Isospin composition of the high-momentum fluctuations in nuclei from asymptotic momentum distributions

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Background: High-momentum nucleons in a nuclear environment can be associated with short-range correlations (SRC) that primarily occur between nucleon pairs. Observations and theoretical developments have indicated that the SRC properties can be captured by general quantitative principles that are subject to model-dependence upon quantification. The variations in the aggregated effect of SRC across nuclei, however, can be quantified in an approximately model-independent fashion in terms of the so-called SRC scaling factors that capture the aggregated effect of SRC for a specific nucleus A relative to the deuteron (A-to-d).

Purpose: Provide predictions for the SRC scaling factors across the nuclear periodic table and determine the relative contribution of the different nucleon pair combinations to this quantity. Determine the SRC scaling factors for both bound protons and bound neutrons and study how these quantities evolve with the neutron-to-proton $(\frac{N}{Z})$ ratio in asymmetric nuclei.

Methods: We employ the low-order correlation operator approximation (LCA) to compute the SRC contribution to the single-nucleon momentum distribution and ratios of A-to-d momentum distributions. We do this for a sample of fifteen nuclei from He to Pb thereby gaining access to the evolution of the SRC scaling factor with the nuclear mass $4 \le A \le 208$ and the neutron-to-proton ratio $1.0 \le \frac{N}{Z} \le 1.54$.

Results: We provide evidence for approximate A-to-d scaling of the single-nucleon momentum distribution at nucleon momenta exceeding about 4 fm⁻¹. For the studied sample of fifteen nuclei, the total SRC scaling factor is in the range 4.05-5.14 of which roughly 3 can be attributed to proton-neutron (pn) correlations. The SRC scaling factors receive sizeable contributions from pp and nn correlations. They depend on the $\left(\frac{N}{Z}\right)$ ratio reflecting the fact that the minority species (protons) becomes increasingly more short-range correlated with increasing $\left(\frac{N}{Z}\right)$. We compare the computed SRC scaling factors in the LCA with those of ab-initio calculations and with measured quantities from SRC-sensitive inclusive electron-scattering data.

Conclusions: It is shown that the LCA provides predictions for the SRC scaling factors across the nuclear table that are in line with measured values. In asymmetric nuclei there are sizeable differences between the SRC scaling factors for protons and neutrons. It is suggested that this phenomenon may impact the variations of the magnitude of the European muon collaboration (EMC) effect across nuclei. Our results corroborate the finding that SRC physics can be qualitatively understood by universal principles that build on local modifications of mean-field wave functions of nucleon pairs.

I. INTRODUCTION

Nuclear short-range correlations (SRC) are a primary source of high-momentum and high-energy spatiotemporal fluctuations in atomic nuclei. They are connected to nucleon-pair correlations in nuclei and induce dynamical effects that go beyond the independentnucleon picture of atomic nuclei [1–4]. Throughout the last decade an improved quantitative understanding of SRC has been accomplished thanks to concerted experimental efforts in exclusive and semi-exclusive electronscattering reactions of nuclei under peculiar kinematics. The analysis of A(e, e'pp), A(e, e'np) [5] and A(e, e'N)reactions has for example provided detailed information on the isospin dependence [5–9], on the quantum numbers [10], and on the center-of-mass motion [11, 12] of short-range correlated nucleon pairs.

There are also two known classes of inclusive electronscattering A(e, e') reactions that have been connected to SRC. In both situations the aggregated impact of SRC in nucleus A is determined relative to the deuteron d and involves the observation of a scaling mechanism of the ratio of the cross sections on A relative to d. Both classes, however, refer to different resolution scales and nucleonmomentum conditions. These physical conditions are commonly quantified by the virtuality $Q^2 = -q_{\mu}q^{\mu}$ of the exchanged virtual photon (four-momentum $q^{\mu}(\omega, \vec{q})$ in the laboratory frame) in the electron-nucleus interaction, and the Lorentz scalar known as the Bjorken-Feynman variable $x = \frac{Q^2}{2M_N\omega}$, with M_N the nucleon mass.

• First, it has been observed that in well-selected kinematics [13]—namely sufficiently small resolution scales and x values $1.5 \leq x \leq 1.9$ that single out virtual-photon absorption on nucleon pairs—the A-to-d (e, e') cross sections approximately scale. The extraction of the scaling factor

$$a_2^{exp}(A) = \frac{2}{A} \frac{\sigma^A(e, e')}{\sigma^d(e, e')} \quad (1.5 \lesssim x \lesssim 1.9 \; ; \; Q^2 \approx 2 \; \text{GeV}^2) \; ,$$
(1)

has been the subject of intense experimental campaigns. To our knowledge, the $a_2^{exp}(A)$ have been measured [14–16] for nine target nuclei: ³He, ⁴He, ⁹Be, ¹²C, ²⁷Al, ⁵⁶Fe, ⁶³Cu, ¹⁹⁷Au, ²⁰⁸Pb.

• The European muon collaboration (EMC) effect refers to the observation that at resolution scales

that probe partons $(Q^2 \gtrsim 5 \text{ GeV}^2)$ and conditions $0.2 \lesssim x \lesssim 0.7$ (moderate- to high-momentum quarks), the ratio of the nucleon-weighted cross sections $\frac{2}{A} \frac{\sigma^A(e,e')}{\sigma^d(e,e')}$ depends on the target nucleus. This observation is commonly parameterized by means of the quantity

$$b_{2}^{exp}(A) \equiv -\frac{dR_{EMC}(A, x)}{dx} \\ = -\frac{d\left(\frac{2F_{2}^{A}(x, Q^{2})}{AF_{2}^{d}(x, Q^{2})}\right)}{dx} \\ \left(0.2 \lesssim x \lesssim 0.7 \; ; \; Q^{2} \gtrsim 5 \; \text{GeV}^{2}\right) \; , \quad (2)$$

where one has that $\sigma^A(e, e') \sim F_2^A(x, Q^2)$. The $b_2^{exp}(A)$ have been measured for the same nine target nuclei for which $a_2^{exp}(A)$ data are available. It came as a rather big surprise [17–19] that within the error bars the size of the EMC effect parameterized by $b_2^{exp}(A)$ is roughly linearly correlated with the measured values of $a_2^{exp}(A)$.

As it is inherently challenging to compute the coefficients $b_2^{exp}(A)$ and $a_2^{exp}(A)$ from ratios of computed $\sigma^A(e, e')$ and $\sigma^d(e, e')$ cross sections in selected but large ranges of phase space, one has resorted to alternate techniques to gain theoretical access to their values. It has been argued that theoretical predictions for the $a_2^{exp}(A)$ (and indirectly for the $b_2^{exp}(A)$) can be obtained by evaluating ratios of bound-nucleon probability distributions in the limits of vanishing relative distance r_{12} , or equivalently, infinitely high relative momentum p_{12}

$$a_2(A) = \lim_{r_{12} \to 0} \frac{\rho^A(r_{12}, \Lambda)}{\rho^d(r_{12}, \Lambda)} , \qquad (3)$$

$$a_2(A) = \lim_{p_{12} \to \infty} \frac{n^A(p_{12}, \Lambda)}{n^d(p_{12}, \Lambda)} .$$
 (4)

Here, the $\rho^A(r_{12}, \Lambda)r_{12}^2 dr_{12}$ is related to the probability to find a nucleon pair in A with a relative separation $r_{12} = |\vec{r_1} - \vec{r_2}|$ in the interval $[r_{12}, r_{12} + dr_{12}]$. Similarly, the $n^A(p_{12}, \Lambda)p_{12}^2 dp_{12}$ is related to the probability to find a nucleon pair in A with a relative momentum $p_{12} = |\vec{p_1} - \vec{p_2}|$ in the interval $[p_{12}, p_{12} + dp_{12}]$. The validity of the Eqs. (3) and (4) is very much based on the idea that the very short internucleon behavior in nuclei is characterized by universal functions that simply differ across nuclei by a scaling factor that relates to the measured $a_2^{exp}(A)$. In coordinate space this property can be captured by the factorization expression

$$\rho_{NN'\in\{\text{pn, pp, nn}\}}^{A}(r_{12} \lesssim r_{\Lambda}, \Lambda)$$

$$\approx C_{NN'}^{A}(\Lambda) |\psi_{NN'}(r_{12}, \Lambda)|^{2} .$$
(5)

Hereby, r_{Λ} is of the order of 1 fm. Its precise value is connected with the ultraviolet regulator scale Λ implicit for a particular nucleon-nucleon interaction model and the larger Λ the smaller r_{Λ} [20]. Further, the variation across

nuclei is contained in the factor $C^A_{NN'}(\Lambda)$, whereby the index NN' accounts for variations in the scaling factors across the different types of nucleon pairs. The quantities $C^A_{NN'}(\Lambda)$ are often referred to as the "contacts" for NN' pairs [21–24]. The distributions in the Eqs. (3) and (4) are model-dependent [20, 25], an aspect that is highlighted by the label Λ . By evaluating A-to-d ratios as in Eqs. (3) and (4), however, one can gain access to quantities that are approximately model-independent and forge connections with measured quantities. The model independence of the ratio of Eqs. (3) can be intuitively understood by realizing that for a given nucleon-nucleon interaction the highly local positional neighbourhood of a nucleon in nucleus A is not very different from the one of a nucleon in the deuteron.

A major challenge is to isolate the generative mechanisms in the scaling factors $a_2^{exp}(A)$ and $b_2^{exp}(A)$. For example, the isospin dependence of the size of the EMC effect $b_2^{exp}(A)$ provides access to the important issue of the flavor dependence in nuclear quark distributions [26, 27], and has been a subject of recent debates [16, 28, 29]. Access to these issues can be gained from determining the contribution of the different nucleon pair combinations to the short-distance modifications of nucleons embedded in a nuclear environment. This is the major topic of investigation in this paper.

Ab-initio low-energy nuclear theory has been used to compute the $a_2(A)$ for a number of light nuclei with $A \leq A$ 40 [20, 30]. The calculations use advanced importancesampling based quantum many-body theories [31–33] in combination with various forms of nucleon-nucleon (NN) interactions to determine the $\lim_{r_{12}\to 0} \frac{\rho^A(r_{12},\Lambda)}{\rho^d(r_{12},\Lambda)}$ of Eq. (3). These calculations have also shed light on the appropriateness of the expression (3) and the sensitivity to the adopted model " Λ ". The ⁴⁰Ca result in Figure 3 of [20] has illustrated that the proposed A-to-dscaling for the relative density distribution at very short internucleon distances is approximate. Also the shrinking size of phase space for $\lim_{r_{12}\to 0}$ poses challenges for the importance-sampling techniques. The (generalized) contact formalism [21–24, 34] builds on the Eq. (5) to construct pair-density functions and correlation functions for the pp, nn and pn pairs. The contact formalism can be applied to heavy nuclei (A > 40) but requires input from either data [5] or from computed momentum distributions [22, 24]. As A > 40 ab-initio calculations are not available, no systematic predictions for the SRC scaling factor for medium-heavy and heavy nuclei have been produced so far.

The low-order correlation operator approximation (LCA) as proposed in [35, 36] is an alternate approximate method to compute the impact of SRC on nuclear momentum distributions. Recently, we have shown [36] that LCA can reproduce the major trends of the observed N/Z dependence of SRC [9]. In line with the results of alternate calculations [37, 38], LCA accounts for the fact that through the operation of the tensor force, the minority component (protons) is substantially more correlated



Figure 1. Schematic representation of the dominant contributions to the single-nucleon momentum distribution $n^A(\vec{p})$ (defined in diagram (a)) in LCA. The $n^A(\vec{p})$ quantifies the probability of removing from the nuclear ground state a momentum \vec{p} at a certain location \vec{r} and putting it instantly back at another location \vec{r}' for all possible combinations of \vec{r} and \vec{r}' . The black dashed lines denote IPM nucleons: they are characterized by their isospin $N, N' \in \{p, n\}$ and other IPM quantum numbers α, β . The purple dotted lines denote the correlation operators in Eq. (8). Diagram (b) is the IPM contribution expressed in the format of Eq. (13). The IPM contribution dominates for $p < p_F$. Diagram (c) represents one of the SRC contributions between nucleon pairs (see Eq. (11)) and provides the bulk of the strength to $n^A(\vec{p})$ for $p > p_F$.

than the majority component (neutrons) in asymmetric nuclei.

In this work we present a systematic study of the SRC scaling factors based on the asymptotic high-momentum behavior of single-nucleon momentum distributions computed in LCA. We include fifteen nuclei in our study, including eight for which $a_2^{exp}(A)$ and $b_2^{exp}(A)$ data is available. One of the major goals of the presented study is to uncover the trends in the isospin (flavor) composition of the high-momentum (short-distance) behavior of nuclei. To this end, we have included both symmetric $(\frac{N}{Z} = 1)$ and asymmetric $(\frac{N}{Z} > 1)$ nuclei providing a window on asymmetric neutron-rich matter [39]. The selection of nuclei was not random but was made on the basis of reaching a good coverage of both the mass dependence $(4 \le A \le 208)$ and the neutron-to-proton dependence $(1 \le \frac{N}{Z} \le 1.54)$ of SRC. The four symmetric nuclei that are contained in our study are: ⁴He, ¹²C, ¹⁶O, ⁴⁰Ca. The eleven asymmetric ones are ⁹Be, ²⁷Al, ⁴⁰Ar, ⁴⁸Ca, ⁵⁶Fe, ⁶³Cu, ⁸⁴Kr, ¹⁰⁸Ag, ¹²⁴Xe, ¹⁹⁷Au, ²⁰⁸Pb. With the presented calculations we can also address questions like (i) the degree of validity of the scaling behavior of the Eq. (4)and, (ii) in how far the short-distance modifications affect protons and neutrons differently in asymmetric nuclear matter.

In what follows, Sec. II A introduces the LCA method for computing the SRC contribution to single-nucleon momentum distributions. In Section II B we discuss the pair composition of the SRC part of the nucleon momentum distributions and forge connections to measured quantities from exclusive electroinduced two-nucleon knockout. In Sec. II C we proceed with presenting and discussing the LCA results for the SRC scaling factors for 15 nuclei. We have included checks and balances and compared the computed SRC scaling factors with both data and theoretical results of ab-initio calculations. We also conduct robustness checks of the presented methodology by testing the sensitivity of the SRC scaling factors to the momentum range that determines the "asymptotic part" of the single-nucleon momentum distribution. Section IID focuses on the differences in the SRC scaling factors for proton and neutrons in asymmetric nuclei. In Sec. II E we exploit the conjectured relationship between the size of the EMC effect and the SRC scaling factors to shed light on the isospin dependence of the underlying (unknown) generative mechanisms.

II. FORMALISM AND RESULTS

A. Single-nucleon momentum distributions

The LCA is a methodology with applications in nuclear reactions and nuclear structure. In LCA one can compute the observables for SRC dominated nucleon knockout reactions [10, 40–43]. Furthermore, the impact of SRC on nuclear momentum distributions [35, 36] can be quantified across the nuclear mass range as even for the heaviest nuclei the numerical calculations are manageable. Central to the results of this work is the singlenucleon momentum distribution that is generally defined as

$$n^{A}(\vec{p}) \sim \langle \Psi_{A} | a^{\dagger}_{\vec{p}} a_{\vec{p}} | \Psi_{A} \rangle , \qquad (6)$$

with $|\Psi_A\rangle$ the ground-state wave function of nucleus A. In LCA, the complexity of the calculation is shifted from the wave functions to the operators. The complicated $|\Psi_A\rangle$ is obtained from a simple wave function $|\Phi_A\rangle$ through the action of an operator

$$|\Psi_A\rangle = \frac{1}{\sqrt{\langle \Phi_A | \,\widehat{\mathcal{G}}^{\dagger}\widehat{\mathcal{G}} | \Phi_A \rangle}} \widehat{\mathcal{G}} \, |\Phi_A\rangle \,\,, \tag{7}$$

where $|\Phi_A\rangle$ is a Slater determinant wave function for nucleus A and $\widehat{\mathcal{G}}$ an operator that accounts for the SRC correlations. In LCA, we account for the central (Jastrow), tensor and spin-isospin SRC correlations

$$\widehat{\mathcal{G}} = \widehat{\mathcal{S}} \left(\prod_{i < j=1}^{A} \left[1 - g_c(r_{ij}) + f_{t\tau}(r_{ij}) \widehat{S}_{ij} \vec{\tau}_i \cdot \vec{\tau}_j \right. \\ \left. + f_{\sigma\tau}(r_{ij}) \vec{\sigma}_i \cdot \vec{\sigma}_j \vec{\tau}_i \cdot \vec{\tau}_j \right] \right) \\
= \widehat{\mathcal{S}} \left(\prod_{i < j=1}^{A} \left[1 + \widehat{\mathcal{G}}_{ij}(r_{ij}) \right] \right),$$
(8)

where \widehat{S} and \widehat{S}_{ij} are the symmetrization and tensor operator. In computing the $n^A(\vec{p})$ in LCA all terms are included up to order $\mathcal{O}(\mathcal{G}^2)$ which implies that the impact of SRC on $n^A(\vec{p})$ is included as two-body operators. The momentum distribution $n^A(\vec{p})$ is then the sum of two terms (see also the diagrams (b) and (c) of Fig. 1)

$$n^{A}(\vec{p}) = n^{A}_{\text{IPM}}(\vec{p}) + n^{A}_{\text{SRC}}(\vec{p}) + \mathcal{O}(\mathcal{G}^{3}) .$$
(9)

The first term n_{IPM}^A (IPM stands for independent particle model) is reminiscent of independent nucleons

$$n_{\rm IPM}^A(\vec{p}) \sim \sum_{N \in \{\rm p,n\}} \sum_{\alpha} \langle N\alpha | \, a_{\vec{p}}^\dagger \, a_{\vec{p}} \, | N\alpha \rangle \ , \tag{10}$$

where α extends over all occupied single-particle states in the Slater determinant $|\Phi_A\rangle$. The second term is the result of the SRC operators of Eq. (8). It is determined by two-nucleon contributions of which the dominant contribution is of the form (see also diagram of Fig. 1(c))

$$n_{\mathrm{SRC}}^{A}(\vec{p}) \sim \sum_{NN' \in \{\mathrm{p,n}\}} \sum_{\alpha\beta} \sum_{\vec{K} \ \vec{k} \ \vec{k'}} \widehat{\mathcal{G}}_{12}^{\dagger} \left(\frac{\vec{K}}{2} + \vec{k} - \vec{p} \right) \widehat{\mathcal{G}}_{12} \left(\frac{\vec{K}}{2} + \vec{k'} - \vec{p} \right) \\ \times \langle N\alpha, N'\beta | a_{\frac{\vec{K}}{2} + \vec{k}}^{\dagger} a_{\frac{\vec{K}}{2} - \vec{k}}^{\dagger} a_{\frac{\vec{K}}{2} - \vec{k'}}^{\dagger} | N\alpha, N'\beta \rangle .$$

$$(11)$$

For the sake of simplicity of the notation we make abstraction of the spin- and isospin dependence of the above two-body matrix elements. Note that in computing the $n_{\rm SBC}^A(\vec{p})$ one integrates over the center-of-mass momentum \vec{K} of the correlated pair, as well as over the relative momenta \vec{k} and $\vec{k'}$. The neglected terms of order $\mathcal{O}(\mathcal{G}^3)$ in Eq. (9) include three-body correlations. The computation of those terms across the nuclear mass table is computationally prohibitive. There are indications, however, that the effect of three-nucleon correlations in the tail part of the $n^A(\vec{p})$ is relatively small. Direct evidence comes from nuclear-matter calculations where the impact of three-nucleon effects has been studied [44]. Indirect theoretical evidence for the dominant role of two-nucleon correlations stems from the fact that QMC calculations for light nuclei, that include all possible diagrams, provide strong indications for A-to-d scaling in the tail part of $n^{A}(\vec{p})$ [33].

We restrict ourselves to spherically symmetric nuclei $n_{\text{SRC}}^A(p) \sim n_{\text{SRC}}^A(\vec{p})$. Of high relevance for the isolation of the isospin composition of SRC is that both contributions (10) and (11) to $n^A(p)$ can be written as a sum of four terms

$$n^{A}(p) \equiv \underbrace{n^{A}_{\rm pp}(p) + n^{A}_{\rm pn}(p)}_{n^{A}_{\rm p}(p) \, (\text{proton part})} + \underbrace{n^{A}_{\rm nn}(p) + n^{[1]}_{\rm nn}(p)}_{n^{A}_{\rm n}(p) \, (\text{neutron part})} \,. \tag{12}$$

As schematically shown in Fig. 1 the separation in the four pair combinations can done for both the IPM and the SRC contribution in Eq. (9). For the SRC contribution of Eq. (11) the pairs $N\alpha$, $N'\beta$ in the matrix elements give

rise to the four pair combinations considered. In order to identify the pair combinations to the IPM contribution, one can rewrite Eq. (10) as

$$n_{\rm IPM}^{A}(\vec{p}) \sim \sum_{N \in \{\rm p,n\}} \sum_{N' \in \{\rm p,n\}} \sum_{\alpha} \sum_{\beta} \sum_{\vec{p}'} \times \langle N\alpha | a_{\vec{p}}^{\dagger} a_{\vec{p}} | N\alpha \rangle \langle N'\beta | a_{\vec{p}'}^{\dagger} a_{\vec{p}'} | N'\beta \rangle$$
(13)

Herein, the summations $\sum_{N \in \{p,n\}} \sum_{N' \in \{p,n\}} give natu$ rally rise to four pair combinations. Note that in iden $tifying the different pair combinations to <math>n^A(p)$ in the IPM, one integrates over the momentum of the second nucleon $N'\beta$. We adopt the normalization convention $\int dp \ p^2 n^A(p) = A$. In the adopted LCA, the four pair combinations stemming from pp, pn, nn and np contribute respectively a fraction $\frac{Z(Z-1)}{(A-1)}$, $\frac{NZ}{(A-1)}$, $\frac{N(N-1)}{(A-1)}$ and $\frac{NZ}{(A-1)}$ to the total norm A of $n^A(p)$. These normalisations are not artificially imposed but obtained by expanding the matrix element of $\langle \Phi_A | \hat{\mathcal{G}}^{\dagger} \hat{\mathcal{G}} | \Phi_A \rangle$ in the denominator in Eq. (7) up to the second order in the correlation operator [35]. One finds

$$\langle \Phi_A | \, \widehat{\mathcal{G}}^{\dagger} \widehat{\mathcal{G}} \, | \Phi_A \rangle = A + \mathcal{C}_A + \mathcal{O} \left(\mathcal{G}^3 \right) \,, \qquad (14)$$

where C_A can be interpreted as a measure for the aggregated effect of SRC in nucleus A(N,Z) [35].

Of great relevance for reactions involving nuclear targets is the probability distribution

$$P^{A}(p) = p^{2} n^{A}(p) / A \quad \left(\int dp P^{A}(p) = 1 \right)$$
(15)

to find a nucleon with momentum p in A(N,Z). An immediate consequence of Eq. (12) is that

$$P^{A}(p) = \underbrace{P^{A}_{pp}(p) + P^{A}_{pn}(p)}_{P^{A}_{p}(p) \text{ (proton part)}} + \underbrace{P^{A}_{nn}(p) + P^{A}_{np}(p)}_{P^{A}_{n}(p) \text{ (neutron part)}} .$$
(16)

The correlation functions in Eq. (8) are input to the LCA approach. We adopt a data-driven methodology and use a set that has been systematically tested in comparisons of reaction-model calculations and SRC-driven data [10, 45–47]. The $f_{t\tau}(r_{12})$ and $f_{\sigma\tau}(r_{12})$ correlation functions are from a variational calculation [48]. An analysis of ${}^{12}C(e, e'pp)$ [45] and ${}^{16}O(e, e'pp)$ [47] experimental results systematically excluded "soft" central correlation functions g_c and preferred a "hard" $g_c(r_{12})$ inferred from a G-matrix calculation with the Reid soft-core interaction in nuclear matter [49].

Different interactions generate different correlations – particularly for the central ones– and are sources of theoretical uncertainties in LCA. In Ref. [36] we have presented LCA results with the "hard" g_c from [49] and the "soft" g_c from [48] that is consistent with the adopted $f_{t\tau}$ and $f_{\sigma\tau}$. The choice of the g_c mainly affects the highest momentum parts of the single-nucleon momentum distributions. We found, however, that for light and mediumheavy nuclei the LCA in combination with the "hard" g_c produces $n^A(\vec{p})$ that are in line with those from quantum Monte Carlo calculations with the effective AV18 NN interaction. In addition, many extracted SRC properties are obtained from ratios of $n^A(\vec{p})$ for which the sensitivity to the choice of the g_c is at the percent level [36].

In this work, all calculations are performed in coordinate space with a "hard" g_c and harmonic oscillator (HO) single-particle states $|N\alpha\rangle$ as they offer the possibility to separate the pair's relative and c.m. motion in the pair wave functions $|N\alpha, N'\beta\rangle$ of Eq. (11) with the aid of Moshinsky brackets. As the major purpose of this study is to determine the systematic properties of the SRC scaling factors and their pair composition, we use the HO parameters from the global parameterization $\hbar\omega = 45A^{-\frac{1}{3}} - 25A^{-\frac{2}{3}}$. More advanced calculations could find the optimum HO parameter for each specific nucleus but this complication is beyond the scope of the current paper. It has been numerically shown [11, 35, 40, 42, 50] and experimentally confirmed [10, 47] that the major source of SRC strength stems from correlation operators acting on IPM pairs in a nodeless relative S-state. This can be intuitively understood by noting that the probability of finding close-proximity IPM pairs is dominated by pairs in a nodeless relative S-state. Those S wave functions are not very sensitive to the details of the meanfield potential which partially explains the robustness of the SRC properties in nuclei.

Figure 2 displays the probability distributions $P^A(p)$ of Eq. (16) for four nuclei out of our sample of fifteen nuclei. In essence, there are two separated momentum regimes in the probability distributions. The underlying generative dynamics for the observed p dependence has been discussed in great detail in Refs. [35, 36]. Summarizing, the low-momentum part is reminiscent of the independentparticle model. The high-momentum regime is characterized by a fat tail that displays a universal momentum dependence across the different nuclei. The pair composition of the low-momentum regime is roughly determined by the combinatorics imposed by the neutron and the proton numbers N and Z. In the SRC regime, on the other hand, there is an obvious proton-neutron dominance. As one approaches the highest momenta studied here, the proton-proton and neutron-neutron parts gain in relative importance relative to the dominant pn contribution. There is a degree of model-dependence in the probability distributions $P^{A}(p)$ of Fig. 2 [25, 36, 51]. Inclusion of SRC physics through the operators of Eq. (8)preserves the long-distance physics which makes the momentum dependence of the probability distributions below the Fermi momentum $p_F = 1.25 \text{ fm}^{-1}$ to be independent of the choices made with regard to the correlation operators. For $p < p_F$ the major effect of the SRC correlations is to deplete the $P^A(p < p_F)$ with a scaling factor that is model-dependent. As we have shown in Ref. [36] the high-momentum tail $P^A(p \gtrsim 2 \text{ fm}^{-1})$ displays some sensitivity to the choices made with respect to the correlation functions. For ⁴⁰Ca —the heaviest nuclei for which ab-initio momentum distributions are available we can compare the LCA result for $P^{A}(p)$ with the one obtained with quantum Monte-Carlo methods using a realistic phenomenological NN interaction [33]. We observe a fair agreement providing confidence in our approach. In the following Sec. IIB we connect the LCA predictions for the pair composition of the SRC tail of $P^{A}(p)$ to recent A(e, e'np) and A(e, e'pp) data.

B. Tail part of single-nucleon momentum distributions

The relative weight of the pp and pn correlations in the tail of the momentum distribution can be "measured" by evaluating the ratio of the triple-coincidence A(e, e'pp) and A(e, e'np) cross sections in a large-acceptance detector thereby probing a large fraction of the phase space and imposing kinematical cuts selecting initial 2N SRC pairs [5]. This amounts to evaluating a cross-section ratio of the form

$$\frac{\sigma_{en}}{2\sigma_{ep}} \frac{\sigma_A(e, e'pp)}{\sigma_A(e, e'np)} \sim \frac{\text{Probability for pp SRC pair in A}}{\text{Probability for pn SRC pair in A}} .$$
(17)

Here, σ_{ep} (σ_{en}) denotes the off-shell electron-proton (electron-neutron) cross section and $\sigma_A(e, e'NN')$ is the cross section for NN' knockout [where typically the "fast" nucleon has $p_N \gg p_F$ and the recoil nucleon of the SRC pair has $p_{N'} = \mathcal{O}(p_F)$] aggregated over a certain initial-nucleon momentum range. The above ratio of probabilities can be made conditional on certain constraints for example with regard to the initial nucleon



Figure 2. The probability distribution $P^{A}(p)$ to find a nucleon with momentum p as computed in LCA for four nuclei. The separate contributions from the four possible NN' combinations detailed in Eq. (16) are shown together with the total. For ⁴⁰Ca we compare the LCA result for $P^{A}(p)$ with the one from the Argonne group obtained with the effective AV18 nucleon-nucleon interaction [33].



Figure 3. The nuclear mass dependence of the ratios (in percent units) of pp-to-pn SRC correlated pairs in two momentum ranges above the Fermi momentum p_F . The blue circles are LCA predictions based on the ratio of the pp and pn contributions to the $P^A(p)$ in the selected momentum ranges. The data are from Ref. [5].

momenta where the picture is adopted that the "fast" nucleon N has absorbed the virtual photon. As experiments probing SRC quantities often tag the momentum of the "active" nucleon and require events with an inactive A-2 core, the single-nucleon momentum distribu-

tion (see diagram (c) in Fig. 1) offers many opportunities for theory-experiment comparisons [36]. The theoretical

counterpart of the ratio (17) reads

$$C \frac{\int_{p_l}^{p_h} dp P_{\rm pp}^A(p)}{\int_{p_l}^{p_h} dp \left[P_{\rm np}^A(p) + P_{\rm pn}^A(p) \right]} , \qquad (18)$$

where p_l and p_h are determined by the experimental cuts for the inferred initial-nucleon momenta. The ratio of Eq. (17) has recently been measured for carbon, aluminium, iron and lead for two initial momentum ranges $[p_l, p_h]$ [5]. We use Eq. (18) to compare those data to the LCA predictions. The results for the other 11 nuclei in our sample provide more detailed information about the variations across nuclei. The results of the theoryexperiment comparisons are summarized in Fig. 3. Apart from effects stemming from detector efficiencies for example, an important contribution to the factor \mathcal{C} in the above equation are the final-state interactions (FSI). Attenuation will roughly equally affect protons and neutrons at the kinetic energies considered [52]. Singlecharge exchange (SCX), however, is an important correction factor [42] when extracting SRC information for two-nucleon knockout reactions. Indeed a considerable amount of detected pp knockout events originate from virtual-photon absorption on pn SRC pairs. In Fig. 3 an overall reduction factor $\mathcal{C} = 0.5$ in the theoretical ratio of Eq. (18) is used. In line with the data, the LCA predictions for the number of pp-to-pn SRC pairs is fairly constant along the fifteen nuclei in our sample and increases with increasing nucleon momentum. For a fixed momentum range, the variation in the predicted pp-topn SRC pair ratios across nuclei is of the order of few percent in line with the experimental observations.

The experimentally determined $a_2^{exp}(A)$ of Eq. (1) is extracted from ratios of A-to-d(e, e') cross section ratios. In the impulse approximation those cross sections can be computed by integrating the phase-space weighted momentum distributions over selected ranges \mathcal{R} determined by experimentally imposed conditions

$$a_2^{exp}(A) = \frac{2}{A} \frac{\sigma^A(e, e')}{\sigma^d(e, e')} \sim \frac{2}{A} \frac{\int_{\mathcal{R}} dp p^2 n^A(p)}{\int_{\mathcal{R}} dp p^2 n^d(p)} \sim \frac{\int_{\mathcal{R}} dp P^A(p)}{\int_{\mathcal{R}} dp P^d(p)}$$
(19)

Here, \mathcal{R} is the momentum-range that corresponds to high initial-nucleon momenta and constant A-to-d (e, e') cross sections. As those conditions can be associated with the tail part of the probability distributions of Fig. 2, an estimate of the $a_2^{exp}(A)$ of Eq. (19) can be obtained from the ratio of the weight in the tail parts of the computed $P^A(p)$

$$a_2(A) = \frac{\int_{p>2 \text{ fm}^{-1}} dp P^A(p)}{\int_{p>2 \text{ fm}^{-1}} dp P^d(p)} .$$
(20)

With the aid of the decomposition (16) the contribution of the pp, nn and pn+np pairs to the numerator can be computed and the isospin composition of the SRC can be quantified. The denominator of Eq. (20) accounts for the weight of the tail part of the deuteron momentum



Figure 4. LCA results for the the SRC scaling factors $a_2(A)$ (orange open diamonds) along with the separate pp (blue open triangles), nn (brown stars) and pn (purple solid circles) contributions plotted versus atomic weight A. The shaded regions mark the pn (blue) and the pp+nn (green) contributions. All results are computed from the A-to-d weight of the tail part ($p > 2 \text{ fm}^{-1}$) of the nucleon probability distribution $P^A(p)$ [see Eq. (20)]. All $P^A(p)$ (including the deuteron one) are computed in LCA. The $a_2^{exp}(A)$ data are from the extended data tables of Ref. [16] and include data from Ref. [15].

distribution. Obviously, this number is model dependent [51, 53]. For example, with the AV18 (LCA) deuteron momentum distribution the denominator is 0.127 (0.103)which corresponds with the tail part carrying about 10-13% of the total probability in the deuteron. In Fig. 4 we present results of the above ratio for the 15 nuclei in our sample. For reasons of consistency, the deuteron probability distribution used is also computed in LCA. From ${}^{4}\text{He}$ to ${}^{208}\text{Pb}$ the SRC scaling factor as computed with the aid of the Eq. (20) has an increment of about 25% — from ≈ 3.8 to ≈ 4.8 — indicative of a very soft A-dependence that is also observed in the data. The soft A-dependence of the a_2 can be intuitively understood by considering that a_2 is determined by the local neighborhood of a nucleon. For light nuclei and increasing $A \lesssim 20$ the local neighborhood gradually fills up to reach approximate saturation for $A \gtrsim 20$. In the A-to-d ratio the pn+np contribution is about 70% of the total value and the pp part is of the order of 10%. For $\frac{N}{Z} = 1$ the pp and nn parts equally contribute. For ¹⁹⁷Au and ²⁰⁸Pb, the two most asymmetric nuclei in our sample, the nn contribution approaches 20% of the total. These numbers are to be compared to $\frac{N(N-1)}{A(A-1)} = 0.36$ and 0.37, and is indicative for the isospin selectivity of the SRC. In comparing the LCA predictions to the data it is important to realize that there are corrections to be applied, for example stemming from the center-of-mass motion of the NN pairs [15, 54] and the fact that in a finite nucleus pairs can have excitation energies [55]. These corrections require either a full reaction model or a detailed Monte

Carlo simulation and are outside the scope of this work.

C. Asymptotic single-nucleon momentum distributions and SRC scaling factors

In what follows we extract the SRC scaling factors a_2 from the asymptotic behavior of the A-to-d momentum distributions. The SRC scaling factors extracted from this method will be compared with those from Fig. 4 that use the aggregated weight in the SRC part of the $P^A(p)$. With this comparison we explore the sensitivity of our methodology to the choices made with regard to the limits of integration in the tail parts of the singlenucleon momentum distributions. We start with studying the momentum dependence of the A-to-d probability distributions to identify the momentum ranges for which an A-to-d scaling behavior emerges. In Fig. 5 we display the momentum dependence of the four ratios

$$\frac{P^{A}(p)}{P^{d}(p)}, \quad \frac{\left(P^{A}_{pn}(p) + P^{A}_{np}(p)\right)}{P^{d}(p)}, \quad \frac{P^{A}_{nn}(p)}{P^{d}(p)}, \quad \frac{P^{A}_{pp}(p)}{P^{d}(p)}$$

for our sample of fifteen nuclei. For each value of the momentum p, the $\frac{P^A(p)}{P^d(p)}$ provides the ratio of the pernucleon probability of finding a nucleon in A(N,Z) relative to the deuteron. Obviously, any deviation from one is a measure for the medium dependence of the nucleon probabilities. The increased A-to-d relative probability $\frac{P^A}{P^d}$ for $0.75 \lesssim p \lesssim 1.65 \text{ fm}^{-1}$ is connected to Fermi motion in finite nuclei. In that momentum range the pp, nn and pn contribute to $\frac{P^A}{P^d}$ roughly in accordance to their weight in $\frac{A(A-1)}{2}$. At $p \gtrsim 2.25$ fm⁻¹ one observes a plateau in the $\frac{P^A(p)}{P^d(p)}$ that extends to the highest momenta studied here. The plateau is characterized by an approximately universal momentum dependence of the A-to-dratio $\frac{P^{A}(p)}{P^{d}(p)}$ at high momenta. Variations across nuclei can be captured by an SRC scaling factor that depends on A(N,Z). The onset of a plateau in the high-momenta results of $\frac{P^A(p)}{P^d(p)}$ in Fig. 5 provide support for the use of Eq. (4) for extracting the SRC scaling factor. Indeed, in the limit of very high nucleon momenta relations between single-nucleon and two-nucleon momentum distributions can be established [22]. The major trends in the A-tod ratios of Fig. 5 are in line with those of a study for six nuclei with $A \leq 10$ reported in [22]. The numerical calculations of that study also identify the $p \gtrsim 4 \text{ fm}^{-1}$ region as the one suitable for extracting the A-to-d SRC scaling factor.

The SRC scaling factor extracted from the "highmomentum" ($p \approx 4.5 \text{ fm}^{-1}$) behavior of $\frac{P^A(p)}{P^d(p)}$ for the total probability distribution for ⁴He is about 4. For the lightest nuclei in our sample — ⁹Be, ¹²C, ¹⁶O, ²⁷Al the SRC scaling factor increases with A to reach the value of approximately 4.8 for ²⁷Al. Small increments in the high-momentum values of $\frac{P^A(p)}{P^d(p)}$ with increasing mass are observed for A > 27.

Yet a closer look at the pp, nn and pn+np contributions to the $\frac{P^A(p)}{P^d(p)}$ in Fig. 5 indicates that the onset of the high-momentum plateau is most outspoken for the pn+np parts. For the pp and nn contributions to $\frac{P^A(p)}{P^d(p)}$ the high-momentum scaling is not so pronounced as for the pn+np parts but there are indications that also these two ratios approximately saturate for $p \gtrsim 4 \text{ fm}^{-1}$. After all, this is not so surprising given that there is no such a thing as proton-proton and neutron-neutron correlations in the deuteron. Along the same lines, there are stronger variations for the pp and nn contributions to $\frac{P^A(p)}{P^d(p)}$ across nuclei than for the pn+np contribution. The variation in the pp and nn contribution to the A-to-d SRC scaling factor cannot be captured by an A-dependence and as will be discussed later on the N/Z ratio plays an important role. For the pn+np parts the A-to-d SRC corrections at nucleon momenta $p \gtrsim 4 \text{ fm}^{-1}$ are substantially larger than the corrections attributed to the Fermi motion in the 0.75 $\lesssim p \lesssim 1.65 \text{ fm}^{-1}$ range. For the pp and nn parts, on the other hand, the SRC A-to-d modifications are of the same order as the ones attributed to Fermi motion. Following up on the above discussion about the fact that the $\frac{P_{\rm pp}^A(p)}{P^d(p)}$ and $\frac{P_{\rm nn}^A(p)}{P^d(p)}$ plateaus are not really very flat at high nucleon momentum, we have confirmed that the corresponding $\frac{P_{\rm pp}^A(p)}{P^{4}_{\rm He}(p)}$ and $\frac{P_{\rm nn}^A(p)}{P^{4}_{\rm He}(p)}$ plateaus are far more flat.

The results of Fig. 5 provide support for extracting to A-to-d SRC scaling factor from the high-momentum behavior of the ratio

$$a_2(A) = \lim_{\text{high } p} \frac{P^A(p)}{P^d(p)} ,$$
 (21)

where "high p" stands for the momentum range for which a plateau in the A-to-d momentum distribution is visible. We stress that the above expression for $a_2(A)$ is similar in vein to the ones of Eqs. (3) and (4) that have been derived within the context of effective field theories (EFTs) [20, 30] and of the contact formalism [21, 23, 24]. The following results are computed in the spirit of the expression (21) whereby we have defined "high p" well in the asymptotic p region of the A-to-d momentum distributions (see Fig. 5). As is clear from Fig. 5 the plateau in the A-to-d probability distributions can be clearly identified for the dominant pn contribution. For the pp and nn parts, on the other hand, the A-to-d scaling is approximately realized but at the highest p there are indications for saturation. To this end, the "high-p limit" $\lim_{high p}$ of the A-to-d probability distributions of Eq. (21) was numerically evaluated by means of the ratios

$$a_2(A) = \lim_{\text{high } p} \frac{P^A(p)}{P^d(p)} \approx \frac{\int_{\Delta p^{\text{high }}} dp \ P^A(p)}{\int_{\Delta p^{\text{high }}} dp P^d(p)}$$
(22)

Similar expressions are used to evaluate the $\lim_{high p}$ of



Figure 5. The nucleon momentum dependence of the ratio of the single-nucleon momentum distribution for nucleus A relative to the deuteron. Ratios are shown for the total momentum distribution, the sum of the proton-neutron and neutron-proton contributions, the neutron-neutron and proton-proton contributions. All the nucleon momentum distributions (including the deuteron one) are computed in LCA. Note that the y-axis scale for the nn and pp contributions (bottom figures) is different from the one used for the "total" and "pn+pn" ones (top figures). The grey shaded area shows the momentum range where Fermi motion dominates the displayed A-to-d momentum distributions.

the ratios $\frac{P_{pq}^{A}}{Pd}$, $\frac{P_{nq}^{A}}{Pd}$, $\frac{P_{np}^{A}}{Pd}$, and $\frac{P_{pq}^{A}}{Pd}$. Based on the location of the occurrence of the plateaus in Fig. 5 the range Δp^{high} of high -p values is $\left[p_l^{\text{high}}, p_u^{\text{high}}\right]$ with $p_l^{\rm high}$ > 3.8 ${\rm fm}^{-1}$ and $p_u^{\rm high}$ < 4.5 ${\rm fm}^{-1}.$ In the process of selecting the boundaries of the range Δp^{high} we have also taken into consideration the good practice of keeping the nucleon momenta smaller than the nucleon mass in non-relativistic calculations. The range Δp^{high} is of the order of 100 MeV. There are some systematic uncertainties in our approach that are connected with the selection of the "high-momentum" regime. Referring to the results of Fig. 5 the highest uncertainty stems from the nn contribution. A very conservative estimate of the error induced by defining a "high-p" regime of the ratios of A-to-d is that it induces an uncertainty in the extracted a_2^p and a_2^n of the order of 0.50, which corresponds to an error of about 10%.

Figure 6 shows the SRC scaling factors as computed with the aid of the expression (22) for the fifteen nuclei in our sample. We provide the total SRC scaling factor as well as the separated proton-proton, neutron-neutron and proton-neutron contributions to it. The results can be compared with those of Fig. 4 that use the aggregated weight in the SRC part of the momentum distributions [Eq. (20)]. All-in-all the two methods to determine the SRC scaling factors $a_2(A)$ provide comparable predictions for all nuclei considered in this work. The method based on the evaluation of the high-p limit of $\frac{P^A(p)}{P^d(p)}$ tends to predict larger pp and nn contributions to $a_2(A)$. In essence, Figs. 4 and 6 use different ranges of integration $(p > 2 \text{ fm}^{-1} \text{ and } 3.8 to determine the <math>a_2(A)$. The difference between the extracted numbers can be seen as a measure for the sensitivity to the adopted ranges of integration in the tail parts of the single-nucleon momentum distributions.

Figure 7 compares the LCA results for a_2 using Eq. (21) with those from ab-initio calculations and data. Within the error bars the LCA results are compatible with those from ab-initio calculations and the data. For 40 Ca and 48 Ca we predict $a_2 = 4.99$ and $a_2 = 4.89$. The heaviest nucleus for which ab-initio results are available is 40 Ca and the LCA result of 4.99 compares well with the ab-initio result of 5.15 ± 0.67 . The LCA prediction for 12 C ($a_2 = 4.48$) is in line with the measured values: $a_2^{exp} = 4.49 \pm 0.17$ [16] and $a_2^{exp} = 4.75 \pm 0.16$ [17].

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Table I. Results for the proton and neutron SRC scaling factors a_2^p and a_2^n and related quantities as computed in LCA for a sample of 15 nuclei. The a_2^p and a_2^n are computed with the aid of the Eq. (25). The $-\frac{dR_{EMC}}{dx}$ are computed with the aid of the Eq. (28).

Nucleus	$\frac{N}{Z}$	a_2^p	a_2^n	$\frac{Za_2^p + Na_2^n}{A}$	a_2^{exp}	$\frac{Za_2^p - Na_2^n}{A}$	$-\frac{dR_{EMC}}{dx}$	b_2^{exp}
$^{4}\mathrm{He}$	1.00	4.05	4.05	4.05	3.60 ± 0.10 [17]	-0.00	0.268	0.207 ± 0.025 [56], 0.222 ± 0.045 [57]
$^{9}\mathrm{Be}$	1.25	4.37	3.97	4.15	3.91 ± 0.12 [17]	-0.26	0.336	0.326 ± 0.026 [56], 0.283 ± 0.028 [57]
$^{12}\mathrm{C}$	1.00	4.48	4.48	4.48	4.75 ± 0.16 [17]	-0.00	0.306	0.340 ± 0.022 [16], 0.285 ± 0.026 [56],
					4.49 ± 0.17 [16]			0.322 ± 0.033 [57]
^{16}O	1.00	4.73	4.73	4.73		-0.00	0.328	
$^{27}\mathrm{Al}$	1.08	4.83	4.69	4.76	4.83 ± 0.18 [16]	-0.10	0.354	0.347 ± 0.022 [16]
$^{40}\mathrm{Ar}$	1.22	5.15	4.72	4.92		-0.28	0.408	
40 Ca	1.00	4.99	4.99	4.99		-0.00	0.351	
48 Ca	1.40	5.33	4.59	4.89		-0.46	0.446	
$^{56}\mathrm{Fe}$	1.15	5.13	4.83	4.97	4.80 ± 0.22 [16]	-0.21	0.397	0.472 ± 0.023 [16], 0.391 ± 0.025 [57]
$^{63}\mathrm{Cu}$	1.17	5.01	4.80	4.89	5.21 ± 0.20 [17]	-0.29	0.407	0.391 ± 0.025 [57]
$^{84}\mathrm{Kr}$	1.33	5.38	4.77	5.03		-0.42	0.450	
$^{108}\mathrm{Ag}$	1.30	5.38	4.85	5.08		-0.39	0.449	
$^{124}\mathrm{Xe}$	1.30	5.42	4.92	5.14		-0.41	0.458	
$^{197}\mathrm{Au}$	1.49	5.34	4.98	5.12	5.16 ± 0.22 [17]	-0.84	0.554	0.511 ± 0.030 [57]
$^{208}\mathrm{Pb}$	1.54	5.64	4.77	5.11	$4.84 \pm 0.20 \ [16]$	-0.66	0.513	0.539 ± 0.020 [16]

D. Proton and neutron SRC scaling factors for symmetric and asymmetric nuclei

In an asymmetric $N \neq Z$ nuclear environment one can anticipate that the A-to-d SRC scaling factors are different for protons and neutrons [36]. In order to quantify this and gain better insight into the $\frac{N}{Z}$ dependence of the SRC scaling factors we introduce

$$a_{2}(A) = \lim_{\text{high } p} \frac{P^{A}(p)}{P^{d}(p)} = \lim_{\text{high } p} \frac{P_{p}^{A}(p) + P_{n}^{A}(p)}{P^{d}(p)}$$
$$\equiv \frac{Za_{2}^{p}(A) + Na_{2}^{n}(A)}{A}.$$
 (23)

We remind that with the adopted normalization conventions one has

$$\int dp P_{\rm p}^A(p) = \frac{Z}{A} , \quad \int dp P_{\rm n}^A(p) = \frac{N}{A} , \qquad (24)$$

and that for the deuteron we can formally write $P^d = P_p^d + P_n^d = 2P_p^d = 2P_n^d$. Rearranging the above equations leads to the definitions $a_2^p(A)$ and $a_2^n(A)$

$$a_2^p(A) = \lim_{\text{high } p} \frac{A P_p^A}{Z P_p^d} , \quad a_2^n(A) = \lim_{\text{high } p} \frac{A P_n^A}{N P_n^d} .$$
(25)

Accordingly, $a_2^p(A)$ encodes the per-proton probability to find a high-momentum proton in A(N,Z) relative to d. Similarly, $a_2^n(A)$ encodes the per-neutron probability to find a high-momentum neutron in A(N,Z) relative to d. Note that $a_2^p(A = d) = a_2^n(A = d) = 1$. A deviation from $a_2^p(A) = a_2^n(A)$ is reminiscent of the fact that there are differences in the per-proton and per-neutron dynamical modifications attributed to the short-distance structure of the nuclear environment in A(N,Z). We stress that in the absence of pp and nn correlations the high-momentum tails of P_p^A (P_n^A) would only receive a P_{pn}^A (P_{np}^A) contribution. For predominant proton-neutron correlations one has that $P_{pn}^A(p > p_F) \approx P_{np}^A(p > p_F)$ and one can infer that

$$a_2^p(A) \approx \frac{N}{Z} a_2^n(A)$$
 (for pn exclusivity). (26)

Note that the a_2^p and a_2^n defined in Ref. [16] obey this "pnexclusivity" inspired relation by construction and that in the limit of vanishing pp and nn correlations one has the strict relationship between a_2 , a_2^p and a_2^n

$$a_2(A) = \frac{2Z}{A} a_2^p(A) = \frac{2N}{A} a_2^n(A) \quad \text{(for pn exclusivity)}.$$
(27)

In Fig. 8 we show the evolution of the computed $a_2^{\nu}(A)$, $a_2^n(A)$ and $a_2(A)$ with mass number A and proton-toneutron ratio $\frac{N}{Z}$. The $\lim_{\text{high } p}$ in Eq. (25) is numerically evaluated as outlined in Eq. (22) and the discussion following this expression. All numerical values for the $a_2^p(A)$ and $a_2^n(A)$ are also contained in Table I. For asymmetric nuclei $\frac{N}{Z} > 1$ one finds that $a_2^p(A) > a_2^n(A)$. This implies that per nucleon the proton minority component contribute more to the SRC scaling factors than the neutron majority component, which is in line with previous observations [36–38]. This result is not surprising given that pn exclusivity gives rise to the relation $a_2^p \approx \frac{N}{Z} a_2^n$ [Eq. (26)]. The ratio $\frac{a_2^p(A)}{a_2^n(A)}$ increases with growing $\frac{N}{Z}$.



Figure 6. LCA results for the the SRC scaling factors $a_2(A)$ (orange open diamonds) along with the separate pp (blue open triangles), nn (brown stars) and pn (purple solid circles) contributions plotted versus atomic weight A. The shaded regions mark the pn (blue) and the pp+nn (green) contributions. All results are obtained from the asymptotic high-p behavior of the A-to-d single-nucleon nucleon momentum distribution $P^A(p)$ (see Eq. (21) and text for details). All $P^A(p)$ (including the deuteron one) are computed in LCA. The $a_2^{exp}(A)$ data are from the extended data tables of Ref. [16] and include data from Ref. [15].

Whereas for $A \gtrsim 27$ the $a_2^n(A)$ varies between 4.59 and 4.98, one observes that the $a_2^n(A)$ increases with $\frac{N}{Z}$ to reach a value of about 5.5 for the most neutron-rich nuclei considered here (¹⁹⁷Au and ²⁰⁸Pb). For ⁴⁸Ca ($\frac{N}{Z} = 1.4$) the $a_2^p(A)$ is about 15% larger than the $a_2^n(A)$. The outlier in the SRC scaling factors at $\frac{N}{Z} = 1.25$ is for ⁹Be and reflects the fact that for light nuclei the a_2 is about one unit smaller than for medium-heavy and heavy nuclei. In other words, ⁹Be is the sole light asymmetric nucleus in our sample. Table I also lists the values of $\frac{Za_2^p - Na_2^n}{A}$ a quantity that vanishes for N = Z nuclei. In asymmetric nuclei, $\frac{Za_2^p - Na_2^n}{A}$ approaches zero in the scenario of prevailing proton-neutron correlations. Obviously, $\frac{Za_2^p - Na_2^n}{A}$ grows increasingly negative with $\frac{N}{Z}$ which reflects the fact that the nn correlations increase in importance with growing $\frac{N}{Z}$ as can be inferred from Figs. 5 and 6.

E. Size of EMC effect

We exploit the conjectured linear relationship between the a_2 coefficients (per nucleon modification relative to the deuteron) and the size of the EMC effect to connect the LCA predictions for $a_2^p(A)$ and $a_2^n(A)$ to the EMC data. We suggest to parameterize the size of the EMC



Figure 7. Comparison of the LCA results for the SRC scaling factors $a_2(A)$ with those from ab-initio calculations and with measured values. The ab-initio results are from Table II of Ref. [20] (results referred to as "N²LO E τ $R_0=1.0$ fm" except for ⁴⁰Ca where the sole available ab-initio result uses the "AV4'+UIX_c" nucleon-nucleon interaction). The $a_2^{exp}(A)$ data are from the extended data tables of Ref. [16] and include data from Ref. [15].

effect as defined in Eq. (2) in the following way

$$b_{2}^{exp}(A) = -\frac{dR_{EMC}(A,x)}{dx}$$

= $m_1 \left(\frac{Za_2^p(A) + Na_2^n(A)}{A} - 1 \right)$
+ $m_2 \left(\frac{Za_2^p(A) - Na_2^n(A)}{A} \right),$ (28)

with m_1 and m_2 two parameters that are here determined from theory-experiment comparisons. By construction the deuteron has a vanishing EMC effect. In the above linear relationship that connects the measured size of the EMC effect $b_2^{exp}(A)$ to the computed SRC scaling factors for protons and neutrons, the first term (weight m_1) is reminiscent of an isospin blind generative mechanism. Indeed, in the first term of Eq. (28) the protons and neutrons contribute according to their weight $\frac{Z}{A}$ and $\frac{N}{A}$ in the total number of nucleons. For this reason, we refer to the term with weight m_1 as the "isoscalar" contribution. We refer to the second term (weight m_2) as the "isovector" contribution that could find its origin in an isospin-dependent generative mechanisms for the EMC effect. Within the framework of relativistic quark-level models of nuclear structure, it has been suggested that those so-called flavor-dependent or isovector nuclear effects influence the size of the EMC effect in nuclei with a neutron excess [26, 27]. We remind that in the limit of vanishing proton-proton and neutron-neutron correlations in $N \neq Z$ nuclei, the $a_2^p(A)$ and $a_2^n(A)$ obey the relation of Eq. (26) and the m_2 term in the above equation vanishes.



Figure 8. The LCA predictions for the SRC scaling factors for a sample of 15 nuclei as a function of A (top panel) and N/Z (bottom panel). Results are displayed for the proton a_2^p (circles), neutron a_2^n (triangles) and total a_2 (diamonds) SRC scaling factors. The LCA results are obtained with the expression (22) with $\Delta p^{\text{high}} \equiv [3.90 \text{ fm}^{-1}, 4.40 \text{ fm}^{-1}]$. The experimental data are from the extended data tables of Ref. [16] and include data from Ref. [15].

In Fig. 9 we compare the LCA predictions based on the Eq. (28) with data for the EMC slopes without applying isoscalar corrections to those data. We use χ^2 minimization to fit the computed $a_2^p(A)$ and $a_2^n(A)$ to 13 measured EMC slopes using the expression (28). We include the measured EMC slopes for the following nuclei (with xm we denote that there are x measurements for a particular target nucleus): ⁴He (2m), ⁹Be (2m), ¹²C (3m), ²⁷Al (1m), ⁵⁶Fe (2m), ⁶³Cu (1m), ¹⁹⁷Au (1m), ²⁰⁸Pb (1m). Accordingly, there are 8 target nuclei included in the fit, including 6 asymmetric ones. The best description of the data is obtained with the combination ($m_1 = 0.0878 \pm 0.003, m_2 = -0.229 \pm 0.030$). The values for the EMC slopes obtained with the Eq. (28) are contained in Table I. The extracted value for $m_1 = 0.0878 \pm 0.003$ is in line with the quoted value $m_1 = 0.084 \pm 0.004$



Figure 9. LCA results for the size of the EMC effect based on a linear connection with the proton and neutron SRC scaling factors. The "LCA (s)" results (blue open circles) assume a generative mechanism that is isospin (flavor) blind $(m_1 =$ $0.103 \pm 0.002, m_2 = 0$ in Eq. (28)). The "LCA (s+v)" results (orange open diamonds) assume generative mechanisms that are the combination of an isospin-dependent and an isospin-independent component $(m_1 = 0.0878 \pm 0.003, m_2 =$ -0.229 ± 0.030 in Eq. (28)). The non-isoscalar corrected $b_2^{exp}(A)$ data for the EMC slopes are from the summarizing tables of Ref. [16]. Overlapping data points have been slightly displaced for the sake of clarity.

in Ref. [20] that is based on fit of $-\frac{dR_{EMC}(A,x)}{dx}$ versus $a_2^{exp}(A)$. The fit of Ref. [20] includes all EMC data for light nuclei $(A \leq 12)$ and the isoscalar-corrected EMC data for ⁵⁶Fe and ¹⁹⁷Au. The results presented in Ref. [20] include solely the first term of the r.h.s. of the Eq. (28). The EMC data for $A \leq 63$ can be reasonably reproduced without inclusion of an isovector term $(m_1 = 0.103 \pm 0.002, m_2 = 0)$ —result referred to as "LCA(s)". Without inclusion of the isovector term, the EMC slope for ⁴He and ²⁷Al tends to be over-predicted whereas for the EMC slopes of ¹⁹⁷Au and ²⁰⁸Pb the opposite is observed. Inclusion of the m_2 term results in a stronger variation of the EMC slopes across the nuclear mass table and results in an improved description of the data. Indeed, after including the m_2 term the reduced χ^2 is 2.66 whereas the fit with solely the m_1 term has a reduced χ^2 of 7.3. Obviously, a more precise determination of the m_2 term requires more data and extended studies on asymmetric $\frac{N}{Z} > 1$ nuclei. For example, the effect of including the m_2 term works very differently for the nuclei ⁴⁰Ca and ⁴⁸Ca. Power-counting arguments within the framework of effective-field theory [20] indicate that the isovector term $\frac{Za_2^p(A) - Na_2^n(A)}{4}$ can be neglected relative to the isoscalar one $\frac{Za_2^{\vec{P}}(A) + Na_2^n(A)}{4}$. Inspecting Table I we find that the isoscalar term is in the range 4.05-5.11, whereas the iosvector term is in the range -0.84 - 0.00. The isovector term is vanishing for N = Z nuclei and reaches its largest values for the

most asymmetric nuclei considered here: -0.66 for ²⁰⁸Pb and -0.84 for ¹⁹⁷Au. We stress that the above theoryexperiment comparisons for the EMC slopes cannot shed light on underlying mechanisms that are due to non-SRC related medium modifications.

III. CONCLUSIONS

The SRC scaling factors a_2 represent the relative probability of nucleon-pair SRC in a specific nucleus relative to the deuteron. They are conventionally expressed per nucleon and can be computed from the high-momentum properties of momentum probability distributions. In the framework of the low-order correlation operator approximation used throughout this work one can determine the pp, pn, nn, np SRC contributions to the momentum probability distributions $P^{A}(p)$ for a specific nucleus A(N,Z). We have determined those contributions for a sample of 15 nuclei extending in mass number from He to Pb. Across that sample, that includes 4 symmetric and 11 asymmetric nuclei, there is relatively little variation in the computed a_2 with values in the range between 4.05 (for ⁴He) and ≈ 5.10 (all studied nuclei with $A \ge 108$). We find that the pn contribution to the SRC scaling factor is approximately 3 and that there are non-negligible contributions from pp and nn correlations in the LCA approach. The pp and pn (nn and np) SRC contributions to the high-momentum probability distributions determine the proton (neutron) SRC scaling factors a_2^p (a_2^n). The a_2^p and a_2^n provide more detailed information on the abundance of nucleon-pair SRC than the "total SRC scaling factor a_2 ". For asymmetric N > Z nuclei one systematically finds that $a_2^p > a_2^n$ with deviations approaching 20% for the most asymmetric nuclei in our study. This means that in N > Z nuclei the SRC induced medium modifications of the protons and the neutrons are substantially

different. We have done robustness checks and used two different techniques to compute the SRC scaling factors (a_2, a_2^p, a_2^n) . For light and medium-heavy nuclei, the LCA predictions for the SRC scaling factors are in line with those from ab-initio approaches and the values extracted from inclusive electron scattering under selected conditions.

In the LCA framework we can shed light on the validity of the A-to-d factorization of the momentum probability distributions by studying the ratios $\frac{P_{NN'}^{A}(p)}{P^{d}(p)}$. For NN'=pn and np the A-to-d factorization is very well re-alized at $p \gtrsim 3.5$ fm⁻¹. For the pp and nn correlations, on the other hand, the A-to-d factorization of $\frac{P_{NN'}^{A}(p)}{P^{d}(p)}$ is only approximate but indications for a plateau are visible for $p \gtrsim 4.0 \text{ fm}^{-1}$. We have expressed the measured size of the EMC effect in terms of the computed proton and neutron SRC scaling factors. The measured size of the EMC effect displays a stronger variation across the nuclear mass table than the SRC scaling factor and larger EMC effects are observed in nuclei with a neutron excess. These qualitative features can be captured in terms of a linear relationship between the size of the EMC effect and the computed proton and neutron SRC scaling factors that includes both an isoscalar and an isovector term.

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