

ONLINE MODELLING AND STATE-OF-CHARGE ESTIMATION FOR  
LITHIUM-TITANATE BATTERY

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Specially dedicated to my beloved father, mother and friends for their  
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## ABSTRACT

Lithium-titanate (LTO) battery, which has features of fast charging and superior safety, is a promising energy storage element for electric vehicles. Its features can be fully utilised by using a fast charger and a high performance battery management system. Battery model is vital to a battery charger design for characterising the charging behaviours of a battery. Additionally, a robust state-of-charge (SoC) estimation should be realised for a reliable battery management. This thesis develops a battery model for charger design and a robust method for SoC estimation by using MATLAB. The thesis proposed a transfer function-based battery model which is applicable for small-signal analysis and large-signal simulation of battery charger design, in order to capture the charging profiles of LTO battery. Busse's adaptive rule, which has simple computations, is applied to improve the accuracy of Kalman filter-based SoC estimation. Busse's adaptive Kalman filters are also applied for SoC estimation with online battery modelling to eliminate the complicated process of battery modelling. This study was conducted by using 2.4 V, 15 Ah LTO batteries. The batteries were tested with continuous current test and pulsed current test at several ambient temperatures (-25 °C, 0 °C, 25 °C and 50 °C) and charge/discharge currents (0.5 C, 1 C, 2 C). Additionally, modified dynamic stress tests at several temperatures (-15 °C, 0 °C, 15 °C, 25 °C, 35 °C and 50 °C) were also performed to test the battery under real EV environment. Results of the battery modelling showed that the developed transfer function-based battery model is accurate where the root-mean-square modelling error is less than 30 mV. The results also revealed that the Busse's adaptive rule has effectively improved the Kalman filter-based SoC estimation for the case of offline battery model by giving a higher accuracy and shorter convergence time. Additionally, Busse's adaptive Extended Kalman Filter gave a better accuracy in SoC estimation with online battery modelling. The proposed transfer function-based battery model provides a helpful solution for the battery charger design while the proposed Busse's adaptive Kalman filter offers an accurate and robust SoC estimation for both offline and online battery models.

## ABSTRAK

Bateri lithium titanat (LTO) yang mempunyai ciri-ciri pengecasan yang cepat dan keselamatan yang unggul merupakan elemen penyimpanan tenaga yang amat diyakini untuk kenderaan elektrik. Ciri-cirinya boleh digunakan sepenuhnya dengan merealisasikan pengecas bateri yang pantas dan sistem pengurusan bateri berprestasi tinggi. Model bateri adalah penting untuk merekabentuk pengecas bateri bagi menentukan tindakbalas bateri ketika dicas. Selain itu, kaedah anggaran keadaan cas (SoC) yang tepat perlu direalisasikan untuk sistem pengurusan bateri. Tesis ini membangunkan model bateri untuk kegunaan reka bentuk pengecas bateri dan juga kaedah anggaran keadaan caj bateri yang mantap menggunakan simulator MATLAB. Dalam tesis ini, model bateri yang berasaskan fungsi pemindahan serta sesuai untuk analisis isyarat kecil dan simulasi isyarat besar dalam merekabentuk pengecas bateri telah dibangunkan bagi mencirikan profil pengecasan bateri LTO. Peraturan penyesuaian Busse yang mempunyai pengiraan mudah telah digunakan untuk meningkatkan ketepatan penapis Kalman dalam anggaran keadaan caj bateri. Selain itu, penapis Kalman menggunakan peraturan penyesuaian Busse ini juga digunapakai untuk anggaran keadaan caj bateri dan model bateri secara talian untuk menghapuskan proses yang rumit dalam pemodelan bateri. Kajian ini telah dijalankan dengan menggunakan 2.4 V, 15 Ah bateri LTO. Bateri-bateri ini telah diuji dengan ujian arus berterusan dan ujian arus berdenyut pada beberapa suhu ambien (-25 °C, 0 °C, 25 °C dan 50 °C) dan arus berlainan (0.5 C, 1 C, 2 C). Selain itu, ujian tekanan dinamik yang telah diubah suai juga dijalankan pada beberapa suhu persekitaran (-15 °C, 0 °C, 15 °C, 25 °C, 35 °C dan 50 °C) untuk mengujikan bateri dalam persekitaran EV yang sebenar. Keputusan pemodelan bateri menunjukkan bahawa model bateri berasaskan fungsi pemindahan yang telah dibangunkan adalah jitu, di mana ralat punca min kuasa dua untuk pemodelan adalah kurang daripada 30 mV. Selain itu, keputusan mendedahkan bahawa peraturan penyesuaian Busse telah meningkatkan prestasi penapis Kalman dalam anggaran keadaan caj bagi kes model bateri luar talian dengan memberikan ketepatan yang lebih tinggi dan masa penumpuan yang lebih singkat. Selain itu, penapis Kalman lanjutan yang menggunakan peraturan penyesuaian Busse ini juga memberi ketepatan yang baik dalam anggaran keadaan caj dan model bateri secara dalam talian. Model bateri yang berasaskan fungsi pemindahan telah menyediakan penyelesaian yang berguna untuk reka pengecas bateri manakala penapis Kalman yang menggunakan peraturan penyesuaian Busse telah menawarkan anggaran keadaan caj bateri yang jitu dan mantap bagi kedua-dua model bateri luar talian dan dalam talian.

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## LIST OF ABBREVIATIONS

AC	-	Alternating current
ADVISOR	-	Advanced Vehicle Simulator
ANN	-	Artificial neural network
Ah	-	Ampere-hour
BMS	-	Battery management system
BV	-	Butler-Volmer
Busse-AEKF	-	Busse's adaptive extended Kalman filter
Busse-AUKF	-	Busse's adaptive unscented Kalman filter
CC-CV	-	Constant current constant voltage
CM-AEKF	-	Covariance-matching adaptive extended Kalman filter
CM-AUKF	-	Covariance-matching adaptive unscented Kalman filter
DST	-	Dynamic stress test
EIS	-	Electrochemical impedance spectroscopy
EKF	-	Extended Kalman filter
EV	-	Electric vehicle
FCEV	-	Fuel cell electric vehicle
GA	-	Genetic algorithm
HEV	-	Hybrid electric vehicle
HPPC	-	Hybrid pulse power characterization
ICEV	-	Internal combustion engine vehicle
IEA	-	International energy agency
I-V	-	Current-voltage
I/O	-	Input to output
KiBaM	-	Kinetic battery model
LCO	-	Lithium cobalt-oxide
LFP	-	Lithium ferro phosphate
LMO	-	Lithium manganese-oxide

LTO	-	Lithium-titanate
Li <sup>+</sup>	-	The ion of lithium
Li-ion	-	Lithium-ion
MCU	-	Main control unit
MRE	-	Mean relative error
MW-RLS	-	Moving window recursive least square
NCA	-	Lithium nickel-cobalt-aluminium-oxide
NEDC	-	New European Driving Cycle
NMC	-	Lithium nickel-manganese-cobalt-oxide
NREL	-	National Renewable Energy Laboratory
NiMH	-	Nickel-metal hydride
OBD	-	On-board diagnosis
OCV	-	Open circuit voltage
PNGV	-	Partnership for a New Generation of Vehicle
RC	-	Resistance-capacitance
RLS	-	Recursive least square
RMSE	-	Root-mean-square error
SVM	-	Support vector machine
SZDC	-	Shenzhen driving cycle
SoC	-	State-of-charge
SoH	-	State-of-health
UKF	-	Unscented Kalman filter
UDDS	-	Urban Dynamometer Driving Schedule
USABC	-	United States Advanced Battery Consortium
UTM	-	Universiti Teknologi Malaysia
VTF	-	Vogel-Tammann-Fulcher

## LIST OF SYMBOLS

$\alpha$	-	Coefficient of scale calculation of UKF
$\beta$	-	Coefficient of weight calculation in UKF
$\rho$	-	Sigma points for the estimated output in UKF
$\mu$	-	Temperature factor for temperature-based normalised charging voltage
$\theta$	-	Vector of parameter for RLS algorithm
$\varepsilon$	-	Coefficient of adaptive forgetting factor equation
$\varepsilon_Q$	-	The window size in Busse's adaptive rule that controls the update change of process noise covariance
$\varepsilon_R$	-	The window size in Busse's adaptive rule that controls the update change of measurement noise covariance
$\lambda$	-	Scale of UKF
$\sigma$	-	Sigma points of states in UKF
$\sigma_c$	-	Capacity coefficient
$\tau_1$	-	Time constant for the first RC parallel network in Thevenin model
$\tau_2$	-	Time constant for the second RC parallel network in Thevenin model
$\Pi$	-	State vector for model parameters
$\emptyset$	-	The ambient temperature
$\chi$	-	Augmented state vector
$\Delta V$	-	DC voltage offset
$\Delta x$	-	The change of estimated state at measurement update of Kalman filter
$\Delta y$	-	The change of estimated output at measurement update of Kalman filter
$A$	-	Jacobian matrix of extended Kalman filter that represents the partial derivative of state equation with respect to states
$B$	-	Jacobian matrix of extended Kalman filter that represents the partial derivative of state equation with respect to input

$C$	-	Jacobian matrix of extended Kalman filter. It represents the partial derivative of output equation with respect to states
$C_i$	-	Capacitor for the $i$ -th RC parallel network in Thevenin model
$C_1$	-	Capacitor for the first RC parallel network in Thevenin model
$C_2$	-	Capacitor for the second RC parallel network in Thevenin model
$C_S$	-	Storage capacitor in resistor-capacitor equivalent circuit model
$C_U$	-	Usable capacity of battery at certain current rate and ambient temperature
$C_b$	-	Storage capacitor in RC model
$C_{sur}$	-	Surface capacitor in RC model
$D$	-	Jacobian matrix of extended Kalman filter. It represents the partial derivative of output equation with respect to input
$E$	-	Statistical expectation operator
$F$	-	Forgetting factor
$G$	-	Covariance matrix for RLS
$G_1$	-	Laplace transform for the time derivative of $f_1$
$G_2$	-	Laplace transform for the time derivative of $f_2$
$H$	-	Average of the square of output residuals
$H_0$	-	Transfer function of battery with removal of DC resistance
$H_b$	-	Overall transfer function for battery
$I$	-	Identity matrix
$I_L$	-	Load current of battery
$K$	-	Algorithm gain
$K_S$	-	Time scaling coefficient
$M$	-	The number of samples of output residuals in covariance matching adaptive rule
$N$	-	Dimension of state vector
$OCV$	-	Open circuit voltage of battery
$P$	-	Error covariance matrix
$P^+$	-	Posterior error covariance matrix
$P^-$	-	Priori error covariance matrix
$P_0$	-	Initial error covariance of Kalman filter
$P_{xy}$	-	Cross-correlated covariance
$P_y$	-	Measurement covariance
$Q$	-	Covariance matrix for process noise

$Q^*$	- Measure of process noise
$R$	- Covariance matrix for measurement noise
$R^*$	- Measure of measurement noise
$R_i$	- Resistor for the $i$ -th RC parallel network in Thevenin model
$R_1$	- Resistor for the first RC parallel network in Thevenin model
$R_2$	- Resistor for the second RC parallel network in Thevenin model
$R_S$	- Series resistor in equivalent circuit model
$R_{dc}$	- DC resistance corresponding to dc offset in curve normalisation
$SoC$	- State-of-charge
$T$	- Normalised charging time
$Tr$	- The trace of the matrix
$V_{cb}$	- Voltage across storage capacitor in RC model
$V_{csur}$	- Voltage across surface capacitor in RC model
$V_i$	- Voltage across the $i$ -th RC parallel network in Thevenin model
$V_1$	- Voltage across the first RC parallel network in Thevenin model
$V_2$	- Voltage across the second RC parallel network in Thevenin model
$V_N$	- Temperature-based normalised charging voltage
$V_R$	- Reference of normalised charging voltage
$V_{c,d}$	- CC charging voltage at $c$ charging rates and $d$ temperatures
$V_t$	- Terminal voltage of battery
$V_{t,EXP}$	- Experimental terminal voltage of battery
$V_{t,SIM}$	- Simulated terminal voltage of battery
$W_i^c$	- Weight of the error covariance for $i$ -th sigma points in UKF
$W_i^m$	- Weight of the $i$ -th sigma points in UKF
$X$	- The true value of state
$Y$	- The measured value of system output
$a_1$ to $a_{10}$	- Coefficient of 9 <sup>th</sup> order polynomial equation
$b$	- The index weighted coefficient of Sage-Husa adaptive rule
$b_1$ to $b_7$	- Coefficients of equation (4.14)
$c_1$ to $c_5$	- Coefficients of equation (4.15)
$cc_1$ to $cc_9$	- Coefficient of second-order Thevenin model at charge condition
$d_1$ to $d_5$	- Coefficient of exponential curve fitting equation in equation (2.5)
$dd_1$ to $dd_9$	- Coefficient of second-order Thevenin model at discharge condition

$dt$	-	Sampling time
$e$	-	Output residuals
$err$	-	Estimation error
$f_1$	-	The fixed component in normalised charging voltage
$f_2$	-	The temperature-based component in normalised charging voltage
$h$	-	Regressor of RLS algorithm
$i$	-	Column of a matrix
$j$	-	Row of a matrix
$k$	-	Discrete-time index
$l$	-	Coefficient of adaptive forgetting factor equation
$n$	-	Number of sample for error analysis
$p_0$ to $p_3$	-	Coefficient of normalised charging curve
$r$	-	Process noise for the model parameters
$r'$	-	Adjustable coefficient in the judgement condition of Sage-Husa adaptive rule
$t$	-	Time
$t_E$	-	Ending time of rest
$t_S$	-	Starting time of charge/discharge process
$t_R$	-	Starting time of rest
$u$	-	System input
$v$	-	Measurement noise of system
$v_R$	-	DC offset due to the DC resistance
$w$	-	Process noise of system
$x$	-	State vector of system
$x_0$	-	Initial state
$x^+$	-	Posterior estimated state
$x^-$	-	Priori estimated state
$y$	-	System output
$z$	-	Discretisation operator in bi-linear transformation
$z'$	-	The output residual of Sage-Husa adaptive rule



**LIST OF APPENDICES**

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## CHAPTER 1

### INTRODUCTION

#### 1.1 Background

Fossil fuels, such as oil, coal and natural gas, are the main resources for the world's energy supply. However, the usage of fossil fuels leads to the emission of greenhouse gas that contributes to global climate change. One of the efforts to reduce greenhouse gas emissions is the transformation of energy technology in the transportation sector. According to International Energy Agency (IEA), this transformation can be realized by implementing electric vehicles (EVs) and hybrid electric vehicles (HEVs) [1]. Through vehicle electrification, vehicles are powered by a rechargeable energy storage system and enabled by an electric motor, thus providing the means for a clean and efficient roadside transportation system. Electric vehicles are expected to aggressively penetrate the market of roadside transportation in the near future, where the sales for both EVs and HEVs are expected to reach 50 million by 2050 [1].

In order to compete with the existing transportation market, attention should be given to the energy storage element of EVs. Generally, energy density (Wh/L) and specific energy (Wh/kg) are the prime considerations for choosing the energy storage element for EVs. High value of energy density and specific energy reduces the size and mass of the energy storage element and thus extends the travel range of EVs. In addition, power density (W/L) and specific power (W/kg) are also important in determining the available power for EVs under various load demands and driving states. Besides, safety also needs to be addressed for

selecting an energy storage element so that the extreme emission of gaseous substances or heat will not take place under normal operation [2]. Other criteria for selecting energy storage elements are efficiency, maintenance requirement, cost, and environmental friendliness [3].

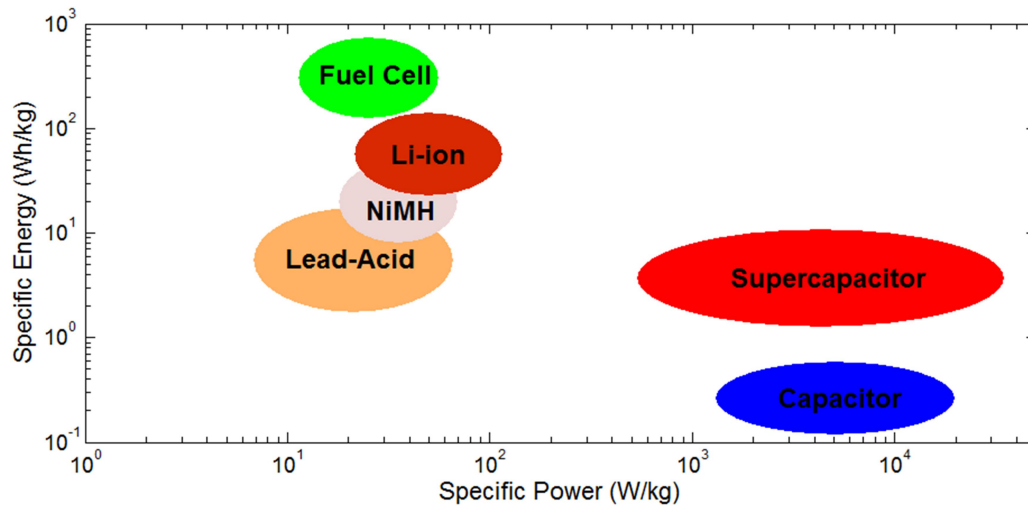
Rechargeable batteries, fuel cells and super-capacitors, are the three potential candidates for the energy storage element of EVs. The comparison of their power density and energy density is shown in Figure 1.1. The diagram reveals that fuel cells have the highest value of energy density among the energy storage elements. Therefore, fuel cells provide a longer travel mileage to the vehicle. Today, several fuel cell electric vehicles (FCEVs) are available in the transportation market, such as Hyundai ix35, Honda FCX Clarity and Toyota Mirai. Theoretically, the electrical energy of a fuel cell is generated by using oxygen from the air and compressed hydrogen through a direct electrochemical reaction without undergoing combustion. The electrochemical process of fuel cells only produces heat and water, thus gives zero greenhouse gases emission [4]. Similar to the conventional internal combustion engine vehicles (ICEVs), FCEVs can be refilled with hydrogen within a very short period. However, due to the low density of hydrogen gas, the on-board hydrogen storage has become a challenging task [5]-[6]. With the same volume, gasoline can give 10 times more of energy than hydrogen gas [5]. Due to this reason, it is costly transporting hydrogen gas from the production site to the refill station. Likewise, a large hydrogen tank is required in each FCEV for energy storage purpose [7]. In addition, a potential risk exists in the storage of hydrogen gas because it is highly flammable. Presently, further development of an efficient hydrogen storage system is required to realise the application of FCEV [6].

Super-capacitor is also potentially applied as the energy storage element for EVs due to its advantages in term of power capability, cycle life performance and charge-discharge efficiency [8]. However, it is also not suitable for application as the primary energy source for EVs due to its extremely low energy density (less than 10Wh/kg) and its high self-discharge rate (i.e. 5% per day [9]). Today, super-capacitors are applied together with batteries or fuel cells to form a hybrid energy storage system [10]-[19], where the advantages of the high power capability of super-capacitors and the high energy density of the batteries are combined to fulfil the power and energy demands of EVs. In this context, the batteries are

operating in nearly steady state conditions whereas the super-capacitors are applied to supply transient power demands and peak loads of EVs [20].

Compared to fuel cells and super-capacitors, rechargeable batteries are considered as the most appropriate choice as the primary energy storage element for EVs. The technology of rechargeable batteries has been improved from lead acid batteries to nickel-metal hydride (NiMH) batteries, and then from NiMH batteries to lithium-ion (Li-ion) batteries. However, the battery technology is often criticized due to its slow progression, and cannot keep up pace with the demands of current technology [21]. Currently, Li-ion battery is considered as the most promising energy storage element for EVs since it owns the highest specific energy ( $150\text{Whkg}^{-1}$ ) and the highest specific power (up to  $5\text{kWkg}^{-1}$ ) compared to other batteries [22]-[23]. Besides, Li-ion battery has no memory effect, long cycle life, and excellent discharge characteristics [24]. Today, Li-ion battery has been applied in several EVs, such as BYD E6, Tesla Motor, Nissan Leaf and Chevrolet Volt [25].

Despite the impressive advantages of Li-ion batteries, several issues are vital to be considered for the application of Li-ion batteries. Firstly, the power density and energy density of Li-ion battery is much lower compared with the fuel of ICEVs. As a result, a huge size of battery pack, which is formed by series and parallel connection of Li-ion cells, is applied to fulfil the energy and power demands of EVs. Besides, the recharge time of Li-ion battery pack is relatively longer compared to the fuel refill time of ICEV. Thirdly, Li-ion battery is chemically reactive and it is sensitive to its operating temperature and voltage. Due to these reasons, the huge size of battery pack, the limited drive range, the lengthy battery recharge time and safety issue have become the main challenges for EV development. The improvement of battery technology and the development of an efficient battery management system (BMS) are the two important aspects to realise a reliable EV.



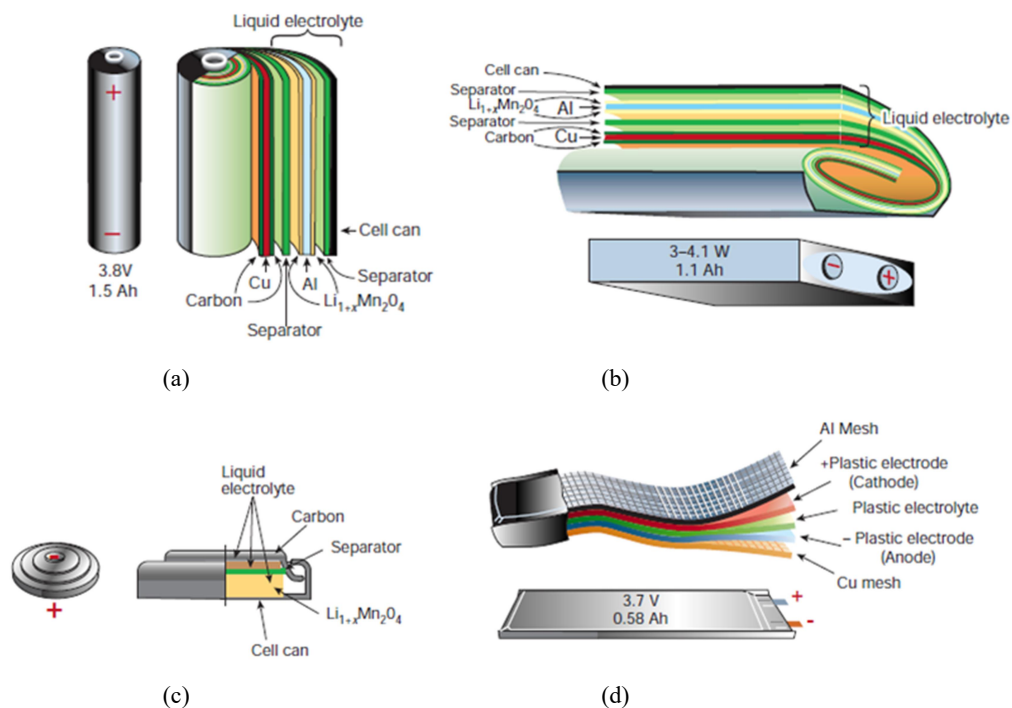
**Figure 1.1** Comparison between various energy storage elements in terms of power and energy density [26]

### 1.1.1 Lithium-ion Battery Technology

Over the years, scientists have been committed towards improving the technology of rechargeable batteries. The rechargeable batteries have been improved from lead acid batteries to nickel-based batteries, and then from nickel-based batteries to Li-ion batteries. Currently, Li-ion battery is considered as the most promising type of rechargeable battery and it has penetrated the market of portable electronic devices.

Theoretically, lithium is the lightest and most electropositive metal, thus owning remarkable characteristics for the design of energy storage element with high energy density and high specific energy. However, lithium metal is highly reactive, and it is flammable when it reacts with water. Therefore, the early developed Li-ion batteries, which used lithium metal as its cathode, suffered from its safety issues [24]. Generally, an external protection case is required for the earlier developed Li-ion battery in order to ensure its safety during usage. This additional packaging not only increases the cost and weight of the battery, but also reduces the flexibility in design.

Today, the safety problems of Li-ion battery have been drastically reduced through the development of advanced materials for its construction. Currently, instead of using lithium metal, lithium liberating compound is applied as cathode material and graphite is applied as anode. Therefore, the operation of modern Li-ion battery is based on the intercalation of lithium ions ( $\text{Li}^+$ ). In this aspect,  $\text{Li}^+$  is intercalated into the cathode in the discharge process and into the anode in the charge process through the electrolyte. Furthermore, the construction of Li-ion battery has been improved with the invention of solid-state cell. Instead of using liquid electrolyte, solid-state cell uses the solid electrolyte in its cell construction. Without the existence of liquid electrolyte, the solid-state cell is free from harmful chemical leakage, thus offering better safety without using heavy protective case. Besides, solid-state cell is flexible enough to be shaped into several shapes according to its usage [27], such as cylindrical, coin, prismatic and flat shapes as shown in Figure 1.2 [21].



**Figure 1.2** Configurations of solid state cell: (a) cylindrical, (b) prismatic, (c) coin, and (d) thin and flat [21]

Several types of Li-ion battery have been developed by using different cathode or anode materials. The Li-ion battery is named based on the main active material that gives its character. Presently, there are six common types of Li-ion in the market, they are lithium cobalt-oxide ( $\text{LiCoO}_2$  or LCO), lithium manganese-oxide ( $\text{LiMn}_2\text{O}_4$  or LMO), lithium nickel-manganese-cobalt-oxide ( $\text{LiNiMnCoO}_2$  or NMC), lithium ferro phosphate ( $\text{LiFePO}_4$  or LFP), lithium nickel-cobalt-aluminium-oxide ( $\text{LiNiCoAlO}_2$  or NCA), and lithium-titanate ( $\text{Li}_4\text{Ti}_5\text{O}_{12}$  or LTO) batteries.

LCO and LMO battery are the most popular Li-ion batteries in the market. They have been widely applied in several digital devices, such as cell phones, laptops and cameras. LCO battery consists of cobalt-oxide cathode which offers a high specific energy [28]. However, its performance is limited by its poor thermal stability. Moreover, the usage of cobalt brings toxic hazards to the environment [24] [29]. Compared to the LCO battery, LMO battery uses lithium manganese-oxide as its cathode, which has spinel structure and provides lower internal resistance, higher current handling capability and higher thermal stability. Additionally, manganese is cheaper and more environmentally friendly compared to cobalt [24]. However, the performance of LMO battery is limited by its short cycle life. Besides, its energy density is 20% lower compared to LCO battery [29].

The advantages of LCO and LMO battery have been combined in the NMC battery. NMC battery consists of cathode material that is formed by the combination of nickel, manganese and cobalt. The ratio of nickel-manganese-cobalt is typically set as 1:1:1 [29]. However, this ratio can be adjusted by NMC battery manufacturers in order to get the highest performance [24]. NMC not only improves the safety of LCO battery, but it is also less expensive than LCO battery. Today, it is a preferred candidate for certain EV manufacturers and it has been applied in Nissan Leaf, Chevy Volt, and BMW i3.

NCA battery, which uses the combination of nickel, cobalt and aluminium as its cathode, shares certain similarities with NMC battery. Currently, NCA battery has been applied in Tesla Motor S-model due to its high specific energy, high specific power and long life span [29]. However, the stability of NCA battery is poorer than NMC battery and LMO

battery. In this aspect, NCA battery has a lower onset temperature (150 °C) for cathode decomposition, and thus it is less resistant to thermal abuse [2]. Due to this reason, the thermal management of NCA battery is vital. For instance, Tesla has assembled the NCA batteries into a liquid-cooled battery pack with strong metal enclosure.

LFP battery is a modern Li-ion battery which uses phosphate as its cathode. It offers superior thermal and chemical stabilities, thus providing a better safety feature than other aforementioned batteries [24][29]. In this aspect, LFP battery has a greater capability to withstand over-voltage and short-circuit conditions. Besides, it also provides several advantages in term of low internal resistance, high current rating and long cycle life [29]. As a trade-off of using phosphate cathode, it has a lower cell voltage and specific energy compared to LCO, LMO, NMC and NCA battery. However, due to its excellent safety features, it has been applied in BYD E6.

Apart from the development of cathode material, Li-ion has also improved in terms of anode material. Instead of using graphite anode, LTO battery uses lithium titanium oxide ( $\text{Li}_4\text{Ti}_5\text{O}_{12}$ ) as its anode. Fast charging is considered the most attractive feature of LTO battery. The nano-particles of LTO increases the electrode-electrolyte contact area and reduces the diffusion distance for ions and electrons, thus reducing the polarisation resistance and allowing for fast charging [30]-[31]. Moreover, it has superior safety, long cycle life, excellent low-temperature performance, low toxicity and good thermal stability. As a trade-off, LTO has a lower cell voltage, and thus has a lower specific energy compared to other Li-ion batteries. Currently, it has a higher cost due to the limited production. However, due to its fast charging capability, it has been applied in several EVs, such as Mitsubishi i-MiEV, Honda Fit EV. The characteristics of these batteries are summarised in Table 1.1 [29][32].



**Table 1.1** : Characteristics of lithium-ion batteries [32][29]

	<b>LCO</b>	<b>LMO</b>	<b>NMC</b>	<b>NCA</b>	<b>LFP</b>	<b>LTO</b>
<b>Cathode</b>	LiCoO <sub>2</sub>	LiMn <sub>2</sub> O <sub>2</sub>	LiNiMnCoO <sub>2</sub>	LiNiCoAlO <sub>2</sub>	LiFePO <sub>4</sub>	Graphite
<b>Anode</b>	Graphite	Graphite	Graphite	Graphite	Graphite	Li <sub>4</sub> Ti <sub>5</sub> O <sub>12</sub>
<b>Nominal voltage (V)</b>	3.6	3.7	3.6	3.6	3.2	2.4
<b>Operating voltage (V)</b>	2.5 – 4.2	2.5 – 4.2	2.5 – 4.2	3.0 – 4.2	2.5 – 3.65	1.5 – 2.75
<b>Operating Temperature (°C)</b>	Charge: 0 – 55 Discharge: -20 – 55	Charge: 0 – 55 Discharge: -20 – 55	Charge: 0 – 55 Discharge: -20 – 55	Charge: 0 – 55 Discharge: -20 – 55	Charge: 0 – 55 Discharge: -20 – 55	Charge: -30 – 55 Discharge: -30 – 55
<b>Specific Energy(Wh/kg)</b>	150 – 200	100 – 150	150 – 220	200 – 260	90 – 120	70 – 80
<b>Typical Charge rate (C)</b>	0.7 – 1.0	0.7 – 1.0	≤ 1.0	≤ 0.7	≤ 1.0	≤ 5.0
<b>Maximum Charge rate (C)</b>	1.0	3.0	1.0	0.7	3.0	5.0
<b>Typical Discharge rate (C)</b>	≤ 1.0	≤ 1.0	≤ 1.0	≤ 1.0	≤ 1.0	≤ 10
<b>Maximum Discharge rate (C)</b>	1.0	30 (pulse)	2.0	1.0	5.0	10
<b>Cycle life</b>	500-1000	1000	2000-3000	2000-3000	> 3000	> 5000
<b>Safety</b>	Average	Good	Good	Average	Very good	Very good
<b>Cost</b>	Low	Low	Low	High	Low	Very high
<b>Application in EV</b>	-	-	Nissan Leaf, BMW i3	Tesla Motor	BYD E6	Mitsubishi i- MiEV

### 1.1.2 Battery Management System

Safety concerns are crucial for the application of Li-ion battery because it is sensitive to its operating condition. In order to ensure its safety, the battery must operate within its safety operating window, which is restricted by voltage and temperature [25]. The battery could burn or even explode if used beyond its maximum operating voltage (over-voltage). Besides, under-voltage or over-discharge of batteries could lead to irrecoverable capacity degradation [33]. On the other hand, the high operating temperature would cause battery destruction and the emission of flammable gases. At extreme high temperatures, the thermal runaway would occur. Besides, low operating temperatures will reduce the cycle life of the battery due to the deposition of metallic lithium on the surface of negative electrode. At the extreme low temperatures, the cathode of the battery will break down and cause internal short circuit of the battery [25]. The concepts of safety operating window is illustrated in Figure 1.3 [34].

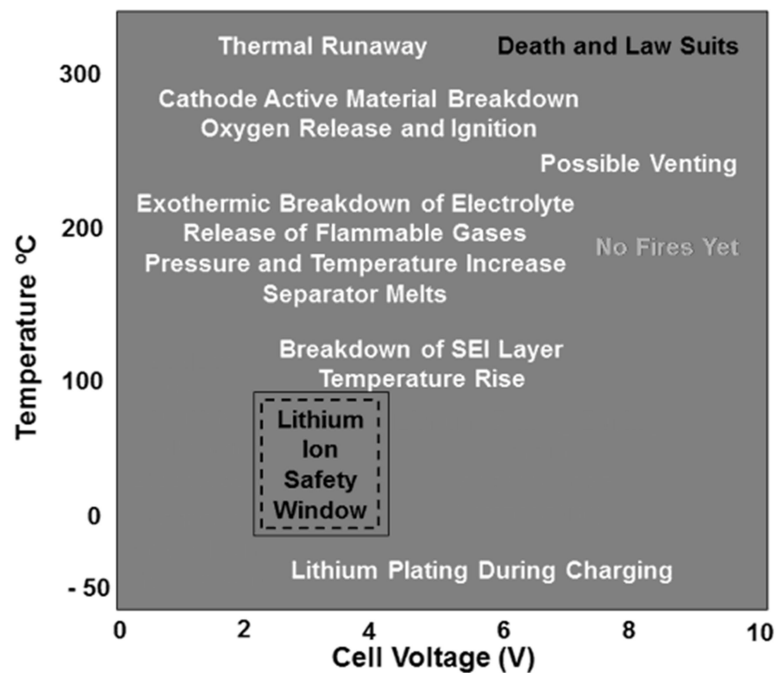
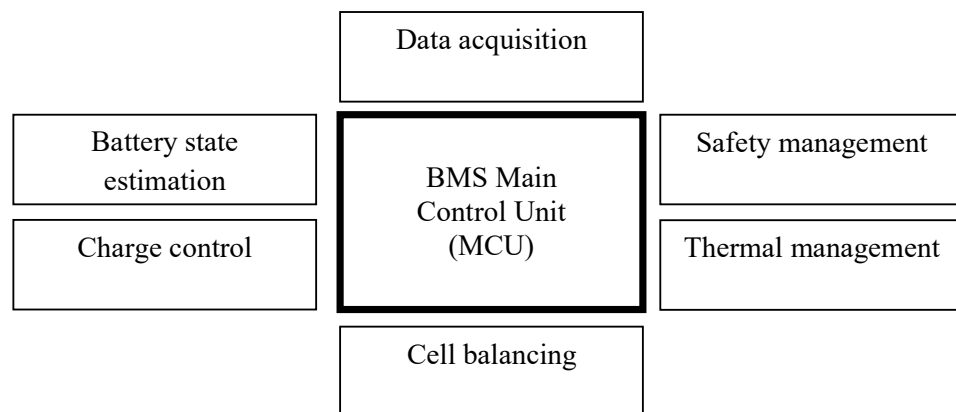


Figure 1.3 Operating window for Li-ion battery [34]

A battery management system (BMS) is vital to realize a safe and reliable EV. The main function of the BMS is to ensure the proper usage of battery packs while it provides the sufficient electrical power for the operation of EVs. Apart from preventing the battery from over-voltage, under-voltage and thermal abuse, the sub-functions of BMS also include data acquisition, battery states estimation, safety management, cell balancing, charge control, and thermal management [25], [35]–[37]. The schematic structure of a typical BMS is shown in Figure 1.4.



**Figure 1.4** Schematic structures of BMS

Data acquisition acts as the input for BMS. Generally, it measures the battery terminal voltage, battery current, battery temperature and ambient temperature. Since the battery pack of EV is built up by multiple battery cells, the measurement on each individual cell is necessary to ensure that each cell operates within its safety window. Advanced data acquisition system also includes smoke detection, collision detection insulation detection and impedance detection for the detection of battery faults.

Safety management is the primary task of BMS to prevent batteries from critical operating conditions, such as over-voltage, under-voltage, ultra high temperature, over-current, short-circuit, and loose connections. For advanced versions of BMS, on-board diagnosis (OBD) system is also included for the maintenance of battery packs. In this aspect, OBD stores the historical data of the battery and discovers the failure and abnormal status of the battery. When an

abnormal status is found, the warning devices will be activated to send an alert to the EV drivers.

Thermal management is also an important function of BMS in order to manage the operating temperature of battery. In this aspect, the temperature among the cells is equalised so that the operation of the battery cells is uniform. Thermal management system detects the temperature distribution in the battery packs, and control the cooling power or heating power for batteries. Generally, due to cost and space limitation, an air-cooling system is applied. Apart from air-cooling, liquid cooling and phase-change materials are also applied in thermal management system [38][39].

Cell balancing is also an important feature of BMS so as to establish the uniformity of each cell in battery packs. This is due to the fact that all cells are not alike although they are same type, same specifications, and manufactured at the same conditions. The differences between each battery cells are unavoidable in term of capacity, internal resistance or self-discharge rate. The difference could be caused by poor production and packaging process of the battery manufacturer. Without this feature, the uniformity of battery cells will be degraded with the increase of operating time, which leads to over-voltage and under-voltage problems in battery pack. Passive balancing and active balancing are the two typical approaches for cell balancing [40]. Passive balancing technique compares the cell voltage to detect the difference between highest voltage cell and lowest voltage cell. Then, the high voltage cell will be discharged by using a discharge resistor. On the other hand, active cell balancing technique transfers charge from high voltage cells to low voltage cells, thus owning higher energy efficiency than passive balancing technique. However, passive balancing technique is still preferred by EV industries because its cost is much lower compared to active balancing technique.

Charger control is an important feature of BMS used in order to control the recharge process of the battery. Generally, constant current constant voltage (CC-CV) charging scheme is applied to charge Li-ion battery. With assistance from cell balancing system and safety management system, a safe and uniform charging

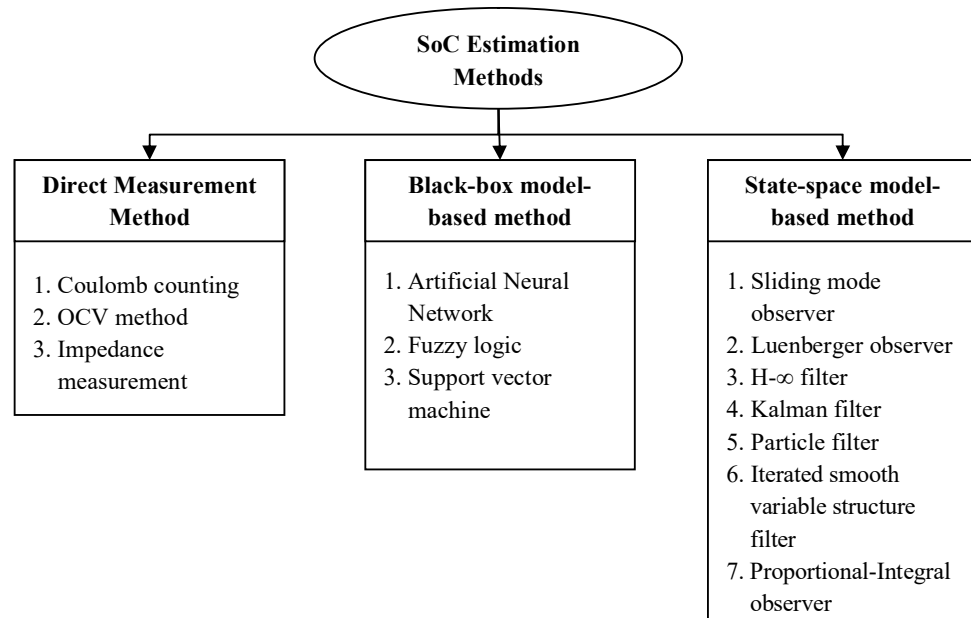
process is expected. Then, a charger control system is applied so that the battery pack is charged under appropriate charging voltage and charging rate. The settings for the charger are unique according to the capacity and voltage of the battery pack.

Battery state estimation is also an important function for BMS. State-of-charge (SoC) and state-of-health (SoH) are the two important states to be estimated. In this context, SoC gives information of the remaining capacity of the battery while SoH presents the performance degradation of battery. These battery states are vital for the EV driver to estimate the real-time status of battery pack. It is considered as the most challenging task for a BMS because the states cannot be measured directly. Moreover, the estimation must be done without affecting the operations of the EV.

### **1.1.3 State-of-charge Estimation**

In general, SoC is defined as the remaining storage energy of a battery. For EV application, SoC estimation acts as the “fuel gauge”, which is crucial for the prediction of driving range. An accurate SoC estimation is required to prevent EVs from running out of charge on the road [41]. Moreover, SoC is important to increase the efficiency of battery by optimally controlling the charge and discharge processes [42], especially in hybrid energy storage systems. However, the estimation of SoC is a complicated process which is dependent on several factors, such as temperature, usable capacity and internal resistance [43]-[44]. Several techniques have been proposed for SoC estimation as shown in Figure 1.5, which can be categorized into three groups [45]-[47]:

- (i) direct measurement methods,
- (ii) black-box model-based methods, and
- (iii) state-space model-based methods.



**Figure 1.5** SoC estimation methods

Direct measurement methods, such as coulomb counting method [48]–[49], open circuit voltage (OCV) method [50] and impedance measurement method [51]–[52], are the open-loop approaches for SoC estimation. These methods indicate SoC by measuring a particular SoC-related parameter. Coulomb counting method, which uses real-time current integration, is widely applied in EVs’ BMS because it is easier to implement with low computation. However, its accuracy is unavoidably affected by the accumulative error caused by uncertain disturbances and sensor noises. Moreover, the method relies on prior knowledge of the initial SoC, which is rarely available in practical applications [46].

OCV method is also applied to indicate SoC by knowing for a fact that the battery terminal voltage at chemical equilibrium state is dependent on SoC. However, an accurate SoC is difficult to be estimated from OCV because the OCV-SoC relationship is nearly flat. It was reported that the variation of OCV is less than 0.2 V for the SoC range between 10 % and 90 % SoC, especially for LFP battery [53]. Therefore, it requires high precision voltage sensors for practical application. Typically, OCV method is applied together with coulomb counting method to

postulate the value of initial SoC. However, a long relaxation time is required for battery to reach its OCV, which is considered impractical for EV applications [54].

Impedance measurement is also a straight-forward method for SoC measurement. In this method, by using electrochemical impedance spectroscopy (EIS), a small alternating current (AC) signal with various frequencies is injected into the battery for impedance measurement. However, the results obtained from EIS is difficult to interpret because the impedance is varied with SoC and temperature [55]. Moreover, the impedance measurement should be done on a battery which is disconnected from a charger or load [56]. Therefore, it is considered not suitable for EV application because the SoC estimation should be done without affecting the EVs' operation.

Black-box battery models, which were established by computational intelligence approaches, are also applied for SoC estimation. In this aspect, a nonlinear relationship between SoC and its influencing parameters are modelled by using artificial neural network (ANN) [57]–[59], fuzzy logic [60]–[62], or support vector machine (SVM) [63][64]. Generally, black-box model-based methods give a good accuracy in SoC estimation due to the powerful capability of the computational intelligence. Unlike coulomb counting method, initial SoC is not required for these methods. Moreover, black-box model can be establishing solely based on the existing input-output training data sets without understanding the chemical reaction of battery. However, their performance is greatly affected by the reliability and the amount of the training data set [65]. Limited amounts of training data set would result in poor robustness [46]. Therefore, a large amount of battery tests are needed to obtain a good model which can be very time-consuming. In addition, the offline learning processes for the black-box model requires iteratively tuning, which leads to heavy computational [47].

State-space model-based methods seem to be the best approach for SoC estimation due to their closed loop nature, real-time estimation, and good reliability. Currently, more attention have been given on the methods and several algorithms, such as sliding-mode observer [66]–[70], Luenberger observer [71], proportional-

integral observer [72], particle filter [73]–[74], iterated smooth variable structure filter [75]–[76],  $H-\infty$  filter [43][77], and Kalman filter [78] have been applied in state-space model-based SoC estimation method. The methods measure current and voltage signals while considering the estimation error range, and thus form a close loop and online SoC estimation method [47][79]. The methods do not rely on an accurate initial SOC, and thus avoids the problem of accumulative error. An accurate state-space model is necessary to establish an accurate SoC estimation. In general practice, state-space model derived from equivalent circuit battery model is applied. Although state-space model can also be derived from electrochemical model [80], a heavier computational burden is required to solve the complicated equations of the electrochemical model.

## 1.2 Problem Statement

The implementation of a new battery technology and development of an efficient BMS is the key to improving the performance of EVs. Currently, LTO battery, which has the features of fast charging and superior safety, is considered as a promising candidate for EV's energy storage system. The fast charging features of a LTO battery can be fully utilised if a reliable battery charger control is realised. For this purpose, an accurate battery model that simulates the charging characteristic of LTO battery is vital.

In addition, an accurate SoC estimation should be realised in order to monitor the operation of the battery. Extended Kalman filter (EKF) and unscented Kalman filter (UKF) are presently considered as the most promising methods for SoC estimation due to their excellent state estimation and noise immunity. However, the accuracy of Kalman filter-based SoC estimation is highly dependent on the prior setting of error covariance. Although the covariance matching adaptive rule is a convenient way to improve the accuracy of Kalman filters, it requires large memory space to operate. An improvement of Kalman filter-based SoC estimation should be



further explored and a new adaptive in order to overcome this shortage must be established.

Meanwhile, the accuracy of the battery model gives a large impact on the Kalman filter-based SoC estimation. Generally, a huge amount of laboratorial experiments are carried out to establish an accurate battery model, which is costly and time consuming. Moreover, the parameters of the battery model are typically varied with several factors, such as SoC, ambient temperature and current. Therefore, the formulated battery model might only be suitable for the specified operating condition. A better approach should be configured to solve these problems.

### **1.3 Thesis Objectives and Contributions**

The objectives of this study are:

- (i) to investigate the dynamic behaviours of LTO battery through several battery tests.
- (ii) to develop a battery model for battery charger design which is suitable for small signal analysis and large signal simulation.
- (iii) to develop a robust SoC estimation method using Kalman filter with genetic algorithm (GA) offline battery modelling.
- (iv) to develop a robust SoC estimation method with online battery modelling using Kalman filter.

While performing this study, the thesis makes the following contributions:

- (i) A new transfer function-based battery model is developed to simulate the charging behaviour of LTO batteries under several charging rates and ambient temperatures. The proposed battery model provides a good solution to the small-signal analysis and large-signal simulation of battery charger designs.
- (ii) Busse's adaptive rule is applied to improve the accuracy of Kalman filter-based SoC estimation. The main motivation is to reduce the

complexity of the existing adaptive rules which require large memory space. Application of Busse's adaptive rule does not need large memory capacity to store the historical data of estimation, and thus is suitable for real-time implementation.

- (iii) Busse's adaptive rule is applied in joint Kalman filter for SoC estimation and online battery modelling. In this aspect, the SoC and model parameters are estimated simultaneously by using Kalman filter. The parameters of the battery model are estimated in real-time without requiring precise measurement tools, experienced researchers and large amount of battery tests, thus reducing the overall complexity of BMS development.

## **1.4 Methodology**

In this thesis, the research methodology is divided into 4 different sessions:

- (i) Experimental test on LTO battery,
- (ii) Formulation of transfer function-based battery model,
- (iii) SoC estimation using Kalman filter, and
- (iv) SoC estimation and online battery modelling using joint Kalman filter.

MATLAB and MATLAB/Simulink are used as the simulator throughout the thesis.

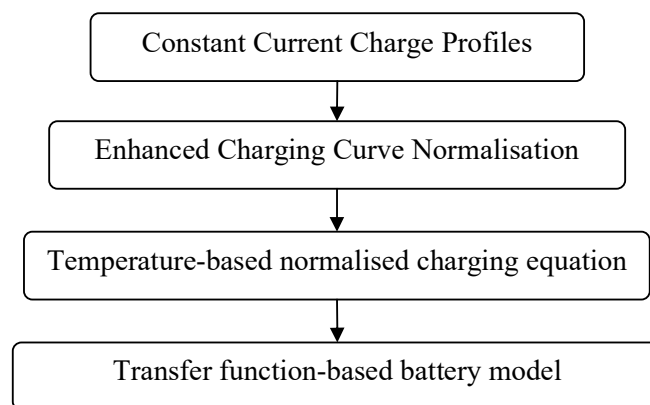
### **1.4.1 Experimental Test on LTO Battery**

First of all, the dynamic voltage-current behaviours of LTO batteries are investigated by using battery tests. In the experimental study, continuous current charge, continuous current discharge, pulsed current charge, and pulsed current discharge tests are combined to form a single profile. This profile is called as continuous current test (CCT) and pulsed current test (PCT). The tests are conducted

by using 3 current rates (i.e. 0.5 C, 1 C, and 2 C) under 4 ambient temperatures (i.e. -25 °C, 0 °C, 25 °C, and 50 °C). Since the PCT is unable to perform at 2 C / -25 °C due to the limitation of battery, only 11 tests are applied for CCT and PCT tests. On the other hand, modified DST is also applied to test the LTO battery under dynamic load conditions. The test is made by modifying the conventional DST so that it suits to our lab capability. The test are conducted under 6 ambient temperature, i.e. -15 °C, 0 °C, 15 °C, 25 °C, 35 °C and 50 °C. Throughout the test, the battery voltage is monitored so that its operating temperature is within 1.6 V – 2.75 V to avoid over-voltage and under-voltage of the battery. The details of the experimental test are further explained in Chapter 3.

#### 1.4.2 Formulation of Transfer function-based Battery Model

In this study, a transfer function-based battery model is formulated to simulate the charging profiles of LTO battery. Figure 1.6 illustrates the methodology for the formulation of transfer function-based battery model.



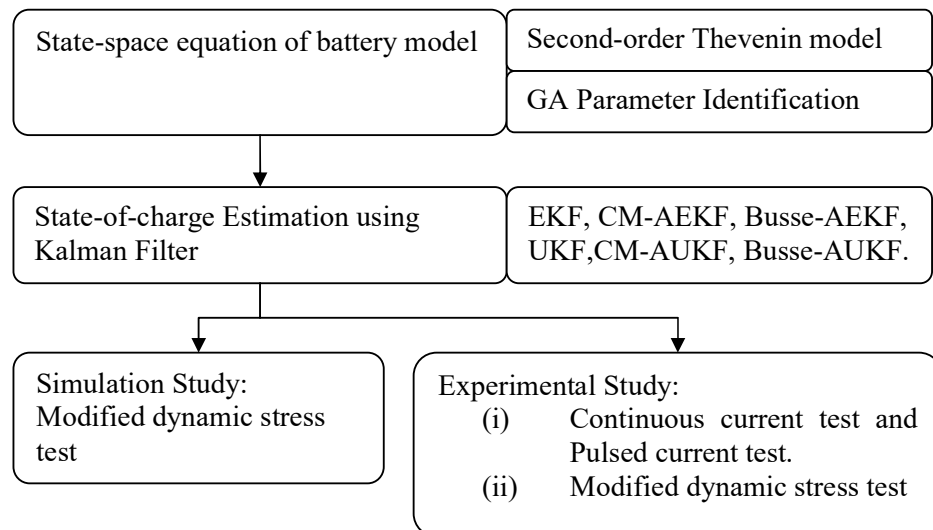
**Figure 1.6** Formulation of transfer function-based battery model

The charging behaviours of LTO battery are obtained from the experimental results of continuous current charge. Enhanced charging curve normalisation is

applied to find out the common characteristics of the battery charging profiles. Then, temperature-based normalised charging equation is developed to simulate the battery charging behaviours at several charge rates and ambient temperatures. Lastly, a transfer function is formulated based on the developed normalised charging equation. The accuracy of the battery model is evaluated by comparing the simulated and experimental charging profiles. Then, the error of the battery modelling is analysed by using root-mean-square error (RMSE) and mean relative error (MRE). The details are further explained in Chapter 4.

### 1.4.3 SoC Estimation using Kalman Filter

Figure 1.7 illustrates the methodology of SoC estimation using Kalman filter; both with adaptive rule and without adaptive rule.



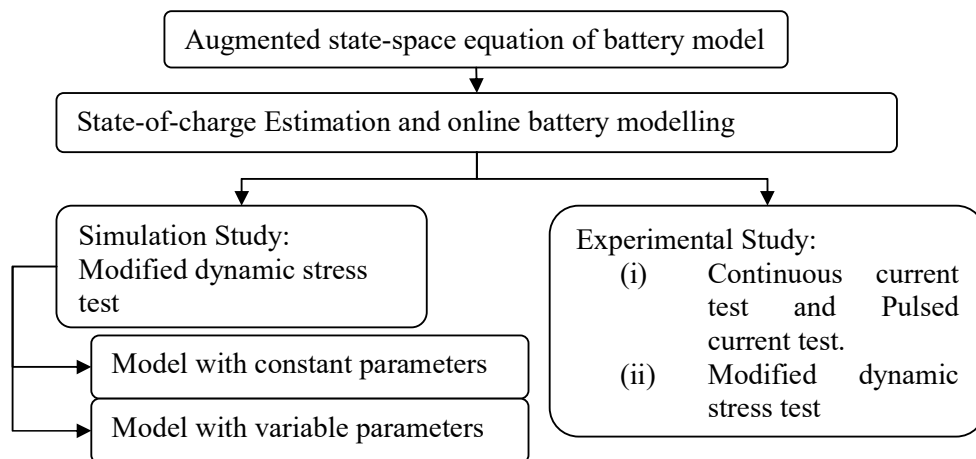
**Figure 1.7** SoC estimation using Kalman filter

In SoC estimation, second-order Thevenin model is used to simulate the electrical behaviours of the battery. Genetic algorithm (GA) is applied to identify the parameters of the battery model. In order to implement Kalman filter-based SoC

estimation, the second-order Thevenin model is first transformed into a state-space model. Based on the state-space model, the SoC estimation is performed by using Extended Kalman filter (EKF), Unscented Kalman filter (UKF), Covariance-matching adaptive EKF, Covariance-matching adaptive UKF, Busse's adaptive EKF, and Busse's adaptive UKF. The accuracy of the SoC estimation is analysed by using simulation and experimental study. Then, the error of SoC estimation is analysed by using root-mean-square error (RMSE) and mean relative error (MRE). The details are further explained in Chapter 5.

#### 1.4.4 SoC Estimation and Online Battery Modelling using Joint Kalman filter

Figure 1.8 illustrates the methodology of SoC estimation and online battery modelling using joint Kalman filter.



**Figure 1.8** SoC estimation and online battery modelling using Joint Kalman filter

In order to implement joint Kalman filter, an augmented state-space model is formed based on the structure of second-order Thevenin model, where the state equation includes both battery state and battery parameters. By using the augmented state-space model, the SoC estimation and online battery modelling are performed simultaneously by using Extended Kalman filter (EKF), Unscented Kalman filter

(UKF), Covariance-matching adaptive EKF, Covariance-matching adaptive UKF, Busse's adaptive EKF, and Busse's adaptive UKF. The accuracy of the SoC estimation is analysed by using simulation and experimental study. In simulation study, battery model with constant parameters, and battery model with variable parameters are applied to investigate the accuracy of SoC estimation and online battery modelling performed by the algorithms. Moreover, the error of SoC estimation and battery modelling are analysed by using root-mean-square error (RMSE) and mean relative error (MRE). The details are further explained in Chapter 6.

## **1.5 Scope of Research**

Battery modelling and SoC estimation are wide-ranging research topics. In this thesis, LTO battery is chosen since it is considered as the latest technology for Li-ion battery. Transfer function-based model and equivalent circuit model are studied in detail in this thesis. The transfer function-based model is developed based on the charging behaviours of LTO cells, however, it is also believed that the methodology of the formulation of transfer function-based model could be applied for another types of battery. The transfer function-based model is developed for the purpose of charger design and it represents battery behaviours as an empirical equation. It is important to clarify that it is not representing the exact electrochemical processes within the battery.

For equivalent circuit model, second-order Thevenin model is applied in this research. The battery model is formulated based on the electrical characteristics of the LTO battery without considering OCV hysteresis effect, self-discharge effect, capacity fading losses and calendar losses. The thermal modelling of the battery is also not included in the battery modelling. Most importantly, only cell level modelling is presented in this thesis, which is not similar to the multiple cells as applied in EV battery pack. This approach is made in order to avoid the multiple cells issues, such as cell imbalance and cell voltage monitoring.

Kalman filter-based SoC estimation technique is chosen for this thesis due to its robustness as proven by the previous literatures. Extended Kalman filter and Unscented Kalman filter are applied in the study. Moreover, covariance matching rule and Busse's adaptive rule are chosen as the adaptive rules for Kalman filter. For the purpose of verification, a benchmark for the SoC estimation is created, where the laboratorial Ah-counting method is applied to find out the true SoC value throughout the battery tests.

## 1.6 Thesis Organisation

The rest of the thesis is organised as follows:

**Chapter 2** provides a literature review on the dynamic behaviours of a battery, battery models, battery tests and parameter identification techniques. The applications of Kalman filters for online battery modelling and SoC estimation are also reviewed. The algorithm of EKF, UKF and the existing adaptive rules are also explained in detail.

**Chapter 3** describes the experimental set-up used in the thesis. The procedures of battery tests, which are used to identify the parameters of the battery model are presented and described.

**Chapter 4** proposes a transfer function-based battery model to simulate the charging behaviours of LTO battery. A new approach of capturing nonlinear charging behaviours is also presented in detail. Simulation and the experimental study on the proposed battery model are also presented. The performance of the proposed battery model is discussed.

**Chapter 5** proposes the application of Busse's adaptive rule in Kalman filter-based SoC estimation. In this case, the Busse's adaptive rule is applied on both EKF

and UKF. The performance of Busse's adaptive EKF and Busse's adaptive UKF is compared with the conventional EKF and UKF, as well as the covariance-matching adaptive EKF and covariance-matching adaptive UKF. Simulation and experimental studies have been done to verify the proposed method.

**Chapter 6** applies Kalman filter for SoC estimation with online battery modelling. In this case, SoC and model parameters are estimated simultaneously by using joint Kalman filters. Similar to Chapter 5, Busse's adaptive rule is proposed to increase the accuracy of the SoC estimation with online battery modelling. The simulation and experimental studies have been done to verify the proposed method.

**Chapter 7** gives the conclusion of the thesis and possible directions of further research on this work.



## REFERENCES

- [1] International Energy Agency (IEA). *Technology roadmap: Electric and plug-in hybrid electric vehicles*. France: Int. Energy Agency. 2011
- [2] D. Doughty and E. P. Roth. A General Discussion of Li Ion Battery Safety. *Electrochem. Soc. Interface*. 2012. Summer: 37–44, 2012.
- [3] A. Rosin and V. Tallinn. Energy storages. In: M. Ehsani, Y. Gao, S. E. Gay, and A. Emadi. *Modern Electric, Hybrid Electric, and Fuel Cell Vehicles*. Florida : CRC Press LLC. 300–332; 2012
- [4] M. Ehsani, Y. Gao, S. E. Gay, and A. Emadi. Fuel Cell Vehicles. In: M. Ehsani, Y. Gao, S. E. Gay, and A. Emadi. *Modern Electric, Hybrid Electric, and Fuel Cell Vehicles*. Florida : CRC Press LLC. 348–373; 2005
- [5] D. Mori and K. Hirose. Recent challenges of hydrogen storage technologies for fuel cell vehicles. *Int. J. Hydrogen Energy*. 2009. Vol. 34 (10): 4569–4574.
- [6] S. G. Chalk and J. F. Miller. Key challenges and recent progress in batteries, fuel cells, and hydrogen storage for clean energy systems. *J. Power Sources*. 2006. Vol. 159 (1): 73–80.
- [7] S. Eaves and J. Eaves. A cost comparison of fuel-cell and battery electric vehicles. *J. Power Sources*. 2004. Vol. 130(1–2): 208–212.
- [8] M. Uno and K. Tanaka. Accelerated Charge – Discharge Cycling Test and Cycle Life Prediction Model for Supercapacitors in Alternative Battery Applications. *IEEE Trans. Industrial Electronics*. 2012. Vol. 59 (12): 4704–4712.
- [9] H. Ibrahim, A. Ilinca, and J. Perron. Energy storage systems—Characteristics and comparisons. *Renew. Sustain. Energy Rev*. 2008. Vol. 12 (5): 1221–1250.
- [10] N. Schofield, H. T. Yap, and C. M. Bingham. Hybrid Energy Sources for Electric and Fuel Cell Vehicle Propulsion. *2005 IEEE Veh. Power Propuls. Conf.* September 7-9, 2005. IL, USA: IEEE. 2005. 42–49.
- [11] P. Thounthong, S. Raël, and B. Davat. Energy management of fuel

- cell/battery/supercapacitor hybrid power source for vehicle applications. *J. Power Sources*. 2009. Vol. 193 (1): 376–385.
- [12] P. Rodatz, G. Paganelli, A. Sciarretta, and L. Guzzella. Optimal power management of an experimental fuel cell/supercapacitor-powered hybrid vehicle. *Control Eng. Pract.* 2005. Vol. 13 (1): 41–53.
- [13] V. Paladini, T. Donato, A. de Risi, and D. Laforgia. Super-capacitors fuel-cell hybrid electric vehicle optimization and control strategy development. *Energy Convers. Manag.* 2007. Vol. 48 (11): 3001–3008.
- [14] J. Wong, N. R. N. Idris, M. Anwari, and T. Taufik. A parallel energy-sharing control for fuel cell-battery-ultracapacitor hybrid vehicle. *Proc. of the 2011 IEEE Energy Convers. Congr. Expo. ECCE 2011*. September 17 – 22, 2011. Phoenix, AZ: IEEE. 2011. 2923–2929.
- [15] P. Thounthong, S. Raël, and B. Davat. Control strategy of fuel cell/supercapacitors hybrid power sources for electric vehicle. *J. Power Sources*. 2006. Vol. 158 (1): 806–814.
- [16] J. H. Wong, N. R. N. Idris, and M. Anwari. Parallel configuration in energy management control for the fuel cell-battery-ultracapacitor hybrid vehicles. *2011 IEEE Appl. Power Electron. Colloq.* April 18-19, 2011. Johor Bahru: IEEE. 2011. 69–74.
- [17] A. Wangsupphaphol, N. R. N. Idris, A. Jusoh, N. D. Muhamad, and I. M. Alsofyani. Acceleration-based design auxiliary power source for Electric Vehicle applications. *2014 11th International Conference on Electrical Engineering/Electronics, Computer, Telecommunications and Information Technology (ECTI-CON)*. May 14-17, 2014. Nakhon Ratchasima: IEEE. 2014. 1–6.
- [18] A. Wangsupphaphol, N. R. N. Idris, A. Jusoh, N. D. Muhamad, and L. W. Yao. The Energy Management Control Strategy for Electric Vehicle Applications. *2014 International Conference and Utility Exhibition on Green Energy for Sustainable Development (ICUE)*. March 19-21, 2014. Pattaya: IEEE. 2014. 1–5.
- [19] A. Wangsupphaphol, N. R. N. Idris, A. Jusoh, N. D. Muhamad, and I. M. Alsofyani. Energy and power control strategy for battery electric vehicle with supercapacitors. *2014 IEEE Conference on Energy Conversion (CENCON)*. Oct. 13-14, 2014. Johor Bahru: IEEE. 2014. 13–18.

- [20] A. Eddahech, M. Ayadi, O. Briat, and J.-M. Vinassa. Online parameter identification for real-time supercapacitor performance estimation in automotive applications. *Int. J. Electr. Power Energy Syst.* 2013. Vol. 51: 162–167.
- [21] J. Tarascon and M. Armand. Issues and challenges facing rechargeable lithium batteries. *Nature.* 2001. Vol. 414 (November): 359–367.
- [22] M. Urbain, M. Hinaje, S. Raël, B. Davat, and P. Desprez. Energetical Modeling of Lithium-Ion Batteries Including Electrode Porosity Effects. *IEEE Trans. Energy Convers.* 2010. Vol. 25 (3): 862–872.
- [23] S. F. Tie and C. W. Tan. A review of energy sources and energy management system in electric vehicles. *Renew. Sustain. Energy Rev.* 2013. Vol. 20: 82–102.
- [24] Electropaedia. Rechargeable Lithium Batteries. *Woodbank Communications Ltd*, 2005. [Online]. Available: <http://www.mpoweruk.com/lithiumS.htm>. [Accessed: 13-Dec-2015].
- [25] L. Lu, X. Han, J. Li, J. Hua, and M. Ouyang. A review on the key issues for lithium-ion battery management in electric vehicles. *J. Power Sources.* 2013. Vol. 226: 272–288.
- [26] M. a. Hannan, F. a. Azidin, and A. Mohamed. Hybrid electric vehicles and their challenges: A review. *Renew. Sustain. Energy Rev.* 2014. Vol. 29: 135–150.
- [27] N. Terada, T. Yanagi, S. Arai, and M. Yoshikawa. Development of lithium batteries for energy storage and EV applications. *J. Power Sources.* 2001. Vol. 100: 80–92.
- [28] E. Corporation. Comparative Lithium Battery Chemistries. [Online]. Available: [http://www.hybridpropulsion.com/battery\\_chemistry\\_lithium\\_iron\\_phosphate.pdf](http://www.hybridpropulsion.com/battery_chemistry_lithium_iron_phosphate.pdf) [Accessed: 05-April-2016]
- [29] A.-I. Stan, M. Swierczynski, D.-I. Stroe, R. Teodorescu, and S. J. Andreasen. Lithium ion battery chemistries from renewable energy storage to automotive and back-up power applications — An overview. *2014 Int. Conf. Optim. Electr. Electron. Equip.* May 22-24, 2014. Bran: IEEE. 2014. 713–720.
- [30] Y. Sha, T. Yuan, B. Zhao, R. Cai, H. Wang, and Z. Shao. Solid lithium electrolyte-Li<sub>4</sub>Ti<sub>5</sub>O<sub>12</sub> composites as anodes of lithium-ion batteries showing high-rate performance. *J. Power Sources.* 2013. Vol. 231:177–185.

- [31] D. Bresser, E. Paillard, M. Copley, P. Bishop, M. Winter, and S. Passerini. The importance of ‘going nano’ for high power battery materials. *J. Power Sources*. 2012. Vol. 219: 217–222.
- [32] I. Buchmann. Types of Lithium-ion. *Cadex Electronics*, 2015. [Online]. Available: [http://batteryuniversity.com/learn/article/types\\_of\\_lithium\\_ion](http://batteryuniversity.com/learn/article/types_of_lithium_ion). [Accessed: 13-Dec-2015].
- [33] Y. Xing, E. W. M. Ma, K. L. Tsui, and M. Pecht. Battery Management Systems in Electric and Hybrid Vehicles. *Energies*. 2011. Vol. 4 (12): 1840–1857.
- [34] Electropedia. Lithium Battery Failures. *Woodbank Communications Ltd*, 2005. [Online] Available: [http://www.mpoweruk.com/lithium\\_failures.htm](http://www.mpoweruk.com/lithium_failures.htm). [Accessed: 05-April-2015].
- [35] D. Y. Jung, B. H. Lee, and S. W. Kim. Development of battery management system for nickel–metal hydride batteries in electric vehicle applications. *J. Power Sources*. 2002. Vol. 109 (1): 1–10.
- [36] K. W. E. Cheng, B. P. Divakar, H. Wu, K. Ding, and H. F. Ho. Battery-Management System (BMS) and SOC Development for Electrical Vehicles. *IEEE Trans. Veh. Technol.* 2011. Vol. 60 (1): 76–88.
- [37] D. D. Friel. Management of Batteries for Electric Traction Vehicles. In: G. Pistoia. *Electric and Hybrid Vehicles*. Elsevier B.V. 493–515; 2010
- [38] Z. J. Tang, Q. Z. Zhu, J. W. Lu, and M. Y. Wu. Study on Various Types of Cooling Techniques Applied to Power Battery Thermal Management Systems. *Adv. Mater. Res.* 2012. Vol. 608–609: 1571–1576.
- [39] S. a. Khateeb, S. Amiruddin, M. Farid, J. R. Selman, and S. Al-Hallaj. Thermal management of Li-ion battery with phase change material for electric scooters: experimental validation. *J. Power Sources*. 2005. Vol. 142 (1–2): 345–353.
- [40] S. W. Moore and P. J. Schneider. *A Review of Cell Equalization Methods for Lithium Ion and Lithium Polymer Battery Systems*. SAE Publication. 2001.
- [41] W. He, N. Williard, C. Chen, and M. Pecht. State of charge estimation for electric vehicle batteries using unscented kalman filtering. *Microelectron. Reliab.* 2013. Vol. 53 (6): 840–847.
- [42] S. Qiu, Z. Chen, M. A. Masrur, and Y. L. Murphey. Battery hysteresis modeling for state of charge estimation based on Extended Kalman Filter.

- 2011 6th IEEE Conference on Industrial Electronics and Applications. June 21-23, 2011. Beijing: IEEE. 2011. 184–189.
- [43] C. Lin, F. Zhang, H. Xue, and X. Lu. Estimation of battery state of charge using  $H_{\infty}$  observer. *2012 7th International Power Electronics and Motion Control Conference*. June 2-5, 2012. Harbin: IEEE. 2012. 422–428.
- [44] W. Junping, G. Jingang, and D. Lei. An adaptive Kalman filtering based State of Charge combined estimator for electric vehicle battery pack. *Energy Convers. Manag.* 2009. Vol. 50 (12): 3182–3186.
- [45] S. Dey, B. Ayalew, and P. Pisu. Nonlinear Robust Observers for State-of-Charge Estimation of Lithium-Ion Cells Based on a Reduced Electrochemical Model. *IEEE Trans. Control Syst. Technol.* 2015. Vol. 23 (5): 1935-1942.
- [46] F. Sun, X. Hu, Y. Zou, and S. Li. Adaptive unscented Kalman filtering for state of charge estimation of a lithium-ion battery for electric vehicles. *Energy*. 2011. Vol. 36 (5): 3531–3540.
- [47] H. He, R. Xiong, X. Zhang, F. Sun, J. Fan, and S. Member. State-of-Charge Estimation of the Lithium-Ion Battery Using an Adaptive Extended Kalman Filter Based on an Improved Thevenin Model. *IEEE Trans. Veh. Technol.* 2011. Vol. 60 (4): 1461–1469.
- [48] K. S. Ng, C.-S. Moo, Y.-P. Chen, and Y.-C. Hsieh. Enhanced coulomb counting method for estimating state-of-charge and state-of-health of lithium-ion batteries. *Appl. Energy*. 2009. Vol. 86 (9): 1506–1511.
- [49] K. Kutluay, Y. Cadirci, Y. S. Ozkazanc, and I. Cadirci. A New Online State-of-Charge Estimation and Monitoring System for Sealed Lead–Acid Batteries in Telecommunication Power Supplies. *IEEE Trans. Ind. Electron.* 2005. Vol. 52 (5): 1315–1327.
- [50] L. Pei, C. Zhu, and R. Lu. Relaxation model of the open-circuit voltage for state-of-charge estimation in lithium-ion batteries. *IET Electr. Syst. Transp.* 2013. Vol. 3 (4): 112–117.
- [51] F. Huet. A review of impedance measurements for determination of the state-of-charge or state-of-health of secondary batteries. *J. Power Sources*. 1998. Vol. 70 (1): 59–69.
- [52] J. Xu, C. C. Mi, B. Cao, and J. Cao. A new method to estimate the state of charge of lithium-ion batteries based on the battery impedance model. *J. Power Sources*. 2013. Vol. 233: 277–284.

- [53] M. Mastali, J. Vazquez-Arenas, R. Fraser, M. Fowler, S. Afshar, and M. Stevens. Battery state of the charge estimation using Kalman filtering. *J. Power Sources*. 2013. Vol. 239: 294–307.
- [54] Y. Hua, M. Xu, M. Li, C. Ma, and C. Zhao. Estimation of State of Charge for Two Types of Lithium-Ion Batteries by Nonlinear Predictive Filter for Electric Vehicles. *Energies*. 2015. Vol. 8 (5): 3556–3577.
- [55] R. Xiong, X. Gong, C. C. Mi, and F. Sun. A robust state-of-charge estimator for multiple types of lithium-ion batteries using adaptive extended Kalman filter. *J. Power Sources*. 2013. Vol. 243: 805–816.
- [56] I. Kim. A Technique for Estimating the State of Health of Lithium Batteries Through a Dual-Sliding-Mode Observer. *IEEE Trans. Power Electron.* 2010. Vol. 25 (4): 1013–1022.
- [57] I. Anand and B. L. Mathur. State of charge estimation of lead acid batteries using neural networks. *2013 International Conference on Circuits, Power and Computing Technologies (ICCPCT)*. March 20-21, 2013. Nagercoil: IEEE. 2013. 596–599.
- [58] C. H. Cai, D. Du, and Z. Y. Liu. Battery state-of-charge (SOC) estimation using adaptive neuro-fuzzy inference system (ANFIS). *The 12th IEEE International Conference on Fuzzy Systems, 2003*. May 25-28, 2003. IEEE/2003. 1068–1073.
- [59] I. Li, W. Wang, S. Su, and Y. Lee. A Merged Fuzzy Neural Network and Its Applications in Battery State-of-Charge Estimation. *IEEE Trans. Energy Convers.* 2007. Vol. 22 (3): 697–708.
- [60] R. Feng, S. Zhao, and X. Lu. On-line estimation of Dynamic State-of-Charge for lead acid battery based on fuzzy logic. *Proceedings of 2013 2nd International Conference on Measurement, Information and Control*. Aug. 16-18, 2013. Harbin: IEEE. 2013. 447–451.
- [61] D. Jiani, L. Zhitao, W. Youyi, and W. Changyun. A fuzzy logic-based model for Li-ion battery with SOC and temperature effect. *11th IEEE International Conference on Control & Automation (ICCA)*. June 18-20, 2014. Taichung: IEEE. 2014. 1333–1338.
- [62] A. J. Salkind, C. Fennie, P. Singh, T. Atwater, and D. E. Reisner. Determination of state-of-charge and state-of-health of batteries by fuzzy logic methodology. *J. Power Sources*. 1999. Vol. 80(1–2): 293–300.

- [63] W. Junping, C. Quanshi, and C. Binggang. Support vector machine based battery model for electric vehicles. *Energy Convers. Manag.* 2006. Vol. 47 (7–8): 858–864.
- [64] J. C. Alvarez Anton, P. J. Garcia Nieto, C. Blanco Viejo, and J. A. Vilan Vilan. Support Vector Machines Used to Estimate the Battery State of Charge. *IEEE Trans. Power Electron.* 2013. Vol. 28 (12): 5919–5926.
- [65] D. Di Domenico, E. Prada, and Y. Creff. An adaptive strategy for Li-ion battery SOC estimation. *IFAC World Congress.* Aug 28 - Sept. 2, 2011. Milano: IFAC. 2011. 9721–9726.
- [66] F. Zhang and G. Liu. A battery state of charge estimation method using sliding mode observer. *2008 7th World Congr. Intell. Control Autom.* June 25-27, 2008. Chongqing: IEEE. 2008. 989–994.
- [67] X. Chen, W. Shen, Z. Cao, and A. Kapoor. Adaptive gain sliding mode observer for state of charge estimation based on combined battery equivalent circuit model. *Comput. Chem. Eng.* 2014. Vol. 64: 114–123.
- [68] I.-S. Kim. The novel state of charge estimation method for lithium battery using sliding mode observer. *J. Power Sources.* 2006. Vol. 163 (1): 584–590.
- [69] M. Gholizadeh and F. R. Salmasi. Estimation of State of Charge, Unknown Nonlinearities, and State of Health of a Lithium-Ion Battery Based on a Comprehensive Unobservable Model. *IEEE Trans. Ind. Electron.* 2014. Vol. 61 (3): 1335–1344.
- [70] I. Kim. Nonlinear State of Charge Estimator for Hybrid Electric Vehicle Battery. *IEEE Trans. Power Electron.* 2008. Vol. 23 (4): 2027–2034.
- [71] X. Hu, F. Sun, and Y. Zou. Estimation of State of Charge of a Lithium-Ion Battery Pack for Electric Vehicles Using an Adaptive Luenberger Observer. *Energies.* 2010. Vol. 3 (9): 1586–1603.
- [72] J. Xu, C. Mi, B. Cao, and J. Deng. The state of charge estimation of lithium-ion batteries based on a proportional-integral observer. *IEEE Trans. Veh. Technol.* 2014. Vol. 63 (4): 1614–1621.
- [73] Y. Wang, C. Zhang, and Z. Chen. A method for state-of-charge estimation of LiFePO<sub>4</sub> batteries at dynamic currents and temperatures using particle filter. *J. Power Sources.* 2015. Vol. 279: 306–311.
- [74] X. Liu, Z. Chen, C. Zhang, and J. Wu. A novel temperature-compensated model for power Li-ion batteries with dual-particle-filter state of charge

- estimation. *Appl. Energy*. 2014. Vol. 123: 263–272.
- [75] T. Kim, Y. Wang, H. Fang, Z. Sahinoglu, T. Wada, S. Hara, and W. Qiao. Model-Based Condition Monitoring for Lithium-ion Batteries. *J. Power Sources*. 2015. Vol. 295: 16–27.
- [76] T. Kim, Y. Wang, Z. Sahinoglu, T. Wada, S. Hara, and W. Qiao. State of charge estimation based on a realtime battery model and iterative smooth variable structure filter. *2014 IEEE Innovative Smart Grid Technologies - Asia (ISGT ASIA)*. May 20-13, 2014. Kuala Lumpur: IEEE. 2014. 132–137.
- [77] F. Zhang, G. Liu, L. Fang, and H. Wang. Estimation of Battery State of Charge With  $H_{\infty}$  Observer: Applied to a Robot for Inspecting Power Transmission Lines. *IEEE Trans. Ind. Electron.* 2012. Vol. 59 (2):1086–1095.
- [78] B. Bhangu and P. Bentley. Observer techniques for estimating the state-of-charge and state-of-health of VRLABs for hybrid electric vehicles. *2015 IEEE Conference on Veh. Power and Propulsion*. Sept. 7-9, Chicago: IEEE. 2005. 780–789.
- [79] Z. Zou, J. Xu, C. Mi, B. Cao, and Z. Chen. Evaluation of Model Based State of Charge Estimation Methods for Lithium-Ion Batteries. *Energies*. 2014. Vol. 7 (8): 5065–5082.
- [80] S. Santhanagopalan and R. E. White. State of charge estimation using an unscented filter for high power lithium ion cells. *Int. J. Energy Res.* 2010. Vol. 34 (2): 152–163.
- [81] R. Rao, S. Vrudhula, and D. Rakhmatov. Battery modeling for energy aware system design. *Computer*. 2003. Vol. 12: 77–87.
- [82] F. Feng, R. Lu, and C. Zhu. A Combined State of Charge Estimation Method for Lithium-Ion Batteries Used in a Wide Ambient Temperature Range. *Energies*. 2014. Vol. 7 (5): 3004–3032.
- [83] L. Gao, S. Liu, and R. A. Dougal. Dynamic lithium-ion battery model for system simulation. *IEEE Trans. Components Packag. Technol.* 2002. Vol. 25 (3): 495–505.
- [84] A. Shafiei, A. Momeni, and S. S. Williamson. Battery modeling approaches and management techniques for Plug-in Hybrid Electric Vehicles. *2011 IEEE Vehicle Power and Propulsion Conference*. Sept 6 - 9, 2011. Chicago: IEEE. 2011. 1–5.
- [85] M. Garcia-Plaza, J. E.-G. Carrasco, and J. Alonso-Martinez. State of charge



- estimation model for Ni-Cd batteries considering capacity and efficiency. *2015 IEEE International Conference on Industrial Technology (ICIT)*. March 17-19, 2015. Seville: IEEE. 2015. 1185–1190.
- [86] D. E. Corp. Temperature Effects on Battery Performance & Life. 2015. [Online] Available: [www.heliant.it/images/FV/ev\\_temperature\\_effects.pdf](http://www.heliant.it/images/FV/ev_temperature_effects.pdf) [Accessed: 05-April-2015].
- [87] C. Zhang, J. Jiang, W. Zhang, Y. Wang, S. M. Sharkh, and R. Xiong. A novel data-driven fast capacity estimation of spent electric vehicle lithium-ion batteries. *Energies*. 2014. Vol. 7 (12): 8076–8094.
- [88] H. Zhang and M. Chow. Comprehensive dynamic battery modeling for PHEV applications. *Power and Energy Society General Meeting*. July 25-29, 2010. MN: IEEE. 2010. 1–6.
- [89] I. Snihir, W. Rey, E. Verbitskiy, A. Belfadhel-Ayeb, and P. H. L. Notten. Battery open-circuit voltage estimation by a method of statistical analysis. *J. Power Sources*. 2006. Vol. 159 (2): 1484–1487.
- [90] M. Coleman and W. G. Hurley. State-of-Charge Determination From EMF Voltage Estimation: Using Impedance, Terminal Voltage, and Current for Lead-Acid and Lithium-Ion Batteries. *IEEE Trans. Ind. Electron.* 2007. Vol. 54 (5): 2550–2557.
- [91] H. He, X. Zhang, R. Xiong, Y. Xu, and H. Guo. Online model-based estimation of state-of-charge and open-circuit voltage of lithium-ion batteries in electric vehicles. *Energy*. 2012. Vol. 39 (1): 310–318.
- [92] F. Baronti, N. Femia, R. Saletti, C. Visone, and W. Zamboni. Hysteresis Modeling in Li-Ion Batteries. *IEEE Trans. Magn.* 2014. Vol. 50 (11): 1–4.
- [93] M. a. Roscher and D. U. Sauer. Dynamic electric behavior and open-circuit-voltage modeling of LiFePO<sub>4</sub>-based lithium ion secondary batteries. *J. Power Sources*. 2011. Vol. 196 (1): 331–336.
- [94] T. Kim, W. Qiao, and L. Qu. Hysteresis Modeling for Model-Based Condition Monitoring of Lithium-Ion Batteries. *2015 IEEE Energy Conversion Congress and Exposition*. Sept 20-24, 2015. Montreal: IEEE. 2015. 5068–5073.
- [95] G. L. Plett. Extended Kalman filtering for battery management systems of LiPB-based HEV battery packs: Part 2. Modeling and identificatio. *J. Power Sources*. 2004. Vol. 134 (2): 262–276.
- [96] C. Weng, J. Sun, and H. Peng. A unified open-circuit-voltage model of

- lithium-ion batteries for state-of-charge estimation and state-of-health monitoring. *J. Power Sources*. 2014. Vol. 258: 228–237.
- [97] Z. Chen, Y. Fu, and C. C. Mi. State of Charge Estimation of Lithium-Ion Batteries in Electric Drive Vehicles Using Extended Kalman Filtering. *IEEE Trans. Veh. Technol.* 2013. Vol. 62 (3): 1020–1030.
- [98] C. Zhang, J. Liu, S. Sharkh, and C. Zhang. Identification of dynamic model parameters for lithium-ion batteries used in hybrid electric vehicles. *High Technol Lett.* 2010. Vol. 1: 6–12.
- [99] R. Benger, H. Wenzl, H. Beck, and M. Jiang. Electrochemical and thermal modeling of lithium-ion cells for use in HEV or EV application. *World Electr. Veh. J.* 2009. Vol. 3 : 1–10.
- [100] Y. Hu, S. Yurkovich, Y. Guezennec, and B. J. Yurkovich. Electro-thermal battery model identification for automotive applications. *J. Power Sources*. 2011. Vol. 196 (1): 449–457.
- [101] K. Murashko, J. Pyrhonen, and L. Laurila. Three-Dimensional Thermal Model of a Lithium Ion Battery for Hybrid Mobile Working Machines: Determination of the Model Parameters in a Pouch Cell. *IEEE Trans. Energy Convers.* 2013. Vol. 28 (2): 335–343.
- [102] F. Feng, R. Lu, G. Wei, and C. Zhu. Online Estimation of Model Parameters and State of Charge of LiFePO<sub>4</sub> Batteries Using a Novel Open-Circuit Voltage at Various Ambient Temperatures. *Energies*. 2015. Vol. 8 (4): 2950–2976.
- [103] Y. Xing, W. He, M. Pecht, and K. L. Tsui. State of charge estimation of lithium-ion batteries using the open-circuit voltage at various ambient temperatures. *Appl. Energy*. 2014. Vol. 113: 106–115.
- [104] K. Smith and C.-Y. Wang. Solid-state diffusion limitations on pulse operation of a lithium ion cell for hybrid electric vehicles. *J. Power Sources*. 2006. Vol. 161 (1): 628–639.
- [105] R. Yazami and Y. Ozawa. A kinetics study of self-discharge of spinel electrodes in Li/LixMn<sub>2</sub>O<sub>4</sub> cells. *J. Power Sources*. 2006. Vol. 153 (2): 251–257.
- [106] I. Buchmann. What does Elevated Self - discharge do. *Cadex Electronics*, 2015. [Online]. Available: [http://batteryuniversity.com/learn/article/elevating\\_self\\_discharge](http://batteryuniversity.com/learn/article/elevating_self_discharge). [Accessed:

25-Dec-2015].

- [107] J. Kang and G. Rizzoni. Study of relationship between temperature and thermal energy, operating conditions as well as environmental factors in large-scale lithium-ion batteries. *Int. J. Energy Res.* 2014. Vol. 38 (15): 1994–2002.
- [108] M. Chen and G. A. Rincón-Mora. Accurate electrical battery model capable of predicting runtime and I-V performance. *IEEE Trans. Energy Convers.* 2006. Vol. 21 (2): 504–511.
- [109] I. Buchmann. What does Elevated Self - discharge do. *Cadex Electronics*, 2015. [Online]. Available: [http://batteryuniversity.com/learn/article/elevating\\_self\\_discharge](http://batteryuniversity.com/learn/article/elevating_self_discharge).
- [110] K. Maher and R. Yazami. A study of lithium ion batteries cycle aging by thermodynamics techniques. *J. Power Sources.* 2014. Vol. 247: 527–533.
- [111] L. Tan, L. Zhang, Q. Sun, M. Shen, Q. Qu, and H. Zheng. Capacity loss induced by lithium deposition at graphite anode for LiFePO<sub>4</sub>/graphite cell cycling at different temperatures. *Electrochim. Acta.* 2013. Vol. 111: 802–808.
- [112] G. Sarre, P. Blanchard, and M. Broussely. Aging of lithium-ion batteries. *J. Power Sources.* 2004. Vol. 127 (1–2): 65–71.
- [113] G. Plett. Dual and Joint EKF for Simultaneous SOC and SOH Estimation. *Proceedings of the 21st Electric Vehicle Symposium (EVS21)*. April 2-6 2005. Monaco: EVS. 2005. 1–12.
- [114] T. Kim, W. Qiao, and L. Qu. Online SOC and SOH estimation for multicell lithium-ion batteries based on an adaptive hybrid battery model and sliding-mode observer. *2013 IEEE Energy Convers. Congr. Expo.* Sept 25-19, 2013. Denver, CO: IEEE. 2013. 292–298.
- [115] T. Kim and W. Qiao. A Hybrid Battery Model Capable of Capturing Dynamic Circuit Characteristics and Nonlinear Capacity Effects. *IEEE Trans. Energy Convers.* 2011. Vol. 26 (4): 1172–1180.
- [116] K. a. Smith, C. D. Rahn, and C.-Y. Wang. Model-Based Electrochemical Estimation and Constraint Management for Pulse Operation of Lithium Ion Batteries. *IEEE Trans. Control Syst. Technol.* 2010. Vol. 18 (3): 654–663.
- [117] M. Corno, N. Bhatt, S. M. Savaresi, and M. Verhaegen. Electrochemical Model-Based State of Charge Estimation for Li-Ion Cells. *IEEE Trans. Control Syst. Technol.* 2015. Vol. 23 (1): 117–127.
- [118] R. Klein, N. a. Chaturvedi, J. Christensen, J. Ahmed, R. Findeisen, and A.

- Kojic. Electrochemical Model Based Observer Design for a Lithium-Ion Battery. *IEEE Trans. Control Syst. Technol.* 2013. Vol. 21 (2): 289–301.
- [119] K. Smith. Electrochemical Control of Lithium-Ion Batteries. *IEEE Control Syst. Mag.* 2010. Vol. 30 (2): 18–25.
- [120] M. W. Verbrugge and P. Liu. Electrochemical characterization of high-power lithium ion batteries using triangular voltage and current excitation sources. *J. Power Sources.* 2007. Vol. 174 (1): 2–8.
- [121] K. a. Smith, C. D. Rahn, and C.-Y. Wang. Control oriented 1D electrochemical model of lithium ion battery. *Energy Convers. Manag.* 2007. Vol. 48 (9): 2565–2578.
- [122] N. Chaturvedi, R. Klein, J. Christensen, J. Ahmed, and A. Kojic. Algorithms for Advanced Battery-Management Systems. *IEEE Control Syst. Mag.* 2010 Vol. 30 (3): 49–68.
- [123] J. C. Forman, S. J. Moura, J. L. Stein, and H. K. Fathy. Genetic parameter identification of the Doyle-Fuller-Newman model from experimental cycling of a LiFePO<sub>4</sub> battery. *Proc. 2011 Am. Control Conf.* June 29 - July 01, 2011. San Francisco, CA: IEEE. 2011. 362–369.
- [124] M. Doyle, T. F. Fuller, and J. Newman. Modeling of Galvanostatic Charge and Discharge of the Lithium / Polymer / Insertion Cell. *New York.* 1993. Vol. 140: 1526–1533.
- [125] G. Sikha and R. E. White. Analytical Expression for the Impedance Response for a Lithium-Ion Cell. *J. Electrochem. Soc.* 2008. Vol. 155 (12): A893-A902.
- [126] S. Santhanagopalan, Q. Guo, and R. E. White. Parameter Estimation and Model Discrimination for a Lithium-Ion Cell. *J. Electrochem. Soc.* 2007. Vol. 154 (3): A198-206.
- [127] R. Ahmed, M. El Sayed, I. Arasaratnam, J. Tjong, and S. Habibi. Reduced-Order Electrochemical Model Parameters Identification and SOC Estimation for Healthy and Aged Li-Ion Batteries Part I: Parameterization Model Development for Healthy Batteries. *IEEE J. Emerg. Sel. Top. Power Electron.* 2014. Vol. 2 (3): 659–677.
- [128] A. Hausmann and C. Depcik. Expanding the Peukert equation for battery capacity modeling through inclusion of a temperature dependency. *J. Power Sources.* 2013. Vol. 235: 148–158.
- [129] M. Jongerden. *Model-based energy analysis of battery powered systems.* PhD.

Thesis. University of Twente; 2010

- [130] L. Lam, P. Bauer, and E. Kelder. A practical circuit-based model for Li-ion battery cells in electric vehicle applications. *2011 IEEE 33rd International Telecommunications Energy Conference (INTELEC)*. Oct 9-13, 2011. Amsterdam: IEEE. 2011. 1–9.
- [131] L. H. Saw, Y. Ye, and A. a. O. Tay. Electrochemical–thermal analysis of 18650 Lithium Iron Phosphate cell. *Energy Convers. Manag.* 2013. Vol. 75: 162–174.
- [132] B. Enache, E. Lefter, and C. Stoica. Comparative study for generic battery models used for electric vehicles. *2013 8th International Symposium on Advanced Topics in Electrical Engineering*. May 23-25, 2013. Bucharest: IEEE. 2013. 1–6.
- [133] A. Szumanowski. Battery Management System Based on Battery Nonlinear Dynamics Modeling. *IEEE Trans. Veh. Technol.* 2008. Vol. 57 (3): 1425–1432.
- [134] J. Zhang, S. Ci, H. Sharif, and M. Alahmad. An enhanced circuit-based model for single-cell battery. *2010 Twenty-Fifth Annu. IEEE Appl. Power Electron. Conf. Expo.* Feb 21-25, 2010. Palm Springs, CA: IEEE. 2010. 672–675.
- [135] J. Zhang, S. Ci, H. Sharif, and M. Alahmad. Modeling Discharge Behavior of Multicell Battery. *IEEE Trans. Energy Convers.* 2010. Vol. 25 (4): 1133–1141.
- [136] S. Liu, J. Jiang, W. Shi, Z. Ma, L. Y. Wang, and H. Guo. Butler-Volmer-Equation-Based Electrical Model for High-Power Lithium Titanate Batteries Used in Electric Vehicles. *IEEE Trans. Ind. Electron.* 2015. Vol. 62 (12): 7557–7568.
- [137] S. Yuan, H. Wu, X. Zhang, and C. Yin. Online Estimation of Electrochemical Impedance Spectra for Lithium-Ion Batteries via Discrete Fractional Order Model. *2013 IEEE Vehicle Power and Propulsion Conference (VPPC)*. Oct 15-18, 2013. Beijing: IEEE. 2013. 1–6.
- [138] A.-I. Stroe, M. Swierczynski, D. Stroe, and R. Teodorescu. Performance model for high-power lithium titanate oxide batteries based on extended characterization tests. *2015 IEEE Energy Conversion Congress and Exposition (ECCE)*. Sept 20-24, 2015. Montreal, QC: IEEE. 2015. 6191–6198.
- [139] J. Illig, J. P. Schmidt, M. Weiss, A. Weber, and E. Ivers-Tiffée. Understanding the impedance spectrum of 18650 LiFePO<sub>4</sub>-cells. *J. Power Sources*. 2013.

Vol. 239: 670–679.

- [140] C. R. Birkl and D. a Howey. Model identification and parameter estimation for LiFePO<sub>4</sub> batteries. *IET Hybrid and Electric Vehicles Conference 2013, HEVC 2013*. Nov 6 -7, 2013. London: IEEE. 2013. 1–6.
- [141] D. Andre, M. Meiler, K. Steiner, H. Walz, T. Soczka-Guth, and D. U. Sauer. Characterization of high-power lithium-ion batteries by electrochemical impedance spectroscopy. II: Modelling. *J. Power Sources*. 2011. Vol. 196 (12): 5349–5356.
- [142] Y. Lee, S. Park, and S. Han, “Online Embedded Impedance Measurement Using High-Power Battery Charger,” *IEEE Trans. Ind. Appl.*, vol. 51, no. 1, pp. 498–508, Jan. 2015.
- [143] T.-H. Kim, S.-J. Lee, and W.-J. W. Choi. Design and control of the phase shift full bridge converter for the on-board battery charger of the electric forklift. *J. Power Electron*. 2011. Vol. 12 (1): 2709–2716.
- [144] J. Jang and J. Yoo. Equivalent Circuit Evaluation Method of Lithium Polymer Battery Using Bode Plot and Numerical Analysis. *IEEE Trans. Energy Convers*. 2011. Vol. 26 (1): 290–298.
- [145] K. M. Tsang, L. Sun, and W. L. Chan. Identification and modelling of Lithium ion battery. *Energy Convers. Manag*. 2010. Vol. 51 (12): 2857–2862.
- [146] G. K. Prasad and C. D. Rahn. Model based identification of aging parameters in lithium ion batteries. *J. Power Sources*. 2013. Vol. 232: 79–85.
- [147] T. R. Tanim, C. D. Rahn, and C.-Y. Wang. State of charge estimation of a lithium ion cell based on a temperature dependent and electrolyte enhanced single particle model. *Energy*. 2015. Vol. 80: 731–739.
- [148] H. He, R. Xiong, and J. Fan. Evaluation of Lithium-Ion Battery Equivalent Circuit Models for State of Charge Estimation by an Experimental Approach. *Energies*. 2011. Vol. 4 (12): 582–598.
- [149] L. Chenglin, L. Huiju, and W. Lifang. A dynamic equivalent circuit model of LiFePO<sub>4</sub> cathode material for lithium ion batteries on hybrid electric vehicles. *2009 IEEE Vehicle Power and Propulsion Conference (VPPC)*. Sept 7-10, 2009. Dearborn: IEEE. 2009. 1662–1665.
- [150] R. Ahmed, M. El Sayed, I. Arasaratnam, J. Tjong, and S. Habibi. Reduced-Order Electrochemical Model Parameters Identification and State of Charge Estimation for Healthy and Aged Li-Ion Batteries—Part II: Aged Battery

- Model and State of Charge Estimation. *IEEE J. Emerg. Sel. Top. Power Electron.*. 2014. Vol. 2 (3): 678–690.
- [151] W. Y. Low, J. a. Aziz, N. R. N. Idris, and R. Saidur. Electrical model to predict current–voltage behaviours of lithium ferro phosphate batteries using a transient response correction method. *J. Power Sources*. 2013. Vol. 221: 201–209.
- [152] H. L. Chan. A New Battery Model for use with Battery Energy Storage Systems and Electric Vehicles Power Systems. *Power Engineering Society Winter Meeting*. Jan 23-27, 2000. Singapore: IEEE. 2000. 470–475.
- [153] Y. Kim and H. Ha. Design of Interface Circuits With Electrical Battery Models. *IEEE Trans. Indus. Elec.* 1997. Vol. 44 (1): 81–86.
- [154] S. M. M. Mousavi G. and M. Nikdel. Various battery models for various simulation studies and applications. *Renew. Sustain. Energy Rev.* 2014. Vol. 32: 477–485.
- [155] M. Sitterly and G. G. Yin. Enhanced Identification of Battery Models for Real-Time Battery Management. *IEEE Trans. Sustain. Energy*. 2011. Vol. 2 (3): 300–308.
- [156] M. Partovibakhsh and G. Liu. An Adaptive Unscented Kalman Filtering Approach for Online Estimation of Model Parameters and State-of-Charge of Lithium-Ion Batteries for Autonomous Mobile Robots. *IEEE Trans. Control Syst. Technol.* 2015. Vol. 23 (1): 357–363.
- [157] A. Vasebi, M. Partovibakhsh, and S. M. T. Bathaee. A novel combined battery model for state-of-charge estimation in lead-acid batteries based on extended Kalman filter for hybrid electric vehicle applications. *J. Power Sources*. 2007. Vol. 174 (1): 30–40.
- [158] A. Vasebi, S. M. T. Bathaee, and M. Partovibakhsh. Predicting state of charge of lead-acid batteries for hybrid electric vehicles by extended Kalman filter. *Energy Convers. Manag.* 2008. Vol. 49 (1): 75–82.
- [159] B. S. Bhangu, P. Bentley, D. a. Stone, and C. M. Bingham. Nonlinear Observers for Predicting State-of-Charge and State-of-Health of Lead-Acid Batteries for Hybrid-Electric Vehicles. *IEEE Trans. Veh. Technol.* 2005. Vol. 54 (3): 783–794.
- [160] V. H. Johnson. Battery performance models in ADVISOR. *J. Power Sources*. 2002. Vol. 110 (2): 321–329.

- [161] K. B. Wipke and M. R. Cuddy. *Using an Advanced Vehicle Simulator (ADVISOR) to Guide Hybrid Vehicle Propulsion System Development*. National Renewable Energy Laboratory, Golden, CO. 1996
- [162] H. He, R. Xiong, H. Guo, and S. Li. Comparison study on the battery models used for the energy management of batteries in electric vehicles. *Energy Convers. Manag.* 2012. Vol. 64: 113–121.
- [163] X. Hu, S. Li, and H. Peng. A comparative study of equivalent circuit models for Li-ion batteries. *J. Power Sources.* 2012. Vol. 198: 359–367.
- [164] R. C. Kroeze and P. T. Krein. Electrical battery model for use in dynamic electric vehicle simulations. *2008 IEEE Power Electron. Spec. Conf.* June 15–19, 2008. Rhodes: IEEE. 2008. 1336–1342.
- [165] Y. Hu, S. Yurkovich, Y. Guezennec, and B. J. Yurkovich. A technique for dynamic battery model identification in automotive applications using linear parameter varying structures. *Control Eng. Pract.* 2009. Vol. 17 (10): 1190–1201.
- [166] J. Xu, B. Cao, Z. Chen, and Z. Zou. An online state of charge estimation method with reduced prior battery testing information. *Int. J. Electr. Power Energy Syst.* 2014. Vol. 63: 178–184.
- [167] D. N. Laboratories, *Electric Vehicle Battery Test Procedures Manual*. USABC. 1996
- [168] M. Dubarry, V. Svoboda, R. Hwu, and B. Y. Liaw. Capacity loss in rechargeable lithium cells during cycle life testing: The importance of determining state-of-charge. *J. Power Sources.* 2007. Vol. 174 (2): 1121–1125.
- [169] S. Abu-Sharkh and D. Doerffel. Rapid test and non-linear model characterisation of solid-state lithium-ion batteries. *J. Power Sources.* 2004. Vol. 130 (1–2): 266–274.
- [170] R. Jackey, M. Saginaw, P. Sanghvi, J. Gazzarri, T. Huria, and M. Ceraolo. Battery Model Parameter Estimation Using a Layered Technique: An Example Using a Lithium Iron Phosphate Cell. 2013. *MathWorks*: 1–14.
- [171] A. A. Hussein. Kalman Filters versus Neural Networks in Battery State-of-Charge Estimation: A Comparative Study. *Int. J. Mod. Nonlinear Theory Appl.* 2014. Vol. 3 (5):199–209.
- [172] S. Castano, L. Gauchia, E. Voncila, and J. Sanz. Dynamical modeling procedure of a Li-ion battery pack suitable for real-time applications. *Energy*



- Convers. Manag.* 2015. Vol. 92: 396–405.
- [173] S. Yuan, H. Wu, and C. Yin. State of Charge Estimation Using the Extended Kalman Filter for Battery Management Systems Based on the ARX Battery Model. *Energies*. 2013. Vol. 6 (1): 444–470.
- [174] H. Wu, S. Yuan, and C. Yin. A Lithium-Ion Battery Fractional Order State Space Model and its Time Domain System Identification. *Proceedings of the FISITA 2012 World Automotive Congress*. 2013. Berlin, Heidelberg: Springer. 2013. pp. 795–805.
- [175] D. O. E. Id-. *PNGV Battery Test Manual*. US Department of Energy. 2001
- [176] C. Zhang, K. Li, L. Pei, and C. Zhu. An integrated approach for real-time model-based state-of-charge estimation of lithium-ion batteries. *J. Power Sources*. 2015. Vol. 283: 24–36.
- [177] J. Yan, G. Xu, H. Qian, and Y. Xu. Robust State of Charge Estimation for Hybrid Electric Vehicles: Framework and Algorithms. *Energies*. 2010. Vol. 3 (10): 1654–1672.
- [178] R. Xiong, H. He, F. Sun, and K. Zhao. Online Estimation of Peak Power Capability of Li-Ion Batteries in Electric Vehicles by a Hardware-in-Loop Approach. *Energies*. 2012. Vol. 5 (12): 1455–1469.
- [179] Y. Tian, B. Xia, W. Sun, Z. Xu, and W. Zheng. A modified model based state of charge estimation of power lithium-ion batteries using unscented Kalman filter. *J. Power Sources*. 2014. Vol. 270: 619–626.
- [180] G. Liu, M. Ouyang, L. Lu, J. Li, and X. Han. Online estimation of lithium-ion battery remaining discharge capacity through differential voltage analysis. *J. Power Sources*. 2015. Vol. 274: 971–989.
- [181] X. Lin, H. E. Perez, S. Mohan, J. B. Siegel, A. G. Stefanopoulou, Y. Ding, and M. P. Castanier. A lumped-parameter electro-thermal model for cylindrical batteries. *J. Power Sources*. 2014. Vol. 257: 1–11.
- [182] L. Lam. *A Practical Circuit-based Model for State of Health Estimation of Li-ion Battery Cells in Electric Vehicles*. PhD. Thesis. Delft University of Technology; 2011
- [183] H.-G. Schweiger, O. Obeidi, O. Komesker, A. Raschke, M. Schiemann, C. Zehner, M. Gehnen, M. Keller, and P. Birke. Comparison of several methods for determining the internal resistance of lithium ion cells. *Sensors*. 2010. Vol. 10 (6): pp. 5604–5625.

- [184] X. X.-Z. Yuan, C. Song, H. Wang, and J. Zhang. *Electrochemical impedance spectroscopy in PEM fuel cells Fundamentals and Applications*. Springer Science & Business Media. 2010
- [185] S. Rodrigues, N. Munichandraiah, and A. Shukla. A review of state-of-charge indication of batteries by means of ac impedance measurements. *J. Power Sources*. 2000. Vol. 87: 12–20.
- [186] N. A. Windarko and J.-H. Choi. LiPB Battery SOC Estimation Using Extended Kalman Filter Improved with Variation of Single Dominant Parameter. *J. Power Electron*. 2012. Vol. 12 (1): 40–48.
- [187] S. Lee, J. J. Kim, J. J. Lee, and B. H. Cho. State-of-charge and capacity estimation of lithium-ion battery using a new open-circuit voltage versus state-of-charge. *J. Power Sources*. 2008. Vol. 185 (2): 1367–1373.
- [188] J. Brand, Z. Zhang, and R. K. Agarwal. Extraction of battery parameters of the equivalent circuit model using a multi-objective genetic algorithm. *J. Power Sources*. 2014. Vol. 247: 729–737.
- [189] K. Thirugnanam, S. Member, and E. R. J. T. P. Mathematical Modeling of Li-Ion Battery Using Genetic Algorithm Approach for V2G Applications. *IEEE Trans. Energy Convers*. 2014. Vol. 29 (2): 332–343.
- [190] P. Kumar and P. Bauer. Parameter extraction of battery models using multiobjective optimization genetic algorithms. *Proc. 14th Int. Power Electron. Motion Control Conf. EPE-PEMC 2010*. Sept 6-8, 2010. Ohrid: IEEE. 2010. 106–110.
- [191] A. Malik, Z. Zhang, and R. K. Agarwal. Extraction of battery parameters using a multi-objective genetic algorithm with a non-linear circuit model. *J. Power Sources*. 2014. Vol. 259: 76–86.
- [192] L. Zhang, L. Wang, G. Hinds, C. Lyu, J. Zheng, and J. Li. Multi-objective optimization of lithium-ion battery model using genetic algorithm approach. *J. Power Sources*. 2014. Vol. 270: 367–378.
- [193] W. Gao, M. Jiang, and Y. Hou. Research on PNGV model parameter identification of LiFePO<sub>4</sub> Li-ion battery based on FMRLS. *2011 6th IEEE Conference on Industrial Electronics and Applications*. June 21-23, 2011. Beijing: IEEE. 2011. 2294–2297.
- [194] D. Sun and X. Chen. Adaptive parameter identification method and state of charge estimation of Lithium Ion battery. *2014 17th Int. Conf. Electr. Mach.*

- Syst.* Oct 22-25, 2014. Hangzhou: IEEE. 855–860.
- [195] H. Wu, a, S. Yuan, and C. Yin. Online state of charge estimation based on adaptive extended kalman filter and linear parameter-varying model with recursive least square technique. *Engine.* North America, 16 May 2013. Retrieved 05 April 2016.
- [196] X. Guo, L. Kang, Y. Yao, Z. Huang, and W. Li. Joint Estimation of the Electric Vehicle Power Battery State of Charge Based on the Least Squares Method and the Kalman Filter Algorithm. *Energies.* 2016. Vol. 9 (2): 100.
- [197] Z. He, M. Gao, J. Xu, and Y. Liu. Battery Model Parameters Estimation with the Sigma Point Kalman Filter. *2009 International Conference on Artificial Intelligence and Computational Intelligence.* Nov 7-8, 2009. Shanghai: IEEE. 2009. 303–306.
- [198] H. He, R. Xiong, and H. Guo. Online estimation of model parameters and state-of-charge of LiFePO<sub>4</sub> batteries in electric vehicles. *Appl. Energy.* 2012. Vol. 89 (1): 413–420.
- [199] F. Baronti, W. Zamboni, N. Femia, H. Rahimi-Eichi, R. Roncella, S. Rosi, R. Saletti, and M.-Y. Chow. Parameter identification of Li-Po batteries in electric vehicles: A comparative study. *2013 IEEE Int. Symp. Ind. Electron.* May 28-31, 2013. Taipei: IEEE. 1–7.
- [200] G. L. Plett. Extended Kalman filtering for battery management systems of LiPB-based HEV battery packs: Part 3. State and parameter estimation. *J. Power Sources.* 2004. Vol. 134 (2): 277–292.
- [201] G. L. Plett. Extended Kalman filtering for battery management systems of LiPB-based HEV battery packs: Part 1. Background. *J. Power Sources.* 2004. Vol. 134 (2): 252–261.
- [202] G. L. Plett. Sigma-point Kalman filtering for battery management systems of LiPB-based HEV battery packs: Part 1: Introduction and state estimation. *J. Power Sources.* 2006. Vol. 161 (2): 1356–1368.
- [203] G. L. Plett. Sigma-point Kalman filtering for battery management systems of LiPB-based HEV battery packs: Part 2: Simultaneous state and parameter estimation. *J. Power Sources.* 2006. Vol. 161 (2): 1369–1384.
- [204] Y. Tian, B. Xia, and W. Sun. SOC estimation of LiNi 1/3 Co 1/3 Mn 1/3 O<sub>2</sub> battery using Unscented Kalman Filtering Method. *2014 IEEE 9th Conference on Industrial Electronics and Applications.* June 9-11, 2014. Hangzhou: IEEE.

2013. 883–887.
- [205] Q. Song. An Adaptive UKF Algorithm for the State Parameter Estimations of a Mobile Robot. *Acta Autom. Sin.* 2008. Vol. 34 (1): 72-79.
- [206] Y. Shi, C. Han, and Y. Liang. Adaptive UKF for target tracking with unknown process noise statistics. *12th International Conference on Information Fusion*. July 6-9, 2009. Seattle, WA: IEEE. 1815–1820.
- [207] A. Mohamed and K. Schwarz. Adaptive Kalman filtering for INS/GPS. *J. Geod.* 1999. Vol. 73: 193–203.
- [208] R. Xiong, H. He, F. Sun, and K. Zhao. Evaluation on State of Charge Estimation of Batteries With Adaptive Extended Kalman Filter by Experiment Approach. *IEEE Trans. Veh. Technol.* 2013. Vol. 62 (1): 108–117.
- [209] J. Du, Z. Liu, and Y. Wang. State of charge estimation for Li-ion battery based on model from extreme learning machine. *Control Eng. Pract.* 2014. Vol. 26: 11–19.
- [210] F. Sun, R. Xiong, and H. He. Estimation of state-of-charge and state-of-power capability of lithium-ion battery considering varying health conditions. *J. Power Sources*. 2014. Vol. 259: 166–176.
- [211] R. Xiong, F. Sun, X. Gong, and H. He. Adaptive state of charge estimator for lithium-ion cells series battery pack in electric vehicles. *J. Power Sources*. 2013. Vol. 242: 699–713.
- [212] J. Han, D. Kim, and M. Sunwoo. State-of-charge estimation of lead-acid batteries using an adaptive extended Kalman filter. *J. Power Sources*. 2009. Vol. 188 (2): 606–612.
- [213] V. Duong, H. A. Bastawrous, K. Lim, K. W. See, P. Zhang, and S. X. Dou. Online state of charge and model parameters estimation of the LiFePO<sub>4</sub> battery in electric vehicles using multiple adaptive forgetting factors recursive least-squares. *J. Power Sources*. 2015. Vol. 296: 215–224.
- [214] T. Kim, Y. Wang, Z. Sahinoglu, T. Wada, S. Hara, and W. Qiao. Fast UD factorization-based RLS online parameter identification for model-based condition monitoring of lithium-ion batteries. *2014 American Control Conference*. June 4-6, 2014. Portland, OR: IEEE. 2014. 4410–4415.
- [215] H. Dai, X. Wei, and Z. Sun. Design and implementation of a UKF-based SOC estimator for LiMnO<sub>2</sub> batteries used on electric vehicles. *Przełąd Elektrotechniczny*. 2012. Vol. 88 (1): 57–63.

- [216] H. Dai, X. Wei, and Z. Sun. State and Parameter Estimation of a HEV Li-ion Battery Pack Using Adaptive Kalman Filter with a New SOC-OCV Concept. *2009 International Conference on Measuring Technology and Mechatronics Automation*. April 11-12, 2009. Hunan: IEEE. 2009. 375–380.
- [217] Z. He, Y. Liu, M. Gao, and C. Wang. A joint model and SOC estimation method for lithium battery based on the sigma point KF. *2012 IEEE Transp. Electrification Conf. Expo, ITEC 2012*. June 18-20, 2012. Dearborn, MI: IEEE. 2012. 1-5.
- [218] Y. Zou, X. Hu, H. Ma, and S. E. Li. Combined SOC and SOH estimation over lithium-ion battery cell cycle lifespan for Electric vehicles. *J. Power Sources*. 2014. Vol. 273: 793–803.
- [219] Z. He, M. Gao, C. Wang, L. Wang, and Y. Liu. Adaptive State of Charge Estimation for Li-Ion Batteries Based on an Unscented Kalman Filter with an Enhanced Battery Model. *Energies*. 2013. Vol. 6 (8): 4134–4151.
- [220] L. Anhui Tiankang (Group) Shares Co. *Lithium Titanate Battery Instructions*. Anhui, China: 2012.
- [221] G. Capponi, F. Pellitteri, L. Rosa, and V. Boscaino. Wireless battery chargers for portable applications: design and test of a high-efficiency power receiver. *IET Power Electron*. 2013. Vol. 6 (1): 20–29.
- [222] Y.-C. Chuang and Y.-L. Ke. High efficiency battery charger with a buck zero-current-switching pulse-width-modulated converter. *IET Power Electron*. 2008. Vol. 1 (4): 433–444.
- [223] R. J. Wai and S. J. Jhung. Design of energy-saving adaptive fast-charging control strategy for Li-FePO<sub>4</sub> battery module. *IET Power Electron*. 2012. Vol. 5 (9): 1684–1693.
- [224] P. Y. Kong, J. A. Aziz, M. R. Sahid, and L. W. Yao. A bridgeless PFC converter for on-board battery charger. *2014 IEEE Conference on Energy Conversion (CENCON)*. Oct 13-14, 2014. Johor Bahru: IEEE. 2014. 383–388.
- [225] H. Chiu, Y. Lo, P. Tseng, and Y. Liu. High-efficiency battery charger with cascode output design. *IET Power Electron*. 2014. Vol. 7 (7): 1725–1735.
- [226] Y. Lu, K. W. E. Cheng, and S. W. Zhao. Power battery charger for electric vehicles. *IET Power Electron*. 2011. Vol. 4 (5): 580–586.
- [227] J. Park, S. Choi, and M. Kim. Zero-current switching series loaded resonant converter insensitive to resonant component tolerance for battery charger. *IET*

- Power Electron.* 2014. Vol. 7 (10): 2517–2524.
- [228] T.-H. Kim, S.-J. Lee, and W.-J. Choi. Design and Control of the Phase Shift Full Bridge Converter for the On-board Battery Charger of Electric Forklifts. *J. Power Electron.* 2012. Vol. 12 (1): 113–119.
- [229] Y.-C. Hsieh and C.-S. Huang. Li-ion battery charger based on digitally controlled phase-shifted full-bridge converter. *IET Power Electron.* 2011. Vol. 4 (2): 242–247.
- [230] G. Di Capua, S. A. Shirsavar, M. A. Hallworth, and N. Femia. An Enhanced Model for Small-Signal Analysis of the Phase-Shifted Full-Bridge Converter. *IEEE Trans. Power Electron.* 2015. Vol. 30 (3): 1567–1576.
- [231] V. Vlatkovic, J. A. Sabate, R. B. Ridley, F. C. Lee, and B. H. Cho. Small-signal analysis of the phase-shifted PWM converter. *IEEE Trans. Power Electron.* 1992. Vol. 7 (1): 128–135.
- [232] J. Gomez, R. Nelson, E. E. Kalu, M. H. Weatherspoon, and J. P. Zheng. Equivalent circuit model parameters of a high-power Li-ion battery: Thermal and state of charge effects. *J. Power Sources.* 2011. Vol. 196 (10): 4826–4831.
- [233] X. Wei, B. Zhu, and W. Xu. Internal Resistance Identification in Vehicle Power Lithium-Ion Battery and Application in Lifetime Evaluation. *2009 Int. Conf. Meas. Technol. Mechatronics Autom.* April 11-12, 2009. Hunan: IEEE. 2009. 388–392.
- [234] X. Yu, S. Sandhu, S. Beiker, R. Sassoon, and S. Fan. Wireless energy transfer with the presence of metallic planes. *Appl. Phys. Lett.* 2011. Vol. 214102 (99): 21–23.
- [235] S. Marcacci. Coming Soon : A Wireless EV Highway Charging System. *Clean Technica*, 2012. [Online]. Available: <http://cleantechnica.com/2012/02/04/coming-soon-a-wireless-ev-highway-charging-system>. [Accessed: 07-Aug-2016].
- [236] R.-J. Chen, T.-D. Lin, H.-Y. Lin, and Y.-C. Hsieh. Electric circuit modelling for lithium-ion batteries by intermittent discharging. *IET Power Electron.* 2014. Vol. 7 (10) : 2672–2677.
- [237] H. Lu, J. Zhan-rong, W. Ming-ming, and Z. Li-xin. Adaptive Extended Kalman Filter Based on Genetic Algorithm for Tightly-Coupled Integrated Inertial and GPS Navigation. *2009 Second International Conference on Intelligent Computation Technology and Automation.* Oct 10-11, 2009.

Changsha: IEEE. 2009. 520–524.

- [238] D. Lee and K. T. Alfriend. Adaptive Sigma Point Filtering for State and Parameter Estimation. *Astrodynamics Specialist Conference and Exhibit*. August 16, 2004. Rhode Island: AIAA. 2004. 1–20.
- [239] F. Busse, J. How, and J. Simpson. Demonstration of Adaptive Extended Kalman Filter for Low Earth Orbit Formation Estimation Using CDGPS. *Navigation*. 2003. Vol. 50 (2): 1–12, 2003.
- [240] A. Hentunen, T. Lehmuspelto, and J. Suomela. Time-Domain Parameter Extraction Method for Thévenin-Equivalent Circuit Battery Models. *IEEE Trans. Energy Convers.* 2014. Vol. 29 (3): 558–566.