

JOINT INVERSION OF LAND AND MARINE  
ELECTRICAL RESISTIVITY TOMOGRAPHY  
FOR IMAGING SUBMARINE FRESHWATER  
DISCHARGE

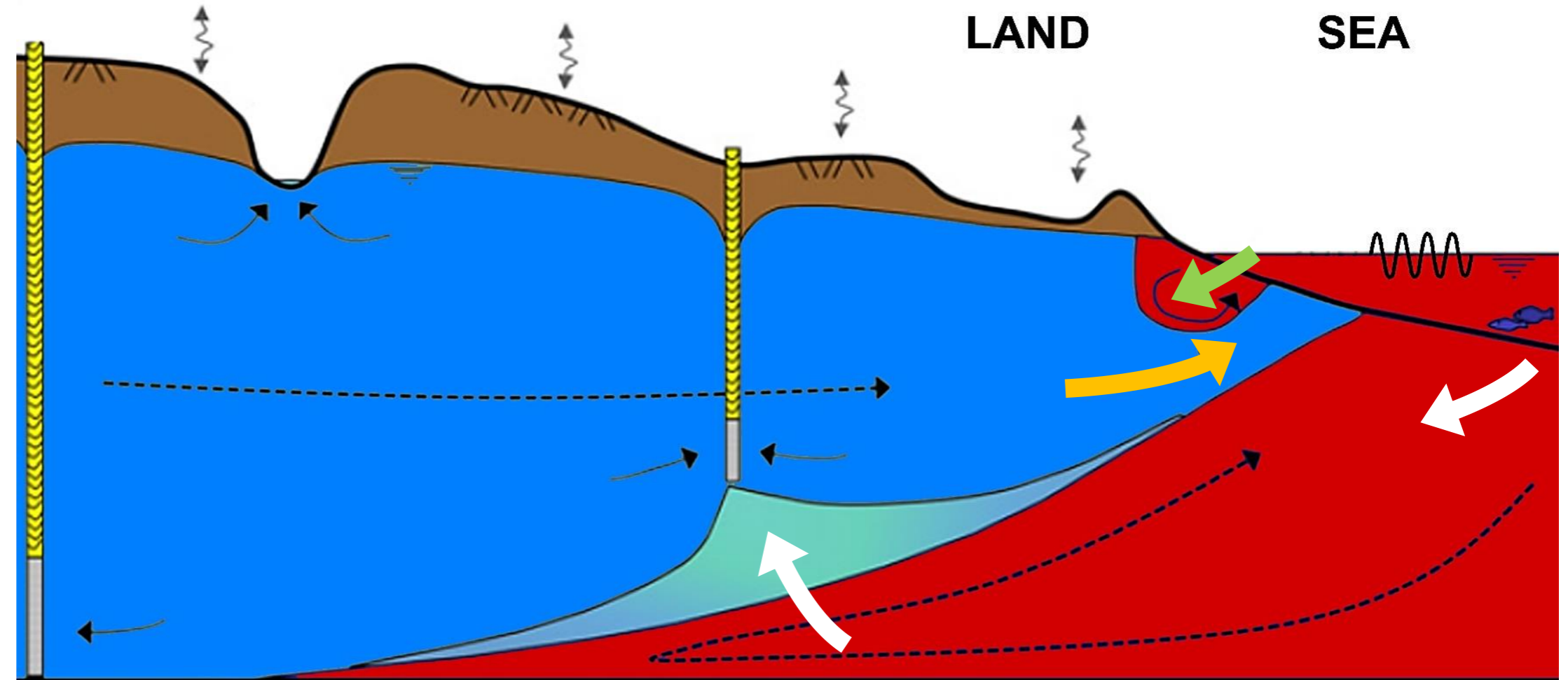
T. Hermans and M. Paepen

# FRESH-/SALTWATER INTERFACE

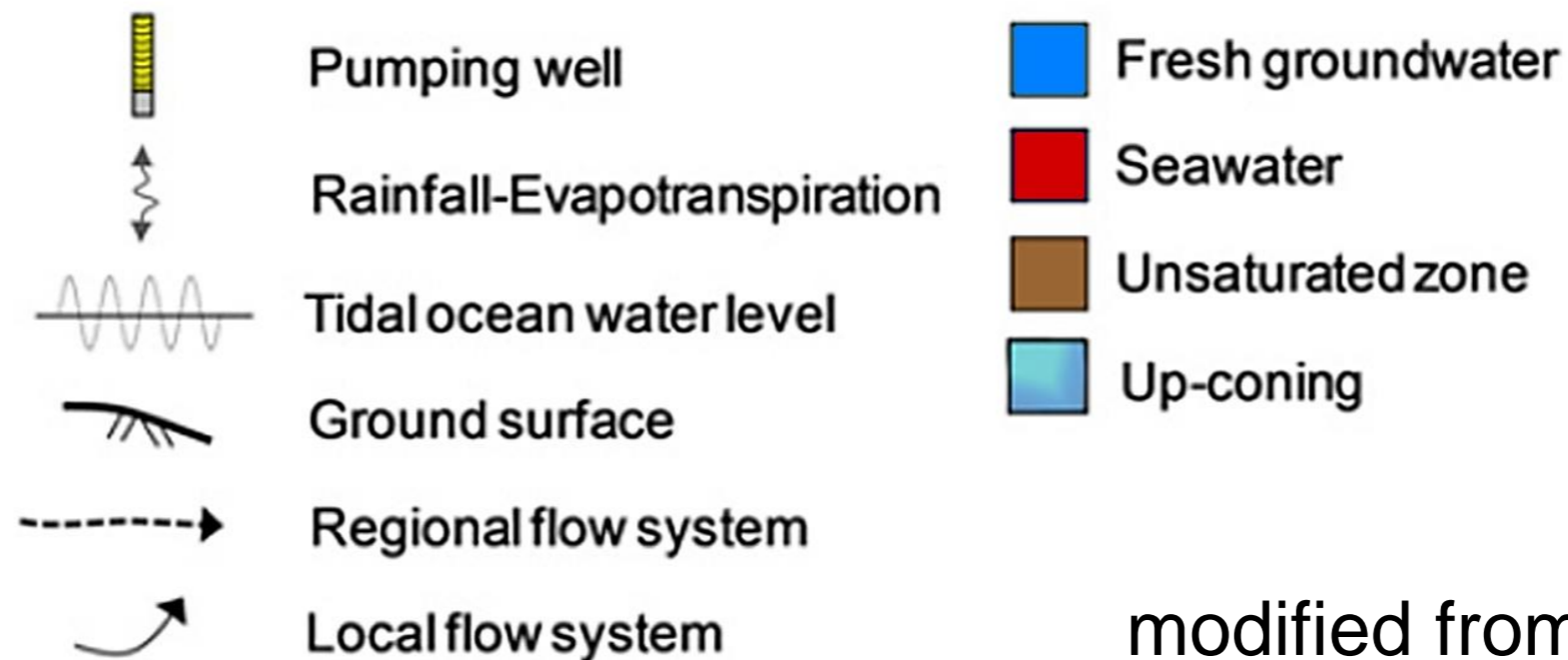
SALTWATER INTRUSION (SI)

INFILTRATION ON THE BEACH SLOPE

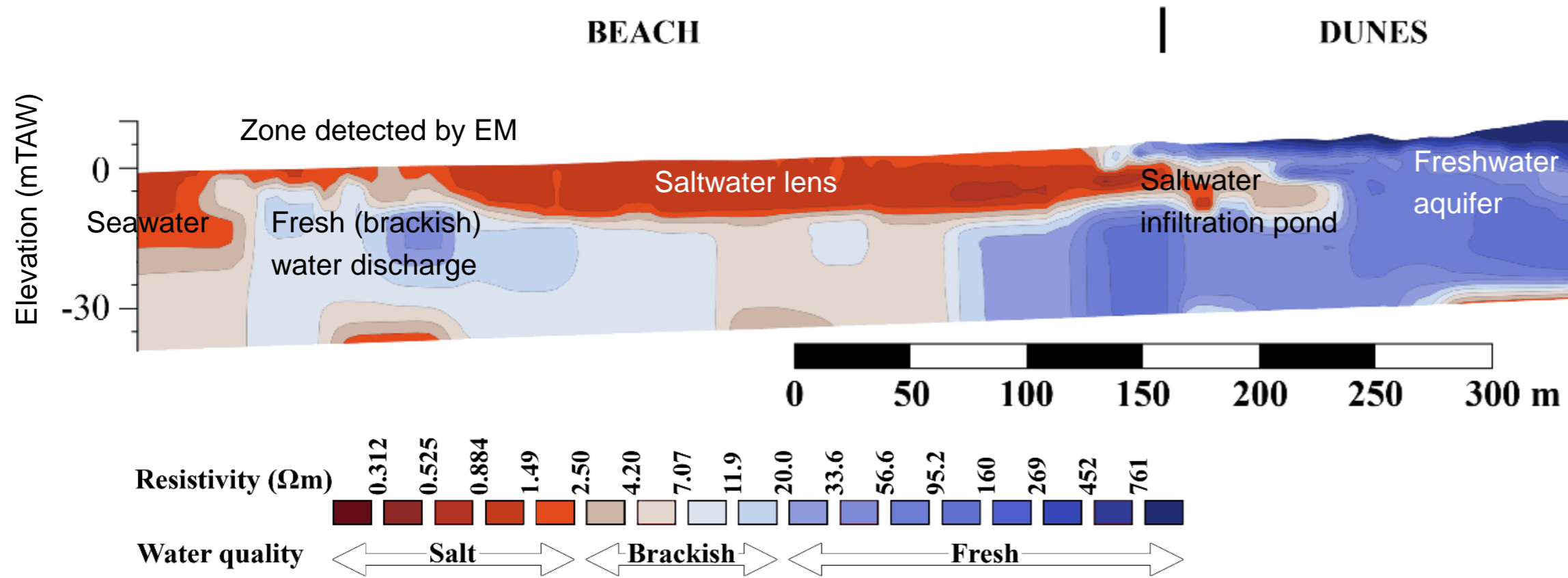
FRESH SUBMARINE GROUNDWATER DISCHARGE (FSGD)



## LEGEND



# ERT ON LAND



Resistivity directly related to water salinity

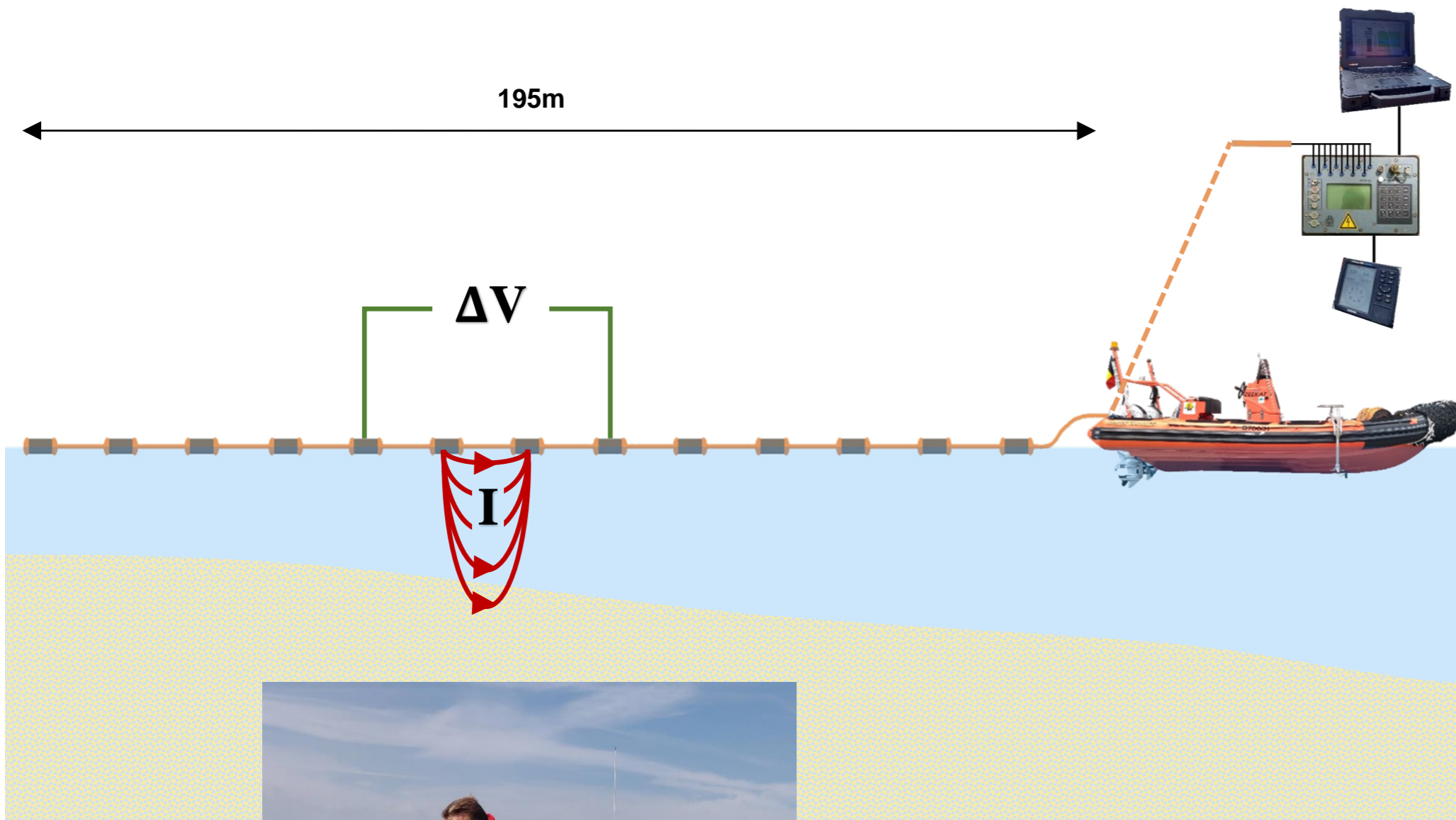
Relatively high resolution

Limited to the intertidal zone





# MARINE ERT

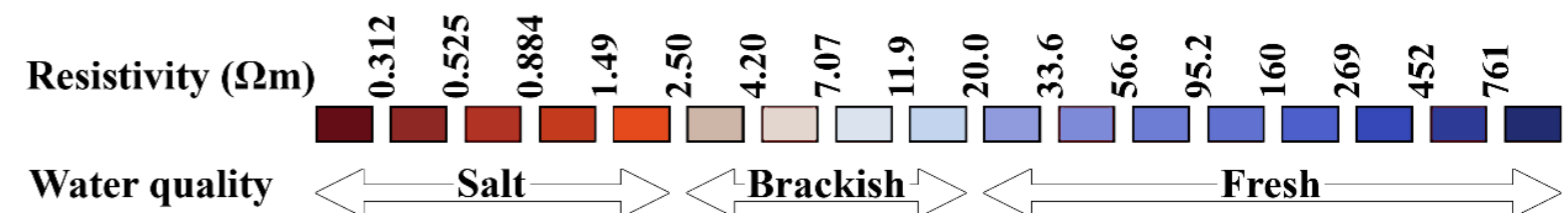
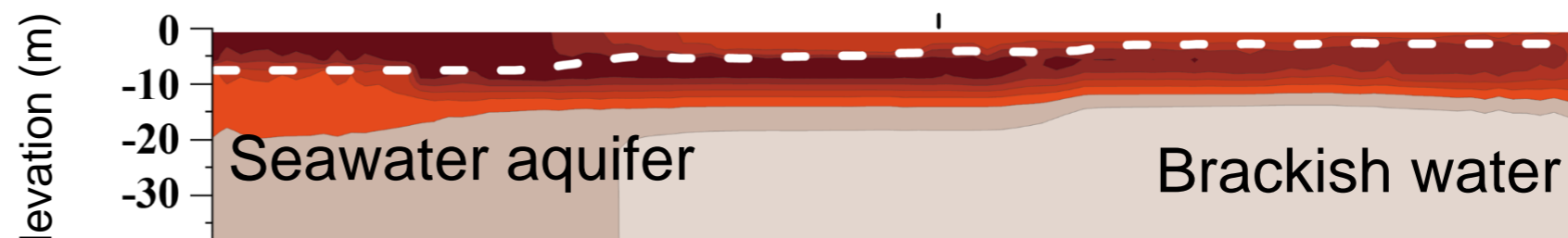
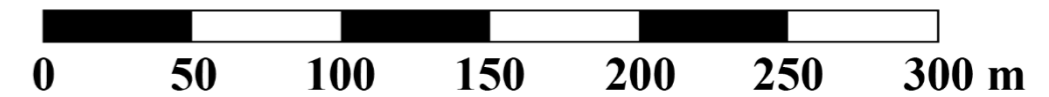


Resistivity directly related to water salinity

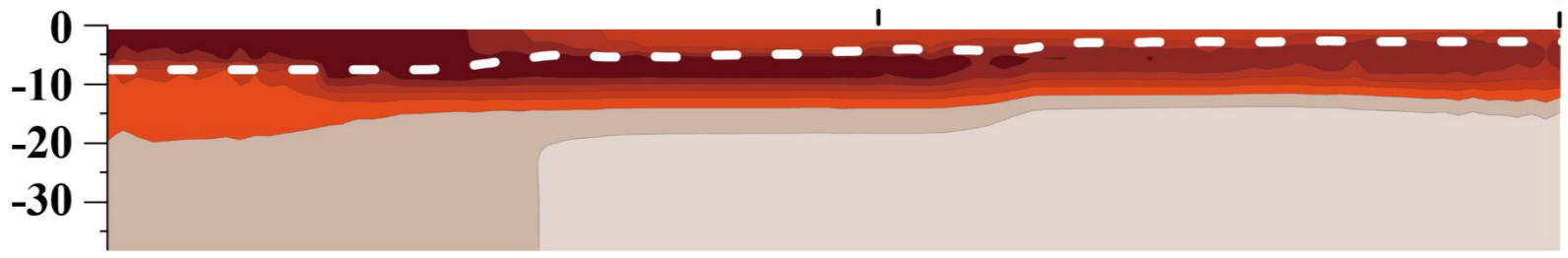
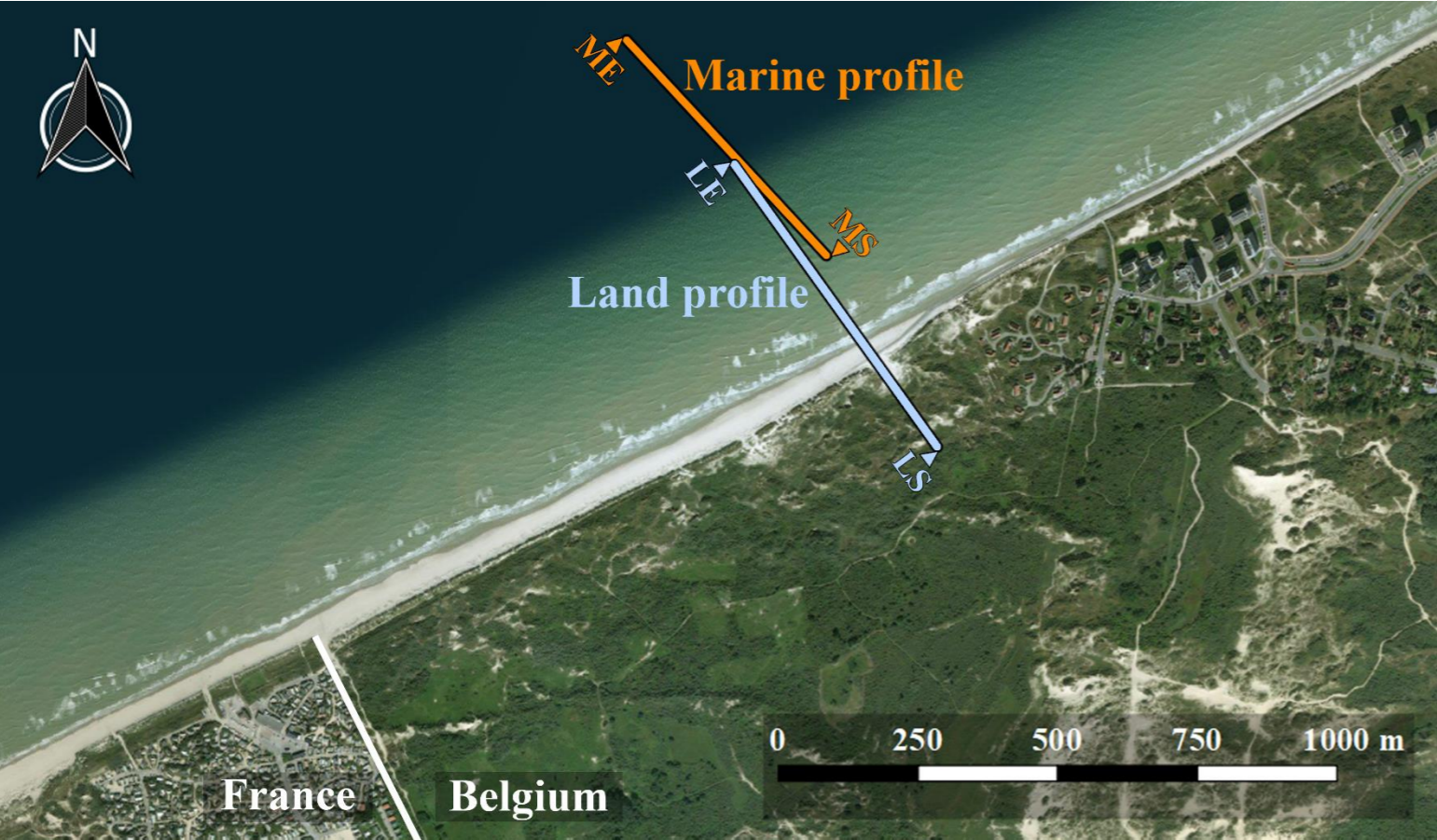
Fast acquisition (5 to 6 km/h)

Influence of the water layer

Lower resolution and depth of investigation



# HOW TO COMBINE BOTH ?



Marine profile





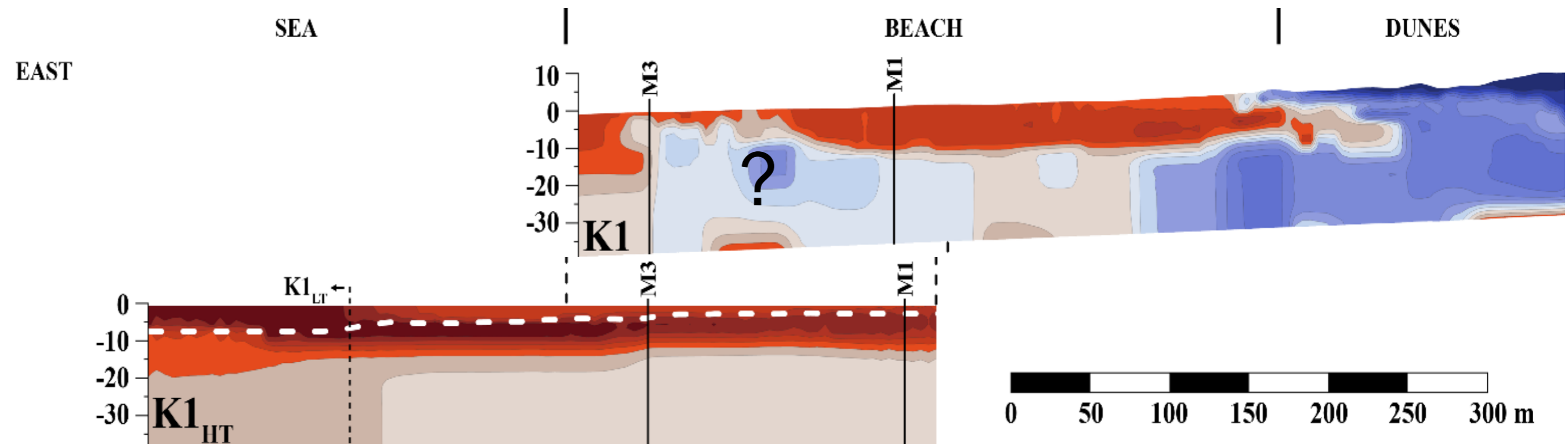
# CAN WE GET A SINGLE MODEL ?

Qualitative coherence between the two images, but:

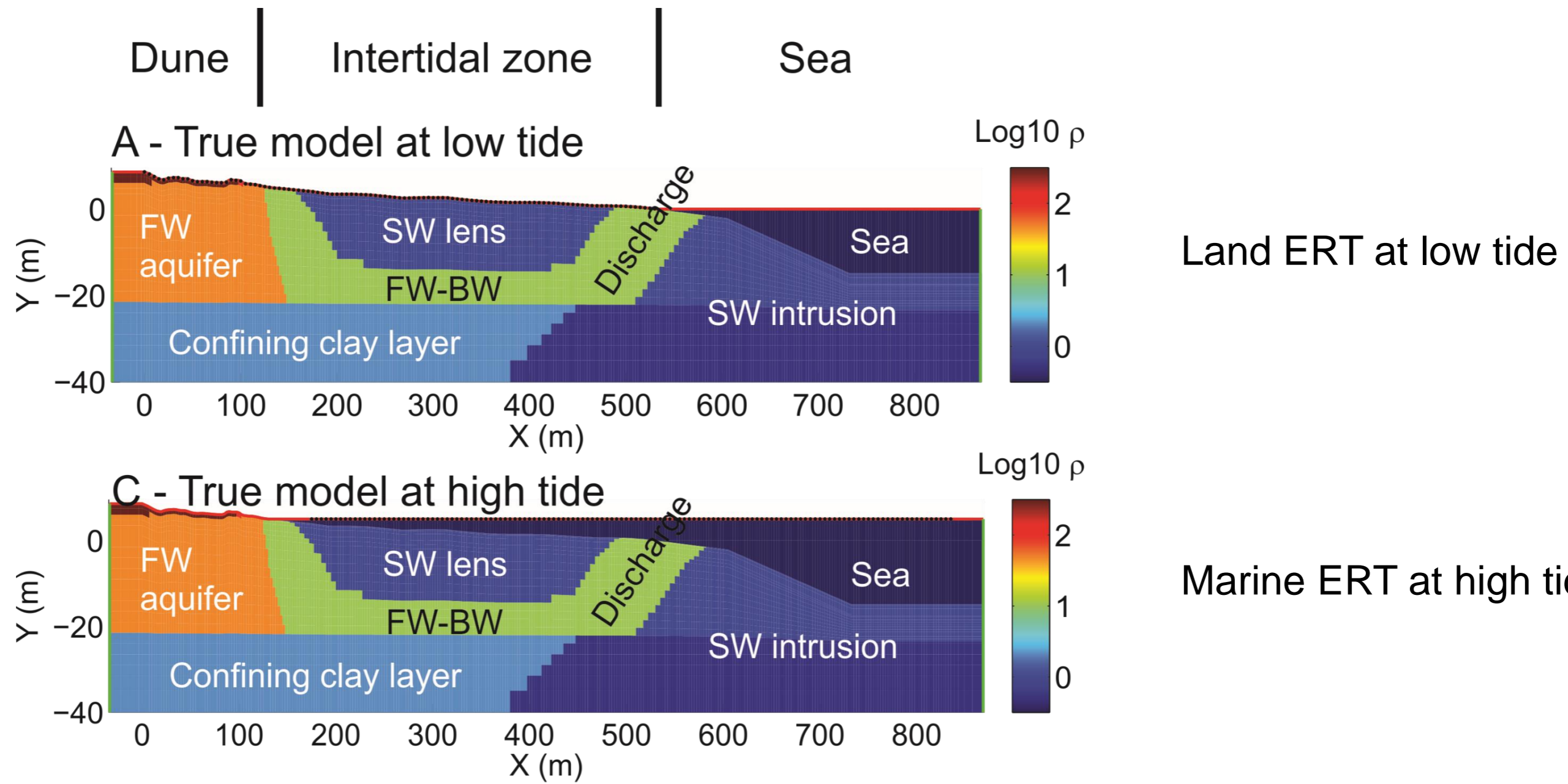
- Difference in resolution
- Resistivity values are not similar

Data should correspond to the same resistivity distribution, but

- Presence of the water layer on marine data
- Influence on the inversion results

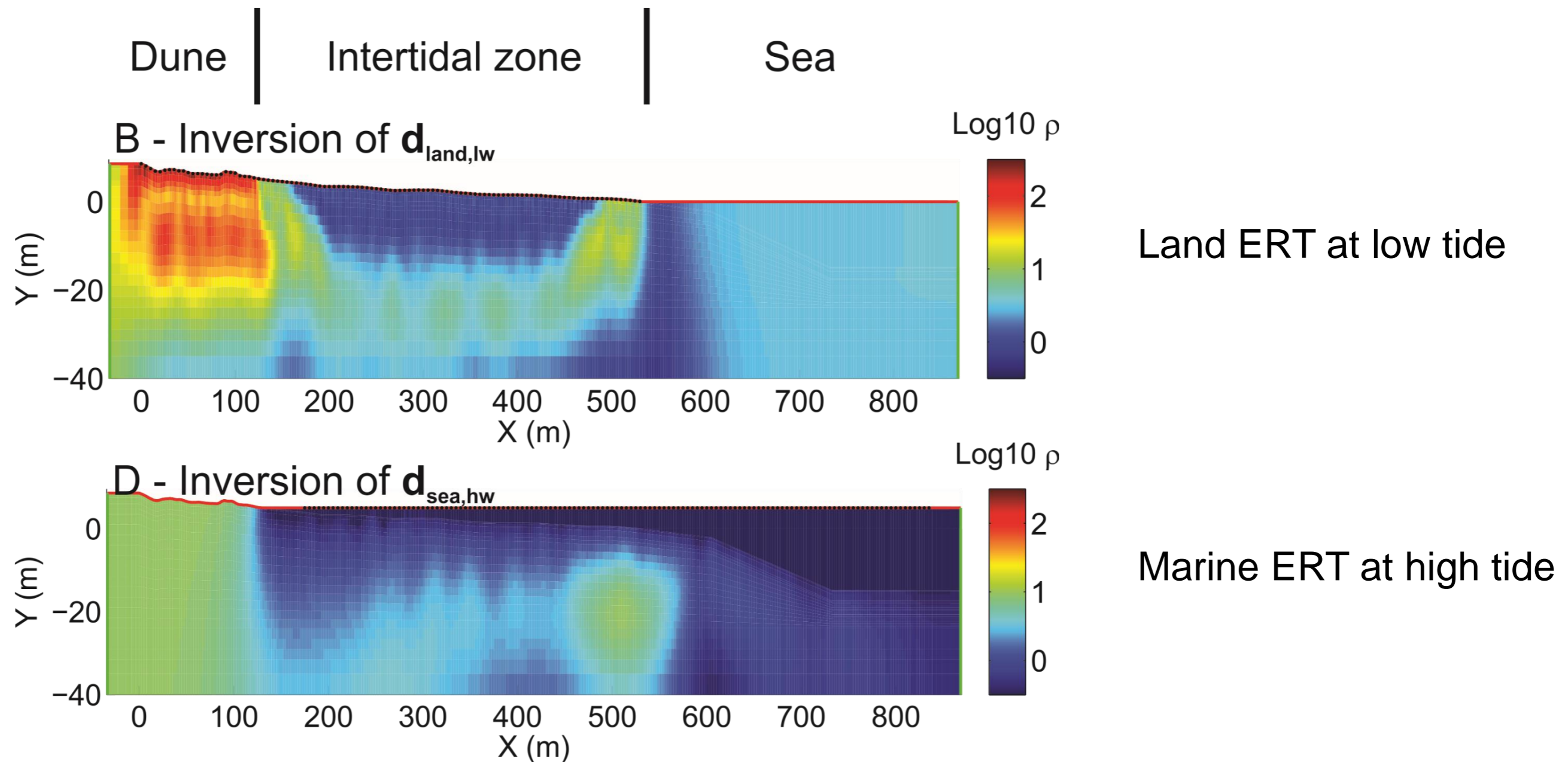


# ACCOUNTING FOR THE SEAWATER LAYER



**The difference between the two conditions is the presence of the water layer during high tide for marine ERT**

# INDIVIDUAL INVERSIONS

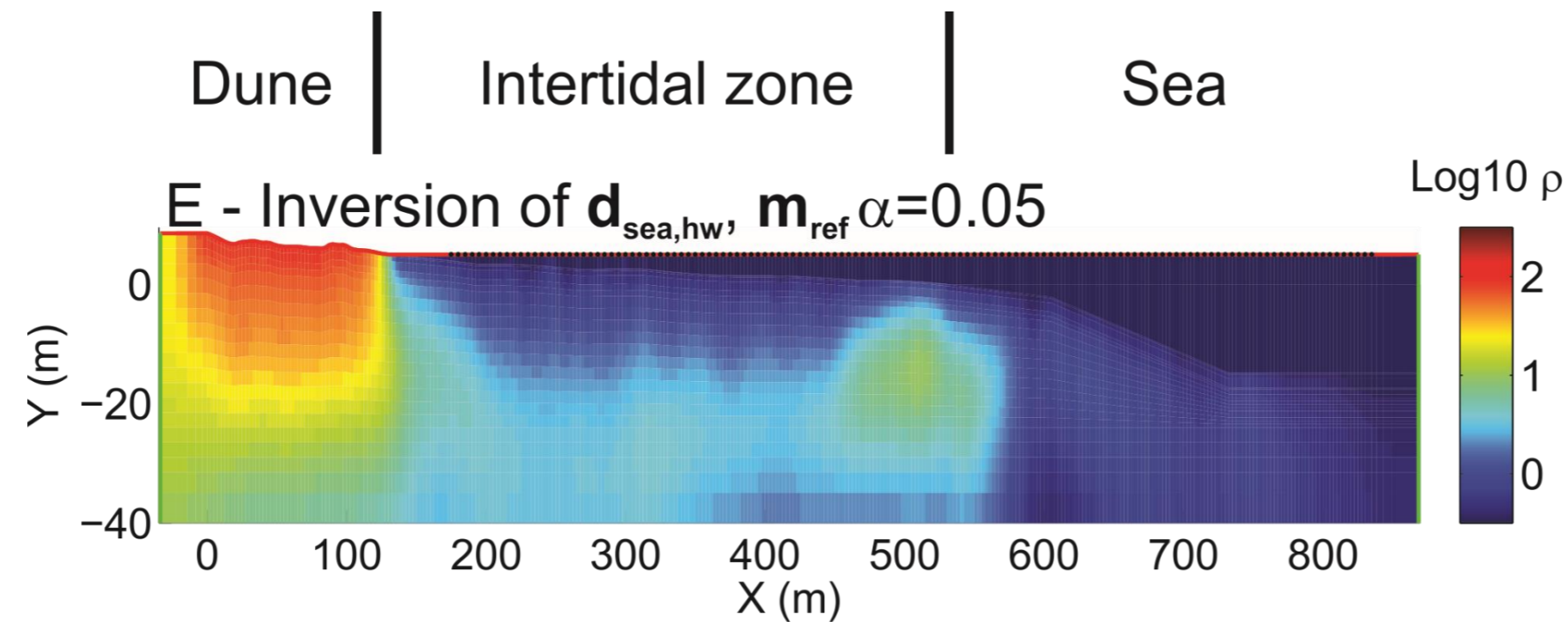


**Both data sets are able to detect the presence of freshwater**

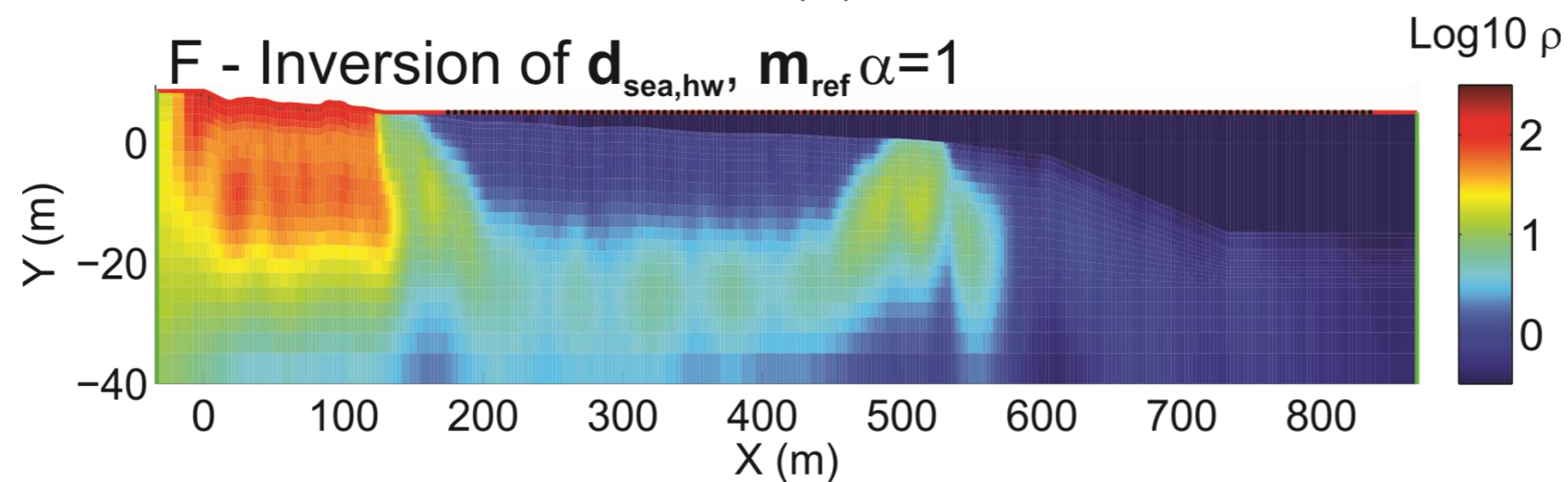
- Land ERT does not get the sea extension
- Marine ERT has a lower resolution



# OPTION 1: LAND ERT AS A REFERENCE MODEL



Marine ERT at high tide  
with land as reference  
Low weight

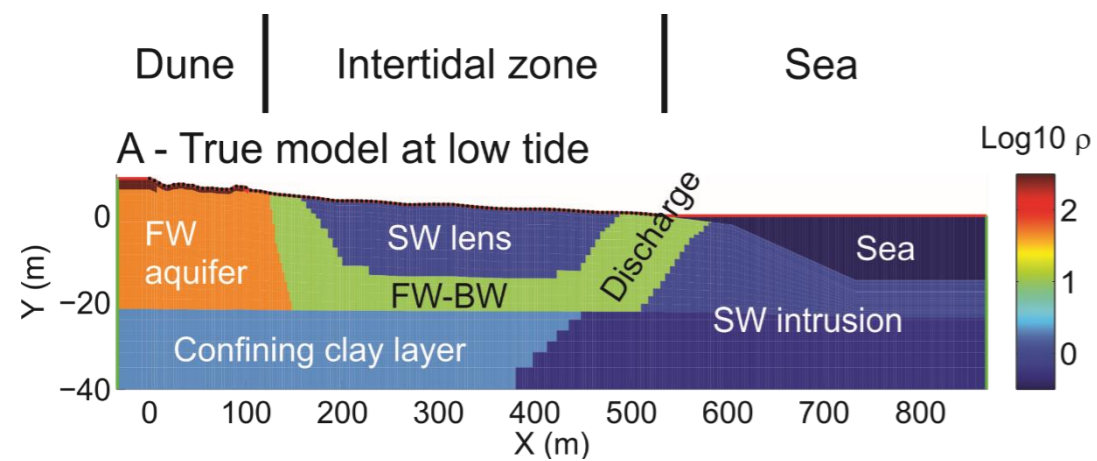


Marine ERT at high tide  
with land as reference  
High weight

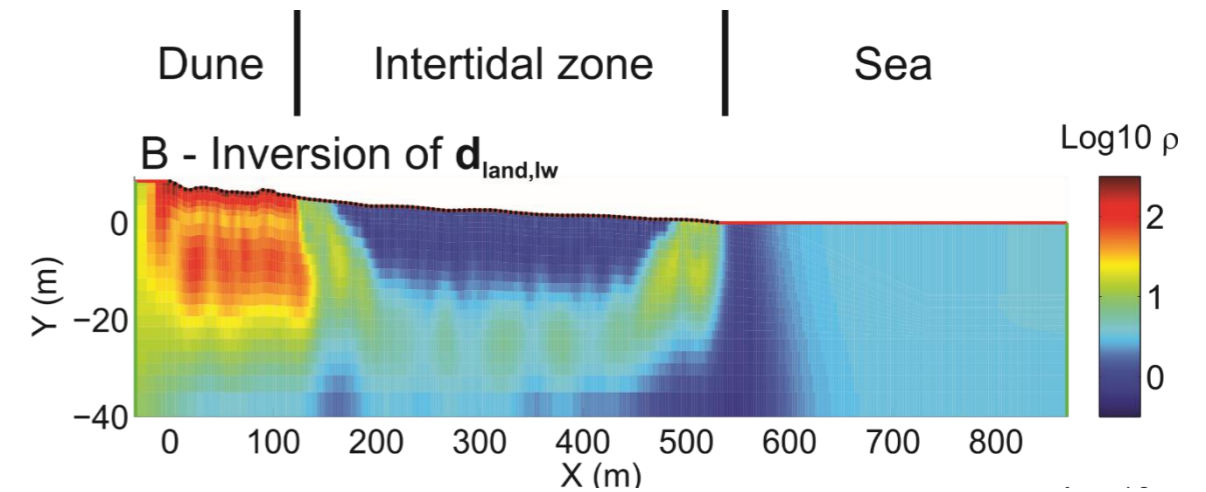
## Improvement of the image

- Discontinuity in the freshwater discharge
- No guaranty that land data remains fitted

# OPTION 2: DATA CORRECTION



1. Inversion



Collected data  $d_{land,lw}$  from  $m_{true}$

What would be the data at high tide  $d_{land,hw}$ ?

$$m_{est} \rightarrow d_{land,lw}^{est} = d_{land,lw} + \epsilon$$

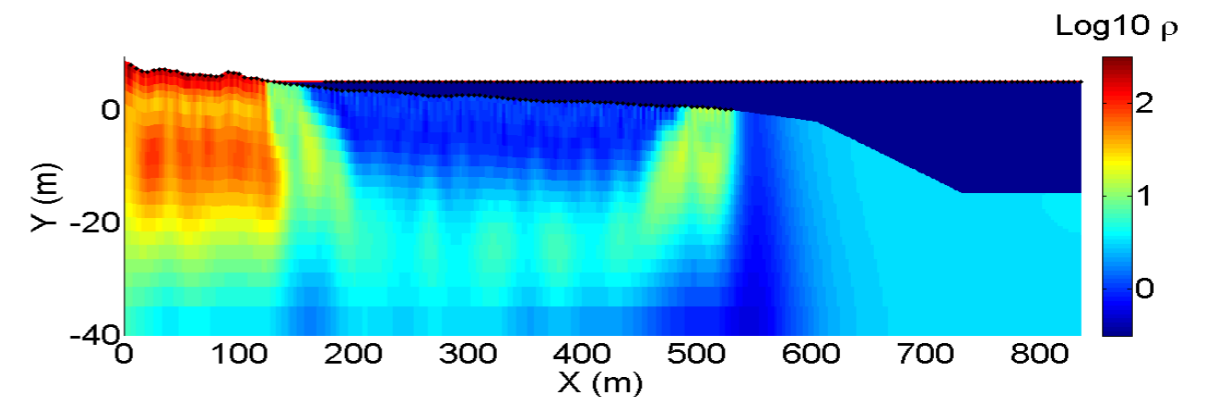
2. Simulate presence of water layer  
Forward model

$$\Delta d = d_{land,hw}^{est} - d_{land,lw}^{est}$$

$$d_{land,hw} = d_{land,lw} + \Delta d$$

$d_{land,hw}$  is used with  $d_{sea}$  for a joint inversion

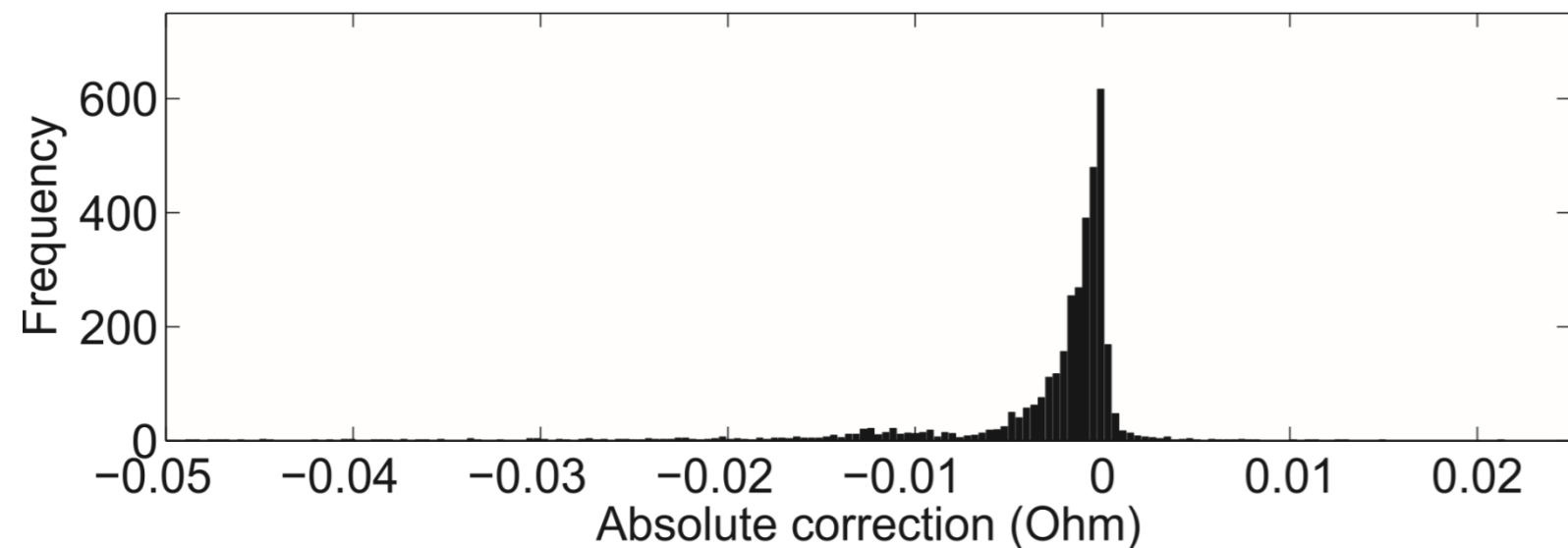
3. Data correction



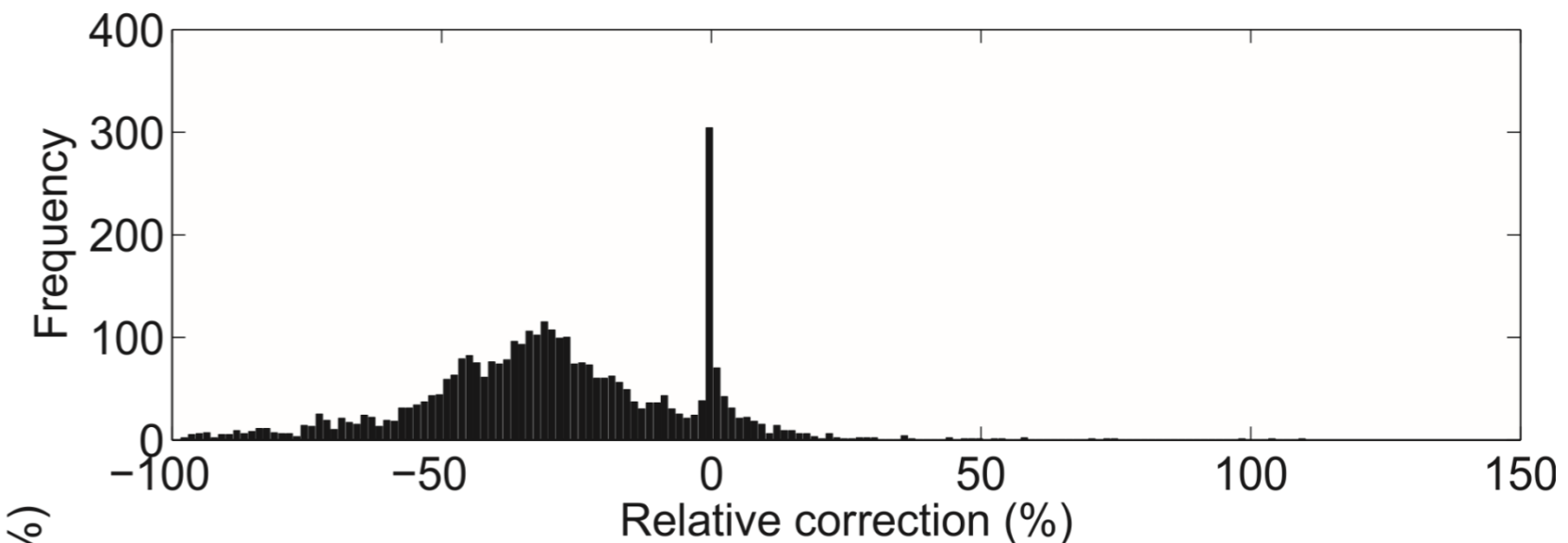
$$d_{land,hw}^{est} = G(m_{est} + \Delta m)$$

# OPTION 2: QUALITY OF CORRECTION

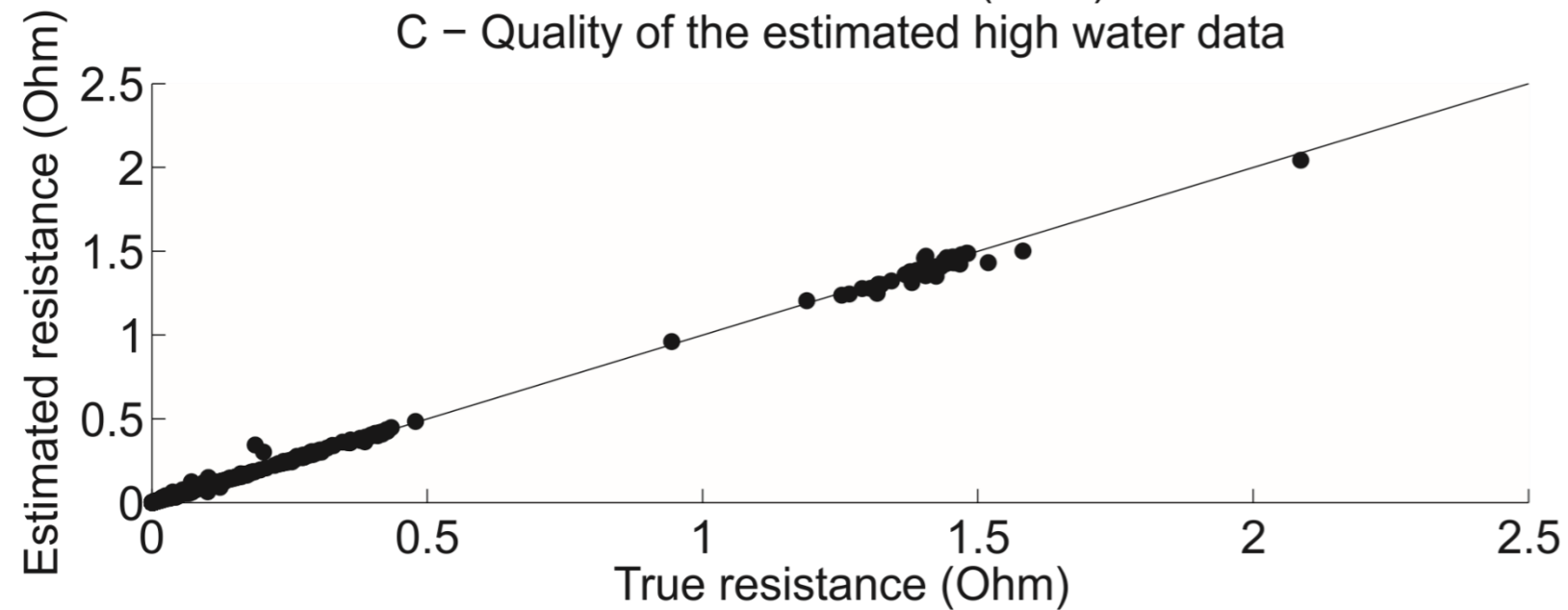
A – Absolute resistance correction



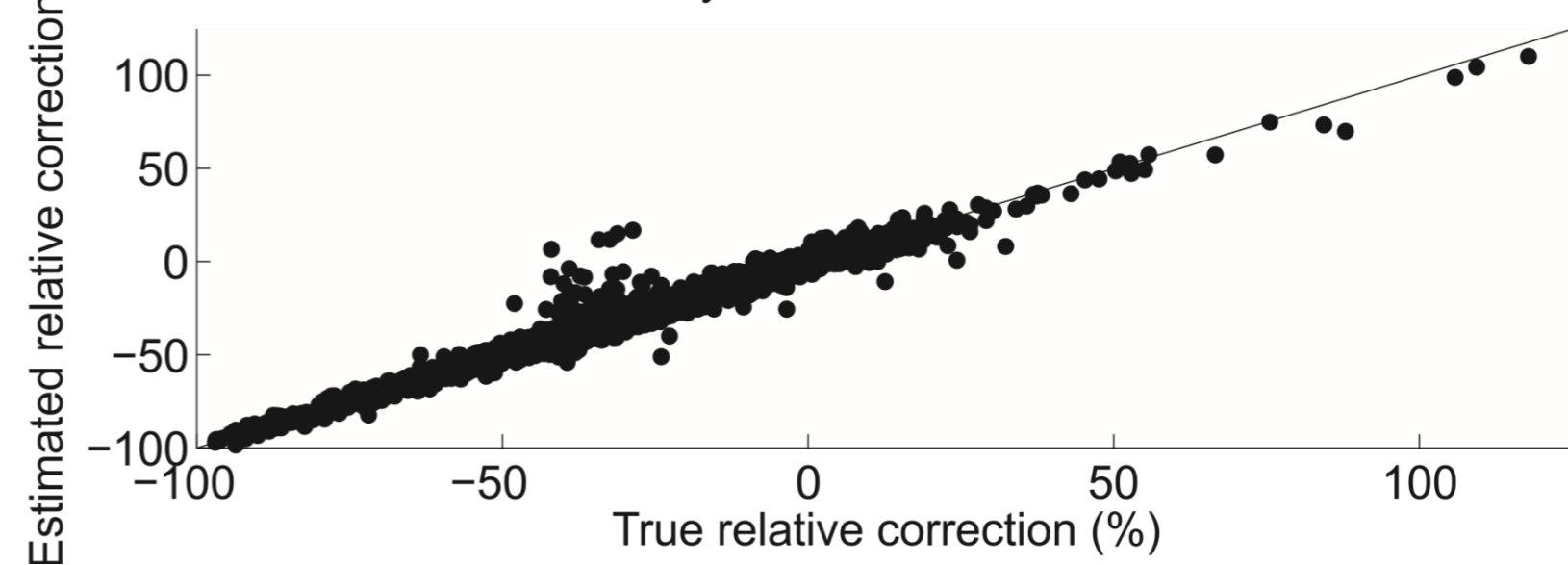
B – Relative resistance correction



C – Quality of the estimated high water data

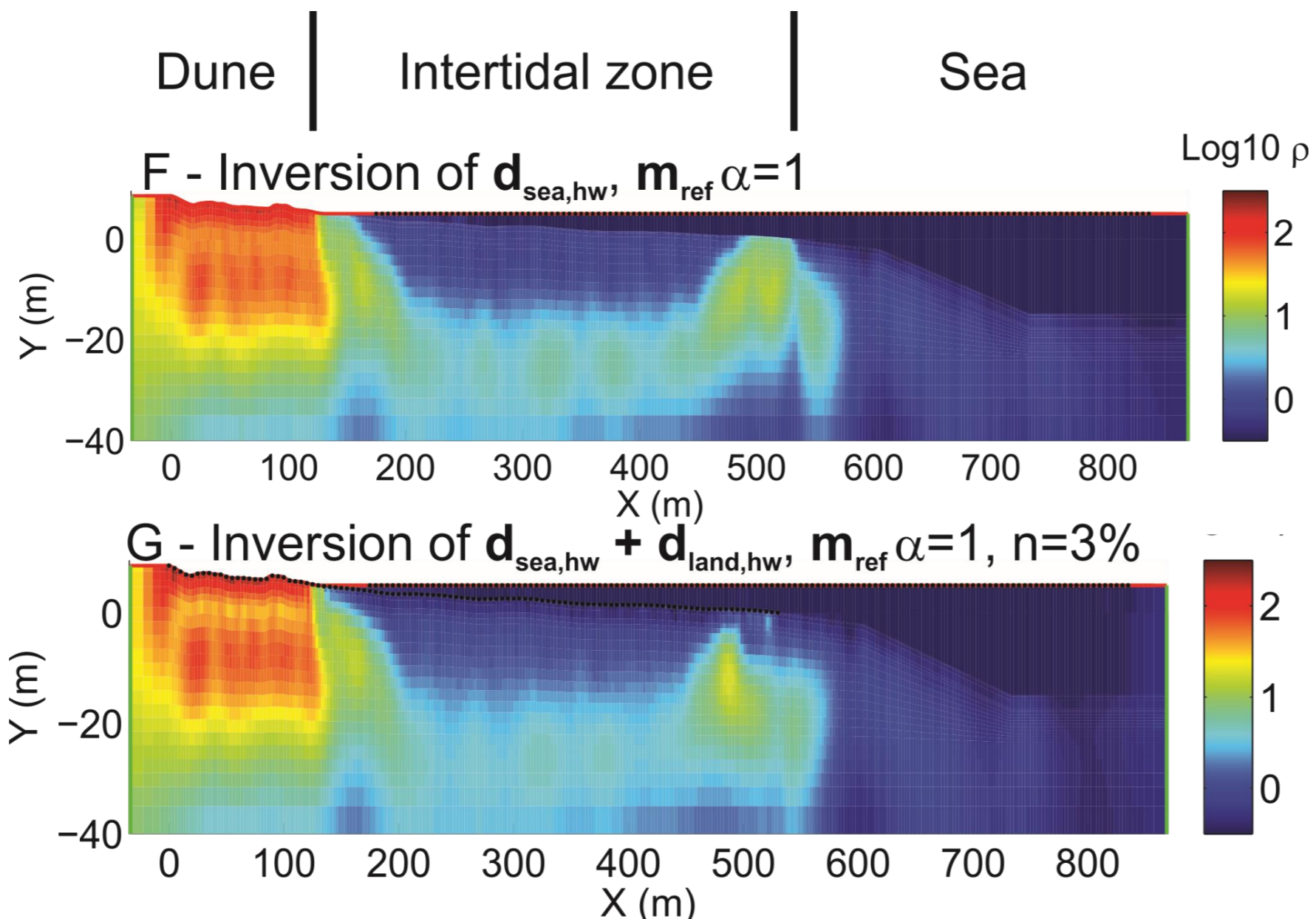


D – Quality of the estimated correction





# OPTION 2: JOINT INVERSION

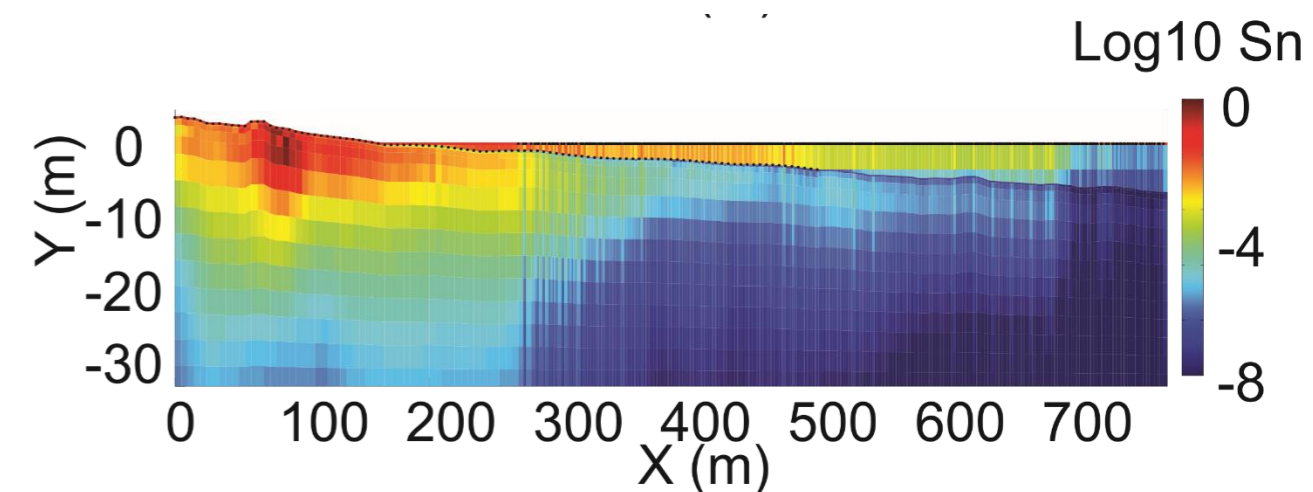


Marine ERT at high tide  
with land as reference

Marine ERT at high tide  
**with data correction** and  
reference land model

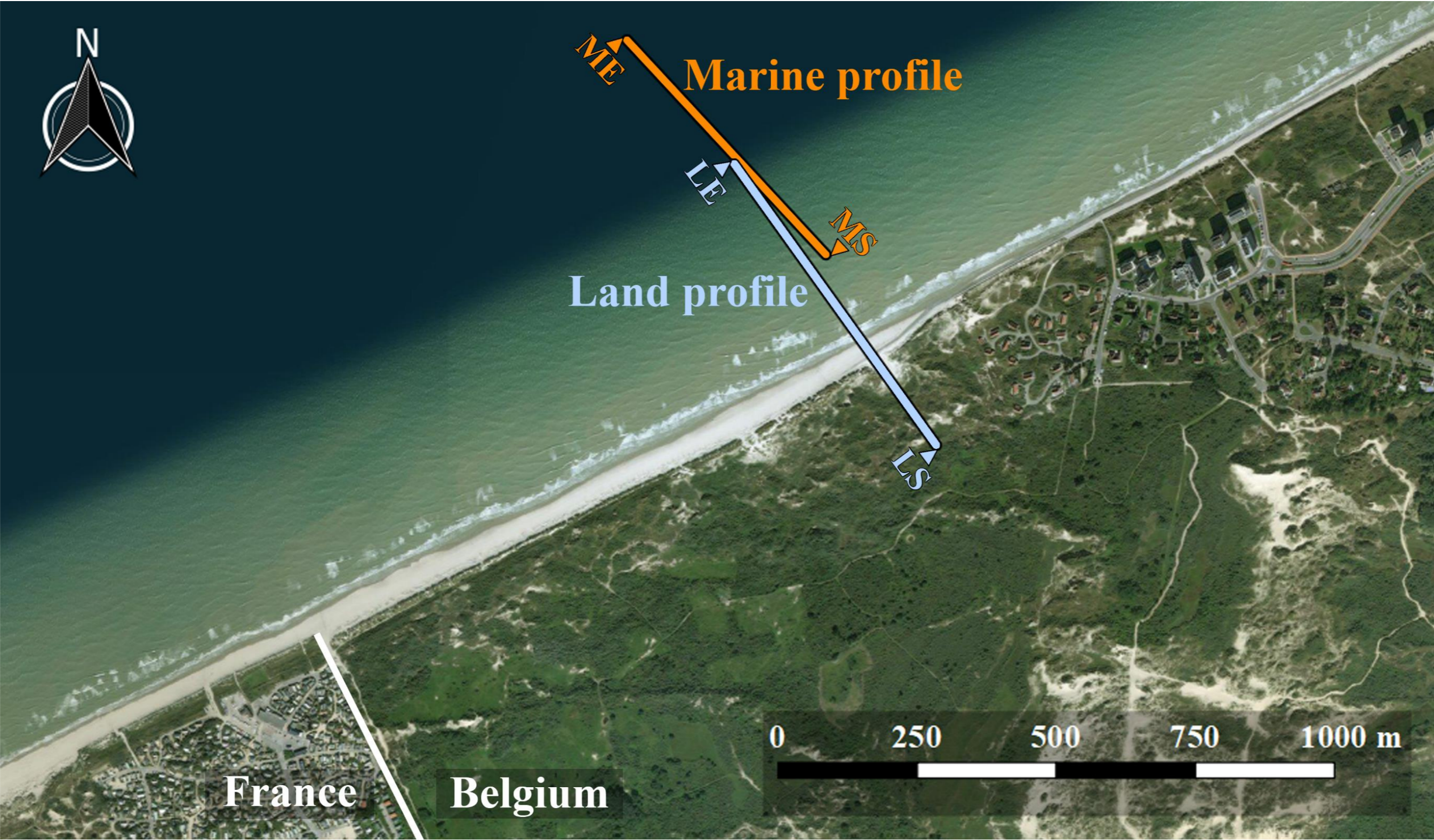
## Joint model

- Data correction ensures land data is still fitted
- Reference model counteracts the apparent loss of resolution for land data due to the water layer



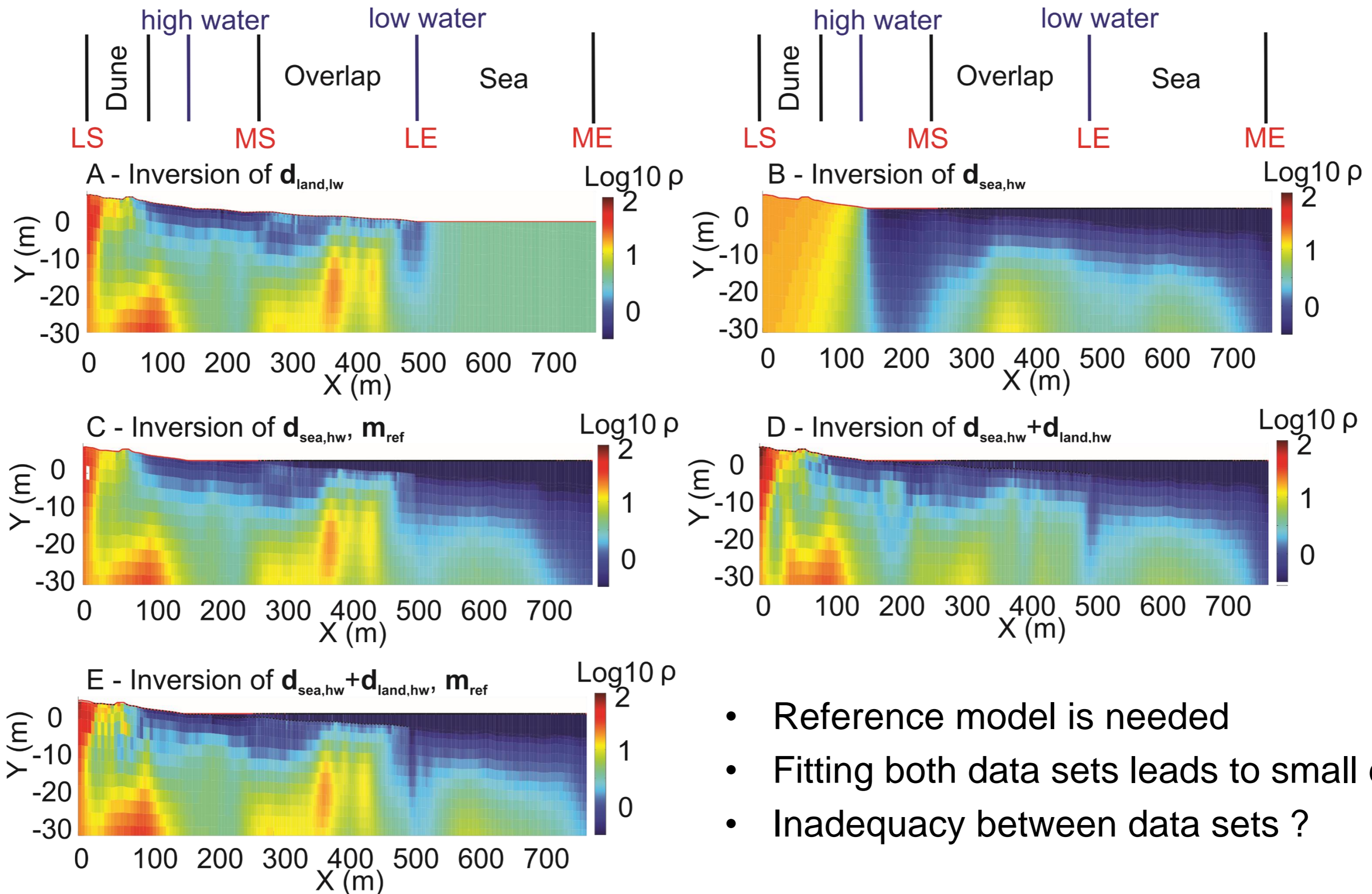


# FIELD APPLICATION





# FIELD APPLICATION



- Reference model is needed
- Fitting both data sets leads to small differences
- Inadequacy between data sets ?



# CONCLUSIONS

- New approach to jointly invert land and marine data with overlapping
  - Data correction to simulate land data with water layer
  - Estimated correction is well estimated
  - Reference model to maintain higher resolution from land data
- Combined resistivity model enables finer interpretation
- Risk of data inadequacy ?
- Immediate extension to monitoring tide processes (time-lapse)

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# CONCLUSIONS

- New approach to jointly invert land and marine data with overlapping
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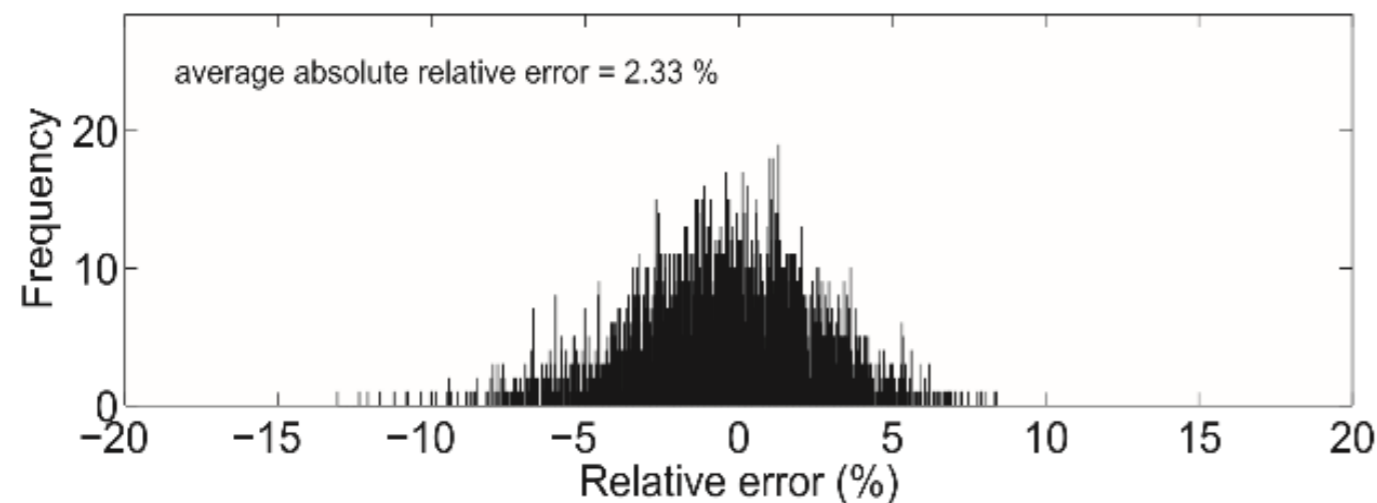


# OPTION 2: DATA CORRECTION

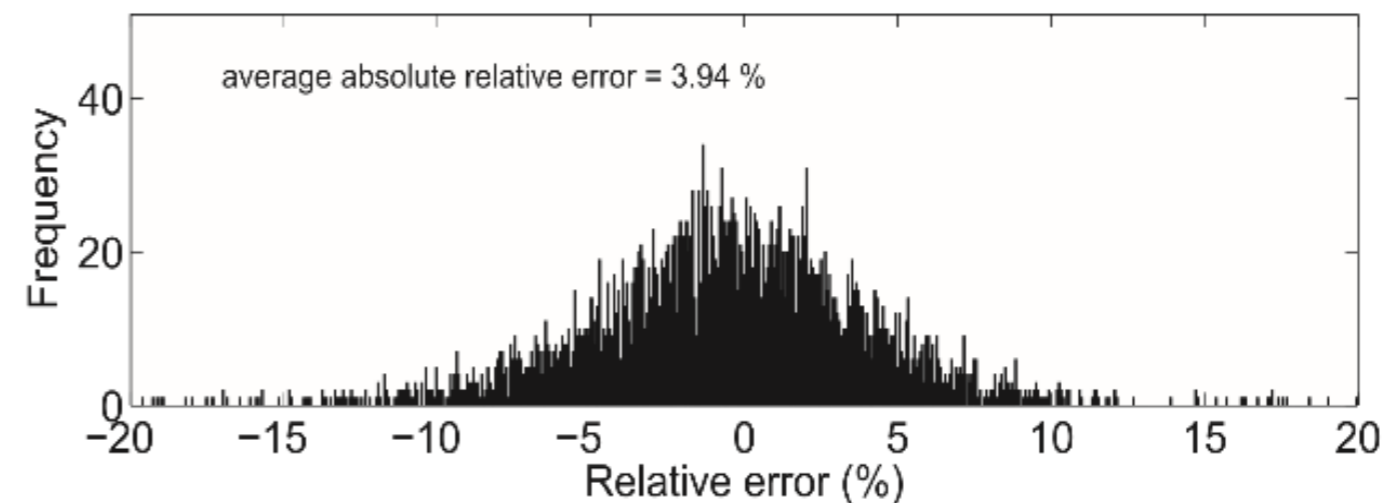
- 1) Measured land data at low tide:  $\mathbf{d}_{land,lw} = \mathbf{G}(\mathbf{m}_{true}) + \epsilon$
- 2) Fictional land data at high tide:  $\mathbf{d}_{land,hw} = \mathbf{G}(\mathbf{m}_{true} + \Delta\mathbf{m}) + \epsilon$
- 3) Taylor's approximation:  $\mathbf{G}(\mathbf{m}_{true} + \Delta\mathbf{m}) = \mathbf{G}(\mathbf{m}_{true}) + \frac{\partial \mathbf{G}(\mathbf{m}_{true})}{\partial \mathbf{m}} \Delta\mathbf{m}$
- 4) Taylor's for data:  $\mathbf{d}_{land,hw} = \mathbf{d}_{land,lw} + \frac{\partial \mathbf{d}_{land,lw}}{\partial \mathbf{m}} \Delta\mathbf{m}$
- 5) Estimating:  $\mathbf{d}_{land,lw}^{est} = \mathbf{G}(\mathbf{m}_{est}) = \mathbf{d}_{land,lw} + \mathbf{e}$
- 6) Estimating:  $\mathbf{d}_{land,hw}^{est} = \mathbf{G}(\mathbf{m}_{est} + \Delta\mathbf{m})$
- 7) Estimating the derivative:  $\frac{\partial \mathbf{d}_{land,lw}}{\partial \mathbf{m}} = \frac{\mathbf{d}_{land,hw}^{est} - \mathbf{d}_{land,lw}^{est}}{\Delta\mathbf{m}}$
- 8) Estimating:  $\mathbf{d}_{land,hw} = \mathbf{d}_{land,lw} + (\mathbf{d}_{land,hw}^{est} - \mathbf{d}_{land,lw}^{est})$
- 9) Joint inversion of  $\mathbf{d}_{land,hw} + \mathbf{d}_{sea,hw}$

# NOISE CONSIDERATION

Before correction

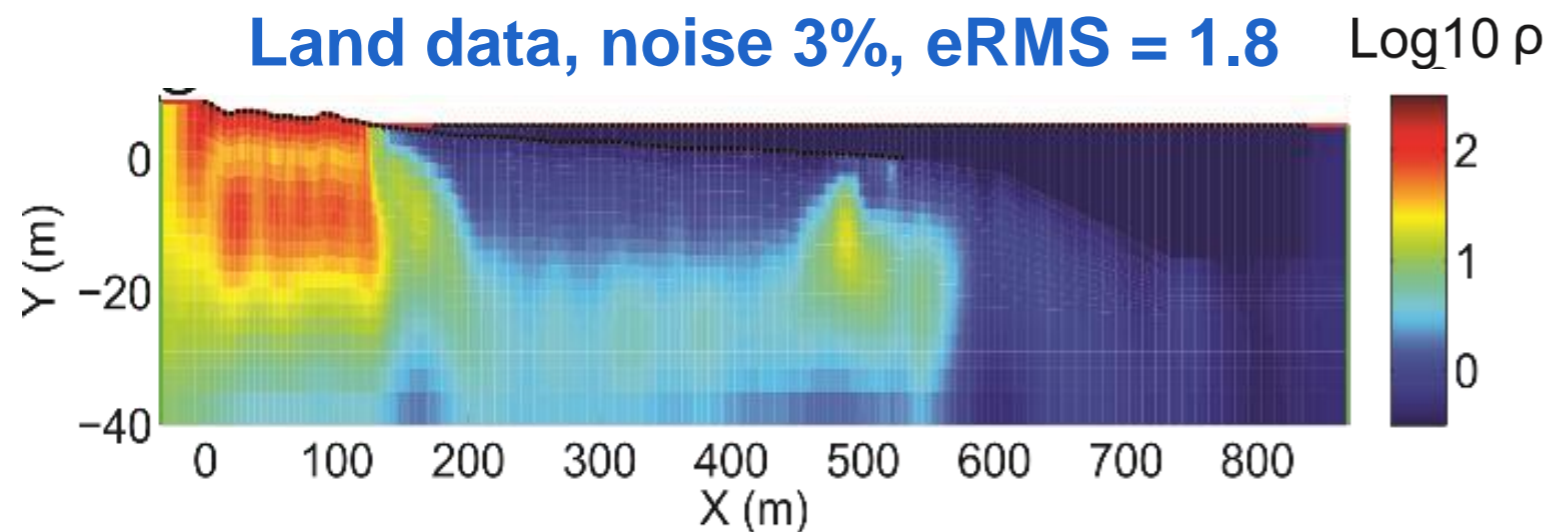


After correction

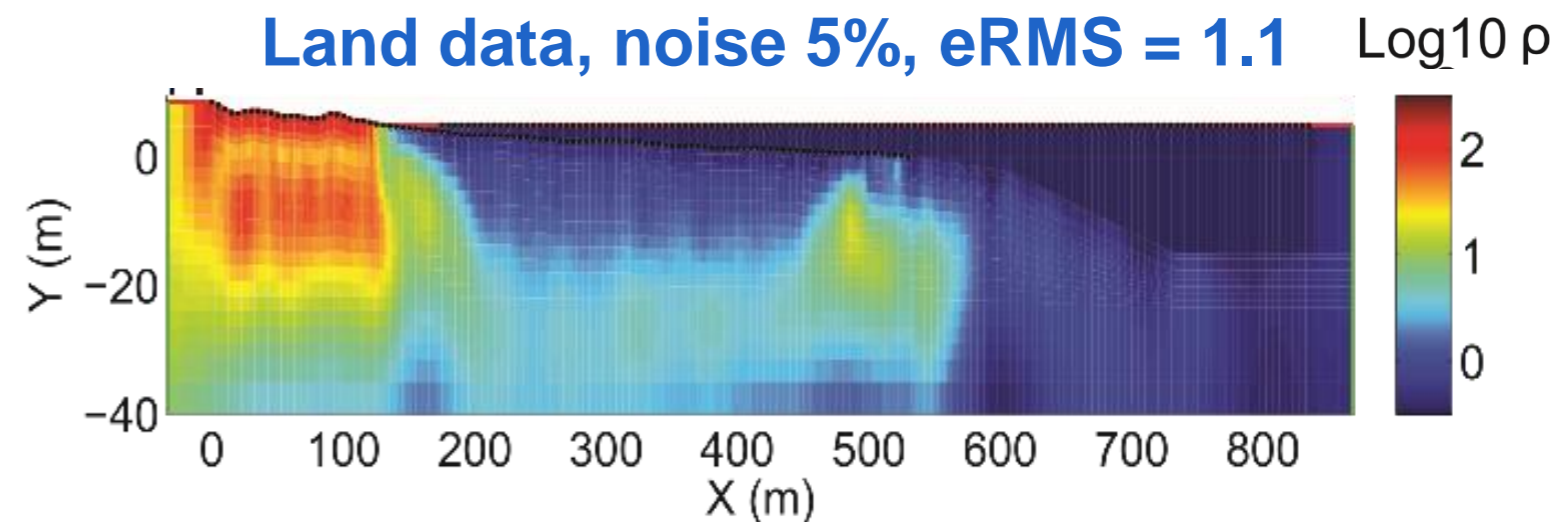


Apparent increase of the relative noise level, because the average resistance decreases

Land data, noise 3%, eRMS = 1.8



Land data, noise 5%, eRMS = 1.1



Noise level of land data must be adapted during inversion to reach the expected noise level  
But few variations are observed in the resistivity model



# VALIDATION OF THE FRESHWATER DISCHARGE

