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Abstract

The low-energy lattice dynamics of the quasiperiodic spin-ladder cuprate Sr_{14-x}Ca_xCu₂₄O₄₁ are investigated using terahertz frequency synchrotron radiation. A high density of low-lying optical excitations is present in the 1-3 THz energy range, while at least two highly absorbing excitations stemming from long-wavelength acoustic oscillations of the incommensurate chain and ladder sublattices, are observed at subterahertz frequencies. The effects of Ca substitution on the subterahertz quasiacoustic sliding mode gaps is investigated using coherent synchrotron radiation. Analysis of the results suggest increasing substitution of Sr for Ca is accompanied by a transfer of spectral weight between sliding modes associated with different chain-ladder dynamics. The observation is consistent with a transfer of hole charges from the chains to the ladders and modification of the sublattice dimensions following Ca substitution. The results are discussed in context to the significance of low-lying vibrational dynamics and electron-phonon coupling in the superconducting state of certain quasiperiodic systems.

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Effects of Ca substitution on quasicoustic sliding modes in $\text{Sr}_{14-x}\text{Ca}_x\text{Cu}_{24}\text{O}_{41}$

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The low-energy lattice dynamics of the quasiperiodic spin-ladder cuprate $\text{Sr}_{14-x}\text{Ca}_x\text{Cu}_{24}\text{O}_{41}$ are investigated using terahertz frequency synchrotron radiation. A high density of low-lying optical excitations is present in the 1–3 THz energy range, while at least two highly absorbing excitations stemming from long-wavelength acoustic oscillations of the incommensurate chain and ladder sublattices, are observed at subterahertz frequencies. The effects of Ca substitution on the subterahertz quasicoustic sliding mode gaps is investigated using coherent synchrotron radiation. Analysis of the results suggest increasing substitution of Sr for Ca is accompanied by a transfer of spectral weight between sliding modes associated with different chain-ladder dynamics. The observation is consistent with a transfer of hole charges from the chains to the ladders and modification of the sublattice dimensions following Ca substitution. The results are discussed in context to the significance of low-lying vibrational dynamics and electron-phonon coupling in the superconducting state of certain quasiperiodic systems.

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I. INTRODUCTION

The significance of neighboring orders and their collective excitations in the thermodynamic landscape of high-temperature superconductors (HTS) is an ongoing question within condensed matter physics. The simple notion of whether or not such orders ultimately enhance or impede superconductivity is examined in numerous HTS systems [1–3]. Recently, the implication of quasiperiodic lattice order with its associated low-energy vibrational modes has also received interest in attempts to understand examples of strong-coupling superconductivity [4–9]. In this context, the quasiperiodic spin-ladder cuprate $\text{Sr}_{14}\text{Cu}_{24}\text{O}_{41}$ (SCO) presents a unique environment to explore these ideas. Built from alternating layers of Sr_2 planes, two-leg Cu_2O_3 ladders, and CuO_2 chains (see Fig. 1), SCO forms a quasiperiodic superlattice due to an incommensurate free arrangement of the chain and Sr-ladder sublattices along the c direction, with $c = 27.5 \text{ \AA} \simeq 10c_{\text{ch}} \simeq 7c_{\text{ld}}$ [10], where c_{ch} and c_{ld} are the c lattice parameters of the chain and ladder sublattices, respectively. A nominal valence of $\text{Cu}^{2.6+}$ for each CuO_2 site intrinsically dopes the chains with ~ 6 hole charge carriers per unit formula [11]. This, in combination with the quasiperiodic lattice, facilitates a number of exotic low-dimensional charge and $S = 1/2$ quantum magnetic properties including anisotropic nonlinear

charge transport [12–14], charge density wave (CDW) charge order [15–18], hole crystallization [19], spin gapped antiferromagnetic dimerization [20–24], and long-range quantum coherence [25].

Substitution of Sr with Ca in compounds of $\text{Sr}_{14-x}\text{Ca}_x\text{Cu}_{24}\text{O}_{41}$ (SCCO) acts to transfer holes from the chains to the ladders, providing control over the unique physics expressed in each sublattice and hence tunability over the landscape of electronic orders [11,26–30]. Perhaps the most significant consequence is the emergence of superconductivity below 12 K for a Ca concentration of $x = 13.6$ and hydrostatic pressure of 3 GPa [31]. The occurrence of superconductivity in SCCO is noted as unique amongst the HTS cuprates because the lattice maintains its one-dimensional nature at high pressure and lacks the familiar CuO_4 square plackets [32]. As such, the nature of superconductivity in SCCO remains poorly understood. Remarkably, recent spectroscopic experiments on the order of 1 meV have revealed the presence of additional acoustic vibrational modes supported by a long-wavelength sliding oscillation of the incommensurate chain and ladder sublattices [33,34]. Theoretically predicted over 30 years earlier [35,36], these quasicoustic sliding modes invoke similarities to the low-frequency vibrational modes of other quasiperiodic superconductors [5,6,8,9] and therefore warrant further attention.

Spectroscopic study of the low-energy dynamics in SCCO has proven to be an effective probe of the interplay between the different electronic orders. However, while

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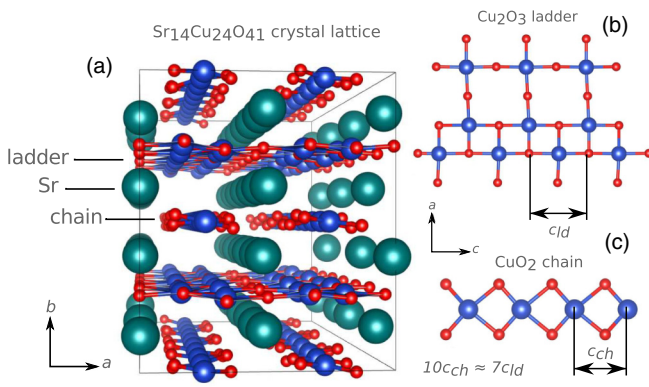


FIG. 1. (a) Supercell structure of $\text{Sr}_{14}\text{Cu}_{24}\text{O}_{41}$ with $a = 11.47 \text{ \AA}$, $b = 13.41 \text{ \AA}$, and $c = 27.5 \text{ \AA}$ lattice parameters. (b) Section of Cu_2O_3 two-leg ladder sublattice with $c_{ld} = 3.95 \text{ \AA}$. (c) Section of CuO_2 chain sublattice with $c_{ch} = 2.75 \text{ \AA}$.

considerable effort has been made to understand the effects of Ca substitution on the charge order [11,26,37] and spin-gap [29,30,38,39] properties, little attention has been given to the effects on the quasiacoustic sliding modes. To address this we have attempted a spectroscopic study on a series of SCCO samples using a combination of synchrotron and laboratory-based terahertz (THz) and far-infrared (FIR) techniques. In combination, the different techniques provide a picture of the low-energy lattice dynamics in relation to changes in temperature and Ca concentration. We observe a number of highly anisotropic optical excitations below 3 THz including strong absorption bands in the sub-THz energy range of SCCO consistent with previous works [17,26,33,34]. Our results show a transfer of spectral weight between sliding mode excitations associated with slow in-phase and fast out-of-phase chain-ladder sliding dynamics. We note that it is within the ladders that the superconducting channels are expected and discuss the implications of our results in this context.

II. EXPERIMENTAL DETAILS

Single crystals of SCCO with $x = 0, 3, 7$, and 11 were grown by the floating zone method and prepared as wafers cut normal to the b axis. Sample dimensions were approximately $5 \times 5 \times 1 \text{ mm}^3$. Details of the sample characterization can be found in references [27,28,40]. Transmission measurements of the $x = 0$ sample in the $0.6\text{--}3.6 \text{ THz}$ spectral range from $5.6\text{--}300 \text{ K}$ were performed at the Australian Synchrotron far-infrared beamline. Spectra were collected using a Bruker IFS125HR FTIR Michelson interferometer with a $75\text{-}\mu\text{m}$ mylar beam splitter and 4.2-K Si Bolometer detector at 0.5 cm^{-1} resolution for polarized $E||c$ and $E||a$ configurations. A 2.5-mm aperture copper mount was used as a reference. Complementary spectra in the same energy range were also collected for the $x = 0$ and $x = 3$ samples using a modified polytec FIR 25 Fourier transform interferometer with mercury lamp source, interfaced to the low-temperature insert of a He cooled 7-T Oxford split-coil superconducting magnet. To test the magnetic activity of observed excitations, experiments were performed at 5 K from 0 to 5 T . However, we observed no magnetic field effects and therefore only

0 T measurements are presented here. Transmission spectra of the $x = 0, 3, 7$, and 11 samples in the $0.2\text{--}1.2 \text{ THz}$ ($6.7\text{--}40 \text{ cm}^{-1}$) spectral range were performed at the SOLEIL synchrotron AILES beamline operating with coherent synchrotron radiation (CSR) in a low- α configuration providing a high-power polarized radiation source in the sub-THz energy range [41,42]. The samples were mounted to an Attocube rotation stage thermally coupled to the cold head of a Cryomech PT 405 pulse tube cryostat, achieving sample temperatures from $16\text{--}300 \text{ K}$. Spectra were collected using a Bruker IFS125 FTIR Michelson interferometer with a $125\text{-}\mu\text{m}$ mylar beam splitter and 1.6-K Si Bolometer detector at 0.5-cm^{-1} resolution. Experimental limitations prevented measurement of a conventional vacuum reference. Therefore, quantitative extraction of sample attenuation was determined by analyzing the rotationally dependent response while assuming a flat contribution for $E||a$. Details of this analysis process are covered in Ref. [43].

III. RESULTS

The general anisotropic and temperature dependent behavior for the conductivity and lattice dynamics of SCO in the far-infrared energy range is captured in the transmission spectra of Fig. 2. As seen in Figs. 2(a) and 2(c), the sample is semi-insulating at low frequency when the electric field is perpendicular to the chains and ladders ($E||a$), transmitting $\sim 10\%$ below 1 THz at room temperature. As the temperature is lowered, the sample transmission increases steadily as a broad absorption continuum shifts to higher frequencies, stabilizing at $\sim 2.75 \text{ THz}$ below $\sim 100 \text{ K}$. This behavior is consistent with reflectivity measurements indicating a suppressed optical conductivity due to a shifting plasma response [37]. It is worth noting that the stabilization of this response below 100 K corresponds to the temperature of spin dimer formation observed in the magnetic susceptibility [21,22]. It suggests a correlation between charge transport and magnetic degrees of freedom in the a direction and marks a crossover from 2D to 1D charge dynamics. On the other hand, when the electric field is parallel to the chains and ladders [$E||c$, Figs. 2(b) and 2(d)], the sample is nontransparent at high temperatures due to the metallic behavior along c . Upon cooling below $\sim 150 \text{ K}$, the transmission abruptly increases following insulating behavior as a result of a pinned charge density wave [18,26,44] in the charge ordered phase emerging at $T_{co} = 200 \text{ K}$ [14,15].

In both polarizations, a number of sharp absorption features are seen, which exhibit abnormally low energy, high density, and fine structure when compared to conventional optical phonon modes in other alkaline cuprates [45–48]. Multiplex fitting and error analysis of the absorption features [Figs. 2(c) and 2(d)] was performed using a Marquardt-Levenberg non-linear least-squares fitting procedure implemented within the WAVE METRICS IGOR PRO software package. Results of the temperature dependence for fitted peak positions labeled from A-R are shown in Figs. 2(e) and 2(f), while the peak intensity of three representative features (B, G, Q) is shown in Fig. 2(g). Minimal broadening and frequency shifts are observed as a function of temperature. The peak intensity profiles reveal three temperature regimes associated with the different

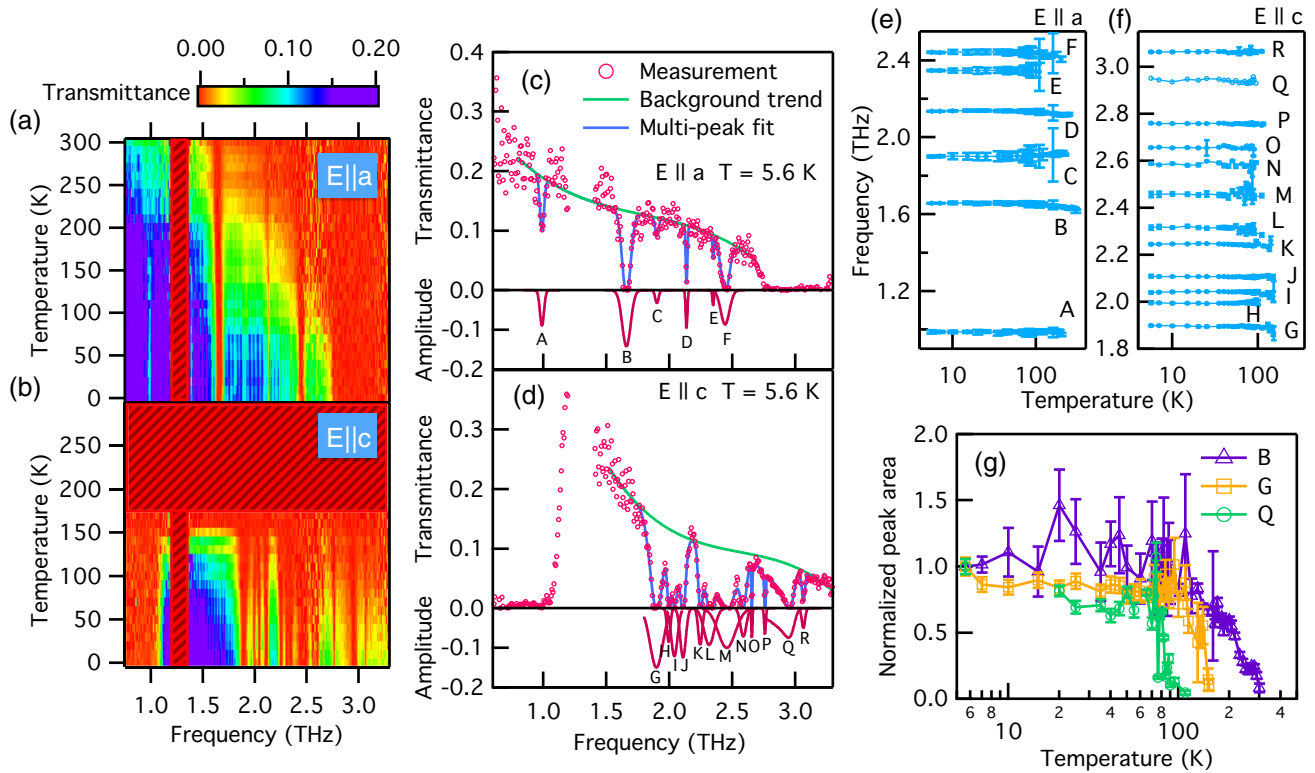


FIG. 2. Temperature dependence of SCO transmission between 0.7 and 3.3 THz for $E||a$ (a) and $E||c$ (b) determined by a ratio with a vacuum reference. Opaque spectra for $E||c$ above 170 K were omitted and are represented by a hatched rectangle. Low signal intensity due to a beamsplitter minimum results in noise artifacts centered on 1.29 THz and are also omitted. Multi-peak fits of the spectra at 5.6 K are shown for $E||a$ (c) and $E||c$ (d). Peaks were fit using Gaussian profiles and a background trend approximated by a third-order polynomial. Temperature dependence of fitted peak positions for $E||a$ (e) and $E||c$ (f). (g) Temperature dependence of fitted peak intensity for selected peaks B, G, and Q determined by peak area normalized to the base temperature (5.6 K) value.

electronic orders of SCO. In the high-temperature regime (200–300 K), the dependence of peak B shows a general increase in phonon intensity as the temperature is lowered. We attribute this to the decreasing optical conductivity that minimizes screening by mobile charges and enhances the observed phonon intensity. Below ~ 200 K, a similar effect is observed along the c direction following the stabilization of the insulating charge ordered phase that is accompanied by the appearance of new modes such as peak G. Below ~ 100 K, SCO is characterized by the stabilization of short range magnetic spin dimer order on the chain sublattice. As observed in similar linear chain compounds featuring charge and spin-dimer order, such as the $(\text{TMTTF})_2\text{X}$ charge-transfer salts, these processes are often accompanied by local charge redistribution that stabilize new vibrational modes [49,50]. The presence of new modes such as peak Q, and the perceived splitting of peaks I and H below ~ 100 K could be attributed to similar behavior in SCO. Overall, the observed lattice dynamics are consistent with the highly ordered supercell structure of SCO, supporting a large number of underdamped, weakly dispersive optical lattice modes and demonstrating a mixing between lattice and electronic order parameters over a broad temperature range [34,37,51,52]. We note that the particularly high density of low-lying phonons observed for the c direction are also likely complemented by zone folded modes due to the incommensurate chain-ladder relationship and charge order

Peierls distortion that modulates the chain and ladder symmetries while maintaining the same overall crystal structure [32,53,54]. The zone folding phenomenon is well documented in other low-dimensional systems exhibiting charge ordering [55–58]. In SCO, the effect has previously been noted by the appearance of new phononlike Raman modes below T_{co} , in the vicinity of 6–18 THz [51]. In general however, due to the large and complex nature of the SCO lattice, a more precise assignment of individual lattice excitations in Fig. 2 remains a challenge.

Finally, we note that measurements performed under magnetic field (not shown) revealed no discernible peak shifts except for a weak signal resulting from Zeeman splitting of the chain localized spin triplet excitations at 2.33 THz (peak E) and 2.63 THz in the $E||a$ configuration. Details of the spin triplet excitations from chain and ladder localized Zhang-Rice singlet states have been covered elsewhere [20,21,23,24] with an analysis of their optical excitation given in Ref. [59]. A further analysis of peak fits in the spectral region of Fig. 2 is addressed in Ref. [60]. More details of the temperature dependence for the peak fitting parameters are provided in Ref. [43].

Apart from the high density of optical phonon modes beginning at ~ 2 THz, a strong absorption band below ~ 1 THz also dominates the spectra in the $E||c$ configuration [Figs. 2(b) and 2(d)]. The position, intensity, and anisotropy of

the band suggests that it is related to gapped acoustic excitations stemming from long-wavelength collective oscillations of the incommensurate chain and ladder sublattices. Such sliding modes are theoretically predicted in low-dimensional incommensurate systems [35,36] and were first identified in SCO by Thorsmølle *et al.* [33]. The strong spectral intensity of these excitations renders the spectrum completely opaque to conventional THz transmission techniques and gives a flat reststrahlen band close to 1 in reflection. These limitations make precise optical measurement of the sliding mode gap difficult. In Ref. [33], combined transmission and reflection techniques were used to give values of 0.25 and 0.38 THz for infrared active modes with different relative sliding motion. Inelastic neutron scattering on SCO single crystals confirms the highly anisotropic acoustic dispersion of the sliding modes with a gap of 0.46 THz [34]. Together, these studies provide a convincing picture of the sub-THz excitations in SCO. However, the discrepancy in the observed gaps and their $\sim 50\%$ lower frequency compared to the absorption band beginning at ~ 1 THz in Fig. 2 suggests that there are more details to be uncovered. Moreover, a study of the effects of Ca doping on the properties of the sliding mode excitations is pertinent in relation to the role of low-frequency lattice modes in the superconducting state [6]. To address these points we performed THz transmission measurements on samples of SCCO with $x = 0, 3, 7$, and 11 using coherent synchrotron radiation. The high flux at low frequency achievable with coherent synchrotron radiation allows measurement of strongly absorbing excitations in transmission geometry without complete attenuation of the signal at the resonant energy. Taking advantage of the one dimensional anisotropic optical response of the samples at low temperature and the naturally polarized radiation of the low- α mode coherent synchrotron, spectra were analyzed by comparing changes in transmitted intensity as the sample is rotated away from a $E||c$ configuration. Following the details provided in Ref. [43], and assuming a flat, sub-THz transmittance for $E||a$ of $T_a = 0.35$ extrapolated from Fig. 2 for the $x = 0$ sample, a quantitative measurement of the attenuation coefficient for $E||c$ is possible. Similar analysis techniques have been implemented in probing highly absorbing excitations in other strongly anisotropic cuprates [61]. The results at 16 K are shown in Fig. 3 in combination with higher-frequency measurements obtained by conventional far infrared methods at 5 K. The data are omitted between 0.6 and 0.77 THz due to noise artifacts at the beam splitter minimum.

Despite limitations of the rotational measurement technique and omitted data at the beam splitter minimum, a clear and broad resonant excitation band is observed centered around 0.6 THz for the $x = 0$ sample in Fig. 3(a). We attribute weak fringes on top of the excitation band to a phase mismatch between the plane parallel interference fringes for $E||c$ and $E||a$ configurations. A nice agreement with the absorption band edge at ~ 1 THz obtained by conventional FIR methods validates the quantitative analysis of the CSR data and provides a broadband picture of the low-frequency optical response along c . Although previous studies have identified a single peak in this region [17,26], we find that the asymmetric sub-THz absorption band is fit best by two Gaussian profiles with energies of 0.48 ± 0.01 and 0.88 ± 0.01 THz designated β_1 and β_2 , respectively. Data for the $x = 3$ Ca-substituted

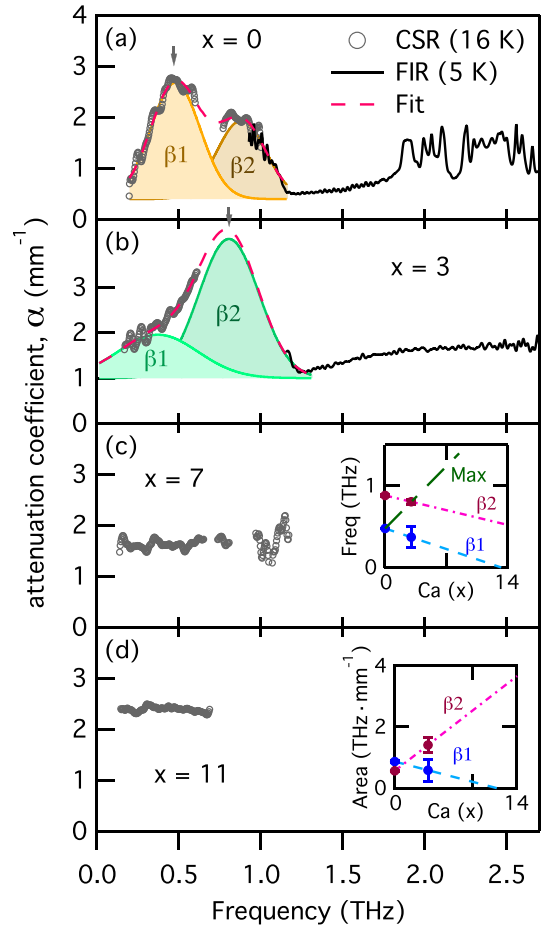


FIG. 3. Low-frequency $E||c$ sample attenuation for SCCO with increasing Ca substitution. Peaks in the spectra correspond to resonant excitations in the sample. All displayed CSR data were measured at 16 K while the FIR data were measured at 5 K. Quantitative analysis of the CSR data was performed using the technique outlined in Ref. [43] with reference angles relative to $E||c$ of $\theta = 12^\circ, 24^\circ, 29^\circ$ and 90° for the samples with Ca concentrations of $x = 0$ (a), 3 (b), 7 (c), and 11 (d), respectively. The FIR data were analyzed using a conventional vacuum reference. Gray arrows indicate the spectral weight maximum. Insets show approximate trends of the fitted peak position, shift in the spectral weight maximum (Max) [(c) insert] and peak area [(d) insert] as a function of Ca substitution.

sample are shown in Fig. 3(b). Here, a combination of the beam splitter minimum and strong sample absorption attenuates the signal between 0.62 and 1.14 THz. Nevertheless, the combined results of the CSR and FIR techniques come together to show a consistent, quantitative picture of the low-frequency spectrum.

Firstly, we note the absence of the optical phonons above 1.5 THz that marks a distinction between the low-frequency optical lattice dynamics in the $x = 0$ and $x = 3$ compounds. This may be a result of hardening due to increased lattice strain pushing the phonons above the detected spectral bandwidth. It may also mark a suppression of zone folding behavior resulting from a different CDW modulation due to the expected transfer of holes from the chains to the ladders with increasing Ca substitution [11]. While the effects of Ca

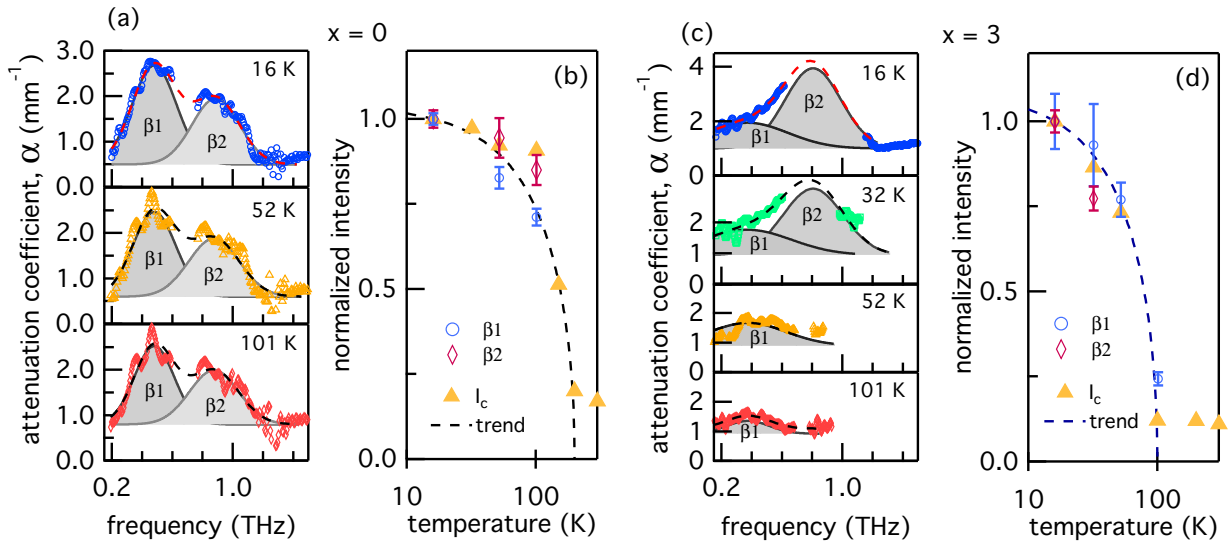


FIG. 4. Temperature dependent CSR spectra and fitted peak parameters of sliding mode gaps in SCCO for $x = 0$ [(a) and (b)] and $x = 3$ [(c) and (d)]. Results above 0.9 THz are combined with the synchrotron spectra in Fig. 2 for $x = 0$ and with the FIR spectra at 5 K in Fig. 3 (b) for $x = 3$. The temperature dependence of broadband transmitted intensity between 0.1 and 1.2 THz for $E||c$ (I_c) along with a $(T_{CO} - T)^{1/2}$ trend is plotted in (b) and (d). $T_{CO} = 200$ K is used for $x = 0$, while $T_{CO} = 100$ K is used for $x = 3$.

substitution on the optical lattice dynamics appear dramatic, the effects on the sliding acoustic dynamics are subtler. As can be seen in Fig. 3(b), the CSR data show a rising absorption band from 0.2 to 0.6 THz. On the other hand, the FIR data show an absorption band edge starting to form below 1.2 THz and suggest the presence of a resonant excitation below this frequency. While the attenuated spectrum between 0.62 and 1.14 THz obscures the complete spectral profile, we find a suitable fit to the available data is given by two Gaussian peak profiles with energies 0.37 ± 0.13 and 0.81 ± 0.03 THz as shown in Fig. 3(b). A resemblance to the sub-THz peaks in the $x = 0$ sample is evidence that the two peaks in Fig. 3(b) are the same gaped sliding modes designated β_1 and β_2 , respectively. While we note that it is difficult to draw solid conclusions about the evolution of the spectral profile between the two samples in the absence of an intermediate measurement between $x = 0$ and $x = 3$ Ca concentrations, the analysis suggests there is a transfer of spectral weight from peak β_1 to β_2 with increasing Ca substitution. The Ca concentration dependence of individual peak positions and area, as well as the spectral weight maximum, are shown in the insets of Figs. 3(c) and 3(d). While our fits reveal a subtle softening of the individual excitations, the general trend indicates a shift in the spectral weight to higher frequencies.

Only low-frequency CSR data are available for the $x = 7$ and 11 samples, shown in Figs. 3(c) and 3(d). In these two cases the sub-THz response is mostly flat. Based on the available literature [26], it is possible the $x = 7$ sample is not completely stabilized in the charge ordered phase at 16 K. The $x = 11$ sample should be either a poor insulator or completely metallic at 16 K. Therefore it is likely that freely mobile charges on the chains and ladders in the $x = 7$ and 11 samples act to screen resonance excitations in the $E||c$ configurations. This could then explain the absence of any resonant signatures of the gaped sliding modes in this energy range.

We now turn our attention to the temperature dependence of the sliding mode excitations for the $x = 0$ and $x = 3$ samples shown in Fig. 4. As established in the spectra of Fig. 2, as well as in the literature [18,26,37,62,63], the relationship between the charge and lattice dynamics in SCCO is highly temperature dependent. Moreover, this dependence shifts for different Ca concentrations and should be considered when comparing results for different samples at a single temperature. As such, we would like to rule out any effects of temperature on the observed transfer of spectral weight between peaks β_1 and β_2 for $x = 0$ and $x = 3$ samples in Fig. 3. The results show negligible shifts in the sliding mode gap for $x = 0$ as a function of temperature evidenced in both the CSR (Fig. 3) and synchrotron (Fig. 2) spectra. Peak intensity determined by the fitted peak area for β_1 and β_2 as a function of temperature is shown in Fig. 4(b) normalized to the value at 16 K. The fitting results are compared with normalized measurements of the average transmission (I_c) in the 0.1 to 1.2 THz range reflecting the general change in optical conductivity. A trend line is included of the form $(T_{CO} - T)^{1/2}$ with $T_{CO} = 200$ K, approximating the charge ordered phase transition at 200 K for $x = 0$. Evidently, the excitation intensity closely follows the charge order temperature dependence. As expected, the increasing conductivity of the sample at higher temperature will allow more effective screening of the sliding mode resonance reducing its spectral intensity. A similar temperature dependence is found for the fitted peaks of the $x = 3$ spectra shown in Figs. 4(c) and 4(d). Here the charge order trend is shown using a critical temperature of $T_{CO} = 100$ K. Interestingly, we find that while peak β_1 generally follows the charge ordering trend, β_2 decreases more rapidly appearing completely suppressed at higher temperatures. Together, the results provide supporting evidence for the intrinsic nature of the observed transfer of spectral weight between β_1 and β_2 in the measurements of the $x = 0$ and $x = 3$ samples at 16 K.

IV. DISCUSSION

We point out that our observations of strongly absorbing sub-THz excitations in SCCO for $x = 0$ and 3 are in close agreement with previous studies noting excitations at similar energies for the two compositions [17,26]. While these results were originally interpreted as density wave dynamics, subsequent optical [33] and neutron scattering [34] experiments have provided a more convincing picture, describing them as gapped sliding or quasiacoustic modes. Such excitations should manifest in low-dimensional systems with incommensurate sublattices such as in SCCO. This is because the long-wavelength translation of one sublattice relative to the other leaves the total system energetically invariant due to their continuous symmetry relation [64]. This effectively introduces additional acoustic modes on top of the conventional acoustic oscillations of the whole structure [35]. If the two incommensurate sublattices (a and b) are oppositely charged, then analogous to electronic plasmon oscillations, the sliding modes will induce a net capacitance across the sample acting as a restoring force for the displacement. In a three-dimensional sample, the restoring electric field is independent of the distance of charge separation, sensitive only to the charge per unit area σ , and the residual permittivity of the lattice $\epsilon_r = \epsilon_0 \epsilon_\infty$ ($E = \sigma / \epsilon_0 \epsilon_\infty$). Therefore, even at the long-wavelength limit, a finite energy is required to excite such modes, with the zone center energy gap given by [36],

$$\omega^2 = \frac{n_a q_a^2}{\epsilon_0 \epsilon_\infty m_a} \left(1 + \frac{n_b m_a}{n_a m_b} \right), \quad (1)$$

where $n_{a,b}$, $q_{a,b}$, and $m_{a,b}$ are the incommensurate a and b sublattice unit cell density, charge, and mass, respectively.

In the case of SCCO the CuO_2 chains feature a nominal charge of $q_{\text{ch}} = (-2 + 0.6)e = -1.4e$ due to the localization of six residual holes over ten chain units, while the $\text{Sr}_2\text{Cu}_2\text{O}_3$ Sr-ladder combination has a net charge of $q_{\text{ld}} = +2e$. We can then estimate the sliding mode energy gap by considering a residual permittivity of $\epsilon_\infty = 15$, consistent with reflectivity measurements available in the literature [33,37], unit cell volumes of $V_{\text{ch}} = 418 \text{ \AA}^3$, $V_{\text{ld}} = 603 \text{ \AA}^3$ [10,32] and masses of $m_{\text{ch}} = (58 + 2 \times 16)m_{\text{p}}$, $m_{\text{ld}} = (2 \times 76 + 2 \times 58 + 3 \times 16)m_{\text{p}}$, where m_{p} is the proton mass. Using these parameters with Eq. (1), we find a sliding mode energy of 0.46 THz, both for modes involving chains sliding relative to static ladders and ladders sliding relative to static chains (see Ref. [43]). The result is in close agreement to our observation of peak $\beta 1 = 0.48$ THz. In fact the small difference between the calculated and observed energies can be accounted for by a slight modification to the residual permittivity ($\epsilon_\infty \approx 14$) within the uncertainty of typical reflectivity measurements, or by considering hole delocalization from the chains to the ladders (giving $q_{\text{ch}} = -1.45e$, $q_{\text{ld}} = +2.1e$) as could be expected in a $x = 0$ SCCO sample with slight impurities [11]. It is also worth noting that the sensitivity of the sliding mode excitations to the permittivity and charge parameters as well as the noted variance in the hole concentrations of different samples [11] could explain the small frequency discrepancies between different observations in the literature [17,26,33,34]. Indeed, oxygen stoichiometry at the surface of cuprate samples has been known to change over time depending on storage conditions

bringing into question differences in sample aging. Finally, the derivation of Eq. (1) assumes the case $k \gg 1/L$ where k is the probing radiation wave vector and L the sample length along c . While $k > 1/L$ is valid for a 5-mm-long sample and 1 THz radiation, for shorter samples and longer wavelengths experiments approach $k = 1/L$, meaning sample dimensions may also play a role in the slightly different energy gaps observed.

Applying the same analysis to peak $\beta 2$ predicts chain and ladder sublattice charges on the order of $q = 2.6\text{--}3.8e$, higher than the expected net valencies of the individual sublattices. Rather, we expect that this could be evidence of a higher order harmonic in which the two sublattices slide out of phase relative to each other (see Ref. [43]), effectively increasing the charge separation and hence the strength of the restoring electric field. Considering Cu_2O_3 ladders decoupled from the Sr_2 ions, sliding out of phase with the CuO_2 chains and producing a combined charge displacement of $q = 3.4e$ we calculate a sliding mode energy gap of 0.88 THz in close agreement with the observation of $\beta 2$. While this interpretation provides one description for a higher order sliding mode, we must also note that similar energy gaps are found by considering different scenarios in which lighter sublattices within the supercell structure move relative to each other. For example decoupling the chain motion from most of the ladder sublattice mass so that they are coupled only to the 180° bonded O_2 atoms in the ladders also gives an energy equivalent to $\beta 2$. Moreover, the possibility that $\beta 2$ represents a different sort of dynamic stemming from different harmonics in the charge ordering cannot be completely ruled out with the experimental evidence available.

Nevertheless, with a general understanding of the contributions to the sliding mode gap, we can now consider the different observations in Figs. 3 and 4. As established by optical [65] and x-ray [11] techniques, Ca substitution in SCCO acts to reduce the distance between chain and ladder layers facilitating the transfer of holes from the chains to the ladders leaving the total number of holes roughly unchanged. This will effectively increase the negative charge on the chains while increasing the positive charge on the ladders. Moreover, Ca substitution acts to reduce the chain and ladder unit cell volumes as well as the $\text{Sr}_2\text{Cu}_2\text{O}_3$ sublattice mass [10,32]. Each of these processes will have the net effect of increasing the energy gap for all sliding mode types. In contrast, reflectivity measurements show an increase in the dielectric permittivity following Ca substitution [37] that would facilitate softening of the sliding modes. As our observations comparing $x = 0$ to $x = 3$ Ca concentrations in Fig. 3 suggest, these contrasting effects are mostly balanced ultimately resulting in a subtle softening of each mode following Ca substitution. On the other hand, the observed transfer of spectral weight between the two modes can be interpreted as an increase in the dipolar moment associated to the higher frequency $\beta 2$ excitation. This effect would be expected following an increase of charge on each sublattice as a result of hole transfer between the chains and ladders as well as from an increase in the relative charge displacement. Since Ca doping leads to an increase in the lattice parameter c_{ch} but a decrease in c_{ld} resulting in a different chain-ladder staggering, we may indeed expect an increase in the relative charge displacement

for a mode where the chains and ladders are displaced in opposite directions. This picture is also consistent with the temperature dependent observations in Fig. 4(c) for the $x = 3$ sample. Since charges are more mobile on the ladders than on the chains [66] one could expect excitations associated with charge localization on the ladders (β_2) to be suppressed in contrast to chain based modes, as the conductivity on the ladders increases at a higher rate than on the chains when subjected to heating.

A. Comparison with other optical spectra

As previously mentioned, there are a number of existing studies which cover the sub-THz spectra of SCCO, notably the work by Thorsmølle *et al.* [33], who first suggested the sliding-mode nature of the excitations in this region. A series of publications by Gorshunov and Vuletić *et al.* [17,26,67–69] also studied the effects of Ca substitution on the spectra of SCCO, primarily focusing on properties associated with the charge ordering such as the CDW gap and MHz frequency phason modes. These studies also revealed strong excitations similar to our sliding mode observations below 1 THz, which Vuletić *et al.* ultimately identified as likely phonon in origin [26,69]. To compare these observations with our own, we have plotted the two datasets together in the Supplemental Material (see Ref. [43]). While the datasets agree on the presence of strong excitations in this region, we note a clear difference in the peak positioning and width profiles. Specifically, for the $x = 0$ sample we note a shift of ~ 0.12 THz to lower frequency when comparing the spectrum of Vuletić *et al.* to our observation of β_1 . There is no clear evidence of a second peak corresponding to our observation of β_2 although there does seem to be a shoulder of the peak profile stretching up to 0.6 THz which is not discussed in the text of Ref. [26]. The results for the $x = 3$ sample display similar behavior, in this case with a shift of ~ 0.12 THz to lower frequency compared to our observation of β_2 . Both datasets agree that there is a shift in spectral weight of ~ 0.3 THz towards higher frequencies when Ca concentration is increased from $x = 0$ to 3. However, while our results can be interpreted as a transfer of spectral weight between two broad modes (β_1 and β_2), the spectra of Vuletić *et al.* rather suggest hardening of a single, more narrow mode. Without more high-resolution measurements taken at intermediate calcium concentrations it is difficult to conclude which interpretation is correct. The relatively broad gaussian profiles of our observed peaks could be a result of in-homogeneous broadening due to disorder or defects in the samples. However, x-ray diffraction analysis indicates high-quality crystals [27].

In support of our observations, we highlight the transmission spectra of Thorsmølle *et al.* [33], which shows a clear absorption band stretching from ~ 0.3 – 1.0 THz covering the span of peaks β_1 and β_2 . We also highlight the reliable FIR absorption edge in Fig. 3. In our spectra we see the band edge for $x = 0$ falls at 1.14 THz, while for $x = 3$ it appears at 1.24 THz revealing a shift of only 0.1 THz. This is lower than the total shift in spectral weight observed in our spectra or the peak position shift presented by Vuletić *et al.* and would suggest that there is not simply a single peak shifting by 0.3 THz. Finally we point out that while

our measurements were performed in transmission geometry, the results of Vuletić *et al.* are determined by a Kramers-Kronig transformation of reflectivity data. Peak profiles at low frequency determined by a Kramers-Kronig transformation are highly sensitive to the accuracy of the reflectivity profile. Considering the intense reststrahlen band found for these excitations [33], it is possible that finer details of the peak profile including a secondary peak could be obscured in a reflectivity measurement. Evidently, transmission based measurements of these unique excitations might offer a different perspective than can be achieved in reflection.

B. Significance to the superconducting state

As a final comment, it is interesting to consider the nature of the sliding lattice dynamics in the context of the superconducting state observed at Ca concentrations of approximately $11 < x < 14$ under pressures on the order of ~ 3 – 5 GPa below ~ 14 K [31,32,70]. It has recently been commented that low-frequency vibrational excitations in other quasiperiodic systems could be significant in relation to observations of strong-coupling superconductivity [4–9]. This is because the electron-phonon coupling is essentially proportional to the inverse of phonon frequency ($\lambda \sim \Sigma_q \omega_q^{-1}$) [6]. Taking our interpretation of the spectra, which involves a softening of the sliding mode gap associated with β_1 , such coupling in SCCO could indeed grow for increasing Ca substitution. While we note that the superconducting channels in SCCO are predicted to occur primarily within the ladders [71,72], it is interesting to point out that the approximate trend of the energy and intensity of β_1 associated with both slow chain and ladder oscillations approaches zero in the $11 < x < 14$ superconducting range. This trend provides a promising indicator that the sliding mode dynamics of SCCO should perhaps be considered within models of the superconducting state. On the other hand, paying more consideration to the overall hardening of the sliding mode spectral weight upon Ca substitution (also supported by the spectra of Vuletić *et al.* [26]), the electron-phonon coupling model actually predicts a decrease in coupling for increased Ca concentration. In this regard, it is important to note other observations in the literature that show CDW softening for increasing Ca substitution in SCCO [26,44] and predict a softening to zero energy for Ca concentrations in the range of $x \approx 10$. Evidently there are a number of different collective dynamics converging at the phase boundaries of SCCO that indicate collective excitations do play a role in the superconducting thermodynamic landscape. We anticipate pressure dependent measurements of the sliding mode gap in SCCO to be a high priority in further understanding its overall significance.

V. CONCLUSION

In conclusion, we have probed the low-energy lattice dynamics of the quasiperiodic spin-ladder cuprate SCCO using synchrotron and laboratory-based THz spectroscopy. Specific focus on the energy gap of quasiaoustic sliding modes reveals two different excitations we associate with slow in-phase and fast out-of-phase chain-ladder sliding dynamics. An analysis of the dependence on Ca concentration of these modes primarily shows a transfer of spectral weight between the slow and

fast oscillations with increasing Ca substitution. We discuss this interpretation in contrast to previous studies which only identify a single strong mode that hardens upon Ca substitution. The approximate trends we observe are consistent with a transfer of intrinsic holes from the chain to ladder sublattices and could suggest complete suppression of the slower oscillations at the phase boundary of the superconducting phase. The results are discussed in the context of recent interest into the significance of low-frequency excitations in aperiodic systems exhibiting superconductivity. We highlight the importance of future experiments aimed at probing the external pressure dependence of these exotic excitations.

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- [1] D. C. Johnston, *Adv. Phys.* **59**, 803 (2010).
- [2] Y. Gallais and I. Paul, *C. R. Phys.* **17**, 113 (2016).
- [3] S. Manzeli, D. Ovchinnikov, D. Pasquier, O. V. Yazyev, and A. Kis, *Nat. Rev. Mater.* **2**, 17033 (2017).
- [4] L. E. Klintberg, S. K. Goh, P. L. Alireza, P. J. Saines, D. A. Tompsett, P. W. Logg, J. Yang, B. Chen, K. Yoshimura, and F. M. Grosche, *Phys. Rev. Lett.* **109**, 237008 (2012).
- [5] D. A. Tompsett, *Phys. Rev. B* **89**, 075117 (2014).
- [6] P. Brown, K. Semeniuk, D. Wang, B. Monserrat, C. J. Pickard, and F. M. Grosche, *Sci. Adv.* **4**, eaao4793 (2018).
- [7] R. Khasanov, H. Luetkens, E. Morenzoni, G. Simutis, S. Schönecker, A. Östlin, L. Chioncel, and A. Amato, *Phys. Rev. B* **98**, 140504(R) (2018).
- [8] M. Santoro, D. Colognesi, B. Monserrat, E. Gregoryanz, L. Ulivi, and F. A. Gorelli, *Phys. Rev. B* **98**, 104107 (2018).
- [9] Y. W. Cheung, Y. J. Hu, M. Imai, Y. Tanioku, H. Kanagawa, J. Murakawa, K. Moriyama, W. Zhang, K. T. Lai, K. Yoshimura, F. M. Grosche, K. Kaneko, S. Tsutsui, and S. K. Goh, *Phys. Rev. B* **98**, 161103(R) (2018).
- [10] E. M. McCarron, III, M. A. Subramanian, J. C. Calabrese, and R. L. Harlow, *Mater. Res. Bull.* **23**, 1355 (1988).
- [11] N. Nücker, M. Merz, C. A. Kuntscher, S. Gerhold, S. Schuppler, R. Neudert, M. S. Golden, J. Fink, D. Schild, S. Stadler *et al.*, *Phys. Rev. B* **62**, 14384 (2000).
- [12] J. Akimitsu, M. Uehara, T. Nagata, S. Matsumoto, Y. Kitaoka, H. Takahashi, and N. Môri, *Physica C (Amsterdam)* **263**, 475 (1996).
- [13] M. Kato, K. Shiota, and Y. Koike, *Physica C (Amsterdam)* **258**, 284 (1996).
- [14] T. Adachi, K. Shiota, M. Kato, T. Noji, and Y. Koike, *Solid State Commun.* **105**, 639 (1998).
- [15] D. E. Cox, T. Iglesias, K. Hirota, G. Shirane, M. Matsuda, N. Motoyama, H. Eisaki, and S. Uchida, *Phys. Rev. B* **57**, 10750 (1998).
- [16] G. Blumberg, P. Littlewood, A. Gozar, B. S. Dennis, N. Motoyama, H. Eisaki, and S. Uchida, *Science* **297**, 584 (2002).
- [17] B. Gorshunov, P. Haas, T. Rößm, M. Dressel, T. Vuletić, B. Korin-Hamzić, S. Tomić, J. Akimitsu, and T. Nagata, *Phys. Rev. B* **66**, 060508(R) (2002).
- [18] K.-Y. Choi, M. Grove, P. Lemmens, M. Fischer, G. Güntherodt, U. Ammerahl, B. Büchner, G. Dhalenne, A. Revcolevschi, and J. Akimitsu, *Phys. Rev. B* **73**, 104428 (2006).
- [19] P. Abbamonte, G. Blumberg, A. Rusydi, A. Gozar, P. G. Evans, T. Siegrist, L. Venema, H. Eisaki, E. D. Isaacs, and G. A. Sawatzky, *Nature (London)* **431**, 1078 (2004).
- [20] R. S. Eccleston, M. Azuma, and M. Takano, *Phys. Rev. B* **53**, R14721(R) (1996).
- [21] M. Matsuda, K. Katsumata, H. Eisaki, N. Motoyama, S. Uchida, S. M. Shapiro, and G. Shirane, *Phys. Rev. B* **54**, 12199 (1996).
- [22] M. Matsuda and K. Katsumata, *Phys. Rev. B* **53**, 12201 (1996).
- [23] R. S. Eccleston, M. Uehara, J. Akimitsu, H. Eisaki, N. Motoyama, and S. Uchida, *Phys. Rev. Lett.* **81**, 1702 (1998).
- [24] M. Matsuda, T. Yoshihama, K. Kakurai, and G. Shirane, *Phys. Rev. B* **59**, 1060 (1999).
- [25] J. E. Lorenzo, L. P. Regnault, C. Boullier, N. Martin, A. H. Moudden, S. Vanishri, C. Marin, and A. Revcolevschi, *Phys. Rev. Lett.* **105**, 097202 (2010).
- [26] T. Vuletić, B. Korin-Hamzić, S. Tomić, B. Gorshunov, P. Hass, T. Rößm, M. Dressel, J. Akimitsu, T. Sasaki, and T. Nagata, *Phys. Rev. Lett.* **90**, 257002 (2003).
- [27] G. Deng, V. Pomjakushin, V. Petříček, E. Pomjakushina, M. Kenzelmann, and K. Conder, *Phys. Rev. B* **84**, 144111 (2011).
- [28] M.-J. Huang, G. Deng, Y. Y. Chin, Z. Hu, J.-G. Cheng, F. C. Chou, K. Conder, J.-S. Zhou, T.-W. Pi, J. B. Goodenough *et al.*, *Phys. Rev. B* **88**, 014520 (2013).
- [29] G. Deng, N. Tsyrlin, P. Bourges, D. L. Amago, H. Ronnow, M. Kenzelmann, S. Danilkin, E. Pomjakushina, and K. Conder, *Phys. Rev. B* **88**, 014504 (2013).
- [30] R. Bag, K. Karmakar, S. Dhar, M. Tripathi, R. J. Choudhary, and S. Singh, *J. Phys. Condens. Matter* **31**, 035801 (2018).
- [31] M. Uehara, T. Nagata, J. Akimitsu, H. Takahashi, N. Môri, and K. Kinoshita, *J. Phys. Soc. Jpn.* **65**, 2764 (1996).
- [32] M. Isobe, T. Ohta, M. Onoda, F. Izumi, S. Nakano, J. Q. Li, Y. Matsui, and E. Takayama-Muromachi, *Phys. Rev. B* **57**, 613 (1998).
- [33] V. K. Thorsmølle, C. C. Homes, A. Gozar, G. Blumberg, J. L. M. van Mechelen, A. B. Kuzmenko, S. Vanishri, C. Marin, and H. M. Ronnow, *Phys. Rev. Lett.* **108**, 217401 (2012).
- [34] X. Chen, D. Bansal, S. Sullivan, D. L. Abernathy, A. A. Aczel, J. Zhou, O. Delaire, and L. Shi, *Phys. Rev. B* **94**, 134309 (2016).
- [35] G. Theodorou and T. M. Rice, *Phys. Rev. B* **18**, 2840 (1978).
- [36] G. Theodorou, *Solid State Commun.* **33**, 561 (1980).
- [37] B. Ruzicka, L. Degiorgi, U. Ammerahl, G. Dhalenne, and A. Revcolevschi, *Eur. Phys. J. B* **6**, 301 (1998).
- [38] N. Motoyama, T. Osafune, T. Kakeshita, H. Eisaki, and S. Uchida, *Phys. Rev. B* **55**, R3386 (1997).
- [39] G. Deng, D. Yu, R. Mole, E. Pomjakushina, K. Conder, M. Kenzelmann, S.-i. Yano, C.-W. Wang, K. C. Rule, J. S. Gardner, H. Luo, S. Li, C. Ulrich, P. Imperia, W. Ren, S. Cao, and G. J. McIntyre, *Phys. Rev. B* **98**, 184411 (2018).

- [40] G. Deng, D. M. Radheep, R. Thiyagarajan, E. Pomjakushina, S. Wang, N. Nikseresht, S. Arumugam, and K. Conder, *J. Cryst. Growth* **327**, 182 (2011).
- [41] J. Barros, C. Evain, L. Manceron, J.-B. Brubach, M.-A. Tordeux, P. Brunelle, L. Nadolski, A. Loulergue, M.-E. Couprie, S. Bielawski, C. Szwaj, and P. Roy, *Rev. Sci. Instrum.* **84**, 033102 (2013).
- [42] J. Barros, C. Evain, E. Roussel, L. Manceron, J.-B. Brubach, M.-A. Tordeux, M.-E. Couprie, S. Bielawski, C. Szwaj, M. Labat *et al.*, *J. Mol. Spectrosc.* **315**, 3 (2015).
- [43] See Supplemental Material at <http://link.aps.org/supplemental/10.1103/PhysRevB.100.184305> for detailed temperature dependence of peak fits, CSR data analysis procedure, spectral comparison with other published data, and diagrams of possible sliding mode excitations.
- [44] T. Osafune, N. Motoyama, H. Eisaki, S. Uchida, and S. Tajima, *Phys. Rev. Lett.* **82**, 1313 (1999).
- [45] C. C. Homes, T. Timusk, R. Liang, D. A. Bonn, and W. N. Hardy, *Phys. Rev. Lett.* **71**, 1645 (1993).
- [46] M. Grüninger, D. van der Marel, H. Geserich, T. Wolf, A. Erb, and T. Kopp, *Physica B (Amsterdam)* **244**, 60 (1998).
- [47] T. Rößm, D. Hüvonen, U. Nagel, J. Hwang, T. Timusk, and H. Kageyama, *Phys. Rev. B* **70**, 144417 (2004).
- [48] M. Ortolani, P. Calvani, S. Lupi, U. Schade, A. Perla, M. Fujita, and K. Yamada, *Phys. Rev. B* **73**, 184508 (2006).
- [49] M. Dumm, M. Abaker, M. Dressel, and L. K. Montgomery, *J. Low Temp. Phys.* **142**, 613 (2006).
- [50] A. Pustogow, T. Peterseim, S. Kolatschek, L. Engel, and M. Dressel, *Phys. Rev. B* **94**, 195125 (2016).
- [51] Z. V. Popović, M. J. Konstantinović, V. A. Ivanov, O. P. Khuong, R. Gajić, A. Vietkin, and V. V. Moshchalkov, *Phys. Rev. B* **62**, 4963 (2000).
- [52] S. Sugai and M. Suzuki, *J. Phys. Chem. Solids* **62**, 119 (2001).
- [53] M. Braden, J. Etrillard, A. Gukasov, U. Ammerahl, and A. Revcolevschi, *Phys. Rev. B* **69**, 214426 (2004).
- [54] A. Ruydi, P. Abbamonte, H. Eisaki, Y. Fujimaki, S. Smadici, N. Motoyama, S. Uchida, Y.-J. Kim, M. Rübhausen, and G. A. Sawatzky, *Phys. Rev. Lett.* **100**, 036403 (2008).
- [55] J. E. Eldridge, C. C. Homes, F. E. Bates, and G. S. Bates, *Phys. Rev. B, Condensed matter* **32**, 5156 (1985).
- [56] C. C. Homes and J. E. Eldridge, *Phys. Rev. B* **40**, 6138 (1989).
- [57] A. Damascelli, D. van der Marel, G. Dhahlenne, and A. Revcolevschi, *Phys. Rev. B* **61**, 12063 (2000).
- [58] B. Gorshunov, E. Zhukova, V. I. Torgashev, L. S. Kadyrov, E. A. Motovilova, F. Fischgrabe, V. Moshnyaga, T. Zhang, R. Kremer, U. Pracht, S. Zapf, and M. Dressel, *Phys. Rev. B* **87**, 245124 (2013).
- [59] D. Hüvonen, U. Nagel, T. Rößm, P. Haas, M. Dressel, J. Hwang, T. Timusk, Y.-J. Wang, and J. Akimitsu, *Phys. Rev. B* **76**, 134418 (2007).
- [60] E. Constable, G. Deng, J. Horvat, and R. A. Lewis, in *Proceedings of the 39th International Conference on Infrared, Millimeter, and Terahertz waves (IRMMW-THz)* (IEEE, Piscataway, NJ, 2014).
- [61] A. Pimenov, A. Pronin, A. Loidl, A. Tsukada, and M. Naito, *Phys. Rev. B* **66**, 212508 (2002).
- [62] T. Osafune, N. Motoyama, H. Eisaki, and S. Uchida, *Phys. Rev. Lett.* **78**, 1980 (1997).
- [63] K. P. Schmidt, C. Knetter, M. Grüninger, and G. S. Uhrig, *Phys. Rev. Lett.* **90**, 167201 (2003).
- [64] J. D. Axe and P. Bak, *Phys. Rev. B* **26**, 4963 (1982).
- [65] M. Osada, M. Kakihana, I. Nagai, T. Noji, T. Adachi, Y. Koike, J. Bäckström, M. Käll, and L. Börjesson, *Physica C (Amsterdam)* **338**, 161 (2000).
- [66] T. Nagata, M. Uehara, J. Goto, J. Akimitsu, N. Motoyama, H. Eisaki, S. Uchida, H. Takahashi, T. Nakanishi, and N. Mōri, *Phys. Rev. Lett.* **81**, 1090 (1998).
- [67] T. Vuletić, B. Korin-Hamzić, S. Tomić, B. Gorshunov, P. Haas, M. Dressel, J. Akimitsu, T. Sasaki, and T. Nagata, *Phys. Rev. B* **67**, 184521 (2003).
- [68] T. Vuletić, T. Ivek, B. Korin-Hamzić, S. Tomić, B. Gorshunov, P. Haas, M. Dressel, J. Akimitsu, T. Sasaki, and T. Nagata, *Phys. Rev. B* **71**, 012508 (2005).
- [69] T. Vuletić, B. Korin-Hamzić, T. Iveka, S. Tomić, B. Gorshunov, M. Dressel, and J. Akimitsu, *Phys. Rep.* **428**, 169 (2006).
- [70] D. M. Radheep, R. Thiyagarajan, S. Esakkimuthu, G. Deng, E. Pomjakushina, C. L. Prajapat, G. Ravikumar, K. Conder, G. Baskaran, and S. Arumugam, [arXiv:1303.0921](https://arxiv.org/abs/1303.0921).
- [71] E. Dagotto, J. Riera, and D. Scalapino, *Phys. Rev. B* **45**, 5744 (1992).
- [72] E. Dagotto, *Rep. Prog. Phys.* **62**, 1525 (1999).