K13= 1.544115E+03 % extension bend y coupling
        K14= -4.905651E+04 % extension bend z coupling
        K14= -4.905651E+04 % extension bend z coupling
        K22= 7.224739E+01 % twist stiffness [G*J]
        K22= 7.224739E+01 % twist stiffness [G*J]
        K23= -0.000000E+00 % twist / bend y coupling
        K23= -0.000000E+00 % twist / bend y coupling
        K24= 0.000000E+00 % twist / bend z coupling
        K24= 0.000000E+00 % twist / bend z coupling
        K33= 1.195708E+02 % bend y stiffness [E*I]
        K33= 1.195708E+02 % bend y stiffness [E*I]
        K34= -4.634442E+01 % bend y / bend z coupling
        K34= -4.634442E+01 % bend y / bend z coupling
        K44= 6.350796E+03 % bend z stiffness
        K44= 6.350796E+03 % bend z stiffness
        }
        }
    }
    }
    }
}
tail_in_right {
tail_in_right {
type = "wing"
type = "wing"
number of elements = 1
number of elements = 1
control surface{
control surface{
% NM = [lead/trail(location),...
% NM = [lead/trail(location),...
% percentage of chord,...
% percentage of chord,...
% start element,...
% start element,...
% end element,...
% end element,...
% memb label]

```
        % memb label]
```

ELR1in = trail 0.98 11 TR1in \% [name, percent of chord, start element, end element]

ELR2in = trail 0.98 11 TR2in \% [name, percent of
chord, start element, end element]
\}
airfoil = NACA0012
aero_coefficient = datatable
AoA $=0$
rigid_element = 1
aerodynamic_spanwise_distribution = 40
fuel_percentage =
chord $=0.11 \quad \%$ Single value is used for \% constant chord length
\% The user may specify
values
 inertia \{

Ixx= 1.597900E-04
Ixy= -0.000000E+00
Ixz= 0.000000E+00
Iyy= $2.914098 \mathrm{E}-06$
Iyz= -1.688579E-22
Izz= $1.568759 \mathrm{E}-04$
\}
stiffness \{ \% Be Set to rigid. These
numbers are dummy

```
    K11= 3.214025E+06 % extension stiffness [E*A]
    K12= 0.000000E+00 % extension twist coupling
    K13= -3.714275E-04 % extension bend y coupling
    K14= -7.441697E+04 % extension bend z coupling
    K22= 2.138858E+01 % twist stiffness [G*J]
    K23= -0.000000E+00 % twist / bend y coupling
    K24= 0.000000E+00 % twist / bend z coupling
    K33= 9.098072E+01 % bend y stiffness [E*I]
    K34= 2.262609E-06 % bend y / bend z coupling
    K44= 4.274273E+03 % bend z stiffness
    }
    rigid_body{
        point_mass = 1 % changed spelling
        nodes = 2
        center_of_gravity = 0.04575 4.95E-04 -0.0005
        mass = 0.04873
    inertia{
        IxX = 4.631E-06
        Ixy = -3.190E-06
        Ixz = -3.057E-07
```

```
                Iyy \(=2.282 \mathrm{E}-05\)
                    Iyz \(=2.644 \mathrm{E}-08\)
                    Izz \(=2.651 \mathrm{E}-05\)
                    \}
                \}
        \}
    \}
    tail_out_right \{
        type = "wing"
        number of elements = 1
        control surface\{
            \% NM = [lead/trail(location),...
            \% percentage of chord,...
            \% start element,...
            \% end element,...
            \% memb label]
            ELR10u = trail 0.9811 TR1ou \% [name, percent of
```

chord, start element, end element]
ELR2ou $=$ trail 0.9811 TR2ou \% [name, percent of
chord, start element, end element]
\}
airfoil = NACA0012
aero_coefficient = datatable
AoA $=0$
rigid_element = 1
aerodynamic_spanwise_distribution = 40
fuel_percentage =
chord $=0.11 \quad \%$ Single value is used for
\% constant chord length
\% The user may specify
values
crosssection \{
reference axis
\% at each Keypoint
reference axis $=0.32350 \%$ location of ra from LE
\% User may choose following
\% type of input for varible
\% reference axis locations
mass_distribution $=0.129$
\% (mass units)/(unit span)
center_of_gravity\{ \% Empty inputs means cg is
$\operatorname{cg} x=0.0$
cgy $=0.008085 \quad \%$ @ c/4
$\operatorname{cgz}=0.0$
\}
inertia \{
Ixx= $1.597900 \mathrm{E}-04$
$I x y=-0.000000 E+00$
Ixz= 0.000000E+00
Iyy= $2.914098 \mathrm{E}-06$
Iyz= -1.688579E-22
$I z Z=1.568759 E-04$
\}
stiffness \{ \% Be Set to rigid. These
numbers are dummy

| K11 $=$ | $3.214025 \mathrm{E}+06$ | \% extension stiffness [E*A] |
| :--- | :--- | :--- |
| K12= | $0.000000 \mathrm{E}+00$ | \% extension twist coupling |
| K13 $=-3.714275 \mathrm{E}-04$ | \% extension bend y coupling |  |
| K14 $=-7.441697 \mathrm{E}+04$ | \% extension bend $z$ coupling |  |

```
            K22= 2.138858E+01 % twist stiffness [G*J]
            K23= -0.000000E+00 % twist / bend y coupling
            K24= 0.000000E+00 % twist / bend z coupling
            K33= 9.098072E+01 % bend y stiffness [E*I]
            K34= 2.262609E-06 % bend y / bend z coupling
            K44= 4.274273E+03 % bend z stiffness
            }
            rigid_body{
            point_mass = 1 % changed spelling
            nodes = 1
            center_of_gravity = 0.0286 0.008395 0.0
            mass = 0.02
            inertia{
                Ixx = 1.866E-07
                Ixy = 1.000E-10
                Ixz = 0.000E+00
                Iyy = 1.341E-06
                Iyz = 0.000E+00
                Izz = 1.311E-06
            }
            }
        }
    }
    tail_in_left {
    type = "wing"
    number of elements = 1
    control surface{
            % NM = [lead/trail(location),...
            % percentage of chord,...
            % start element,...
            % end element,...
            % memb label]
            ELL1in = trail 0.98 1 1 TL1in % [name, percent of
chord, start element, end element]
                    ELL2in = trail 0.98 1 1 TL2in % [name, percent of
chord, start element, end element]
    }
    airfoil = NACA0012
    aero_coefficient = datatable
    AoA = 0
    rigid_element = 1
    aerodynamic_spanwise_distribution = 40
    fuel_percentage =
    chord = 0.11 % Single value is used for
                                    % constant chord length
                            % The user may specify
values
```



```
        cgz = 0.0
    }
        inertia {
        Ixx= 1.597900E-04
        Ixy= -0.000000E+00
        Ixz= 0.000000E+00
        Iyy= 2.914098E-06
        Iyz= -1.688579E-22
        Izz= 1.568759E-04
    }
    stiffness { % Be Set to rigid. These
numbers are dummy
        K11= 3.214025E+06 % extension stiffness [E*A]
        K12= 0.000000E+00 % extension twist coupling
        K13= -3.714275E-04 % extension bend y coupling
        K14= -7.441697E+04 % extension bend z coupling
        K22= 2.138858E+01 % twist stiffness [G*J]
        K23= -0.000000E+00 % twist / bend y coupling
        K24= 0.000000E+00 % twist / bend z coupling
        K33= 9.098072E+01 % bend y stiffness [E*I]
        K34= 2.262609E-06 % bend y / bend z coupling
        K44= 4.274273E+03 % bend z stiffness
        }
        rigid_body{
            point_mass = 1 % changed spelling
            nodes = 2
            center_of_gravity = -0.04575 4.95E-04 -0.0005
            mass = 0.04873
            inertia{
                Ixx = 4.631E-06
                Ixy = -3.190E-06
                Ixz = -3.057E-07
                Iyy = 2.282E-05
                Iyz = 2.644E-08
                Izz = 2.651E-05
            }
            }
        }
    }
    tail_out_left {
    type = "wing"
    number of elements = 1
    control surface{
            % NM = [lead/trail(location),...
            % percentage of chord,...
            % start element,...
            % end element,...
            % memb label]
            ELL1ou = trail 0.98 1 1 TL1ou % [name, percent of
chord, start element, end element]
            ELL2ou = trail 0.98 1 1 TL2ou % [name, percent of
chord, start element, end element]
    }
    airfoil = NACA0012
    aero_coefficient = datatable
    AoA = 0
    rigid_element = 1
```

```
            aerodynamic_spanwise_distribution = 40
            fuel_percentage =
            chord = 0.11 % Single value is used for
                        % constant chord length
                        % The user may specify
values
    crosssection { % at each Keypoint
        reference axis = 0.3235 0% location of ra from LE
                        % User may choose following
                                % type of input for varible
                                % reference axis locations
        mass_distribution = 0.129 % (mass units)/(unit span)
        center_of_gravity{ % Empty inputs means cg is
            cgx = 0.0
            cgy = 0.008085 % @ c/4
            cgz = 0.0
        } % located at ra
        inertia {
            Ixx= 1.597900E-04
            Ixy= -0.000000E+00
            Ixz= 0.000000E+00
            Iyy= 2.914098E-06
            Iyz= -1.688579E-22
            Izz= 1.568759E-04
        }
        stiffness { % Be Set to rigid. These
numbers are dummy
        K11= 3.214025E+06 % extension stiffness [E*A]
        K12= 0.000000E+00 % extension twist coupling
        K13= -3.714275E-04 % extension bend y coupling
        K14= -7.441697E+04 % extension bend z coupling
        K22= 2.138858E+01 % twist stiffness [G*J]
        K23= -0.000000E+00 % twist / bend y coupling
        K24= 0.000000E+00 % twist / bend z coupling
        K33= 9.098072E+01 % bend y stiffness [E*I]
        K34= 2.262609E-06 % bend y / bend z coupling
        K44= 4.274273E+03 % bend z stiffness
        }
        rigid_body{
            point_mass = 1 % changed spelling
            nodes = 1
            center_of_gravity = -0.0286 0.008395 0.0
            mass = 0.02
            inertia{
                Ixx = 1.866E-07
                Ixy = 1.000E-10
                Ixz = 0.000E+00
                Iyy = 1.341E-06
                    Iyz = 0.000E+00
                    Izz = 1.311E-06
            }
        }
    }
}
fairing_center {
        type = "vtail"
```

```
number of elements \(=1\)
airfoil = NACA0018
aero_coefficient = datatable
```

\%
values
are dummy

```
crosssection {
```

crosssection {
reference axis= 0.6093 0%0 0%
reference axis= 0.6093 0%0 0%
mass_distribution= 1.0e-8 % (mass units)/(unit span)
mass_distribution= 1.0e-8 % (mass units)/(unit span)
inertia {
inertia {
IxX= 1.0e-8
IxX= 1.0e-8
Ixy= 0
Ixy= 0
Ixz= 0
Ixz= 0
Iyy= 1.0e-8
Iyy= 1.0e-8
Iyz= 0
Iyz= 0
IzZ= 1.0e-8
IzZ= 1.0e-8
}
}
stiffness { % Be Set to rigid. These numbers
stiffness { % Be Set to rigid. These numbers
K11= 5.390E+07 % extension stiffness [E*A]
K11= 5.390E+07 % extension stiffness [E*A]
K12= 0 % extension twist coupling
K12= 0 % extension twist coupling
K13= 0 % extension bend y coupling
K13= 0 % extension bend y coupling
K14= 0 % extension bend z coupling
K14= 0 % extension bend z coupling
K22= 5.390E+07 % twist stiffness [G*J]
K22= 5.390E+07 % twist stiffness [G*J]
K23= 0 % twist / bend y coupling
K23= 0 % twist / bend y coupling
K24= 0 % twist / bend z coupling
K24= 0 % twist / bend z coupling
K33= 5.390E+07 % bend y stiffness [E*I]
K33= 5.390E+07 % bend y stiffness [E*I]
K34= 0 % bend y / bend z coupling
K34= 0 % bend y / bend z coupling
K44= 5.390E+07 % bend z stiffness
K44= 5.390E+07 % bend z stiffness
}
}
rigid_body{
rigid_body{
point_mass = 2 % changed spelling
point_mass = 2 % changed spelling
nodes = 1 2
nodes = 1 2
center_of_gravity{
center_of_gravity{
cgx{
cgx{
0% 0.0125 % 0.0125 % center pod battery
0% 0.0125 % 0.0125 % center pod battery
0%-0.0031
0%-0.0031
}
}
cgy{
cgy{
-0.0009 % 0.0591 % center pod battery
-0.0009 % 0.0591 % center pod battery
0.0431
0.0431
}
}
cgz{
cgz{
-0.0689 %-0.0689 % center pod battery
-0.0689 %-0.0689 % center pod battery
0.0116
0.0116
}
}
}
}
mass{
mass{
0.3960
0.3960
1.0248

```
            1.0248
```

```
    }
        inertia{
        Ixx{
            1.160E-03
            1.476E-02
        }
        Ixy{
            0.000E+00
            2.322E-04
        }
        Ixz{
                        0.000E+00
                        2.267E-05
        }
        Iyy{
            9.485E-05
            2.816E-03
        }
        Iyz{
            0.000E+00
            4.500E-04
            }
            Izz{
                    1.098E-03
                    2.503E-04
        }
                }
                }
    }
}
fairing_up_right {
    type = "vtail"
    number of elements = 1
    airfoil = NACA0018
    aero_coefficient = datatable
    airfoilfile = mh78.dat
    AoA = 0
    rigid_element = 1
    aerodynamic_spanwise_distribution = 40
    fuel_percentage =
    chord = 0.37 % Single value is used for
                                    % constant chord length
                                    % The user may specify
                                    % at each Keypoint
    crosssection {
        reference axis= 0.6093 0%0 0%
        mass_distribution= 1.0e-8 % (mass units)/(unit span)
        inertia {
            Ixx=1.0e-8
                Ixy= 0
                Ixz= 0
                Iyy= 1.0e-8
                Iyz= 0
                Izz= 1.0e-8
        }
```

```
stiffness { % Be Set to rigid. These numbers
```

```
    K11= 5.390E+07 % extension stiffness [E*A]
```

    K11= 5.390E+07 % extension stiffness [E*A]
    K12= 0 % extension twist coupling
    K12= 0 % extension twist coupling
    K13= 0 % extension bend y coupling
    K13= 0 % extension bend y coupling
    K14= 0 % extension bend z coupling
    K14= 0 % extension bend z coupling
    K22= 5.390E+07 % twist stiffness [G*J]
    K22= 5.390E+07 % twist stiffness [G*J]
    K23= 0 % twist / bend y coupling
    K23= 0 % twist / bend y coupling
    K24= 0 % twist / bend z coupling
    K24= 0 % twist / bend z coupling
    K33= 5.390E+07 % bend y stiffness [E*I]
    K33= 5.390E+07 % bend y stiffness [E*I]
    K34= 0 % bend y / bend z coupling
    K34= 0 % bend y / bend z coupling
    K44= 5.390E+07 % bend z stiffness
    K44= 5.390E+07 % bend z stiffness
    }
}
rigid_body{
rigid_body{
point_mass = 2 % changed spelling
point_mass = 2 % changed spelling
nodes = 1 2
nodes = 1 2
center_of_gravity{
center_of_gravity{
cgx{
cgx{
0.0125 % 0.0125 % right pods battery
0.0125 % 0.0125 % right pods battery
-0.0062
-0.0062
}
}
cgy{
cgy{
-0.0009 % 0.0591 % right pods battery
-0.0009 % 0.0591 % right pods battery
0.0662
0.0662
}
}
cgz{
cgz{
-0.0689 %-0.0689 % right pods battery
-0.0689 %-0.0689 % right pods battery
0.0066
0.0066
}
}
}
}
mass{
mass{
0.3960
0.3960
1.0571
1.0571
}
}
inertia{
inertia{
Ixx{
Ixx{
1.160E-03
1.160E-03
1.134E-02
1.134E-02
}
}
Ixy{
Ixy{
0.000E+00
0.000E+00
-1.212E-03
-1.212E-03
}
}
Ixz{
Ixz{
0.000E+00
0.000E+00
1.055E-05
1.055E-05
}
}
Iyy{
Iyy{
9.485E-05
9.485E-05
3.209E-03
3.209E-03
}
}
Iyz{
Iyz{
0.000E+00
0.000E+00
4.595E-05
4.595E-05
}
}
Izz{
Izz{
1.098E-03

```
            1.098E-03
```

are dummy

```
                                    8.484E-03
                                    }
                                    }
                }
        }
    }
    fairing_up_left {
        type = "vtail"
        number of elements = 1
        airfoil = NACA0018
        aero_coefficient = datatable
        airfoilfile = mh78.dat
        AoA = 0
        rigid_element = 1
        aerodynamic_spanwise_distribution = 40
        fuel_percentage =
        chord = 0.37 % Single value is used for
                                    % constant chord length
                                    % The user may specify
values
are dummy
```

```
    crosssection {
```

    crosssection {
    ```
    crosssection {
        reference axis= 0.6093 0%0 0%
        reference axis= 0.6093 0%0 0%
        reference axis= 0.6093 0%0 0%
        mass_distribution= 1.0e-8 % (mass units)/(unit span)
        mass_distribution= 1.0e-8 % (mass units)/(unit span)
        mass_distribution= 1.0e-8 % (mass units)/(unit span)
        inertia {
        inertia {
        inertia {
            Ixx= 1.0e-8
            Ixx= 1.0e-8
            Ixx= 1.0e-8
            Ixy= 0
            Ixy= 0
            Ixy= 0
            Ixz= 0
            Ixz= 0
            Ixz= 0
            Iyy= 1.0e-8
            Iyy= 1.0e-8
            Iyy= 1.0e-8
            Iyz= 0
            Iyz= 0
            Iyz= 0
            Izz= 1.0e-8
            Izz= 1.0e-8
            Izz= 1.0e-8
        }
        }
        }
        stiffness { % Be Set to rigid. These numbers
        stiffness { % Be Set to rigid. These numbers
        stiffness { % Be Set to rigid. These numbers
```

            K11= 5.390E+07 % extension stiffness [E*A]
    ```
            K11= 5.390E+07 % extension stiffness [E*A]
```

            K11= 5.390E+07 % extension stiffness [E*A]
            K12= 0 % extension twist coupling
            K12= 0 % extension twist coupling
            K12= 0 % extension twist coupling
            K13= 0 % extension bend y coupling
            K13= 0 % extension bend y coupling
            K13= 0 % extension bend y coupling
            K14= 0 % extension bend z coupling
            K14= 0 % extension bend z coupling
            K14= 0 % extension bend z coupling
            K22= 5.390E+07 % twist stiffness [G*J]
            K22= 5.390E+07 % twist stiffness [G*J]
            K22= 5.390E+07 % twist stiffness [G*J]
            K23= 0 % twist / bend y coupling
            K23= 0 % twist / bend y coupling
            K23= 0 % twist / bend y coupling
            K24= 0 % twist / bend z coupling
            K24= 0 % twist / bend z coupling
            K24= 0 % twist / bend z coupling
            K33= 5.390E+07 % bend y stiffness [E*I]
            K33= 5.390E+07 % bend y stiffness [E*I]
            K33= 5.390E+07 % bend y stiffness [E*I]
            K34= 0 % bend y / bend z coupling
            K34= 0 % bend y / bend z coupling
            K34= 0 % bend y / bend z coupling
            K44= 5.390E+07 % bend z stiffness
            K44= 5.390E+07 % bend z stiffness
            K44= 5.390E+07 % bend z stiffness
        }
        }
        }
            rigid_body{
            rigid_body{
            rigid_body{
            point_mass = 2 % changed spelling
            point_mass = 2 % changed spelling
            point_mass = 2 % changed spelling
            nodes = 1 2
            nodes = 1 2
            nodes = 1 2
            center_of_gravity{
            center_of_gravity{
            center_of_gravity{
                    cgx{
                    cgx{
                    cgx{
                        -0.0125 %-0.0125 % left pods battery
                        -0.0125 %-0.0125 % left pods battery
                        -0.0125 %-0.0125 % left pods battery
                        0.0062
                        0.0062
                        0.0062
            }
            }
            }
                cgy{
                cgy{
                cgy{
                        -0.0009 % 0.0591 % left pods battery
                        -0.0009 % 0.0591 % left pods battery
                        -0.0009 % 0.0591 % left pods battery
                        0.0662
                        0.0662
                        0.0662
                }
    ```
                }
```

                }
    ```
```

    cgz{
        -0.0689 %-0.0689 % left pods battery
                        0.0066
    }
    }
    mass{
    0.3960
    1.0571
    }
    inertia{
        Ixx{
            1.160E-03
            1.134E-02
        }
        Ixy{
            0.000E+00
            -1.212E-03
        }
        Ixz{
            0.000E+00
            1.055E-05
        }
        Iyy{
            9.485E-05
            3.209E-03
        }
        Iyz{
            0.000E+00
            4.595E-05
        }
        Izz{
            1.098E-03
            8.484E-03
            }
                }
            }
    }
    }
motor_fairing {
type = "vtail"
number of elements = 1
airfoil = NACA0018
aero_coefficient = datatable
airfoilfile = mh78.dat
AoA = 0
rigid_element = 1
aerodynamic_spanwise_distribution = 40
fuel_percentage =
chord = 0.37 % Single value is used for
% constant chord length
% The user may specify
% at each Keypoint
crosssection {
reference axis= 0.6093 0%0 0%
mass_distribution= 1.0e-8 % (mass units)/(unit span)
inertia {

```
```

    Ixx= 1.0e-8
    Ixy= 0
    Ixz= 0
    Iyy= 1.0e-8
    Iyz= 0
    Izz= 1.0e-8
    }
stiffness { % Be Set to rigid. These numbers
are dummy
K11= 5.390E+07 % extension stiffness [E*A]
K12= 0 % extension twist coupling
K13= 0 % extension bend y coupling
K14= 0 % extension bend z coupling
K22= 5.390E+07 % twist stiffness [G*J]
K23= 0 % twist / bend y coupling
K24= 0 % twist / bend z coupling
K33= 5.390E+07 % bend y stiffness [E*I]
K34= 0 % bend y / bend z coupling
K44= 5.390E+07 % bend z stiffness
}
rigid_body{
point_mass = 2 % changed spelling
nodes = 1 2
center_of_gravity{
cgx{
0.0 % 0.0125 % right pods battery
0.0
}
cgy{
-0.0109 % 0.0591 % right pods battery
0.0562
}
cgz{
-0.0689 %-0.0689 % right pods battery
0.0066
}
}
mass{
0.3960
0.4000
}
inertia{
IxX{
1.160E-04
1.134E-03
}
Ixy{
0.000E+00
-1.212E-03
}
Ixz{
0.000E+00
1.055E-05
}
Iyy{
9.485E-05
3.209E-03

```
```

                    }
                    Iyz{
                        0.000E+00
                        4.595E-05
                            }
        Izz{
            1.098E-03
                        8.484E-03
                            }
        }
        }
        }
        }
    }
    }
Loads {
frame = body_follower % or body_follower or
inertial
load_vec{
% [(1) (2) (3) (4) (5) (6) OPTIONAL (7) OPTIONAL (8)]
% (1): load type (force)
% (2): member designation
% (3): location type(keypoint or node)
% (4): location number
% (5): cartesian direction
% (6): time-independent value
% (7): time-independent value (OPTIONAL)
% (8): start time (OPTIONAL)
% (9): stop time (OPTIONAL)
Mot1 = force PODC node 1 y
0.987101270333469%0.987101042245488%0.987157990615576% -
0.5*sin(2*pi/0.10*(t-0.01)) 0.01 0.11
Mot2 = force POD1up node 1 y
0.987101270333469%0.987101042245488%0.987157990615576% -
0.5*sin(2*pi/0.10*(t-0.01)) 0.01 0.11
Mot3 = force POD2up node 1 y
0.987101270333469%0.987101042245488%0.987157990615576% -
0.5*sin(2*pi/0.10*(t-0.01)) 0.01 0.11
Mot4 = force POD3up node 1 y
0.987101270333469%0.987101042245488%0.987157990615576% -
0.5*sin(2*pi/0.10*(t-0.01)) 0.01 0.11
Mot5 = force POD4up node 1 y
0.987101270333469%0.987101042245488%0.987157990615576% -
0.5*sin(2*pi/0.10*(t-0.01)) 0.01 0.11
D1 = force PODC node 2 y -0.4408
D2 = force POD1up node 2 y -0.4408
D3 = force POD2up node 2 y -0.4408
D4 = force POD3up node 2 y -0.15
D5 = force POD4up node 2 y -0.15
% Fexample = force WL1 node 60 z 30*sin(20*t)
% [(1) (2) (3) (4) (5) (6) OPTIONAL (7) OPTIONAL (8)]
% (1): load type (force_dist)
% (2): member designation
% (3): starting element
% (4): ending element
% (5): cartesian direction

```
```

    % (6): time-independent value
    % (7): time-independent value (OPTIONAL)
    % (8): start time (OPTIONAL)
    % (9): stop time (OPTIONAL)
    % FD1 = force_dist MB 1 20 z 50*sin(40*t)+25
    % [(1) (2) (3) (4) (5) (6) OPTIONAL (7) OPTIONAL (8)]
    % (1): load type (moment)
    % (2): member designation
    % (3): location type(keypoint or node)
    % (4): location number
    % (5): cartesian direction
    % (6): time-independent value
    % (7): time-independent value (OPTIONAL)
    % (8): start time (OPTIONAL)
    % (9): stop time (OPTIONAL)
    % M1 = moment MB node 60 x 50
    % [(1) (2) (3) (4) (5) (6) OPTIONAL (7) OPTIONAL (8)]
    % (1): load type (moment_dist)
    % (2): member designation
    % (3): starting element
    % (4): ending element
    % (5): cartesian direction
    % (6): time-independent value
    % (7): time-independent value (OPTIONAL)
    % (8): start time (OPTIONAL)
    % (9): stop time (OPTIONAL)
    % MD1 = moment_dist MB 9 10 z 50
    % [load type, member designation, element start, element end,
    mode, voltage value, OPTIONAL--> start time, stop time,...] % NEED TO
COMPLETE
% VA1 = actuator_volt VA1 1 10
% [(1) (2) (3) OPTIONAL (4) OPTIONAL (5)]
% (1): load type (control_surf)
% (2): control surface designation
% (3): time-independent value
% (4): time-independent value (OPTIONAL)
% (5): start time (OPTIONAL)
% (6): stop time (OPTIONAL)
DEFTAIL1= control_surf ELR1in -7.830535569853027%-
7.830535463594316%-7.830173052395354 %12*sin(2*pi/6.3*t)%
0.01 0.11
DEFTAIL2= control_surf ELR1ou -7.830535569853027%-
7.830535463594316%-7.830173052395354 %12*sin(2*pi/6.3*t)% 0.01 0.11
DEFTAIL3= control_surf ELR2in -7.830535569853027%-
7.830535463594316%-7.830173052395354 %12*sin(2*pi/6.3*t)% 0.01 0.11
DEFTAIL4= control_surf ELR2ou -7.830535569853027%-
7.830535463594316%-7.830173052395354 %12*sin(2*pi/6.3*t)% 0.01 0.11
DEFTAIL5= control_surf ELL1in -7.830535569853027%-
7.830535463594316%-7.830173052395354 %12*sin(2*pi/6.3*t)% 0.01 0.11
DEFTAIL6= control_surf ELL1ou -7.830535569853027%-
7.830535463594316%-7.830173052395354 %12*sin(2*pi/6.3*t)% 0.01 0.11
DEFTAIL7= control_surf ELL2in -7.830535569853027%-
7.830535463594316%-7.830173052395354 %12*sin(2*pi/6.3*t)% 0.01 0.11
DEFTAIL8= control_surf ELL2ou -7.830535569853027%-
7.830535463594316%-7.830173052395354 %12*sin(2*pi/6.3*t)% 0.01 0.11
DEFAilR= control_surf AilR 0 -5*sin(2*pi/5*t) 0.1 10
DEFAilL= control_surf AilL 0 -5*sin(2*pi/5*t) 0.1 10
}

```
```

Simulation {
mode = "new"
type = "dynamic"
% Model Construction Parameters
structural damping = 1e-4 % Structural damping
parameter
structure
first mode damping = -1e-4 % First mode damping (set
to
% Steady State Simulation Parameters
sssim{
sim_type = "nonlinear" % "nonlinear" or
"linearized"
relative tolerance = .001 % Relative tolerance for
static
numerical damping = . 8 % solution convergence
parameter
max iterations = 100
iterations
state
% solution
}
% Time Simulation Parameters
timesim{
integration_type = "Gen-Alpha" %"Trapz"% or
sim_type = "linear" % "nonlinear" or "linear" /
"reduced_order"
time_duration = 10
time_step = 0.0001 % or time_divisions=4000
% restart_filename = "wbt_smpl" % ??????
rho_inf_1 = 0.999
rho_inf_2 = 0.999
time_step_save = 100
start_time_flag = 0 % put a 1 to start from previous
conditions fresh simulations require 0
n_sub_add_time_step = 1
error_states_0 = []
gust_input = 0
local_wrinkling = 0
ref_val_1 = 1e10
ref_val_2 = 1e10
time_sim_tol = 1e1
no_rigidbody_dof = 0
}
% Flutter Analysis Parameters
flutsim{

```

parameters \{ \% They overide the values set in the previous sections (as in Loads Structure)
baoa 7.828876272969460 0.01 \% Body angle of attack, initial guess, increment

DEFTAIL1 -7.830535463594316 0.01 \% CS name, initial guess, increment

Mot1 0.987101042245488 0.01 \% Load name (pt load),
initial guess, increment
Mot2 0.987101042245488 0.01
Mot3 0.987101042245488 0.01
Mot4 0.987101042245488 0.01
Mot5 0.987101042245488 0.01
DEFTAIL2 -7.830535463594316 0.01 \% CS name, initial guess,
increment
DEFTAIL3 -7.830535463594316 0.01 \% CS name, initial guess,
increment
DEFTAIL4 -7.830535463594316 0.01 \% CS name, initial guess, increment

DEFTAIL5 -7.830535463594316 0.01 \% CS name, initial guess,
increment
DEFTAIL6 -7.830535463594316 0.01 \% CS name, initial guess,
increment
DEFTAIL7-7.830535463594316 0.01 \% CS name, initial guess,
increment
DEFTAIL8 -7.830535463594316 0.01 \% CS name, initial guess,
increment
\}
\}
\}
Screen Output\{
refgeom\{
undeformed_geometry \(=0\)
sketch_plot \(=0\)
color_style = "gray" \% "spring" or "summer" or
"autumn" or "winter" or "gray"
\}
sssim\{
static_deformed_geometry = 0
no_force_lines \(=0\)
text \(=1\)
print_lift_moment = 1
figure_position \(=0.050 .050 .600 .60\)
figure_color = 0
view \(=16045\)
animate_response \(=1\)
movie
iteration_output = 1
\}
timesim\{
time_step_output \(=1\)
iteration_output = 1
progress_bar = 0
\}
flutsim\{
plot_poles = 1
\}
modalsim \{
```

    numberofmodes = 10 % Number of modes to be
    displayed on screen
scale = 1 % Factor to scale the mode
shapes NOTE: No normalization is done with the modes
}
trimsim{
}
% print_to_file{
% stiffness_matrix = 1
% interial_matrix = 1
% trim_input = 1
% trim_output = 1
% modal_analysis = frequency
% }
generate_input_treeI = 1
generate_input_treeC = 1
response_plot {
keypoint 2 pos_z
keypoint 2 vel_z
}
load_plot = FL1 F1
File Output{
% Time Simulation File Output Request
timesim{
bframe_flight_path = 1
bframe_flight_velocity = 1
euler_angles = 1
displacement{
WR3 node 9
WR3 node 6
WR3 node 3
WR3 node 1
WR2 node 3
WR2 node 1
WR1 node 3
WR1 node 1
WL3 node 9
WL3 node 6
WL3 node 3
WL3 node 1
WL2 node 3
WL2 node 1
WL1 node 3
WL1 node 1
}
displacement{
all
}
displacementsort = "node" % "node" or "time"
liftdist{
all
}
}
}

```

\section*{Appendix C. Input File for the \(\mathbf{8}\) Meter, No Aileron Input Linear Case,}

\section*{Case 7}
```

% This is from the input flie 8_meter_ailerons_case0.nin
title="XHALE_Dec2009_TEST"
filename="xHALE_dec_2009_test"
Aerodynamics {
drag
drag_derivatives = 1 %or 0
inflow_forces = 0 %or 0
inflow_expansion = 6
% stall_model = "model_name"
load_factor = 1
pg_correction = 0
nominal_mach = 0.3
vertical_aero_load = 0
stall_on = 0
stall_model_type = 1
reynolds_number = 150000
}
Flight Conditions {
altitude = 30
pressure =
load_factor = 1 % gravmult
density
velocity = 14
gustx =
gusty =
gustz =
}
Pilot Input {
}
Structure {
baoa = -0.587176915651974%-0.046047309451146%-
0.045987813505220
fuel_mass = 0;
keypoints {

| 0 | 0 | 0 | $\% 1$ | Center |
| ---: | :--- | :--- | :--- | :--- |
| 1 | 0 | 0 | $\% 2$ | kpt 1 on the right |
| -1 | 0 | 0 | $\% 3$ | kpt 1 on the left |
| 2 | 0 | 0 | $\% 4$ | kpt-extension on the right |
| -2 | 0 | 0 | $\% 5$ | kpt-extension on the right |
| 4.037 | 0 | 0.174 | $\% 6$ | kpt-extension on the right |
| -4.037 | 0 | 0.174 | $\% 7$ | kpt-extension on the right |
| 1 | 0 | -0.184 | $\% 8$ | R1 Pod down |

```
\begin{tabular}{|c|c|c|c|}
\hline 1 & -0.650 & 0 & \%12 R1 Tailboom \\
\hline 0.7625 & -0.650 & 0 & \%13 R1 Tail inner tip \\
\hline 1.2375 & -0.650 & 0 & \%14 R1 Tail outer tip \\
\hline -1 & -0.650 & 0 & \%15 L1 Tailboom \\
\hline -0.7625 & -0.650 & 0 & \%16 L1 Tail inner tip \\
\hline -1.2375 & -0.650 & 0 & \%17 L1 Tail outer tip \\
\hline 2 & -0.650 & 0 & \%18 R2 Tailboom \\
\hline 1.7625 & -0.650 & 0 & \%19 R2 Tail inner tip \\
\hline 2.2375 & -0.650 & 0 & \%20 R2 Tail outer tip \\
\hline -2 & -0.650 & 0 & \%21 L2 Tailboom \\
\hline -1.7625 & -0.650 & 0 & \%22 L2 Tail inner tip \\
\hline -2.2375 & -0.650 & 0 & \%23 L2 Tail outer tip \\
\hline 0 & 0 & -0.184 & \%24 Center pod down \\
\hline 3 & 0 & 0 & \%25 kpt-extension on the \\
\hline -3 & 0 & 0 & \%26 kpt-extension on the \\
\hline 3.052 & 0 & 0 & \%27 kpt-extension on the \\
\hline -3.052 & 0 & 0 & \%28 kpt-extension on the \\
\hline ```
}
members{
``` & & & \\
\hline \% [memb & name, & (key poi & s ...), propertiy] \\
\hline PODC & 124 & & fairing_center \%1 \\
\hline WR1 & 12 & & main_wing \%2 \\
\hline P0D1up & 28 & & fairing_up_right\%3 \\
\hline BR1 & 212 & & boom \%4 \\
\hline TR1in & 1213 & & tail_in_right \%5 \\
\hline TR10u & 1214 & & tail_out_right \%6 \\
\hline WR2 & 24 & & main_wing \%7 \\
\hline P0D3up & 410 & & fairing_up_right\%8 \\
\hline BR2 & 418 & & boom \%9 \\
\hline TR2in & 1819 & & tail_in_right \%10 \\
\hline TR2ou & 1820 & & tail_out_right \%11 \\
\hline WR3 & 425 & & main_wing \%12 \\
\hline WR4 & 2527 & 6 & main_wing_dih \%13 \\
\hline WL1 & 13 & & main_wing \%14 \\
\hline P0D2up & 39 & & fairing_up_left \%15 \\
\hline BL1 & 315 & & boom \%16 \\
\hline TL1in & 1516 & & tail_in_left \%17 \\
\hline TL10u & 1517 & & tail_out_left \%18 \\
\hline WL2 & 35 & & main_wing \%19 \\
\hline POD4up & 511 & & fairing_up_left \%20 \\
\hline BL2 & 521 & & boom \%21 \\
\hline TL2in & 2122 & & tail_in_left \%22 \\
\hline TL2ou & 2123 & & tail_out_left \%23 \\
\hline WL3 & 526 & & main_wing \%24 \\
\hline WL4 & 2628 & 7 & main_wing_dih \%25 \\
\hline \multicolumn{4}{|l|}{\}} \\
\hline
\end{tabular}
integration_direction= \(1 \begin{array}{lllllllllllllllllll} & 1 & 1 & -1 & -1 & 1 & 1 & 1 & -1 & -1 & 1 & 1 & 1 & -1 & 1 & -1 & 1 & -1 & -\end{array}\)
\(\begin{array}{llllll}1 & 1 & -1 & 1 & -1 & -1\end{array}\)
    group\{
    grp1\{
        1
        \}
    grp2\{
        23
        24
        45
```

            4
            7
            7
            7 9
            9 10
            11
            12
            12 13
            }
    grp3{
14 15
14 16
16 17
16 18
14 19
1920
19 21
21 22
21 23
19 24
24 25
}
}
inter member constraint{
}
member properties {
boom {
type = "fuselage"
diameter = 0.024 0.013
number of elements = 1
rigid_element = 1
crosssection {
reference axis = 0.5 0 % location of ra from LE
% User may choose following
% type of input for varible
% reference axis locations
mass_distribution = 0.01%0.119339623
% (mass units)/(unit span)
center_of_gravity{ % Empty inputs means cg is
}
inertia {
Ixx= 2.914E-09
Ixy= 0
Ixz= 0
Iyy= 1.457E-09
Iyz= 0
Izz= 1.457E-09
}
stiffness { % Be Set to rigid. These numbers
K11= 5.390E+07 % extension stiffness [E*A]
K12= 0 % extension twist coupling
K13= 0 % extension bend y coupling
K14= 0 % extension bend z coupling
K22= 5.390E+07 % twist stiffness [G*J]
K23= 0 % twist / bend y coupling
K24= 0 % twist / bend z coupling

```
are dummy
```

                K33= 5.390E+07 % bend y stiffness [E*I]
                    K34= 0 % bend y / bend z coupling
                    K44= 5.390E+07 % bend z stiffness
                }
        }
    }
main_wing {
type = "wing"
number of elements = 2
control surface{
}
airfoil = NACA4415
aero_coefficient = datatable
airfoilfile = EMX07.dat
AoA = 5
rigid_element =
aerodynamic_spanwise_distribution = 0
fuel_percentage
chord = 0.2 % Single value is used for
% constant chord length
% The user may specify
values

```
```

    crosssection {
    ```
    crosssection {
        reference axis = 0.2878 0
        reference axis = 0.2878 0
                                    % location of ra from LE
                                    % location of ra from LE
                                    % User may choose following
                                    % User may choose following
                                    % type of input for varible
                                    % type of input for varible
                                    % reference axis locations
                                    % reference axis locations
        mass_distribution = 0.319
        mass_distribution = 0.319
        center_of_gravity{
        center_of_gravity{
            cgx = 0.0
            cgx = 0.0
            cgy = 0.00756 % @ c/4
            cgy = 0.00756 % @ c/4
            cgz = 0.0
            cgz = 0.0
        }
        }
        inertia {
        inertia {
            Ixx= 8.089765E-04
            Ixx= 8.089765E-04
            Ixy= -0.000000E+00
            Ixy= -0.000000E+00
            IxZ= 0.000000E+00
            IxZ= 0.000000E+00
            Iyy= 1.221712E-05
            Iyy= 1.221712E-05
            Iyz= -6.493531E-06
            Iyz= -6.493531E-06
            Izz= 7.967593E-04
            Izz= 7.967593E-04
        }
        }
        stiffness {
        stiffness {
            K11= 2.140827E+06 % extension stiffness [E*A]
            K11= 2.140827E+06 % extension stiffness [E*A]
            K12= 0.000000E+00 % extension twist coupling
            K12= 0.000000E+00 % extension twist coupling
            K13= 1.544115E+03 % extension bend y coupling
            K13= 1.544115E+03 % extension bend y coupling
            K14= -4.905651E+04 % extension bend z coupling
            K14= -4.905651E+04 % extension bend z coupling
            K22= 7.224739E+01 % twist stiffness [G*J]
            K22= 7.224739E+01 % twist stiffness [G*J]
            K23= -0.000000E+00 % twist / bend y coupling
            K23= -0.000000E+00 % twist / bend y coupling
            K24= 0.000000E+00 % twist / bend z coupling
            K24= 0.000000E+00 % twist / bend z coupling
            K33= 1.195708E+02 % bend y stiffness [E*I]
            K33= 1.195708E+02 % bend y stiffness [E*I]
            K34= -4.634442E+01 % bend y / bend z coupling
            K34= -4.634442E+01 % bend y / bend z coupling
            K44= 6.350796E+03 % bend z stiffness
            K44= 6.350796E+03 % bend z stiffness
        }
        }
    }
```

    }
    ```
```

    }
    main_wing_dih {
        type = "wing"
        number of elements = 1 2
        control surface{
            AilR = trail 0.40 2 3 WR4 % [name, percent of chord,
    start element, end element]
AilL = trail 0.40 2 3 WL4 % [name, percent of chord,
start element, end element]
}
airfoil = NACA4415
aero_coefficient = datatable
% airfoilfile = EMX07.dat
AoA = 5 5 5
rigid_element =
aerodynamic_spanwise_distribution = 40
fuel_percentage =
chord = 0.2 % Single value is used for
% constant chord length
% The user may specify
values
% at each Keypoint
crosssection {
reference axis = 0.2878 0
% location of ra from LE
% User may choose following
% type of input for varible
% reference axis locations
mass_distribution = 0.319
center_of_gravity{
% (mass units)/(unit span)
% Empty inputs means cg is
cgx = 0.0
cgy = 0.00756 % @ c/4
cgz = 0.0
}
inertia {
Ixx= 8.089765E-04
Ixy= -0.000000E+00
Ixz= 0.000000E+00
Iyy= 1.221712E-05
Iyz= -6.493531E-06
Izz= 7.967593E-04
}
stiffness {
K11= 2.140827E+06 % extension stiffness [E*A]
K12= 0.000000E+00 % extension twist coupling
K13= 1.544115E+03 % extension bend y coupling
K14= -4.905651E+04 % extension bend z coupling
K22= 7.224739E+01 % twist stiffness [G*J]
K23= -0.000000E+00 % twist / bend y coupling
K24= 0.000000E+00 % twist / bend z coupling
K33= 1.195708E+02 % bend y stiffness [E*I]
K34= -4.634442E+01 % bend y / bend z coupling
K44= 6.350796E+03 % bend z stiffness
}
}
}

```
tail_in_right \{
        type = "wing"
        number of elements = 1
        control surface\{
            \% NM = [lead/trail(location),...
            \% percentage of chord,...
            \% start element,...
            \% end element,...
            \% memb label]
            ELR1in = trail 0.9811 TR1in \% [name, percent of
chord, start element, end element]
                            ELR2in = trail 0.9811 TR2in \% [name, percent of
chord, start element, end element]
    \}
    airfoil = NACA0012
    aero_coefficient = datatable
    AoA \(=0\)
    rigid_element = 1
    aerodynamic_spanwise_distribution = 40
    fuel_percentage =
    chord \(\quad=0.11 \quad \%\) Single value is used for
        \% constant chord length
        \% The user may specify
values

```

                rigid_body{
                point_mass = 1 % changed spelling
                        nodes = 2
                        center_of_gravity = 0.04575 4.95E-04 -0.0005
                        mass = 0.04873
                inertia{
                    IxX = 4.631E-06
                        Ixy = -3.190E-06
                Ixz = -3.057E-07
                Iyy = 2.282E-05
                Iyz = 2.644E-08
                Izz = 2.651E-05
                    }
                }
        }
    }
tail_out_right {
type = "wing"
number of elements = 1
control surface{
% NM = [lead/trail(location),...
% percentage of chord,...
% start element,...
% end element,...
% memb label]
ELR1ou = trail 0.98 1 1 TR1ou % [name, percent of
chord, start element, end element]
ELR2ou = trail 0.98 1 1 TR2ou % [name, percent of
chord, start element, end element]
}
airfoil = NACA0012
aero_coefficient = datatable
AoA = 0
rigid_element = 1
aerodynamic_spanwise_distribution = 40
fuel_percentage =
chord = 0.11 % Single value is used for
% constant chord length
% The user may specify

```

values
```

        Iyz= -1.688579E-22
            Izz= 1.568759E-04
    }
    stiffness { % Be Set to rigid. These
    numbers are dummy
K11= 3.214025E+06 % extension stiffness [E*A]
K12= 0.000000E+00 % extension twist coupling
K13= -3.714275E-04 % extension bend y coupling
K14= -7.441697E+04 % extension bend z coupling
K22= 2.138858E+01 % twist stiffness [G*J]
K23= -0.000000E+00 % twist / bend y coupling
K24= 0.000000E+00 % twist / bend z coupling
K33= 9.098072E+01 % bend y stiffness [E*I]
K34= 2.262609E-06 % bend y / bend z coupling
K44= 4.274273E+03 % bend z stiffness
}
rigid_body{
point_mass = 1 % changed spelling
nodes = 1
center_of_gravity = 0.0286 0.008395 0.0
mass = 0.02
inertia{
Ixx = 1.866E-07
Ixy = 1.000E-10
Ixz = 0.000E+00
Iyy = 1.341E-06
Iyz = 0.000E+00
Izz = 1.311E-06
}
}
}
}
tail_in_left {
type = "wing"
number of elements = 1
control surface{
% NM = [lead/trail(location),...
% percentage of chord,...
% start element,...
% end element,...
% memb label]
ELL1in = trail 0.98 1 1 TL1in % [name, percent of
chord, start element, end element]
ELL2in = trail 0.98 1 1 TL2in % [name, percent of
chord, start element, end element]
}
airfoil = NACA0012
aero_coefficient = datatable
AoA = 0
rigid_element = 1
aerodynamic_spanwise_distribution = 40
fuel_percentage =
chord = 0.11 % Single value is used for
% constant chord length
% The user may specify
values
% at each Keypoint

```
```

    crosssection {
        reference axis = 0.3235 0% location of ra from LE
                        % User may choose following
                        % type of input for varible
                                % reference axis locations
    mass_distribution = 0.129
                                % (mass units)/(unit span)
    center_of_gravity{ % Empty inputs means cg is
            cgx = 0.0
            cgy = 0.008085 % @ c/4
            cgz = 0.0
    }
    inertia {
        Ixx= 1.597900E-04
        Ixy= -0.000000E+00
        Ixz= 0.000000E+00
        Iyy= 2.914098E-06
        Iyz= -1.688579E-22
        Izz= 1.568759E-04
    }
    stiffness { % Be Set to rigid. These
    numbers are dummy
K11= 3.214025E+06 % extension stiffness [E*A]
K12= 0.000000E+00 % extension twist coupling
K13= -3.714275E-04 % extension bend y coupling
K14= -7.441697E+04 % extension bend z coupling
K22= 2.138858E+01 % twist stiffness [G*J]
K23= -0.000000E+00 % twist / bend y coupling
K24= 0.000000E+00 % twist / bend z coupling
K33= 9.098072E+01 % bend y stiffness [E*I]
K34= 2.262609E-06 % bend y / bend z coupling
K44= 4.274273E+03 % bend z stiffness
}
rigid_body{
point_mass = 1 % changed spelling
nodes = 2
center_of_gravity = -0.04575 4.95E-04 -0.0005
mass = 0.04873
inertia{
IxX = 4.631E-06
Ixy = -3.190E-06
Ixz = -3.057E-07
Iyy = 2.282E-05
Iyz = 2.644E-08
Izz = 2.651E-05
}
}
}
}
tail_out_left {
type = "wing"
number of elements = 1
control surface{
% NM = [lead/trail(location),...
% percentage of chord,...
% start element,...
% end element,...
% memb label]

```

ELL1ou = trail 0.98 11 TL1ou \% [name, percent of chord, start element, end element]

ELL2ou \(=\) trail 0.9811 TL2ou \% [name, percent of chord, start element, end element]
\}
airfoil = NACA0012
aero_coefficient = datatable
AoA \(=0\)
rigid_element = 1
aerodynamic_spanwise_distribution = 40
fuel_percentage =
chord \(=0.11 \quad \%\) Single value is used for \% constant chord length
\% The user may specify
values
 inertia \{

Ixx= 1.597900E-04
Ixy= -0.000000E+00
Ixz= 0.000000E+00
Iyy= \(2.914098 \mathrm{E}-06\)
Iyz= -1.688579E-22
Izz= \(1.568759 \mathrm{E}-04\)
\}
stiffness \{ \% Be Set to rigid. These
numbers are dummy
```

    K11= 3.214025E+06 % extension stiffness [E*A]
    K12= 0.000000E+00 % extension twist coupling
    K13= -3.714275E-04 % extension bend y coupling
    K14= -7.441697E+04 % extension bend z coupling
    K22= 2.138858E+01 % twist stiffness [G*J]
    K23= -0.000000E+00 % twist / bend y coupling
    K24= 0.000000E+00 % twist / bend z coupling
    K33= 9.098072E+01 % bend y stiffness [E*I]
    K34= 2.262609E-06 % bend y / bend z coupling
    K44= 4.274273E+03 % bend z stiffness
    }
    rigid_body{
        point_mass = 1 % changed spelling
        nodes = 1
        center_of_gravity = -0.0286 0.008395 0.0
        mass = 0.02
    inertia{
        IxX = 1.866E-07
        Ixy = 1.000E-10
        Ixz = 0.000E+00
    ```
```

                Iyy = 1.341E-06
                    Iyz = 0.000E+00
                    Izz = 1.311E-06
                    }
                }
        }
    }
    fairing_center {
        type = "vtail"
        number of elements = 1
        airfoil = NACA0018
        aero_coefficient = datatable
        airfoilfile = mh78.dat
        AoA = 0
        rigid_element = 1
        aerodynamic_spanwise_distribution = 40
        fuel_percentage =
        chord = 0.37 % Single value is used for
                        % constant chord length
                        % The user may specify
                                % at each Keypoint
    crosssection {
        reference axis= 0.6093 0%0 0%
        mass_distribution= 1.0e-8 % (mass units)/(unit span)
        inertia {
            Ixx= 1.0e-8
            Ixy= 0
            Ixz= 0
            Iyy= 1.0e-8
            Iyz= 0
            Izz= 1.0e-8
        }
        stiffness { % Be Set to rigid. These numbers
    are dummy
K11= 5.390E+07 % extension stiffness [E*A]
K12= 0 % extension twist coupling
K13= 0 % extension bend y coupling
K14= 0 % extension bend z coupling
K22= 5.390E+07 % twist stiffness [G*J]
K23= 0 % twist / bend y coupling
K24= 0 % twist / bend z coupling
K33= 5.390E+07 % bend y stiffness [E*I]
K34= 0 % bend y / bend z coupling
K44= 5.390E+07 % bend z stiffness
}
rigid_body{
point_mass = 2 % changed spelling
nodes = 1 2
center_of_gravity{
cgx{
0% 0.0125 % 0.0125 % center pod battery
0%-0.0031
}
cgy{
0.0591 % 0.0591 % center pod battery
0.0431

```
```

    }
    cgz{
                        -0.0689 %-0.0689 % center pod battery
                        0.0116
    }
    }
    mass{
        0.3960
        1.0248
        }
        inertia{
        Ixx{
            1.160E-03
            1.476E-02
        }
        Ixy{
            0.000E+00
                    2.322E-04
        }
        Ixz{
            0.000E+00
            2.267E-05
        }
        Iyy{
            9.485E-05
            2.816E-03
        }
        Iyz{
            0.000E+00
            4.500E-04
        }
        Izz{
            1.098E-03
            2.503E-04
            }
        }
        }
        }
    }
fairing_up_right {
type = "vtail"
number of elements = 1
airfoil = NACA0018
aero_coefficient = datatable
airfoilfile = mh78.dat
AoA = 0
rigid_element = 1
aerodynamic_spanwise_distribution = 40
fuel_percentage =
chord = 0.37 % Single value is used for
% constant chord length
% The user may specify
% at each Keypoint
crosssection {
reference axis= 0.6093 0%0 0%
mass_distribution= 1.0e-8 % (mass units)/(unit span)

```
\%
values
```

inertia {
IxX= 1.0e-8
Ixy= 0
Ixz= 0
Iyy= 1.0e-8
Iyz= 0
IzZ= 1.0e-8
}
stiffness { % Be Set to rigid. These numbers
K11= 5.390E+07 % extension stiffness [E*A]
K12= 0 % extension twist coupling
K13= 0 % extension bend y coupling
K14= 0 % extension bend z coupling
K22= 5.390E+07 % twist stiffness [G*J]
K23= 0 % twist / bend y coupling
K24= 0 % twist / bend z coupling
K33= 5.390E+07 % bend y stiffness [E*I]
K34= 0 % bend y / bend z coupling
K44= 5.390E+07 % bend z stiffness
}
rigid_body{
point_mass = 2 % changed spelling
nodes = 1 2
center_of_gravity{
cgx{
0.0125 % 0.0125 % right pods battery
-0.0062
}
cgy{
0.0591 % 0.0591 % left pods battery
0.0662
}
cgz{
-0.0689 %-0.0689 % right pods battery
0.0066
}
}
mass{
0.3960
1.0571
}
inertia{
1.160E-03
1.134E-02
}
Ixy{
0.000E+00
-1.212E-03
}
Ixz{
0.000E+00
1.055E-05
}
Iyy{
9.485E-05

```
are dummy
```

                                    3.209E-03
            }
            Iyz{
                        0.000E+00
                        4.595E-05
                    }
            Izz{
                1.098E-03
                        8.484E-03
            }
                }
                }
        }
    }
fairing_up_left {
type = "vtail"
number of elements = 1
airfoil = NACA0018
aero_coefficient = datatable
airfoilfile = mh78.dat
AoA = 0
rigid_element = 1
aerodynamic_spanwise_distribution = 40
fuel_percentage =
chord = 0.37 % Single value is used for
% constant chord length
% The user may specify
% at each Keypoint
crosssection {
reference axis= 0.6093 0%0 0%
mass_distribution= 1.0e-8 % (mass units)/(unit span)
inertia {
Ixx=1.0e-8
Ixy= 0
Ixz= 0
Iyy= 1.0e-8
Iyz= 0
Izz= 1.0e-8
}
stiffness { % Be Set to rigid. These numbers
are dummy
K11= 5.390E+07 % extension stiffness [E*A]
K12= 0 % extension twist coupling
K13= 0 % extension bend y coupling
K14= 0 % extension bend z coupling
K22= 5.390E+07 % twist stiffness [G*J]
K23= 0 % twist / bend y coupling
K24= 0 % twist / bend z coupling
K33= 5.390E+07 % bend y stiffness [E*I]
K34= 0 % bend y / bend z coupling
K44= 5.390E+07 % bend z stiffness
}
rigid_body{
point_mass = 2 % changed spelling
nodes = 1 2
center_of_gravity{

```
```

    cgx{
                        -0.0125 %-0.0125 % left pods battery
                        0.0062
            }
            cgy{
                        0.0591 % 0.0591 % left pods battery
                        0.0662
            }
            cgz{
                        -0.0689 %-0.0689 % left pods battery
                        0.0066
            }
        }
        mass{
            0.3960
            1.0571
        }
        inertia{
            Ixx{
            1.160E-03
            1.134E-02
        }
        Ixy{
            0.000E+00
            -1.212E-03
        }
        Ixz{
            0.000E+00
            1.055E-05
        }
        Iyy{
            9.485E-05
            3.209E-03
        }
        Iyz{
            0.000E+00
            4.595E-05
        }
        Izz{
            1.098E-03
            8.484E-03
        }
        }
        }
        }
        }
    }
    }
Loads {
frame = body_follower % or body_follower or
inertial
load_vec{
% [(1) (2) (3) (4) (5) (6) OPTIONAL (7) OPTIONAL (8)]
% (1): load type (force)
% (2): member designation
% (3): location type(keypoint or node)

```
```

    % (4): location number
    % (5): cartesian direction
    % (6): time-independent value
    % (7): time-independent value (OPTIONAL)
    % (8): start time (OPTIONAL)
    % (9): stop time (OPTIONAL)
    Mot1 = force PODC node 1 y
    1.381910189857558%1.393017135044694%1.397558812228706
%1.179272806499928%2.076274838533569 -0.5*sin(2*pi/0.10*(t-0.01))
0.01 0.11
Mot2 = force POD1up node 1 y
1.381910189857558%1.393017135044694%1.397558812228706
%1.179272806499928%2.076274838533569 -0.5*sin(2*pi/0.10*(t-0.01))
0.01 0.11
Mot3 = force POD2up node 1 y
1.381910189857558%1.393017135044694%1.397558812228706
%1.179272806499928%2.076274838533569 -0.5*sin(2*pi/0.10*(t-0.01))
0.01 0.11
Mot4 = force POD3up node 1 y
1.381910189857558%1.393017135044694%1.397558812228706
%1.179272806499928%2.076274838533569 -0.5*sin(2*pi/0.10*(t-0.01))
0.01 0.11
Mot5 = force POD4up node 1 y
1.381910189857558%1.393017135044694%1.397558812228706
%1.179272806499928%2.076274838533569 -0.5*sin(2*pi/0.10*(t-0.01))
0.01 0.11
D1 = force PODC node 2 y -0.4408
D2 = force POD1up node 2 y -0.4408
D3 = force POD2up node 2 y -0.4408
D4 = force POD3up node 2 y -0.4408
D5 = force POD4up node 2 y -0.4408
% Fexample = force WL1 node 60 z 30*sin(20*t)
% [(1) (2) (3) (4) (5) (6) OPTIONAL (7) OPTIONAL (8)]
% (1): load type (force_dist)
% (2): member designation
% (3): starting element
% (4): ending element
% (5): cartesian direction
% (6): time-independent value
% (7): time-independent value (OPTIONAL)
% (8): start time (OPTIONAL)
% (9): stop time (OPTIONAL)
% FD1 = force_dist MB 1 20 z 50*sin(40*t)+25
% [(1) (2) (3) (4) (5) (6) OPTIONAL (7) OPTIONAL (8)]
% (1): load type (moment)
% (2): member designation
% (3): location type(keypoint or node)
% (4): location number
% (5): cartesian direction
% (6): time-independent value
% (7): time-independent value (OPTIONAL)
% (8): start time (OPTIONAL)
% (9): stop time (OPTIONAL)
% M1 = moment MB node 60 x 50
% [(1) (2) (3) (4) (5) (6) OPTIONAL (7) OPTIONAL (8)]
% (1): load type (moment_dist)
% (2): member designation

```
```

    % (3): starting element
    % (4): ending element
    % (5): cartesian direction
    % (6): time-independent value
    % (7): time-independent value (OPTIONAL)
    % (8): start time (OPTIONAL)
    % (9): stop time (OPTIONAL)
    % MD1 = moment_dist MB 9 10 z 50
    % [load type, member designation, element start, element end,
    mode, voltage value, OPTIONAL--> start time, stop time,...] % NEED TO
COMPLETE
% VA1 = actuator_volt VA1 1 10
% [(1) (2) (3) OPTIONAL (4) OPTIONAL (5)]
% (1): load type (control_surf)
% (2): control surface designation
% (3): time-independent value
% (4): time-independent value (OPTIONAL)
% (5): start time (OPTIONAL)
% (6): stop time (OPTIONAL)
DEFTAIL1= control_surf ELR1in 0.255459746972205%-
0.797452909688008%-0.798991452122181% 12*sin(2*pi/7.4*t) %-
0.5*sin(2*pi/0.10*(t-0.01)) 0.01 0.11
DEFTAIL2= control_surf ELR1ou 0.255459746972205%-
0.797452909688008%-0.798991452122181% 12*sin(2*pi/7.4*t) %-
0.5*sin(2*pi/0.10*(t-0.01)) 0.01 0.11
DEFTAIL3= control_surf ELR2in 0.255459746972205%-
0.797452909688008%-0.798991452122181% 12*sin(2*pi/7.4*t) %-
0.5*sin(2*pi/0.10*(t-0.01)) 0.01 0.11
DEFTAIL4= control_surf ELR2ou 0.255459746972205%-
0.797452909688008%-0.798991452122181% 12*sin(2*pi/7.4*t) %-
0.5*sin(2*pi/0.10*(t-0.01)) 0.01 0.11
DEFTAIL5= control_surf ELL1in 0.255459746972205%-
0.797452909688008%-0.798991452122181% -12*sin(2*pi/7.4*t) %-
0.5*sin(2*pi/0.10*(t-0.01)) 0.01 0.11
DEFTAIL6= control_surf ELL1ou 0.255459746972205%-
0.797452909688008%-0.798991452122181% -12*sin(2*pi/7.4*t) %-
0.5*sin(2*pi/0.10*(t-0.01)) 0.01 0.11
DEFTAIL7= control_surf ELL2in 0.255459746972205%-
0.797452909688008%-0.798991452122181% -12*sin(2*pi/7.4*t) %-
0.5*sin(2*pi/0.10*(t-0.01)) 0.01 0.11
DEFTAIL8= control_surf ELL2ou 0.255459746972205%-
0.797452909688008%-0.798991452122181% -12*sin(2*pi/7.4*t) %-
0.5*sin(2*pi/0.10*(t-0.01)) 0.01 0.11
DEFAilR = control_surf AilR 0 %-25*sin(2*pi/5*t)% 0.1 10
DEFAilL = control_surf AilL 0 %-25*sin(2*pi/5*t)% 0.1 10
}
}
Simulation {
mode = "new"
type = "dynamic"
% Model Construction Parameters
structural damping = 1e-4 % Structural damping
parameter

```
```

% (set to 0 for no
structure
first mode damping = -1e-4 % First mode damping (set
to
% Steady State Simulation Parameters
sssim{
sim_type = "nonlinear" % or "linearized"
relative tolerance = .001 % Relative tolerance for
static
% solution convergence
numerical damping = . }8\quad%\mathrm{ Numerical damping
parameter
max iterations = 100
iterations
state
% negative value to use the
% given alphD)
% for static solution
% Maximum number of
% allowed in each steady
% solution
}
% Time Simulation Parameters
timesim{
integration_type = "Gen-Alpha" %"Trapz"% or
sim_type = "linear" % "nonlinear" or "linear" /
"reduced_order"
time_duration = 15
time_step = 0.001 % or time_divisions=4000
% restart_filename = "wbt_smpl" % ??????
rho_inf_1 = 0.999
rho_inf_2 = 0.999
time_step_save = 100
start_time_flag = 0 % put a 1 to start from previous
conditions fresh simulations require 0
n_sub_add_time_step = 1
error_states_0 = []
gust_input = 0
local_wrinkling = 0
ref_val_1 = 1e10
ref_val_2 = 1e10
time_sim_tol = 1e1
no_rigidbody_dof = 0
}
% Flutter Analysis Parameters
flutsim{
flight_index = 5 % Flight indices where
vehicle
% stability is calculated
altitude = 30 30 30 30 30
% Altitudes at each index
fuel_mass = 0 0 0 0 0
% Fuel mass
body_angle = 2.205322913566195 -0.045987813505220 -
1.443354591065910-2.368166336699205 -3.011227170417016
% Body angle will come from
trim solution and have same number of inputs as speeds sep by spaces

```

```

        Mot2 4 0.1
        Mot3 4 0.1
        Mot4 4 0.1
        Mot5 4 0.1
        DEFTAIL1 2 0.1 % CS name, initial guess, increment
        DEFTAIL2 2 0.1 % CS name, initial guess, increment
        DEFTAIL3 2 0.1 % CS name, initial guess, increment
        DEFTAIL4 2 0.1 % CS name, initial guess, increment
        DEFTAIL5 2 0.1 % CS name, initial guess, increment
        DEFTAIL6 2 0.1 % CS name, initial guess, increment
        DEFTAIL7 2 0.1 % CS name, initial guess, increment
        DEFTAIL8 2 0.1 % CS name, initial guess, increment
        }
    }
    }
Screen Output{
refgeom{
undeformed_geometry = 1
sketch_plot = 1
color_style = "gray" % "spring" or "summer" or
"autumn" or "winter" or "gray"
}
sssim{
static_deformed_geometry = 1
no_force_lines = 0
text = 1
print_lift_moment = 1
figure_position = 0.05 0.05 0.60 0.60
figure_color = 0
view = 160 45
animate_response = 1
movie
iteration_output = 1
}
timesim{
time_step_output = 1
iteration_output = 1
progress_bar = 0
}
flutsim{
plot_poles = 0
}
modalsim {
numberofmodes = 10 % Number of modes to be
displayed on screen
scale = 1 % Factor to scale the mode
shapes NOTE: No normalization is done with the modes
}
trimsim{
}
print_to_file{
stiffness_matrix = 1
interial_matrix = 1
trim_input = 1
trim_output = 1
modal_analysis = frequency
}

```
```

% generate_input_treeI = 1
% generate_input_treec = 1
% response_plot {
% keypoint 2 pos_z
% keypoint 2 vel_z
% }
% load_plot = FL1 F1
}
File Output{
% Time Simulation File Output Request
timesim{
bframe_flight_path = 1
bframe_flight_velocity = 1
euler_\overline{angles = 1}
displacement{
WR4 node 9
WR4 node 6
WR4 node 3
WR3 node 6
WR3 node 3
WR2 node 6
WR2 node 3
WR1 node 6
WR1 node 3
WR1 node 1
WL4 node 9
WL4 node 6
WL4 node 3
WL3 node 6
WL3 node 3
WL2 node 6
WL2 node 3
WL1 node 6
WL1 node 3
WL1 node 1
}
displacement{
all
}
displacementsort = "node" % "node" or "time"
liftdist{
all
}
}
}

```

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\begin{tabular}{|c|c|c|c|c|c|c|c|}
\hline \multicolumn{7}{|c|}{REPORT DOCUMENTATION PAGE} & Form Approved OMB No. 074-0188 \\
\hline \multicolumn{8}{|l|}{he public reporting burden for this collection of information is estimated to average 1 hour per response, including the time for reviewing instructions, searching existing data sources, gathering and maintaining the data needed, and completing and reviewing the collection of information. Send comments regarding this burden estimate or any other aspect of the collection of information, including suggestions for reducing this burden to Department of Defense, Washington Headquarters Services, Directorate for
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\hline \multicolumn{3}{|l|}{1. REPORT DATE (DD-MM-YYYY)
16 June 2011} & \multicolumn{4}{|l|}{\multirow[t]{2}{*}{2. REPORT TYPE Master's Thesis}} & \begin{tabular}{l}
3. DATES COVERED (From - To) \\
March 2010 - June 2011
\end{tabular} \\
\hline \multicolumn{6}{|l|}{\multirow[t]{3}{*}{\begin{tabular}{l}
4. TITLE AND SUBTITLE \\
Simulations for the Test Flight of an Experimental HALE Aircraft
\end{tabular}}} & \multicolumn{2}{|l|}{} \\
\hline & & & & & & \multicolumn{2}{|l|}{5b. GRANT NUMBER} \\
\hline & & & & & & \multicolumn{2}{|l|}{5c. PROGRAM ELEMENT NUMBER} \\
\hline \multicolumn{6}{|l|}{\multirow[t]{3}{*}{\begin{tabular}{l}
6. AUTHOR(S) \\
Brooke E. Kaszynski, \(2^{\text {nd }}\) Lieutenant, USAF
\end{tabular}}} & \multicolumn{2}{|l|}{5d. PROJECT NUMBER} \\
\hline & & & & & & \multicolumn{2}{|l|}{5e. TASK NUMBER} \\
\hline & & & & & & \multicolumn{2}{|l|}{5f. WORK UNIT NUMBER} \\
\hline \multicolumn{7}{|l|}{\begin{tabular}{l}
7. PERFORMING ORGANIZATION NAMES(S) AND ADDRESS(S) \\
Air Force Institute of Technology \\
Graduate School of Engineering and Management (AFIT/EN) \\
2950 Hobson Way, Building 640 \\
WPAFB OH 45433-8865
\end{tabular}} & \begin{tabular}{l}
8. PERFORMING ORGANIZATION REPORT NUMBER \\
AFIT/GAE/ENY/11-J02
\end{tabular} \\
\hline \multicolumn{7}{|l|}{\begin{tabular}{l}
9. SPONSORING/MONITORING AGENCY NAME(S) AND ADDRESS(ES) \\
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\end{tabular}} & \begin{tabular}{l}
10. SPONSOR/MONITOR'S ACRONYM(S) \\
AFRL/RBSD \\
11. SPONSOR/MONITOR'S REPORT NUMBER(S)
\end{tabular} \\
\hline \multicolumn{8}{|l|}{12. DISTRIBUTION/AVAILABILITY STATEMENT APPROVED FOR PUBLIC RELEASE; DISTRIBUTION UNLIMITED.} \\
\hline \multicolumn{8}{|l|}{\begin{tabular}{l}
13. SUPPLEMENTARY NOTES \\
This material is declared a work of the U.S. Government and is not subject to copyright protection in the United States.
\end{tabular}} \\
\hline \multicolumn{8}{|l|}{14. abstract Recent events, such as the crash of NASA's Helios aircraft during a test flight, show that more must be known about the nonlinear control of HALE aircraft. Shearer, Cesnik and their co-workers have developed a code that is a practical solution to the coupled nonlinear aeroelasticity and flight dynamics of very flexible aircraft called the University of Michigan's Nonlinear Aeroelastic Simulation Toolbox (UM/NAST). They are also in the process of developing a model HALE aircraft called X-HALE which will be used to validate this code experimentally. This research performs flight simulations with UM/NAST so as to make predictions about X-HALE's future test flights and subsequently uncover the strengths and weaknesses of UM/NAST when X-HALE is finally flown. These simulations include simulations of straight and level flight and rolling flight. Rolling simulations involve periodic changes in the angle of the ailerons. Both the 6 meter and the 8 meter models of X-HALE are studied. Two control models are compared. These include the linear and non-linear models of UM/NAST.} \\
\hline \multicolumn{8}{|l|}{15. SUBJECT TERMS Aircraft, flexible coupling, high altitude, long endurance, HALE, UM/NAST, RPV, simulations} \\
\hline \multicolumn{3}{|l|}{16. SECURITY CLASSIFICATION OF:} & \multirow[t]{2}{*}{\begin{tabular}{l}
17. LIMITATION OF ABSTRACT \\
uU
\end{tabular}} & \multirow[t]{2}{*}{18.NUMBER OF PAGES 205} & \multicolumn{3}{|l|}{\multirow[t]{2}{*}{\begin{tabular}{l}
19a. NAME OF RESPONSIBLE PERSON Christopher Shearer, Lt Col, USAF 19b. TELEPHONE NUMBER (Include area code) (937) 255-1179 \\
(christopher.shearer@wpafb.af.mil)
\end{tabular}}} \\
\hline \(\underset{\text { REPORT }}{\text { a, }}\) & \({ }_{\text {ABSTRACT }}\) & \({ }_{\text {PAGE }}^{\text {c. }}{ }^{\text {THIS }}\) & & & & & \\
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