HIDDEN SURFACE

LINE DRAWING ALGORITHM
by

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## ABSTRACT

This paper describes a fast procedure in processing hidden surface pictures with the output in vector form. The program has been written expressly for a Decsystem 10 and has performed successfully on three different installations.

The algorithm which is being used is a modification to the Watkins' Algorithm. Consequently, the program has inherited many key features which provide for speed, compactness, and flexibility.

## INTRODUCTION

There has long been a need for a very fast hidden surface line drawing algorithm. At the University of Utah, Dr. Gary Watkins developed a very efficient continuous tone hidden surface algorithm which could be implemented in hardware to produce pictures at rates of 30 frames per second. It turns out that with a few minor modifications, the same algorithm can be adapted to produce line drawings.

There were two requirements that had to be fulfilled: (1) A procedure had to be developed that would handle horizontal edges, since these were discarded during preframe processing and (2) Information would have to be extracted from the existing algorithm which could generate lines. It will be necessary to briefly explain Watkins' Algorithm in order to understand the line drawing procedure more clearly.

## WATKINS' ALGORITHM

Hidden surface pictures are processed by using a raster approach originally developed by the Romney Hidden Surface Algorithm. The user is required to describe his objects in terms of polygons and associated edges. Preframe processing clips all of these edges so that they are within the view area, and then sorts them with respect to $Y$.

On any given scan line, pairs of edges that belong to the same polygon are linked together to form segments. For the current scan line, these segments are compared to determine which set of segments is visible.


RELATIONSHIP BETWEEN EDGES AND SEGMENTS

From this point, the information is passed to a shader which produces the continuous tone for a visible segment. After a scan line has been completed, all segments are updated to the next scan line. Some minor sorting is performed at this time, due to exiting edges and new entering edges.

## LINE DRAWING ALGORITHM

During preframe processing, all horizontal edges are saved in a free storage list with a pointer to the polygon to which they belong. These horizontal edges are also sorted in $Y$. When the hidden surface algorithm comes up with a visible segment, this segment is checked to see if the polygon to which it belongs has a horizontal edge existing within the region of the visible span. One minor problem arises with this type of an approach. Preframe processing stores all edges so that the vertices lie between scan lines. Two polygons which shared the same horizontal edge were processed in a way that the hidden surface algorithm physically separated the two polygons which led to the two displayed horizontal edges. In order to keep the sorting of these edges as simple as possible, a simple rule was formed: All horizontal edges are visible on the current scan line to which they really belong, and possibly on the previous scan line. Thus, when two polygons share an edge, the edge will be displayed twice, but the two lines will be coincident. Since each segment is composed of a left and a right edge, it is very easy to add flags to the segment block indicating if the edge is


SEGMENT BLOCK
really visible on this scan line. Every time the hidden surface algorithm passes a visible segment over to the "shader," a counter in the segment block is incremented for the left or right edge of the segment, stating that the edge has been visible for " N " scan lines. Two conditions now arise stipulating when a line should be physically drawn. If the edge is exiting on this scan line, then draw. If the edge was visible on the previous scan line and not this scan line, then draw. Whenever an edge is drawn, the counter inside the segment block is cleared. The first time that an edge becomes visible, the starting point of the edge is stored so that the end point of the line is available. This holds true for edges which are intermittently visible. Following is a picture of the segment block.

Unfortunately, there are three minor flaws which exist as a result of letting the Watkins' Algorithm do the hidden surface processing.

It was stated earlier that preframe processing stores edges so that vertices lie between scan lines. Consequently, a line is drawn so that it extends from a point that lies between scan lines. The difficulty arises when two adjacent edges are visible on a scan line, but one of the edges crosses in front of the other edge on the next scan line. Drawing to the midpoint between scan lines results in lines extending a little over other edges. Fortunately, there is enough information available at this time to capture this problem and draw the correct line without overlap for edges that are visible on the previous scan line. Edges which enter for the first time run the risk of creating overlap. This problem could be handled by storing the previous scan line of information.

The second problem deals with intersection of surfaces. Since an imaginary edge exists at points of intersection, there does not exist a segment block where a counter could be incremented to specify that the edge of intersection has been visible. There are two solutions to this dilemma. Whenever an intersection is encountered by the "shader," it will display a dot. The second solution is to create a segment block which contains similar edge information, and then process the line. This would require some overhead in programming, but the aesthetics of the lines would be worth the effort.

The third problem deals with the resolution of the picture. The package which is distributed works with a resolution of 256 scan lines in $Y$. Thus, objects may look a little distorted when displayed, due to the perspective transformation and roundoff to the scan line. The user can compensate for this by changing the source code so that the resolution is greater. Computation time will increase linearly. In file FSTLIN.F4, change BUCKY (0/255), $\operatorname{HBUCKY}(256)$ to BUCKY (0/1023), HBUCKY (1024) and in file EDGLIN.MAC, change YRESOLUTION=256 to YRESOLUTION=1024, if the user wishes to increase the $Y$ resolution to 1024. Increasing the resolution will also decrease the amount of overlap when edges cross. There is no point in making the resolution greater than the resolution of the display device.

There are a number of very useful features concerning the hidden surface line drawing algorithm. Since the program works on a low resolution, very little time is devoured in processing a picture. Pictures containing 1000 edges take about 15 seconds of $C P U$ time on a Decsystem 10. Timesharing users don't have to wait very long for a picture to be processed.

Code and data for the algorithm require about 2000 words of memory. Consequently, the program will do little page faulting during execution. 1.0: $=$

Each edge requires four words of memory from the free storage list, thus permitting complex pictures to reside in a very limited area when core is at a premium.

Perhaps the modification of the Watkins' Algorithm was not the most ideal approach to hidden surface processing for line drawings. However, it is believed that speed, compactness, and flexibility of the procedure will keep many users happy for the present.

Following is a brief explanation of how an edge is processed. The data describing the end point is stored into working registers. This data is then clipped to the four planes of the cone of vision ( $Z=Y$, $Z=-Y, Z=-X, Z=X)$. The processed edge is checked to see if it lies within the cone of vision. If the edge is visible and not a horizontal, then the data for the edge is packed into a four word block for hidden surface processing.


This page defines the registers which are used inside the routine EDGMAK. It should be noted that accumulators are not saved, with the exception of AC7. All arithmetic is performed in $A C O, A C l$, and $A C 2$, while indexing is performed in AC3, AC4, AC5, and AC6. The only subroutines external to EDGMAK are IFIX, VECTO, MOVETO, and GETVAR, which returns a block from free storage. There are three entry points to this routine: EDGMAK, POLMAK, and INTCLP. Data is passed over in global areas FREE, SCOPE, CLIP2, CLIPH, CLIP3, EYES, and COLOUR. Data is sent out to the world via global areas INTENS, and FREE.

TIILE EDGMAK
ENIRY EJGMAK，PULMAK，INTCLP
EXIERN IFIX，FREE，GETVAR，SCJPE
EXIERN CLIP2．CLIPH，CLIP3
TRESOLUIIOV＝＾D255 ：CHANGE IHIS NUMBER IF MORE
；rRECISION DESINED IN Y DIRECTIDiN．KEEP T］A PUNEK DF TNU．jI？．1024，
＊＊）48
PUIMPI：$Z$ ：POLYGON TU WHICH THIS EDGE BELUNGS
FLAGS＝7 ：［HE FULLONING THIRTEEN FLAGS WILL BE SIORED IN AC7
AL＝400000 ：CUUNTER FUR TOP LEFT CORNER
$4 R=200000$ CUUNTEK FOR TJP RIGHI CORNER
$3 L=100000 \quad$ CJUNTER FJR BOTFUM LEF［ CJRNER
$3 K=40000 \quad$ CUUNTER FOR BJTROM RIGHT CORNER
$千 U=20000$ ：CUUN＾ER FOR TOP WINDDW
$\mathrm{HD}=10000 \quad$ COUNTER FOR BJTLO：WINJOH
$\dashv \mathrm{L}=4000$ ；CJUNTER FOR LEFT NINDJN
t $\mathrm{H}=2000$ ：CJUNTER FUR RIGHT WINDON
$X \Gamma=1000$ ；POLYGUN PASSES UN THE RIGHT OF ORIGIN
$Y V=400$ ；PJLYGON PASSES ON TUP DF JKIGIN
$\angle N=200$ ；PiJLYGON PASSES IN FRONT OF ORIGIN
$1 D H U=100$ HULDU．OR．HULDD
© $X F=40 \quad ; C X=0$ IS TRUE FLAG
$\therefore x=C L I P 2 \quad$ ；$X$ COEFFICIENT OF PLANAR EOUAIIDiv
CY＝CLIP2＋I $\quad$ Y COEFFICIENT OF PLANAR EOUATION
$\because \angle=C L I P 2+2 \quad ; 2$ COEFFICIENT OF PLANAR EQUATIUN
$20=$ CLIP $2+3$ ；CJNSTANT IN PLANAR EJUATIDN
CULJK＝CLIP2＋4；COLOR OF POLYGON
1 RHIORIIY＝CLIP2＋5 ：PRIURITY OF POLYOON（0－15）
HII $=$ CLIPH +3 INTENSITY COMPONENT
$X P[1=C L I+3$ ：$X$ BEGIN
Y ن「1＝CLIP3＋1 ：Y BEGIN
－ $\mathrm{P} \Gamma 1=$ CLIP $3+2$ ： 2 BEGIN
NPII＝CLIP 3＋3 INTENSITY BEGIN
$X P[2=C L I P 3+4$ ；$X$ END
YPI2 $=$ CLIP3＋5 $\quad$ Y END
ZP「2＝CLIP3＋6 ：Z END
$\because+2=$ CLIP3＋7 INTENSITY END
LASEDG $=$ CLIP3＋10 ：LAST EDGE FLAG
रR：$Z$ ：$X$ RESOLUTION
YR：Z ：Y RESOLUTION
ZUCKY＝SCUPE $\quad$ Y BUCKET SORT ARRAY
HJJCKY＝SCOPE＋YRESOLUTIDN ：HORIZUNTAL EDGE BUCKEI SJRT ARRAY
VX：3LJCK 10 ： 10 VEriIICE ARRAY
VY：BLUCK 10 ：Y VERIICE ARRAY
VZ：BLJCK 10 ：Z VERTICE ARRAY
$Y X=3$ ：IVDEX PJIVTER FOR BEGIN PUINI
$Y B=5 \quad: D[\Gamma[J$
Y $L=4$ ：IVDEX PUINTER FOR END PJINI
YE＝6 ：DITID
［ESPX：$Z$ REGISTER FOK CLIPPED $X$
［EIPY：$Z$ REGISTER FOR CLIPPED Y
［FAPZ：$Z$ ：REGISTER FOR CLIPPED $Z$
；ALL ARITYMETIC IS PERFORMED IN ACO，ACI，AC2
：AC7－17 ARE NU［ T］BE［OUCHED SINCE THEY ARE USEO IN THE CALLER ${ }^{\wedge} \mathrm{L}$

INTCLP is responsible for initializing the appropriate flags for hidden surface processing. $X R$ and $Y R$ are used in perspective scaling transformations. BUCKY and HBUCKY have to be filled with ones prior to each new frame.


EXIERN EYES,INTENS
LISTMD=EYES+1
I IENHI=INTENS :INTENSITY PASSED TU ALGOKIIHM
I TENLJ=INTENS+1 I INTENSITY PASSED TO ALGORITHM
BACKG=INTENS+? BACKGRUUND PEHCENTAUE
IFXI: 1000 RESOLUTION IN $X$
IFYI: YRESJLUTION :RESULUTIDIV IN Y
IBACK=EYES+3 BACKGROUND INTEN JSED BY PRJGKAM
IENHIH=EYEj+4 BHI INTEN USED BY PROGRAM
IENLOM=EYES+ら :LU INTEN USED BY PROGRAM
$I X=E Y E S+6$ : $X$ RESULUTIDIV USED BY HIDDEN
I $Y=E Y E S+7$; $Y$ RESOLUTION USED BY HIDDEN
LISISI=FREE+3 :ADDRESS DF FIRST EDGE BLDCK
IdTCLP: $Z$
MOVE gO(16)
MOVEM PICTURE\#
SEIOM POLYPT :CLEAR PJLYGON POINTER
SETIJM LISTST ICLEAR LISI START ADDRESS
SEIZM LISTMD :CLEAR LISI kade up FLAG
MOVE I,IFYI
CLRBUK: SETJ: BUCKY-I (1)
SETJM HBUCKY-I(1)
sOJg I.CLRBUK
FIXRES: MOVE IFXI
SOJ
MJVEM IX IIX_IFXI-I
ASH 10
MOVE XR :XR_IX*256
MOVE IFYI
$\begin{array}{lll}\text { ASH } & -1 & \\ \text { MOVEM } & \text { YR } & \text { YR_IFYI/2 }\end{array}$
MOVE IFYI
SOJ
MJVEM IY :IY_[FYI-1
MJVEI YKESOLUTION :GET IT
AS' - 11
AUJ 0,0
MUVNS 0.0

ASH -7
HRYM DRAN2
MOVE INTENS+4 :GET Y SCREEN SIZE
ASH -7
HRKM DRAW3
JKA 16,(16)

## POLMAK

POLMAK clears the clipping flags and increments the polygon count. These macros perform some simple algebraic manipulations. The $Y$ intersection is basically: TEMPY=ALPHA*DY+VY in the case of clipping to the plane $z=Y$. The $X$ intersection is: TEMPX=ALPHA*DX+VX in the case of clipping to the plane $\mathrm{Z}=\mathrm{Y}$.

```
PJLMAK: Z
    AUS POLYPT
    SETZM FLGLOC# ; CLEAR CLIPPING FLAGS
    JRA 10.(16)
    IEFINE JIFFER (A,B,C) :A_B-C
    <NJVE 3
    SUB C
    MOVEM A>
    DEFINE TIXURT2 (A) {PERFOR'AS [I.XOK.[2
    <VJVE TI
    XDR T2
    JUMPGE A> {JUMP IF EDGE DID NOT CROSS
    DEFINE CLIPPER (DELI,TMP1, BEO1,DEL2,IMP2,3EG2,C)
    <JSR ALPHA :GET THE ALPHA
    INCSCT DELI,TMPI,3EGI
    MOV'S 1,TEMPZ
    INTSCT DEL2,TMP2,3EG2>
    DEFINE INTSCT (DELTA,LOC,BEGIN)
    <NIDVE 1,DELTA
    MUL 1.0
    ASHC 1.1
    ADJ 1,BEGIN
    MOVEM I.LOC> :LOC=DELTA*ALPHA+BEGIN
ALPHA: Z iTHIS SUBRJU[INE CALCULATES ALPHA
    MOVE 2.TI
    SU3 2.52
    MOVE TI
    SECZ 1.
    ASHC 0,-1
    DIV O.?
    JRGT gALPHA :ALPHA=TI/(TI-T2)
    DEFINE SUM (A,B,C) A_B+C
    <MJVE B
    ADO C
    MOVEM A>

SLOPE evaluates the expression: SLO=(BEGVALUE-ENDVALUE)/DELTAY. BEGPNT evaluates the expression: BEG=STARTVALUE+SLOPE/2. CORNER is responsible to evaluate the \(X, Y\), and \(Z\) value at a corner when a polygon wraps around said point. The planar equations are used in this case. \(V X=C D /(C X-C Y-C Z)\) where \(-X=Z=Y\). Consequently, \(V Y=-V X\) and \(V Z=-V X\).


PERSP performs the perspective transformation. The equation is: PERS = (VAL*RES)/ZVAL+RES where VAL may be either \(X\) or \(Y\). RES was calculated inside INTCLP. Note that if the user specified the \(X\) resolution to be 1024, the RES would be 512*511. Consequently, the use of double precision arithmetic was used so that the user could provide \(X\) and \(Y\) values up to 2**35-1.

ZINVRS performs a 1/Z operation, where 1 is essentially 2**30-1.

DEFINE DUBSTR (A,B)
<MOVEM I, V'A+B :STORE ENDPJINT INTU NORKING REGISTER MOVEM \(\quad 1, V^{\prime} A+B+2>\)
DEFINE STOREZ (A,B)
<MJVE \(1, A\)
DUSSTR Z,3>
DEFINE STORXY (A,B,C)
<MUVE I,A
DURSTR B,C>
DEFINE PERSP (PERS,VAL, HES,ZVAL) :PERSPECTIVE TRANSFORMAIIJN
<MUVE VAL
MUL RES
DIV ZVAL
ADJ HES
MOVEM PERS>
DEFINE ZINVHS (PERS,ZVAL) :INVERSE Z VALUE
<HRLUI 7777
SKIPG I,ZVAL :SKIP IF Z IS STRICTLY POSITIVE
MOVEI 1,1
IDIV 0,1
NOVEM PERS>

\section*{EDGMAK}

The calling program passes the begin point \(X, Y, Z\) and end point X, Y, Z. These numbers are stuffed into working registers called VX, VY, VZ. Locations 1 and 2 of these registers contain the initial values; locations 3 and 4 contain the clipped values; 5 and 6 retain the most recent left or right clipped value; and locations 7 and 8 contain the transformed perspective value.


EDMAK: 2
MUVEM 7.AC7\#
MDVE FLAGS,FLGLOC
- THE FJLL!VING CJDE PLACES THE BEGIN AND END POINTS OF THE
; EJGE INTO NORKING REGISTERS. DX,DY,DZ,DN AKE THE DIFFEPENCES
; JF THE BEOIN AND END POINTS.
STURXY XPTI,X,O
SIDRXY XPT2,X,1
STJRXY YPTI,Y,O
STORXY YPI2,Y,1
STJREZ ZPTI.O
STUREZ ZPT2.I
MOVEI YB,I
MOVEI YE,2
DIFFER DX\#, VX+1,VX
DIFFER DY\#,VY+1,VY
DIFFER DZ\#, VZ+I,VZ
SETZM T3\#
SEIZK T4\#
\({ }^{\wedge}\) L

The TIXORT2 check determines if the edge crosses the plane which is going to be clipped to. CLIPPER evaluates the XYZ coordinate of intersection. T1XORT2 and STUFF now determine if the new clipped point should be stuffed into the begin or end clipped point location ( \(\mathrm{V} *+3,4\) ).

: IHIS PAGE JF CODE PERFORMS THE CLI PPING AT THE FJUR ?LANES
: UF THE CUVE VISIOIV. THE JRDER DF CLIPPING IS \(L=Y, L=-Y, L=X, L=-X\).
DIFFER TI\#,VL,VY
DIFFER T2\#, VZ \(+1, V Y+1\)
T1XJRT2 P23
CLI PPER DY, TEMPY, VY, DX,TEMPX,VX,EM
STJFF P26
P26: MOVN TEMPZ
CAMLE TEMPX
TRS FLAGS,AL
; CJMe ABOVELEF C COUNTER If EDGE Chus
**E0

م23:
MOVM TEYPX
CAMG TEMPZ
TRC FLAGS,HU
: COMP HOLDUP If EDGE CROSjED NINDUN
SUM TI,VZ,VY
SUM T2,VZ V +,\(V Y+1\)
TIXORT2 P38
CLIPPER DY, TEMPY,VY,DX, ГEMPX,VX,NY
SUM \(\quad T 1, V Z+2, V Y+2\)
SUM T2,VZ \(+3, V Y+3\)
TIXDRT2 P36
SIJFF P36
P35: MOVE TEMPZ
CAMGE TEMPX
TKC FLAGS,BR :COMP BLJNRGHT COUNTEG IF EDGE CHJSS
**1)
MOVM TEMPX
CAKO TEXPZ
TRC FLAGS,HO :CJMP:HLDDNN IF EDGE CRJSSD 3JI aIN
\(\star \star\),
r33: DIFFER TI,VZ,VX
DI FFER \([2, V Z+1, V X+1\)
IIXORT2 P48
CLIPPER DX,TEMPX,VX,DY, IEMPY,VY,EM
DIFFER TI,VZ+2,VX+2
1)IFFER T2,VZ+3,VX+3

TIXORT2 446
AiJ T4
STUFF P46
P45: MOVE TEMPZ
CAKS TEMPY
TRC FLAGS,AH :COMP ABUVERIGHI IF EJOE ORJSSED
r43: SUN TI,VX,V
SUA T2, VX+1,VZ+1
[IXORT2 P58
CLIPPER DX,TEMPX,VX,DY,TEMPY,VY,NM
SUM TI,VX+2,VZ+2
SUN T2,VX+3,VZ+3
T1XIRT2 P56
AIS T3
STUFF Pb6
POS: MOVN TEMPZ
CAML TEMPY
TRC FLAGS,BL
:CUMP BELUNLEFT COJITER IF EDGE CRJS
\(\star \star E D\)
~L

Once all the clipping has been performed, a check is made to see if the edge lies within the window. If it does, then additional checks must be made to see if the processed edge crossed either the left or right window boundary. If so, then store the clipped value into either location 4 (right) or 5 (left) of the \(V *\) register. If this is an even time that an edge has crossed a boundary, then generate a new edge at the boundary.

```

rכ3: MOVM VY+2
CAMLE VZ+2
JKST P7j ;JUMP IF CLIPPED EDGE IS UUTSIDE NINDUN
MOVM VX+?
CAMLE VZ+2
JRST P75 :JUMP IF CLIPHED EDGE IS DUTSIDE ,VINDJir
MOVEI YB,3
MOVN VZ+2
CANE VX+2
MOVEI YB,4
MOVE T3
JUMPG P68 ;JUMP IF EDGE CROSSED LEFT II.NDO\#
P54: MOVEI YE,3
MOVE VZ+2
CAME VX+2
MOVEI YE,4
MOVE T4
JUMPG P70 :JUMP IF EDGE CRJSSED RIGHI NINDON
PSK: MOVEI YX,3
MOVEI YZ,4
MOVEI P75
HRRG JUMPER
JHST P90 :GO PRUCESS THIS EDGE
NO%: TRCE FLAGS,HL
JRST P72
TH.NSFR 5,YB
JRST P64
<70: TRCE FLAGS,HR
JRST H74
TRNSFR 6,YE
JRST P66
P12: MOVE YX,YB
MOVEI YZ,5
MOVEI PG4
HRKM JUMPER
JRST HوO
r74: MOVE YX,YE
MOVEI YZ.O
:MOVEI P6O
HRRM JUMPER
JRST P9O
^L

```

If this is the last edge of the polygon, then all the clipping flags must be checked to see if an unclosed polygon currently exists. One of the pieces of information required is the intersection of the polygon with the \(X, Y\), and \(Z\) axis.

The flags are interrogated first to see if any processing need be done on the left side of the window, then similarly for the right side of the boundary.
```

^7j: SKIPL LASEDG ;SKIr Ir IHIS IS THE LASI EDGE DF rulyGDiv
JRST pg% :NJT LAST EDGE
TR:NN FLAGS,AL+RL+AR+BR
J\&ST pg8 iJUMP IF ALL EUGES ARE PROCESSED
TRNE FLAGS,HU+HD
IRJ FLAGS,4DHU :SET IF HU.JR.HD IS T{UE
SKIPN CX
TRJ FLAGS,CXF ;SET IF CX=0 IS TrUE
DEFINE PLivINT (AXIS,FLG)
<MJVE AXIS
XON CD
JUXPGE .+2
IRJ FLAGS,FLG> :SET IF FLAG INTERSECIS JV +AXIS
PLVINT CX,XT
PL.vINT CY,YV
PLNINT CZ,ZN
TRC FLAGS,-1 :COMPLIMENT THE WDRLD
OHOUND RULES FOR IYING UP THE LOOSE ENDS:
;A "|" IMPLIES FALSE
*A "O" IMPLIES TRUE
:TRNN IAPLIES SKIP IF A FALSE
ITONE IMPLIES SKIP IF A [RUE
MUVEI YX,1
MOVSI YZ,2
IR.NE FLAGS,HL
JRST P\&O :JUMP IF NUTHING IO BE DONE DIN [HE LEFI
MOVEI YZ,5
MUVEI P80
HKRM JUMPER
TRNE FLAGS,AL
JKST .+4
IR.JE FLAGS,YV
Trive FLAGS,BL
J.SST P83 :CONVECT TJ TOPLEFT
NOVEI YX,2
JRST P84 :CONNECT TO BOTTOMLEFT
P30: FR.VE FLAGS,HR
JRST P81 :JUMP IF NOTHING TU BE DONE ON THE RIOHT
MOVEI YX,I
MOVEI YZ.G
MOVEI P8I
HRHM JUYPER
THNE FLAGS,AR
JRSI .+4
TRINE FLAGS,YV
IRNE FLAGS,BR
MRST P8K
JHST P88 ;CJNNECT TO BOTTO:KRIUHT
^L

```

The equation which is used to ascertain connect to top and bottom left is:
(.NOT.HL.AND.AL.AND.BL.AND.
(( \(\mathrm{HU} . \mathrm{OR} \cdot \mathrm{HD}\) ).AND. (.NOT.XT.OR. (CXF))) .OR.
(.NOT.(HU.OR.HD).AND.ZN))).

The equation which is used to ascertain connect to top and bottom right is:
(.NOT.HR.AND.AR.AND.BL.AND. (( (HU.OR.HD).AND. (XT.OR.CXF))) .OR. (.NOT. (HU.OR.HD) .AND. ZN) ).



This sets up the code for the appropriate corner calculation.
When the program has arrived at P 90 , the end points of the edge to be processed are held in index locations \(Y X\) and \(Y Z\). Perspective transformation yields 0.LEQ.VX.LEQ.FRAMEX-1 and O.LEQ.VY.LEQ.FRAMEY. The EXCH is performed to insure that \(V *+7\) is the begin point (has the highest \(Y\) value).

HORZED makes up a horizontal edge block for the hidden surface algorithm. This edge is then entered in the HBUCKY list at the appropriate scan line on which it exists. It is also entered on the previous scan line. Following is a picture of the horizontal edge block.
\begin{tabular}{|c|l|}
\hline POLYPT & \begin{tabular}{l} 
NEXT \\
EDGE
\end{tabular} \\
\hline XLEFT & XRIGHT \\
\hline
\end{tabular}
; IJplefr cJr.ver calculation
H33: CORNER O,FSBR,FSBR,NM,NM
CAIN YZ. 5
JRST P90
:3JTTOMLFF[ CORNER CALCULATION
P84: CORNER 1,FADR,FSBR,EM,NM
JRST P 90
: IJPRIGHT CORNER CALCULATIDN
-SO: CORNER O,FADR,FADR,EM,EM
CAIN YZ,6
JRST P90
; BOTIOMRIGHT CORNER CALCULATION
P83: CORNER 1,FSBR,FADR,N:K,EM
P90: PERSP \(V X+6, V X-I(Y X), X R, V Z-1(Y X)\)
PERSP \(\quad V X+7, V X-I(Y Z), X R, V Z-I(Y Z)\)
PERSP \(\quad V Y+\sigma, V Y-I(Y X), Y R, V Z-1(Y X)\)
PERSP \(\quad V Y+1, V Y-I(Y Z), Y R, V Z-I(Y Z)\)
MOVE O.PICTURE
JUMPL O,LINMOD :JUMP IF VECTOR MODE IS SET
ZINVRS \(V Z+5, V Z-I(Y X)\)
ZINVRS VZ+7,VZ-I(YZ)
MOVEI \(Y X, 6\)
MOVEI YZ. 7
MOVE \(\quad V Y+6\)
CAML \(\quad V Y+7\)
EXCH YX,YZ
P94: MOVE 2.VY(YX)
SUB 2,VY(YZ)
JUMPE 2,HORZED :JUMP IF HORIZIJNTAL EDGE
MOVEM 2.DELTAY\# :DELTAY_VY(YX)-VY(YZ)
SLJBEG \(V X(Y Z), I X B E G \#, I X S L \#, V X(Y X)\)
SLOBEG VZ(YZ),IZBEG\#,IZSL\#,VZ(YX)
MOVE IPRIORITY
ASH 6
ADDM IZBEG :ADD PHIJRITY TD Z BEGI^
JRST PACK
HURZED: MOVEI 2,2
JSA 16.GETVAK
JUMP 2 RETURN POINTER IN AC2
JUMP 2 GET A BLOCK OF SIZE 2
MOVE O,POLYPT :GET PIJLYGON PJINTER
HRLM O,FREE-1(2) :STORE IT
MOVE \(0, V X(Y X)\) GET \(X\)
MOVE I,VX(YZ) :GET X
CAML 0,1 INSURE XLEFI IS IN ACO ANO
EXCH 0,1 :XRIGHT IS IN ACl
ASH \(0,-11\) :DROP FRACTIONAL BITS
ASH 1.-11 :DITIO
HRLM O,FREE(2) :STJRE XL
HRRM I,FREE(2) :STIRE XR
MOVE I,VY(YX) :GET SCAN LINE
JUMPE I.JUMPER :DON'T DO IT IF SCAN LINE O
HRAE O.HBUCKY-I(1) :GET NEXT POINIER
HRRM 2.HBUCKY-I(1) :CURRENT LINE
HRLM 2.HBUCKY(1) :PHEVIOUS LINE
HRRM O,FREE-I(2) :STURE NEXT PUINTER

PACK

PACK obtains a four word block from free storage. It then takes all the describing information of this edge and packs it into the four words according to the drawing below.

EDGEPT


The bucket list is updated so that the edge is entered at the appropriate scan line location.

```

PACK: MOVEI 2,4
JSA 16.GETVAR
JUMP 3
JUMP 2
MOVE IXBEG
HRL IXSL :XSLJPE GOES IN TJPHALF
MOVEM FREE-1(3)
MOVE I.IZSL
LSH 1.6 :PUSH TO TJP OF WURD
MOVE PDLYPT
LSHC -6 :PUT LOW ORDER PULYPT IN TOP JF ACI
MOVEM 1,FREE(3)
MOVE I.IZBEG
LSH 1.0 ;PUSH TO TOP OF NORD
LSHC -6 :PUT HIGH ORDER POLYPT IN IOP OF ACI
MOVEM 1,FREE+1(3)
MOVE DELTAY
MOVE 4,VY(YZ) {GET Y
HRL O,3UCKY-1(4) :GET NEXT EDGE POINTER
MOVEM 3,BUCKY-1(4)
MOVEM O,FREE+2(3)
JUYPER: JRST O
P93: MOVEM FLAGS,FLGLOC :SAVE FLAGS
MOVE 7.AC7
SETZM VZ+6
JRA 16.0(16)
LINMDD: MOVE 2.VX+6
ASH 2.11
JSA 16.DRANM
JUMP 2
JUMP VY+6
MOVE 2,VX+7
AS4 2.11
JSA 16.DRANV
JUMP 2
JUMP VY+7
JRSI JUMPER

```

\section*{cross}

\begin{abstract}
CROSS has the responsibility to see if two edges that are visible on a scan line cross on the next scan line. This subroutine will then determine the X point of intersection and draw the edge which is no longer visible. If everything seems to be in order, a flag is set in the segment block stating that the edge is visible on this scan line.
\end{abstract}

EXIERNAL FREE, MOVETO, VECTO, INTENS, CLPPER
INIERNAL DRAN,DRAWA,DRANV,SEILIN,CNOSS
EXIERNAL OLDEDG
OLDXI=JLDEDG
\(J\) LDX \(2=\) JLDEDG +1
OLDSEG=OLDEDG +2
CRUSS: \(Z\)
mOVE
ADJ TRZ MOVE
ADD MOVE TRZ IOR MOVEM MOVE MOVE A DD MOVE MOVEM CAML JRST
CAIE
JRST
HLRE
SKIPA
a CHECK TO SEE IF EDGES CRJSS
2, 3 (16) GET IY
2.
2.777770 :ONLY ivEED LUN BITS

1,92(16)
1.CLPPER+12

FREE-I(1) BGET THE SETLIN
7
2
FREE-1(1)
:MASK IY+I INTO NDRD
1. 中1 (16)
2.1
1. CLPPER +12

3,FREE-1(1) :GET CURRENT \(X\)
3, \(V \mathrm{X}+6\)
3.JLDXI if JLDXI IN FRONT?

CRSXIT
2. 3

CRSRGT : MUST BE RIGHT EDGE
FREE-2(1) \&GET YLEFI

When the program is at this point, everything is guaranteed that the two edges do, in fact, cross. The \(Z\) value for both of the edges must be calculated for the two edges at the point of crossing to determine which edge will be drawn. The edge with the smallest \(Z\) value will be drawn.

\begin{tabular}{|c|c|c|}
\hline -2SROT: & HRRE & FREE-4(1) :GET YRIOHI \\
\hline & JURPE & CRSXIT ; JUMP IF EOGE EXITED \\
\hline & move & 5.90(16) GGET PREVIJUS \(x\) \\
\hline & move & 6,5 \\
\hline & SUB & 6, 12DX2 \\
\hline & SUB & 5,3 \\
\hline & SU3 & 5,3LDX2 \\
\hline & ADI & 5, ULDX1 \\
\hline & DIV & 6,5 ; AC6_(NENX2-NENXI)/(OLDX1-JLUX2-NEWX1+iNENXく) \\
\hline & ASH & 6,-21 :GET DELTA \\
\hline & MOVE & OLDXI \\
\hline & SU3 & OLDX2 \\
\hline & MUL & 0,6 \\
\hline & ASHC & 0,21 \\
\hline & ADD & OLDX2 :GET X PUINT AT CROSSING \\
\hline & HLRZ & 1, JLDSEG \\
\hline & ADD & 1, OLDSEG \\
\hline & MOVE & 2,FREE+4(1) ;GET ZSLOpE FJR OLJEDJE \\
\hline & MUL & 2,6 \\
\hline & AStC & 2,21 \\
\hline & MOVE & 3,FREE+3(1) 3GET Z FOR OLDEUGE \\
\hline & SUB & 3,2 GET 2 A CROSSING FOR OLDEDGE \\
\hline & MOVE & 1, \%1(16) \\
\hline & AD & 1,CLPPER+12 \\
\hline & move & 4,FREE+4(1) GET ZSLOPE FOR CURRENT ETGE \\
\hline & MUL & 4.6 \\
\hline & ASHC & 4,21 \\
\hline & move & 2,FREE+3(1) :GET Z FOR CURREINT EDGE \\
\hline & SU3 & 2,4 GET 2 AI CHOSSING FOR CURRENI EJ JE \\
\hline & CAMG & 2,3 \\
\hline & JRST & CRSCUR DRAN CURRENT EDGE \\
\hline & HLRZ & 7, JLDSEG \\
\hline & CAIE & 7,3 \\
\hline & SOJ & 7. \\
\hline & ADD & 7,OLDSEG :GET ADDRESS FOR OLDE GEE \\
\hline & JRST & DrivCRS-2 \\
\hline CRSCUR: & MOVE & 7,91(16) \\
\hline & CAIE & 7,3 \\
\hline & SOJ & 7. \\
\hline & AD) & 7,CLPPER+12 GE[ A 12 doress fur Curhen e edge \\
\hline & HRRZ & 4,FREE+7(7) \\
\hline & JUAPE & 4,CRSXIT-1 JUMP IF ALGEADY DRANN \\
\hline
\end{tabular}

DRAW

DRWCRS gets the \(X\) and \(Y\) point of intersection for drawing purposes. A YOFFSET value must be calculated since the intersection occurred between scan lines. The end point of the edge is extracted from the segment block and the line is completely drawn.

Subroutine DRAW has the responsibility to draw the line for an edge which has exited or was completely visible on the previous scan line. Note that half of the slope is added so that the line will be defined as existing between scan lines.


DRAWM - DRAWV - SETLIN

DRAWM and DRAWV expect the \(X\) value to be of the form ( \(N, M\) ), where \(N\) is the integer part and \(M\) is the fractional part. This results in no loss in precision while scaling and drawing the line. The \(Y\) value is right justified in the word. DRAW4 makes certain that the line will not go outside of the specified window vłewing area. SETLIN is called when the hidden surface algorithm determines that the edge of a segment is visible for the first time. This subroutine will store the begin point of the edge for future reference when the line will be actually drawn. Note that half of the slope is subtracted so that the line actually begins between scan lines.

```

OUTSTR - LDLPT - LDRPT -
STLPT - STRPT - LOD2HF -
STR2HF - MYMAXO - MYMINO

```

OUTSTR will output a string of text on the teletype using a TTCALL. This was implemented to avoid difficulty between FORTRAN I/O and SAIL I/O.

LDLPT, LDRPT, STLPT, and STRPT all perform half word transfers. Note that the loading routines do a sign extend.

LOD2HF and STR2HF expect the arguments to be located at some address inside the array free. Note that LOD 2 HF expects the arguments to be at the address plus two. The reason is that the majority of the loads come from this address.

MYMAXO and MYMINO are similar to the FORTRAN functions, except that these functions work on two arguments.

TITLE U[ILITY ROUTINES FUR HIDDEN SURFACE PROCESSING

I NIERNAL UNPACK, XIITER, ZVALUE
EXIERNAL FREE, CLPPER
DUTSTR: 2 iTYPE DUT A VESSAGE
TTCALL 3,20(16)
JHA 16,1(16)
LDLPT: 0 LJAD LEFT HALF OF ARG2 INTU ARGI
HLRE \(0.1(16)\)
MOVEM O.EO (16)
JRA 16.2(16)
LURPT: 0 LOAD RIGHT HALF OF ARG? INTJ ARGI
HKRE O.OI(16)
YCVEM 0, GO (16)
JRA 16,2(16)
LOJ2HF: Z GET LEFT AND RIOHT HALF JF 3RD LUC OF FRGE RLUCK
MOVE 1.7O(16)
HLRE O,FREE+I(1)
MOVEM 0.11(16)
HRRE O,FREE+I(1)
MOVE O, 0 , 2(16)
JRA 16.3(16)
AYMAXO: \(Z\) iMAX VALUE \(G F 2\) ARGS
MOVE \(Q(16)\) GET IS I ARS
CA:GGE Q1(16) iSKIP IF .GE. TO 2VD ARG
MOVE Ql(16) ; 2ND ARG WINS
JRA 16,2(16)
AYIINO: Z iMIN VALUE UF 2 args
:MOVE G(16) :GET IST AKG
CAMLE \(\quad 1(16)\) ISKIF IF .LE. TO 2ND ARG
MOVE :I (16) ; 2ND ARG NIINS
JRA \(16,2(16)\)
STLPT: 0 :STORE ARGI INTD LEFT HALF DF ARG?
MOVE 0. DO(16)
HRLM \(0,01(16)\)
JRA 16,2(16)
S「YPT: 0 STDRE ARGI INTO RIGHT HALF OF ARG?
MOVE O,QO(16)
HRRM \(0,01(16)\)
JRA 16,2(16)
STR2HF: Z Z STORE ARG2 AND ARG3 INTJ LEF[ AND RI:HH LOCS JF F:
**-1 (ARG1)
MOVE 1,00(16)
MOVE 2.01(16)
HKLM 2,FKEE-1(1) .
MOVE 2.O2(16)
HRAM 2,FREE-1(1)
JRA 16.3(16)

UNPACK

UNPACK extracts the data from the four word edge block created by EDGMAK and places the answers in specific locations in common area EDGARG.


\section*{XINTER}

When the hidden surface algorithm has determined that two potentially visible segments are intersecting, XINTER will evaluate the X value. A subroutine was used for this purpose, since the arithmetic resulted in numbers containing 50 bits and thus created the need for using fractional operators.
```

IAL=CLPPER ;Z LEFT OF LINE A
\angleAK=CLPPER+1
CL=CLPPER+2
ZCR=CLPPER+3
ZCR=CLPPER+3
XRIGHT=CLPPER+5 ; X VALUE JF NEN LINE A
XLEFT=CLPPER+5 ; X VALUE OF NEN LINE A
ZRIGHT=CLPPER+7 ; Z VALUE OF NEN LINE A
ZLEFT=CLPPEP+10;Z VALUE OF NEN LINE A
XKCLIP=CLPPER+|! :X RIGHT OF POINT BEING CLIPPED 门
ZS=CLPPER+12 :PHEVIOUS LINE C (SEGPT,XL,XR,ZL,ZR)
XAYXL=CLPPER+17 ;PIJINT OF INTERSECIION DF LINE A AND:
: *** Z NUMBERS ARE 30 BITS, X NUMBEHS ARE 20 3ITS
XINTER: Z ;THIS ROUTINE COMPUTES THE INTENSECTIJN UF A AND C
MOVE 2,ZCL
SU3 2,ZAL
SUR 2,ZCH
AD: 2,ZAR
MOVE O,ZAR
SU3 O,ZCR
MUL 0,XLCLIP
DIV 0,2
MOVE 4,ZAL
SU3 4,ZCL
MUL 4,XRCLIP
DIV 4,2
SUR 0,4
CAMGE XLCLIP : IS XINTERSECTION LESS THAN XLCLIP?
YOVE XLCLIP IYES
CA:{LE XRCLIP IIS XINTERSECIIJN GREAIER [HA\ XRCLIP?
MOVE XRCLIP
MOVEM O,XAMXL
; XAMXL=(XLCLIP*(ZAR-ZCR)-XRCLIP*(ZAL-ZCL))/(ZCL-ZAL-ZCR+ZAR)
JKA 16,(16)
^L

```

\section*{ZVALUE}

Subroutine ZVALUE performs the arithmetic formally described as the clipper in the Watkins' Algorithm. Given a \(x\) left clip point and a \(X\) right clip point, this routine evaluates the \(Z\) values for two segments. This information is passed back to the hidden surface algorithm for comparison.

```

ZVALJE: 2 :THIS ROUTINE CUMPUIES ZAL, ZAR.ZCL, ZCX
MJVE O.ZLLFT
SU3 0,ZRIGHT
MOVE 2,XLCLIP
SUB 2,XHIGHT
MOVE 4,XLEFT
SUB 4, XhighT
MUL 2.0
DIV 2.4
AD) 2,ZRIGHT
HDVET 2,ZAL
; $2 A L=((X L C L I P-X K I G H T) *(Z L E F T-Z R I G H T)) /(X L E F T-X R I G H \Gamma)+\angle R I G I T$
MOVE 2,XHCLIP
SU3 2,XRIGHT
MUL 2.0
DIV 2.4
ADD 2,ZRIGHT
YOVE! 2,ZAR
: $2 A R=(($ XHCLIP-XRIGHT)*(ZLEFT-ZRIOHT))/(XLEFI-XRIGGT) $+\angle R I G 4 T$
move 0.25+3
SUB $0,2 S+4$
MOVE 2.XLCLIP
SU3 2.25+2
MOVE $4,25+1$
SU3 4, 2S+2
MUL 2,0
DIV 2,4
AD. $\quad 2,2 S+4$
MOVEN 2,2CL
: ZCL=((XLCLIP-ZS(3))*(ZS(4)-ZS(5)))/(ZS(2)-25(3))+2S(j)
MOVE 2,XHCLIP
SUB 2,2s+2
MUL 2,0
DIV 2,4
AD) $\quad 2,2 S+4$
MOVEM 2,2CR
:ZCK=(XRCLIP-ZS(3))*(ZS(4)-ZS(5)))/(ZS(2)-Z.S(3))+ZS(5)
JRA 16,(16)
ENJ

```
```

INFREE - GETVAR - LSTSET -
GETBLK - RETBLK

```

INFREE initializes the FREE array. The first argument is the number of locations which must be zeroed - four is the minimum. The second argument is the length of the free array. This value should be the same as the dimension of FREE in the user's program.

GETVAR gets a variable sized block from the array FREE. The first argument is returned to the user and is the index into the FREE array. The second argument is supplied by the user and is the length of the block that is desired.

LSTSET is used by the hidden surface algorithm. The remaining area inside FREE is broken into blocks of size N. These blocks are used as segment storage areas and are linked together.

GETBLK returns to the hidden surface algorithm a block of size N for storing of segment data.

RETBLK returns to free storage a block of segment data. This block is then available for future use.

SUBROUTINE IVFRFE(I LENGFH)
COMUON/CORE/FREEST, LEN,FREEPT/FREE/FREE(1)
IMPLICI I INTEGER (A-Z)
IF(I.LE.O)GOTD 2
DU \(1 K=1,1\)
FHEE(K) \(=0\)
LEN=LEIVGTH
FREESI=1+I
RETURN
E(v)
SUBrUUTINE GETVAR(INDEX,LENGIH)
COMMON/CURE/FREEST, LEN,FREEPT
IMPLICIL INTEGER (A-Z)
INJEX=FREEST
FKEEST=FREEST+LENGTH
IF(FREEST.LT.LEN)RETURN
CALL DJSSTR('MAX STDRAGE')
CALL EXIT
END
SUBRUUTINE LSISET(N)

IMPLICIT INTEGER (A-Z)
FAEEPT=0
\(K=L E N-V+1\)
IF (K.LI.FREEST)RETURiN
FHFEPT=FHEEST
DO 1 I=FHEEST,K,N
\(A=1\)
FhEE (I) \(=\mathrm{I}+\mathrm{N}\)
\(\mathrm{FH}_{\mathrm{H}}=E(\mathrm{M})=0\)
HETURN
EN)
SU'3RUUTINE GETBLK (INDEX)
COMYON/CORE/FREEST, LEN,FREFHT/FRFE/FREE(I)
IMPLICI「 INTEGER (A-Z)
IF(FKEERT.EO.O)GD TO
I. \(\mathrm{VDEX}=\mathrm{FAEEPT}\)

FRECPT=FREE(FREFPT)
RETURN
CALL DJISTR('MAX SIURAGE')
CALL EXIT
ENO
SU3RJUTINE RETBLK (INDEX)
COMMON/CDRE/FREEST, LEN,FREEPT/FREE/FREE(I)
I:\{PLICII INTEGER (A-Z)
FREE (INDEX) =FREEPT
FRSEFT = INDEX
RE TURN
ENJ

\section*{HIDDEN}

Following is a description of the code used in solving the hidden surface problem. No attempt is going to be made to explain the reasons or theory behind the algorithm. If the reader is really curious, it is suggested he look into the references at the end of this report.

By the time HIDDEN is called, all the edges should have been clipped and stored into the FREE array. In addition to this, they should have been sorted in \(Y\) and entered into the bucket array. The initialization procedure consists of setting IY=FRAMEY and setting up the size of the segment blocks by calling LSTSET. At the beginning of each scan line, the program jumps to label 204 to get the first edge entering on the scan line. Label 210 is the location where the program keeps looping to pick up all edges entering on the current scan line.
```

    SUZROUTINE HIDDEN
    COMMON/SCOPE/BUCKY(0/2ちら),HBUCKY(256),BB
    COMMON/CLPPER/ZAL,ZAR,ZCL,ZCR,XLCLIP,XRIGHI,XLEFT,ZRIOHI
    1,ZLEFT,XRCLIP,ZS(5),XAMXR
    COMMON/EDGARG/EDGEPT,POLYPT,DELY,XSLOPE,ZSLUPE
    COMMON/FREE/EDGE(I)
    COMMON/EYES/O1(6),FRAMEX,FRAMEY
    CJMMDIN/JLDEDG/JLDX1,JLDX2,OLDSEG
    IMPLICII INTEGER (A-Z)
    DIMENSIJN SEG(1),SAM(4)
    EOUIVALENCE (EDGE,SEG)
    C INITIALIZAIION.
I Y=FRA*NEY
CALL LSISE[(13)
SEGXST=0
204 EDGEP\Gamma=BUCKY(IY)
210 IF(EDGEPT) GO TO 242
CALL UNPACK
O SET PIINIER [J FIRST OF SEG LIST
SEGPT=SEGXST
rREV=0
SPLIT=.FALSE.
^L

```

A block is retrieved from free storage and the edge information is stored into the segment as the left edge. The segment list is searched to see where the new segment block should be entered with respect to X . At times, a current segment block must be split into two segments, since the entering segment must be placed between the two edges.

Label 242 is where the scan line count is decremented and the scan processing begins. The XIEFT sample point (SAM(2)) is set to zero and the XRIGHT sample point (SAM(1)) is set to 1024.
```

` STJKE EDGE DAIA IN SEG BLOCK
CALL GETALK(I)
SEG(I+2)=DELY*262144
SEG(I+I)=PJLYPT
SEO(I+3)=XLEFT
SEG(I+4)=XSLOPE
SEG(I+8)=2SLOPE
SEG(I+7)=ZLEFT
SEG(I+11)=0
C SO SEAHCH X SURT LIST TO SEE WHERE NEN EDJGE WILL GO
214 JF(SEGPT.EQ.O)GO TO 226
CALL LJD2HF(SEGPT,YENDI,YEND2)
TEI =XLEFT-SEG(SEGPT+3)
TE2=XLEFT-SEG(SEGPT+ら)
IF(POLYPT.NE.(SEG(SEGP[+1).AND..NOT.262143))OJ [O 220
IF(YENDI.GE.O)GO TO 221
C SEE IF EXISTING SEGMENT MUST BE SPLIT FOR NEN EDGE
IF(TEI.LT.O)GO TO 226
IF(YENO2.GE.O.OR.TE2.GE.O.OR.SPLIT) GO TO 219
C LOAD \&IGHT EDGE OF SEGMENT INTU NEN BLOCK
SPLIT=.TRUE.
SEG(I+5)=SEG(SEGPT+5)
SEG(I+
SEG(I +9)=SEG(SEGPT+9)
SEG(I+1))=SEG(SEGPT +10)
SEG(I+12)=SEG(SEGP\Gamma+12)
CALL SIRPT(YEND2,SEG(I+2))
CALL STRPT(0,SEG(SEGPT+2))
219 PREV=SEGPT
C SEI PJINTER IO NEXT SEGMENT BLOCK
CALL LDRPT(SEGPT,SEG(SEGPT))
GO ru 214
220 IF(YENDI.GE.O)GO TO 22I
IF(TE1)226,219,219
<21 IF(YEND2.GE.O):30 TO 219
IF(TE2)226,219,219
225 SEG(I)=SEGPT
O [NSERT THIS NEW SEGMENT BLJCK 3ETWEEN EXISTIN SEGMENTS
IF(PREV.NE.O)SEG(PREV)=I
IF(PREV.EQ.O)SEGXST=I
GO TU 210
C .JEChEmENT SCAN LINE CUUNI
242 I Y=IY-I
INTSC[=.FALSE.
OLDXI=0
SEGS2=0
SE SL2=0
SAM(2)=0
SEJACT=0
C JET ivEXT LEFT SAMPLE POINT
231 SAM(1)=SAM(2)+1024
ZS(1)=0
FRJM=0
SEGPT=SEGACT
SEGACT=0
EXIEND=.TRUE.

```

\section*{55}

Due to edges entering and exiting, the X sort segment list must be updated so that all edges are linked together as segments belonging to polygons. This is one of the critical areas in the algorithm, since a great deal of time could be consumed in re-sorting the list. However, it turns out that an extremely small percent of the time is spent here, since a picture changes very little between scan lines.


\section*{57}

This page of code performs the updating of the segments. Since each segment contains the slope information for both the left and right edge, this data is added to the current values of \(X\) and \(Z, g i v i n g\) the new \(X\) and \(Z\) for the next scan line.
```

30j XLEFI=SEG(SEGPT+3)
XRIGHT=SEG(SEGPT+5)
IF((.NOT.EXTEND.OK.ZS(1).NE.O).AND.XLEFT.OE.SAM(2))UJ [O }34
FR.JM=-1
CAIL LDRPT(SEGXST,SEO(SEGPT))
ZLEFI=SEG(SEGPT+7)
ZHISHT=SEG(SEGPT+9)
C JPDALE XLEFT,XRIGHT,ZLEFT,ZRIGHT
SEG(5EGPT+3)=SEG(SEGP[+3)+SEG(SEGP[+4)
SET(SEGPi+ j)=SEG(SEGP \Gamma+5)+SEG(SEGPT+6)
SEG(SFGPT+7)=SEG(SEGPT+7)+SEG(SEGPT+8)
SET(SEGPT+9)=SEG(SEGPT+9)+SEG(SEGPT+10)
INI=0
C JpDATE YLEFT AND YRIGHT SCAN LINE COUNT
CALL LUD2HF(SEGPT, YENDI, YENID2)
YENDI =YENDI + I
YEND2=YEND2+1
CALL ST_2HF(SEGPT+2,YENDI,YEND2)
C BACK POINTERS NEEDED UN NEN LIST.
30Y1 IX=SEG(SEGr:+3)
IF(YENDI.GE.O)IX=SEG(SEGPT+う)
S2=0
SI=SEGL2
3092 IF(SI.EO.O)GO TO 3094
IXI=SEG(SI+3)
IF(SEG(SI+2).GE.O)IXI=SEG(S1+5)
IF(IX.GE.IXI)GO TO 3094
S2=S1
CALL LDLPT(SI,SEG(SI))
GO TU 3092
IF(S2.NE.O)SEG(SEGPT)=S2
CALL STLPT(SI.SEG(SEGPT))
IF(S2.NE.O)CALL STLPT(SEGPT,SEG(S2))
IF(S2.EO.0)SEGL2=SEGPT
IF(SI.NE.O)CALL STRPT(SEGPT.SEG(SI))
IF(SI.EO.O)SEGS2=SEGPT
312 IF(XRIGHT.LE.SAM(1))GJ TJ 345
~L

```

When the program has reached this point, it is ready to perform the depth processing on two segments to see which is visible for a span. The \(z\) values for the two segments are evaluated at the \(X\) left clip point and the X right clip point. The program calls zVALUE to obtain this information. If an intersection is determined, then XINTER is called to evaluate the point of crossing.
```

3lכ CON[INUE
C ADIIIIUN TIME ONE.
INISCT=.FALSE.
ABLLE=S4M(1).GE.XLEF [
A 3RLT=XKIGHT.LT.SAM(2)
C UET X LEFT CLIP POINT
XLCLIP=SAM(1)
IF(.NOT.ABLLE)XLCLIP=XLEFT
\therefore GET X KIOHI CLIP POINT
XRCLIP=SAM(2)
IF(ABRLI)XHCLIP=XRIGHT
JO30X=.FALSE.
J3OXES=.TRUE.
IF((ZS(I).EO.O).AND..NOT.ABLLE)GJ [O 335
JB]XES=.FALSE.
IF((ZS(I).EQ.O).AND.ABLLE)GU TU 3311
323 CONTINUE
GE[Z VALUES FOK NEN AND OLD LINES AT CLIr POINTS
CALL ZVALUE
ABBCKL=2CL.GE.ZAL
A BBCKR=ZCR.GE.ZAR
JO30X=A 33CKL. AND. ABBCKR
O JUYR IF 43 BACK DIN LEFT AND RIGHT
IF(JOBOX)GU TO 335
JIBDX=ABLLE.AND..NJI.ABBCKL.AND..NOT.ABBCK:R
C JUMP IF AB NJF BACK ON LEFI AND RIGHT
IF(J|BUX)GJ TO 331I
JINTER=(ABBCKL.AND. .NOT.ABBCKR).DR.(.NOT.A3BCKL.AND.A 33CKR.AN
**`.     |A3LLE) ` JUMP IF [HE TND SURFACES INTERSECTED
IF(JIN[ER)GO TO 326
JBITXES=.TRUE.
` JBIJESS=.NOT.ABLLE.AND..NOT.ABBCKL BY DEFAULT
GO T口 335
:GET THE X INIERSECTION POINT
326 CALL XINTEH
INTSCT=.TRUE.
33i) SAM(2)=XAMXH
SAM(3)=SAM(2)/256
SAM(4)=0
EX[END=.FALSE.
IF(ABBCKR)GO TO 3312
GO [O 335

* L

```

The visible span has been determined, and now the program must evaluate the next potential visible segment which should be compared. When the program has reached label 350, a visible segment is available for display. If an intersection is involved, then the procedure will display a dot.
\(\because \quad\) MAKE A UNE ELEMENT BUX．
3311 IF（ZS（1）．NE．O．AND．ABRLI）EXIEND＝．FALSE．
IF（．：NJ．．A3RLT．AND．．AVUT．EXTEND）GJ TO 3312
\(S A K(2)=X H I S H T\)
SAX（3）\(=X R\) IOHT／256
CALL LDLPT（SAM（4），SEG（SEGPT＋6））
\(3312 \quad\) ZS（1）＝SEGP
\(Z S(2)=X L E F T\)
LS（3）＝XRIGHT
\(\angle S(4)=\angle L E F I\)
\(\angle S(5)=\angle H I O H T\)
335 CONTINJE
IF（JOBIX．AND．．NOT．（XRIGHT．LE．SAR（2））EXTEND＝．FALSE． IF（JOBIXX．AND．（XRIGHT．LE．SAM（2）））G］TU 345
CALL S「RPT（SEGACT，SEG（SEGPT＋1））
SEGACT＝SEGPI
IF（．NJT．JBOXES）GJ［D 345
EXIEVD＝．FALSE．
SA：（ 2 ）＝XLEFT
SAM（3）＝XLEFT／256
CALL LDLPT（SAM（4），SEG（SEGPT＋4））
\(342 \quad \mathrm{SEGPT}=\mathrm{NEXT}\)
IF（FROM．EO．O）GOTO 301
GO T门 304
\(\therefore\) DUTPUT GEGYENTS．
3ヵO CJITINUE
IF（EXIEND）SEGACT＝0
FWOOFSCAN＝（SEGPT．ER．O）．AND．EXTEND
IF（．NUT．IWISCT）GO T］ 355
CALL ！JArll：（XAMXR，IY）
CALL OXArV（XAMXR，IY）

Since all segment data has been updated to the next scan line, it is necessary to evaluate the data for the current scan line by subtracting the slope from the x values. If the X value of the segment equals that of the sample point, then subroutine CROSS is called, which will update a flag, indicating that the edge is visible for this scan line. Subroutine SETLIN will be called if the edge is visible for the first time. At this time, the beginning \(X\) and \(Y\) coordinate values of the edge are stored. If the edge is going to exit on the next scan line, then it is drawn, since the edge will be deleted on the re-sorting of the segment list. The above procedure is performed for both the left and right edges of the segment.

Label 17 through label 15 handle the horizontal edge problem. If there are any horizontal edges on the current scan line, then the visible segment is checked to see if it has the same polygon which has a horizontal edge within the visible span. If so, then the line is drawn. Otherwise, the rest of the horizontal edge list for this scan line is searched for a match.

Finally, the edges in the segment list are checked to see if they were visible on the previous scan line but not this scan line. If so, then a line is drawn. The program checks to see if the end of the scan line has been reached, and then jumps to either process another scan line or get another visible segment.
```

3jう [F (LS(1).EQ.O) GO IJ 15
\thereforeJHDAFE LEFT EDGE IF VISIBLE SEGMENT EOUALS THE REAL SEGAENI.
INC=SEG(ZS (1) +3)-SEG(ZS (I)+4)
IF(SAM(1).NE.INC+1O24) GU IU 1%
IF(SEG(ZS(1)+11).E?.O) CALL SETLIN(INC,4,11,IY)
C JE[ERWINE IF THE PHEVIDUS LINE AND CURREN[ LINE CRUSS
CALI CH!JSS(INC,3,1I,IY)
`CHECK TO SEE IF LEFT UF SEG NILL EXII 'JN NEXT LINE 16 IF(SEG(LS(I)+2)/262144.EO.O) CALL DRAit(INC,4,II,IY) C jrdate right edge if visible segment equalS the real segami.     INC=SEG(ZS(1)+5)-SEG(ZS(1)+6)     IF(SAM(2).NE.INC) GO TU 17     IF(SEG(ZS(I)+12).EQ.O) CALL SETLIN(INC,6,12,IY) C DETERAINE IF IHE PREVIOUS LINE AND CURRENT LINE CNJYS     CALL CRUSS(INC.5,12,IY) ; CHECK TO SFE IF RIGHT OF SEG NILL EXIT ON NEXT LINE 11 IF((SEG(ZS(I)+2).AND.262143).ED.O) CALL DRAM(INC,5,12,IY)     CALL LORPT(J,HBUCKY(IY+2))     CURLIN=.TRIJE. C ARE IHERE HORIZONTAL LINES DIN THIS SCANLINE? 13 IF (J) GO TO 14     CALL LOD2HF(J-1,4XL,HXK)     CALL LOD2HF(J-2,POLYHI,J) J JUES [HIS PDLYGON HAVE HORIZUNIAL LINES         IF (POLYPT.NE.SEG(ZS(I)+1)/262144) G\ IO 13     SAIAL=SAM(1)/262144-1     SAMH=SAM(2)/262144 O IS IHE LINE IN THE VISIBLE SEGMENT REGIUN?         IF (SAML.GE.HXR) GO TJ 13         IF (SAMH.LE.HXL) GJ [O 13 C DRAN HDRIZONTAL LINE         CALL DRANM(NYMAXO(SAML,HXL)*252144,IY-CURLIM)         CALL DRANV(MYKINO(SAMR,HXR)*262144,IY-CIJRLI, (v)         OU \Gamma丁 13 14 CUHLIN=.NOF.CURLIN         J=H3UCKY(IY+2)/262144         IF (.NJ[.CUKLIN) GU [J 13 Ij IF(.NO[.ENUUFSCAN)GU IO 281 O BACK PJINTEN NDT NEEDED NUN.         IF(SEGL2.NE.O)SEG(SEGL2)=0         SETXST=SEGS2 C O] [HRUUSH ALL SEG BLDCKS TU SEE IF AN EUGE WAS` VISIBLE IN THE LAST SCAN LINE BUT NAS NII DISPLAYED.
ZS(1)=SSGXST
40 IF(ZS(1).EO.0) GO TO bo
; CHECK LEFT EDGE
IF((SEG(ZS(1)+1|).AND.7).E?.((IY+2).AND.7))
1 CALL DRAN(SEG(ZS(1)+3)-2* SEG(ZS(1)+4),4,11,IY+1)
- CHECK RIGHI EIOGE
41 IF((SEG(ZS(1)+12).AND.7).EO.((IY+2).AND.7))
1 CALL DHAN(SEG(ZS(1)+5)-2*SEG(ZS(1)+6),6,12,IY+1)
O SEI NEX[ SEGHENT BLOCK
42 LS(1)=SEG(ZS(I)).AND.262143
GTTJ40
50 IF (IY.GE.O) GO TO 204
RETURN
EN!)

* L

```


Figure 1:

Intersection of two spheres at 256 scan line resolution.


This picture was processed at 256 scan line resolution. The perspective transformation distorts some of the objects. Processing time on the 295 edges which compose this picture was 7.2 seconds.


This picture was processed at 1024 scan line resolution. Quality of the picture is greatly enhanced as a result of the increase in resolution. Processing time increased to 23.7 seconds. Notice that some lines are composed of dots. These are a result of intersection of surfaces.


Figure 4:

1600 edge object with and without hidden surface removal at 256 scan line resolution. Computation time is 16.3 seconds.

Romney, G. W., "Computer Assisted Assembly and Rendering of Solids," Computer Science Technical Report 4-20, Computer Science Division, University of Utah, Salt Lake City, August 1969.

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