# Spatial Identification of Passive Radio Frequency Identification Tags Using Software Defined Radios 

Paul A. Cornn

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SPATIAL IDENTIFICATION OF
PASSIVE RADIO FREQUENCY IDENTIFICATION TAGS USING SOFTWARE DEFINED RADIOS

THESIS
Paul A. Cornn, Captain, USAF
AFIT/GCE/ENG/12-04

DEPARTMENT OF THE AIR FORCE AIR UNIVERSITY

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# SPATIAL IDENTIFICATION OF <br> PASSIVE RADIO FREQUENCY IDENTIFICATION TAGS USING SOFTWARE DEFINED RADIOS 

## THESIS

Presented to the Faculty<br>Department of Electical and Computer Engineering Graduate School of Engineering and Management Air Force Institute of Technology<br>Air University<br>Air Education and Training Command<br>In Partial Fulfillment of the Requirements for the<br>Degree of Master of Science in Computer Engineering

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March 2012

# SPATIAL IDENTIFICATION OF <br> PASSIVE RADIO FREQUENCY IDENTIFICATION TAGS USING SOFTWARE DEFINED RADIOS 

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## Abstract

This research seeks to utilize a software defined radio for the detection and spatial identification of radio frequency identification tags. A software defined radio (SDR) is a hardware platform that provides the ability to broadcast and receive across multiple bands of the radio frequency ( RF ) spectrum, depending on the RF front end and software profile loaded on it. The focus of this research is on the spatial identification (SID) of passive radio frequency identification tags (RFID). It should be noted that this is closely related to the more common term of geo-location, but differs in a fundamental way. Geo-location focuses on obtaining the precise location of the target object, while SID aims to not only locate the object in three dimensional space, but also provide information on its velocity and bearing. This research is applicable to many areas of day-to-day operation both within the DoD and industry. Flight line safety tracking of equipment and personnel, as well as perimeter defense, are two areas that may benefit from this technology. One dual-purpose, civilian and military, application would be the tracking and locating of inventory within a warehouse. This research developed and implemented a SID process, and proved its suitability to quickly identify and locate target tags within range. A profile of the system's capabilities and limitations in the lab environment was developed including the range, sensitivity and accuracy.

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Most of all, I owe a sincere debt of gratitude to my advisor, Maj. Mark Silvius, USAF. His willingness to re-teach signal processing and patience as I worked through it allowed me to cross the finishline. In addition his calm under fire attitude excused repeated salvos of water from his students at the combat dining in. Thank you.

Paul A. Cornn

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# SPATIAL IDENTIFICATION OF PASSIVE RADIO FREQUENCY IDENTIFICATION TAGS USING SOFTWARE DEFINED RADIOS 

## I. Introduction

### 1.1 Introduction

While many technological devices are currently employed to detect intruders at the perimeter of secured areas, they are not always able to discern between a human intruder and natural occurrences. Animals, blowing grass, or heavy rain and snow can cause motion sensors and ground based radar to provide false alarms. In order to eliminate these false alarms, a perimeter security system would need to detect a truly human characteristic. One such characteristic is the array of electronic devices that we carry every day. Items such as cell phones, two-way radios, and radio frequency identification (RFID) tags can be found on just about every person. This research focuses on the development of a software defined radio solution to identify and provide the spatial identification of passive RFID tags. To this end, a spatial identification algorithm and hardware implementation is developed and validated using a demonstration platform. The ability to identify and track these devices from a distance would allow security personnel to focus their attention on viable threats - and spend less time chasing coyotes across missile fields.

### 1.2 Goals and Hypothesis

It is possible to locate and track a signal if one knows some information about it such as its center frequency and transmission power. The challenge comes when you want to identify and track a signal without prior knowledge of its transmission characteristics. Techniques such as RSSI would be able to tell you if the signal was moving towards you or away and at what bearing it is but not specifics like the range to target. Therefore, if the signal is analyzed in a different manor using Phase Difference Of Arrival (PDOA), a vector can be generated on a map showing the direction of travel, velocity, and range to target of the unknown transmitter. The goal of this research is to show, that it is possible to generate a vector for a captured signal based on analysis of its PDOA. The hypothesis of this research is that it is possible to take a transmitter that has not be previously characterized can be spatially identified using PDOA. For this research, the spatial identification method is measured against a simulation of the same transmitter modeled in three dimensional space with reflection and additive white Gaussian noise. An effective spatial identification will produce a location vector to with no more than a order of magnitude margin of error.

### 1.3 Motivation

The United States (U.S.) Department of Defense (DoD) spends millions of dollars each year securing the perimeters of its military installations and the high-valued assets within those bases. Fiber optic fence sensors, which detect vibrations, and ground based radars, which detect anomalies at the perimeter, are often put into
an alarm state by natural phenomena. High winds can cause a fence to vibrate, and wildlife or even blowing grass can cause either of these sensors to enter an alarm state. In order to tune out these false alarms, the sensitivity would have to be reduced to a level that could allow an intruder to bypass them. In addition to the false alarm problem, ground based radar has no way to uniquely identify a target once it has been spotted. Two targets can approach each other and their image will merge. Upon separation, there is no way to identify each target. An effective way to protect these areas is through the use of infrared cameras, but they cost tens of thousands of dollars each and require line-of-sight which limits their range. In addition to perimeter security, this technology could be adapted for safety and logistics applications. It stands to reason, that if we can identify and track an unknown transmitter entering the base, we could track known transmitters within areas of the base. In this way, we could tag vehicles, workers, and even tools along the flight line. This would allow a clear picture of where personnel are, if they are where they are supposed to be, and even detect possible accidents before they happen. Now, in addition to a painted "red line" that has to be physically watched by Security Forces, a virtual line would also exist. Some tags would be permitted to cross it at given times, while other tags would never be allowed into this exclusion zone. I propose a new way of looking at both the security and safety problems, by expanding the way that we locate and track spurious emitters. In particular, I look at Radio Frequency Identification (RFID) tags. These tags are appealing, because many people carry them every day without realizing it. They are included in some Department of Defense (DoD) Common Access Cards (CAC),

Enhanced ID Driver's Licenses, US and European Passports, tags sewn into clothing to prevent theft, and even casino poker chips. While we cannot count on a potential intruder to carry a pocketful of tagged poker chips while sneaking onto the flight line, these tracking techniques will be applicable to a large range of emitters from RFID tags to cell phones, Bluetooth, WiFi, and walkie-talkies. The flexibility of this approach comes from two areas: the spatial identification (SID) technique chosen, and the hardware on which it is implemented.

### 1.4 Materials and Equipment

For this research, I have chosen to use a software defined radio (SDR). A SDR incorporates many of the traditional hardware parts of a radio such as mixers, filters, modulators, and demodulators, and implements them in software on a PC, a modular daughtercard, or an embedded field programable gate array (FPGA). An SDR radio that is an RFID tag reader, can easily be reprogrammed, even from a distance, into a walkie-talkie repeater or some other use. In this way, one SDR could be used to track many of the devices listed above, allowing our security posture to rapidly adapt to the environment in which they are operating. Standard EPC Generation 2 RFID tags, for example, operate at 915 MHz in North America and 850 MHz in the European Union [1]. If we used commercial readers, the system built for stateside deployment would have to be redesigned for the European hardware. However, a SDR would simply need a quick code change or possibly even a menu choice by the operator.

This flexibility also provides a level of cost savings. A SDR can be bought for under a thousand dollars, while consumer level RFID readers start at two thousand dollars.

### 1.5 Methodology

To complete the characterization of the RFID tag transaction, we configured the SDR as a listener that captures the transaction between the commercial reader and the tag. In this way we can use the commercial reader to read the tag and use the SDR to record the electronic conversation from different angles and distances to both the reader and the tag. Our initial setup of this configuration seperates the reader antennas and the tag by one meter, with the SDR antenna positioned directly between them to capture the transaction. In this way, we are able to examine the Alien 9800 commercial reader's output and the log file from the SDR listener, as seen in Figure 1.1, to find the query, query repeat (QREP), and acknowledgements (ACK) of the tag. The times listed in the left column are in seconds and taken from the system time. For the first query at 0.627 seconds, I had removed all tags from within range by obstructing the stationary tag with an anti-static bag. As a result, the reader sends all six Qrep slot advertisements, explained in further detail in Chapter 3 , before starting a new query. At the 0.725 seconds query, the tag was visible to the reader and you can see its response at 0.806 seconds. The low latency evident in this response further illustrates the issue with using TDOA to calculate a RFID tags SID. This system also has the benefit of reporting tag errors in a separate tag log file. In this file, we record read/response errors of the tag reads. The most common error

```
56493.432
56493.624
56493.627
56493.628
56493.629
-
56493.720
56493.721
56493.722
56493.723
56493.725
56493.726
56493.727
56493.728
-
56493.803
56493.804
56493.806
    POWER UP
    POWER UP
    QUERY
    QREP
    QREP
    QREP
    QREP
    QREP
    QREP
    QUERY
    QREP
    QREP
    QREP
    QREP
    QREP
    ACK
```

Figure 1.1: SDR Listener Log
is a cyclic redundancy check (CRC) error in which only a portion of the tag ID is received. The next step is to modify the flow graph of the listener above to not only listen for the interaction, but to pipe the $I$ and $Q$ data from the interaction to a file for analysis in MATLAB. From that pointa system can map the phase interaction of the read and response of the tag at different known locations and apply the phase based SID models that are discussed in Chapter 2.

### 1.6 Scope

There are three portions of the phase based SID model: Time Domain Phase Difference of Arrival (TD-PDOA), Frequency Domain Phase Difference of Arrival (FD-PDOA), and Spatial Domain Phase Difference of Arrival (SD-PDOA) [7]. Each of these three domains provides us with a different portion of the SID puzzle. TDPDOA provides us with an angular velocity of the tag relative to the reader, or how
fast it is moving towards or away from the reader. FD-PDOA, much like traditional radar or sonar, provides a distance of the tag to the reader but due to the stationary antenna used in our experiments it does not provide a direction. This direction, or bearing, to the tag can be provided by the SD-PDOA. For this research effort I focus on TD-PDOA and FD-PDOA.

## II. Background

### 2.1 Introduction

The commercial use of the DoD Global Positioning System (GPS) has brought awareness of geolocation to all corners of the population. The desire by commanders to have real time data on both friendly and opposing forces is ever growing. The tracking of friendly forces can be achieved in many ways, but is simplified by having them carry a tracking device. RFID tags provide a unique challenge for geo-location. The tags work by modulating the signal they receive and reflecting back to a reader. Passive tags, the focus of this research, does this without the aid of an internal power source. They provide a relatively short range communication channel of only about 30 feet in commercial applications when implemented in the $902-928 \mathrm{MHz}$ band [1]. The use of passive tags is further complicated by the fact that this band is unlicensed in the United States, so noise floor can vary greatly based on the location [8]. This chapter provides a background on the geo-location techniques available today, an overview of RFID tags, and the SDR radios that can be used to track them. Finally, a survey of related research is presented.

### 2.2 Geo-Location Techniques

There are three primary geo-location techniques in use today. The two most popular are Time Difference of Arrival (TDOA) and Receive Signal Strength Indication (RSSI). The third method, Phase Difference of Arrival (PDOA), is not as widely used but, is well suited for the spatial identification of uncooperative targets.


Figure 2.1: Time Domain Of Arrival Illustration
2.2.1 Time Difference of Arrival. TDOA is the most commonly used method of geo-location. It is the basis for the GPS system and receivers are embedded in everything from mobile phones to dog collars [9]. TDOA uses the difference in arrival times from multiple, at least three, transmitters to triangulate a target's position. In order to achieve this, several pieces of information must be known. First is the exact location of each transmitter. In the case of GPS, your receiver knows where each satellite is in geostationary orbit over a specific latitude and longitude. Second is the propagation delay of the signal in the transmission medium. GPS uses a radio signal through the atmosphere, but this could just as easily be a sound wave through water such as SONAR interaction with transponders. Given these two data points, the receiver then calculates the distance from each of the transmitters. When plotted, these distance will intersect at a point, or the location of the receiver, as illustrated in Figure 2.1 by the star. Accuracy of TDOA is increased by the availability of additional transmitters and the modeling of propagation delay for the system. As we all know by the success of GPS, this technique can rapidly provide the location of
a receiver to within a couple of feet. The problem with using TDOA for the perimeter defense senerio is that an intruder is not going to be carrying a GPS receiver and will not be willingly transmiting their location to Security Forces.

Passive RFID tag geo-location based on TDOA is not feasible due to the limited range of RFID tags. A GPS signal travels, at a minimum, thirty five thousand kilometers to the receiver. The signal from tag to receiver can travel, at most, 20 meters. At this distance, the receiver would have to be able to detect a nanosecond difference in the arrival of the signals, to calculate the target's location within a meter. Which is why TDOA is not suitable for passive RFID tracking.

### 2.2.2 Receive Signal Strength Indicator. RSSI uses the known propagation

 properties of a signal in the transmission medium to determine the distance from the sensor. There are two ways that RSSI can be used. The first is tracking a target with a transmitter. Multiple sensors receive the signal from the target transmitter and determine the distance to the target. The point where those distances intersect is the location of the target, much like TDOA. The shortcoming of this approach is that you need to know, or be able to calculate, the transmission power of the target transmitter. For the identification and tracking of a friendly target this is just a matter of procedure. For an unknown target multiple sensors would have to work together to model the decay of the received signal strength. The second RSSI technique is more applicable for such a target. In this technique a grid of transmitter and receiver pairs is set up and the signal strength is baselined. When an object moves in between oneof the pairs, the signal will be degraded. Based on experimental data from [10], one can then identify the size and rough shape of the object. The downside of this method is the extensive setup and calibration of the system. Even an active transmitter from the first method will be affected by environmental changes as demonstrated in the LANDMARC system [11].
2.2.3 Phase Difference of Arrival. Given the difficulties stated above with more traditional geo-location techniques, the research has shifted to using the phase of the modulated signal as a means to find the SID of a tag [7]. The phase of the signal is a preferred method for spatial identification of passive RFID tags, because it is not dependant on the power incident to the tag. In this way, we are able to isolate one of the variables in the spatial identification problem, and focus on those items that allow us to place the tag in three-dimensional space. Nikitin Et al. look at three different techniques; each one calculates part of the puzzle [7].
2.2.3.1 Time Domain PDOA. Time Domain PDOA (TD-PDOA) allows for the estimation of a velocity vector with respect to the reader. This method calculates this vector as the derivative of the phase with respect to time, as seen in Equation 2.1. Where c is the speed of light, f is the carrier frequency and $\pi$ is the phase of the signal. The heart of this method is to compare the phase of a received signal at two points in time. If we know, or can calculate, the center frequency of a signal, we can predict the phase of the second sample to be relative to the first. When the target, an RFID tag in this case, is moving, the phase shifts slightly from
the expected value. This shift then allows us to calculate a velocity vector. This vector is relative to the receive antenna of the sensor and represents the velocity of the target when it is moving away from the antenna.

$$
\begin{equation*}
V=\frac{-c}{4 \pi f} \cdot \frac{\delta \phi}{\delta t} \tag{2.1}
\end{equation*}
$$

2.2.4 TD-PDOA Derivation. Inspection of the signal phase on arrival in the time domain allows us to calculate the velocity of the target relative to the sensor, i.e. how fast it is moving towards or away from it. For a signal in free space, this is represented by the phaser formula in Equation 2.2 where $k$ is the wave-vector defined as $k=\frac{2 \pi f}{c}$. In this way, $d 1$ and $d 2$, can be used to calculate the phase change due to the distance traveled, for each moment in time. This is shown in Figure 2.2. If the distance is constant between two separate points in time, then the velocity is zero. However, if there is a change in the distance, then the target has moved some distance between the two samples.

$$
\begin{equation*}
\phi_{\text {prop }}=-2 k d \tag{2.2}
\end{equation*}
$$

To derive Equation 2.1, it is best to start with the definition of velocity as seen in Equation 2.3. The term $\frac{\Delta d}{\Delta t}$ can be expanded into the difference in the distance, divided by the difference in the time of each sample, as seen in Equation 2.4. In the next step, both sides of the equation are multiplied by $-\frac{4 \pi f}{-c}$, as seen in Equation 2.5.


Figure 2.2: Time Domain PDOA Illustration

Equation 2.6 substitutes the wave-vector, $k$, for a portion of the multiplicand from the previous step. The distributive property is applied and the result, Equation 2.7, contains two terms that equal the right side of the phasor formula. The angles $\phi_{1}$ and $\phi_{2}$ can then be substituted for these terms as seen in Equation 2.8. After solving for $V_{r}$ and a substitution for $\frac{\phi_{1}-\phi_{2}}{t_{1}-t_{2}}$, we arrive at Equation 2.10. If the target is moving sufficiently fast and we can sample such that $\Delta t \rightarrow 0$, we arrive at Equation 2.1.

$$
\begin{align*}
V_{r} & =\frac{\Delta d}{\Delta t}  \tag{2.3}\\
V_{r} & =\frac{d_{1}-d_{2}}{t_{1}-t_{2}}  \tag{2.4}\\
V_{r} \cdot-\frac{4 \pi f}{-c} & =-\frac{4 \pi f}{-c} \cdot \frac{d_{1}-d_{2}}{t_{1}-t_{2}}  \tag{2.5}\\
V_{r} \cdot-\frac{4 \pi f}{-c} & =-2 k \frac{d_{1}-d_{2}}{t_{1}-t_{2}}  \tag{2.6}\\
V_{r} \cdot-\frac{4 \pi f}{-c} & =\frac{-2 k d_{1}--2 k d_{2}}{t_{1}-t_{2}}  \tag{2.7}\\
V_{r} \cdot-\frac{4 \pi f}{-c} & =\frac{\phi_{1}-\phi_{2}}{t_{1}-t_{2}}  \tag{2.8}\\
V_{r} & =\frac{-c}{4 \pi f} \cdot \frac{\phi_{1}-\phi_{2}}{t_{1}-t_{2}}  \tag{2.9}\\
V_{r} & =\frac{-c}{4 \pi f} \cdot \frac{\Delta \phi}{\Delta t} \tag{2.10}
\end{align*}
$$

Equation 2.10 makes the assumption that the TX (Reader) and RX (Sensor) are co-located. In this way the distance to and from the tag are equal. If the TX/RX antennas are not co-located a correction for the difference in the transmission path will have to be added to the formula. Figure 2.3 illustrates this case. To correct for this we will need to find the angle of arrival for each sample. This value, $\theta$, can be found using Spatial Domain PDOA (SD-PDOA) as seen in Section 3.1.5 for the sample taken at $t 1$ and the sample at $t 2$. With the assumption that the distance to the reader is greater than one wavelength the phase change due to the different propagation paths is $\frac{2 \pi}{\lambda}\left(\sin \theta_{2}-\sin \theta_{1}\right)$. Including this term in Equation 2.10 gives us an updated formula seen in Equation 2.11.


Figure 2.3: Time Domain PDOA Illustration

$$
\begin{equation*}
V_{r}=\frac{-c}{4 \pi f} \cdot \frac{\Delta \phi-\left(\frac{2 \pi f}{c}\left(\sin \theta_{2}-\sin \theta_{1}\right)\right)}{\Delta t} \tag{2.11}
\end{equation*}
$$

2.2.4.1 Frequency Domain PDOA. Frequency Domain PDOA (FDPDOA) allows one to measure the distance to the tag by measuring the phase shift in different frequencies. This is calculated by taking the derivative of the phase with respect to frequency as seen in Equation 2.12.

$$
\begin{equation*}
d=\frac{-c}{4 \pi} \cdot \frac{\delta \phi}{\delta f} \tag{2.12}
\end{equation*}
$$

In order to do this, we sample the received signal at its center frequency, 915 MHz in the case of RFID tags, and a frequency just off center, say 914 MHz . A good analogy for how this works is to compare two tires of different sizes. Tire one has a circumference of one meter while tire two meters has a circumference of 0.75 meters,


Figure 2.4: Frequency Domain PDOA Illustration
each starting with a line painted on them pointed at the ground. If we roll both of them two linear meters, tire one will stop with its mark pointed at the ground, while tire two's mark will be about sixty degrees from top dead center, as seen in Figure 2.4. By comparing where the mark, symbolic of the tire's phase is when the wheels arrive, we can calculate the distance traveled. Due to the fact that these samples are taken at the same moment in time, this technique is available even if the target is not moving, unlike TD-PDOA.
2.2.5 FD-PDOA Derivation. FD-PDOA, like TD-PDOA, uses the physical principle that the propagation of sinusoids of different frequencies, and hence different wavelengths, propagate at different rates through space. To compare the relative phase difference in the received signals to calculate a distance to the transmission source. If two frequencies start at the same point, and at the same phase, as the response from the tag would they will arrive at the sensor with aphase difference, $\Delta \phi$. This effect is illustrated in Figure 2.5. In this research, the phase difference is found


Figure 2.5: Frequency Domain PDOA Illustration
using the center carrier frequency and one of the side lobes of the FFT discussed in Section 2.3 with the phase of this lobe calculated in the same manner as the phase of the center frequency.

To derive the FD-PDOA formula, Equation 2.12, we first define the expected phase in terms of the two frequencies, $f_{1}$ and $f_{2}$, and the distance to the tag, $d_{t a g}$. This process can be seen in Equations 2.13-2.20. Subtracting Equation 2.20 from Equation 2.19 results in Equation 2.21 which combines the two phase terms into a single equation. As was done in the derivation of the TD-PDOA formula, the term $\phi_{2}-\phi_{1}$ and $f_{2}-f_{1}$ can now be represented as a delta of the phase and frequency, respectively, as seen in Equation 2.22. Solving for $d_{t a g}$ results in Equation 2.23. Once again, if we were able to get $\Delta f$ to approach zero, we would end in our given FDPDOA seen in Equation 2.12.

$$
\begin{align*}
\phi_{1} & =-2 k_{1} d_{t a g}  \tag{2.13}\\
\phi_{2} & =-2 k_{2} d_{t a g}  \tag{2.14}\\
k_{1} & =\frac{2 \pi f_{1}}{c}  \tag{2.15}\\
k_{2} & =\frac{2 \pi f_{2}}{c}  \tag{2.16}\\
\phi_{1} & =-2\left(\frac{2 \pi f_{1}}{c}\right) d_{t a g}  \tag{2.17}\\
\phi_{2} & =-2\left(\frac{2 \pi f_{2}}{c}\right) d_{t a g}  \tag{2.18}\\
\phi_{1} & =\frac{-4 \pi f_{1}}{c} d_{t a g}  \tag{2.19}\\
\phi_{2} & =\frac{-4 \pi f_{2}}{c} d_{t a g}  \tag{2.20}\\
\phi_{2}-\phi_{1} & =-\frac{4 \pi d_{t a g}}{c}\left(f_{2}-f_{1}\right)  \tag{2.21}\\
\Delta \phi & =-\frac{4 \pi d_{t a g}}{c} \Delta f  \tag{2.22}\\
d_{t a g} & =-\frac{c}{4 \pi} \frac{\Delta \phi}{\Delta f} \tag{2.23}
\end{align*}
$$

### 2.2.5.1 Spatial Domain PDOA. Spatial Domain PDOA (SD-PDOA)

allows for the estimation of the bearing, or the angle of arrival. This technique differs from the other two in that it requires at least two antennas to calculate the desired result. By spacing the two antennas apart the signal received will have to travel two different distances. Much like the tire metophor above, the signal will arrive at the two locations at a different phase. Dividing by the distance between the two antennas, $a$, the difference in phase will provide theta, or the bearing from antenna one to the
target tag. Several considerationsmust be calculated in when this measurement is performed. The phase progression within the transmission lines of the two antennas will have to be accounted for very carefully.

$$
\begin{equation*}
\theta=\arcsin \left(\frac{-c}{2 \pi f} \cdot \frac{\phi_{2}-\phi_{1}}{a}\right) \tag{2.24}
\end{equation*}
$$

Analysis of the phase in the spatial domain differs from the other two in that a second receive antenna is required. In this way the phase of the arriving signal is measured at two points in space, separated by some distance, $a$. In is important that these receivers be coherent or in-phase with each other. In this research, this requirement is accomplished by using two daughter cards on the same USRP1 main board. By using coherent receivers, we only have to account for the additional phase delay due to propagation through the antennas' transmission lines of segment $a$ from Figure 2.6, because segment $b$ 's delay cancels out. If coherent receivers are not possible a correction for the propagation across $b$ and $a$ must be accounted for. The setup for this metric can be seen in Figure 2.6. Much like the inspection of the TD-PDOA, the signal travels two distinct paths. Unlike TD-PDOA, the signal departs the tag at a single point in time and travels the the receive antennas, transversing some distance $d_{1}$ or $d_{2}$. Since the length of these paths differ, the signal will arrive at RX1 and RX2 with two different phase values due to the length of the propagation channel. Through application of right triangle geometry, we can then calculate the angle of arrival of the signal to the primary sensor, RX1.


Figure 2.6: Spatial Domain PDOA Illustration
To derive the formula for the we start with the phasor formula for each of the two receive antennas and solve for $d_{1}$ and $d_{2}$. These steps can be seen in Equations $2.25-2.30$. The term $d_{2}-d_{1}$ provides us with the length of one of the legs of the right triangle created by extending a line from RX1 to a point on $d_{2}$. In this case, it is the opposite side from the angle we want to calculate, giving Equation 2.32, In the case of Figure 2.6 the result of $d_{2}-d_{1}$ is positive and will result in a positive value for $\theta$. If the difference was negative, the resulting $\theta$ would also be negative. What this means in terms of an $(x, y)$ coordinate is discussed in Section 2.3

$$
\begin{align*}
\phi_{1} & =-k d_{1}  \tag{2.25}\\
\phi_{2} & =-k d_{2}  \tag{2.26}\\
\phi_{1} & =-\frac{2 \pi f}{c} d_{1}  \tag{2.27}\\
\phi_{2} & =-\frac{2 \pi f}{c} d_{2}  \tag{2.28}\\
\phi_{1}\left(-\frac{c}{2 \pi f}\right) & =d_{1}  \tag{2.29}\\
\phi_{2}\left(-\frac{c}{2 \pi f}\right) & =d_{2}  \tag{2.30}\\
-\frac{c}{2 \pi f}\left(\phi_{2}-\phi_{1}\right) & =d_{2}-d_{1}  \tag{2.31}\\
\sin \theta & =\frac{d_{2}-d_{1}}{a}  \tag{2.32}\\
\sin \theta & =\frac{-\frac{c}{2 \pi f}\left(\phi_{2}-\phi_{1}\right)}{a}  \tag{2.33}\\
\sin \theta & =-\frac{c}{2 \pi f} \frac{\phi_{2}-\phi_{1}}{a}  \tag{2.34}\\
\theta & =\arcsin -\frac{c}{2 \pi f} \frac{\phi_{2}-\phi_{1}}{a} \tag{2.35}
\end{align*}
$$

### 2.3 Spatial Identification (SID) Solution

Sections 3.1.3 - 3.1.5 provide us with a method to extract three different metrics by analyzing the received phase of the target signal. These metrics, however, are not useful to an operator as they stand, nor do they truly spatially identify a target. This section illustrates how the metrics calculated can be translated into $(x, y)$ coordinates and an actual velocity of the target. As it stands, this system would only function


Figure 2.7: SID Solution
in a two dimensional field with the SD-PDOA being the limiting factor. The two receiver model described in Section 3.1.5 provides an angle of arrival on the ( $\mathrm{x}, \mathrm{y}$ ) plane. It would be possible to add the third dimension if another receive antenna was positioned directly above RX1 at some height $a_{z}$. Using this new receiver, a second angle of arrival, $\theta_{z}$, could be calculated using SD-PDOA with Equation 2.35. Figure 2.7 illustrates the metrics we have all ready found. The velocity relative to the sensor, $V_{r}$, is found using Equation 2.1. The distance to target, $D_{t a g}$ is found using Equation 2.12, and $\theta$ is found using Equation 2.24.

In order to translate these metrics into something that could be ploted on a map and be useful to an operator, we look at the geometry of Figure 2.7. By defining the sensor location as the origin, we can calculate an $(x, y)$ position pair that could later be overlayed to a map given a latitude, longitude for the sensor. This also lets us form a right triangle with the $x$ and $y$ offsets from the sensor as the legs and the metric $D_{\text {tag }}$ as the hypotenuse. Since we already know one of the angles, $\theta$, finding the lengths of the legs becomes an exercise in trigonometry. The $x$ value shown in Equation 2.36 is based on the fact that it is opposite the known angle, $\theta$. In a similar fashion, the $y$ value is calculated using Equation 2.37 and its relationship to $\theta$. While the $V_{r}$ metric provides us with an instantaneous value for the velocity relative to the sensor, a single value of $V_{r}$ is not sufficient to calculate an estimate of the velocity components in the $x$ and $y$ directions, $(\dot{x}, \dot{y})$. The value $V_{r}$ does provide the operator with a closing rate of the target to the sensor, and can be used to provide a sanity check on the velocities $(\dot{x}, \dot{y})$. In order to calculate this value, we would have to have at least two samples that provide both $d_{t a g}$ and $\theta$, as well as the time difference between the two samples, $\Delta t$. By applying Equations 2.36 and 2.37 to these two samples we can arrive at $x_{1}, x_{2}, y_{1}$ and $y_{2}$. Going back to the definition of velocity as discussed in section 2.2.4we arrive at Equations 2.38 and 2.39. As when calculating $V_{r}$, the smaller we are able to make $\Delta t$, the more accurate our velocity vector estimation and the sooner we detect a change in direction.

$$
\begin{equation*}
x=d_{t a g} \sin \theta \tag{2.36}
\end{equation*}
$$

$$
\begin{gather*}
y=d_{t a g} \cos \theta  \tag{2.37}\\
\dot{x}=\frac{d_{t a g 1} \sin \theta_{1}-d_{t a g 2} \sin \theta_{2}}{\Delta t}  \tag{2.38}\\
\dot{y}=\frac{d_{t a g 1} \cos \theta_{1}-d_{t a g 2} \cos \theta_{2}}{\Delta t} \tag{2.39}
\end{gather*}
$$

### 2.4 Radio Frequency Identification Tags

Radio Frequency Identification (RFID) Tags are an emerging technology whose adoption has grown immensely over the past ten years. There are two broad categories of RFID tags: active and passive. Active tags have a power source within them and when they are queried by a reader, they draw power from their internal source to respond. Examples of active tags include those used to track cargo containers within a shipyard and the automatic toll readers such as iPass of Illinois and EZPass of New York. The higher signal strength of active tags have made them more favorable to geolocation and are the basis for earlier research [11]. Passive tags harvest the power from the read signal, apply internal logic, and reflect the signal back to the reader. Due to their lower cost, passive tags are much more common in commercial applications. They can be found in the new electronic passports, enhanced driver's licenses and even retail anti-theft devices. The rest of this section describes the physical, link, and session layer communications of the passive RFID tags used in this research.
2.4.1 Symbol Encoding - Physical Layer. This section goes into greater detail of the physical layer of the EPC Gen 2 RFID tags used in this research. The encoding method, backscatter coupling, and pulse shaping is described.
2.4.1.1 On Off Keying (OOK). The EPC Gen 2 RFID reader and tags used in this research encode the query and response using On-Off Keying (OOK) [12]. OOK is a digital modulation technique that uses the absence of a carrier wave to encode data. It is a simple scheme for of Amplitude Shift Keying (ASK) and as such is sensitive to atmospheric noise and distortion in the transmission path. The biggest advantage of OOK over other forms of ASK is that it does not require phase lock between radios, which means it can be non-coherently demodulated. The implementation of RFID OOK in the UHF band is defined in ISO-IEC 1800 part 6 [1]]. One of the key characteristics of OOK is the length of a symbol. If you equate a zero and one in OOK to a dot and dash on an old telegraph line the issue becomes apparent: "was that a dot or dash that just came in." In Morse code the standard became the length of a dot, a dash being equal to three dots. ISO 1800-6 defines the standard time unit for RFID communications as a Tari. A Tari is defined as 20 microseconds with a tolerance of plus or minus 100 pulses per minute [1]. This means that a Tari must last between 19 and 21 microseconds to remain within specification. While all data is encoded in binary as either a one or zero, there are actually four symbols used in RFID communication. Aside from the before mentioned one and zero, there is a Start of Frame (SOF), and End of Frame (EOF) symbol. These symbols and their encoding can be seen in Figure 2.8. As can be seen, the four symbols are not the same duration, ranging from one to four Taris. The biggest impact of this encoding method is that the data rate is defined by the content of the frame. If we


Figure 2.8: RFID OOK Symbols [1].
look at Morse code again, six dashes would take three times longer to transmit that six dots. In RFID OOK, 16 bits of ones would take twice as long as 16 bits of zeros.

### 2.4.1.2 Backscatter Coupling. The on/off pulses for the encoding

 process in the tag are generated using backscatter coupling. The power from the reader is incident on the tag's antenna. In a normal surface, the antenna would backscatter a portion of the signal directly to the reader. In RFID tags this power provides the power up current for the logic on the tag. RFID tags also have a resistor connected in parallel to the antenna and logic circuits. Using this resistor, the load connected to the antenna can be controlled by the logic circuit. By tuning this load from high to low, the amount of power that is reflected back is varied from high to

Figure 2.9: Simple Tag Schematic [2]
low generating the OOK response. A simplified circuit diagram of this resistor layout is shown in Figure 2.9 [2].
2.4.1.3 Pulse-Interval Encoding. Given the binary nature of OOK and the data being encoded, one might expect a zero to be represented by a lack of carrier and a one to have the carrier present. While this would standardize the data rate it would cause problems in passive RFID tags. A frame with a lot of zeros would not provide sufficient power to the tag in order for it to provide a response. In light of this the symbols were designed using pulse-interval encoding (PIE). The encoding of the symbols using this PIE scheme ensures that a query from the reader, even if all zeros, will transmit at full power at least fifty percent of the time. There is now sufficient energy, given the tag is in range with a clear path, for the tag to power up and provide a response if needed. This requirement for power from the reader also adds complications in the session layer, as discussed in a later section.
2.4.1.4 Pulse Shaping. One other consideration of the encoding method is the bandwidth of the spectrum occupied by the communications. As UHF

RFID communications occurs in the unlicensed portion of the UHF spectrum, it must limit the amount of power that is evident at frequencies other than the designated carrier frequency. These frequencies are 840 MHz in Europe and 915 MHz in the United States [1]. A sharp cut off of the signal as represented in Figure 2.8, would cause a significant amount of power bleed into other frequencies, as shown in Figure 2.10. A purely digital OOK generates a rectangular pulse function as seen in the left side of Equation 2.40. The Fourier Transform of a rectangular pulse is the sinc function as seen on the right side of Equation 2.40. If the time domain pulse is first convolved with the impulse response of a pulse shaping low pass filter, the side lobes in the frequency domain will be significantly attenuated. This shaping of the symbol, as seen on the right side of Figure 2.10, attenuates the power signature in frequencies far from the carrier [3]. An example of a portion of a tag response is shown in Figure 2.11 with the digital symbols overlayed on the actual transmission. If the FFT is taken of the symbols from Figure 2.11, the power attenuation discussed earlier is evident as seen in Figure 2.12. The central spike shows the frequency that this interaction took place at, 925 MHz . This frequency is not the before mentioned 915 MHz operating frequency of the tags. This frequency is a result of a frequency hopping implementation in the reader; the tag just reflects the frequency it receives. Readers can be configured to hop frequencies within the unlicensed 900 MHz band in order to minimize interference. During the data capture portion of this research, the reader was observed to operate on frequencies ranging from 908 MHz up to 925 MHz .


Figure 2.10: RFID Symbol Shaping [3]

Figure 2.13 shows the phase of each index of the FFT. At the peak power level, 925 MHz , the phase is -0.69 radians.

$$
f[x]=\left\{\begin{array}{ll}
1 & \text { if On }  \tag{2.40}\\
0 & \text { if Off }
\end{array} \Longleftrightarrow F(\omega)=\operatorname{sinc} \frac{\omega}{2}=\frac{\sin (\pi \omega)}{\pi \omega}\right.
$$

### 2.4.2 RFID Standard Frame - Link Layer.

2.4.2.1 Reader Frame Types. Frames from the reader come in two formats, long and short. The short format command frame is 16 bits long and its structure can be seen in Table 2.1. The short format command is limited in that it can not reference an individual tag as there is no allocation for the unique identified (UID) or sub unique identifier (SUID). The UID is similar to a Media Access Control (MAC)


Figure 2.11: OOK Symbols Overlayed on Capture


Figure 2.12: Magnitude of OOK '010' Symbols


Figure 2.13: Phase of OOK '010' Symbols

| SOF | RFU | Command Code | Parameters/Flags | CRC- 5 | EOF |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 bit | 6 bits | 4 bits | 5 bits |  |

Table 2.1: $\quad$ Short Command Format
number on a network device. It begins with the manufacturer code and is followed by the individual tag's identifier. The SUID consists of only the tag's individual identifier. Due to this limitation the most common use of the short format is the QueryRep command. This command will be explained further in the next section as it relates to the communication protocol used in RFID tags. The format of the long command format is shown in Table 2.2. The longer formats SUID field enables it to issue commands to a single tag even if several are within range.

| SOF | RFU | Command <br> Code | Parameters <br> or Flags | CRC-5 | SUID | Data | Data- <br> optional | CRC-16 | EOF |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  | 1 bit | 6 bits | 4 bits | 5 bits | 40 bits | 8 bits | 8 to n | 16 bits |  |

Table 2.2: Long Command Format

| Preamble | Flags | Parameters | Data | CRC-16 |
| :--- | :--- | :--- | :--- | :--- |

Table 2.3: Tag Response Format
2.4.2.2 Tag Frame Types. The general format of the tag response frame can be seen in Table 2.3. In obvious contrast to the reader frame formats, the tag response lacks sizes for each of the fields. The lengths for each of these fields is driven by the command the tag is responding to and the state of the tag. All responses will include the SUID in the data field so the reader knows what tag it is talking to.
2.4.3 RFID Tag-Reader Interaction - Session Layer. Most commercial RFID readers work in one of two modes, Global Scroll and Inventory. The benefits and mechanisms of each mode are described in the following subsections.
2.4.3.1 Global Scroll. The first, more primitive, method is called global scroll. In this method the reader sends a single request out and all tags that receive it respond. This mode allows for more rapid reads of a single tag, but if multiple tags are in the area, only the strongest response signal is read. The trade space created by the rapid read times of a single tag make this ideal for high speed applications, where only a single tag will be within view of the reader at a time, like assembly lines. An illustration of the reader to single tag interaction is shown in Figure 2.14. In the single tag example the reader sends the query and the tag responds. All future interactions from the reader to the tag will include the tag's SUID. This prevents a new tag from entering the area and interfering in the ongoing


Figure 2.14: Global Scroll Single Tag Interaction


Figure 2.15: Global Scroll Multiple Tag Interaction
exchange. In the case of multiple tags, as shown in Figure 2.15, we can see all three tags respond. Tags two and three's responses are represented as a weaker signal by the thinner and dashed lines. In this case, the reader responds only to tag one's stronger signal, once again including tag one's SUID to let the tags know who it is talking to.
2.4.3.2 Inventory. The second read method is called inventory and is based on the Time Slotted ALOHA protocol. The original ALOHA protocol was developed at the University of Hawaii Manoa campus as a computer network topology [13]. It had no collision prevention technique. If a computer had data to send, it tried to send it. If a collision occurred, it would wait and try again at a later
point in time. Time slotted ALOHA was an improvement on this as it introduced time slots. A node could only begin transmission at the beginning of a slot, and the message had to fit inside the time slot. This improved throughput and did not require central coordination. It did require a common time reference between the nodes. This common time reference is not available in RFID tags, particularly passive tags. The solution for this was to modify the slotted ALOHA protocol to be centrally coordinated, or polled in this case. The reader serves as the central coordinator and will start an inventory round by advertising the number of slots it is using. This is an integer and can range from 1 to 1024, determination of the optimal number of slots depends on the number of tags expected to be in range. This advertisement of the number of slots occurs in the Query command message, 2.16 (a). The tags each then pick a random number between 0 and the number of slots minus 1 . This slot choice is shown in Figure 2.16 in parasynthesis after each tag. Each time the reader sends out a QueryRep short command, 2.16 (b-d), the tag increments its internal counter. When the counter and the selected slot number match the tag sends an ACK response including the tag's SUID. In Figure 2.16 (e,f) two tags had chosen slot 2 and responded to the reader in this same slot. Upon seeing the multiple backscatter responses the reader can either try to filter the stronger one out and respond to it or ignore both. Our example ignores both and sends the next QueryRep (g). Tags one and two, having not been acknowledged now await the beginning of a new inventory round where they will pick new random slots. In step (g), Tag 3 sees the new QueryRep and increments its counter to match the random slot it choose earlier and responds, (h).


Figure 2.16: Inventory Query Round

Since it is the only tag to respond in this slot the reader sends an ACK including the tag's SUID,(i), similar to the way a teacher would call on a student in a classroom. Further commands are then executed depending on the reader's configuration, (j). Once the interaction is complete and since the reader has checked all slots it will start a new inventory round, allowing tag one and two to try and report again.

### 2.5 Software Defined Radios

Software defined radios have been utilized as experimental platforms for RFID research at the University of Washington. Michael Buettner is the author of the Gen2 RFID reader and listener [14]. This software package is widely used in SDR circles as the building block for any RFID related system. Chris Paget used it when he set his RFID tag read distance record of 217 feet [15]. Mr. Buettner also used the software as a basis for several papers on RFID technology [16-18]. Of particular interest
to this research is his paper titled"A Software Radio-based UHF RFID Reader for PHY/MAC Experimentation." Buettner provides a solid background on the actual interaction of the reader and tag, as well as a software platform that can be easily modified to capture data not readily available on commercial RFID readers. The rest of this section provides an overview of the USRP1 main board and Flex 900 daughtercard used in this research.
2.5.1 USRP 1 Mainboard. The USRP 1 main board is manufactured by Ettus Research LLC as a reference design and experiment platforms for engineers and students. When paired with a daughter card it is capable of sending and receiving a wide range of signal types. The USRP 1 used in this research has been discontinued and replaced with the USRP E100 series of boards. Figure 2.17 show the internals of the USRP. In general terms it consists of: 1. FPGA; 2. Analog to Digital / Digital to Analog Converters; 3. USB Controller; and 4. Clock. Each of these subsystems is discussed at more length in the following subsections.
2.5.1.1 FPGA. The FPGA in the USRP 1 is from Altera's Cyclone family, the EP1C12 to be precise. This FPGA operates at 1.5 V and uses a 0.13 $\mu m$ manufacturing process. The EP1C12 is the second most powerful member of the Cyclone family and has 12,060 logic elements (LE) and 239,616 total RAM bits [19]. While Ettus does not make mention of the FPGA utilization of the standard USRP1 firmware in any of its documentation, a installation guide generated by UCLA students shows $92 \%$ utilization. According to the Ettus web site FAQs, the newer


Figure 2.17: USRP 1

USRP, which utilize the Spartan 3, have up to $63 \%$ of their logic elements free for user functions.

### 2.5.1.2 Analog to Digitial (ADC) / Digitial to Analog (DAC) Converter.

 The ADC/DAC subsystem of the USRP 1 is implemented in Analog Devices' MixedSignal Front-End Processor for Broadband Communications, AD9862 chip. As can be seen in Figure 2.18, each of the two chips on the main board consist of dual ADC and DAC pipelines. The ADC are 12-bit converters and are capable of processing up to 64 megasamples per second (MSPS). The DAC, while not used in this research, are 14 -bit and can handle up to 128 megasamples per second. The chip integrates a programable gain amplifier (PGA) to boost a weaker signal and maximizes the resolution of the digitized sample. The PGA can provide from 0 to 20 dB of gain in 1 dB steps. The AD9862 provides good channel isolation of greater than 80 dB between the two receive channels and greater than 90 dB between transmission and receive channels [4].2.5.1.3 USB Controller. The heart of the USB controller is the CY7C68103A integrated circuit. This chip is manufactured by Cypress and marketed as the EZ-USB FX2 USB Microcontroller. It supports the USB 2.0 standard and supports the standard's maximum data rate of 56 MBytes per second [20]. All communications between the main board and GNU Radio on the host PC take place through this controller. More recent USRP models have moved some (E100) or all (N210) of this communication to a Gigabit Ethernet port which would allow the host


Figure 2.18: ADC/DAC Functional Block Diagram [4]
computer to be located in a different location. While most of this communication is directed towards the Cyclone FPGA, direct communications with the daughter cards is possible using standard SPI and I2C bus protocols. The controller is able to run at either $48 \mathrm{MHz}, 24 \mathrm{MHz}$ or 12 MHz . In the USRP 1 , it runs at 24 MHz and has its own oscillator, the ECSR240EX.
2.5.2 Flex 900 Daughter Card. The Flex 900 daughter card used in this research contains both a receive $(\mathrm{Rx})$ and transmission $(\mathrm{Tx})$ path and is shown in Figure 2.19. The Tx capabilities of the card were not used and are omitted from this description. The key elements of the Rx path are: 1. Analog Mixer, 2. Frequency Synthesizer, 3. and Band-Pass Filters. The main function of this Rx path is to down convert the received RF signal to an intermediate frequency (IF). The band-pass filters are hard-wired LRC networks on the daughter card, and they are specifically tuned for the frequency range of the Flex 900. Similar networks would exist on other daughter cards and would be tuned for the frequency of the card. The demodulator and local oscillator are described in the following subsections.

### 2.5.2.1 Analog Mixer. The first stage mixer on the Flex 900 is im-

 plemented by Analog Devices' 0.8 GHz to 2.7 GHz Direct Conversion Quadrature Demodulator (AD8347). The functional block diagram for this self contained, surface mount, IC is shown in Figure 2.20. As is evident from the AS8347's long name the chip can process signals from 800 MHz to 2.7 GHz . The AD8347 takes the signal from the antenna and mixes it with a sinusoid from the local oscillator to provide I and

Figure 2.19: Flex 900 Daughter Card


Figure 2.20: Analog Mixer Functional Block Diagram [5]

Q channels for A-to-D conversion on the main board. The Flex 900 also utilizes the chip's integrated separate I and Q amplifiers after processing the channels through hard-wired band-pass filters. Total possible gain from the variable amplifiers and final amplifiers is 69.5 dB . The external band pass filters prior to final amplification allow the Flex 900 to remove high level out of channel noise [5].


Figure 2.21: Frequency Synthesizer Functional Block Diagram [6]
2.5.2.2 Frequency Synthesizer. The frequency synthesizer used in the first stage down conversion stage on the Flex 900 is implemented on Analog Devices' Integrated Synthesizer and VCO (ADF4360-3). The ADF4360 operates on a center frequency of 1750 MHz . It uses a divide by 2 operation to generate sinusoids with frequencies from 800 to 975 MHz . A functional block diagram can be seen in Figure 2.21 [6].

### 2.6 System Overview

The USRP 1 system is capable of transmitting and receiving on a wide range of frequencies from 1 MHz to 5 GHz depending on the daughter card installed. This research used the Flex 900 daughter card which has a frequency range of 840 to 975

MHz. The IF is limited by the 64 MSPS rate of the ADC. To meet Nyquist and frequency translation requirements the centering of the RF signal an IF range of 16 84 MHz is possible.

### 2.7 System Logical Block Diagrams

This section provides a logical view of a received signal's transition from a real RF signal to the I and Q baseband information transmitted over USB to the host PC.
2.7.1 Flex 900 Logical Block Diagram. The target signal is received from the user selected antenna and goes to the MGA82563 amplifier. After amplification the signal travels through a hard wired band-pass filter to remove out of band noise from the signal. The band for this filter is the entire range of the daughter card, in this case 840-975 MHz. From the filter the signal enters the AD8347 mixer and proceeds through the internal two-stage variable amplifiers. The gain for these amplifiers is controlled by the Digital AGC signal from the main board. The other external signal to the AD8347 is from the ADF 4360. The ADF 4360 synthesizes the local oscillator based on the $C l k$ and Data information it receives from the main board over the SPI bus. The gain for the Digital AGC and Data signal from the main board are both determined by the Python code generated by GNU Radio on the host PC. This local oscillator signal from the ADF 4360 then goes through a phase splitter in the AD 3847 to generate the $\sin$ and $\cos$ signals used to mix the signal. Once the RF signal is mixed with the two local oscillator signals the two portions, the I-Analog and Q-Analog, are again amplified by internal variable gain amplifiers before entering


Figure 2.22: Flex 900 Rx Functional Block Diagram
into external hard-wired band-pass filters. The last stop on the daughter card for the two signals is to go back through the output amplifier in the AD8347. This output amplifier uses active feedback to boost the output to a level useable by most A-toD converters while minimizing distortion. For this research, this entire process is happening in parallel on the second Flex 900 daughter card as well. Each Flex 900 receives the same $C l k$ and Data signal from the mainboard, so the local oscillators can be considered coherent.
2.7.2 Mainboard Logical Block Diagram. For this research, the mainboard receives and processes two signals from separate daughter cards at the same time. This section describes the transition of one signal, the second signal transitions through the same process in parallel. The mainboard receives the two analog IF channels of the target signal from the daughter card in analog. Each channel enters into one of the ADC in the AD9862 chip. The signals are first amplified by the internal PGA, the gain controlled by a function of user settings and an effort to maximize resolution. The ADC then converts each to a 12-bit digital signal that transitions into the FPGA.

Once in the FPGA, each signal channel enters the second stage down-converter. The purpose of this second stage is to convert the digital IF signal to digital baseband. To accomplish this, task each IF channel is mixed with a cosine or sine signal provided by a CORDIC algorithm running in the FPGA. While the block diagram shows two mixers, they are implemented on the FPGA as a single complex multiplier. The signals now pass to a digital low pass filter before entering into the 4 stage CIC Decimator. Normally the decimator would be preceded by its own low-pass filter, but since the mixer would have one also the FPGA implements both as a single low-pass filter. The purpose of the decimator is to remove samples so that the signal sent to the USB controller can transmit it to the host computer without being overloaded. In this research, with the USB only responsible for sending a receive signal to the PC and no transmit signal from the PC , the minimum decimation rate we were able to achieve was four. Equation 2.41 illustrates the considerations that go into the minimum decimation rate. The max sample rate is determined by the ADC and is 64 megasamples a second, each sample being 16 bits longs. This research used two daughtercards. Without decimation this would result in 128 MBytes per second of data. With the additional data required for the USB frames a minimum decimation rate of four is necessary. Now the two A-Side channels and the two B-Side channels arrive at a multiplexer. The baseband I and Q signals are interleaved by the MUX and its control logic before moving to the USB controller. The USB controller then


Figure 2.23: Main Board Functional Block Diagram
puts them into USB frames for transmission to the host PC.
$\left(\frac{(\text { Max Sample Rate })\left(\frac{16 \text { bits }}{1 \text { sample }}\right)\left(\frac{1 \text { byte }}{8 \text { bits }}\right)}{\text { Decimation rate }}\right) *$ Daughter cards + USB Overhead $\leq$ USB bandwidth

### 2.8 Signal processing in SDR

2.8.1 Antenna. When the USRP receives the signal at the antenna, in the case of shaped OOK RFID encoding, it is a chain of high and low pulses shaped by a low-pass filter. The time domain formula for such a signal can be seen in Equation 2.42. The $s(t)$ term represents the shaping function and $h(t)$ is the data to be encoded. The carrier frequency is present in the cosine function. When transformed into the frequency domain, the signal takes the form seen in Equation 2.43. In the frequency


Figure 2.24: Antenna signal in frequency domain.
domain, the signal forms a SINC function centered on the carrier frequency, $\Omega_{c}$ as seen in Figure 2.24

$$
\begin{gather*}
x_{1}(t)=[s(t) \star h(t)] \cos \left(\Omega_{c} t\right)+h(t)  \tag{2.42}\\
X_{1}(\Omega)=1 / 2 S\left(\Omega-\Omega_{c}\right) H\left(\Omega-\Omega_{c}\right)+1 / 2 S\left(\Omega+\Omega_{c}\right) H\left(\Omega+\Omega_{c}\right) \tag{2.43}
\end{gather*}
$$

2.8.2 Entering First Stage Mixer. Prior to entering the mixer chip for first stage mixing, the signal is amplified and goes through a band-pass filter, as shown by Figure 2.25. This increases the amplitude of the signal by a gain factor of $A$ and attenuates the out of band noise levels. A graphical representation of this effect in the frequency domain can be seen in Figure 2.26
2.8.3 Frequency Synthesized Local Oscillator. In the first mixing stage the signal is down-mixed with a synthesized local oscillator to the IF. The mathematical representation of this synthesized frequency can be seen in Equation 2.44. When plotted in the frequency domain it can be seen in Figure 2.27.


Figure 2.25: Band pass filter in frequency domain.


Figure 2.26: Filtered signal in frequency domain.


Figure 2.27: Synthesized local oscillatorl in frequency domain.

$$
\begin{equation*}
F_{I F}=\Im\left\{\cos \left(\Omega_{I F} t\right)\right\}=1 / 2 \delta\left(\Omega-\Omega_{I F}\right)+1 / 2 \delta\left(\Omega+\Omega_{I F}\right) \tag{2.44}
\end{equation*}
$$

2.8.4 After First Stage Mixer. The signal is now convolved with the synthesized local oscillator from the previous section down to the IF and is represented by $x_{2}(t)$. The equation for the in-phase portion of the signal in the time domain is shown in equation 2.45 and the frequency domain is shown in Equation 2.46. To generate the quadrature signal, the inbound signal is mixed with the sine function of the local oscillator, as seen in Equation 2.47 and Equation 2.48. This mixing action attenuates the power signature and creates duplicate sincs in the frequency domain as seen in Figure 2.28.

$$
\begin{gather*}
x_{2}(t)=x_{1} \cos \left(\Omega_{I F} t\right)  \tag{2.45}\\
X_{2}=\frac{1}{2} X_{1}\left(\Omega-\Omega_{I F}\right)+\frac{1}{2} X_{1}\left(\Omega+\Omega_{I F}\right)  \tag{2.46}\\
x_{2}(t)=x_{1} \sin \left(\Omega_{I F} t\right) \tag{2.47}
\end{gather*}
$$



Figure 2.28: First stage mixed signal in frequency domain.

$$
\begin{equation*}
X_{2}=j\left(\frac{1}{2} X_{1}\left(\Omega-\Omega_{I F}\right)+\frac{1}{2} X_{1}\left(\Omega+\Omega_{I F}\right)\right) \tag{2.48}
\end{equation*}
$$

2.8.5 Final Analog Band Pass Filter. Just prior to leaving the daughter card the signal travels through one more band pass filter. This filter is designed so that it removes the duplicate SINCs in the frequency filter that result from the first stage mixing. The result of Figure 2.28 is convolved with this band pass function as seen in Figure 2.29. This final analog signal is then passed from the daughter card to the ADC on the main board.
2.8.6 ADC Sampling Pulse. Within the ADC a sampling pulse is generated. The frequency of this pulse, $f_{s}$, is determined by the sampling rate of the hardware. In the USRP 1 this is 64 MHz . A representation of this pulse in the time domain is seen in first line of Figure 2.30. Each pulse in that figure is spaced $T_{s}$, which is the sampling period, or $\frac{1}{f_{s}}$. Based on the sampling frequency of 64 MHz this is $1.67 * 10^{-7}$ seconds. In the frequency domain, this appears as a series of impulses space at integer multiples of the sampling frequency, as shown on second line of Figure 2.30.


Figure 2.29: Final analog signal in frequency domain.


Figure 2.30: Digital sampling signal.


Figure 2.31: Digitaly sampled signal.
2.8.7 Analog-to-Digital Converter. The ADC converts the continuous time signal, $X$, to discrete time by multiplying it by the sampling pulse as shown in Equation 2.49. In this way, the signal transform from a continuous wave to a series of impulses spaced $T_{s}$ apart. The results of this function is shown in Figure 2.31 (a). It appears in the frequency domain as shown in Figure 2.31 (b.)

$$
\begin{equation*}
x_{5}[n]=x_{3}\left(n T_{s}\right) \tag{2.49}
\end{equation*}
$$

2.8.8 Frequency Synthesized Digital Local Oscillator. As with the first stage mixer, the second down converter generates a cosine function but this one is digital. The digital cosine is generated by equation 2.50. Equation 2.51 is the frequency domain equivalent.


Figure 2.32: Digital baseband signal.

$$
\begin{gather*}
f[n]=\cos \left(\Omega_{I F} n T_{s}\right)  \tag{2.50}\\
\omega=\frac{\omega}{\omega_{s}} 2 \pi \tag{2.51}
\end{gather*}
$$

2.8.9 Digital Mixing from IF to Baseband. The system then mixes the digital IF signal with the synthesized local oscillator to generate the digital baseband signal. This mixing causes constructive interference and raises the magnitude of the signal back to $\mathrm{A} / 2$. It also moves the signal to the discrete time domain. The discrete time frequency domain representation of the digital baseband signal can be seen in Figure 2.32.
2.8.10 Digital Decimation. The four stage decimator removes a set number of samples dependant on the decimation rate set by the user. As discussed earlier the minimum decimation rate is four. Figure 2.33 shows the effect of the reduced number of samples in the frequency domain.


Figure 2.33: Decimated digital baseband signal.

### 2.9 Related Research

2.9.1 LANDMARC. Due to the inability to use TDOA, many of the earlier localization methods for RFID tags, such as LANDMARC [11], use a read/no-read of the subject marker, known tags, and known readers to calculate a location based on Received Signal Strength Indicator (RSSI). This localization technique querys a array of readers, whose positions are known, to see which tags they can see and at what power level they can see them. A sample array is shown in Figure 2.34. When a target tag is identified, it compares its received power levels it was read at to the power levels that known tags are read at. By comparing the distances of the known tags and their power levels to the power levels of the target tag a location can be surmised [11]. The subject paper recognized that this procedure works but we identified several issues for real world implementation. RSSI can be severely affected by the propagation environment. If a new object enters the area, be it an emitter or absorber of RF, the system must recalibrate the power levels of the known tags. It was also found that the power incident on a tag can cause its calculated location to vary greatly.


Figure 2.34: LANDMARC Identification Layout

## III. Methodology for SID of Passive RFID Tags

### 3.1 Approach

This research develops and analyzes the effectiveness of the three-part PDOA spatial identification algorithm. The first part of PDOA is time domain analysisto provide a relative velocity towards the receive antenna. The second part is frequency domain analysis which provides a range to the target signal. The final portion of the PDOA algorithm is the spatial domain analysis, in which two receive antennas provide a bearing to the target signal. The locations provided by all three parts are compared to the same portion of the algorithm from a simulation of the same target signal.
3.1.1 Create Simulation. In order to determine the effectiveness of the spatial identification method, a simulation of the test bed is created to provide a baseline for comparison. These simulations provide verification that, given a good extraction of the phase of a signal, the PDOA metrics can be calculated from captured data. The velocity of the target signal, reflection from the table surface, and the path traveled are modeled in MATLAB. Additive Gaussian White Noise is also added to the simulated signal based on the observed noise floor of the laboratory in use. Multiple simulations are run for each configuration and the results are averaged to establish the baseline performance expected out of the real world system.
3.1.2 Phase of Received Signal. The phase of the captured signal is calculated using a Fast Fourier Transform in MATLAB. Once the I and Q data is imported

$$
\begin{array}{|l|}
\hline \text { X1_freq }=\mathrm{fft}(\mathrm{x} 1) ; \\
\text { phase_x1_fc }=\text { angle(X1_freq(kc)); }
\end{array}
$$

Figure 3.1: Code to Extract Phase of Received Signal

$$
\left.\operatorname{v\_ r}(\text { sample })=\left(3 \mathrm{e} 10 /\left(4^{*} \mathrm{pi}{ }^{*} \mathrm{fc}\right)\right)^{*}((\text { phase_x1_fc(sample })-\text { phase_x1_fc(sample-1) }) / \text { step }\right) ;
$$

Figure 3.2: Code for TD-PDOA
and the start of the tag response is located in the capture, the FFT is found using the code snippet in Figure 3.1, where $k c$ is the center frequency of the captured signal. Since an EPC Gen 2 tag is used in all tests, the center frequency remains constant at 915 MHz . This step is repeated for every sample captured in each test.
3.1.3 Time Domain PDOA. When the PDOA is analyzed in the time domain it yields the velocity of the target transmitter with respect to the receive sensor. This is done with the code snippet contained in Figure 3.2 in MATLAB based on the phase found in 3.1.2.

This code snippet implements Equation 2.1 described in Chapter 2. The center frequency, $f c$, is found for each signal sample piece using FFT. In all cases the distances are in centimeters. The speed of light required in all calculations, $c$, is also represented in $\mathrm{cm} / \mathrm{s}$ or $3 \mathrm{e} 10 . \delta \phi$ is calculated by taking the angle of the FFT bin that represents the center frequency of each signal sample. The time delta is simply the time between the two samples stored in the variable named step. If the tag is stationary the phase of sample and sample- 1 will be the same resulting in an angular velocity of zero. The function will also report an angular velocity of zero at the center crossing of the tag, when the target is directly in front of the sensor antenna. This

$$
\text { d_found }(\text { sample })=-\left(3 \mathrm{e} 10 /\left(4^{*} \mathrm{pi}\right)\right)^{*}((\text { phase_x1_fc(sample)-phase_x1_fc2(sample))} /(\mathrm{fc}-\mathrm{fc} 2)) ;
$$

## Figure 3.3: Code for FD-PDOA

point also marks the instant that the function will transition from positive to negative, or negative to positive, velocity as the target transitions from moving towards to away from the sensor antenna.
3.1.4 Frequency Domain PDOA. When the PDOA is analyzed in the frequency domain it yields the distance from the target transmitter to the receive sensor. We do this once again based on the phase found in Section 3.1.2 but we also must find the phase of the captured signal at a different frequency. Based on the $f c$ found previously a frequency 1 MHz from the signal center frequency is selected and is represented by the variable $f c 2$. The code snippet in Figure 3.3 implements Equation 2.12 from Chapter 2. The difference, $f c-f c 2$, will remain constant at 1 MHz this combined with the fact that the equation relies on the same sample allows this technique to find the range to the target transmitter even if it is stationary. For a target moving in a straight line perpendicular to the antenna array this value will have a minimum value at the center crossing to the sensor antenna.
3.1.5 Spatial Domain PDOA. To analyze the PDOA in the spatial domain, a second antenna is added to the software defined radio. If the phase of the received signal is inspected at each of the receive antennas, a bearing to the target transmitter can be calculated. This bearing to the target transmitter is found using the following the code seen in Figure 3.4. For this calculation, a second capture is taken from

$$
\text { theta_found } \left.\left.=\arcsin \left(-\left(3 \mathrm{e} 10 /\left(2^{*} \mathrm{pi}^{*} \mathrm{fc}\right)\right)^{*}((\text { phase_x1_fc(sample })-\text { phase_y1_fc(sample })\right) / \mathrm{a}\right)\right) ;
$$

## Figure 3.4: Code for SD-PDOA

the USRPśs second daughter card. The antenna for this capture is positioned a set distance from the first antenna. In the code, this distance is represented by $a$ and is given in centimeters. The phase for the second capture is calculated using the same function as Section 3.1.2 and the samples are aligned in time. The phase of the second sample is stored in the array phase ${ }_{-} 11_{-} f c$. The SD-PDOA equation assumes that the tag is at a distance greater than one wavelength. The experiment is configured so that the tag is never closer than 86.0 cm - more than double the 37.5 cm wavelength of a 915 MHz signal. The result of this function, theta_found, is the bearing to the target tag from receive Antenna \#1. Negative values distinguish that a target transmitter is on the far side of Antenna $\# 2$ relative to Antenna \#1. Positive values represent a target transmitter that is on the same side of the Antenna \#1 as Antenna \#2.

### 3.2 System boundaries

The system under test (SUT) consists of a small scale test bed. This test bed consists of a commercial RFID tag reader, a software defined radio, a track for the tag to move along, and a controller for tag movement. A block diagram of the SUT is shown in Figure 3.5 Each section is described in the following subsections.
3.2.1 RFID Reader. The commercial RFID tag reader is an Alien 9800, and it is used to energize the tag so that the interaction can be captured. It is controlled by a Windows based PC via Ethernet. The reader is operated in Global Scroll mode.


Figure 3.5: $\quad$ System Under Test Block Diagram

This mode allows for faster reads, as it simplifies the query process by removing the time slots that allow a reader to interact with multiple tags. In order to remove the possibility of errant reads the lab is kept clear of other RFID tags that operate in the 900 MHz band.
3.2.2 Windows PC. The Windows PC is a Dell Laptop running Windows XP. The laptop directly controls the tag movement through the USB to serial port adapter. It also interfaces to the Alien 9800 reader over the Ethernet connection.
3.2.3 Software Defined Radio. The receive sensor is a software defined radio; a USRP 1 was selected for its low cost, flexibility and the ability to hold two daughter cards. The two daughter cards, both which operate in the 900 MHz


Figure 3.6: SDR RFID Reader
band, are required in order to accomplish the spatial domain PDOA. The radio is configured to capture a 2.5 MHz band of the spectrum centered at 915 MHz with a sample rate of 1.35 megasamples per second. The initial vision of the SUT had the SDR acting as the RFID tag reader, capturing the interaction. To this end, the RFID Gen2 reader developed by Buettner et al. was installed on the USRP 1 and configured using the Linux workstation. This configuration can be seen in Figure 3.6 and consists of a Macbook running Ubuntu 10.10 and GNU Radio, a USRP1 SDR with a Flex 900 daughter card and two Alien 9611-CR antennas. The GNU Radio installation has been modified to enable the faster response times required by RFID tags. Initial experiments focused on the use of a newer USRP 2 model, but due to a requirement to use its proprietary UHD drivers, we reverted to the USRP1 which
uses the open-source drivers included in GNU Radio. As each tag response is received by the reader, a '0u' pattern is output to the terminal as can be seen in Figure 3.6. We are able to match the read distances of commercial readers. While the EPC Generation 2 specification is 3 m , this is largely dependant on line-of-sight and can be reduced quickly by interference of metallic objects in the lab. This verification was completed by mounting the two antennas along one lab wall and walking away from it with various tags. The edge of the read range was defined as the distance when the successful read rate dropped below $75 \%$. The location of this cutoff was then marked on the floor. Without moving the tape, and with the SDR configured at the same power level and query rate the range to the read rate failure was verified for all tags tested. While the SDR was capable of reading the tags, limitations in either the USB interface or the age of the Macbook prevented the capture of all of the required signal information. It was decided that moving the burden of the tag query off of the Linux PC and onto the commercial reader would reduce this bottleneck.

The SDR is now configured with two Flex 900 daughter cards and twin whip style antennas. The SDR with Antenna \#1 is positioned between the Rx and Tx antennas of the commercial reader as seen in Figure 3.7. This position allows for the strongest signal reception for the TD-PDOA and FD-PDOA. Antenna \#2 is mounted to the test bench outside the $\mathrm{Rx} / \mathrm{Tx}$ pair and alternate left and right for different test runs. This new configuration was then tested to verify the ability to capture the data required for the testing. Figure 3.8 shows an early capture of the interaction. The query/response can be clearly seen in this segment with the reader sending out the


Figure 3.7: SDR RFID Reader
higher signal in the left portion of the wave and the tag's modulated response to the right.
3.2.4 Linux PC. The radio is controlled by a Ubuntu 10.04 computer running GNU radio and the GNU Radio companion. The start and stop signal for the the capture is received over Ethernet from the PC controlling the reader and tag track. Each capture is saved to a different file for offline analysis on a workstation class computer.
3.2.5 Tag Track. The tag tack is actually not a metal track, but a course of rope suspended twelve inches above the test table on wooden rods with nylon pulleys. The actual path of the tag can be changed by moving the wooden rods to other sets


Figure 3.8: SDR RFID Reader

Table 3.1: $\quad$ Speed Verification Test Results

| Desired <br> Speed <br> $(\mathrm{cm} / \mathrm{s})$ | $(\mathrm{cm} / \mathrm{s})$ | $(\mathrm{cm} / \mathrm{s})$ | $(\mathrm{cm} / \mathrm{s})$ | $(\mathrm{cm} / \mathrm{s})$ | $(\mathrm{cm} / \mathrm{s})$ | $(\mathrm{cm} / \mathrm{s})$ | Run | Run 3 | Run 4 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :--- | :---: |
| $(\mathrm{s})$ | Run | Run 6 | Avg Time <br> $(\mathrm{cm} / \mathrm{s})$ | Observed <br> Speed <br> $(\mathrm{cm} / \mathrm{s})$ |  |  |  |  |  |
| 10 | 10.59 | 10.53 | 10.69 | 10.56 | 10.60 | 10.66 | 10.60 | 9.42 | 0.57 |
| 15 | 7.09 | 7.06 | 7.13 | 7.12 | 7.19 | 7.12 | 7.12 | 14.04 | 0.95 |
| 20 | 5.18 | 5.25 | 5.25 | 5.34 | 5.28 | 5.21 | 5.25 | 19.04 | 0.96 |
| 25 | 4.00 | 4.09 | 4.06 | 4.13 | 4.13 | 4.13 | 4.09 | 24.44 | 0.55 |
| 30 | 3.35 | 3.29 | 3.38 | 3.59 | 3.49 | 3.50 | 3.43 | 29.12 | 0.87 |
| 35 | 3.00 | 2.97 | 2.90 | 2.97 | 2.88 | 2.90 | 2.94 | 34.05 | 0.95 |
| 40 | 2.62 | 2.62 | 2.54 | 2.50 | 2.56 | 2.53 | 2.56 | 39.04 | 0.96 |
| 45 | 2.19 | 2.25 | 2.25 | 2.22 | 2.22 | 2.18 | 2.22 | 45.08 | -0.08 |

of holes on the pegboard table. Four track configurations are tested, and these can be seen in Figure 3.9. The speed of the tag was verified by placing two posts one meter apart on the test table. A red marker was placed on the rope track. The time to transverse the distance was measured, and six trials at each speed were conducted. The results from those trials can be seen in Table 3.1
3.2.6 Windows Workstation. The windows workstation is used to do the offline processing of the collected data. It is a Dell Precision T7500 with 12 GB of


Figure 3.9: Traçk Configurations


Figure 3.10: $\quad$ Stepper Motor Drive Wave

RAM and 2TB of hard drive storage. It is running Windows 7 with MATLAB r2010b. The processing of the tag's spatial identification was moved to this system because of the large size of the capture files. This system implements the code from Sections 3.1.3-3.1.5.
3.2.7 Tag Controller. The velocity and direction of travel of the tag is directed by the same PC as the Alien reader by serial port. A connection from the serial port to a ML507 Virtex board provides a timed pulse wave to a 12 V stepper motor via an H-bridge to protect the electronics on the ML507. A stepper motor was chosen over a conventional motor due to the precise control it provides. Given a set pulse wave from the control board, the motor will always spin at the same velocity regardless of fluctuations in the supply voltage. The stepper motor is a bipolar 1.8 degree per step motor. The motor has four wires which connect to two different coils. In order to drive the motor, the coils must be activated in the sequence shown in Figure 3.10 Each progression in the waveform, called a "step," drives the motor $1 / 200$ th of a revolution, or 1.8 degrees. To reverse the direction of the motor, the coil activation sequence is simply reversed. A commercially H-bridge kit is inserted inline between the ML507 and the stepper motor. This H-bridge converts the 3.3 V


Figure 3.11: Motor Hardware Circuit
TTL level logic from the output pins of the ML507 to the 12 V required to drive the motor. Diodes on the bridge also prevent feedback from the inductive motor from flowing back to the ML507 and damaging the lower voltage components. Figure 3.11 depicts the motor controller's hardware circuit. Pins $\Phi 1$ and $\Phi 1^{\prime}$ are driven by $j k 1$ and $j k 2$, while pins $\Phi 2$ and $\Phi 2^{\prime}$ are driven by $j k 3$ and $j k 4$. The GND and 12 V inputs are driven by an external computer power supply. This power supply was also used to power the ML507 so that a common ground was present from the two systems. The VHDL module developed functions as a finite state machine and produces the required waveform from the diagram in Figure 3.10. When the direction input is set to ' 0 ,' the module drives through a state table containing the coil activation sequences in the proper order. When the direction input is set to 1 the module iterates the state
table in the reverse order. At line 166 the std_logic_vector speed pulled from the bus in line 152 is converted to an unsigned integer using the conv_integer command. By multiplying this value by 20000 we cause the FSM to wait for 30 microseconds times the value of speed. For example if speed equaled 60 cycles each step would be spaced 180 microseconds apart. Early versions of this code simply accepted the speed from the bus and attempted to drive the motor at that speed. It was observed if that the speed was changed too quickly the motor would lock up. In order to prevent that a ramping function was added, lines 169-173, to the code so that the speed the motor received is increased, or decreased, by one each step it takes.
3.2.8 Tag. Different tags are tested to observe differences in the response due to antenna shape. All tags are EPC generation two tags and respond to queries in the 915 MHz band. Four examples of the different antenna patterns under test are shown in Figure 3.12. The large silver shape in each tag is the antenna; the actual logic circuit for each tag is contained within the small black dot at the center of the antenna.

### 3.3 System Parameters

The workload parameters of the system are set to provide proof-of-concept for the use of PDOA as a spatial identification technique in regards to passive RFID tags. These parameters include the number of tags, distance to reader, and velocity of tag.


Figure 3.12: Sample RFID Tag Antenna
3.3.1 Number of Tags. The number of tags under test is limited to one in this research. While the reader is able to query multiple tags, only one is visible at a time. The reason for this is so that the reader can stay in Global Scroll mode for more rapid reads. While only one tag is visible at a time, several different tag antenna configurations are tested to compare accuracy.
3.3.2 Distance to Reader. As shown above in Figure 3.9, the tag will not move more than two meters from the tag reader and sensor receiver. This is well within the specification of the EPC Gen 2 tags. The specification is for read distances of up to three meters and extended reads demonstrated at ranges of approximately six meters. The tags are kept within this range in order to ensure consistent, rapid, reads of the tags. If the test was to extend to the edge of the RFID tag's range there
would be additional noise as well as erroneous reads which could negatively affect the accuracy of the system.
3.3.3 Velocity of Tags. Tag velocity represents the final variable in the system under test. The velocity is set at $10,20,30$ and $40 \mathrm{~cm} / \mathrm{s}$. These boundaries represent the equivalent of a slow crawl to the speed of a person walking. Given the small scale of the system, faster speeds are not able to provide enough captures of the tag moving in any one direction to produce an accurate characterization of the tag's spatial identification.
3.3.4 RFID Reader Configuration. As stated above the commercial reader is operated in Global Scroll mode. This mode was selected for the rapid read rates of a single visible tag. If the test was expanded to track multiple tags the reader would require reconfiguration.
3.3.5 SDR Configuration. The configuration of the SDR remains constant throughout the testing. Location and wiring of the antennas themselves remains constant throughout testing.
3.3.6 Tag track. The tag track is reconfigurable on the test bed. Paths along the track were chosen to vary the movement of the tag with respect to the receive antenna. By having the tag move in different directions relative to the antenna, it could be observed if the system is more proficient at detecting targets moving in different orientations. The tracks tested are illustrated in Figures 3.9
3.3.7 Tag type. Different RFID tags used different styles of antennas as shown in Figure 3.12. Runs of the same velocity and target track are repeated with different tags to observe any variation in accuracy of the different tags.

### 3.4 Performance Metrics

The metrics of the SID PDOA system measure the system performance. They are generally effective when comparing the system to the simulations and to judge the feasibility of the overall system. For this experiment the metric is the accuracy of the computed SID. The difference of the observed SID and the baseline will be found, and the variance of the observed SIDS will be calculated.

### 3.5 Evaluation Technique

The evaluation technique used to determine the performance of the PDOA algorithm is the analysis of an actual system. All three elements of the PDOA algorithm have been shown to be effective in simulation. What makes this research unique is the capture of real world data with the use of a SDR. The query of the tag is provided by an Alien 9800 RFID reader and two attached ALR-9611-CR antennas. The EPC Generation 2 RFID tags under test are shown in Figure 3.12. A python script running on the PC laptop controls the direction and velocity of the tag. Each capture started by the script is saved to the hard drive with a date and time stamp. Offline analysis of these captures occurs on a Dell T7500 workstation class PC using MATLAB 2010b.
3.5.1 Selection of Data Samples. The initial captures of reader and tag interaction showed a large variance in several variables which made automatic processing of the data difficult. The first of these is the timing of the interactions. The Alien 9800 , due largely to the robust design, reads at random times and spacing depending on the environment. This results in inventory rounds that are not evenly spaced in the time domain. Second is the highly variable power level of the response. If the tag is able to harvest a large portion of the reader's power the response can be relatively strong, $50-75 \%$ of reader's power. More often than not, the power level of the tags response is less than $50 \%$ of the reader's power level. For these reasons, analysis of the interactions was done manually.

The first analysis step is to plot the entire capture in the time domain as seen in Figure 3.13. This particular capture is from Configuration $\# 2$ with the tag moving at 10 centimeters per second towards the reader. After enlarging one interaction group, as shown in Figure 3.14, the sample numbers for the start of each reader message and tag response is logged in an Excel spreadsheet. The iteration in Figure 3.14 is the first group seen in Figure 3.13 and shows ten queries of the one tag within range. From this interaction two tag reads and their corresponding responses are selected for analysis. The phase of the response of the tag, $\phi_{t a g 1}$ and $\phi_{t a g 2}$, is based on the signal it receives from the reader. This signal has its own phase, $\phi_{\text {reader } 1}$ and $\phi_{\text {reader } 2}$. If the reader is coherent between messages, than this will cancel out. If not, the final phases used in the SID metric calculation is the phase of the response minus the phase of the reader message, $\phi_{\text {tag } 1}-\phi_{\text {reader } 1}$ and $\phi_{\text {tag } 2}-\phi_{\text {reader } 2}$. I am using the first and last


Figure 3.13: Reader and tag interaction.
reader/tag pairs. These two pairs were chosen because of their separation in time. Given the known velocity of the tag, it had traveled about 11 centimeters between the first tag response and the last, and it should offer the best chance to see a phase difference due to movement. The starting sample numbers and the corresponding time are shown in Table 3.2. The time epoch was determined by taking the sampling rate, 1.35 megasamples per second after decimation, and multiplying by the sample number. The first 2048 samples after the time epoch are then copied into a new vector. The number of samples to analyze was chosen to be the largest power of two that will not exceed the tag's initial response. This sample size is large enough to include the preamble wave form, the SOF and 32 bits of data. The analysis of these vectors is discussed in the next section.


Figure 3.14: $\quad$ Single group of reader and tag interactions.

Table 3.2: $\quad$ Sample Vector Epochs

| Vector | Sample Number | Time Epoch |
| :---: | :---: | :---: |
| Tx-1 | 10861525 | 8.045131 |
| Rx-1 | 10878579 | 8.057763 |
| Tx-2 | 12383164 | 9.172210 |
| RX-2 | 12396643 | 9.182193 |

$$
\text { [C,index] }=\text { abs(fftshift(fft(data_complex))/data_complex_len) }
$$

Figure 3.15: Code to Calculate Sample Vector Center Frequency

Table 3.3: Vector Phases

| Vector | Frequency | Observed Phase |
| :---: | :---: | :---: |
| Tx-1 | 914.8 MHz | -2.09953 radians |
| Rx-1 | 914.8 MHz | 2.97874 radians |
| Tx-2 | 914.8 MHz | -2.13302 radians |
| RX-2 | 914.8 MHz | -3.11687 radians |

3.5.2 Finding the Vector's Phase. To find the phase of each of the selected vectors we first need to find the Fast Fourier Transform (FFT). MATLAB implements the FFT using FFTW, an adaptive software package that chooses the Cooley-Tukey algorithm or a modified form, depending on the data being processed. Either way the FFT is an N-point Discrete Fourier Transform (DFT), and in the case of this research, $N=2048$. The first step in finding the sample vector's phase is to plot the magnitude of the FFT of the sample vector, this is shown in Figure 3.16 for the first reader transmission. Using the MATLAB max command, the center frequency of the sample vector is found. In this case it is just above 915 MHz . The index of this value is noted and the value at that index for the argument of the sample vector is found. As shown in Figure 3.17, the value is -2.00954 radians for the first reader transmission. This process is then repeated for each of the sample vectors identified. The phases found for the example sample can be seen in Table 3.3. The phase found for all other samples are then stored in the same Excel spreadsheet, as well as the vector time epochs for computation via the SID metric algorithms.


Figure 3.16: Magnitude of FFT of reader transmission.


Figure 3.17: Phase of FFT of reader transmission.

Table 3.4: Experiment Configurations

| Configuration | Speed (cm/s) | Tag | Number of Runs |
| :---: | :---: | :---: | :---: |
| Config 1 | 10 | 1 | 5 |
| Config 1 | 20 | 1 | 5 |
| Config 1 | 30 | 1 | 5 |
| Config 1 | 40 | 1 | 5 |
| Config 2 | 10 | 1 | 5 |
| Config 2 | 20 | 1 | 5 |
| Config 2 | 30 | 1 | 5 |
| Config 2 | 40 | 1 | 5 |
| Config 3 | 10 | 1 | 5 |
| Config 3 | 20 | 1 | 5 |
| Config 3 | 30 | 1 | 5 |
| Config 3 | 40 | 1 | 5 |
| Config 4 | 10 | 1 | 5 |
| Config 4 | 20 | 1 | 5 |
| Config 4 | 30 | 1 | 5 |
| Config 4 | 40 | 1 | 5 |
| Config 2 | 20 | 1 | 5 |
| Config 2 | 20 | 2 | 5 |
| Config 2 | 20 | 3 | 5 |
| Config 2 | 20 | 4 | 5 |

### 3.6 Experimental Design

Table 3.4 shows the different configurations of the experiment and the number of runs for each configuration. The configurations referenced are shown in Figure 3.9.

### 3.7 Methodology Summary

This research is performed in two parts. First, a simulation models the physical test bed as shown in Figure 3.9. All of the plan tests in Table 3.4 are run in simulation
to provide a baseline of the system and provide expected values. Second the described runs are performed on the physical test bed with their data stored for offline analysis.

## IV. Results

### 4.1 Introduction

This chapter provides a discussion of the simulations used as the baseline, the data collected from the testbed, as well as the outcome of the analysis of that data. Due to the nature of the results arrived at in this research, there will also be analysis of the resolution required in the data for phas-based spatial identification to be successful, and how this resolution compares to the capabilities of the USRP software defined radio.

### 4.2 Simulation of RFID Tag Movement

The simulation described in Chapter 3 was tailored to fit the real world dimensions of the testbed and are listed in Table 4.1. The level of Additive Gaussian White noise used was based on the noise floor of the laboratory the research was conducted in. This noise floor was measured on a Sunday morning with only one person in the lab and all extraneous transmitters (cell phones, RFID reader, computer WiFi, etc.) turned off. These simulations represent what would amount to an ideal situation for the tag to be tracked. A constant tone is available and only the phase offset due

| Testbed Feature | Variable | Value |
| :--- | :---: | :---: |
| Sampling Frequency | fs | 500 MHz |
| Center Frequency | fc | 915 MHz |
| Secondary Frequency | fc 2 | 914 MHz |
| Height of reader from tabletop | zReader | 20 cm |
| Tag vertical offset from reader | z | 10 cm |
| 3dB angle of sensor antenna | theat3db | 0.698 radians |

Table 4.1: $\quad$ Simulation Enviromental Elements
to the propagation channel is measured. This constant response is mixed with the AGWN and a multipath response that simulates the multipath due to reflection off of the wooden tabletop. Due to the short range of the RFID tags and the distance to other reflectors in the laboratory, multipath from other objects was not considered. The error introduced due to multipath was minimal as can be seen in Figure 4.1 Figure 4.16.

In all figures the dark line represents the one ray model with no multipath, the lighter shaded area is the two-ray model simulating the reflection from the tabletop. Only in Configuration \#2 when the tag is traveling directly at the reader, is the noise from the multipath evident. In reality, the multipath level in this configuration is no higher than the other configurations, but due to the relative speed remaining constant over the course of the run. Only when the graph is zoomed in to seven significant figures to the right of the decimal point, does the noise becomes evident.

### 4.3 Capture of Real RFID Tag Interaction

The test runs described in Chapter 3 were run on the testbed and all data recorded into separate files. These captures took place on Sunday, 11 December in the morning, with extraneous emitters turned off to minimize the noise floor in the lab, in an effort to recreate the environment represented in the simulation. Despite the optimal configuration of the Alien 9800 reader and USRP, several problems with the captures emerged. First, the Alien is not configurable to perform continuous reads. As can be seen in Figure 4.17, there is not a steady series of queries and responses as


Figure 4.1: Configuration \#1: $10 \mathrm{~cm} / \mathrm{s}$ Relatvie Velocity


Figure 4.2: Configuration \#1: $20 \mathrm{~cm} / \mathrm{s}$ Relatvie Velocity


Figure 4.3: Configuration \#1: $30 \mathrm{~cm} / \mathrm{s}$ Relatvie Velocity


Figure 4.4: Configuration \#1: $40 \mathrm{~cm} / \mathrm{s}$ Relatvie Velocity


Figure 4.5: Configuration $\# 2: 10 \mathrm{~cm} / \mathrm{s}$ Relatvie Velocity


Figure 4.6: Configuration \#2: $20 \mathrm{~cm} / \mathrm{s}$ Relatvie Velocity


Figure 4.7: Configuration \#2: $30 \mathrm{~cm} / \mathrm{s}$ Relatvie Velocity


Figure 4.8: Configuration \#2: $40 \mathrm{~cm} / \mathrm{s}$ Relatvie Velocity


Figure 4.9: Configuration $\# 3: 10 \mathrm{~cm} / \mathrm{s}$ Relative Velocity


Figure 4.10: Configuration $\# 3: 20 \mathrm{~cm} / \mathrm{s}$ Relative Velocity


Figure 4.11: Configuration $\# 3: 30 \mathrm{~cm} / \mathrm{s}$ Relative Velocity


Figure 4.12: Configuration $\# 3: 40 \mathrm{~cm} / \mathrm{s}$ Relative Velocity


Figure 4.13: Configuration \#4: $10 \mathrm{~cm} / \mathrm{s}$ Relative Velocity


Figure 4.14: Configuration \#4: $20 \mathrm{~cm} / \mathrm{s}$ Relative Velocity


Figure 4.15: Configuration \#4: $30 \mathrm{~cm} / \mathrm{s}$ Relative Velocity


Figure 4.16: Configuration \#4: $40 \mathrm{~cm} / \mathrm{s}$ Relative Velocity


Figure 4.17: Entire Capture
anticipated. Two distinct sets of reads can been seen starting at about $0.6 \times 10^{7}$ and $1.3 x 10^{7}$ samples. In addition to the fact that there is not a constant query/response interaction from the reader, the two sets of reads are at different frequencies within the specification, 924.9 MHz and 908 MHz , respectively. While this difference in frequency would complicate phase-based spatial identification it could be accounted for. It does become a problem when we look at spatial identification as a doppler problem. This is discussed in Section 4.4.2

The good news is that the query from the reader and the tag's response are easy to distinguish when you enlarge a set of reads as seen in Figure 4.18. The clusters with the larger amplitudes are the queries from the reader, with the clusters with smaller amplitudes being the responses from the tag. Zooming further into one of the tag responses, it is possible to visually decode the response of the on-off keying used in the EPC Gen 2 Type A tags, as seen in Figure 4.19. As described in the specification [1],


Figure 4.18: Reader/Tag Conversation


Figure 4.19: Decoded Tag Response
a frame starts with the SOF (Start of Frame) symbol, followed by the data, and closes with a EOF (End of Frame). Each bit of data is encoded as a function of the Tari. One Tari equals roughly 20 microseconds, as defined in the standard. A zero is encoded as off for one half a Tari then high for the second half. A one is encoded as off for one half a Tari and then on for one and a half Taris. In this way we can simply read the ones and zeros of the data portion by the width of the on portions of the signal. It should be noted that with this method of encoding the frame size in time is determined by the payload. This introduces another complicating factor, in that tag responses do not contain the same number of samples from one frame to another. Simply put, ignoring the SOF and EOF, a frame consisting of sixteen bits of zeros would provide roughly half of the samples of a frame consisting of all ones. In the phase-based analysis this would not matter, but once again, it is problematic when approaching the issue from a frequency/doppler standpoint.

### 4.4 Analysis of Data for Spatial Identification

The data for the first run of Configuration \#2 at $10 \mathrm{~cm} / \mathrm{s}$, (sample run) is analyzed in detail to show how the results were computed. Results for all other runs were analyzed in the same way but only a summary of the results for those runs is presented. The rest of this section is divided into two parts. The first subsection describes analysis of the captured data using the phase-base algorithms. The second subsection describes the requirements that would be needed if we tried to apply doppler radar principles to the captures.
4.4.1 Analysis by Phase Based Spatial Identification. When the real portion of the entire run was plotted in Figure 4.20, one can see that there were six groups of interactions between the tag and reader. The fifth group was examined but the signal to noise ratio in this group is to low to pick out the clear starts of the reader and the tag responses, so it was ignored. As described in Chapter 3, Methodology, the starting epochs of each of the reader and tag transmissions was entered into a spreadsheet. These spreadsheets can be found in Appendix A. Each table is labeled with the configuration, velocity and run number. Each grouping has 40 pairs of reader/tag interaction, resulting in 200 epoch pairs for the entire run. The phases were calculated as described in Chapter 3. The phases found were then put into Equation 2.1 and the relative velocities were calculated. The results showed significant variation, so the signal to noise ratio (SNR) for both the Alien reader and the tag's response were also found for analysis. The results for the sample run can be seen in Table 4.2. One can see that as the SNR increases the error, in general, decreases. While one run at one speed allows us to only draw preliminary conclusions, it does provide clues on how the rest of the data could be sorted and analyzed. To this end, the summary of the remaining results are grouped by both the SNR of the reader and the SNR of the tag. Calculated velocities are grouped according to Reader SNR in the following three categories: $\leq 5,5.01-6$, and $>6$. In a similar fashion, the calculated velocities are sorted by the tag's response SNR in the following three categories: $\leq 2.5,2.51-$ 3.5 , and $>3.5$. Each of these is described in Table 4.3 as Low SNR, Medium SNR, and High SNR. Each tag/reader group will then be placed in one of nine squares on


Figure 4.20: Configuration 2, $10 \mathrm{~cm} / \mathrm{s}$, Run 1

Table 4.2: Sample Run TD-PDOA Results

| Group | Relative Velocity (cm/s) | Error $(\mathrm{cm} / \mathrm{s})$ | Reader SNR | Tag SNR |
| :---: | :---: | :---: | :---: | :---: |
| 1 | 47 | 37 | 5.68 | 2.70 |
| 2 | -9.0 | 19 | 4.90 | 2.31 |
| 3 | 37 | 27 | 6.50 | 3.38 |
| 4 | 11 | 1 | 6.50 | 3.55 |
| 5 | -18 | 28 | 3.86 | 2.30 |

the chart with low reader SNR and low tag SNR being in the upper left hand corner and high/high SNR in the lower right hand corner. When one considers that the tag's actual velocity was $\pm 2 \mathrm{~cm} / \mathrm{s}$ when programmed for $10 \mathrm{~cm} / \mathrm{s}$ the results in Table 4.3 for those groups with a high reader SNR, $40 \%$ of observed groups, are within $11 \mathrm{~cm} / \mathrm{s}$ of the actual velocity. The low variance of the Medium tag/high reader SNR block is shows how tightly these are grouped.
4.4.2 Requirements for Doppler Spatial Identification. Given the issues with determining the relative velocity of the tag based on the phase of the response an attempt to look at the doppler shift of the response frequency was made. The

Table 4.3: Configuration 2, $10 \mathrm{~cm} / \mathrm{s}$ TD-PDOA Results

|  | Tag SNR <br> Low | Tag SNR <br> Medium | Tag SNR |
| :---: | :---: | :---: | :---: |
| High |  |  |  |
| Reader | Groups: 14 | Groups: 4 | Groups: None Observed |
| SNR | Average Velocity: -5.8 | Average Velocity: 17.6 |  |
| Low | Variance: 0.46 | Variance: 0.16 |  |
| Reader | Groups: 1 | Groups: 3 | Groups:1 |
| SNR | Velocity: 47 | Average Velocity: | 32.1 Velocity: 5.3 |
| Medium | Variance: N/A | Variance: 11 | Variance: N/A |
| Reader | Groups: 6 | Groups: 7 | Groups:4 |
| SNR | Average Velocity: 26.1 | Average Velocity: 21.2 | Velocity:14.5 |
| High | Variance: 0.11 | Variance: 0.04 | Variance:0.06 |

Table 4.4: Configuration 2, $20 \mathrm{~cm} / \mathrm{s}$ TD-PDOA Results

|  | Tag SNR | Tag SNR | Tag SNR |
| :---: | :---: | :---: | :---: |
|  | Low | Medium | High |
| Reader | Groups: 5 | Groups: 1 | Groups:None Observed |
| SNR | Average Velocity: -13.0 | Average Velocity: 6.7 |  |
| Low | Variance: 0.58 | Variance: N/A |  |
| Reader | Groups: 1 | Groups: 7 | Groups:None Observed |
| SNR | Velocity: 9.3 | Average Velocity: 41.8 |  |
| Medium | Variance: N/A | Variance: 0.24 |  |
| Reader | Groups: TBD | Groups: 3 | Groups:1 |
| SNR | Average Velocity: TBD | Average Velocity: 23.5 | Velocity:11 |
| High | Variance: TBD5 | Variance: 0.04 | Variance:TBD |

Table 4.5: Configuration 2, $30 \mathrm{~cm} / \mathrm{s}$ TD-PDOA Results

|  | Tag SNR <br> Low | Tag SNR Medium | $\begin{gathered} \text { Tag SNR } \\ \text { High } \end{gathered}$ |
| :---: | :---: | :---: | :---: |
| Reader SNR Low | Groups: 7 <br> Average Velocity: 16 <br> Variance: 0.36 | Groups: 1 <br> Average Velocity: 60.8 Variance: N/A | Groups:None Observed |
| Reader SNR <br> Medium | $\begin{gathered} \text { Groups: } 2 \\ \text { Velocity: } 52.7 \\ \text { Variance: } 0.13 \end{gathered}$ | Groups: 3 <br> Average Velocity: 41.8 <br> Variance: . 24 | Groups:None Observed |
| $\begin{gathered} \text { Reader } \\ \text { SNR } \\ \text { High } \end{gathered}$ | Groups: 4 Average Velocity: 15.5 Variance: 0.03 | Groups: 2 <br> Average Velocity: 28.1 <br> Variance: 0.11 | Groups:1 Average Velocity:45.3 Variance:N/A |

Table 4.6: Configuration 2, $40 \mathrm{~cm} / \mathrm{s}$ TD-PDOA Results

|  | Tag SNR <br> Low | Tag SNR <br> Medium | Tag SNR <br> High |
| :---: | :---: | :---: | :---: |
| Reader | Groups: 7 | Groups: None Observed | Groups:None Observed |
| SNR | Average Velocity: -22.7 |  |  |
| Low | Variance: 0.61 |  |  |
| Reader | Groups: 4 | Groups: 1 | Groups:None Observed |
| SNR | Velocity: 26.1 | Average Velocity: 78.3 |  |
| Medium | Variance: 0.95 | Variance: N/A |  |
| Reader | Groups: 6 | Groups: None Observed | Groups:2 |
| SNR | Average Velocity: 66.8 |  | Average Velocity:32.7 |
| High | Variance: 0.81 |  | Variance:0.43 |

calculations below were made assuming a tag moving in Configuration \#2. This configuration is the easiest for analysis, due to the fact that the motion of the tag generates a velocity vector that is one hundred percent in the direction of the sensor. In line with Richards [21], the Doppler frequency is the difference between the tx (reader) and $\mathrm{rx}(\mathrm{tag})$ frequencies. Equation 4.1 is used to calculate the value of this frequency given the velocity of the target relative to the sensor, $v_{r}$, the speed of light, $c$, and the carrier frequency, $f_{\text {carrier }}$. When the parameters of the system under test are entered into Equation 4.1, we arrive at $f_{d}=2.44 \mathrm{~Hz}$, as seen in Equation 4.2. This means that when we analyze the captured interaction, we would have to separate the responses into FFT bins of size 2.44 Hz or less. This proves problematic due to the bursty nature of the communications between the reader and tags. With the short bursts of response the smallest bin size that I was able to achieve in this research was 330 Hz , much larger than the 2.44 Hz that would be required to accurately estimate the velocity of the tag.

$$
\begin{equation*}
f_{d}=\frac{2 v_{r}}{c} f_{\text {carrier }} \tag{4.1}
\end{equation*}
$$

$$
\begin{equation*}
f_{d}=\frac{2(.4 \mathrm{~m} / \mathrm{s})}{3 \times 10^{8} \mathrm{~m} / \mathrm{s}} 915 \times 10^{6} \mathrm{~Hz}=2.44 \mathrm{~Hz} \tag{4.2}
\end{equation*}
$$

## V. Conclusions

### 5.1 Completed Objectives

The objectives of this research were attained as follows.
5.1.1 Validation of PDOA by Simulation. The simulations developed as a part of this researched showed that, given a strong signal, the PDOA metrics described in Chapter 2 will provide an accurate characterization of a moving target signal. This model included multipath from the table top and AGWN to simulate the lab environment.
5.1.2 Generate SID of RFID Tag in Physical Space. The results presented in Chapter 4 show a notable level of success in this area. While the SNR of both the captured tag reader and tag return impact the accuracy of the results greatly when the SNR is above certain thresholds, the calculated SIDs are within reasonable limits. Improvements to the SNR, expanded on in the future works section, would only serve to enhance the accuracy of this method.

### 5.2 Summary of Research Thrusts

This research's goal of successful SID measurement of a moving passive RFID tag is reliant on a foundation of four research thrusts. These thrusts are: algorithm theory, quality hardware, algorithm theory, and a reliable testbed.
5.2.1 Algorithm Theory. While the formulas for this research have been published previously [7], the publications did not provide any details to validate the correctness of the formulas. To this end, I started from basic princeples, and I solved for and derived in the literature. In this, an added level of confidence could be assigned to the accuracy of the formulas. In addition, the digital signal processing (DSP) theory for the USRP 1 was verified by construction of detailed block diagrams of the mainboard and the Flex 900 daughter card. Once the block diagram was created and the logical flow of the signal was mapped, the signal was modeled at each stage of the system. This analysis of the signal as it flowed through the system served to give the reader an understanding of the mixing of the signal from an analog RF signal to the digital baseband signal. That none of the specfic details required for the SID solution were omitted in any way.
5.2.2 Quality Hardware. The second thrust, quality hardware, showed issues with both the commercial tag reader and the USRP 1. Several assumptions were made in the early stages of the research that had to be adjusted as the research moved forward. First was control of the read patterns of the commercial Alien RFID reader. It was assumed that the reader would produce a rapid series of reads with little time gaps between queries when operating in Global Scroll mode. The reality was that the reads contained a series of large gaps in between them, a few as large as a second. This lack of control over the Alien 9800 read times created captures with an inconsistent number of reads per experiment. The lack of documentation also required
additional inital assumptions to be modified during the research. First among these was a lack of clear documenation for both the hardware and the supporting GNU Radio software. Installing the software and communicating with the radio is not a trival task. Following the installation documentation with the software, more often than not, resulted in a cryptic error message. This most often occured during the process of unpacking the software, compilation, and installation of the software on the system. Often collaboration with other students using the same system or searching online help forums was the only way to decipher the process. The other main concern with the USRP, was the sampling rate that was attainable for the research. The documented 64 megasample a second data rate is not achievable in reality on the hardware. As shown in the hardware description in Chapter 2 the ADC is capable of a raw 64 MSPS rate, but half of this is for the I portion and half being the Q portion. A large decimation rate is required to prevent overloading the USB interface. A sampling rate of 1.35 megasamples a second was the best achieved in practice by this research. The low sampling rate, after decimation, of the USRP 1 resulted in loss of fidelity in the data.
5.2.3 Algorithm Validation. A simulation of the testbed was created to validate the SID algorithms based on the assumption of a clear measurement of the target signal's phase. These simulations provided a verification that, given a accurate extraction of the phase of a signal, the PDOA metrics can be calculated from the captured data. The velocity of the target signal's source, reflection off of the table's
surface, and the path traveled in space were all modeled in MATLAB. Additive Gaussian White Noise was also added to the simulated signal based on the observed noise floor of the laboratory in use. These simulations support the results in Chapter 4, and show that the velocity and distance to the tag can be calculated within a reasonable margin of error given a sufficently high SNR.
5.2.4 Reliable Testbed. The testbed was able to reliably produce consistent speeds over a set track for data capture. The flexability of the pegboard surface allowed the four track configurations to be created and data recorded. There was some apparent stretching of the track's rope towards the end of data collection, so additional tension was later added but the velocity remained within $1 \mathrm{~cm} / \mathrm{s}$ of the target velocity. The only possible issue with the testbed would be the noise floor of the lab. The reconfiguration of large metal shelving units and desks between data collection periods could have changed the RF fingerprint of the lab, while the research was ongoing.

### 5.3 Contributions

Several contributions to SID and SDR community resulted from this research.
5.3.1 USRP 1 Documentation. When this research started, the documentation of the USRP 1 and Flex 900 daughter cards was either spread across several sources or minimal. In the process of determining the shortfalls of the gathered data, extensive research was completed on the hardware platform itself. In one instance,
the system schematic called out a crystal oscillator that was not on the board, the functionality had been moved to a synthesized oscillator. In another case, packaged integrated circuits were swapped for updated versions. While this is normally a form, fit, and function, the newer chips had different operating characteristics that were not documented. In both cases assumptions on the operation of the equipment needed to be adjusted to fit the hardware that was actually implemented.
5.3.2 Identified Capability Gaps in $S D R$. The USRP 1 is a very capable platform but has significant capability gaps in regards to spatial identification and navigation applications. In particular the sampling rate rates that are attainable do not support either TDOA or dopler ranging of targets as described in Chapter 4.
5.3.3 Validated Feasibility of Velocity Estimation using TD-PDOA. The ability to calculate an estimate of relative velocity of a target signal was demonstrated. While it is largely dependant on the SNR of the reader and tag, velocity was calculated within an order of magnitude for all observed SNR values.

### 5.4 Future Work

This research raised additional questions and opportunities for continued research.
5.4.1 Improved Simulation. One possible improvement to the modeling and simulation portion of this research would be to better model the reader/tag interaction. The current simulation models a continuous wave in the 915 MHz band.

A more complete model would modulate this wave with data, model the delay between reader Tx and tag Rx , attenuate the powers realistically. This could also represent the bursty nature of the RFID communication link with varying start and stop times of the data.
5.4.2 Develop Method to Increase SNR for RFID. With the robust OOK data encoding method, the primary focus of RFID tag antenna design is size to harvest enough power to reply. Additional effort and optimization of the antennas to improve the SNR would give the added benefit of improved SID accuracy. Increasing the SNR would also increase the read range and increase the number of situations in which the tags could be used.
5.4.3 Implement Reader on USRP N210. Transistioning the tag reader to the USRP N210 would give a researcher more control over the read cycles and enable more reads of the tag as it transits through the range of the reader. Compatibility issues would still have to taken into consideration so as to not violate the rules of the unlicensed spectrum band in which the tags operate in.

### 5.5 Summary

This research's goal of successful SID measurement of a moving passive RFID tag is reliant on a foundation of four research thrusts. These thrusts are: algorithm theory, quality hardware, algorithm validation and a reliable testbed. First, the algorithm theory was validated through signal analysis of the theoretical waveform as
it transition through the SDR and through the derivation of the PDOA metrics. Second thrust, quality hardware, did show some potential issues. The inability to precisely control the read sequence of the Alien 9800 and the limited sampling rate of the USRP 1 hampered the success of this area. The lack of control over the Alien 9800 read times created captures with an inconsistent number of reads per trip. The low sampling rate, after decimation, of the USRP 1 resulted in loss of fidelity in the data. Third, validation of the algorithm with the simulation adequately supported this research, but could befurther improved as mentioned in the future work section. Fourth, the testbed was able to reliably produce consistent speeds over a set track for data capture. The only possible issue with the testbed would be the noise floor of the lab. In summary, this research established a solid, four focused research foundation for continued investigation into SID with SDR.

## Appendix A. Raw Data

The following tables contain the raw data for the first three runs in configuration 2
at $10 \mathrm{~cm} / \mathrm{s}$.

Table A.1: Configuration $210 \mathrm{~cm} / \mathrm{s}$ Run 1

| Zoom <br> start <br> point | Reader <br> Epoch | Entire <br> Capture <br> Epoch | Time: | Phase <br> Read | Tag <br> Epoch | Entire <br> Capture <br> Epoch | Time: | Delta <br> Time | Phase <br> Response | Phase due to travel | Instant <br> Velocity |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 10800000 | 61525 | 10861525 | 8.045 | -2.0995 | 78579 | 10878579 | 8.058 | 0.01263 | 2.9787435 | 5.078279 | 10.44984 |
| 10800000 | 89577 | 10889577 | 8.066 | -0.6303 | 102955 | 10902955 | 8.076 | 0.00991 | -2.783440 | -2.15315 | -8.38029 |
| 10800000 | 116390 | 10916390 | 8.086 | -1.2789 | 129883 | 10929883 | 8.096 | 0.00999 | 2.9743207 | 4.253265 | 5.635786 |
| 10800000 | 148824 | 10948824 | 8.110 | -1.6221 | 162304 | 10962304 | 8.120 | 0.00998 | -2.556050 | -0.93393 | -0.16304 |
| 10800000 | 221530 | 11021530 | 8.164 | -2.3683 | 238534 | 11038534 | 8.176 | 0.01259 | -2.949371 | -0.58109 | 0.868145 |
| 10800000 | 249412 | 11049412 | 8.184 | -1.6176 | 262841 | 11062841 | 8.194 | 0.00995 | -2.797710 | -1.18016 | -5.48834 |
| 10800000 | 281175 | 11081175 | 8.208 | -1.4276 | 294716 | 11094716 | 8.218 | 0.01003 | 2.3586412 | 3.786259 | -0.16808 |
| 10800000 | 308104 | 11108104 | 8.228 | -1.3041 | 321596 | 11121596 | 8.238 | 0.00999 | 2.6104310 | 3.914521 | 1.383694 |
| 10800000 | 381521 | 11181521 | 8.282 | 2.21781 | 398528 | 11198528 | 8.295 | 0.0126 | 3.1102997 | 0.892490 | 8.049314 |
| 10800000 | 409497 | 11209497 | 8.303 | 1.79103 | 422933 | 11222933 | 8.313 | 0.00995 | -2.893336 | -4.68437 | -9.25181 |
| 10800000 | 441636 | 11241636 | 8.327 | -0.8304 | 454962 | 11254962 | 8.337 | 0.00987 | 2.8976389 | 3.728074 | 6.779140 |
| 10800000 | 468496 | 11268496 | 8.347 | -1.3499 | 481892 | 11281892 | 8.356 | 0.00992 | -2.804587 | $-1.45471$ | -0.19796 |
| 10800000 | 541528 | 11341528 | 8.401 | -2.0384 | 558531 | 11358531 | 8.413 | 0.01259 | -3.062421 | -1.02400 | -5.91455 |
| 10800000 | 569410 | 11369410 | 8.421 | -1.2906 | 587803 | 11387803 | 8.435 | 0.01362 | 2.6003854 | 3.891030 | 5.480277 |
| 10800000 | 606006 | 11406006 | 8.448 | -1.7395 | 619420 | 11419420 | 8.458 | 0.00994 | -2.767483 | -1.02795 | -0.09787 |
| 10800000 | 638228 | 11438228 | 8.472 | -1.7879 | 651675 | 11451675 | 8.482 | 0.00996 | -2.726226 | -0.93833 | -3.10429 |
| 10800000 | 701510 | 11501510 | 8.519 | -2.0134 | 718578 | 11518578 | 8.532 | 0.01264 | 2.9442863 | 4.957697 | 0.732851 |
| 10800000 | 729392 | 11529392 | 8.540 | -1.2732 | 749108 | 11549108 | 8.554 | 0.0146 | 3.0492997 | 4.322520 | 10.11914 |
| 10800000 | 767536 | 11567536 | 8.568 | 1.91484 | 780970 | 11580970 | 8.578 | 0.00995 | -2.915754 | -4.83059 | -0.03560 |
| 10800000 | 794398 | 11594398 | 8.588 | 2.02606 | 807899 | 11607899 | 8.598 | 0.01 | -2.777317 | -4.80338 | -2.69866 |
| 10800000 | 861517 | 11661517 | 8.638 | 2.3333 | 878507 | 11678507 | 8.650 | 0.01258 | 2.9393849 | 0.606085 | -1.24761 |
| 10800000 | 889443 | 11689443 | 8.658 | 1.62808 | 902846 | 11702846 | 8.668 | 0.00993 | 3.0962222 | 1.468139 | 2.901882 |
| 10800000 | 917350 | 11717350 | 8.679 | -1.7498 | 930797 | 11730797 | 8.689 | 0.00996 | -2.584344 | -0.83452 | -5.25501 |
| 10800000 | 949212 | 11749212 | 8.703 | -1.5892 | 962852 | 11762852 | 8.713 | 0.0101 | 2.3584122 | 3.947612 | -0.72886 |
| 10800000 | $1 \mathrm{E}+006$ | 11821507 | 8.756 | -2.5404 | $1 \mathrm{E}+006$ | 11838609 | 8.769 | 0.01267 | 2.9747465 | 5.515160 | 9.767917 |
| 10800000 | $1 \mathrm{E}+006$ | 11849406 | 8.777 | -1.4816 | $1 \mathrm{E}+006$ | 11862835 | 8.787 | 0.00995 | -2.684394 | -1.20277 | -8.00987 |
| 10800000 | $1 \mathrm{E}+006$ | 11876350 | 8.797 | -1.8086 | $1 \mathrm{E}+006$ | 11889762 | 8.807 | 0.00993 | 3.1116312 | 4.920246 | 6.658885 |
| 10800000 | $1 \mathrm{E}+006$ | 11903329 | 8.817 | -1.2913 | $1 \mathrm{E}+006$ | 11921611 | 8.830 | 0.01354 | -2.391757 | -1.10049 | -0.10717 |
| 10800000 | $1 \mathrm{E}+006$ | 11981558 | 8.875 | -1.6544 | $1 \mathrm{E}+006$ | 11998545 | 8.887 | 0.01258 | -2.520830 | -0.86641 | 0.365167 |
| 10800000 | $1 \mathrm{E}+006$ | 12009356 | 8.895 | -1.6104 | $1 \mathrm{E}+006$ | 12022818 | 8.905 | 0.00997 | -2.728411 | -1.11804 | -0.64587 |
| 10800000 | $1 \mathrm{E}+006$ | 12036283 | 8.915 | -2.1400 | 1E+006 | 12050271 | 8.926 | 0.01036 | -2.754627 | -0.61467 | -0.02276 |
| 10800000 | $1 \mathrm{E}+006$ | 12063785 | 8.936 | -2.2652 | $1 \mathrm{E}+006$ | 12082101 | 8.949 | 0.01357 | -2.859319 | -0.59410 | -0.02808 |
| 10800000 | 1E+006 | 12141507 | 8.993 | -2.4388 | $1 \mathrm{E}+006$ | 12158544 | 9.006 | 0.01262 | -2.971918 | -0.53316 | -8.71111 |
| 10800000 | $1 \mathrm{E}+006$ | 12169387 | 9.014 | -2.4089 | $1 \mathrm{E}+006$ | 12182932 | 9.024 | 0.01003 | 3.0891168 | 5.498015 | 1.057119 |

Table A.1: Configuration $210 \mathrm{~cm} / \mathrm{s}$ Run 1

| Zoom <br> start <br> point | Reader <br> Epoch | Entire <br> Capture <br> Epoch | Time: | Phase <br> Read | Tag <br> Epoch | Entire <br> Capture <br> Epoch | Time: | Delta <br> Time | Phase <br> Response | Phase <br> due to <br> travel | Instant <br> Velocity |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 10800000 | 1E+006 | 12196398 | 9.034 | -2.2082 | $1 \mathrm{E}+006$ | 12209859 | 9.044 | 0.00997 | 2.4817541 | 4.689918 | -0.32624 |
| 10800000 | 1E+006 | 12223212 | 9.054 | -2.2046 | $1 \mathrm{E}+006$ | 12241559 | 9.067 | 0.01359 | 2.7789235 | 4.983511 | -0.08515 |
| 10800000 | $2 \mathrm{E}+006$ | 12301459 | 9.112 | -2.2706 | $2 \mathrm{E}+006$ | 12318478 | 9.124 | 0.01261 | 2.8988199 | 5.169441 | 8.306549 |
| 10800000 | $2 \mathrm{E}+006$ | 12329405 | 9.132 | -2.1271 | $2 \mathrm{E}+006$ | 12342803 | 9.142 | 0.00992 | -2.693895 | -0.56678 | 2.216121 |
| 10800000 | $2 \mathrm{E}+006$ | 12356370 | 9.152 | -0.6989 | $2 \mathrm{E}+006$ | 12369731 | 9.162 | 0.0099 | -2.959818 | -2.26092 | -1.67155 |
| 10800000 | $2 \mathrm{E}+006$ | 12383164 | 9.172 | -2.1330 | $2 \mathrm{E}+006$ | 12396643 | 9.182 | 0.00998 | -3.116866 | -0.98384 | -0.00593 |
| $2.30 \mathrm{E}+07$ | 511783 | 23511783 | 17.42 | 1.48801 | 528714 | 23528714 | 17.43 | 0.01254 | 2.3789842 | 0.890971 | -0.30793 |
| $2.30 \mathrm{E}+07$ | 539560 | 23539560 | 17.44 | 0.85039 | 553050 | 23553050 | 17.45 | 0.00999 | 1.9541020 | 1.103712 | 0.426082 |
| $2.30 \mathrm{E}+07$ | 571346 | 23571346 | 17.46 | 1.58806 | 584854 | 23584854 | 17.47 | 0.01001 | 2.3070714 | 0.719008 | -1.38454 |
| $2.30 \mathrm{E}+07$ | 598293 | 23598293 | 17.48 | 0.93451 | 611828 | 23611828 | 17.49 | 0.01003 | 2.7137572 | 1.779248 | 0.497871 |
| $2.30 \mathrm{E}+07$ | 671400 | 23671400 | 17.53 | 1.19560 | 688407 | 23688407 | 17.55 | 0.0126 | 1.8924730 | 0.696871 | 0.259281 |
| $2.30 \mathrm{E}+07$ | 699312 | 23699312 | 17.55 | 1.3826 | 712803 | 23712803 | 17.56 | 0.00999 | 1.8998977 | 0.517298 | 0.259668 |
| $2.30 \mathrm{E}+07$ | 732280 | 23732280 | 17.58 | 2.79728 | 746903 | 23746903 | 17.59 | 0.01083 | 3.0631997 | 0.265922 | -0.91961 |
| $2.30 \mathrm{E}+07$ | 760421 | 23760421 | 17.60 | 0.75412 | 773739 | 23773739 | 17.61 | 0.00986 | 1.7206449 | 0.966523 | 0.201159 |
| $2.30 \mathrm{E}+07$ | 831369 | 23831369 | 17.65 | 1.74333 | 848439 | 23848439 | 17.66 | 0.01264 | 2.2832593 | 0.539932 | -0.78203 |
| $2.30 \mathrm{E}+07$ | 859330 | 23859330 | 17.67 | 1.10158 | 872804 | 23872804 | 17.68 | 0.00998 | 2.1824441 | 1.080863 | 0.133725 |
| $2.30 \mathrm{E}+07$ | 886242 | 23886242 | 17.69 | 1.07354 | 899732 | 23899732 | 17.70 | 0.00999 | 2.0521763 | 0.978635 | 0.316592 |
| $2.30 \mathrm{E}+07$ | 913233 | 23913233 | 17.71 | 0.74765 | 931412 | 23931412 | 17.73 | 0.01347 | 1.4415528 | 0.693902 | -0.05014 |
| $2.30 \mathrm{E}+07$ | 991417 | 23991417 | 17.77 | 1.58625 | $1 \mathrm{E}+006$ | 24008408 | 17.78 | 0.01259 | 2.3897480 | 0.803494 | -0.63257 |
| $2.30 \mathrm{E}+07$ | 1E+006 | 24019253 | 17.79 | 0.88346 | $1 \mathrm{E}+006$ | 24037493 | 17.80 | 0.01351 | 2.2092731 | 1.325809 | -0.70565 |
| $2.30 \mathrm{E}+07$ | 1E+006 | 24051042 | 17.81 | 0.40505 | $1 \mathrm{E}+006$ | 24074126 | 17.83 | 0.0171 | 2.4647209 | 2.059674 | 0.548998 |
| $2.30 \mathrm{E}+07$ | 1E+006 | 24087595 | 17.84 | 0.92734 | $1 \mathrm{E}+006$ | 24101115 | 17.85 | 0.01001 | 2.5663723 | 1.639035 | 0.276639 |
| $2.30 \mathrm{E}+07$ | 1E+006 | 24155387 | 17.89 | 1.49234 | $1 \mathrm{E}+006$ | 24172456 | 17.90 | 0.01264 | 2.5710935 | 1.078756 | -0.12577 |
| $2.30 \mathrm{E}+07$ | $1 \mathrm{E}+006$ | 24183223 | 17.91 | 0.92647 | $1 \mathrm{E}+006$ | 24196728 | 17.92 | 0.01 | 2.0918927 | 1.165422 | 0.685749 |
| $2.30 \mathrm{E}+07$ | $1 \mathrm{E}+006$ | 24210166 | 17.93 | 0.93909 | $1 \mathrm{E}+006$ | 24223610 | 17.94 | 0.00996 | 1.5811822 | 0.642088 | -0.19875 |
| $2.30 \mathrm{E}+07$ | 1E+006 | 24237078 | 17.95 | 0.90220 | $1 \mathrm{E}+006$ | 24255461 | 17.97 | 0.01362 | 1.7240024 | 0.821801 | 0.098102 |
| $2.30 \mathrm{E}+07$ | 1E+006 | 24311387 | 18.01 | 1.37629 | $1 \mathrm{E}+006$ | 24328363 | 18.02 | 0.01257 | 1.9950587 | 0.618767 | -0.64668 |
| $2.30 \mathrm{E}+07$ | $1 \mathrm{E}+006$ | 24339254 | 18.03 | 0.87465 | $1 \mathrm{E}+006$ | 24352681 | 18.04 | 0.00995 | 1.9398616 | 1.065215 | 0.026768 |
| $2.30 \mathrm{E}+07$ | 1E+006 | 24366166 | 18.05 | 0.78972 | $1 \mathrm{E}+006$ | 24379609 | 18.06 | 0.00996 | 1.8344743 | 1.044751 | -0.61152 |
| $2.30 \mathrm{E}+07$ | 1E+006 | 24393077 | 18.07 | 1.17960 | $1 \mathrm{E}+006$ | 24411348 | 18.08 | 0.01353 | 2.7753524 | 1.595754 | 0.296891 |
| $2.30 \mathrm{E}+07$ | $1 \mathrm{E}+006$ | 24471419 | 18.13 | 1.11693 | $1 \mathrm{E}+006$ | 24488457 | 18.14 | 0.01262 | 2.0627770 | 0.945843 | 0.239065 |
| $2.30 \mathrm{E}+07$ | $1 \mathrm{E}+006$ | 24499286 | 18.15 | 0.63708 | $2 \mathrm{E}+006$ | 24517450 | 18.16 | 0.01345 | 1.3861503 | 0.749072 | -0.21702 |
| $2.30 \mathrm{E}+07$ | $2 \mathrm{E}+006$ | 24530932 | 18.17 | 1.03284 | $2 \mathrm{E}+006$ | 24544344 | 18.18 | 0.00993 | 1.9476063 | 0.914764 | 0.136882 |
| $2.30 \mathrm{E}+07$ | $2 \mathrm{E}+006$ | 24562688 | 18.19 | 1.16778 | $2 \mathrm{E}+006$ | 24581025 | 18.21 | 0.01358 | 1.9400059 | 0.772223 | 0.008244 |
| $2.30 \mathrm{E}+07$ | $2 \mathrm{E}+006$ | 24631388 | 18.24 | 1.29373 | $2 \mathrm{E}+006$ | 24648364 | 18.26 | 0.01257 | 2.0501966 | 0.756464 | -0.05243 |
| $2.30 \mathrm{E}+07$ | $2 \mathrm{E}+006$ | 24659208 | 18.27 | 0.87256 | $2 \mathrm{E}+006$ | 24672667 | 18.28 | 0.00997 | 1.6652033 | 0.792640 | -0.69494 |
| $2.30 \mathrm{E}+07$ | $2 \mathrm{E}+006$ | 24686167 | 18.29 | 0.76857 | $2 \mathrm{E}+006$ | 24699625 | 18.30 | 0.00997 | 2.0930608 | 1.324486 | 0.543424 |
| $2.30 \mathrm{E}+07$ | $2 \mathrm{E}+006$ | 24713236 | 18.31 | 0.52206 | $2 \mathrm{E}+006$ | 24726523 | 18.31 | 0.00984 | 1.4315862 | 0.909522 | -0.05607 |
| $2.30 \mathrm{E}+07$ | $2 \mathrm{E}+006$ | 24791373 | 18.36 | 1.51850 | $2 \mathrm{E}+006$ | 24808411 | 18.38 | 0.01262 | 2.5583655 | 1.039864 | 0.119496 |
| $2.30 \mathrm{E}+07$ | $2 \mathrm{E}+006$ | 24819256 | 18.38 | 0.96203 | $2 \mathrm{E}+006$ | 24832699 | 18.39 | 0.00996 | 1.9194984 | 0.957470 | -0.28046 |

Table A.1: Configuration $210 \mathrm{~cm} / \mathrm{s}$ Run 1

| Zoom <br> start <br> point | Reader <br> Epoch | Entire <br> Capture <br> Epoch | Time: | Phase <br> Read | $\begin{gathered} \text { Tag } \\ \text { Epoch } \end{gathered}$ | Entire <br> Capture <br> Epoch | Time: | Delta <br> Time | Phase <br> Response | Phase due to travel | Instant <br> Velocity |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $2.30 \mathrm{E}+07$ | $2 \mathrm{E}+006$ | 24846152 | 18.40 | 1.05035 | $2 \mathrm{E}+006$ | 24864424 | 18.42 | 0.01353 | 2.2604187 | 1.210069 | -0.59227 |
| $2.30 \mathrm{E}+07$ | $2 \mathrm{E}+006$ | 24877862 | 18.43 | 0.92354 | $2 \mathrm{E}+006$ | 24891366 | 18.44 | 0.01 | 2.5866133 | 1.663070 | 0.524247 |
| $2.30 \mathrm{E}+07$ | $2 \mathrm{E}+006$ | 24951420 | 18.48 | 1.425 | $2 \mathrm{E}+006$ | 24968381 | 18.49 | 0.01256 | 1.9418616 | 0.516862 | -0.68357 |
| $2.30 \mathrm{E}+07$ | $2 \mathrm{E}+006$ | 24979257 | 18.50 | 0.41037 | $2 \mathrm{E}+006$ | 24997514 | 18.52 | 0.01352 | 1.4925825 | 1.082214 | -0.44025 |
| $2.30 \mathrm{E}+07$ | $2 \mathrm{E}+006$ | 25010981 | 18.53 | 0.82648 | $2 \mathrm{E}+006$ | 25024517 | 18.54 | 0.01003 | 2.2461851 | 1.419706 | 0.151377 |
| $2.30 \mathrm{E}+07$ | $2 \mathrm{E}+006$ | 25037924 | 18.55 | 0.86507 | $2 \mathrm{E}+006$ | 25051382 | 18.56 | 0.00997 | 2.1693273 | 1.304255 | 0.010313 |
| $3.30 \mathrm{E}+07$ | 111259 | 33111259 | 24.53 | -0.1761 | 128213 | 33128213 | 24.54 | 0.01256 | -1.236608 | -1.06055 | 1.849340 |
| $3.30 \mathrm{E}+07$ | 139082 | 33139082 | 24.55 | 0.49794 | 152561 | 33152561 | 24.56 | 0.00998 | -1.840907 | -2.33885 | 0.381486 |
| $3.30 \mathrm{E}+07$ | 166086 | 33166086 | 24.57 | 0.66892 | 179511 | 33179511 | 24.58 | 0.00994 | -1.961796 | -2.63072 | -0.88498 |
| $3.30 \mathrm{E}+07$ | 192944 | 33192944 | 24.59 | 0.16991 | 211273 | 33211273 | 24.6 | 0.01358 | -1.662823 | -1.83273 | -0.09682 |
| $3.30 \mathrm{E}+07$ | 271213 | 33271213 | 24.64 | -0.3536 | 288257 | 33288257 | 24.66 | 0.01262 | -1.974702 | -1.62114 | 0.308017 |
| $3.30 \mathrm{E}+07$ | 299088 | 33299088 | 24.66 | -0.0960 | 317379 | 33317379 | 24.68 | 0.01355 | -1.971796 | -1.87579 | 0.132293 |
| $3.30 \mathrm{E}+07$ | 330844 | 33330844 | 24.69 | 0.05693 | 344377 | 33344377 | 24.70 | 0.01002 | -1.920258 | -1.97719 | -0.89252 |
| $3.30 \mathrm{E}+07$ | 357772 | 33357772 | 24.71 | -0.2095 | 371225 | 33371225 | 24.72 | 0.00996 | -1.506429 | -1.29692 | 0.216197 |
| $3.30 \mathrm{E}+07$ | 431208 | 33431208 | 24.76 | -0.4358 | 448268 | 33448268 | 24.78 | 0.01264 | -2.205589 | -1.76978 | 0.703661 |
| $3.30 \mathrm{E}+07$ | 459164 | 33459164 | 24.78 | 0.30136 | 472616 | 33472616 | 24.79 | 0.00996 | -1.954799 | -2.25616 | -0.50746 |
| $3.30 \mathrm{E}+07$ | 486065 | 33486065 | 24.80 | -0.0826 | 504469 | 33504469 | 24.82 | 0.01363 | -1.879849 | -1.79728 | -0.04368 |
| $3.30 \mathrm{E}+07$ | 517961 | 33517961 | 24.83 | 0.23980 | 532438 | 33532438 | 24.84 | 0.01072 | -1.522795 | -1.76260 | 1.611850 |
| $3.30 \mathrm{E}+07$ | 591254 | 33591254 | 24.88 | 3.04007 | 608245 | 33608245 | 24.89 | 0.01259 | -2.191379 | -5.23145 | -1.55782 |
| $3.30 \mathrm{E}+07$ | 619128 | 33619128 | 24.90 | 2.74949 | 632545 | 33632545 | 24.91 | 0.00994 | -1.407287 | -4.15678 | -0.21254 |
| $3.30 \mathrm{E}+07$ | 646024 | 33646024 | 24.92 | 2.71930 | 664860 | 33664860 | 24.94 | 0.01395 | -1.242505 | -3.96180 | 0.227124 |
| $3.30 \mathrm{E}+07$ | 678398 | 33678398 | 24.95 | 2.43701 | 691745 | 33691745 | 24.96 | 0.00989 | -1.698146 | -4.13515 | -2.36257 |
| $3.30 \mathrm{E}+07$ | 751260 | 33751260 | 25 | -3.0880 | 768224 | 33768224 | 25.01 | 0.01257 | -2.093590 | 0.994395 | 7.994864 |
| $3.30 \mathrm{E}+07$ | 779080 | 33779080 | 25.02 | 2.66586 | 793676 | 33793676 | 25.03 | 0.01081 | -2.116514 | -4.78237 | -4.32620 |
| $3.30 \mathrm{E}+07$ | 807109 | 33807109 | 25.04 | 0.11399 | 821651 | 33821651 | 25.05 | 0.01077 | -1.232576 | $-1.34657$ | 3.675206 |
| $3.30 \mathrm{E}+07$ | 835071 | 33835071 | 25.06 | 2.74980 | 848547 | 33848547 | 25.07 | 0.00998 | -1.402987 | -4.15278 | -1.31952 |
| $3.30 \mathrm{E}+07$ | 911204 | 33911204 | 25.12 | -0.4955 | 928216 | 33928216 | 25.13 | 0.0126 | -1.663833 | -1.16837 | 0.76138 |
| $3.30 \mathrm{E}+07$ | 939187 | 33939187 | 25.14 | 0.38339 | 953621 | 33953621 | 25.15 | 0.01069 | -1.334106 | -1.71750 | 2.621952 |
| $3.30 \mathrm{E}+07$ | 967068 | 33967068 | 25.16 | 2.81961 | 980566 | 33980566 | 25.17 | 0.01 | -0.903539 | -3.72315 | 0.579102 |
| $3.30 \mathrm{E}+07$ | 993980 | 33993980 | 25.18 | 2.55259 | $1 \mathrm{E}+006$ | 34007456 | 25.19 | 0.00998 | -1.612640 | -4.16523 | -2.63255 |
| $3.30 \mathrm{E}+07$ | $1 \mathrm{E}+006$ | 34071229 | 25.24 | -2.9581 | 1E+006 | 34088269 | 25.25 | 0.01262 | -1.083709 | 1.874405 | 8.835876 |
| $3.30 \mathrm{E}+07$ | $1 \mathrm{E}+006$ | 34099151 | 25.26 | 2.62679 | $1 \mathrm{E}+006$ | 34112611 | 25.27 | 0.00997 | -1.604820 | -4.23161 | 0.992496 |
| $3.30 \mathrm{E}+07$ | $1 \mathrm{E}+006$ | 34126074 | 25.28 | 2.70403 | 1E+006 | 34140643 | 25.29 | 0.01079 | -2.317410 | -5.02144 | -0.59434 |
| $3.30 \mathrm{E}+07$ | $1 \mathrm{E}+006$ | 34155153 | 25.30 | 2.79563 | 1E+006 | 34173381 | 25.31 | 0.0135 | -1.673429 | -4.46906 | 0.195967 |
| $3.30 \mathrm{E}+07$ | $1 \mathrm{E}+006$ | 34231251 | 25.36 | 3.00429 | 1E+006 | 34248210 | 25.37 | 0.01256 | -1.881068 | -4.88536 | -0.78551 |
| $3.30 \mathrm{E}+07$ | $1 \mathrm{E}+006$ | 34259098 | 25.38 | 2.46819 | 1E+006 | 34272531 | 25.39 | 0.00995 | -1.874815 | -4.34300 | 0.034352 |
| $3.30 \mathrm{E}+07$ | $1 \mathrm{E}+006$ | 34286021 | 25.40 | 2.53278 | 1E+006 | 34299454 | 25.41 | 0.00995 | -1.836478 | -4.36926 | -0.54023 |
| $3.30 \mathrm{E}+07$ | $1 \mathrm{E}+006$ | 34312901 | 25.42 | 2.51793 | $1 \mathrm{E}+006$ | 34326388 | 25.43 | 0.00999 | -1.438246 | -3.95618 | 0.059779 |
| $3.30 \mathrm{E}+07$ | $1 \mathrm{E}+006$ | 34391386 | 25.47 | 2.49403 | 1E+006 | 34408292 | 25.49 | 0.01252 | -1.601150 | -4.09518 | 0.556347 |
| $3.30 \mathrm{E}+07$ | $1 \mathrm{E}+006$ | 34419169 | 25.49 | 2.46868 | $1 \mathrm{E}+006$ | 34433733 | 25.51 | 0.01079 | -2.028320 | -4.49700 | -1.63533 |

Table A.1: Configuration $210 \mathrm{~cm} / \mathrm{s}$ Run 1

| Zoom <br> start <br> point | Reader <br> Epoch | Entire <br> Capture <br> Epoch | Time: | Phase <br> Read | $\begin{gathered} \text { Tag } \\ \text { Epoch } \end{gathered}$ | Entire <br> Capture <br> Epoch | Time: | Delta <br> Time | Phase <br> Response | Phase due to travel | Instant <br> Velocity |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $3.30 \mathrm{E}+07$ | $1 \mathrm{E}+006$ | 34456939 | 25.52 | -0.0873 | $1 \mathrm{E}+006$ | 34470477 | 25.53 | 0.01003 | $-2.878418$ | -2.79113 | -0.13161 |
| $3.30 \mathrm{E}+07$ | $1 \mathrm{E}+006$ | 34483884 | 25.54 | 0.22045 | 1E+006 | 34497352 | 25.55 | 0.00998 | -2.470269 | -2.69072 | -0.64302 |
| $3.30 \mathrm{E}+07$ | $2 \mathrm{E}+006$ | 34551229 | 25.59 | -0.4855 | $2 \mathrm{E}+006$ | 34568214 | 25.60 | 0.01258 | -1.882600 | -1.39715 | -0.31313 |
| $3.30 \mathrm{E}+07$ | $2 \mathrm{E}+006$ | 34579142 | 25.61 | 0.08890 | $2 \mathrm{E}+006$ | 34593738 | 25.62 | 0.01081 | -1.081352 | -1.17025 | 3.077118 |
| $3.30 \mathrm{E}+07$ | $2 \mathrm{E}+006$ | 34611991 | 25.64 | 2.52466 | $2 \mathrm{E}+006$ | 34625397 | 25.65 | 0.00993 | -1.411219 | -3.93588 | -0.69725 |
| $3.30 \mathrm{E}+07$ | $2 \mathrm{E}+006$ | 34639408 | 25.66 | 2.39153 | $2 \mathrm{E}+006$ | 34652815 | 25.67 | 0.00993 | -1.001636 | -3.39316 | -0.01935 |
| $4.42 \mathrm{E}+07$ | 99949 | 44299949 | 32.81 | -1.4063 | 116997 | 44316997 | 32.83 | 0.01263 | 0.5094232 | 1.915766 | -0.39720 |
| $4.42 \mathrm{E}+07$ | 127926 | 44327926 | 32.83 | -2.4883 | 141352 | 44341352 | 32.84 | 0.00994 | -0.297935 | 2.190394 | -0.09089 |
| $4.42 \mathrm{E}+07$ | 159732 | 44359732 | 32.86 | -2.4039 | 177968 | 44377968 | 32.87 | 0.01351 | -0.119007 | 2.284871 | -1.64318 |
| $4.42 \mathrm{E}+07$ | 191425 | 44391425 | 32.88 | -3.0233 | 209900 | 44409900 | 32.89 | 0.01368 | 0.7510971 | 3.774446 | 1.181410 |
| $4.42 \mathrm{E}+07$ | 259945 | 44459945 | 32.93 | -2.1126 | 276972 | 44476972 | 32.94 | 0.01261 | -0.587667 | 1.524905 | -1.71872 |
| $4.42 \mathrm{E}+07$ | 287828 | 44487828 | 32.95 | -2.9523 | 306097 | 44506097 | 32.97 | 0.01353 | -0.006286 | 2.945998 | 0.657109 |
| $4.42 \mathrm{E}+07$ | 319522 | 44519522 | 32.98 | -2.6777 | 332974 | 44532974 | 32.99 | 0.00996 | -0.233051 | 2.444614 | -0.81560 |
| $4.42 \mathrm{E}+07$ | 346502 | 44546502 | 33.00 | -2.7767 | 359964 | 44559964 | 33.01 | 0.00997 | 0.2928391 | 3.069543 | 0.469322 |
| $4.42 \mathrm{E}+07$ | 419980 | 44619980 | 33.05 | -2.4545 | 436959 | 44636959 | 33.06 | 0.01258 | -0.410784 | 2.043689 | -0.31092 |
| $4.42 \mathrm{E}+07$ | 447889 | 44647889 | 33.07 | -2.7029 | 461370 | 44661370 | 33.08 | 0.00999 | -0.443709 | 2.259160 | 0.135034 |
| $4.42 \mathrm{E}+07$ | 479670 | 44679670 | 33.09 | $-2.3500$ | 493112 | 44693112 | 33.10 | 0.00996 | -0.212534 | 2.137476 | -1.94769 |
| $4.42 \mathrm{E}+07$ | 506611 | 44706611 | 33.11 | -2.8954 | 520218 | 44720218 | 33.12 | 0.01008 | 0.7408885 | 3.636257 | 0.757808 |
| $4.42 \mathrm{E}+07$ | 579938 | 44779938 | 33.17 | $-2.3131$ | 597007 | 44797007 | 33.18 | 0.01264 | -0.328878 | 1.984257 | -1.64709 |
| $4.42 \mathrm{E}+07$ | 607908 | 44807908 | 33.19 | -2.7298 | 621457 | 44821457 | 33.20 | 0.01004 | 0.3977147 | 3.127523 | 1.194417 |
| $4.42 \mathrm{E}+07$ | 639634 | 44839634 | 33.21 | $-2.6717$ | 653044 | 44853044 | 33.22 | 0.00993 | -0.615266 | 2.056456 | -1.33198 |
| $4.42 \mathrm{E}+07$ | 666511 | 44866511 | 33.23 | -2.9049 | 680018 | 44880018 | 33.24 | 0.01 | 0.1715913 | 3.076445 | 0.390516 |
| $4.42 \mathrm{E}+07$ | 739989 | 44939989 | 33.29 | -2.5782 | 756952 | 44956952 | 33.3 | 0.01256 | -0.354646 | 2.223523 | -0.61998 |
| $4.42 \mathrm{E}+07$ | 767927 | 44967927 | 33.31 | -2.7409 | 786675 | 44986675 | 33.32 | 0.01389 | 0.0057913 | 2.746670 | 5.917805 |
| $4.42 \mathrm{E}+07$ | 805167 | 45005167 | 33.34 | 2.78574 | 818491 | 45018491 | 33.35 | 0.00987 | 0.1872757 | -2.59846 | -5.83051 |
| $4.42 \mathrm{E}+07$ | 841655 | 45041655 | 33.36 | -2.9363 | 855204 | 45055204 | 33.37 | 0.01004 | 0.5420611 | 3.478392 | 0.872129 |
| $4.42 \mathrm{E}+07$ | 899937 | 45099937 | 33.41 | -2.1936 | 916977 | 45116977 | 33.42 | 0.01262 | -0.244676 | 1.948955 | -1.43845 |
| $4.42 \mathrm{E}+07$ | 927788 | 45127788 | 33.43 | -2.7638 | 941295 | 45141295 | 33.44 | 0.01 | 0.1782153 | 2.942011 | 0.605399 |
| $4.42 \mathrm{E}+07$ | 954768 | 45154768 | 33.45 | -2.8331 | 968204 | 45168204 | 33.46 | 0.00995 | -0.353615 | 2.479533 | -0.83931 |
| $4.42 \mathrm{E}+07$ | 981642 | 45181642 | 33.47 | -2.7214 | 995223 | 45195223 | 33.48 | 0.01006 | 0.4019354 | 3.123319 | 0.343473 |
| $4.42 \mathrm{E}+07$ | $1 \mathrm{E}+006$ | 45260036 | 33.52 | -2.8088 | $1 \mathrm{E}+006$ | 45276983 | 33.54 | 0.01255 | -0.482682 | 2.326084 | -0.31820 |
| $4.42 \mathrm{E}+07$ | $1 \mathrm{E}+006$ | 45287823 | 33.54 | -2.7984 | $1 \mathrm{E}+006$ | 45306053 | 33.56 | 0.0135 | -0.209744 | 2.588685 | 6.43149 |
| $4.42 \mathrm{E}+07$ | 1E+006 | 45320638 | 33.57 | 1.51790 | 1E+006 | 45334047 | 33.58 | 0.00993 | -1.004684 | -2.52258 | 0.195720 |
| $4.42 \mathrm{E}+07$ | $1 \mathrm{E}+006$ | 45347586 | 33.59 | 1.63190 | 1E+006 | 45360982 | 33.60 | 0.00992 | -1.040338 | -2.67224 | -0.55511 |
| $4.42 \mathrm{E}+07$ | $1 \mathrm{E}+006$ | 45419944 | 33.64 | 1.02501 | 1E+006 | 45436974 | 33.66 | 0.01261 | -0.449656 | -1.47467 | 1.719017 |
| $4.42 \mathrm{E}+07$ | $1 \mathrm{E}+006$ | 45447815 | 33.66 | 1.27193 | 1E+006 | 45461391 | 33.67 | 0.01006 | -1.394322 | -2.66625 | 0.004017 |
| $4.42 \mathrm{E}+07$ | $1 \mathrm{E}+006$ | 45474750 | 33.68 | 1.38203 | 1E+006 | 45488310 | 33.69 | 0.01004 | -1.287296 | -2.66932 | 0.360904 |
| $4.42 \mathrm{E}+07$ | $1 \mathrm{E}+006$ | 45501727 | 33.70 | 1.77337 | $1 \mathrm{E}+006$ | 45515155 | 33.71 | 0.00995 | -1.170995 | -2.94437 | -0.36024 |
| $4.42 \mathrm{E}+07$ | $1 \mathrm{E}+006$ | 45579953 | 33.76 | 0.89948 | $1 \mathrm{E}+006$ | 45597002 | 33.77 | 0.01263 | -1.207848 | -2.10733 | -0.52593 |
| $4.42 \mathrm{E}+07$ | $1 \mathrm{E}+006$ | 45607837 | 33.78 | 1.43360 | $1 \mathrm{E}+006$ | 45621288 | 33.79 | 0.00996 | -0.311114 | $-1.74472$ | 0.491856 |

Table A.1: Configuration $210 \mathrm{~cm} / \mathrm{s}$ Run 1

| Zoom <br> start <br> point | Reader <br> Epoch | Entire <br> Capture <br> Epoch | Time: | Phase <br> Read | $\begin{gathered} \text { Tag } \\ \text { Epoch } \end{gathered}$ | Entire <br> Capture <br> Epoch | Time: | Delta <br> Time | Phase <br> Response | Phase <br> due to <br> travel | Instant <br> Velocity |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $4.42 \mathrm{E}+07$ | $1 \mathrm{E}+006$ | 45634730 | 33.80 | 1.11277 | 1E+006 | 45648242 | 33.81 | 0.01001 | -1.008320 | -2.12109 | 0.839252 |
| $4.42 \mathrm{E}+07$ | $1 \mathrm{E}+006$ | 45661662 | 33.82 | 1.62244 | $1 \mathrm{E}+006$ | 45675148 | 33.83 | 0.00999 | -1.139698 | -2.76214 | -0.28753 |
| $4.42 \mathrm{E}+07$ | $2 \mathrm{E}+006$ | 45739943 | 33.88 | 1.24783 | $2 \mathrm{E}+006$ | 45756992 | 33.89 | 0.01263 | -0.846231 | -2.09406 | -0.46428 |
| $4.42 \mathrm{E}+07$ | $2 \mathrm{E}+006$ | 45767801 | 33.9 | 1.27291 | $2 \mathrm{E}+006$ | 45781297 | 33.91 | 0.01 | -0.500796 | -1.77371 | 0.80976 |
| $4.42 \mathrm{E}+07$ | $2 \mathrm{E}+006$ | 45799665 | 33.92 | 1.35826 | $2 \mathrm{E}+006$ | 45813164 | 33.93 | 0.01 | -1.148017 | -2.50628 | 2.135945 |
| $4.42 \mathrm{E}+07$ | $2 \mathrm{E}+006$ | 45826581 | 33.94 | 1.83948 | $2 \mathrm{E}+006$ | 45840211 | 33.95 | 0.0101 | -2.306860 | -4.14634 | -0.02998 |
| $5.10 \mathrm{E}+07$ | 38904 | 51038904 | 37.80 | -0.1493 | 55842 | 51055842 | 37.82 | 0.01255 | 0.1437535 | 0.293033 | -1.31079 |
| $5.10 \mathrm{E}+07$ | 66799 | 51066799 | 37.83 | -0.0194 | 80195 | 51080195 | 37.84 | 0.00992 | 1.1798949 | 1.199262 | 1.102619 |
| $5.10 \mathrm{E}+07$ | 93639 | 51093639 | 37.85 | 0.80887 | 107100 | 51107100 | 37.86 | 0.00997 | 1.1659389 | 0.357071 | -0.27814 |
| $5.10 \mathrm{E}+07$ | 120571 | 51120571 | 37.87 | 0.30673 | 134032 | 51134032 | 37.87 | 0.00997 | 0.8764564 | 0.569730 | 0.124704 |
| $5.10 \mathrm{E}+07$ | 198821 | 51198821 | 37.92 | 0.68315 | 215780 | 51215780 | 37.94 | 0.01256 | 0.9634731 | 0.280323 | -0.96449 |
| $5.10 \mathrm{E}+07$ | 226680 | 51226680 | 37.94 | 0.07666 | 240093 | 51240093 | 37.95 | 0.00994 | 1.0227010 | 0.946040 | 0.835641 |
| $5.10 \mathrm{E}+07$ | 258374 | 51258374 | 37.97 | 0.28016 | 271825 | 51271825 | 37.98 | 0.00996 | 0.4734181 | 0.193257 | -1.23326 |
| $5.10 \mathrm{E}+07$ | 285365 | 51285365 | 37.99 | -0.2554 | 298757 | 51298757 | 38.00 | 0.00992 | 0.8807696 | 1.136175 | 0.934750 |
| $5.10 \mathrm{E}+07$ | 358784 | 51358784 | 38.04 | 1.11236 | 375797 | 51375797 | 38.05 | 0.0126 | 0.2041416 | -0.90822 | -2.51534 |
| $5.10 \mathrm{E}+07$ | 386824 | 51386824 | 38.06 | -0.6410 | 400216 | 51400216 | 38.07 | 0.00992 | 0.1944754 | 0.835506 | 0.862382 |
| $5.10 \mathrm{E}+07$ | 419567 | 51419567 | 38.09 | 1.20171 | 442697 | 51442697 | 38.10 | 0.01713 | 0.9971794 | -0.20453 | 0.133493 |
| $5.10 \mathrm{E}+07$ | 456097 | 51456097 | 38.11 | 1.49586 | 469852 | 51469852 | 38.12 | 0.01019 | 1.1884286 | -0.30744 | -0.75771 |
| $5.10 \mathrm{E}+07$ | 518777 | 51518777 | 38.16 | 0.63439 | 535822 | 51535822 | 38.17 | 0.01263 | 1.7460082 | 1.111618 | 3.502249 |
| $5.10 \mathrm{E}+07$ | 546740 | 51546740 | 38.18 | 1.91997 | 560120 | 51560120 | 38.19 | 0.00991 | 0.6157436 | -1.30423 | -0.76101 |
| $5.10 \mathrm{E}+07$ | 573646 | 51573646 | 38.20 | 1.80043 | 587036 | 51587036 | 38.21 | 0.00992 | 1.0777038 | -0.72272 | -1.26366 |
| $5.10 \mathrm{E}+07$ | 600494 | 51600494 | 38.22 | 1.19933 | 618756 | 51618756 | 38.23 | 0.01353 | 1.6145407 | 0.415207 | 0.215937 |
| $5.10 \mathrm{E}+07$ | 678804 | 51678804 | 38.28 | 0.52287 | 695850 | 51695850 | 38.29 | 0.01263 | 0.4654764 | -0.05740 | -0.07321 |
| $5.10 \mathrm{E}+07$ | 706672 | 51706672 | 38.30 | 1.36616 | 724892 | 51724892 | 38.31 | 0.0135 | 1.3691262 | 0.002964 | 1.171138 |
| $5.10 \mathrm{E}+07$ | 738356 | 51738356 | 38.32 | 1.06414 | 751958 | 51751958 | 38.33 | 0.01008 | 0.1672258 | -0.89692 | -1.13229 |
| $5.10 \mathrm{E}+07$ | 765812 | 51765812 | 38.34 | 1.33467 | 779265 | 51779265 | 38.35 | 0.00996 | 1.3155371 | -0.01914 | 0.310161 |
| $5.10 \mathrm{E}+07$ | 838862 | 51838862 | 38.40 | 1.29639 | 855829 | 51855829 | 38.41 | 0.01257 | 0.6030945 | -0.69330 | -0.49225 |
| $5.10 \mathrm{E}+07$ | 866736 | 51866736 | 38.42 | 1.06978 | 880253 | 51880253 | 38.43 | 0.01001 | 0.7177923 | -0.35198 | 1.010644 |
| $5.10 \mathrm{E}+07$ | 893726 | 51893726 | 38.44 | 1.82047 | 907164 | 51907164 | 38.45 | 0.00995 | 0.6963781 | -1.12410 | -1.26622 |
| $5.10 \mathrm{E}+07$ | 920574 | 51920574 | 38.46 | 1.27137 | 938995 | 51938995 | 38.47 | 0.01364 | 1.2914948 | 0.020129 | 0.802497 |
| $5.10 \mathrm{E}+07$ | 998978 | 51998978 | 38.52 | 2.10818 | 1E+006 | 52015824 | 38.53 | 0.01248 | 0.3779752 | -1.73020 | 0.155178 |
| $5.10 \mathrm{E}+07$ | $1 \mathrm{E}+006$ | 52026730 | 38.54 | 2.18180 | 1E+006 | 52045063 | 38.55 | 0.01358 | 0.3227910 | -1.85901 | -1.79816 |
| $5.10 \mathrm{E}+07$ | $1 \mathrm{E}+006$ | 52058451 | 38.56 | 1.75609 | $1 \mathrm{E}+006$ | 52076719 | 38.57 | 0.01353 | 1.5130608 | -0.24303 | 0.006820 |
| $5.10 \mathrm{E}+07$ | 1E+006 | 52090204 | 38.58 | 1.18086 | $1 \mathrm{E}+006$ | 52103636 | 38.59 | 0.00995 | 0.9326136 | -0.24824 | -0.18146 |
| $5.10 \mathrm{E}+07$ | $1 \mathrm{E}+006$ | 52158794 | 38.63 | 0.57626 | 1E+006 | 52175829 | 38.65 | 0.01262 | 0.6999234 | 0.123662 | 1.147198 |
| $5.10 \mathrm{E}+07$ | $1 \mathrm{E}+006$ | 52186683 | 38.65 | 1.37276 | $1 \mathrm{E}+006$ | 52201212 | 38.67 | 0.01076 | 0.6697530 | -0.70301 | -2.71928 |
| $5.10 \mathrm{E}+07$ | $1 \mathrm{E}+006$ | 52214667 | 38.68 | -0.1021 | $1 \mathrm{E}+006$ | 52228207 | 38.69 | 0.01003 | 1.2788841 | 1.380951 | -2.29174 |
| $5.10 \mathrm{E}+07$ | $1 \mathrm{E}+006$ | 52241575 | 38.70 | -2.7454 | $1 \mathrm{E}+006$ | 52255034 | 38.71 | 0.00997 | 0.3809093 | 3.126331 | 1.020028 |
| $5.10 \mathrm{E}+07$ | $1 \mathrm{E}+006$ | 52318812 | 38.75 | 0.72140 | $1 \mathrm{E}+006$ | 52335887 | 38.77 | 0.01265 | 1.5064162 | 0.785013 | -5.34108 |
| $5.10 \mathrm{E}+07$ | $1 \mathrm{E}+006$ | 52346742 | 38.77 | -2.7845 | $1 \mathrm{E}+006$ | 52360348 | 38.78 | 0.01008 | 1.7094532 | 4.493999 | 5.53851 |

Table A.1: Configuration $210 \mathrm{~cm} / \mathrm{s}$ Run 1

| Zoom <br> start <br> point | Reader <br> Epoch | Entire <br> Capture <br> Epoch | Time: | Phase <br> Read | $\begin{gathered} \text { Tag } \\ \text { Epoch } \end{gathered}$ | Entire <br> Capture <br> Epoch | Time: | Delta <br> Time | Phase <br> Response | Phase <br> due to <br> travel | Instant <br> Velocity |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $5.10 \mathrm{E}+07$ | $1 \mathrm{E}+006$ | 52373698 | 38.79 | 0.04046 | $1 \mathrm{E}+006$ | 52387133 | 38.80 | 0.00995 | 0.3229584 | 0.282500 | -0.96056 |
| $5.10 \mathrm{E}+07$ | $1 \mathrm{E}+006$ | 52400593 | 38.81 | 0.19353 | $1 \mathrm{E}+006$ | 52415116 | 38.82 | 0.01076 | 1.2391131 | 1.045585 | 0.676566 |
| $5.10 \mathrm{E}+07$ | $1 \mathrm{E}+006$ | 52478803 | 38.87 | 0.83937 | $1 \mathrm{E}+006$ | 52495955 | 38.88 | 0.0127 | 0.3322719 | -0.50710 | 1.08533 |
| $5.10 \mathrm{E}+07$ | $2 \mathrm{E}+006$ | 52506871 | 38.89 | 2.85264 | $2 \mathrm{E}+006$ | 52529690 | 38.91 | 0.0169 | 1.3061127 | -1.54653 | -0.31831 |
| $5.10 \mathrm{E}+07$ | $2 \mathrm{E}+006$ | 52543222 | 38.92 | 1.70546 | $2 \mathrm{E}+006$ | 52562630 | 38.93 | 0.01438 | 0.4566020 | -1.24886 | $-2.24628$ |
| $5.10 \mathrm{E}+07$ | $2 \mathrm{E}+006$ | 52576111 | 38.94 | 0.04273 | $2 \mathrm{E}+006$ | 52589551 | 38.95 | 0.00996 | 0.5106245 | 0.467891 |  |
|  |  |  |  |  |  |  |  |  |  | Averages: | 0.133129 |

Table A.2: Configuration $210 \mathrm{~cm} / \mathrm{s}$ Run 2

| Zoom <br> start point | Reader <br> Epoch | Entire <br> Capture <br> Epoch | Time: | Phase <br> Read | Tag <br> Epoch | Entire <br> Capture <br> Epoch | Time: | Delta <br> Time | Phase <br> Response | Phase <br> due to <br> travel | Instant <br> Velocity |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $9.00 \mathrm{E}+06$ | 369529 | 9369529 | 6.94001 | 3.0466 | 386559 | 9386559 | 6.9526 | 1.5298 | -1.5168 | -9.34792 |  |
| $9.00 \mathrm{E}+06$ | 397395 | 9397395 | 6.96065 | $-2.345$ | 410860 | 9410860 | 6.9706 | 2.5876 | 4.93214 | 2.359182 |  |
| $9.00 \mathrm{E}+06$ | 424313 | 9424313 | 6.98059 | -1.991 | 442542 | 9442542 | 6.9941 | 0.8188 | 2.81023 | 6.870658 |  |
| $9.00 \mathrm{E}+06$ | 456034 | 9456034 | 7.00408 | 1.6923 | 469513 | 9469513 | 7.0141 | -0.758 | -2.4505 | -0.97464 |  |
| $9.00 \mathrm{E}+06$ | 529536 | 9529536 | 7.05853 | 1.2517 | 546632 | 9546632 | 7.0712 | 0.9350 | -0.3167 | -6.56246 |  |
| $9.00 \mathrm{E}+06$ | 557431 | 9557431 | 7.07919 | -2.489 | 570841 | 9570841 | 7.0891 | 1.7045 | 4.1935 | 3.982295 |  |
| $9.00 \mathrm{E}+06$ | 584342 | 9584342 | 7.09912 | -3.032 | 602548 | 9602548 | 7.1126 | -2.424 | 0.6089 | -0.60224 |  |
| $9.00 \mathrm{E}+06$ | 616017 | 9616017 | 7.12258 | 0.5103 | 629473 | 9629473 | 7.1326 | 1.5795 | 1.06924 | 0.981072 |  |
| $9.00 \mathrm{E}+06$ | 689535 | 9689535 | 7.17704 | 1.8829 | 706523 | 9706523 | 7.1896 | 0.8062 | -1.0767 | 0.177562 |  |
| $9.00 \mathrm{E}+06$ | 717368 | 9717368 | 7.19765 | 2.714 | 730886 | 9730886 | 7.2077 | 1.5144 | -1.1996 | 3.460556 |  |
| $9.00 \mathrm{E}+06$ | 749112 | 9749112 | 7.22117 | 2.8521 | 762572 | 9762572 | 7.2311 | -1.460 | -4.3125 | -10.5018 |  |
| $9.00 \mathrm{E}+06$ | 776048 | 9776048 | 7.24112 | $-1.366$ | 789504 | 9789504 | 7.2511 | 2.3505 | 3.71697 | 1.793129 |  |
| $9.00 \mathrm{E}+06$ | 849511 | 9849511 | 7.29553 | -1.674 | 866547 | 9866547 | 7.3082 | -1.879 | -0.2049 | -5.10947 |  |
| $9.00 \mathrm{E}+06$ | 877470 | 9877470 | 7.31624 | -2.044 | 890965 | 9890965 | 7.3262 | 1.2929 | 3.33698 | 1.576837 |  |
| $9.00 \mathrm{E}+06$ | 904436 | 9904436 | 7.33622 | 0.3559 | 922743 | 9922743 | 7.3498 | 2.2704 | 1.91444 | 7.070518 |  |
| $9.00 \mathrm{E}+06$ | 937280 | 9937280 | 7.36054 | 1.2124 | 950758 | 9950758 | 7.3705 | -2.496 | -3.7089 | -0.63838 |  |
| $9.00 \mathrm{E}+06$ | 1009589 | 10009589 | 7.4141 | -0.335 | 1026558 | 10026558 | 7.4267 | -2.670 | -2.3352 | -6.56955 |  |
| $9.00 \mathrm{E}+06$ | 1037397 | 10037397 | 7.4347 | 0.5191 | 1050900 | 10050900 | 7.4447 | 2.7238 | 2.20471 | 2.860114 |  |
| $9.00 \mathrm{E}+06$ | 1064315 | 10064315 | 7.45464 | $-1.253$ | 1077754 | 10077754 | 7.4646 | -1.228 | 0.02427 | -2.42341 |  |
| $9.00 \mathrm{E}+06$ | 1092376 | 10092376 | 7.47542 | -2.292 | 1105857 | 10105857 | 7.4854 | -0.334 | 1.95771 | 1.154708 |  |
| $9.00 \mathrm{E}+06$ | 1169536 | 10169536 | 7.53258 | -1.977 | 1186526 | 10186526 | 7.5452 | -2.664 | -0.6867 | -5.09673 |  |
| $9.00 \mathrm{E}+06$ | 1197362 | 10197362 | 7.55319 | $-2.544$ | 1211968 | 10211968 | 7.564 | 0.4506 | 2.99453 | 3.015732 |  |
| $9.00 \mathrm{E}+06$ | 1225426 | 10225426 | 7.57397 | -2.563 | 1239933 | 10239933 | 7.5847 | -1.963 | 0.60034 | 3.392044 |  |
| $9.00 \mathrm{E}+06$ | 1267797 | 10267797 | 7.60536 | 1.8214 | 1281326 | 10281326 | 7.6154 | -1.564 | -3.3857 | -1.76398 |  |
| $9.00 \mathrm{E}+06$ | 1329539 | 10329539 | 7.65109 | 1.9906 | 1346566 | 10346566 | 7.6637 | 1.8720 | -0.1186 | $-2.26267$ |  |
| $9.00 \mathrm{E}+06$ | 1357521 | 10357521 | 7.67182 | 0.4786 | 1372090 | 10372090 | 7.6826 | 1.9995 | 1.52092 | -2.16904 |  |
| $9.00 \mathrm{E}+06$ | 1386602 | 10386602 | 7.69336 | -1.090 | 1410407 | 10410407 | 7.7110 | 2.7903 | 3.88038 | 4.401195 |  |

Table A.2: Configuration $210 \mathrm{~cm} / \mathrm{s}$ Run 2

| Zoom <br> start <br> point | Reader <br> Epoch | Entire <br> Capture <br> Epoch | Time: | Phase <br> Read | $\begin{gathered} \text { Tag } \\ \text { Epoch } \end{gathered}$ | Entire <br> Capture <br> Epoch | Time: | Delta <br> Time | Phase <br> Response | Phase due to travel | Instant <br> Velocity |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $9.00 \mathrm{E}+06$ | 1423770 | 10423770 | 7.72089 | -0.700 | 1437203 | 10437203 | 7.7308 | -0.168 | 0.53232 | 1.428516 |  |
| $9.00 \mathrm{E}+06$ | 1489540 | 10489540 | 7.7696 | 2.4306 | 1506521 | 10506521 | 7.7822 | 0.1518 | -2.2788 | -0.53341 |  |
| $9.00 \mathrm{E}+06$ | 1517382 | 10517382 | 7.79022 | 0.3492 | 1530923 | 10530923 | 7.8003 | $-1.560$ | -1.9093 | 0.237306 |  |
| $9.00 \mathrm{E}+06$ | 1544307 | 10544307 | 7.81017 | -0.125 | 1558876 | 10558876 | 7.8210 | -2.223 | -2.0976 | 1.295356 |  |
| $9.00 \mathrm{E}+06$ | 1572293 | 10572293 | 7.8309 | -0.046 | 1585826 | 10585826 | 7.8409 | -3.135 | -3.0887 | -2.39571 |  |
| $9.00 \mathrm{E}+06$ | 1649556 | 10649556 | 7.88813 | 0.5396 | 1666525 | 10666525 | 7.9007 | 2.9395 | 2.39983 | 2.117432 |  |
| $9.00 \mathrm{E}+06$ | 1677364 | 10677364 | 7.90872 | -3.026 | 1695945 | 10695945 | 7.9225 | -2.394 | 0.63133 | -2.75002 |  |
| $9.00 \mathrm{E}+06$ | 1709354 | 10709354 | 7.93242 | -2.170 | 1722803 | 10722803 | 7.9424 | 0.5582 | 2.72815 | 4.809235 |  |
| $9.00 \mathrm{E}+06$ | 1736288 | 10736288 | 7.95237 | 0.3575 | 1749783 | 10749783 | 7.9624 | -0.598 | -0.9554 | 0.70135 |  |
| $9.00 \mathrm{E}+06$ | 1809517 | 10809517 | 8.00661 | 2.9143 | 1826576 | 10826576 | 8.0192 | 0.4299 | -2.4844 | -6.55530 |  |
| $9.00 \mathrm{E}+06$ | 1837593 | 10837593 | 8.02741 | -2.584 | 1850962 | 10850962 | 8.0373 | -0.531 | 2.05379 | 4.433737 |  |
| $9.00 \mathrm{E}+06$ | 1864394 | 10864394 | 8.04726 | -0.442 | 1877873 | 10877873 | 8.0572 | $-1.776$ | -1.3335 | -5.25711 |  |
| $9.00 \mathrm{E}+06$ | 1891312 | 10891312 | 8.06719 | -0.216 | 1904768 | 10904768 | 8.0772 | 2.4648 | 2.68044 | 0.04016 |  |
| $1.40 \mathrm{E}+07$ | 169521 | 14169521 | 10.4954 | -0.032 | 186480 | 14186480 | 10.508 | -1.094 | -1.0611 | -6.63086 |  |
| $1.40 \mathrm{E}+07$ | 197430 | 14197430 | 10.516 | -1.405 | 210856 | 14210856 | 10.526 | 2.1221 | 3.52756 | 3.297688 |  |
| $1.40 \mathrm{E}+07$ | 229018 | 14229018 | 10.5394 | -2.236 | 242588 | 14242588 | 10.549 | -1.679 | 0.55685 | -6.70927 |  |
| $1.40 \mathrm{E}+07$ | 255945 | 14255945 | 10.5594 | -2.759 | 269381 | 14269381 | 10.569 | 2.9012 | 5.66012 | 1.725057 |  |
| $1.40 \mathrm{E}+07$ | 329459 | 14329459 | 10.6138 | $-2.335$ | 346507 | 14346507 | 10.626 | -0.452 | 1.88304 | -0.59641 |  |
| $1.40 \mathrm{E}+07$ | 357459 | 14357459 | 10.6346 | -1.844 | 370968 | 14370968 | 10.645 | 0.4528 | 2.29721 | 2.435199 |  |
| $1.40 \mathrm{E}+07$ | 385431 | 14385431 | 10.6553 | -2.196 | 398942 | 14398942 | 10.665 | $-1.833$ | 0.36328 | -4.72843 |  |
| $1.40 \mathrm{E}+07$ | 412487 | 14412487 | 10.6753 | -2.608 | 430747 | 14430747 | 10.689 | 2.0247 | 4.63265 | 1.577771 |  |
| $1.40 \mathrm{E}+07$ | 489480 | 14489480 | 10.7324 | 1.2797 | 506497 | 14506497 | 10.745 | 2.5194 | 1.23969 | -0.12860 |  |
| $1.40 \mathrm{E}+07$ | 517412 | 14517412 | 10.753 | -2.423 | 530780 | 14530780 | 10.763 | -1.094 | 1.32835 | -2.38571 |  |
| $1.40 \mathrm{E}+07$ | 544294 | 14544294 | 10.773 | -0.933 | 557815 | 14557815 | 10.783 | 2.2263 | 3.15938 | 9.417442 |  |
| $1.40 \mathrm{E}+07$ | 571736 | 14571736 | 10.7933 | 2.2982 | 585251 | 14585251 | 10.803 | $-1.878$ | -4.1757 | -1.85659 |  |
| $1.40 \mathrm{E}+07$ | 649601 | 14649601 | 10.851 | -2.376 | 666475 | 14666475 | 10.863 | -2.271 | 0.10536 | 0.907091 |  |
| $1.40 \mathrm{E}+07$ | 677352 | 14677352 | 10.8715 | 0.1784 | 690806 | 14690806 | 10.881 | -0.343 | -0.5212 | 3.210221 |  |
| $1.40 \mathrm{E}+07$ | 704256 | 14704256 | 10.8914 | 0.3810 | 717739 | 14717739 | 10.901 | -2.595 | -2.9757 | -4.55402 |  |
| $1.40 \mathrm{E}+07$ | 731192 | 14731192 | 10.9114 | -3.101 | 744646 | 14744646 | 10.921 | -2.599 | 0.50291 | 1.236896 |  |
| $1.40 \mathrm{E}+07$ | 809554 | 14809554 | 10.9694 | 0.1892 | 826495 | 14826495 | 10.982 | -2.182 | -2.3712 | -3.12689 |  |
| $1.40 \mathrm{E}+07$ | 837305 | 14837305 | 10.99 | 2.8856 | 850794 | 14850794 | 11 | 2.6714 | -0.2142 | 2.142733 |  |
| $1.40 \mathrm{E}+07$ | 869060 | 14869060 | 11.0135 | -0.139 | 882545 | 14882545 | 11.024 | -2.285 | -2.1456 | -2.52543 |  |
| $1.40 \mathrm{E}+07$ | 896100 | 14896100 | 11.0335 | -0.203 | 909430 | 14909430 | 11.043 | -0.421 | -0.2181 | -0.06263 |  |
| $1.40 \mathrm{E}+07$ | 969599 | 14969599 | 11.088 | 0.6302 | 986486 | 14986486 | 11.100 | 0.5491 | -0.0810 | -0.26281 |  |
| $1.40 \mathrm{E}+07$ | 997452 | 14997452 | 11.1086 | 3.0023 | 1011002 | 15011002 | 11.119 | 3.1042 | 0.10187 | -1.54237 |  |
| $1.40 \mathrm{E}+07$ | 1024426 | 15024426 | 11.1286 | -1.473 | 1037826 | 15037826 | 11.139 | -0.196 | 1.2764 | $-1.56420$ |  |
| $1.40 \mathrm{E}+07$ | 1056044 | 15056044 | 11.152 | -2.385 | 1069539 | 15069539 | 11.162 | 0.2998 | 2.68466 | 1.380256 |  |
| $1.40 \mathrm{E}+07$ | 1129495 | 15129495 | 11.2064 | $-2.667$ | 1146477 | 15146477 | 11.219 | -2.997 | -0.3301 | -0.69803 |  |
| $1.40 \mathrm{E}+07$ | 1157354 | 15157354 | 11.2271 | -2.694 | 1170805 | 15170805 | 11.237 | $-2.542$ | 0.152 | 1.55813 |  |
| $1.40 \mathrm{E}+07$ | 1189144 | 15189144 | 11.2506 | 2.9922 | 1202540 | 15202540 | 11.261 | 1.7404 | -1.2518 | -0.55955 |  |

Table A.2: Configuration $210 \mathrm{~cm} / \mathrm{s}$ Run 2

| Zoom <br> start <br> point | Reader <br> Epoch | Entire <br> Capture <br> Epoch | Time: | Phase <br> Read | Tag <br> Epoch | Entire <br> Capture <br> Epoch | Time: | $\begin{aligned} & \text { Delta } \\ & \text { Time } \end{aligned}$ | Phase <br> Response | Phase due to travel | Instant <br> Velocity |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $1.40 \mathrm{E}+07$ | 1222018 | 15222018 | 11.2749 | -1.250 | 1240324 | 15240324 | 11.289 | -1.901 | -0.6516 | 2.518828 |  |
| $1.40 \mathrm{E}+07$ | 1289450 | 15289450 | 11.3249 | 2.7363 | 1306517 | 15306517 | 11.338 | -2.649 | -5.3848 | -12.7344 |  |
| $1.40 \mathrm{E}+07$ | 1317329 | 15317329 | 11.3455 | -2.855 | 1330851 | 15330851 | 11.356 | 0.5575 | 3.41232 | 2.200557 |  |
| $1.40 \mathrm{E}+07$ | 1344284 | 15344284 | 11.3655 | -2.706 | 1357714 | 15357714 | 11.375 | -0.972 | 1.73414 | 1.314284 |  |
| $1.40 \mathrm{E}+07$ | 1371169 | 15371169 | 11.3854 | 2.4726 | 1389424 | 15389424 | 11.399 | 3.0236 | 0.55099 | -1.37833 |  |
| $1.40 \mathrm{E}+07$ | 1449486 | 15449486 | 11.4434 | -2.867 | 1466486 | 15466486 | 11.456 | 0.6999 | 3.56639 | 11.17503 |  |
| $1.40 \mathrm{E}+07$ | 1477333 | 15477333 | 11.4641 | 2.5849 | 1490804 | 15490804 | 11.474 | -1.564 | -4.1485 | -6.19241 |  |
| $1.40 \mathrm{E}+07$ | 1509208 | 15509208 | 11.4877 | 0.4604 | 1522619 | 15522619 | 11.498 | 1.9049 | 1.44451 | 6.784865 |  |
| $1.40 \mathrm{E}+07$ | 1536052 | 15536052 | 11.5076 | 1.8169 | 1549539 | 15549539 | 11.518 | -1.924 | -3.7407 | 0.747278 |  |
| $1.40 \mathrm{E}+07$ | 1609487 | 15609487 | 11.5619 | 2.4224 | 1626528 | 15626528 | 11.575 | -2.952 | -5.3740 | -9.03954 |  |
| $1.40 \mathrm{E}+07$ | 1637385 | 15637385 | 11.5826 | -2.484 | 1650926 | 15650926 | 11.593 | -1.597 | 0.88712 | -0.16781 |  |
| $1.40 \mathrm{E}+07$ | 1664356 | 15664356 | 11.6026 | -2.013 | 1682617 | 15682617 | 11.616 | -0.975 | 1.03809 | 2.935017 |  |
| $1.40 \mathrm{E}+07$ | 1700935 | 15700935 | 11.6297 | 0.9392 | 1714352 | 15714352 | 11.640 | -0.667 | -1.6062 | -0.00312 |  |
| $3.45 \mathrm{E}+07$ | 469177 | 34969177 | 25.9017 | 0.7637 | 486192 | 34986192 | 25.914 | 0.8640 | 0.10025 | -7.64728 |  |
| $3.45 \mathrm{E}+07$ | 497131 | 34997131 | 25.9224 | -2.807 | 510967 | 35010967 | 25.933 | 2.6715 | 5.47889 | 5.799531 |  |
| $3.45 \mathrm{E}+07$ | 529222 | 35029222 | 25.9461 | -3.049 | 542627 | 35042627 | 25.956 | -2.783 | 0.26627 | 1.513445 |  |
| $3.45 \mathrm{E}+07$ | 556091 | 35056091 | 25.966 | -1.216 | 569564 | 35069564 | 25.976 | -2.107 | -0.8911 | -2.58570 |  |
| $3.45 \mathrm{E}+07$ | 629249 | 35129249 | 26.0202 | -2.727 | 646213 | 35146213 | 26.033 | 2.0088 | 4.7354 | 12.0264 |  |
| $3.45 \mathrm{E}+07$ | 657265 | 35157265 | 26.041 | 1.5517 | 671101 | 35171101 | 26.051 | $-2.210$ | -3.7618 | -8.37023 |  |
| $3.45 \mathrm{E}+07$ | 689385 | 35189385 | 26.0648 | -2.335 | 703025 | 35203025 | 26.075 | 1.4890 | 3.82406 | -0.19418 |  |
| $3.45 \mathrm{E}+07$ | 716322 | 35216322 | 26.0847 | -3.021 | 729778 | 35229778 | 26.095 | 0.9506 | 3.97154 | 1.553374 |  |
| $3.45 \mathrm{E}+07$ | 789168 | 35289168 | 26.1387 | -1.594 | 806196 | 35306196 | 26.151 | -0.993 | 0.60159 | 1.473622 |  |
| $3.45 \mathrm{E}+07$ | 817152 | 35317152 | 26.1594 | -2.077 | 830575 | 35330575 | 26.169 | -2.495 | -0.4183 | 3.109202 |  |
| $3.45 \mathrm{E}+07$ | 844073 | 35344073 | 26.1794 | 1.1748 | 857546 | 35357546 | 26.189 | -1.624 | -2.7990 | -3.85878 |  |
| $3.45 \mathrm{E}+07$ | 875994 | 35375994 | 26.203 | 0.5184 | 889353 | 35389353 | 26.213 | 1.2038 | 0.68541 | -2.11025 |  |
| $3.45 \mathrm{E}+07$ | 949200 | 35449200 | 26.2572 | -2.865 | 966179 | 35466179 | 26.270 | 2.4226 | 5.2879 | 1.876193 |  |
| $3.45 \mathrm{E}+07$ | 977037 | 35477037 | 26.2778 | -2.637 | 990511 | 35490511 | 26.288 | 1.3548 | 3.99189 | 2.721384 |  |
| $3.45 \mathrm{E}+07$ | 1004498 | 35504498 | 26.2982 | -1.715 | 1022791 | 35522791 | 26.312 | -0.217 | 1.49801 | -1.19158 |  |
| $3.45 \mathrm{E}+07$ | 1036256 | 35536256 | 26.3217 | -0.420 | 1049713 | 35549713 | 26.332 | 1.9889 | 2.40873 | -0.42807 |  |
| $3.45 \mathrm{E}+07$ | 1109281 | 35609281 | 26.3758 | -2.958 | 1126228 | 35626228 | 26.388 | 0.3808 | 3.33858 | 9.09682 |  |
| $3.45 \mathrm{E}+07$ | 1137069 | 35637069 | 26.3964 | 2.1113 | 1150493 | 35650493 | 26.406 | -0.817 | -2.9279 | -3.58262 |  |
| $3.45 \mathrm{E}+07$ | 1163989 | 35663989 | 26.4163 | -0.632 | 1177430 | 35677430 | 26.426 | -0.820 | -0.1882 | 3.155586 |  |
| $3.45 \mathrm{E}+07$ | 1195766 | 35695766 | 26.4399 | -0.018 | 1209251 | 35709251 | 26.450 | -3.057 | -3.0388 | 1.439347 |  |
| $3.45 \mathrm{E}+07$ | 1269167 | 35769167 | 26.4942 | 3.1310 | 1286262 | 35786262 | 26.507 | -3.055 | -6.1857 | -13.9151 |  |
| $3.45 \mathrm{E}+07$ | 1297036 | 35797036 | 26.5149 | -2.779 | 1310492 | 35810492 | 26.525 | 0.6069 | 3.38611 | 2.171855 |  |
| $3.45 \mathrm{E}+07$ | 1324021 | 35824021 | 26.5349 | -2.873 | 1343240 | 35843240 | 26.549 | -1.506 | 1.36697 | -0.75281 |  |
| $3.45 \mathrm{E}+07$ | 1361627 | 35861627 | 26.5627 | -2.245 | 1376203 | 35876203 | 26.574 | -0.173 | 2.07144 | -0.33900 |  |
| $3.45 \mathrm{E}+07$ | 1429166 | 35929166 | 26.6127 | $-1.071$ | 1446178 | 35946178 | 26.625 | 1.6739 | 2.74486 | 0.949186 |  |
| $3.45 \mathrm{E}+07$ | 1457035 | 35957035 | 26.6334 | -2.652 | 1470491 | 35970491 | 26.643 | -0.562 | 2.08971 | -0.12428 |  |
| $3.45 \mathrm{E}+07$ | 1483956 | 35983956 | 26.6533 | 0.1487 | 1498468 | 35998468 | 26.664 | 2.3372 | 2.18842 | 2.694628 |  |

Table A.2: Configuration $210 \mathrm{~cm} / \mathrm{s}$ Run 2

| Zoom <br> start <br> point | Reader <br> Epoch | Entire <br> Capture <br> Epoch | Time: | Phase <br> Read | $\begin{gathered} \text { Tag } \\ \text { Epoch } \end{gathered}$ | Entire <br> Capture <br> Epoch | Time: | Delta <br> Time | Phase <br> Response | Phase due to travel | Instant <br> Velocity |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $3.45 \mathrm{E}+07$ | 1512004 | 36012004 | 26.6741 | 3.0004 | 1525897 | 36025897 | 26.684 | 3.0906 | 0.09015 | 1.487572 |  |
| $3.45 \mathrm{E}+07$ | 1589157 | 36089157 | 26.7312 | 2.2884 | 1606167 | 36106167 | 26.744 | -1.011 | -3.2997 | -7.75406 |  |
| $3.45 \mathrm{E}+07$ | 1617080 | 36117080 | 26.7519 | -2.051 | 1635381 | 36135381 | 26.765 | 1.0797 | 3.13118 | -0.02114 |  |
| $3.45 \mathrm{E}+07$ | 1648920 | 36148920 | 26.7755 | $-2.383$ | 1662285 | 36162285 | 26.785 | 0.7645 | 3.14733 | 6.14904 |  |
| $3.45 \mathrm{E}+07$ | 1675773 | 36175773 | 26.7954 | 3.0145 | 1689762 | 36189762 | 26.806 | 1.3653 | -1.6492 | -1.95056 |  |
| $3.45 \mathrm{E}+07$ | 1749172 | 36249172 | 26.8498 | -2.542 | 1766245 | 36266245 | 26.862 | 0.0436 | 2.58601 | 6.778392 |  |
| $3.45 \mathrm{E}+07$ | 1777079 | 36277079 | 26.8704 | -0.262 | 1791018 | 36291018 | 26.881 | -2.443 | -2.1811 | -4.90639 |  |
| $3.45 \mathrm{E}+07$ | 1804524 | 36304524 | 26.8908 | -0.255 | 1817956 | 36317956 | 26.901 | 1.3164 | 1.57102 | -1.12107 |  |
| $3.45 \mathrm{E}+07$ | 1831543 | 36331543 | 26.9108 | -0.493 | 1844942 | 36344942 | 26.921 | 1.9364 | 2.42988 | 2.31764 |  |
| $3.45 \mathrm{E}+07$ | 1913338 | 36413338 | 26.9714 | 1.7705 | 1930391 | 36430391 | 26.984 | -1.422 | -3.1923 | -8.84278 |  |
| $3.45 \mathrm{E}+07$ | 1941045 | 36441045 | 26.9919 | -2.388 | 1959284 | 36459284 | 27.005 | 1.6725 | 4.06096 | -0.18994 |  |
| $3.45 \mathrm{E}+07$ | 1972802 | 36472802 | 27.0154 | -3.004 | 1986412 | 36486412 | 27.025 | 1.2033 | 4.20724 | 3.780139 |  |
| $3.45 \mathrm{E}+07$ | 2004574 | 36504574 | 27.0389 | -3.108 | 2022861 | 36522861 | 27.052 | -2.812 | 0.29572 | 0.00407 |  |
| $4.75 \mathrm{E}+07$ | 369001 | 47869001 | 35.4566 | -0.564 | 286011 | 47786011 | 35.395 | -1.570 | -1.0056 | -4.09005 |  |
| $4.75 \mathrm{E}+07$ | 296952 | 47796952 | 35.4032 | -1.472 | 315242 | 47815242 | 35.417 | 0.9160 | 2.38845 | 6.002641 |  |
| $4.75 \mathrm{E}+07$ | 328731 | 47828731 | 35.4267 | -0.321 | 342130 | 47842130 | 35.437 | -2.515 | -2.1935 | 1.010692 |  |
| $4.75 \mathrm{E}+07$ | 355619 | 47855619 | 35.4467 | -0.074 | 369049 | 47869049 | 35.457 | -3.040 | -2.9659 | -1.19983 |  |
| $4.75 \mathrm{E}+07$ | 429095 | 47929095 | 35.5011 | 0.7901 | 446023 | 47946023 | 35.514 | 0.4461 | -0.344 | 2.069522 |  |
| $4.75 \mathrm{E}+07$ | 456949 | 47956949 | 35.5217 | -0.551 | 470459 | 47970459 | 35.532 | -2.331 | -1.7797 | -4.84115 |  |
| $4.75 \mathrm{E}+07$ | 483884 | 47983884 | 35.5417 | 0.6378 | 497344 | 47997344 | 35.552 | 2.5532 | 1.91531 | 2.852769 |  |
| $4.75 \mathrm{E}+07$ | 515710 | 48015710 | 35.5652 | 0.4902 | 529153 | 48029153 | 35.575 | -0.171 | -0.6608 | 0.020309 |  |
| $4.75 \mathrm{E}+07$ | 589028 | 48089028 | 35.6195 | 1.9728 | 606049 | 48106049 | 35.632 | 1.2676 | -0.7052 | -3.55249 |  |
| $4.75 \mathrm{E}+07$ | 616866 | 48116866 | 35.6402 | -0.052 | 630343 | 48130343 | 35.650 | 1.6928 | 1.74494 | 2.40303 |  |
| $4.75 \mathrm{E}+07$ | 643816 | 48143816 | 35.6601 | 2.1606 | 657277 | 48157277 | 35.670 | 2.0681 | -0.0925 | 2.90306 |  |
| $4.75 \mathrm{E}+07$ | 670765 | 48170765 | 35.6801 | 0.3065 | 688944 | 48188944 | 35.694 | -2.396 | -2.7023 | -1.26798 |  |
| $4.75 \mathrm{E}+07$ | 749007 | 48249007 | 35.738 | -2.521 | 766044 | 48266044 | 35.751 | -2.448 | 0.07301 | -5.47875 |  |
| $4.75 \mathrm{E}+07$ | 776876 | 48276876 | 35.7587 | -2.839 | 795148 | 48295148 | 35.772 | 1.7607 | 4.59976 | 12.80662 |  |
| $4.75 \mathrm{E}+07$ | 808545 | 48308545 | 35.7821 | 2.7953 | 822052 | 48322052 | 35.792 | -2.386 | -5.1817 | -7.62831 |  |
| $4.75 \mathrm{E}+07$ | 835557 | 48335557 | 35.8021 | -0.132 | 849002 | 48349002 | 35.812 | 0.5231 | 0.65462 | -1.53970 |  |
| $4.75 \mathrm{E}+07$ | 913009 | 48413009 | 35.8595 | -2.541 | 930104 | 48430104 | 35.872 | 1.6588 | 4.19965 | 11.19896 |  |
| $4.75 \mathrm{E}+07$ | 940977 | 48440977 | 35.8802 | 1.2868 | 954415 | 48454415 | 35.890 | -2.243 | -3.5295 | -0.71756 |  |
| $4.75 \mathrm{E}+07$ | 967941 | 48467941 | 35.9002 | 1.0520 | 981365 | 48481365 | 35.910 | -1.929 | -2.9805 | 1.019854 |  |
| $4.75 \mathrm{E}+07$ | 999640 | 48499640 | 35.9237 | 2.7697 | 1013095 | 48513095 | 35.934 | -1.129 | -3.8992 | -2.58964 |  |
| $4.75 \mathrm{E}+07$ | 1068989 | 48568989 | 35.9751 | -0.861 | 1086190 | 48586190 | 35.988 | 0.6132 | 1.47457 | 9.074025 |  |
| $4.75 \mathrm{E}+07$ | 1096894 | 48596894 | 35.9957 | 2.2164 | 1110315 | 48610315 | 36.006 | -2.524 | -4.7401 | -5.02751 |  |
| $4.75 \mathrm{E}+07$ | 1123765 | 48623765 | 36.0156 | -2.890 | 1146891 | 48646891 | 36.033 | -2.410 | 0.48025 | 3.207747 |  |
| $4.75 \mathrm{E}+07$ | 1160417 | 48660417 | 36.0428 | 2.3693 | 1173855 | 48673855 | 36.053 | 0.3940 | -1.9752 | -1.71606 |  |
| $4.75 \mathrm{E}+07$ | 1228999 | 48728999 | 36.0936 | -1.855 | 1246048 | 48746048 | 36.106 | -0.313 | 1.54183 | 4.436516 |  |
| $4.75 \mathrm{E}+07$ | 1256920 | 48756920 | 36.1143 | 1.8097 | 1275309 | 48775309 | 36.128 | -0.334 | -2.1436 | -5.99946 |  |
| $4.75 \mathrm{E}+07$ | 1289717 | 48789717 | 36.1385 | -2.703 | 1303177 | 48803177 | 36.149 | -0.100 | 2.60291 | 4.278535 |  |

Table A.2: Configuration $210 \mathrm{~cm} / \mathrm{s}$ Run 2

| Zoom <br> start <br> point | Reader <br> Epoch | Entire <br> Capture <br> Epoch | Time: | Phase <br> Read | Tag <br> Epoch | Entire <br> Capture <br> Epoch | Time: | Delta <br> Time | Phase <br> Response | Phase due to travel | Instant <br> Velocity |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $4.75 \mathrm{E}+07$ | 1316604 | 48816604 | 36.1585 | 1.2584 | 1330130 | 48830130 | 36.168 | 0.5875 | -0.6709 | -0.98826 |  |
| $4.75 \mathrm{E}+07$ | 1389002 | 48889002 | 36.2121 | -2.669 | 1405991 | 48905991 | 36.225 | -1.212 | 1.45744 | 0.162724 |  |
| $4.75 \mathrm{E}+07$ | 1417026 | 48917026 | 36.2328 | $-2.234$ | 1430395 | 48930395 | 36.243 | -0.890 | 1.3447 | 6.472563 |  |
| $4.75 \mathrm{E}+07$ | 1443961 | 48943961 | 36.2528 | 1.1632 | 1457425 | 48957425 | 36.263 | -2.459 | -3.6221 | -7.40490 |  |
| $4.75 \mathrm{E}+07$ | 1470787 | 48970787 | 36.2727 | -1.233 | 1489092 | 48989092 | 36.286 | 1.8015 | 3.03492 | 1.599073 |  |
| $4.75 \mathrm{E}+07$ | 1548998 | 49048998 | 36.3306 | -2.321 | 1566020 | 49066020 | 36.343 | $-2.778$ | -0.4573 | -0.95571 |  |
| $4.75 \mathrm{E}+07$ | 1576898 | 49076898 | 36.3513 | -2.008 | 1595125 | 49095125 | 36.365 | -1.675 | 0.33234 | 1.845607 |  |
| $4.75 \mathrm{E}+07$ | 1608583 | 49108583 | 36.3747 | 0.2490 | 1622060 | 49122060 | 36.385 | -0.830 | -1.0789 | 3.084542 |  |
| $4.75 \mathrm{E}+07$ | 1635501 | 49135501 | 36.3947 | 0.5179 | 1649026 | 49149026 | 36.405 | -2.922 | -3.4403 | 0.120219 |  |
| $4.75 \mathrm{E}+07$ | 1708995 | 49208995 | 36.4491 | 2.1100 | 1726017 | 49226017 | 36.462 | -1.593 | -3.7030 | $-7.02334$ |  |
| $4.75 \mathrm{E}+07$ | 1736959 | 49236959 | 36.4698 | 1.3937 | 1750420 | 49250420 | 36.480 | 2.5563 | 1.1626 | 3.682822 |  |
| $4.75 \mathrm{E}+07$ | 1768785 | 49268785 | 36.4934 | 0.7490 | 1787199 | 49287199 | 36.507 | -1.934 | $-2.6827$ | -5.05904 |  |
| $4.75 \mathrm{E}+07$ | 1800608 | 49300608 | 36.517 | -2.845 | 1814103 | 49314103 | 36.527 | -1.664 | 1.18127 |  |  |
|  |  |  |  |  |  |  |  |  | Averages= | -0.06827 |  |

Table A.3: Configuration $210 \mathrm{~cm} / \mathrm{s}$ Run 3

| Zoom <br> start <br> point | Reader <br> Epoch | Entire <br> Capture <br> Epoch | Time: | Phase <br> Read | Tag <br> Epoch | Entire <br> Capture <br> Epoch | Time: | Delta <br> Time | Phase <br> Response | Phase due to travel | Instant <br> Velocity |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $9.00 \mathrm{E}+05$ | 74993 | 974993 | 0.722177 | 0.0324 | 92059 | 992059 | 0.7348 | 1.5635 | 1.531140 | -1.05249 |  |
| $9.00 \mathrm{E}+05$ | 102864 | 1002864 | 0.742821 | $-2.792$ | 117449 | 1017449 | 0.7536 | -0.502 | 2.289779 | 1.869244 |  |
| $9.00 \mathrm{E}+05$ | 130998 | 1030998 | 0.763660 | -0.645 | 144362 | 1044362 | 0.7736 | 0.217 | 0.861608 | 1.071816 |  |
| $9.00 \mathrm{E}+05$ | 167534 | 1067534 | 0.790722 | -0.592 | 180892 | 1080892 | 0.8006 | -0.842 | -0.24992 | 1.833265 |  |
| $9.00 \mathrm{E}+05$ | 234940 | 1134940 | 0.840650 | 1.7273 | 252002 | 1152002 | 0.8533 | -2.224 | -3.95083 | 0.257100 |  |
| $9.00 \mathrm{E}+05$ | 262793 | 1162793 | 0.861281 | 1.7058 | 281275 | 1181275 | 0.8750 | -2.459 | -4.16449 | -0.38733 |  |
| $9.00 \mathrm{E}+05$ | 294560 | 1194560 | 0.884811 | 2.5108 | 308015 | 1208015 | 0.8948 | -1.360 | -3.87046 | -4.14756 |  |
| $9.00 \mathrm{E}+05$ | 321478 | 1221478 | 0.904749 | -1.872 | 339787 | 1239787 | 0.9183 | -2.001 | -0.12945 | 1.812149 |  |
| $9.00 \mathrm{E}+05$ | 394437 | 1294437 | 0.958789 | 2.5877 | 411934 | 1311934 | 0.9717 | -1.253 | -3.84107 | -3.40718 |  |
| $9.00 \mathrm{E}+05$ | 422822 | 1322822 | 0.979814 | 1.1663 | 436239 | 1336239 | 0.9898 | -0.324 | -1.49012 | -6.56696 |  |
| $9.00 \mathrm{E}+05$ | 449708 | 1349708 | 0.999729 | -1.588 | 463162 | 1363162 | 1.0097 | 1.941 | 3.529140 | 2.248486 |  |
| $9.00 \mathrm{E}+05$ | 481539 | 1381539 | 1.023306 | -2.678 | 494956 | 1394956 | 1.0332 | -1.179 | 1.499647 | 0.581115 |  |
| $9.00 \mathrm{E}+05$ | 554939 | 1454939 | 1.077673 | -1.499 | 571979 | 1471979 | 1.0903 | -1.270 | 0.228972 | 1.660946 |  |
| $9.00 \mathrm{E}+05$ | 582872 | 1482872 | 1.098363 | 2.9602 | 597345 | 1497345 | 1.1091 | 1.9931 | -0.96711 | 2.597576 |  |
| $9.00 \mathrm{E}+05$ | 616213 | 1516213 | 1.123059 | 1.0809 | 629660 | 1529660 | 1.1330 | -2.269 | -3.35011 | 0.175407 |  |
| $9.00 \mathrm{E}+05$ | 643201 | 1543201 | 1.143049 | 1.4526 | 656562 | 1556562 | 1.1529 | -2.031 | -3.48407 | -1.58742 |  |
| $9.00 \mathrm{E}+05$ | 714917 | 1614917 | 1.196169 | -1.269 | 731977 | 1631977 | 1.2088 | -1.354 | -0.08546 | -0.39028 |  |
| $9.00 \mathrm{E}+05$ | 742900 | 1642900 | 1.216896 | -1.554 | 757523 | 1657523 | 1.2277 | -1.356 | 0.197584 | 7.205332 |  |
| $9.00 \mathrm{E}+05$ | 770905 | 1670905 | 1.237639 | 2.8842 | 784376 | 1684376 | 1.2476 | -2.411 | -5.29528 | $-2.51561$ |  |
| $9.00 \mathrm{E}+05$ | 797914 | 1697914 | 1.257645 | 2.7548 | 811272 | 1711272 | 1.2675 | -0.620 | -3.37448 | -1.11069 |  |

Table A.3: Configuration $210 \mathrm{~cm} / \mathrm{s}$ Run 3

| Zoom <br> start <br> point | Reader <br> Epoch | Entire <br> Capture <br> Epoch | Time: | Phase <br> Read | Tag <br> Epoch | Entire <br> Capture <br> Epoch | Time: | $\begin{aligned} & \text { Delta } \\ & \text { Time } \end{aligned}$ | Phase <br> Response | Phase <br> due to travel | Instant <br> Velocity |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $9.00 \mathrm{E}+05$ | 874975 | 1774975 | 1.314724 | 3.0316 | 891924 | 1791924 | 1.3273 | 2.2002 | -0.83140 | 3.912011 |  |
| $9.00 \mathrm{E}+05$ | 902887 | 1802887 | 1.335398 | 2.2106 | 916369 | 1816369 | 1.3454 | -1.336 | -3.54622 | -4.62692 |  |
| $9.00 \mathrm{E}+05$ | 929794 | 1829794 | 1.355328 | -2.825 | 948039 | 1848039 | 1.3688 | -2.212 | 0.613766 | -7.22978 |  |
| $9.00 \mathrm{E}+05$ | 961475 | 1861475 | 1.378795 | -3.140 | 974908 | 1874908 | 1.3887 | 2.9888 | 6.12855 | 2.806304 |  |
| $9.00 \mathrm{E}+05$ | 1035036 | 1935036 | 1.433281 | 1.1426 | 1051947 | 1951947 | 1.4458 | 1.1336 | -0.00903 | 4.395710 |  |
| $9.00 \mathrm{E}+05$ | 1062862 | 1962862 | 1.453892 | 1.3225 | 1076279 | 1976279 | 1.4638 | -1.723 | -3.04543 | -3.11222 |  |
| $9.00 \mathrm{E}+05$ | 1089710 | 1989710 | 1.473778 | -1.742 | 1103170 | 2003170 | 1.4837 | -2.411 | -0.66953 | 3.938660 |  |
| $9.00 \mathrm{E}+05$ | 1116644 | 2016644 | 1.493728 | 2.3321 | 1130212 | 2030212 | 1.5038 | -1.361 | -3.69323 | -2.87502 |  |
| $9.00 \mathrm{E}+05$ | 1194920 | 2094920 | 1.551707 | -0.573 | 1211955 | 2111955 | 1.5643 | 2.4058 | 2.978583 | 7.583311 |  |
| $9.00 \mathrm{E}+05$ | 12227788 | 13127788 | 9.723753 | 2.534 | 1241039 | 2141039 | 1.5859 | -0.749 | -3.28273 | -10.9911 |  |
| $9.00 \mathrm{E}+05$ | 1255500 | 2155500 | 1.596579 | -2.785 | 1268937 | 2168937 | 1.6065 | 2.637 | 5.422199 | 6.153907 |  |
| $9.00 \mathrm{E}+05$ | 1282402 | 2182402 | 1.616505 | 2.0023 | 1295887 | 2195887 | 1.6265 | 2.7163 | 0.713925 | 1.118339 |  |
| $9.00 \mathrm{E}+05$ | 1354930 | 2254930 | 1.670227 | -1.247 | 1371926 | 2271926 | 1.6828 | -2.947 | -1.70021 | 5.176455 |  |
| $9.00 \mathrm{E}+05$ | 1382967 | 2282967 | 1.690994 | 2.1688 | 1396371 | 2296371 | 1.7009 | -3.124 | -5.29253 | -6.04565 |  |
| $9.00 \mathrm{E}+05$ | 1414604 | 2314604 | 1.714427 | -0.536 | 1428062 | 2328062 | 1.7244 | -0.389 | 0.146617 | -4.06517 |  |
| $9.00 \mathrm{E}+05$ | 1441598 | 2341598 | 1.734422 | -2.936 | 1455007 | 2355007 | 1.7444 | 0.3206 | 3.256246 | 3.977141 |  |
| $9.00 \mathrm{E}+05$ | 1514921 | 2414921 | 1.788732 | 3.0876 | 1531949 | 2431949 | 1.8013 | -2.343 | -5.43109 | -4.16226 |  |
| $9.00 \mathrm{E}+05$ | 1542985 | 2442985 | 1.809519 | 0.4753 | 1556351 | 2456351 | 1.8194 | -2.072 | -2.54768 | -1.96883 |  |
| $9.00 \mathrm{E}+05$ | 1569784 | 2469784 | 1.829369 | 2.9096 | 1583258 | 2483258 | 1.8393 | 1.8659 | -1.04375 | -4.02860 |  |
| $9.00 \mathrm{E}+05$ | 1596734 | 2496734 | 1.849331 | -2.599 | 1615036 | 2515036 | 1.8629 | -0.009 | 2.590644 | -0.00461 |  |
| $7.20 \mathrm{E}+06$ | 174906 | 7374906 | 5.462593 | -2.759 | 191918 | 7391918 | 5.4752 | 0.4702 | 3.228902 | 8.865066 |  |
| $7.20 \mathrm{E}+06$ | 202739 | 7402739 | 5.483209 | 0.7331 | 216190 | 7416190 | 5.4932 | -2.147 | -2.87967 | 2.127821 |  |
| $7.20 \mathrm{E}+06$ | 230772 | 7430772 | 5.503973 | 3.0635 | 244226 | 7444226 | 5.5139 | -1.510 | -4.57324 | -6.92212 |  |
| $7.20 \mathrm{E}+06$ | 257698 | 7457698 | 5.523917 | -2.943 | 271188 | 7471188 | 5.5339 | -2.217 | 0.725143 | -0.28171 |  |
| $7.20 \mathrm{E}+06$ | 334901 | 7534901 | 5.581101 | -2.493 | 351913 | 7551913 | 5.5937 | -1.122 | 1.370751 | 5.090453 |  |
| $7.20 \mathrm{E}+06$ | 362843 | 7562843 | 5.601798 | -0.150 | 376349 | 7576349 | 5.6118 | -2.311 | -2.16058 | -1.02505 |  |
| $7.20 \mathrm{E}+06$ | 389721 | 7589721 | 5.621706 | 0.6147 | 408075 | 7608075 | 5.6353 | -0.623 | -1.23734 | -0.36326 |  |
| $7.20 \mathrm{E}+06$ | 421510 | 7621510 | 5.645252 | 2.1431 | 435166 | 7635166 | 5.6554 | 1.1851 | -0.95797 | -0.64380 |  |
| $7.20 \mathrm{E}+06$ | 494847 | 7694847 | 5.699573 | -1.934 | 511857 | 7711857 | 5.7122 | -1.490 | 0.443714 | 0.352997 |  |
| $7.20 \mathrm{E}+06$ | 522739 | 7722739 | 5.720233 | -0.563 | 536179 | 7736179 | 5.7302 | -0.363 | 0.199977 | -2.03450 |  |
| $7.20 \mathrm{E}+06$ | 549717 | 7749717 | 5.740215 | -0.422 | 567998 | 7767998 | 5.7538 | 1.6153 | 2.037769 | 2.352563 |  |
| $7.20 \mathrm{E}+06$ | 581397 | 7781397 | 5.763681 | -1.447 | 594878 | 7794878 | 5.7737 | -1.204 | 0.242528 | 0.286248 |  |
| $7.20 \mathrm{E}+06$ | 654914 | 7854914 | 5.818135 | -2.566 | 671876 | 7871876 | 5.8307 | -2.949 | -0.38318 | -4.37491 |  |
| $7.20 \mathrm{E}+06$ | 628703 | 7828703 | 5.798720 | -2.46 | 701041 | 7901041 | 5.8523 | 0.7791 | 3.239110 | 9.101404 |  |
| $7.20 \mathrm{E}+06$ | 715655 | 7915655 | 5.863126 | 3.1233 | 734012 | 7934012 | 5.8767 | -2.157 | -5.27997 | -2.41275 |  |
| $7.20 \mathrm{E}+06$ | 747403 | 7947403 | 5.886641 | 1.2539 | 760867 | 7960867 | 5.8966 | -2.187 | -3.44051 | -2.70374 |  |
| $7.20 \mathrm{E}+06$ | 814853 | 8014853 | 5.936602 | -1.602 | 831911 | 8031911 | 5.9492 | 0.4106 | 2.012590 | 3.501556 |  |
| $7.20 \mathrm{E}+06$ | 842697 | 8042697 | 5.957226 | -2.117 | 856176 | 8056176 | 5.9672 | -2.516 | -0.39950 | -0.89548 |  |
| $7.20 \mathrm{E}+06$ | 874511 | 8074511 | 5.980790 | -1.498 | 887954 | 8087954 | 5.9907 | -1.090 | 0.408356 | -0.28809 |  |
| $7.20 \mathrm{E}+06$ | 906239 | 8106239 | 6.004291 | -1.814 | 919727 | 8119727 | 6.0143 | -1.145 | 0.668217 | 0.310554 |  |

Table A.3: Configuration $210 \mathrm{~cm} / \mathrm{s}$ Run 3

| Zoom <br> start <br> point | Reader <br> Epoch | Entire <br> Capture <br> Epoch | Time: | Phase <br> Read | Tag <br> Epoch | Entire <br> Capture <br> Epoch | Time: | Delta <br> Time | Phase <br> Response | Phase <br> due to <br> travel | Instant <br> Velocity |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $7.20 \mathrm{E}+06$ | 978847 | 8178847 | 6.058072 | -3.114 | 995864 | 8195864 | 6.0707 | -3.117 | -0.00303 | -0.58151 |  |
| $7.20 \mathrm{E}+06$ | 1006755 | 8206755 | 6.078743 | -2.429 | 1020186 | 8220186 | 6.0887 | -2.031 | 0.398491 | -1.18284 |  |
| $7.20 \mathrm{E}+06$ | 1033635 | 8233635 | 6.098653 | -2.718 | 1052005 | 8252005 | 6.1123 | -1.251 | 1.466965 | -2.13011 |  |
| $7.20 \mathrm{E}+06$ | 1065486 | 8265486 | 6.122245 | -0.749 | 1078942 | 8278942 | 6.1322 | 2.3464 | 3.095899 | 2.914894 |  |
| $7.20 \mathrm{E}+06$ | 1134841 | 8334841 | 6.173617 | 2.6925 | 1151869 | 8351869 | 6.1862 | -0.246 | -2.93891 | -7.14789 |  |
| $7.20 \mathrm{E}+06$ | 1162742 | 8362742 | 6.194283 | 0.0011 | 1181032 | 8381032 | 6.2078 | 2.98 | 2.978918 | -0.30286 |  |
| $7.20 \mathrm{E}+06$ | 1194490 | 8394490 | 6.217799 | -2.156 | 1207953 | 8407953 | 6.2278 | 1.0542 | 3.210382 | 9.670078 |  |
| $7.20 \mathrm{E}+06$ | 1226286 | 8426286 | 6.24135 | 2.6697 | 1239724 | 8439724 | 6.2513 | -2.842 | -5.51155 | -3.65363 |  |
| $7.20 \mathrm{E}+06$ | 1294838 | 8494838 | 6.292127 | 0.2933 | 1311844 | 8511844 | 6.3047 | 2.2623 | 1.968978 | 8.625103 |  |
| $7.20 \mathrm{E}+06$ | 1322711 | 8522711 | 6.312772 | 2.8187 | 1336173 | 8536173 | 6.3227 | -1.169 | -3.98820 | -9.50393 |  |
| $7.20 \mathrm{E}+06$ | 1354498 | 8554498 | 6.336317 | -2.638 | 1367903 | 8567903 | 6.3462 | 1.9346 | 4.572816 | 7.102472 |  |
| $7.20 \mathrm{E}+06$ | 1381351 | 8581351 | 6.356207 | -1.533 | 1394815 | 8594815 | 6.3662 | -2.386 | -0.85353 | -1.87658 |  |
| $7.20 \mathrm{E}+06$ | 1454950 | 8654950 | 6.410721 | -2.166 | 1471840 | 8671840 | 6.4232 | 1.0836 | 3.249931 | 4.464893 |  |
| $7.20 \mathrm{E}+06$ | 1482780 | 8682780 | 6.431335 | 0.874 | 1496228 | 8696228 | 6.4413 | 1.0327 | 0.158644 | -0.37593 |  |
| $7.20 \mathrm{E}+06$ | 1509733 | 8709733 | 6.451299 | -1.765 | 1528024 | 8728024 | 6.4648 | -1.267 | 0.497982 | -0.25930 |  |
| $7.20 \mathrm{E}+06$ | 1541438 | 8741438 | 6.474783 | 0.2063 | 1554989 | 8754989 | 6.4848 | 0.9028 | 0.696481 | -1.14986 |  |
| $7.20 \mathrm{E}+06$ | 1614864 | 8814864 | 6.529170 | -0.452 | 1631861 | 8831861 | 6.5418 | 2.7543 | 3.205860 | 11.28869 |  |
| $7.20 \mathrm{E}+06$ | 1642703 | 8842703 | 6.549790 | 1.4676 | 1656151 | 8856151 | 6.5598 | -3.111 | -4.5785 | -4.27411 |  |
| $7.20 \mathrm{E}+06$ | 1670157 | 8870157 | 6.570125 | 3.1181 | 1688473 | 8888473 | 6.5837 | 2.4615 | -0.65661 | 0.049675 |  |
| $7.20 \mathrm{E}+06$ | 1706721 | 8906721 | 6.597208 | -1.749 | 1720226 | 8920226 | 6.6072 | -2.450 | -0.70139 | -0.00505 |  |
| $1.20 \mathrm{E}+07$ | 178812 | 12178812 | 9.020846 | -2.182 | 195873 | 12195873 | 9.0335 | -2.414 | -0.23202 | -4.42513 |  |
| $1.20 \mathrm{E}+07$ | 206653 | 12206653 | 9.041468 | -0.849 | 220145 | 12220145 | 9.0515 | 1.9678 | 2.817159 | 2.867211 |  |
| $1.20 \mathrm{E}+07$ | 233694 | 12233694 | 9.061497 | 2.5913 | 248156 | 12248156 | 9.0722 | 3.1285 | 0.537130 | 4.190459 |  |
| $1.20 \mathrm{E}+07$ | 266638 | 12266638 | 9.085899 | 1.3373 | 285554 | 12285554 | 9.0999 | -2.575 | -3.91187 | -1.78604 |  |
| $1.20 \mathrm{E}+07$ | 334792 | 12334792 | 9.136380 | -1.792 | 351816 | 12351816 | 9.1490 | -2.344 | -0.55211 | -1.28677 |  |
| $1.20 \mathrm{E}+07$ | 362659 | 12362659 | 9.157022 | 0.7398 | 376098 | 12376098 | 9.1670 | 1.0747 | 0.334921 | 6.715029 |  |
| $1.20 \mathrm{E}+07$ | 389575 | 12389575 | 9.176958 | 2.0743 | 403056 | 12403056 | 9.1869 | -2.730 | -4.80419 | -3.27831 |  |
| $1.20 \mathrm{E}+07$ | 416494 | 12416494 | 9.196897 | 0.1989 | 429978 | 12429978 | 9.2069 | -2.100 | -2.29860 | -1.66312 |  |
| $1.20 \mathrm{E}+07$ | 494808 | 12494808 | 9.254904 | -2.463 | 511829 | 12511829 | 9.2675 | -0.897 | 1.565965 | 6.009792 |  |
| $1.20 \mathrm{E}+07$ | 522643 | 12522643 | 9.275522 | 3.0037 | 536137 | 12536137 | 9.2855 | 0.4224 | -2.58129 | 1.183840 |  |
| $1.20 \mathrm{E}+07$ | 549591 | 12549591 | 9.295482 | 2.6138 | 563056 | 12563056 | 9.3055 | -0.872 | -3.48599 | -4.20705 |  |
| $1.20 \mathrm{E}+07$ | 576510 | 12576510 | 9.315421 | 2.4368 | 590004 | 12590004 | 9.3254 | 2.1693 | -0.26747 | -0.66450 |  |
| $1.20 \mathrm{E}+07$ | 654869 | 12654869 | 9.373461 | -0.932 | 671832 | 12671832 | 9.3860 | 0.3438 | 1.276171 | 6.092085 |  |
| $1.20 \mathrm{E}+07$ | 682669 | 12682669 | 9.394053 | 2.9876 | 696221 | 12696221 | 9.4041 | 0.0458 | -2.94188 | -9.22942 |  |
| $1.20 \mathrm{E}+07$ | 709665 | 12709665 | 9.414049 | -1.924 | 723098 | 12723098 | 9.424 | 2.1764 | 4.100304 | 0.126893 |  |
| $1.20 \mathrm{E}+07$ | 736494 | 12736494 | 9.433921 | -1.422 | 749962 | 12749962 | 9.4439 | 2.5812 | 4.003530 | 1.425410 |  |
| $1.20 \mathrm{E}+07$ | 814776 | 12814776 | 9.491905 | -1.067 | 831829 | 12831829 | 9.5045 | -0.376 | 0.690687 | -3.95581 |  |
| $1.20 \mathrm{E}+07$ | 842730 | 12842730 | 9.512610 | -2.403 | 856173 | 12856173 | 9.5226 | 1.0211 | 3.424564 | 0.332799 |  |
| $1.20 \mathrm{E}+07$ | 874601 | 12874601 | 9.536217 | -2.673 | 888095 | 12888095 | 9.5462 | 0.4499 | 3.122968 | 3.556132 |  |
| $1.20 \mathrm{E}+07$ | 901478 | 12901478 | 9.556125 | -1.620 | 914943 | 12914943 | 9.5661 | -1.208 | 0.412516 | 1.489885 |  |

Table A.3: Configuration $210 \mathrm{~cm} / \mathrm{s}$ Run 3

| Zoom <br> start <br> point | Reader <br> Epoch | Entire <br> Capture <br> Epoch | Time: | Phase <br> Read | Tag <br> Epoch | Entire <br> Capture <br> Epoch | Time: | $\begin{aligned} & \text { Delta } \\ & \text { Time } \end{aligned}$ | Phase <br> Response | Phase <br> due to travel | Instant Velocity |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $1.20 \mathrm{E}+07$ | 974773 | 12974773 | 9.610414 | 0.3129 | 991794 | 12991794 | 9.6230 | -2.525 | -2.83802 | -0.51699 |  |
| $1.20 \mathrm{E}+07$ | 1002724 | 13002724 | 9.631118 | 0.2097 | 1020999 | 13020999 | 9.6447 | -2.200 | -2.40938 | -4.46541 |  |
| $1.20 \mathrm{E}+07$ | 1034479 | 13034479 | 9.654639 | 0.9278 | 1047973 | 13047973 | 9.6646 | 1.9379 | 1.010088 | 6.166887 |  |
| $1.20 \mathrm{E}+07$ | 1061459 | 13061459 | 9.674623 | 2.1064 | 1074863 | 13074863 | 9.6846 | -1.591 | -3.69761 | -0.79614 |  |
| $1.20 \mathrm{E}+07$ | 1134793 | 13134793 | 9.728941 | 2.9115 | 1151788 | 13151788 | 9.7415 | 0.9525 | -1.95897 | 3.728345 |  |
| $1.20 \mathrm{E}+07$ | 1162715 | 13162715 | 9.749623 | 2.5187 | 1176257 | 13176257 | 9.7597 | -2.030 | -4.54888 | -11.9963 |  |
| $1.20 \mathrm{E}+07$ | 1189785 | 13189785 | 9.769674 | -1.534 | 1203112 | 13203112 | 9.7795 | 3.0632 | 4.596992 | 11.34611 |  |
| $1.20 \mathrm{E}+07$ | 1216582 | 13216582 | 9.789522 | 2.9927 | 1234873 | 13234873 | 9.8031 | -2.641 | -5.63342 | -0.46438 |  |
| $1.20 \mathrm{E}+07$ | 1294771 | 13294771 | 9.847437 | 1.8932 | 1311779 | 13311779 | 9.8600 | -2.726 | -4.61955 | -4.27656 |  |
| $1.20 \mathrm{E}+07$ | 1322664 | 13322664 | 9.868097 | 0.4339 | 1336103 | 13336103 | 9.8781 | -1.233 | -1.66642 | -7.35487 |  |
| $1.20 \mathrm{E}+07$ | 1349657 | 13349657 | 9.888091 | -1.882 | 1363048 | 13363048 | 9.8980 | 2.0772 | 3.959646 | 2.031626 |  |
| $1.20 \mathrm{E}+07$ | 1376528 | 13376528 | 9.907994 | -2.904 | 1390006 | 13390006 | 9.9180 | -0.499 | 2.404814 | 3.177332 |  |
| $1.20 \mathrm{E}+07$ | 1454778 | 13454778 | 9.965954 | 2.1788 | 1471786 | 13471786 | 9.9786 | -2.793 | -4.97188 | -12.3091 |  |
| $1.20 \mathrm{E}+07$ | 1482700 | 13482700 | 9.986636 | -2.677 | 1496317 | 13496317 | 9.9967 | 0.9229 | 3.600369 | 4.461013 |  |
| $1.20 \mathrm{E}+07$ | 1514320 | 13514320 | 10.01006 | -1.034 | 1527817 | 13527817 | 10.020 | -1.423 | -0.38893 | -0.61277 |  |
| $1.20 \mathrm{E}+07$ | 1541239 | 13541239 | 10.03000 | -2.761 | 1554704 | 13554704 | 10.04 | -2.682 | 0.078801 | -0.45968 |  |
| $1.20 \mathrm{E}+07$ | 1614804 | 13614804 | 10.08449 | -1.848 | 1631867 | 13631867 | 10.097 | -0.762 | 1.085782 | -1.85402 |  |
| $1.20 \mathrm{E}+07$ | 1642710 | 13642710 | 10.10516 | 0.1644 | 1656191 | 13656191 | 10.115 | 2.5304 | 2.366052 | 7.006134 |  |
| $1.20 \mathrm{E}+07$ | 1674420 | 13674420 | 10.12864 | 1.4012 | 1689513 | 13689513 | 10.140 | -2.860 | -4.26163 | -5.34169 |  |
| $1.20 \mathrm{E}+07$ | 1707820 | 13707820 | 10.15338 | 1.1356 | 1721236 | 13721236 | 10.163 | 1.6846 | 0.549040 | 0.004382 |  |
| $1.88 \mathrm{E}+07$ | 133843 | 18933843 | 14.02430 | -0.676 | 150866 | 18950866 | 14.037 | -0.777 | -0.10147 | -3.13020 |  |
| $1.88 \mathrm{E}+07$ | 161699 | 18961699 | 14.04493 | -0.232 | 180762 | 18980762 | 14.059 | 2.3232 | 2.555196 | -1.31833 |  |
| $1.88 \mathrm{E}+07$ | 192256 | 18992256 | 14.06756 | -2.657 | 207738 | 19007738 | 14.079 | 0.9076 | 3.564808 | 4.789902 |  |
| $1.88 \mathrm{E}+07$ | 226085 | 19026085 | 14.09262 | -1.724 | 239550 | 19039550 | 14.103 | -2.485 | -0.76102 | 0.429026 |  |
| $1.88 \mathrm{E}+07$ | 289848 | 19089848 | 14.13985 | 1.1912 | 306836 | 19106836 | 14.152 | -0.389 | -1.58055 | -0.66230 |  |
| $1.88 \mathrm{E}+07$ | 317702 | 19117702 | 14.16048 | 1.7033 | 331135 | 19131135 | 14.170 | 0.5796 | -1.12368 | -1.67440 |  |
| $1.88 \mathrm{E}+07$ | 344636 | 19144636 | 14.18043 | -2.553 | 358058 | 19158058 | 14.190 | -2.397 | 0.156101 | -2.00498 |  |
| $1.88 \mathrm{E}+07$ | 372579 | 19172579 | 14.20113 | -0.806 | 386031 | 19186031 | 14.211 | 0.9419 | 1.748310 | 1.259309 |  |
| $1.88 \mathrm{E}+07$ | 449856 | 19249856 | 14.25837 | 0.766 | 466837 | 19266837 | 14.271 | -0.375 | -1.14056 | 3.269545 |  |
| $1.88 \mathrm{E}+07$ | 477690 | 19277690 | 14.27898 | 2.211 | 495941 | 19295941 | 14.293 | -1.631 | -3.84198 | -3.94423 |  |
| $1.88 \mathrm{E}+07$ | 509397 | 19309397 | 14.30247 | 3.0436 | 522922 | 19322922 | 14.312 | 2.2228 | -0.82083 | -0.74713 |  |
| $1.88 \mathrm{E}+07$ | 541257 | 19341257 | 14.32607 | 2.5566 | 554777 | 19354777 | 14.336 | 2.4114 | -0.14518 | -1.06119 |  |
| $1.88 \mathrm{E}+07$ | 609888 | 19409888 | 14.37690 | 0.9368 | 626864 | 19426864 | 14.389 | 2.9633 | 2.026534 | 4.028048 |  |
| $1.88 \mathrm{E}+07$ | 637738 | 19437738 | 14.39753 | -2.093 | 651168 | 19451168 | 14.407 | -2.846 | -0.75270 | -1.34420 |  |
| $1.88 \mathrm{E}+07$ | 664693 | 19464693 | 14.41750 | -3.000 | 678081 | 19478081 | 14.427 | -2.725 | 0.274320 | -5.48932 |  |
| $1.88 \mathrm{E}+07$ | 691553 | 19491553 | 14.43739 | -2.643 | 705036 | 19505036 | 14.447 | 1.8314 | 4.474910 | 3.385222 |  |
| $1.88 \mathrm{E}+07$ | 769851 | 19569851 | 14.49539 | 3.0046 | 786875 | 19586875 | 14.508 | -0.386 | -3.39010 | -4.76591 |  |
| $1.88 \mathrm{E}+07$ | 797738 | 19597738 | 14.51604 | 2.6658 | 811158 | 19611158 | 14.526 | 2.5612 | -0.10461 | 1.932020 |  |
| $1.88 \mathrm{E}+07$ | 824816 | 19624816 | 14.53610 | 0.1711 | 847818 | 19647818 | 14.553 | -1.944 | -2.11535 | 1.836753 |  |
| $1.88 \mathrm{E}+07$ | 861332 | 19661332 | 14.56315 | 2.0189 | 874820 | 19674820 | 14.573 | -1.504 | -3.52334 | -2.11632 |  |

Table A.3: Configuration $210 \mathrm{~cm} / \mathrm{s}$ Run 3

| Zoom <br> start <br> point | Reader <br> Epoch | Entire <br> Capture <br> Epoch | Time: | Phase <br> Read | Tag <br> Epoch | Entire <br> Capture <br> Epoch | Time: | $\begin{aligned} & \text { Delta } \\ & \text { Time } \end{aligned}$ | Phase <br> Response | Phase <br> due to travel | Instant Velocity |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $1.88 \mathrm{E}+07$ | 929878 | 19729878 | 14.61392 | -1.280 | 946870 | 19746870 | 14.627 | -0.474 | 0.805455 | 1.509517 |  |
| $1.88 \mathrm{E}+07$ | 957723 | 19757723 | 14.63455 | 2.6334 | 971169 | 19771169 | 14.645 | 2.3975 | -0.23585 | 1.594245 |  |
| $1.88 \mathrm{E}+07$ | 985133 | 19785133 | 14.65485 | -0.977 | 998653 | 19798653 | 14.665 | -2.457 | -1.47976 | 3.200908 |  |
| $1.88 \mathrm{E}+07$ | 1012570 | 19812570 | 14.67517 | 1.2127 | 1026011 | 19826011 | 14.685 | -2.753 | -3.96580 | -1.81836 |  |
| $1.88 \mathrm{E}+07$ | 1089831 | 19889831 | 14.73240 | -1.497 | 1106839 | 19906839 | 14.745 | -1.290 | 0.206661 | 1.380855 |  |
| $1.88 \mathrm{E}+07$ | 1117697 | 19917697 | 14.75304 | 0.9249 | 1131133 | 19931133 | 14.763 | 0.1792 | -0.74569 | -5.93430 |  |
| $1.88 \mathrm{E}+07$ | 1145776 | 19945776 | 14.77384 | -2.505 | 1159235 | 19959235 | 14.784 | 1.4837 | 3.988637 | 7.611767 |  |
| $1.88 \mathrm{E}+07$ | 1172678 | 19972678 | 14.79376 | 1.0491 | 1186153 | 19986153 | 14.804 | -0.779 | -1.82811 | 1.215011 |  |
| $1.88 \mathrm{E}+07$ | 1249871 | 20049871 | 14.85094 | 3.0373 | 1266849 | 20066849 | 14.864 | -1.574 | -4.61157 | -12.2314 |  |
| $1.88 \mathrm{E}+07$ | 1277794 | 20077794 | 14.87162 | -1.138 | 1291243 | 20091243 | 14.882 | 2.7207 | 3.858985 | -0.68776 |  |
| $1.88 \mathrm{E}+07$ | 1304728 | 20104728 | 14.89157 | -2.194 | 1318278 | 20118278 | 14.902 | 2.193 | 4.386844 | 3.053101 |  |
| $1.88 \mathrm{E}+07$ | 1336541 | 20136541 | 14.91514 | 0.0894 | 1349910 | 20149910 | 14.925 | 1.7345 | 1.645145 | 1.547141 |  |
| $1.88 \mathrm{E}+07$ | 1409950 | 20209950 | 14.96951 | -0.622 | 1426860 | 20226860 | 14.982 | -2.357 | -1.73465 | -2.19721 |  |
| $1.88 \mathrm{E}+07$ | 1437599 | 20237599 | 14.98999 | -0.131 | 1451148 | 20251148 | 15 | -0.350 | -0.21964 | 0.632078 |  |
| $1.88 \mathrm{E}+07$ | 1464633 | 20264633 | 15.01001 | -1.458 | 1482828 | 20282828 | 15.023 | -2.247 | -0.78811 | -3.27324 |  |
| $1.88 \mathrm{E}+07$ | 1496266 | 20296266 | 15.03344 | -1.721 | 1519868 | 20319868 | 15.051 | 0.9325 | 2.653811 | -0.89042 |  |
| $1.88 \mathrm{E}+07$ | 1569819 | 20369819 | 15.08792 | -1.593 | 1586833 | 20386833 | 15.101 | 2.754 | 4.346571 | 4.512828 |  |
| $1.88 \mathrm{E}+07$ | 1597741 | 20397741 | 15.10861 | -2.176 | 1612245 | 20412245 | 15.119 | -1.085 | 1.090907 | 0.889721 |  |
| $1.88 \mathrm{E}+07$ | 1625738 | 20425738 | 15.12934 | -2.227 | 1643857 | 20443857 | 15.143 | -1.934 | 0.292438 | 1.108112 |  |
| $1.88 \mathrm{E}+07$ | 1657371 | 20457371 | 15.15277 | -0.234 | 1670796 | 20470796 | 15.163 | -0.789 | -0.55502 | 0.005860 |  |
| $3.15 \mathrm{E}+07$ | 229694 | 31729694 | 23.50218 | 2.1358 | 246706 | 31746706 | 23.515 | -0.295 | -2.43097 | -2.91835 |  |
| $3.15 \mathrm{E}+07$ | 257634 | 31757634 | 23.52288 | -0.919 | 271127 | 31771127 | 23.533 | -1.326 | -0.40770 | -3.38730 |  |
| $3.15 \mathrm{E}+07$ | 289318 | 31789318 | 23.54635 | -2.506 | 302793 | 31802793 | 23.556 | 0.1318 | 2.637385 | 2.701855 |  |
| $3.15 \mathrm{E}+07$ | 316278 | 31816278 | 23.56632 | -2.463 | 334514 | 31834514 | 23.580 | -2.259 | 0.204280 | 0.518232 |  |
| $3.15 \mathrm{E}+07$ | 389685 | 31889685 | 23.62069 | -1.595 | 406685 | 31906685 | 23.633 | -2.452 | -0.85751 | 0.598152 |  |
| $3.15 \mathrm{E}+07$ | 417576 | 31917576 | 23.64135 | 1.3933 | 431028 | 31931028 | 23.651 | 0.1224 | -1.27088 | -2.22638 |  |
| $3.15 \mathrm{E}+07$ | 444476 | 31944476 | 23.66127 | -1.847 | 457928 | 31957928 | 23.671 | -1.418 | 0.429336 | -5.69872 |  |
| $3.15 \mathrm{E}+07$ | 471390 | 31971390 | 23.68121 | -2.229 | 484851 | 31984851 | 23.691 | 2.5558 | 4.784986 | 3.784189 |  |
| $3.15 \mathrm{E}+07$ | 549698 | 32049698 | 23.73921 | 2.56 | 566675 | 32066675 | 23.752 | -1.445 | -4.00535 | -8.24521 |  |
| $3.15 \mathrm{E}+07$ | 577527 | 32077527 | 23.75982 | -2.747 | 590995 | 32090995 | 23.770 | -1.060 | 1.687338 | 2.918989 |  |
| $3.15 \mathrm{E}+07$ | 609305 | 32109305 | 23.78336 | 0.1968 | 622835 | 32122835 | 23.793 | -0.754 | -0.95117 | -4.20861 |  |
| $3.15 \mathrm{E}+07$ | 636212 | 32136212 | 23.80329 | -2.133 | 649774 | 32149774 | 23.813 | 0.1342 | 2.267476 | 2.873154 |  |
| $3.15 \mathrm{E}+07$ | 709681 | 32209681 | 23.85771 | 2.1583 | 725588 | 32225588 | 23.869 | -1.758 | -3.91639 | -0.09381 |  |
| $3.15 \mathrm{E}+07$ | 737618 | 32237618 | 23.87840 | 2.4626 | 751072 | 32251072 | 23.888 | -1.386 | -3.84852 | -7.80989 |  |
| $3.15 \mathrm{E}+07$ | 764589 | 32264589 | 23.89838 | -1.209 | 778495 | 32278495 | 23.909 | 1.0228 | 2.231591 | 0.540956 |  |
| $3.15 \mathrm{E}+07$ | 801704 | 32301704 | 23.92587 | -0.934 | 819931 | 32319931 | 23.939 | 0.6617 | 1.595247 | 2.619384 |  |
| $3.15 \mathrm{E}+07$ | 869680 | 32369680 | 23.97622 | 0.4782 | 886703 | 32386703 | 23.989 | -2.892 | -3.37005 | -5.24520 |  |
| $3.15 \mathrm{E}+07$ | 897617 | 32397617 | 23.99691 | -2.834 | 915823 | 32415823 | 24.010 | -1.868 | 0.966109 | 4.354651 |  |
| $3.15 \mathrm{E}+07$ | 938986 | 32438986 | 24.02756 | 1.506 | 952459 | 32452459 | 24.038 | -2.057 | -3.56301 | -10.2585 |  |
| $3.15 \mathrm{E}+07$ | 970785 | 32470785 | 24.05111 | -3.098 | 984253 | 32484253 | 24.061 | 2.5984 | 5.696370 | 1.685166 |  |

Table A.3: Configuration $210 \mathrm{~cm} / \mathrm{s}$ Run 3

| Zoom <br> start <br> point | Reader <br> Epoch | Entire <br> Capture <br> Epoch | Time: | Phase <br> Read | $\begin{gathered} \text { Tag } \\ \text { Epoch } \end{gathered}$ | Entire <br> Capture <br> Epoch | Time: | Delta <br> Time | Phase <br> Response | Phase <br> due to travel | Instant <br> Velocity |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $3.15 \mathrm{E}+07$ | 1029688 | 32529688 | 24.09474 | -1.987 | 1046743 | 32546743 | 24.107 | 0.7202 | 2.706823 | 3.789003 |  |
| $3.15 \mathrm{E}+07$ | 1057609 | 32557609 | 24.11542 | $-1.766$ | 1075822 | 32575822 | 24.129 | -2.187 | -0.42110 | -0.09992 |  |
| $3.15 \mathrm{E}+07$ | 1089268 | 32589268 | 24.13887 | 2.3948 | 1102713 | 32602713 | 24.149 | 2.05 | -0.34483 | -2.46437 |  |
| $3.15 \mathrm{E}+07$ | 1116184 | 32616184 | 24.15881 | -0.502 | 1129645 | 32629645 | 24.169 | 1.037 | 1.539376 | -1.33046 |  |
| $3.15 \mathrm{E}+07$ | 1189662 | 32689662 | 24.21323 | -2.178 | 1206646 | 32706646 | 24.226 | 2.2701 | 4.447747 | 7.646785 |  |
| $3.15 \mathrm{E}+07$ | 1217608 | 32717608 | 24.23393 | 1.4684 | 1235890 | 32735890 | 24.247 | -0.432 | -1.90070 | 2.518200 |  |
| $3.15 \mathrm{E}+07$ | 1249386 | 32749386 | 24.25747 | 2.3974 | 1262884 | 32762884 | 24.267 | -1.433 | -3.83049 | -4.98013 |  |
| $3.15 \mathrm{E}+07$ | 1276293 | 32776293 | 24.2774 | -2.075 | 1289761 | 32789761 | 24.287 | -2.106 | -0.03058 | 0.914760 |  |
| $3.15 \mathrm{E}+07$ | 1349661 | 32849661 | 24.33174 | 1.9177 | 1366659 | 32866659 | 24.344 | -0.110 | -2.02756 | -3.91368 |  |
| $3.15 \mathrm{E}+07$ | 1377637 | 32877637 | 24.35247 | -2.504 | 1391107 | 32891107 | 24.362 | -1.815 | 0.688757 | 3.090238 |  |
| $3.15 \mathrm{E}+07$ | 1404514 | 32904514 | 24.37237 | 2.184 | 1418039 | 32918039 | 24.382 | 0.5101 | -1.67396 | -3.04149 |  |
| $3.15 \mathrm{E}+07$ | 1431453 | 32931453 | 24.39233 | 1.9944 | 1449735 | 32949735 | 24.406 | 3.0572 | 1.062839 | 0.263609 |  |
| $3.15 \mathrm{E}+07$ | 1509644 | 33009644 | 24.45024 | -2.610 | 1526667 | 33026667 | 24.463 | -2.122 | 0.487107 | 1.626755 |  |
| $3.15 \mathrm{E}+07$ | 1537503 | 33037503 | 24.47088 | -0.720 | 1550971 | 33050971 | 24.481 | -1.355 | -0.63530 | -1.66899 |  |
| $3.15 \mathrm{E}+07$ | 1569336 | 33069336 | 24.49446 | -2.979 | 1582772 | 33082772 | 24.504 | -2.107 | 0.871463 | -5.62646 |  |
| $3.15 \mathrm{E}+07$ | 1596211 | 33096211 | 24.51436 | -3.057 | 1609750 | 33109750 | 24.524 | 2.1238 | 5.180664 | 1.818700 |  |
| $3.15 \mathrm{E}+07$ | 1669673 | 33169673 | 24.56878 | -2.520 | 1686712 | 33186712 | 24.581 | -1.313 | 1.207014 | 2.141827 |  |
| $3.15 \mathrm{E}+07$ | 1697571 | 33197571 | 24.58944 | -0.112 | 1716378 | 33216378 | 24.603 | -0.709 | -0.59681 | -0.77787 |  |
| $3.15 \mathrm{E}+07$ | 1729824 | 33229824 | 24.61333 | 0.6774 | 1743349 | 33243349 | 24.623 | 0.6762 | -0.00121 | -0.76836 |  |
| $3.15 \mathrm{E}+07$ | 1761524 | 33261524 | 24.63681 | -1.313 | 1774953 | 33274953 | 24.647 | -0.625 | 0.688171 | 0.022258 |  |
| $3.65 \mathrm{E}+07$ | 29594 | 36529594 | 27.05747 | -1.078 | 46652 | 36546652 | 27.070 | -2.457 | -1.37917 | -2.87117 |  |
| $3.65 \mathrm{E}+07$ | 57479 | 36557479 | 27.07812 | -2.701 | 80511 | 36580511 | 27.095 | -1.320 | 1.380679 | 3.688543 |  |
| $3.65 \mathrm{E}+07$ | 94084 | 36594084 | 27.10524 | 0.6881 | 112221 | 36612221 | 27.119 | -1.252 | -1.93982 | -4.75579 |  |
| $3.65 \mathrm{E}+07$ | 125695 | 36625695 | 27.12865 | 0.4847 | 139156 | 36639156 | 27.139 | 2.1815 | 1.696749 | 0.586544 |  |
| $3.65 \mathrm{E}+07$ | 189678 | 36689678 | 27.17604 | -2.766 | 206659 | 36706659 | 27.189 | -2.193 | 0.572724 | 2.752329 |  |
| $3.65 \mathrm{E}+07$ | 211727 | 36711727 | 27.19238 | 2.6758 | 232088 | 36732088 | 27.207 | 1.2616 | -1.41420 | 4.805869 |  |
| $3.65 \mathrm{E}+07$ | 245452 | 36745452 | 27.21736 | 3.1309 | 258934 | 36758934 | 27.227 | -1.946 | -5.07692 | -4.09171 |  |
| $3.65 \mathrm{E}+07$ | 277254 | 36777254 | 27.24091 | -0.243 | 290711 | 36790711 | 27.251 | -1.629 | -1.38571 | -1.90669 |  |
| $3.65 \mathrm{E}+07$ | 349640 | 36849640 | 27.29453 | -2.522 | 366652 | 36866652 | 27.307 | 0.2028 | 2.724923 | -0.56505 |  |
| $3.65 \mathrm{E}+07$ | 377533 | 36877533 | 27.31519 | -0.248 | 390960 | 36890960 | 27.325 | 2.8664 | 3.114856 | 5.335304 |  |
| $3.65 \mathrm{E}+07$ | 404497 | 36904497 | 27.33516 | -1.315 | 422707 | 36922707 | 27.349 | -3.009 | -1.69369 | -5.47908 |  |
| $3.65 \mathrm{E}+07$ | 441010 | 36941010 | 27.36221 | -2.929 | 454462 | 36954462 | 27.372 | 0.3168 | 3.245678 | 2.326785 |  |
| $3.65 \mathrm{E}+07$ | 509665 | 37009665 | 27.41306 | 0.818 | 526617 | 37026617 | 27.426 | -0.703 | -1.52055 | -2.27921 |  |
| $3.65 \mathrm{E}+07$ | 537495 | 37037495 | 27.43367 | 1.4726 | 555750 | 37055750 | 27.447 | 1.8371 | 0.364492 | -1.02528 |  |
| $3.65 \mathrm{E}+07$ | 569179 | 37069179 | 27.45714 | -3.078 | 582593 | 37082593 | 27.467 | -1.932 | 1.145809 | 0.912559 |  |
| $3.65 \mathrm{E}+07$ | 600886 | 37100886 | 27.48063 | -1.264 | 614366 | 37114366 | 27.491 | -0.942 | 0.322673 | -1.90296 |  |
| $3.65 \mathrm{E}+07$ | 669668 | 37169668 | 27.53157 | -2.456 | 686649 | 37186649 | 27.544 | 1.7721 | 4.227641 | 10.91506 |  |
| $3.65 \mathrm{E}+07$ | 697501 | 37197501 | 27.55219 | 0.7039 | 710931 | 37210931 | 27.562 | -2.593 | -3.29660 | -1.08709 |  |
| $3.65 \mathrm{E}+07$ | 724449 | 37224449 | 27.57215 | 0.5949 | 737914 | 37237914 | 27.582 | -1.869 | -2.46386 | -1.63864 |  |
| $3.65 \mathrm{E}+07$ | 756067 | 37256067 | 27.59557 | 1.6679 | 769560 | 37269560 | 27.606 | 0.6762 | -0.99170 | -2.15345 |  |

Table A.3: Configuration $210 \mathrm{~cm} / \mathrm{s}$ Run 3

| Zoom <br> start <br> point | Reader <br> Epoch | Entire <br> Capture <br> Epoch | Time: | Phase <br> Read | Tag <br> Epoch | Entire <br> Capture <br> Epoch | Time: | Delta <br> Time | Phase <br> Response | Phase due to travel | Instant <br> Velocity |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $3.65 \mathrm{E}+07$ | 829614 | 37329614 | 27.65005 | -2.706 | 846623 | 37346623 | 27.663 | 1.0135 | 3.719511 | 7.511571 |  |
| $3.65 \mathrm{E}+07$ | 857517 | 37357517 | 27.67071 | -1.420 | 870953 | 37370953 | 27.681 | -2.889 | -1.46879 | -4.31003 |  |
| $3.65 \mathrm{E}+07$ | 884452 | 37384452 | 27.69066 | $-1.153$ | 898953 | 37398953 | 27.701 | 0.8038 | 1.957239 | 1.839316 |  |
| $3.65 \mathrm{E}+07$ | 912390 | 37412390 | 27.71136 | -1.630 | 925907 | 37425907 | 27.721 | -1.08 | 0.549793 | 0.217784 |  |
| $3.65 \mathrm{E}+07$ | 989593 | 37489593 | 27.76854 | $-2.507$ | 1006627 | 37506627 | 27.781 | -2.456 | 0.050727 | 2.237358 |  |
| $3.65 \mathrm{E}+07$ | 1017446 | 37517446 | 27.78917 | -0.370 | 1030906 | 37530906 | 27.799 | -1.862 | -1.49139 | -1.33862 |  |
| $3.65 \mathrm{E}+07$ | 1045545 | 37545545 | 27.80999 | $-1.135$ | 1058984 | 37558984 | 27.820 | -1.560 | -0.42436 | 4.726212 |  |
| $3.65 \mathrm{E}+07$ | 1072445 | 37572445 | 27.82991 | 1.2339 | 1085967 | 37585967 | 27.840 | -2.811 | -4.04475 | -3.57495 |  |
| $3.65 \mathrm{E}+07$ | 1149593 | 37649593 | 27.88705 | -1.790 | 1166617 | 37666617 | 27.900 | 2.3506 | 4.140396 | 12.12872 |  |
| $3.65 \mathrm{E}+07$ | 1177462 | 37677462 | 27.90770 | 1.9706 | 1190947 | 37690947 | 27.918 | -2.266 | -4.23700 | -5.68964 |  |
| $3.65 \mathrm{E}+07$ | 1204439 | 37704439 | 27.92768 | -2.623 | 1217835 | 37717835 | 27.938 | -2.517 | 0.106052 | 4.456310 |  |
| $3.65 \mathrm{E}+07$ | 1231323 | 37731323 | 27.94759 | 0.9572 | 1244824 | 37744824 | 27.958 | -2.351 | -3.30835 | -0.00793 |  |
| $3.65 \mathrm{E}+07$ | 1309590 | 37809590 | 28.00556 | 2.8128 | 1326595 | 37826595 | 28.018 | -0.477 | -3.28995 | -2.45785 |  |
| $3.65 \mathrm{E}+07$ | 1337462 | 37837462 | 28.02621 | -0.903 | 1350941 | 37850941 | 28.036 | -2.494 | -1.59118 | -7.42908 |  |
| $3.65 \mathrm{E}+07$ | 1369168 | 37869168 | 28.04969 | -2.890 | 1382622 | 37882622 | 28.060 | 2.2004 | 5.090508 | 5.204102 |  |
| $3.65 \mathrm{E}+07$ | 1396107 | 37896107 | 28.06965 | 1.1079 | 1409589 | 37909589 | 28.080 | 2.2143 | 1.106406 | 0.374751 |  |
| $3.65 \mathrm{E}+07$ | 1469606 | 37969606 | 28.12409 | $-1.960$ | 1486589 | 37986589 | 28.137 | -1.672 | 0.287213 | 4.111272 |  |
| $3.65 \mathrm{E}+07$ | 1497606 | 37997606 | 28.14483 | 1 | 1511021 | 38011021 | 28.155 | -1.564 | -2.56438 | -2.15943 |  |
| $3.65 \mathrm{E}+07$ | 1529357 | 38029357 | 28.16834 | -0.277 | 1547654 | 38047654 | 28.182 | -0.596 | -0.31861 | -5.15898 |  |
| $3.65 \mathrm{E}+07$ | 1561012 | 38061012 | 28.19179 | $-2.784$ | 1574459 | 38074459 | 28.202 | 0.8227 | 3.607220 |  |  |
|  |  |  |  |  |  |  |  | Averages= |  | -0.08121 |  |

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