# Photogrammetry in Traffic Accident Reconstruction 

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I am submitting herewith a dissertation written by Lara Lynn O'Shields entitled "Photogrammetry in Traffic Accident Reconstruction." I have examined the final electronic copy of this dissertation for form and content and recommend that it be accepted in partial fulfillment of the requirements for the degree of Doctor of Philosophy, with a major in Industrial Engineering.

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To the Graduate Council:
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Major Professor

We have read this dissertation and recommend its acceptance:

## Tyler Kress

Kenneth E. Kirby
Lee D. Han
Stephen H. Richards
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Accepted for the Council:
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Vice Provost and Dean of the Graduate School

# PHOTOGRAMMETRY IN TRAFFIC ACCIDENT RECONSTRUCTION 

A Dissertation<br>Presented for the<br>Doctor of Philosophy Degree<br>The University of Tennessee, Knoxville

Lara Lynn O'Shields
August 2007

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## DEDICATION

There are several to whom I wish to dedicate this dissertation.
Firstly, this dedication goes to my paternal grandmother, Blanche O'Shields, who passed away in January 2004. Words can't express how my life was so richly blessed with you in it. I'll never forget your love, your words of encouragement, and your unique sense of humor. You had such a prevalent presence in my life; I was at your house more than my own at times. For this reason, you are partly responsible for whom I am today, and I thank you immensely for that. You were certainly a fine lady, Mamaw, and I'll never forget you.


Blanche and Lara O'Shields circa 1974

This dissertation is also dedicated to my maternal grandparents, Ann and Furman Smoak formerly of Canadys, South Carolina. They passed away in February and April 2005, respectively. As a child, I remember how I would get so excited when visiting their house. Papaw Smoak was such a sweet and kind soul; he instilled in me a love for nature and the outdoors. Mamaw Smoak was the best cook in the South and always had a gift waiting for me when I would visit. They remembered every single one of my birthdays with a card and a piece of money. I miss you two so much. Even though I reside in Tennessee, South Carolina will always be my other home.


Furman \& Ann Smoak in SC in the late 1940's

I love you and miss you all so terribly. Life won't be the same without you.

Finally, I dedicate this dissertation to al/ my family and friends (some who are begrudgingly unidentified), who have helped me emotionally, financially, and otherwise over the years. I couldn't have done this at all without your help.

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a small fraction of his intelligence, then I would be awesome.
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#### Abstract

The aim of this research is to utilize PhotoModeler, a closerange photogrammetry software package, in various traffic accident reconstruction applications. More specifically, three distinct studies were conducted: 1.) vehicle crush measurement, 2.) road curve measurement, and 3.) an evaluation of common traffic accident reconstruction measurement methodologies.

The first study applied the photogrammetric process to controlled crash information generated by the National Highway Traffic Safety Administration (NHTSA). A statistical procedure known as bootstrapping was utilized to generate distributions from which the variability was examined. The "within" subject analysis showed that $44.8 \%$ of the variability is due to the technique itself and the "between" subjects analysis demonstrated that 55.2\% of the variability is attributable to vehicle type-roughly half and half. Additionally, a 95\% CI for the "within" analysis revealed that the mean difference (between this study and NHTSA) fell between -


2.52 mph and +2.74 mph ; the "between" analysis showed a mean difference between -3.26 and +2.41 mph .

The second study focused on photogrammetry in road curve measurement. More particularly, this study applied photogrammetry to (simulated) road curves in lieu of traditional measurement methods, such as measuring tapes and measuring wheels. In this work, thirty (30) different radii of curvature of various known sizes were deliberately constructed. Then photogrammetry was used to measure each of the constructed curves. A comparison of the known "R's" (control group) and photogrammetry's value of "R" (treatment group) was then made. Matched Pairs or Paired Comparisons were then used to examine these two populations. The difference between the photogrammetry " $R$ " and the known " $R$ " range is between $0.001 \%$ and $0.874 \%$. Additionally, we are $95 \%$ confident that the mean difference of the two techniques is between -0.33 and 0.51 feet. Since this interval contains zero, we can conclude that the two techniques do not differ.

The third study's aim was to learn what causes variation in three common traffic accident reconstruction measurement techniques: measuring tape, measuring wheels and photogrammetry. These three techniques were evaluated against a known benchmark distance measured by a total station. A full factorial $2^{3}$ Design of Experiments study with four replicates was applied to each technique. The following results were found:

Measuring tape experiment: None of the main effects or crosseffects were significant. Measuring wheel experiment: Two main effects ( $\mathrm{p}<0.0001$ and $\mathrm{p}<0.0060$ ) and all of the cross-effects ( $\mathrm{p}<0.0079$ to 0.0345 ) were significant. Photogrammetry experiment: One main effect ( $\mathrm{p}<0.0063$ ) and one cross effect ( $\mathrm{p}<0.0325$ ) were significant. The measuring wheel is most sensitive to surface type (smooth or rough surface) and photogrammetry is most sensitive to digital resolution (low or high resolution).

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## INTRODUCTION

## General Introduction

This dissertation is a collection of three (3) experimental studies that focuses on PhotoModeler, a close-range photogrammetric software package, and its role in traffic accident reconstruction. Photogrammetry is the science and art of obtaining measurements from photographs, hence; photogrammetric measurements useful to Accident Reconstructionists are at the core of this dissertation. In the first two studies, the extracted photogrammetric measurements + engineering equations = information that is useful to the accident reconstructionist, such as speed prior to impact and the critical speed of a curve. (The third study is simply an evaluation of various measurement techniques available to accident reconstructionists, including photogrammetry.)

Part One of this work involves vehicle crush measurement using photogrammetry. If one can measure the amount of crush in a vehicle, the speed prior to impact may be determined either from crush alone or crush plus other engineering analyses; this, of course, is dependent on the particulars of the accident. The relationship of
crush and speed is approximately linear in nature or proportional to one another; the more the vehicle is crushed, the faster it was going prior to impact and vice versa. The crush analysis process essentially involves the collection of the following: 1.) Six (6) evenly-spaced crush measurements from the affected crush area 2.) Crush coefficients specific to the subject vehicle; they can be computed, estimated, or purchased 3.) Other information such as vehicle weight and width of crush. The above information is then used in the crush equation developed by Campbell [1] and later revised by McHenry [2], which will yield the energy dissipated by crush. Speed due to this energy (hence, the speed of the vehicle) can subsequently be computed.

Photogrammetric crush measurement involves creating a 3-D model of the superimposed crushed and exemplar vehicles with the photogrammetry software. The pre- and post-impact crush positions are known precisely, which makes it superior to other crushmeasurement methodologies like measuring poles, measuring tapes, and tarp and plumb bob. Moreover, this study makes use of controlled crash data (in the form of photographs and other vehicle
information) generated by NHTSA. NHTSA conducts its frontal barrier crash testing at around 35 mph . So if this study's results are close to thirty-five (35) mph, all the better. For all intents and purposes, Part One is comprised of the following: photographs from the NHTSA frontal crash test reports are examined for photogrammetric feasibility; from "approved" reports/photographs, a 3-D model is generated and crush measurements are extracted; speed is computed using the aforementioned crush equations in a spreadsheet-type format; and finally an analysis using bootstrapping of this study's speed estimate versus the actual speed stated in the report was performed.

Part Two of this research concerns photogrammetric road curve measurement. Instead of using traditional measurement techniques such as measuring tapes or wheels, photogrammetry was used to measure curves. Thirty (30) known radii of curvature were deliberately constructed at a local airport using a pre-measured cable. Six (6) specifically made targeted traffic cones were used in this analysis; five (5) were placed along the arc of the curve and one (1) was placed directly across from the others. Various photographs
from various angles were then taken of the cones. The curves were ultimately measured by extracting an " I " or chord and an " h " or middle ordinate from the photogrammetry software. $r=\frac{r^{2}}{8 h}+\frac{h}{2}$ was then used to generate an estimate for each of the photogrammetrically-induced radii. These radii (treatment group) were compared to the known radii (control group) and a statistical procedure called Matched Pairs or Paired Comparisons was used to investigate the two groups.

Part Three examines the inherent variation in three common accident reconstruction measurement methodologies: the measuring tape, the measuring wheel, and photogrammetry. A $2^{3}$ full-factorial Design of Experiments study was performed to study these variations. A pre-measured distance of forty-eight (48) feet, established by a total station, was used as a benchmark
measurement in this experiment. This benchmark distance was measured a grand total of one hundred and twenty (120) times in Part Three; each of the above techniques measured the benchmark forty (40) times (each technique utilized a $2^{3}$ full factorial with four
(4) replicates, which equals forty observations total). The factors selected for this study are as follows: Measuring Tape-tape type (cloth or steel), amount of masking tape used (low or high), and exposure to the road (low or high). Measuring Wheel-surface type (smooth or rough), wheel diameter (small or large) and road exposure (low or high). Photogrammetry-Number of pictures (low (4) or high (8)), digital resolution of the camera (low or high), and road exposure (low or high). The statistical software program JMP randomly determined the sequence of each of the treatment combinations via the embedded DOE tool. Each of the treatment combinations were recorded and input into the DOE tool and were subsequently analyzed for statistical significance.

## Background

## Photogrammetry In General

## History

"Photogrammetry", as defined by the American Society for Photogrammetry and Remote Sensing (ASPRS), "is the art, science, and technology of obtaining reliable information about physical objects and the environment, through processes of recording,
measuring, and interpreting (photographic) images and patterns of electromagnetic radiant energy and other phenomena"; this is the definition from the ASPRS website [11]. It is interesting to note that this website definition and the Manual of Photogrammetry Fifth

Edition [3] are nearly word-for-word except for the word "photographic". The Manual (current as of 2004, but quoting the $19804^{\text {th }}$ edition definition) includes the words "photographic images". Perhaps the website definition is acknowledging the emergence and use of digital technologies; "photographs" can be construed by some as strictly coming from a film camera. Remote Sensing came a part of the American Society for Photogrammetry in 1975 [3] in name and in definition. The abovementioned definition which states
"interpreting (photographic) images and patterns of electromagnetic radiant energy and other phenomena" obviously reflects the inclustion of remote sensing into ASPRS. For the purposes of this work, the American Society for Photogrammetry's 1934 defintion [3]
will be rightfully appropriate: "The science and art of obtaining reliable measurements by means of photographs", with the
understanding that "photograph" can mean either "digital photograph" or "film photograph" in the work of this research.

Since photogrammetry's beginnings in the mid $19^{\text {th }}$ century, its main objective was for map-making purposes [3] and in fact, still is [6]. Topographic photogrammetry has object to camera distances of up to many miles, for example; an airplane performing an aerial survey at 10,000 feet would fit into this category. Non-topographic photogrammetry or close-range photogrammetry has object to camera distances of inches to hundreds of feet; accident reconstruction applications like crush measurement and accident scene documentation belong here. The Handbook of NonTopographic Photogrammetry [3] defines this distance to be not more that three hundred (300) meters or nine hundred eighty-four (984) feet.

Photogrammetry's inception, from a practical or serviceable standpoint, began with the invention of photography in the mid $19^{\text {th }}$ century; photogrammetry's primary media, of course, are photographs. However, the optical principles that lay the foundation for photogrammetry actually came earlier-around two thousand
years earlier with Aristotole in 350 B.C. and later in 1492 with Leonardo da Vinci.

Photogrammetry, thus far, has evolved in four (4) different phases or cycles, with each reflecting the up-and-coming technologies of the day: The First Generation: Early Developments in Photogrammetry (1850 to 1900), The Second Generation: The Analog Phase (1900 to 1960), The Third Generation: The Analytical Phase (1960 to 1990), and The Fourth Generation: The Digital Phase (1990 to Present) [3, 4, 6, 12].

Before a discussion of the Four Generations is developed, there is a phase or cycle that is notable to mention which lays the foundation for all of photogrammetry, which will be called here the "Precursors to Photogrammetry" [4]. This particular phase includes all the developments leading up to the invention of photogrammetry, such as Durer's outlined Law's of Perspective (1525), Lambert's "Free Perpective", which combined mathematics with perspective and utilized them for map-making purposes (1759), and Daguerre's first practical photograph on metal plates, called Daguerreotypes (1837).

The emergence of photographs heralded a new era: The First Generation of Photogrammetry.

Generation One began when Colonel Aime Laussedat made maps from photographs in 1849. His efforts earned him the name "The Father of Photogrammetry". People using photogrammetry in this era would mount cameras onto balloons or kites to gain a higher viewpoint, however; these experiments usually yielded disappointing results for map-making purposes. Therefore, mapping operations (such as those carried out by Deville in Canada) largely utilized ground photography for their surveying functions.

The Second Generation of photogrammetry was dubbed the Analog Era. It was "flung" into existence by the invention of the airplane. Airplanes were mounted with large format cameras and photos would be taken of various terrains for map-making purposes. 3-D models could be subsequently generated from hardcopy 2-D images using optical or mechanical means. This was usually accomplished by large machines specifically designed for this purpose; The Autocartograph, Stereoplanigraph, and the Aerocartograph are some examples [4]. "When transparencies of
overlapping photos were properly oriented in their projectors, corresponding light rays from the two photos were projected through objective lenses to create an accurate model of the overlapping terrain, and a map of the model could be drawn" [14]. The map generated in this process is an analog of the images themselves, hence the name.

The computer was the impetus for the Third Generation, the Analytical Era. In this cycle, 3-D models were created mathematically from photographs (as opposed to being physically fashioned by machine in the previous era). The photogrammetric equations, highly mathematical, iterative, and analytical in nature, were now made useful with the advent of the computer. Previously, analytical solutions ran the risk of being riddled with errors and took enormous amounts of time to solve. The computer made analytical solutions practical [4, 7]. The analytical equations themselves have inclusions for object space coordinates, image space coordinates, and camera parameters, and will be discussed in a following section. Analytical photogrammetry was used primarily for topographical purposes,
however; non-topographic photogrammetry (aka close-range photogrammetry) got its start during this era.

The Fourth Generation, called the Digital Era, became apparent upon the creation of the charged-coupled-device (CCD), the primary component in digital cameras. Digital photogrammetry develops analytical solutions via digital images. Fraser [13] says "in the arena of non-topographic applications, digital photogrammetry has rendered film-based systems largely obsolescent." Additionally, Wolf [14] states that "Digital photogrammetry can be performed at a savings in labor and in cost," thereby circumventing the charge for the film itself and its processing, and time lost attributable to film processing and scanning. However, the use of digital photos is not without its critics. Unfortunately, digital photos have the ability to be "enhanced" with photographic software. This "enhancement" can range from the variation of the brightness and contrast values to a fraudulent manipulation of the components of the image itself, possibly revealing/removing elements that weren't there initially. So in some situations, using film over digital images is not a failure of the application of technology, but simply a preference for a particular
documentation medium which may or may not have later legal implications. Table 1, History of Photogrammetry, delineates significant developments throughout these four phases.

## Theory

Analytical photogrammetry, as mentioned above, is where the coordinates of the objects of interest (and subsequently their measurements) are computed mathematically with algorithms. Essentially what is taking place in analytical photogrammetry is a conversion of one coordinate system to another coordinate system [4, 15-20], i.e., 3-D to 2-D or the reverse. The first coordinate system, called object space, is 3-dimensional in nature. It is the "real world" in which we live. For example, the left corner of a desk has components in three directions, $\mathrm{X}, \mathrm{Y}$, and Z (object space is designated by the uppercase coordinates), when associated with some arbitrary coordinate system. The second coordinate system, called image space, is 2-dimensional in nature. A photograph (or digital image printed on paper) in and of itself has 2-D characteristics. Using the above desk example, one could easily identify the left corner of a desk in a photograph, which would have

Table 1. History of Photogrammetry

| HISTORY OF PHOTOGRAMMETRY |  |  |  |
| :---: | :---: | :---: | :---: |
| Date | Contributor | Contribution | Source |
| 350 BC | Aristotle | Referred to the process of projecting images optically | [5] |
| 1492 | Leonardo da Vinci | Developed the principles of perspective and optical projection which forms the basis of photogrammetric theory | $\begin{aligned} & {[4],[6],} \\ & {[7],[8]} \end{aligned}$ |
| Early $16^{\text {th }}$ Century | Desargues \& Pascal | Mathematicians that had proven some of the laws of perspective | [4] |
| 1525 | Albrecht Durer | Outlined the laws of perspective and developed a mechanical device that produced a true perspective drawing | $\begin{aligned} & {[4],[6],} \\ & {[7],[8]} \end{aligned}$ |
| 1574 | Aughtread | Constructed the first slide rule | [4] |
| $\begin{aligned} & \text { Circa } \\ & 1574 \\ & \hline \end{aligned}$ | John Napier | Published tables of logarithms | [4] |
| $\begin{aligned} & \text { Circa } \\ & 1574 \end{aligned}$ | Blaise Pascal | Created a desk calculator | [4] |
| $\begin{array}{\|l} \hline \text { Circa } \\ 1600 \\ \hline \end{array}$ | Johannes Kepler | Gave a precise definition of stereoscopy | [4] |
| $\begin{aligned} & \text { Circa } \\ & 1600 \\ & \hline \end{aligned}$ | Jacopo Chimenti | Produced the first hand-drawn stereo-picture pair | [4] |
| $\begin{aligned} & \text { Circa } \\ & 1630 \end{aligned}$ | Issac Newton and Gottfried von Leibnitz | Presented scholars with differential and integral calculus | [4] |
| 1715 | Brook Taylor | Published a book on linear perspective | [5], [9] |
| 1726 | F. Kapeller | Constructed a topographic map of Mt. Pilatus, near Lake Lucerne in Switzerland | 4] |
| 1759 | Schultz | Observed that silver nitrate blackens when exposed to sunlight | [4] |
| 1783 | Montgolfier | Made the first successful hot-air balloon flights near Paris | [4] |
| 1837 | Jacques <br> Mande <br> Daguerre | Created the first "practical" photographs on metal plates called daguerreotypes | $\begin{aligned} & {[4],[5],} \\ & {[6],[8],} \\ & {[14]} \end{aligned}$ |
| 1840 | Dominique Francois Jean Arago | Advocated the use of photography by topographers to members of the French Arts and Science Academy | [4], [6] |
| 1849 | Aime Laussedat | First to use photographs for map making; "The Father of Photogrammetry" | $\begin{aligned} & {[4],[6],} \\ & {[9]} \end{aligned}$ |
| 1855 | Tournachon (aka Nadar) | Obtained the first aerial photograph | [4], [6] |
| 1858 | Aime Laussedat | Suspended a camera with kites and balloons for map-making purposes | [4], [6] |
| 1858 | A. Meydenbauer | Performed surveys of historical monuments, churches, and buildings | [7] |
| 1859 | Aime Laussadat | Presented the use of the phototheodolite (a camera and theodolite) for map making to the Academy of Science in Paris | [4], [6] |

## Table 1. cont'd

| HISTORY OF PHOTOGRAMMETRY |  |  |  |
| :---: | :---: | :---: | :---: |
| Date | Contributor | Contribution | Source |
| 1867 | Aime Laussadat\| | Publicly exhibited the first known phototheodolite and a plan of Paris based on photographic surveys | [4], [6] |
| 1868 | Chevallier | Developed the photographic plane table | [4], [6] |
| 1871 | Ernst Abbe | Studied the design of optical elements and their combination with an intense mathematical basis | [4] |
| 1885 | George Eastman | Used nitrocellulose as a film base and later (1890) replaced the photographic dry plate for roll film | [5], [6] |
| 1886 | E. Deville | Used ground Photogrammetry for topographic mapping of the rugged mountains of Western Canada | $\begin{aligned} & {[4],[5],} \\ & {[7],[9]} \end{aligned}$ |
| 1893 | A. Meydenbauer | Published a paper on photographic surveying in which the term "Photogrammetry" was first used | [4] |
| 1896 | E. Deville | Invented the first stereoscopic-plotting instrument | [4], [6] |
| 1899 | Sebastian Finsterwalder | Published "Fundamental Geometry of Photogrammetry" a seminal paper on analytical Photogrammetry | [4], [6] |
| 1901 | Carl Pulfrich | Designed the first stereocomperator, the first photogrammetric instrument manufactured by Zeiss | [5], [6] |
| $\begin{array}{\|l} \hline \text { Circa } \\ 1901 \\ \hline \end{array}$ | Henry George Fourcade | Independently developed a similar stereocomperator to Pulfrich's | 6] |
| 1902 | Wright Brothers | Invented the airplane | $\begin{aligned} & {[5],[6],} \\ & {[14]} \end{aligned}$ |
| 1907 | Ritter von Orel | Developed the first stereoautograph | [6] |
| 1910 |  | The International Society for Photogrammetry was formed | [7] |
| 1913 |  | The airplane was first used for obtaining photographs for mapping | [5], [14] |
| 1914 | Arthur and Norman Brook | Physically mounted an aerial camera to an airplane instead of holding the camera over the side | 6] |
| 1921 | Reinhard Hugershoff | Created the first analog plotter called the autocartograph | 4], [6] |
| 1923 | Zeiss Works | Produced a plotting instrument known as the Zeiss Stereoplanigraph | [4] |
| 1924 | Otto von Gruber | Derived the projective equations and their differentials which are fundamental to analytical Photogrammetry | 6] |
| 1926 | Reinhard Hugershoff | Created the Aerocartograph, a lighter version of the Autocartograph | 4], [6] |
| 1930's | TVA \& USGS | Undertook the topographic mapping of the entire Tennesse river basin by aerial Photogrammetry ( 40,000 square miles) | [4], [14] |
| 1930 | Earl Church | Developed analytical solutions to space resection, orientation, intersection, rectification, and control extension using direction cosines | [4], [6] |
| 1934 |  | The American Society for Photogrammetry was formed | [4] |
| 1941 | Zure | Invented the computer in Germany | [6] |

## Table 1. cont'd

| HISTORY OF PHOTOGRAMMETRY |  |  |  |
| :---: | :---: | :---: | :---: |
| Date | Contributor | Contribution | Source |
| 1942 | Bausch \& Lomb Optical Company | Engaged in a comprehensive manufacturing program for photogrammetric optics, photointerpretation equipment, and map-producing devices | [4] |
| 1943 | Aitken | Independently invented the computer in the US | [6] |
| 1951 | Everett Merritt | Extended Church's work by making it more complete and published a complete exposition of his work in analytical photogrammetry in 1958 | [4], [6] |
| 1953 | Helmut Schmid | Developed the principles of modern multi-station analytical photogrammetry using matrix notation | [4], [6] |
| 1955 | Duane Brown | Developed new approaches to camera calibration on the utilization of the bundle adjustment | [4], [6] |
| 1956 | Paul Herget | Developed an approach to analytical control using vector notation | [4], [6] |
| 1957 | Uki Helava | Invented the analytical stereoplotter | [4], [6] |
| $\begin{aligned} & \hline \text { Late } \\ & 1950 \text { 's } \\ & \hline \end{aligned}$ | G.M. Schut | Applied the coplaniarity concept to analytical triangulation | [4], [6] |
| 1959 | Hellmut Schmid | Applied the least-squares method to the simultaneous solution to any number of photographs and the first photogrammetrist to plan his solutions in the anticipation of high-speed computers | [4] |
| $\begin{aligned} & 1951 \text { to } \\ & 1967 \end{aligned}$ | Gilbert Hobrough | Helped to develop Digital Photogrammetry through various inventions | 6] |
| $\begin{aligned} & 1959 \text { to } \\ & 1972 \end{aligned}$ |  | The Corona program was the first major satellite photo intelligence gathering system during the cold war | [4] |
| $\begin{aligned} & 1967 \text { to } \\ & 1992 \\ & \hline \end{aligned}$ | Uki Helava | Helped to develop Digital Photogrammetry through various inventions | 6] |
| 1971 | Houssam Karara | Developed Direct Linear Transformation (DLT), a method that does not require camera calibration data | 6] |
| $\begin{aligned} & \text { 1980's } \\ & \text { to } \\ & 1990 \text { 's } \end{aligned}$ |  | Expanded development and utilization of the conversion of hardcopy photographs to digital form via scanners | [4] |
| $\begin{aligned} & 1990 \text { 's } \\ & \text { to } \\ & \text { Present } \end{aligned}$ |  | CCD (Charged Couple Devices) allow for non-photographic imaging and the direct digital storage to computers | [6] |

associated 2-D coordinates (x \& y, lowercase) with respect to an arbitrary 2-D coordinate system. The third coordinate system, which this author terms "model space", is 3-D in nature. This 3-D space is reconstructed from the 2-D photographs. Note that in order to perform this type of reconstruction, a minimum of two (2) photographs are required. Some accident reconstruction applications only require 2-D photogrammetry, such as documentation of a road scene-here only one (1) photo is needed. But 3-D applications, such as vehicle crush measurement, require a minimum of two (2) photos to get that third dimension. For clarification, think about the human eyes. With only one (1) eye, we can see only in 2-D. But with both eyes, we see in 3-D because each eyeball has a slightly different perspective of the subject and the brain fuses or combines the two scenes. A similar situation is the children's toy, the Viewmaster. Photos of the Viewmaster are taken with a stereocamera, which is a two-camera or a two-lens specialty camera which takes two (2) photos of a slightly different perspective simultaneously. The result when looking through the Viewmaster is a 3-D image that has depth, or a stereomodel.

In this work, the coordinate conversions are as follows: 3-D (object space) $\rightarrow$ 2-D (image space) $\rightarrow 3$-D (model space). This is illustrated with an example in Figure 1. On the far left in Figure 1, we have a 3-Dimensional car that exists in the "real world" or Object Space. If we want, we can give, say, the left corner of the hood, a 3-D coordinate ( $X, Y$, and $Z$ ). In the center of Figure 1, we have several 2-D representations or photographs of the 3-D object. We could, if necessary, identify the same point (left corner of the hood) in at least three (3), probably four (4) of those photographs. The points on the photographs would be of the form ( $x, y$ ) and would be considered to be in Image Space. The right-most portion of Figure 1 is a screenshot from Case \#5 in Part One of this work. In the upperleft corner of the screenshot, one can see PhotoModeler's 3-D

Viewer, which is a black-filled window with a wire-frame model of the car. After much manipulation of the PhotoModeler software, and through the magic of analytical photogrammetry, a 3-D model can be recovered or recaptured from the 2-Dimensional photographs.


Figure 1. Coordinate Conversion Example

Objects in the 3-D Viewer have coordinates of the form ( $X, Y, Z$ ) and exist in Model Space. Only after a 3-D model is created can measurements be extracted. When operating within PhotoModeler, coordinate systems are automatically assigned to the project, so the act of going from 3-D to 2-D to 3-D (object to image to model) is a seamless operation unknown to the user, however; seasoned PhotoModeler users can find indications of this process in various locations throughout the software.

## The Collinearity Condition

The Collinearity Condition [4, 5, 16, 17], the basis behind the collinearity equations, is illustrated in Figure 2. The Collinearity Condition requires that the object point $A$, the perspective center $C$ (at the camera lens) and the image point a, all lie in a straight line. This straight line requirement is exploited to develop the collinearity equations. In Figure 2, one can see the straight line requirement of $A$, $a$, and $C$. " $A$ " possesses the three (3) coordinates $X_{A}, Y_{A}$, and $Z_{A}$ (uppercase denoting object space) and "a" has its respective 2-D image space coordinates $x_{a}$ and $y_{a}$. Note that " $A$ " and " $a$ " are homologous; they are the same point, but in different coordinate


Figure 2. The Collinearity Condition
systems. In the collinearity equations, the image point "a" is put in terms of the principal point "PP" and its respective coordinates $\mathrm{X}_{0}$ and $y_{0}$. The principal point is where the principal ray (the straight-line ray that travels from point " $A$ " through the center of the lens to the center of the imaging plane unrefracted [4, 16, 21]) intersects the image plane, and is usually the center of the negative or CCD. In Figure 2, "PP" appears not to be in the center as it should be, but for illustration, it was (probably) offset to demonstrate that it also possesses its own respective image space coordinates. "-f" is the
focal length of the camera (sometimes it is denoted with a " +f ", depending on which convention is used) and " C " denotes the center of the camera lens with its respective object space coordinates $X_{C}$, $Y_{C}$, and $Z_{c}$. In reality, each camera has inherent lens distortion, making this straight-line assumption invalid, however; cameras that are calibrated (either via a calibration program or calibration certificate) have these lens distortion characteristics known, making it a much more accurate device for measuring (camera calibration is the process of taking photos of a special grid from a variety of angles to determine lens distortion, principal point location, focal length, and format size). The author has calibrated several cameras for this work and other works using PhotoModeler's embedded camera calibrator program; the results of the calibrations are located in the Appendix 1 and 13.

## Collinearity Equations

As mentioned previously, the collinearity condition is used to develop the collinearity equations. The collinearity equations [4, 5, 16, 17] associate 3-D object space to 2-D image space in a mathematical fashion. They relate the 2-D image space coordinates
in terms of principal point, focal length, camera location, camera
rotation, and the 3-D coordinates of the object point. The derivation of the equations will not be done here. The reader is referred to the Manual of Photogrammetry [4] or one of the many other photogrammetry texts available $[5,17,18,20]$. The equations are as follows:

$$
\begin{aligned}
& x_{A}=x_{0}-f\left[\frac{m_{11}\left(X_{A}-X_{C}\right)+m_{12}\left(Y_{A}-Y_{C}\right)+m_{13}\left(Z_{A}-Z_{C}\right)}{m_{31}\left(X_{A}-X_{C}\right)+m_{32}\left(Y_{A}-Y_{C}\right)+m_{33}\left(Z_{A}-Z_{C}\right)}\right] \\
& y_{A}=y_{0}-f\left[\frac{m_{21}\left(X_{A}-X_{C}\right)+m_{22}\left(Y_{A}-Y_{C}\right)+m_{23}\left(Z_{A}-Z_{C}\right)}{m_{31}\left(X_{A}-X_{C}\right)+m_{32}\left(Y_{A}-Y_{C}\right)+m_{33}\left(Z_{A}-Z_{C}\right)}\right]
\end{aligned}
$$

where:
$x_{A}$ and $y_{A} \quad$ are A's image space coordinates
$X_{A}, Y_{A}$, and $Z_{A}$ are A's object space coordinates
$X_{c}, Y_{c}$, and $Z_{C}$ are the object space coordinates of the camera
$m_{11}$ thru $m_{33} \quad$ are the coefficients of the Rotation Matrix
$x_{0}$ and $y_{0} \quad$ are the image space coordinates of the principal point
$f \quad$ is the focal length of the camera lens

The Rotation Matrix, in terms of camera rotation angles $\omega, \phi$, and $\kappa$, is as follows:

$$
\begin{aligned}
& m_{11}=\cos \omega \cdot \cos \phi \\
& m_{12}=\cos \omega \cdot \sin \phi \\
& m_{13}=-\sin \omega \\
& m_{21}=\sin \kappa \cdot \sin \omega \cdot \cos \phi-\cos \kappa \cdot \sin \phi \\
& m_{22}=\cos \kappa \cdot \cos \phi+\sin \kappa \cdot \sin \omega \cdot \sin \phi \\
& m_{23}=\sin \kappa \cdot \cos \omega \\
& m_{31}=\cos \kappa \cdot \sin \omega \cdot \cos \phi+\sin \kappa \cdot \sin \phi \\
& m_{32}=\cos \kappa \cdot \sin \omega \cdot \sin \phi-\sin \kappa \cdot \cos \phi \\
& m_{33}=\cos \kappa \cdot \cos \omega
\end{aligned}
$$

## PhotoModeler Software

It is not known precisely how analytical photogrammetry solutions are performed within the PhotoModeler Pro Software, however; it is assumed that the collinearity equations are used in some capacity. Many times in the PhotoModeler software help files [21] the collinearity condition is indirectly referenced particularly in the areas which explain how PhotoModeler works. The author is reluctant to contact PhotoModeler directly for information on their algorithm—most likely this is intellectual property and/or a proprietary secret. In fact, the PhotoModeler website states in a 2001 press release that their algorithm "is the result of more than 8 years of development and contains many of the known leading solution methods along with a number of proprietary improvements" [22]. But EOS Systems Inc. (PhotoModeler's parent company) does concede on the website and help files that a "bundle adjustment" is used and processing is executed in three stages (orientation, global optimization, and self-calibration) for the arrival of an optimal solution. The inclusion of a description of this process will not be
done here; readers are referred to the sources above for more clarification.

## Accuracy

Photogrammetric accuracy can range from low (1:5000) to high $(1: 50,000)$ and its cost is typically proportional to its accuracy (\$1000 to $\$ 100,000$, respectively) [46]. The notation of $1: N$, with $N$ being some number is a common technique to depict accuracy in photogrammetry. This methodology is a much better descriptor of accuracy than saying "It's $1 / 2$ of an inch off." This statement tells the interested persons little to nothing about the scale of the project being measured, but 1 : N incorporates the scale automatically into this expression. Being 0.5 of an inch off is rather good if the project is around 500 feet in length $(1: 12,000)$ but not so good if the project were about 1 ft in length (1:24). Conversely, a 1:10,000 accuracy could apply to a 50ft object (0.06 of an inch in error) or to a 1 ft object ( 0.0012 of an inch in error) [47]. The following table is a summary of a sample of photogrammetric studies in which their accuracies are reported. It is interesting to note that PhotoModeler's accuracies range from 1:75 to 1:30,000. Alan Walford (president of 25

EOS Systems) states on the PhotoModeler website that 1:300,000 "could be the project accuracy" and "for most projects the accuracy would be lower than this" [28]. While researching the literature the author uncovered variety of software packages that were used in the studies such as PhotoModeler, Foto-G, OrthoMAX, self-developed software, and others. The majority of the studies provide a declaration of a benchmark measurement, with the preferred technique being the Total Station. A benchmark measurement is a reference measurement by which the study's measurements are compared. (The Total Station is well-regarded in terms of accuracy, but equipment cost and usability are common drawbacks.) One can see from a quick look of the table that a whole host of accuracies are realized. This author's previous accuracies with PhotoModeler are about 1:750 for crush measurement projects and up to 1:5400 for a bank robbery project (forensic photogrammetry). Potential users of photogrammetry will have to decide how much budgetary constraints will play when purchasing software; as said before, accuracy is proportional to cost in most cases. Overall, PhotoModeler is a very good buy in terms of accuracy and value. Table 2 is as follows:

Table 2. Reported Accuracies For Selected Photogrammetric Studies

| TABLE OF ACCURACY SUMMARIES |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Author | Application | Benchmark | Software/Method Used | Reported Accuracy |
| Kullgren, et al. [23] | Vehicle Crush (TAR) | Not Given | Self-Developed Software | 1:325 |
| Rentschler \& Uffenkamp [24] | Vehicle Crush (TAR) | CMM | Imetric | 1:4250 |
| Switzer \& Candrlic [25] | An Accuracy Study for AR's | Total Station | PhotoModeler | 1:75 to 1:5500 |
| Pepe et al. [8] | An Accuracy Study for AR's | Total Station | FotoGram, Plantran, TRANS4, and Others | 1:50 to 1:125 |
| Zicarelli [26] | Industrial PG | Not Given | PM ${ }^{3}$ Lite | 1:3100 |
| Aguilar et al. [27] | Agricultural PG | Laser Scanner | Shape Capture | 1:2400 |
| PhotoModeler Website [28] | Accuracy Table on Website | Not Given | PhotoModeler | 1:350 to 1:300,000 |
| Deng \& Faig [29] | An Accuracy Study | Total Station | PhotoModeler | 1:800 to 1:1700 |
| Fraser and Riedel [30] | Industrial PG | Not Given | Austrailis | 1:9000 |
| Fenton et al. [10] | Vehicle Crush (TAR) | Not Given | PhotoModeler | 1:1400 |
| Jordan et al. [31] | PGM of Horse Hooves | CMM | PhotoModeler | 1:2500 to 1:5000 |
| Chandler et al. $\qquad$ [32] | $\begin{gathered} \hline \text { PG Accuracy } \\ \text { Study } \\ \hline \end{gathered}$ | Total Station | Imagine's Ortho BASE Pro | 1:1000 to 1:8000 |
| Guarnieri et al. $\qquad$ [33] | $\begin{gathered} \text { Architectural } \\ \text { PG } \\ \hline \end{gathered}$ | Total Station | PhotoModeler | 1:600 to 1:2700 |
| Tumbas et al. [34] | An Accuracy Study for AR's | Total Station | Fotogram, Plantran, TRANS4, and Others | 1:200 |
| Hanke [35] | $\begin{array}{\|c\|} \hline \text { A PM Accuracy } \\ \text { Study } \\ \hline \end{array}$ | Total Station | PhotoModeler | 1:1700 to 1:8000 |
| Jauregi et al. [36] | PGM of Bridge Deflection | Total Station | FotoG-FMS | 1:1700 to 1: 8000 |
| Pappa et al. [37] | PGM of Space Antennas | Not Given | PhotoModeler | 1:5000 to 1:28000 |
| Delorme et al. [38] | Medical PG | CT Scan | Self-Developed Software Using DLT | 1:86 to1:1200 |
| Fedak [39] | Industrial PG | Total Station | PhotoModeler | 1:6700 to 1:23000 |
| Townes \& Williamson [40] | An Accuracy Study for AR's | Total Station | PhotoWin 35 | 1:2400 |
| Brashington \& Smart [41] | PG in Geomorphology | Total Station | Imagine's OrthoMAX | 1:700 to 1:1750 |
| Lane et al. [42] | PG in Geomorphology | Total Station | Imagine's OrthoMAX | 1:800 |
| Pottler et al. [43] | PGM of Solar Concentrators | Not Given | Vision Measurement System (VMS) | 1:47000 |
| Wallace et al. [44] | PG in Aerospace | Not Given | Self Developed Software | 1:1350 |
| $\begin{gathered} \hline \text { Mills and Carty } \\ {[45]} \\ \hline \end{gathered}$ | PM in Vehicle Crush (TAR) | Total Station | PhotoModeler | 1:250 |
| KEY: TAR=Traffic Accident Reconstruction; AR's=Accident Reconstructionists; PG=Photogrammetry; PGM Photogrammetric Measurement; DLT=Direct Linear Transformation |  |  |  |  |

## Photogrammetry In Accident Reconstruction

The first use of photogrammetry for traffic accident reconstruction use, according to this Berling [32], was in 1932 by German police. Several sources maintain that photogrammetry was used for the first time in 1933 (or 1934, depending on which source one chooses) in Zurich Switzerland. Nonetheless, these first uses probably functioned with stereo-cameras and plotters; in other words, specialty machines would trace/draw maps sourced from two photographs of the accident scene. Graphical methods were prevalent in traffic accident reconstruction until the advent of the computer; as the PC became more available to the masses, analytical methods (using the mathematical/collinearity equations to make measurements) became practical and the norm. The fact is that the majority of the material is published after 1980-this directly corresponds to the increased use of computers. Table 3 outlines the history of photogrammetry in accident reconstruction. A sincere attempt was made to include all articles that could be acquired, but some articles were in different languages (prevalently in German \& Chinese); obviously, those sources could not be embraced.

## Table 3. History of Photogrammetry in Accident Reconstruction

| HISTORY OF PHOTOGRAMMETRY IN ACCIDENT RECONSTRUCTION |  |  |  |
| :---: | :---: | :---: | :---: |
| Date | Contributor | Contribution | Source |
| 1932 | Zeiss Works | German police suggested to the Zeiss firm to develop photogrammetric equipment for police use. The result was the DK 120. | [48] |
| $\begin{aligned} & \text { Either } \\ & 1933 \text { or } \\ & 1934 \end{aligned}$ | Zurich Switzerland Police | The first known instance where photogrammetry was used for accident reconstruction purposes; used stereo-cameras | $[49],[50]$, $[51],[52]$, $[53],[84]$ |
| 1935 | German Police Agencies | Close-Range Photogrammetry was adopted for police use | [53] |
| 1952 | Doris L. Rock | Used analytical photogrammetry (computed by hand) to determine the length of skid marks | 49] |
| 1954 | Bertil Hallert | Used stereo-photogrammetry to measure deformation in a model airplane wing | 54] |
| 1960 | D.I. Burnett | A summary paper which mentions that photogrammetry is used for "road traffic accidents" | 55] |
| 1963 | Robert N. Colwell | Photography is unfortunately not always recognized by all "as an unbiased source of truth" and hence photogrammetry and photo interpretation | 56] |
| 1964 | John N. Schernhorst | Various types of photogrammetry (single photo, stereo-photogrammetry, and x-ray photogrammetry) are available for accident/crime investigation | 50] |
| 1964 | James R. Salley | Advocates the use of stereo-photogrammetry in liew of measuring tapes or pacing for traffic accident investigation | 51] |
| 1967 | Iruma City, Japan Police | Obtained a specialty vehicle outfitted with stereo-cameras for "accident disposal" | 53] |
| 1970 | Dietrich W. Berling and Karl Zeiss | Describes photogrammetric equipment instruments used in collision investigation by German police and the importance of a "true to scale" survey of the accident scene | 48] |
| 1971 | Thomas M. Lillesand and James L. Clapp | Evaluated stereometric camera systems in traffic accident reconstruction. The authors "concluded that stereometric methods can significantly improve the collection, accuracy, preservation, and presentation of metric accident data" | 52] |
| 1974 | Clifford G. Bryner | A final report from a NHTSA grant which covers the use of a fabricated stereocamera system from consumer components in accident scene measurement, vehicle deformation measurement and anthropometric measurement | 57] |
| 1976 | Robert L. Bleyl | Employed a hand technique (rectification) to convert traffic accident scenes from a perspective view and converted it to a top-down view from which measurement could be made | 58] |
| 1976 | Joel Kobelin | Uses a truck outfitted with a stereometric camera system for the specific purpose of mapping traffic accident scenes in Florida | 59] |
| 1978 | William G. Hyzer | A quick manual photogrammetric method that employed perspective grids; limited use for flat surfaces only; buildings, streets, etc. | 60] |
| 1979 | A.O. Quinn | Advises the photogrammetrist on what to expect when testifying about his/her photogrammetric products in a court of law | 61] |
| 1980 | Robert M. Haralick | Informs the reader to the theory behind 2-D and 3-D perspective scene transformation and applies this transformation to an example | 62] |
| 1980 | A.W. Thebert | Utilizes a reverse-projection technique which consists of digitizing equipment and a computer algorithm that converts perspective pictures to a top-down map for making measurements of skid marks | [63] |
| 1980 | Sanjib K. Ghosh | Describes the use of close-range photogrammetry for traffic accident in Japan by police. Specialty vehicles with mounted stereo-cameras are used throughout Japan with much success | 53] |
| 1980 | Allan D. Howarth | A thesis that shows that a simple system consisting of non-metric cameras and perspective grid theory meets or exceeds conventional methods. This was accomplished through a review of literature, interviews of (police) personnel, and planned experimentation | 64] |
| 1981 | A. Lozzi \& J. Chapman | Uses a single stereo-photogrammetric technique to determine the displacements and velocities of dummies in a car-to-pole side impact | 65] |
| 1982 | J.P. Verriest | Uses cinephotogrammetry to get the dynamic deformation of the torsos of cadaveric specimens or animals (pigs); the experiment itself simulates conditions similar to a vehicle crash | 66] |

## Table 3. cont'd

| HISTORY OF PHOTOGRAMMETRY IN ACCIDENT RECONSTRUCTION |  |  |  |
| :---: | :---: | :---: | :---: |
| Date | Contributor | Contribution | Source |
| 1983 | Francois Mesqui \& Peter Niederer | Studied the head trajectories of pedestrian surrogates in a simulated vehiclepedestrian collision via cinephotogrammetry | [67] |
| 1984 | Peter Niederer \& Max Schlumpf | Cinephotogrammetry was used to study the impact of variable vehicle front geometry on the trajectories of pedestrian heads in a simulated accident | [68] |
| 1984 | P. Waldhausl \& H. Kager | Used a self-developed photogrammetric package called ORIENT to examine traffic accident scenes in Austria | [69] |
| 1985 | Haim B. Papo | Developed a proposed method for the analysis of deformations of engineering objects and structures using close-range photogrammetry | [70] |
| 1985 | W. Hoechtl | Stereo-photogrammetry was used at VW to measure the crush deformation of vehicles engaged in crash tests | [71] |
| 1985 | John F. Kerkhoff | Extracted information (measurements) from photos using graphical techniques that follow the principals of perspective | [72] |
| 1985 | Peter Niederer et al. | Used a single-view photogrammetric technique for accident scene documentation with the assistance of computers that helped with image analysis | [73] |
| 1985 | Steven L. Birge | Developed a system that exploited the geometry of perspective and created a specialized adapted theory for their own use for real-time highway documentation | [74] |
| 1986 | Larry Gillen | A report on forensic photogrammetry at the ASPRS-ACSM meeting. Various photogrammetric and legal topics are discussed | [75] |
| 1986 | Wilfried WesterEbbinhaus \& Ulrich <br> E. Wezel | Used a metric photogrammetric system, the Rolleiflex SLX, in the deformation analysis in the Porsche car crash tests. Talked about the benefits over a traditional measuring technique. | [76] |
| 1986 | Larry Gillen | Utilized stereo-photogrammetry to map deformations. A stereo-camera, surveyor's range poles, and a stereo-plotter are used in this technique | [77] |
| 1986 | Kevin C. Breen \& Carl E. Anderson | A paper that reports how photogrammetry was useful in a case study involving measurements of a windshield | [78] |
| 1986 | Wesley D. Grimes et. al. | A paper that shows that FOTOGRAM can be utilized for accident reconstruction purposes; illustrated with a single case. | [79] |
| 1986 | J. Rolly Kinney \& Bill Magedanz | TRANS4 is a photogrammetric program that will transform 4 points 9hence the name0 from a real surface to a photograph surface; illustrated with a single example | [80] |
| 1986 | Janet Brelin et al. | Discussed FotoGram, a 2-D photogrammetric software package. FotoGram was developed by GM for accident reconstruction purposes | 81] |
| 1986 | J. Stannard Baker | A topic in a manual for traffic accident investigators. Tells readers how to utilize graphical techniques for accident map reconstruction; mentions stereocameras and their associated plotters | [132] |
| 1988 | Gregory C. Smith | A dissertation in which a mathematical model for dealing with single-photo situations is presented. Self-developed computer programs are created to assist in this work. | [82] |
| 1988 | Jack Whitnall et al. | The authors utilize reverse camera projection to extract measurements for a 2 year old case in which the intersection of interest was completely repaved and revamped. | [83] |
| 1989 | Taichi Oshima \& Kiyoshi Oyamada | Summarized the current state of a country-wide implementation of specially outfitted photogrammetric vehicles for police use in Japan | [84] |
| 1989 | T.K. Коо | Developed a photogrammetric system that integrates a DLT analytical algorithm with a CAD program for accident mapping. The DLT algorithm is selfdeveloped. | 85] |
| 1989 | Michael D. Pepe et al. | Discussed the history and theory of photogrammetry. Several case studies in which photogrammetry was employed were mentioned also. | [8] |
| 1989 | Terry D. Day and Randall L. Hargens | An article which warns about the misapplication of computer programs in accident reconstruction. Photogrammetry is mentioned; says of 4 control points, 3 must not be in a straight line | [86] |
| 1989 | Gregory C. Smith \& Douglas Allsop | A review paper of single-image photogrammetric methods. A summary of dissertation; discusses his self-developed single-photo analytical method | [87] |

## Table 3. Cont'd

| HISTORY OF PHOTOGRAMMETRY IN ACCIDENT RECONSTRUCTION |  |  |  |
| :---: | :---: | :---: | :---: |
| Date | Contributor | Contribution | Source |
| 1990 | Robert Godding | VW used photogrammetry to evaluate a dummy's deformations and motion during crash tests | [88] |
| 1990 | Terry D. Day \& Randall L. Hargens | A section in a topic of a manual for traffic accident reconstruction. Illustrates graphical photogrammetry with an example of how to measure skids using a single photo. | [133] |
| 1991 | $\begin{aligned} & \text { T.K. Koo \& Y. B. } \\ & \text { Aw } \end{aligned}$ | A refinement of a previous technique where this technique allows shaded renderings of accident scenes. | [89] |
| 1991 | Masary Yeyama, et. al. | The authors studied various deformation patterns of vehicles from various start positions. Photogrammetry was used to measure the deformations (used a stereo-camera system) | [90] |
| 1991 | Albert V. Karvelis, et. al | The authors developed a Photogrammetry Vision System (PVS) to analyze the deformations in high speed crash tests | [91] |
| 1991 | Ronald L. Woolley, et al. | Vehicle crush is determined using the "Two-Image Camera Reverse-Projection Method"; this technique was compared to the results of a Total Station | [92] |
| 1992 | Andrew C. Henry | Photogrammetry and traditional survey techniques were used to generate a 3-D model of a hill on which an accident occurred | 93] |
| 1992 | W. Faig et. al. | A technique was developed for vehicle-damage investigation; employed the use of a non-metric stereo-camera and a slide projector-tablet digitizermicrocomputer combination | [94] |
| 1993 | Annette L. Rizer et. al. | VROOM (Visual Reconstruction of Object Motion), a specialized cinephotogrammetry program, was used to reconstruct the vehicle's kinematics from film or video in a large environment | [95] |
| 1993 | A.T. Campbell and Richard L. Friedrich | A CAD program was used to model items first of a known nature, and next unknown items. These scenes are matched in the CAD program and measurements are subsequently extracted | [96] |
| 1993 | Pepe, Michael E. et. Eva al. | Evaluation of the accuracy of 3-D photogrammetry by examining four situations: 1. planar 2. non-planar 3. non-planar compound 4. crush | [97] |
| 1994 | A. Kullgren, et. al. | Developed a photogrammetric system by which the exterior deformations of nearly 500 cases and 15 different car models have been examined. Time in the field and time to process photogrammetric measurements have been reduced greatly. | [98] |
| 1994 | A. Kullgren, et. al. | A more comprehensive version of the above study. Same study. Utilized nontechnical and technical personnel. Used 2 models for each vehicle: an exemplar and a crushed and then made measurements separately (I use a superimposed method) | [23] |
| 1994 | Nicholas S. Tumbas et. al. | One 2-D and six 3-D experiments were evaluated for accuracy. Non-metric and metric cameras were used as were different photogrammetric programs (FotoGram, Trans4, Plantran) | [34] |
| 1995 | Ron Rohde | Used Adobe Photoshop to transform images without the use of photogrammetry software. Once the images were transformed, they are suitable for measurement extraction | [99] |
| 1995 | A. Kullgren et al. | An entire fleet of one particular make and model of car was outfitted with lowcost accelerometers. The interiors of the cares were evaluated and linked to the injuries of the occupants. Photogrammetry helped them to "judge the interior contacts." | [100] |
| 1995 | Donald F. Rudny \& David W. Sallmann | An experiment not performed. An instruction-type paper that informs accident reconstructionists about the procedures on how to survey a scene with electronic survey equipment. Talks about how electronic survey can be important to photogrammetry in accident reconstruction situations | [101] |
| 1995 | Bruce W. Main and Eric A Knopf | A report on a new technique developed by the authors; an extension of the camera reverse projection technique (using model cars) was used to get the measurements needed | [102] |
| 1996 | Paul Duignan et. al. | A photogrammetric system at the Roads and Traffic Authority in N.S.Wales Australia examined 500 vehicles to date. A modification of the Lie [23] system was used | [103] |
| 1996 | Michael D. Pepe et. al. | Instead of rectifying a number of points (or line drawings) the authors rectified the entire image using DIREC, thereby supplying a great deal of more information as opposed to traditional methods | [104] |

## Table 3. Cont'd

HISTORY OF PHOTOGRAMMETRY IN ACCIDENT RECONSTRUCTION

| Date | Contributor | Contribution | Source |
| :---: | :---: | :---: | :---: |
| 1996 | Yih-Ping Huang et. al. | Two photos were used by the authors-one was supplied and one was "synthetic"-so that measurements could be extracted from the scene. A mathematical relationship relates the dimensions of the 2 photos. | [105] |
| 1996 | Fay \& Gardner | The authors use a pseudo-camera-reverse-projection technique to verify actual photos of a scene to the animation for accuracy. | 106] |
| 1997 | William E. Cliff et. al. | Compared to PC-Rect's (2-D) results to survey results. Only good for flat scenes. Typical scenes are rectified with in a $1 \%$ accuracy. | [107] |
| 1997 | Stephen Fenton \& Richard Kerr | A report of a newly developed technique. The authors generated an accident scene diagram using one "ole" and many "new" photographs. (The new photographs have features in common with the old photo.) | [108] |
| 1998 | A. E. Peterson et. al. | Developed a photogrammetric program called TRIPLET based on the collinearity equations to study velocity and acceleration at 2 particular intersections in Canada using video-taped footage. | [109] |
| 1998 | Harry W. Townes \& James R. <br> Williamson | Completed an accuracy study using an accident scene. Used ICE (Iteration of the Collinearity Equations) in this study. Uses single and multiple photos and two different focal lengths. | [110] |
| 1998 | David J. Massa \& Roger W. Barrette | The authors state that 3DD can assist in a computer-reverse projection photogrammetry analysis when mapping a vehicle | [111] |
| 1999 | Mohammed Obaidat | Used a system that integrated stereo-photogrammetry and GIS to collect and process traffic accident data. Outputs are 3-D coordinates and time. | [112] |
| 1999 | David A. Switzer \& Trevor M. Candrlic | The authors conducted a study to understand the specific variables affecting the accuracy of PhotoModeler, such as camera info known/unknown, fiducials present/not present, digitizing technique, image cropping, and number of control points | [25] |
| 1999 | Stephen Fenton et. al. | PhotoModeler was used by the authors to analyze a single vehicle's crush and to determine its EBS. PhotoModeler did the photogrammetry and EDCRASH determined the EBS. | [10] |
| 1999 | David J. Massa | A report of a technique in which accident scene information was located not from photographs (as in photogrammetry) but from animations or computergenerated images | 113] |
| 1999 | Walter Rentschler \& Volker Uffenkamp | The authors use photogrammetry to measure the deformation during Phorche crash tests. Claims there is a reduction of $50 \%$ in measuring costs verses traditional measuring techniques | [24] |
| 1999 | Bruno Esteve et. al. | Discussed the use of photogrammetry in the measurement of drivers' visibility fields using a fish-eye lens | 114] |
| 1999 | Ruldolf Limpert | A section in a traffic accident reconstruction manual. Informs readers to a couple of graphical photogrammetric methods: the linear method and the grid field method | 134] |
| 2000 | Lara L. O'Shields | A Master's Thesis that concerned the use of PhotoModeler in accident reconstruction; more specifically the measurement of a single vehicle deformation case compared against NHTSA crash test results and a single pre-measured accident scene. | [115] |
| 2000 | Stephen Fenton, et. al. | PhotoModeler was used to determine crash severity and assist in the study of occupant kinematics. Very close to their 1999 SAE paper. | [116] |
| 2000 | Scott A. Cooner \& Kevin N. Balke | A study that involved the determination of the feasibility of integrating photogrammetry into how Texas DOT and police agencies document crash scenes. Includes a survey of police agencies currently using photogrammetry. | [117] |
| 2000 | Zonghe Guo et. al. | Developed a video camera/self-developed software system to document traffic accidents in China. Presents the theory used \& calibration data, but results from a traffic accident are not presented | 118] |
| 2000 | Samuel R. Rod | An article in a magazine aimed at those who use imaging equipment. Contains basic information on photogrammetry used in crime scenes and accident reconstruction | [119] |
| 2001 | William G. Hyzer | A chapter out of an online forensic reference book. Would bemore aptly entitled "Forensic Photography" rather than "Forensic Photogrammetry." Lightly uses graphical and analytical photogrammetric methods. | [120] |

## Table 3. Cont'd

| HISTORY OF PHOTOGRAMMETRY IN ACCIDENT RECONSTRUCTION |  |  |  |
| :---: | :---: | :---: | :---: |
| Date | Contributor | Contribution | Source |
| 2001 | H. Becker et. al. | Created a new photogrammetric vehicle documentation system at VW. Vehicles' deformations are later examined for directional force estimation and for assistance in the accident reconstruction | [121] |
| 2001 | Stephen Fenton et. al. | In lieu of using a transparency to match the accident scene (the traditional camera-matching method), the computer software is used to match the scene. A case study was utilized where the results of the camera matching technique was compared against a surveyed scene with known dimensions | 122] |
| 2001 | Bryan C. Randles et. al. | PhotoModeler was used to aid in the verification/'validation of pedestrian throw equations at a particular intersection in Helsinki, Finland equipped with a video camera | 123] |
| 2001 | Carol H. Waters \& Scott A. Cooner | Suggested the use of photogrammetry to alleviate traffic jam situations due to traffic accidents. This alleviation might help in the prevention of road rage | 124] |
| 2001 | J. Stannar Baker et. al. | A chapter in a traffic investigation manual. Covers graphical techniques such as grids. Reverse camera projection and computer reverse projection are included. Discusses mathematical methods and computer programs | [135] |
| 2003 | Dirk Behring et. al. | Researchers at VW examine vehicle crash test deformation using photogrammetric software called TRITOP. Can measure up to 5000 points in less than two hours | 125] |
| 2004 | Lara L. O'Shields et. al. | Used PhotoModeler to examine NHTSA crash tests and verified the computed EBS value to the actual test speed. The variations were examined with bootstrapping. $45 \%$ of the variability is due to technique, $55 \%$ of variability is due to vehicle type | [126] |
| 2004 | William T.C. Neale, et. al. | The authors documented three different scenes/items with video, as opposed to using still photographs for photogrammetric purposes. Used a software program called Boujou 2.0. | 127] |
| 2005 | Robert V. <br> McClenathan et. al. | Applied "real-time" photogrammetry in crash tests to study dummy occupant motion and vehicle deformation. FalCon eXtra 4.05 was the software used in this study. | [128] |
| 2005 | Fiona Coyle et. al. | The authors compared PhotoModeler's results to tape measure and measuring jig/pipes in a single crush measurement experiment | 129] |
| 2005 | Angelo Toglia et. al. | Four types of projects were completed in this work: 1. single-photo calibrated/2. inverse camera and 3. multi-photo calibrated/4. inverse camera. Three accident scenes were analyzed under different conditions. Claimed to have presented new tools/methodologies in the application of PhotoModeler | 130] |
| 2005 | Raymond M. Brach \& R. Matthew Brach | Included a photogrammetry chapter in a traffic accident reconstruction text. Discusses reverse projection, planar (2-D) photogrammetry, and 3-D photogrammetry. Also photogrammetry in vehicle crush is mentioned | 15] |
| 2006 | Clifford C. Chou | Photogrammetry was used in a dynamic setting in a roll-over crash test using camera matching. Vehicle roll angle and rate were measured with photogrammetry and compared with vehicle sensors. Roll angles were in close agreement with the sensors; rate data was not. | 131] |

## Photogrammetry in Other Areas

It would be a great injustice to discuss photogrammetry by not
discussing the other areas beneficially affected by this great art and
science. There is a wide variety of the application of
photogrammetry. Table 4, Application of Photogrammetry in Other
Areas is by no means a comprehensive, all-inclusive list of
possibilities; it is simply a mere sampling of uses.

Table 4. Photogrammetry in Other Areas

| PHOTOG <br> Applicatio | RAMMETRY IN OTHER AREAS Description | Software | Source |
| :---: | :---: | :---: | :---: |
| Forensic | Compared bank video to actual suspect and found similarities in gait and other measures | PhotoModeler | [136] |
| Forensic | Introduced a preliminary study that attempts to make identification of persons from surveillance cameras using photogrammetry | PhotoModeler | [137] |
| Forensic | Photogrammetry assisted in the matching of a muzzle of a gun to wounds on a person's face | RolleiMetric | [138] |
| Forensic | A soft-tissue injury to the face was matched to tire tracks using photogrammetry | RolleiMetric | 139] |
| Architectural | Used PhotoModeler to help document and conserve Brazil's historic towns and urban areas | PhotoModeler | 140] |
| Architectural | Mounted a camera on a RC helicopter; took video of various national treasures; extracted stills from video; used PhotoModeler to create 3-D of national treasure | PhotoModeler | [141] |
| Architectural | A tutorial on the theory, procedures, and tools for architectural documentation via photogrammetry | PhotoModeler | [142] |
| Engineering | Photogrammetry was used to measure the amount of deformation of the wings of wind-tunnel models to help compute aerodynamic force | Self-developed | 143] |
| Engineering | PhotoModeler was used to model an automotive exhaust system and body. | PhotoModeler | 144] |
| Engineering | Iowa DOT used photogrammetry with low-flight helicopter photography for mapping in highway engineering. | SoftPlotter | [145] |
| Engineering | PhotoModeler helped to study acoustical phenomena of bells. A bell sounds differently while it is being struck and shortly after being struck. | PhotoModeler | 146] |
| Engineering | Used PhotoModeler, video cameras, lasers, and filters to study the dynamic properties in solar sails which are clear or aluminum | PhotoModeler | 147] |
| Engineering Education | Outlines a lab exercise for undergraduate mechanical engineering students. Used PhotoModeler Lite to model and measure some arbitrary part | PhotoModeler Lite | 148] |
| Biological | PhotoModeler was used to measure the surface area of corals and other irregular objects utilizing underwater photography | PhotoModeler | 149] |

## Relevance of This Work

There are a host of advantages for using photogrammetry in traffic accident reconstruction. The preceding sections maintain that photogrammetry is accurate and widely used in accident reconstruction (AR), but why? The following is a list of reasons (in no particular order) which make photogrammetry beneficial for the AR field:

- Cost: PhotoModeler, in comparison with other photogrammetry packages, is very affordable. PhotoModeler 6.0 sells for around $\$ 1000$ USD. Some photogrammetry packages mentioned previously costs $\$ 100,000+$. PhotoModeler requires no specialized equipment-just a computer and a consumer-grade camera of your choice.
- Efficiency: Using photogrammetry results in less time in the field. The photos can be taken of the object of interest (a car, or an accident scene) and the much needed measurements can be obtained at a later time at the office. Also it has been written that photogrammetry may help alleviate traffic jam
situations which could help prevent further delays (and further accidents, see below) since it is quicker than total stations [117, 124].
- Safety: Photogrammetry is a safer alternative to using conventional measurement techniques because it is generally quicker. This is because personnel are not placed in harm's way (in the path of traffic) for as long when documenting accident scenes using photogrammetry [117, 124].
- Accuracy: The previous section attests to photogrammetry's accuracy. Its accuracy is in excess of what is required for most accident reconstruction applications. Speed estimates from skids and the CRASH3 algorithm require much less that what photogrammetry is capable of doing.
- Timeless application: Photogrammetry can be used at the time of the accident or even years later. Sometimes the accident reconstructionist is given photos of a vehicle that was crushed many years earlier. Perhaps that vehicle, in its crushed state, is not available for inspection because it was scraped, repaired, or even destroyed. Photogrammetry can determine
the amount of crush (and hence, a proper delta-v) for that vehicle even if it doesn't exist anymore. In this sense, photogrammetry is timeless; it doesn't care if the car was crushed two years ago even two days ago-it still can do the job. The same can go for accident scenes. Many times the scene has been "revamped" either by repaving or reconfiguration. It is possible for photogrammetry to extract needed measurements from the scene photos just as long as some components remain the same-like road signs, guard rails, manhole covers, and other prominent landmarks.


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## PART ONE VEHICLE CRUSH MEASUREMENT

Part One is lightly revised version of a paper published at the 2004 SAE World Congress in Detroit by Lara L. O'Shields, Tyler A. Kress, John C. Hungerford, and C.H. Aikens:

O'Shields, Lara L. et. al. "Determination and Verification of Equivalent Barrier Speeds (EBS) Using PhotoModeler as a Measurement Tool" SAE Paper 2004-01-1208, SAE International, Warrendale, PA, 2004. (126)

The content of this publication was an extension of O'Shields' Master of Science Thesis work. The Master's work and the PhD's work are similar in that they both used NHTSA's controlled crash data, however; they are dissimilar in the fact that this work analyzed twenty-one (21) different NHTSA vehicles as opposed to only one (1) vehicle in the Master's work. Kress gave O'Shields the idea of using NHTSA crash data back in 1998. Kress also helped with document edits. Hungerford provided the use of the PhotoModeler software and Aikens assisted with the statistical analysis portion of this work. Photogrammetry, spreadsheet development, bootstrapping, and document development were all done by O'Shields.

## Abstract

This study focused on the role of PhotoModeler, a close-range photogrammetry software package, in an important facet of traffic accident reconstruction-vehicle crush measurement. More specifically, this study applied the PhotoModeler process to controlled crash information generated by the National Highway Traffic Safety Administration (NHTSA). A statistical technique known as
bootstrapping was utilized to generate distributions from which the variability was examined. The "within" subject analysis showed that $44.8 \%$ of the variability is due to the technique itself and the "between" subjects analysis demonstrated that 55.2\% of the variability is attributable to vehicle type-roughly half and half. Additionally, a 95\% CI for the "within" analysis revealed that the mean difference (between this study and NHTSA) fell between -2.52 mph and +2.73 mph ; the "between" analysis showed a mean difference between -3.26 mph and +2.41 mph .

## Introduction

In the accident reconstruction community, it has been known for thirty years or more that vehicle crush can be used to determine the equivalent barrier speed (EBS). Emori [150] and Campbell [1] each showed that the relationship between crush and speed is linear in nature. Additionally, Campbell [1] related vehicle crush and the vehicle's stiffness characteristics to the amount of energy absorbed; this energy can be subsequently used to compute the EBS.

Campbell's work is the foundation for the equations and software
used by accident reconstructionists to determine crush energy and, consequently, the EBS.

In order to get the energy from crush, the crush must first be measured. There are a variety of techniques available: tape measures, measuring poles, grids, and photogrammetry. The major problem with the first three techniques is that one is measuring against a "phantom" pre-impact boundary. The post-impact vehicle position/shape is located easily enough, but not the pre-impact vehicle boundary position/shape. With these two techniques, locating the front of the vehicle prior to frontal impact could be described as an educated guess at best. But with photogrammetry, the locations of the pre- and post-impact components are both known. The technique is one where 3-D models are created of both the crushed and the exemplar vehicles. The models of the two vehicles are "superimposed" on top of one another. Crush measurements can then be established from the pre- and post-impact points of the 3-D model. An energy calculation can then be made using vehicle stiffness data and the pre-impact speed can be determined via a correlation.

The main objective of this study was to show that
PhotoModeler is a suitable measurement tool for vehicle crush measurement. This was accomplished by applying PhotoModeler plus crush equations to NHTSA controlled crash data. The consistency of the studies' results with the nominal 35 mph is the indicator of acceptability of the technique.

Two statistical analyses were performed: (1) the "within" subject design and (2) the "between" subject design. The first involved measuring the same vehicle twenty different times. This gave us a good idea of the repeatability of the experiment. The second involved measuring various types of vehicle categories (such as SUV's, Pickup Trucks, Luxury Cars, Mid-Size Cars) to examine the variability between vehicle classes.

The NHTSA photographs needed for this study's analysis are problematic to use for this work because of their poor quality and limited quantity. Therefore, this effort could not support a large sample size needed for most statistical analysis. As will be discussed later, a "bootstrapping" technique allowed statistical analyses to determine variance. In effect, there were two experiments (the
"within" and the "between") and they each had their own associated bootstrapping analysis to determine each variance.

## Selection of Samples

As mentioned previously, photographs from NHTSA reports
were used. The specific sample that was used in the "within" subjects
design was of a 1998 Ford Contour (NHTSA test \# 2708). The
specific samples that were used in the "between" subjects design are
delineated in Table 1 below.

Table 1. Vehicles Used in the "Between" Subjects Design

| Case | Category | Vehicle | NHTSA Test \#: |
| :--- | :--- | :--- | :--- |
| 1 | Large Luxury Cars | 2002 Cadillac DeVille | 4238 |
| 2 | Midsize Luxury Cars | 2003 Mercedes E320 | 4483 |
| 3 | Large Family Cars | 2001 Buick LeSabre | 3520 |
| 4 | Midsize Moderately Priced | 2003 Toyota Avalon | 4486 |
| 5 | Midsize Moderately Priced | 2002 Audi A4 | 3566 |
| 6 | Midsize Inexpensive | 2003 Hyundai Accent | 4473 |
| 7 | Midsize Inexpensive | 2001 Chevy Malibu | 3666 |
| 8 | Convertibles | 2003 Honda S2000 | 4462 |
| 9 | Small Cars | 2002 Mini Cooper | 4273 |
| 10 | Small Cars | 2003 Toyota Corolla | 4266 |
| 11 | Utility Vehicles | 2002 Chrysler PT Cruiser | 4230 |
| 12 | Midsized Utility Vehicles | 2002 Ford Explorer Sport | 4223 |
| 13 | Midsized Utility Vehicles | 2002 Nissan Pathfinder | 4263 |
| 14 | Small Utility Vehicles | 2002 Toyota Highlander | 4265 |
| 15 | Small Utility Vehicles | 2003 Subaru Forrester | 4479 |
| 16 | Large Pickups | 2002 Dodge Ram 1500 | 4240 |
| 17 | Large Pickups | 2001 Nissan Frontier | 3574 |
| 18 | Large Pickups | 2003 Chevy Silverado | 4472 |
| 19 | Passenger Vans | 2001 Dodge Wagon Van | 3639 |
| 20 | Passenger Vans | 2001 Dodge Caravan | 3659 |

Note that these samples were selected as having sufficient quality photographs.

## PhotoModeler Procedure

## Description of the Software

PhotoModeler is a photogrammetry software package presented by EOS Systems in Vancouver, British Columbia. The specific version of PhotoModeler used in this study was version 4.0 g . PhotoModeler can be used for a multitude of different measuring applications, including plant engineering, forensics, anthropology, and of course, traffic accident reconstruction. Interested readers can visit http://www.photomodeler.com for purchasing and additional information. PhotoModeler is capable of handling 2-D AR projects like accident scene measurement, and 3-D projects such as vehicle crush measurement.

## Description of a Generic PhotoModeler Procedure

The first step of a new PhotoModeler project involves taking pictures of the object or scene of interest. A new project is then created using the software's Project Setup Wizard; this is where the
user enters fundamental information such as location of the digitized photos, approximate size of the object, and camera information.

After that, the user marks features with a mouse on each photograph using the various tools available. Next the project is processed and PhotoModeler creates a 3-D model from the 2-D photographs. The user then gives the project dimension by scaling it. At this point, the user can extract the desired measurements from the marked features.

## Camera Calibration

For use in this study, a digital Olympus C-5050 was calibrated using the embedded Camera Calibrator program in PhotoModeler. Camera calibration ensures an accurate measuring device. This particular camera was chosen because of its (relatively high at the time of the study) resolution (5.0 Mega pixels), its use of ordinary rechargeable AA batteries (the author has several sets of AA batteries on hand when performing photogrammetry work) and its ability to hold two (2) digital storage cards (an xD and a Compact Flash). The process involved taking eight (8) pictures of a special grid which was
projected onto a wall. On the following page, this is illustrated with
Figure 1, which is a screenshot (a depiction of what one might see on the computer screen) of the procedure. The calibration procedure is well documented in O'Shields [115] and in Appendix 1 and 13. After points were marked and processed with the Camera Calibrator software, camera information such as focal length, format size, and principal point was determined as a result. Figure 2 shows the C5050's resultant camera information.


Figure 1. Camera Calibration Grid


## Figure 2. Result of the Olympus C-5050 Calibration Procedure

## Exemplar Modeling

Note: A more involved and more detailed description of vehicle modeling can be found in O'Shields [115]; the following is a suitable but succinct version of the vehicle modeling process. The first step in the crush measurement project was to determine the year, make, and model of the subject or crushed vehicle and then locate an exemplar of that particular vehicle model at a local dealership.

Several pictures from a variety of angles were then taken of the exemplar with the calibrated camera. In order for

PhotoModeler to create an accurate 3-D model, every point must reside in at least two (2) photographs, preferably three (3.) The user's picture taking technique needs to reflect this requirement, hence; the pictures must overlap. Figure 3 helps to demonstrate this point. For instance, a single point like Point \# 8 (which is a point on the front badge of the vehicle) must reside in three (3) different photographs (Photo 1, Photo 2, Photo 3). The camera positions were typically at the four sides and at the four corners of the vehicle, which allowed for good overlap. For scaling purposes, at least one physical measurement must be made on the exemplar. This particular measurement can be between any two distinct points on the vehicle. Normally, the length along the bottom edge of a (front) door or the wheelbase was selected for the sake of simplicity. The photos themselves were downloaded from the camera to the computer via USB cable and stored in a folder marked "Exemplar Malibu" (or whatever the vehicle model may be) on the computer's desktop for easy retrieval.

Using PhotoModeler's "Project Setup Wizard", two or three photos at a time were opened up and distinct points on the vehicle were marked and referenced on all photos. "Marking a point" entails selecting the point tool which looks like a single " $x$ " on the toolbar. The user would then mark a distinct point on the first photograph, such as point \# 8 which is the edge of one of the stars on the Subaru badge. "Referencing a point" required the use of the referencing tool on the toolbar which resembles a double "x." Referencing "notifies" PhotoModeler of Point \# 8's location on the other photos (Photos \# 2 and \# 3), i.e., this allows PhotoModeler to recognize that this is the same physical point in space. This procedure of marking and referencing continued until the entire exemplar was modeled. After processing and scaling, the exemplar model was exported into a .dxf format for the control point file. This step was completed in PhotoModeler under the File menu.

## Crushed Vehicle Modeling

The first task in this portion of the study was to obtain pictures of the crushed vehicles. The user could download the pictures, print them
out, and digitize them via flatbed scanner, or, download and save the pictures directly. This was the procedure utilized in this study, with the exception of the vehicle examined in the "within" subjects design (a 1998 Ford Contour). In this instance, the authors had the NHTSA report already in their possession and the photos were digitized with the scanner. The NHTSA website to visit to obtain the crash test photos is http://www-nrd.nhtsa.dot.gov/database/nrd$11 /$ veh_db.html. The digitized photos were then opened into the exemplar project (saved under another name) and the .dxf control point file was opened. Control points were marked on undamaged portions of the crushed vehicle and referenced across the exemplar.

After processing, points on the damaged portion of the crushed vehicle were marked and referenced. The project was processed one final time. Reference lines were established and measurements were extracted. Figure 3, a screenshot of the 2003 Subaru Forester utilized in the study, shows exemplar and crushed photos, as well as a 3-D viewer. The 3-D viewer reveals the 3-D model created in the study; the exemplar is shown with white lines, while the crushed vehicle is indicated by blue points. One can easily see how much crush can be


Figure 3. Screenshot of 2003 Subaru Forester
realized in each vehicle. Unfortunately, there were no screenshots generated from the "within" subjects study. Appendix 2 contains all 20 screenshots generated from the "between" subjects study.

## EBS Determination

This study utilized equations put forth in Traffic Accident Reconstruction by Cooper [153]. The equations themselves are the

CRASH3 model equations which are based on Campbell's work; this is how this study determined EBS (Equivalent Barrier Speed) and is the authors' preferred method. In using this relationship, vehicle weight, width of crush, and crush coefficients are required input and must be known prior to the calculation of EBS. The first two can be determined easily; the last can be approximated or purchased.

## Crush Coefficient Determination

This study made use of the CRASH3 equations for crush coefficients. They are:

$$
\begin{aligned}
& \begin{array}{l}
A=\frac{w b_{0} b_{1}}{g L} \\
\quad B=\frac{w b_{1}^{2}}{g L} \\
b_{1}=\frac{\left(v_{\mathrm{i}}-b_{0}\right)}{C_{\text {ave }}} \\
\text { where }
\end{array} \\
& \mathrm{w}=\text { weight of test vehicle (lbs.) } \\
& \mathrm{b}_{0}=\text { maximum impact speed without damage (mph) } \\
& \mathrm{b}_{1}=\text { slope (rate at which permanent deformation occurs)(mph/in) } \\
& \mathrm{v}_{\mathrm{i}}=\text { velocity of crash test vehicle } \\
& \mathrm{g}=\text { gravitational constant (in/sec }{ }^{2} \text { ) } \\
& \mathrm{L}=\text { width of crush region on test vehicle (in) } \\
& \mathrm{c}_{\text {ave }}=\text { average crush depth of test vehicle }
\end{aligned}
$$

Figure 4 shows a typical spreadsheet used in crush coefficient determination. This particular example is of a 2003 Mercedes E320. The needed crash test data was taken directly from the NHTSA website which was given previously. Note that the crash test data is in metric units; this is specified on the right portion of the page. These dimensions were subsequently converted to English units, which are shown on the left portion of the page. Crush coefficients A

| Crash Test <br> Information |  |
| :--- | :--- |

Impact velocity of test:
Maximum speed w/o permanent damage: (b0)

Crush measurements from crash test report:

Average crush amount
Test vehicle weight

Width of crush damage

35.20071 mph

5 mph

| 15.31496 | in (c1) | 389 | $\mathrm{~mm} \mathrm{(c1)}$ |
| :--- | :--- | :--- | :--- |
| 19.88189 | in (c2) | 505 | $\mathrm{~mm} \mathrm{(c2)}$ |
| 22.83465 | in (c3) | 580 | $\mathrm{~mm} \mathrm{(c3)}$ |
| 22.67717 | in (c4) | 576 | $\mathrm{~mm} \mathrm{(c4)}$ |
| 19.76378 | in (c5) | 502 | $\mathrm{~mm} \mathrm{(c5)}$ |
| 13.97638 | in (c6) | 355 | $\mathrm{~mm} \mathrm{(c6)}$ |

19.0748 in
4265.945 lbs
71.34646 in

1935 kg

1990 mm
b1 $1.583277 \mathrm{mph} / \mathrm{in}$

A $\quad 362.6139 \mathrm{lb} / \mathrm{in}$
B $\quad 109.7281 \mathrm{lb} / \mathrm{in}^{\wedge} 2$

Figure 4. Crush Coefficient Determination
and $B$ were easily computed with the above formulas, information from the website, and the spreadsheet. The initial value of $A$ and $B$ in Figure 4 was determined with a $\mathrm{b}_{0}=5 \mathrm{mph}$. Appendix 3 contains all initial crush coefficient spreadsheet information. Additionally, a sensitivity analysis for the crush coefficients was established. This involved using various values of $b_{0}$, which in turn, generated different crush coefficients. This can be seen in Figure 5. The $b_{0}$ values were


Figure 5. Crush Coefficient Sensitivity Analysis
approximately centered around 5 mph , ranging from 4 mph to 6.25
mph. Then the average $A$ and $B$ were computed, which is indicated by the center of the figure. These average crush coefficients were the final values used in EBS computations. Appx. 4 contains all spreadsheets for the sensitivity analysis performed. Appx. 9 contains the crush coefficients (purchased from Neptune Engineering) for the 1998 Ford Contour which was used in the "within" study. These coefficients were used in the Thesis work also [115].

## Computing EBS

The EBS equations used in the study were:

$$
E=\frac{W}{5}\left[\begin{array}{l}
5 G+ \\
\frac{A}{2}\left(C_{1}+2 C_{2}+2 C_{3}+2 C_{4}+2 C_{5}+C_{6}\right)+ \\
\frac{B}{6}\left(C_{1}^{2}+2 C_{2}^{2}+2 C_{3}^{2}+2 C_{4}^{2}+2 C_{5}^{2}+C_{6}^{2}+C_{1} C_{2}+C_{2} C_{3}+C_{3} C_{4}+C_{4} C_{4}+C_{5} C_{6}\right)
\end{array}\right]\left(1+\tan ^{2} \theta\right)
$$

which computes the amount of energy dissipated by crush damage,
where $E=$ the amount of energy dissipated (in-lbs)
$\mathrm{W}=$ the width of the crushed region (in)
$\mathrm{G}=$ the "energy" dissipated before permanent deformation occurs (lbs) $\mathrm{G}=\frac{\mathrm{A}^{2}}{2 B}$
$A=$ crush coeffiecient A ; the maximum force per inch of damage which will not cause permanent damage ( $\mathrm{lb} / \mathrm{in}$ )
$B=$ crush coeffiecient $B$; the spring stiffness per inch of damage width $\left(\mathrm{lb} / \mathrm{in}^{2}\right)$
$\mathrm{C}_{1} \rightarrow \mathrm{C}_{6}=$ the crush measurements obtained by PhotoModeler (in)
$\theta=$ the angle of the force to the vehicle's surface (degrees)
and
$E B S=v=\sqrt{\frac{2 g E}{w}}$
which computes the velocity (EBS) of the vehicle, where
$\mathrm{v}=$ the velocity of the vehicle $(\mathrm{ft} / \mathrm{sec})$
$\mathrm{g}=$ the gravitational constant ( $\mathrm{ft} / \mathrm{sec}^{2}$ )
$\mathrm{E}=$ the amount of energy dissipated by the crush (ft-lbs)
$\mathrm{w}=$ the weight of the vehicle (lbs)
The EBS calculations for each case examined in this study were computed using spreadsheets and can be found in Appendices 5 \& 6 .

Appendix 5 contains the "within" subject spreadsheets, and Appendix 6 the "between" spreadsheets. PhotoModeler provided the width of crush and c1 through c6 measurements for these spreadsheets.

## Bootstrapping

As mentioned previously, the photographs needed for this study are limited in number due to their poor quality. The authors had quite a dilemma finding twenty (20) sets of photographs suitable for use with PhotoModeler. Since good photographs were limited in number, it was essential to find a statistical technique which focused on small samples. There are a variety of small sample techniques
available to researchers. They include, but are not limited to, Bootstrapping, Jackknife, and Cross-Validation. These techniques, which are very computer intensive, fall under the umbrella of Resampling Techniques. Bootstrapping is the most popular of the three, and it is the preferred technique of this study.

The Bootstrapping procedure is quite simple. Figure 6 and these bullets will help illustrate:

- Part A: Start out with an original data set, of say 20 points.
- Part B: The computer algorithm will make a copy of each point, say a billion times
- Part C: All copies are placed in a "bin" and are thoroughly shuffled
- Part D: From this conglomerate, bootstrap samples are extracted.
- Statistical inferences (like variance) are made on the bootstrapped samples

The bootstrapping software utilized in this study was "Resampling Stats for Excel 2.0", which is an add-in module to Microsoft Excel [151]. For this portion of the work, each set of "seed" data for the


Figure 6. Explanation of Bootstrapping Procedure
"within" and "between" subjects design was entered in an Excel worksheet (these "seed" data sets are precisely the differences found in Tables 2 and 3.) Then resampling with replacement was selected (resampling with replacement is Bootstrapping; resampling without replacement is known as the Jackknife procedure.) 100 independent samples of the twenty data points were subsequently generated along with their associated mean and variances. Appendix 7 contains "within" bootstrap data; Appendix 8 contains the "between" bootstrap data. At the end of each of these appendices, a grand total mean and variance of the 100 samples were computed for both studies. These numbers gave rise to the statistical analysis from which the statistics of the complete study were examined.

## Results

## Within Subjects Design

The test vehicle's reported velocity for this segment was 34.98 mph
(NHTSA test \# 2708). Table 2 shows the twenty replications of the
"within" subjects' estimated EBS values and their differences from the actual test velocity (units are in mph).

## Between Subjects Design

Table 3 summarizes the study's between subjects EBS estimates, their actual test velocities, and differences (units are in mph).

Table 2. Results of the "Within" Subjects Design

| Replication <br> $\#:$ | EBS Using PhotoModeler's <br> Results | Difference |
| :---: | :---: | :---: |
| 1 | 33.75 | -1.23 |
| 2 | 33.34 | -1.64 |
| 3 | 34.63 | -0.35 |
| 4 | 35.50 | 0.52 |
| 5 | 34.42 | -0.56 |
| 6 | 35.17 | 0.19 |
| 7 | 33.95 | -1.03 |
| 8 | 34.24 | -0.74 |
| 9 | 33.74 | -1.24 |
| 10 | 34.60 | -0.38 |
| 11 | 34.79 | -0.19 |
| 12 | 33.98 | -1.00 |
| 13 | 35.46 | 0.48 |
| 14 | 34.82 | -0.16 |
| 15 | 34.78 | -0.20 |
| 16 | 38.55 | 3.57 |
| 17 | 36.55 | 1.57 |
| 18 | 37.43 | 2.45 |
| 19 | 35.21 | 0.23 |
| 20 | 36.86 | 1.88 |

Table 3. Results of the "Between" Subjects Design

| Case \#: | EBS Using PM's <br> Results | Actual Test <br> Velocity | Difference | NHTSA <br> Test \#: |
| :---: | :---: | :---: | :---: | :---: |
| 1 | 33.55 | 35.30 | -1.75 | 4238 |
| 2 | 32.70 | 35.20 | -2.50 | 4483 |
| 3 | 35.20 | 35.10 | 0.01 | 3520 |
| 4 | 32.71 | 35.20 | -2.49 | 4486 |
| 5 | 34.21 | 35.00 | -0.79 | 3566 |
| 6 | 33.37 | 34.70 | -1.33 | 4473 |
| 7 | 35.87 | 34.52 | 1.35 | 3666 |
| 8 | 34.20 | 35.40 | -1.20 | 4462 |
| 9 | 36.46 | 34.90 | 1.56 | 4273 |
| 10 | 33.27 | 34.74 | -1.47 | 4266 |
| 11 | 32.43 | 35.00 | -2.57 | 4230 |
| 12 | 35.77 | 34.56 | 1.21 | 4223 |
| 13 | 35.97 | 34.90 | 1.07 | 4263 |
| 14 | 33.24 | 34.68 | -1.44 | 4265 |
| 15 | 34.36 | 35.40 | -1.04 | 4479 |
| 16 | 35.54 | 35.10 | 0.44 | 4240 |
| 17 | 34.14 | 34.89 | -0.75 | 3574 |
| 18 | 36.66 | 34.73 | 1.93 | 4472 |
| 19 | 35.44 | 34.71 | 0.73 | 3639 |
| 20 | 34.95 | 34.55 | 0.40 | 3659 |

## Bootstrapping

Complete bootstrapping results can be found in Appendix 7 \&
8. The computed variances from the bootstrapped samples are given below:
$\sigma_{W}^{2}=1.64$ the "within" variance
$\sigma_{B}^{2}=2.02$ the "between" variance, and
$\sigma_{T}^{2}=\sigma_{W}^{2}+\sigma_{B}^{2}=3.66$ the total variance

## Conclusion

To get an idea of the repeatability of PhotoModeler as a measurement tool, one needs to look at the proportion of the within variance to the total variance, or $\frac{\sigma_{w}^{2}}{\sigma_{T}^{2}}$. The other proportion, $\frac{\sigma_{B}^{2}}{\sigma_{T}^{2}}$,
indicates the variability due to vehicle type. The actual computation of the proportions is as follows:

$$
\frac{\sigma_{W}^{2}}{\sigma_{T}^{2}}=\frac{1.64}{3.66}=44.8 \% \quad \text { and } \quad \frac{\sigma_{B}^{2}}{\sigma_{T}^{2}}=\frac{2.02}{3.66}=55.2 \%
$$

The first proportion indicates the source of $44.8 \%$ of the variability is the technique itself, while the second proportion indicates that 55.2\% of the variability is attributable to vehicle type-so the variation on the whole is split half and half.

Additionally, a 95\% confidence interval for the within subjects design is given by:
$\bar{x} \pm 1.96 \cdot s d$
$0.11 \pm 1.96 \cdot 1.34$
(-2.52, 2.73)

A 95\% confidence interval for the between subjects design is given by:
$\bar{x} \pm 1.96 \bullet$ sd
$-0.43 \pm 1.96 \cdot 1.45$
(-3.26, 2.41)
One could interpret the "within" CI with the following statement:
"There is a .95 probability that the mean difference wil fall between 2.52 mph and 2.73 mph ." In other words a discrepancy of anywhere between 2.5 mph below the actual speed and 2.73 mph above the actual speed could be realized. This is a 5.25 mph range. Conversely, one could interpret the "between" CI with the following: "There is a .95 probability that the mean difference will fall between -3.26 mph and 2.41 mph ." In other words, a discrepancy of anywhere between 3.26 mph below and 2.4 mph above the actual speed could be realized. This is a 5.67 mph range.

## Future Directions / Research

- An extension of this work could include utilizing NHTSA photos which show the location of CMM measurement points. Sometimes photos will have distinct " $x$ " marks across the front bumper or some similar point indicators. That way PhotoModeler could be compared directly against the CMM
measurement data. Figure 7 illustrates these marks. The significance of the "L" and "R" are unknown. This idea was taken from the reviewers' comments which are in Appendix 10.
- Since publication of 2004-01-1208 (126), more NHTSA controlled crash data has been conducted. A PhotoModeler analysis could be performed on these new cases as well, and possibly a larger sample could result and more traditional statistical techniques such as Paired Comparisons could be


Figure 7. CMM Measurement Marks
employed (in lieu of Bootstrapping).

- Also since the publication of 2004-01-1208, the author has run across a better method of crush coefficient estimation. The procedure is outlined in Chapter 8 of Brach and Brach's Vehicle Accident Analysis and Reconstruction [15]. Chapter 8 in this book is entitled "Crush Energy and $\Delta \mathrm{V}$ " and the particular area of concern is based on Prasad [152]. The following equation is the basis for this method:
$\sqrt{\frac{2 E_{C}}{w}+d_{o}+d_{1} c}$
where
$E_{C}$ is the crush energy
$w$ is the width of crush
$d_{0}$ and $d_{1}$ are the stiffness coefficients
After one computes $\mathrm{d}_{0}$ and $\mathrm{d}_{1}$, the "traditional" crush coefficients A and $B$ can be computed using the following relationship:
$d_{1}=\sqrt{B}$
$d_{0}=\frac{A}{\sqrt{B}}$

Figure 8 is one of the author's spreadsheets using this new method.


Figure 8. Spreadsheet of New Crush Coefficient Method

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## PART TWO

## PHOTOGRAMMETRIC CURVE MEASUREMENT


#### Abstract

This study focused on the role of PhotoModeler, a close-range photogrammetry software package, in an important facet of traffic accident reconstruction-road curve measurement. More specifically, this study applied photogrammetry to (simulated) road curves in lieu of traditional measurement methods, such as measuring tapes and measuring wheels. In this particular work, thirty (30) different radii of curvature of various known sizes were deliberately constructed. Then photogrammetry was used to measure each of the constructed curves. A comparison of the known "R's" (control group) and photogrammetry's value of "R" (treatment group) was then made. Matched Pairs or Paired Comparisons was then used to examine these two populations.

The difference between photogrammetry's " R " and the known " R " range is between $0.001 \%$ and $0.845 \%$. Additionally, we are $99 \%$ confident that the mean difference of the two techniques is between -0.48 and 0.66 feet. Since this interval contains zero, we can conclude that the two techniques do not differ.


## Introduction

For many years, accident reconstructionists have used the Critical Speed Formula to determine the speed at which vehicles begin to sideslip around a curve. This formula in one of its simplest forms, $v=\sqrt{g r} \mu$, requires a value for $r$, or the radius of the path of the vehicle's center of gravity. "R's" use in this equation can manifest in one of two ways: (1) in yaw mark applications and (2) in road curve applications. For the first case, the radii of yaw marks and the Critical Speed Formula have been studied extensively [154164] and will not be discussed here. References 8, 9, and 10 make mention of case two, road curve applications, and provide an estimate for " $r$ " through the following formulas:

$$
r=\frac{l^{2}}{8 h}+\frac{h}{2} \quad \text { or, } \quad R=\frac{C^{2}}{8 M}+\frac{M}{2}
$$

where $r(R)=$ radius, $I(C)=$ chord, and $h(M)=$ middle ordinate. These equations will be discussed in detail later. Additionally, the authors of these references (161, 162, and 163) make suggestions on how to measure I (or C) and h (or M ) with tape measures.

The main goal of this study is to show that the measurement of I and h can be accomplished with photogrammetry. Photogrammetry is the science and art of making measurements with photographs, and to date, has not been used in this capacity.

A technique called Matched Pairs was used for the statistical analysis. As mentioned before, thirty (30) known radii were assembled. Each known "r" was "paired up" with photogrammetry's outcome for " $r$ ". The consistency of this study's results to the known results is an indicator of the acceptability of the technique.

## Selection Of Samples

The sizes of the thirty (30) known radii were intentionally chosen to represent driving situations most anyone would encounter. It was decided that radii between 50 and 500 feet would be satisfactory in terms of approximating real-world situations and from a construction feasibility standpoint. The random number generator in Excel was used to create thirty random numbers between 50 and 500, which is shown in the first column of Table 1. The second
column is an ordered version of column 1. This column was helpful in marking off the various distances on the cable that was used to construct the radii; this will be discussed later in the paper. Lastly, column three shows the Critical Speed for the sorted radii and using a coefficient of friction of 0.7 . One can see that speeds between 23 and 72 run the gamut of driving situations.

Table 1. Radii Selected for Use in This Study

| Random Radit between 75 and 500 feet | Random Radf Sorted | Critical Speed (using sorted radif and $\mu=0.7$ ) |
| :---: | :---: | :---: |
| 141 | 50 | 22.89 |
| 80 | 62 | 25.49 |
| 109 | 80 | 28.95 |
| 85 | 82 | 29.31 |
| 171 | 85 | 29.84 |
| 128 | 109 | 33.80 |
| 287 | 112 | 34.26 |
| 124 | 116 | 34.86 |
| 424 | 124 | 36.05 |
| 409 | 128 | 36.62 |
| 471 | 141 | 38.44 |
| 145 | 145 | 38.99 |
| 497 | 171 | 42.33 |
| 220 | 183 | 43.79 |
| 347 | 220 | 48.01 |
| 318 | 224 | 48.45 |
| 267 | 267 | 52.89 |
| 383 | 287 | 54.84 |
| 112 | 291 | 55.22 |
| 50 | 318 | 57.72 |
| 183 | 346 | 60.21 |
| 224 | 347 | 60.30 |
| 62 | 383 | 63.35 |
| 399 | 399 | 64.66 |
| 116 | 409 | 65.46 |
| 461 | 424 | 66.65 |
| 291 | 459 | 69.35 |
| 459 | 461 | 69.50 |
| 82 | 471 | 70.25 |
| 346 | 497 | 72.16 |

## Radii Construction

The radii used in this study were constructed in June 2004 at the Gatlinburg-Pigeon Forge Airport in Sevierville, TN at the tie-down area north of the runway. The cable used in this study was $1 / 8^{\prime \prime}$ insulated steel cable purchased at a local hardware store. The cable itself was affixed to a steel pin which was driven into the ground for stability. Figure 1 shows the pin and the spool of cable.


Figure 1. Steel Pin and Cable Used in the Study

The cable itself was marked off according to the second column of Table 1, an ordered random set between 50 and 500 feet. A tape measure was used to mark these distances. This is illustrated in Figure 2. Marking the radii onto the pavement was accomplished by using a stick of soapstone, which leaves a bright white mark when applied. The radii were marked as according to the first column in Table 1, the original random set.


Figure 2. Marking the Cable

## PhotoModeler Procedure

## Description of the Software

PhotoModeler is a photogrammetry software package by EOS Systems in Vancouver, British Columbia. The version used for this study was version 4.0g. PhotoModeler can be used for a multitude of different measuring applications, including traffic accident reconstruction. PhotoModeler can handle 2-D accident reconstruction projects like accident scene measurement and 3-D projects such as vehicle crush measurement. Interested readers can visit http://www.photomodeler.com for additional information.

## Description of a Generic PhotoModeler Procedure

The first step of a new PhotoModeler project involves taking pictures of the object or scene of interest. A new project is then created using the software's Project Setup Wizard; this is where the user enters fundamental information such as location of the digitized photos, approximate size of the object being modeled, and camera information. After that, the user marks features with a mouse on each photograph using the various tools available. Next the project
is processed and PhotoModeler creates a 2-D or 3-D model from the 2-D photographs. The user then gives the project dimension by scaling it. At this point, the user can extract the desired measurements from the marked features.

## Camera Calibration

In this study, a digital Olympus C-5050 was calibrated using the embedded Camera Calibrator program in PhotoModeler. Camera calibration ensures an accurate measuring device. This camera was chosen for its (relatively high) resolution (5.0 Mega pixels), its use of ordinary AA batteries (which are easily rechargeable) and its ability to hold two (2) digital storage cards (xD and Compact Flash). The process itself (well documented in Appendix $1 \& 13$ ) involved taking eight (8) pictures of a special grid which was projected onto a wall. This is illustrated with Figure 3, which is a screenshot of the procedure. After points were marked and processed with the Camera Calibrator software, camera information such as focal length, format size, and


Figure 3. Camera Calibration Grid
principal point was determined as a result. Figure 4 shows the C5050's resultant camera information.

## Targeted Cone Placement

This study utilized a special form of the ordinary traffic conethe targeted cone. Each targeted cone has a total of three (3) targets, two (2) placed on the exterior and one (1) placed on top. The minimum number of points PhotoModeler needs for a project to process is six (6) points; hence this study uses six (6) targeted cones.


Figure 4. Result of the Olympus C-5050 Calibration Procedure

The top targets were precisely constructed at a local sign shop.
Figure 5 shows the targets. What is important to note about these targets is that they are sufficiently thin enough that the point in the center, whether photographed from either side, occupies the same point in space. This is important when referencing the points in PhotoModeler. The targets for the exterior of the cone were printed out by an inkjet printer onto label paper, cut out, and placed on the
outside of the cone. Figure 6 shows a targeted cone straddling a soapstone mark (sorry for the camera strap in photo).

Five (5) targeted cones are placed on the soapstone marks along the radius. The sixth cone is placed directly across from the third or middle cone. For ease in conspicuity, alternating square and round targets are utilized. Figure 7 shows this configuration.

## Curve Modeling

The first step in curve modeling is to take pictures of the


Figure 5. Targets for the Top of the Cones


Figure 6. Target Cone on a Mark


Figure 7. Arrangement of Cones Along Radius
targeted cones from both sides, i.e., from an upstream and a downstream location. In order for PhotoModeler to create an accurate model, each point must reside in at least two (2) photographs, preferably three (3). The user's picture taking technique needs to reflect this requirement, hence; about four or five pictures were taken on each side for this study. For scaling purposes, a physical measurement of the curve must be made. This measurement can be between any two cones; for this study the scaling measurement was made between cones \#3 (the middle cone in the arc) and \#6 (the cone across from all other cones) with a measuring wheel and recorded.

Using PhotoModeler's "Project Setup Wizard", four (4) or five (5) photos from a single side (upstream or downstream) were opened up and the centers of all targets were marked and referenced across all photos. "Marking a point" entailed selecting the point tool which looks like a single " $x$ " on the toolbar. The user would then mark a target on the first photograph. "Referencing a point" required the use of the referencing tool on the toolbar which resembles a double "x". Referencing "notifies" PhotoModeler that that particular
point is the same across all photos; it allows PhotoModeler to recognize that this is the same physical point in space. This procedure of marking and referencing points continued across all eight (8) or ten (10) photos until all points were marked and referenced. Then the project was processed and scaled. After that, two lines were drawn using the line tool on the PhotoModeler toolbar. The first line is drawn between cone \#1 and cone \#5. This measurement is our chord. The next line is drawn between cone\#3 and cone \#6. Where the first line intersects the second line to cone \#3 is our middle ordinate. These two measurements can be extracted from PhotoModeler using the measuring tool on the toolbar. Figure 8 illustrates the chord and middle ordinate measurements which can be seen in the 3-D viewer. Note that a measurement of 5.869 ft is circled in blue. This is case 14 's measurement for $h$. To get a radius measurement, use PhotoModeler's results for I and h , and plug into $r=\frac{l^{2}}{8 h}+\frac{h}{2} \quad$ for an estimate for the radius.


Figure 8. Chord and Middle Ordinate

## Results

Table 2 shows the results for this study. Columns included in the table are the following: the known " r ", which is the random number set from Table 1; the scale factor, which is the distance used by PhotoModeler for scaling purposes; I and h, the chord and middle ordinate measurements extracted directly from PhotoModeler; the

Table 2. Results of the Study

| \# | known "r" | scale factor | I | h | computed "r" | diff (ft) | diff (inch) | \%difference | speed (known "r") | speed (comp. "r") | diff (mph) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 141 | 27.3333333 | 75.419 | 5.16 | 140.3713169 | -0.6286831 | -7.544197 | 0.44587455 | 38.43749612 | 38.35170898 | -0.085787138 |
| 2 | 80 | 28 | 77.127 | 9.897 | 80.07952618 | 0.0795262 | 0.9543142 | 0.099407728 | 28.95279707 | 28.96718423 | 0.014387161 |
| 3 | 109 | 29 | 88.794 | 9.429 | 109.2374403 | 0.2374403 | 2.8492841 | 0.217835178 | 33.79549267 | 33.83228197 | 0.036789301 |
| 4 | 85 | 21.08333333 | 95.36 | 14.534 | 85.47610967 | 0.4761097 | 5.7133161 | 0.560129028 | 29.84386012 | 29.92732555 | 0.083465426 |
| 5 | 171 | 34.0833333 | 116.639 | 10.223 | 171.4601296 | 0.4601296 | 5.5215549 | 0.269081622 | 42.32954382 | 42.38645618 | 0.056912364 |
| 6 | 128 | 19.25 | 74.631 | 5.593 | 127.2776854 | -0.7223146 | -8.667775 | 0.564308256 | 36.62271335 | 36.51923476 | -0.103478592 |
| 7 | 287 | 23.08333333 | 148.954 | 9.832 | 286.9961225 | -0.0038775 | -0.04653 | 0.001351042 | 54.83861545 | 54.83824515 | -0.000370303 |
| 8 | 124 | 21.08333333 | 96.455 | 9.783 | 123.765657 | -0.234343 | -2.812116 | 0.188986274 | 36.04594166 | 36.01186471 | -0.034076954 |
| 9 | 424 | 25.16666667 | 111.039 | 3.635 | 425.8085427 | 1.8085427 | 21.702512 | 0.426543084 | 66.65434441 | 66.79634807 | 0.142003659 |
| 10 | 409 | 21.95833333 | 108.472 | 3.593 | 411.1401816 | 2.1401816 | 25.682179 | 0.523271786 | 65.46470074 | 65.63575659 | 0.171055848 |
| 11 | 471 | 27.45833333 | 112.145 | 3.345 | 471.6463799 | 0.6463799 | 7.7565583 | 0.137235639 | 70.25156225 | 70.299751 | 0.048188748 |
| 12 | 145 | 17.16666667 | 84.254 | 6.233 | 145.4784548 | 0.4784548 | 5.741458 | 0.329968853 | 38.97889597 | 39.04315221 | 0.064256248 |
| 13 | 497 | 26.125 | 117.186 | 3.448 | 499.5690767 | 2.5690767 | 30.828921 | 0.516916843 | 72.16452 | 72.35079506 | 0.186275059 |
| 14 | 220 | 22.16666667 | 100.902 | 5.869 | 219.7775227 | -0.2224773 | -2.669727 | 0.101126024 | 48.01278226 | 47.98849954 | -0.024282723 |
| 15 | 347 | 17.41666667 | 89.158 | 2.901 | 343.9681217 | -3.0318783 | -36.38254 | 0.873740149 | 60.29902228 | 60.03501611 | -0.264006173 |
| 16 | 318 | 20.95833333 | 72.018 | 2.051 | 317.1269337 | -0.8730663 | -10.4768 | 0.274549154 | 57.72435553 | 57.64506036 | -0.079295176 |
| 17 | 267 | 28.41666667 | 130.705 | 8.069 | 268.6862075 | 1.6862075 | 20.23449 | 0.631538404 | 52.89336092 | 53.06011914 | 0.166758213 |
| 18 | 383 | 17.20833333 | 91.422 | 2.75 | 381.2832765 | -1.7167235 | -20.60068 | 0.448230667 | 63.34975212 | 63.20761633 | -0.142135794 |
| 19 | 112 | 15.41666667 | 76.294 | 6.637 | 112.9458624 | 0.9458624 | 11.350349 | 0.844520034 | 34.25741149 | 34.4017628 | 0.144351314 |
| 20 | 50 | 10.41666667 | 42.637 | 4.775 | 49.97686568 | -0.0231343 | -0.277612 | 0.046268639 | 22.88919585 | 22.88390003 | -0.005295812 |
| 21 | 183 | 15.8333333 | 80.74 | 4.527 | 182.2653666 | -0.7346334 | -8.815601 | 0.401439028 | 43.78961005 | 43.70162749 | -0.087982565 |
| 22 | 224 | 13.70833333 | 97.535 | 5.409 | 222.5481916 | -1.4518084 | -17.4217 | 0.648128728 | 48.44729593 | 48.29004042 | -0.157255513 |
| 23 | 62 | 17.41666667 | 48.628 | 4.937 | 62.33993974 | 0.3399397 | 4.0792769 | 0.548289904 | 25.48832978 | 25.5581093 | 0.069779519 |
| 24 | 399 | 27.625 | 106.086 | 3.549 | 398.1621936 | -0.8378064 | -10.05368 | 0.209976547 | 64.65944622 | 64.59152588 | -0.067920339 |
| 25 | 116 | 18.6666667 | 74.7222 | 6.153 | 116.5050546 | 0.5050546 | 6.0606555 | 0.435391918 | 34.86378443 | 34.93959914 | 0.075814709 |
| 26 | 461 | 30.8333333 | 123.069 | 4.123 | 461.2531918 | 0.2531918 | 3.0383011 | 0.054922291 | 69.50179092 | 69.52087447 | 0.019083551 |
| 27 | 291 | 21.75 | 101.913 | 4.49 | 291.3947653 | 0.3947653 | 4.7371834 | 0.135658173 | 55.21944374 | 55.25688604 | 0.037442296 |
| 28 | 459 | 28.875 | 119.449 | 3.901 | 459.143002 | 0.143002 | 1.7160235 | 0.03115511 | 69.35086394 | 69.36166645 | 0.010802511 |
| 29 | 82 | 17.41666667 | 49.833 | 3.869 | 82.1660808 | 0.1660808 | 1.9929696 | 0.202537564 | 29.31247294 | 29.34214239 | 0.029669446 |
| 30 | 346 | 21 | 118.378 | 5.102 | 345.8808433 | -0.1191567 | -1.42988 | 0.034438354 | 60.21207339 | 60.20170464 | $-0.010368757$ |

d-bar: 0.09100141 .0920172
std dev: $1.1297617 \quad 13.55714$
computed " r " which uses PhotoModeler's results for I and h and $r=\frac{\rho^{2}}{8 h}+\frac{h}{2}$ to compute the radius; diff (ft) and diff (inch) are the differences of the known "r" and PhotoModeler's computed "r"; \% difference is the \% difference between the known " $r$ " and the computed "r"; speed (known "r" and comp "r") uses the Critical Speed Formula $v=\sqrt{g r} \mu$ with coefficient of friction $=0.7$; diff (mph) is the difference between the two speeds. The results of the Matched Pairs analysis are shown in Figure 9, which is a JMP screenshot. Appx. 11 contains all screenshots for the thirty (30) cases.

## Conclusion

When looking at Table 2, the "\% differences" range from $0.001 \%$ to $0.874 \%$. When examining the JMP screenshots, we can see that a 95\% C.I. indicates that we are 95\% confident that the difference lies between -0.33 and 0.51 feet. Additionally, by looking at the two-tailed t-test, the difference between the two techniques is not significant. Since the p-value is not small (>0.05), we accept the


Figure 9. Matched Pairs Results
null hypothesis and say that the mean difference between the two techniques is zero. This is further evidenced by zero in the confidence interval. On average, the methods are the same. Also if one looks at $\mathrm{R}^{\mathbf{2}}$, one can see that it is very close to one, which indicates an almost perfect relationship. This suggests that the known "r's" predict the computed "r's" exactly.

## Future Directions

- Measure photogrammetry's results against a number of realworld curves. Ideally, the curves to be measured would have their own blueprints, design plans, or total station documentation where values for radius (also grade and superelevation) are easily obtained, and photogrammetry could be measured against these benchmarks.
- Supplement this study with photogrammetry's results vs. the Tape Measure Method. Paired Comparisons could be utilized for the statistical portion. This idea was taken from a reviewer for this study. In 2005, this study was not accepted for publication for the SAE Congress, unless certain changes were made. As to date, the changes haven't been made and this study remains unpublished. Appendix 12 contains the reviewers' comments.
- Develop procedures to measure superelevation and grade with photogrammetry. The author was going to include these items
in a separate paper, but a reviewer suggested it be included with this one.
- Perform a study on the scaling measurement itself. A reviewer recommended this, and at first, this author thought it was an unwise suggestion. After some thought, however, it's actually not a bad idea-perhaps not for a curve paper, but a paper affecting the accuracy of PhotoModeler. Digital resolution has a big impact on accuracy (as one will find out in Part Three) and somewhat, on the scaling measurement. It is this author's experience that a scaling measurement that encompasses a big chunk of the object being modeled makes for a better project in terms of accuracy. In other words, don't use a scaling measurement of 0.5 ft when the object being modeled is 30 ft long. Pick something on the object that is well defined and bigger. This suggestion certainly warrants some investigation.
- Examine the impact on accuracy due to the number of photos in a curve project. What is optimal? What is minimally
required? Theoretically, only two photos are required.
However, this author knows more pictures increase accuracy. (You can have too many pictures; the potential for error is great with a lot of pictures). PhotoModeler doesn't like two photo projects (as evidenced in the Process dialog), but it'll do them (reluctantly).
- Consider the effect of targets on error when grade or superelevation is present. As stated before, a prospective direction for the study is to include superelevation and grade in photogrammetric curve measurement. Part Two's experiments were conducted on (relatively) flat terrain where e and G were not an issue. A targeted cone takes on an interesting appearance when on a hill-the cone is in agreement with the alignment on the grade, but the target itself remains straight up and down. This is because the target dangles on top of the cone; it is not permanently affixed to it. Some trial experiments would quickly determine if this is an issue or not; if so, a cone could be constructed with a fixed, rigid target.


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## PART THREE

## AN EVALUATION OF COMMON ACCIDENT RECONSTRUCTION MEASUREMENT METHODOLOGIES


#### Abstract

This study's aim was to learn what causes variation in three common traffic accident reconstruction measurement techniques: measuring tape, measuring wheels and photogrammetry (PhotoModeler). These three techniques were evaluated against a known benchmark distance (48 feet) measured by a total station. A full factorial $2^{3}$ Design of Experiments study with four replicates was applied to each technique. The following results were found: Measuring tape experiment: None of the main effects or crosseffects was significant. Measuring wheel experiment: Two main effects ( $\mathrm{p}<0.0001$ and $\mathrm{p}<0.0060$ ) and all of the cross-effects ( $p<0.0079$ to 0.0345 ) were significant. Photogrammetry experiment: One main effect ( $\mathrm{p}<0.0063$ ) and one cross effect ( $\mathrm{p}<0.0325$ ) were significant. The measuring wheel is most sensitive to surface type (smooth or rough surface) and photogrammetry is most sensitive to digital resolution (low or high resolution).


## Introduction

It is often necessary for physical measurements to be taken from the highway. This can be done for a variety of reasons: making accident diagrams, identifying the locations of the resting positions of vehicles, or measuring skidmarks. The measurement process itself can manifest in one of several forms: pacing, total stations, lasers, measuring tapes, measuring wheels, or photogrammetry. This study will examine various factors that could affect the accuracy of the later three abovementioned measurement techniques. The tool utilized for this purpose is the Design of Experiments (DOE). Analysis of Variance (ANOVA) will determine which details of the experiment are significant or relevant.

## Design of Experiments

## History

According to Joan Fisher Box [165], Design of Experiments got its start in the agriculture industry. R.A. Fisher was a statistician working at the Rothamsted Experimental Station in England. It was
at this location that Fisher developed DOE; here he planned different experiments on crops and fertilizers. In the abstract of her article, Box eloquently describes how analysis of variance brought about the need for DOE, factorial blocking designs, randomization, and replication. In 1935, Fisher wrote the book, Design of Experiments which contained few numerical examples and masses of theory [166]. Initially, Fisher's experiments received much opposition. His critics maintained that the experiments themselves were too complex but they eventually began to appreciate their merit to the agricultural world.

## DOE Variable Definition

The main objective in experimental studies is to evaluate the set of pre-selected variables at different intensities to investigate their reaction to a variable of interest [167]. The pre-selected variables are identified as factors, different intensities as levels, and variable of interest as response variable. To improve the accuracy of your experiment the following is suggested [167]:

- Blocking (removes nuisance errors)
- Randomization (removes nuisance errors)
- Replication (removes random errors)
- Repeat measurements (removes measurement errors)


## Experimental Designs

Tamhane [167] explains that the completely randomized design (CRD) is an experiment where the treatments are assigned in a random order, however; CRD designs can mask the effects of treatment effects, especially if one or more of the same treatment is in the same block. Randomized Block Designs (RBD) are random and unique within the blocks, reducing the effect of a nuisance variable (an additional treatment in a block.) Fig. 1 shows a CRD and RBD.

| Completely Randomized Design |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Block | $\underset{2}{\text { Block }}$ | $\underset{3}{\text { Block }}$ | ${ }_{4}^{\text {Block }}$ | ${ }_{5}^{\text {Block }}$ |
| A | C | D | D | B |
| B | A | A | C | D |
| C | D | B | A | C |
| $\mathrm{B}_{4}$ | $\mathrm{C}_{4}$ | D | B | A |
| B's | 2 C 's |  |  |  |

Nuisance
unbalanced
factors could
confound your
results here
Figure 1. Illustration of CRD and RBD Designs

Factorial Designs
$\underline{2}^{2}$ Design
For this situation, we have 2 levels ${ }^{(2 \text { factors })}=2^{2}=4$, hence we have 4 treatment combinations possible. Table 1 delineates this type of design.
$\underline{2}^{3}$ Design
In a similar fashion, the $2^{3}$ Design will have 3 factors, resulting in a possible 8 treatment combinations. Table 2 delineates this type of design.

## Table 1. $2^{2}$ Design

| Factor A | Factor B | Treatment <br> combination | Interpretation of <br> experiment |
| :---: | :---: | :---: | :--- |
| - | - | $(1)$ | Low level of A with low level <br> of B |
| $\mathbf{+}$ | - | a | High level of A with low level <br> of B |
| - | $\mathbf{+}$ | b | Low level of A with high level <br> of B |
| $\mathbf{+}$ | $\mathbf{+}$ | ab | High level of A with High <br> level of B |

## Table 2. $2^{3}$ Design

| Factor |  |  | Treatment Combination | Interpretation |
| :---: | :---: | :---: | :---: | :---: |
| A | B | C |  |  |
| - | - | - | (1) | Low levels of $\mathrm{A}, \mathrm{B}$, and C |
| + | - | - | a | High A, Low B \& C |
| - | + | - | b | Low A, High B, Low A |
| + | + | - | ab | High A, High B, Low C |
| - | - | + | c | Low A, Low B, High C |
| + | - | + | ac | High A, Low B, High C |
| - | + | + | bc | Low A, High B, High C |
| + | + | + | abc | High levels of $A, B$, and $C$ |

## Analysis of Variance (ANOVA)

## History

As mentioned earlier, Box [165] informed that ANOVA's
beginnings were the results of DOE. Scheffe [168] claims that Fisher "coined" the terms variance and analysis of variance, but others before him were using ANOVA's components long before Fisher. Scheffe also conveys that many subsequent improvements have been made to Fisher's ANOVA tables since their inception-the table you see today is roughly the table Fisher created years ago.

## The Delineated ANOVA Table

Below is a typical ANOVA table (Table 3) which can be used in conjunction with DOE. In lieu of hand calculations it is advisable to use software packages such as JMP or SAS to do the calculations.

## Research Design

The objective of this project is to reveal the sources of variability in different measuring techniques. As mentioned previously, the total station, the common measuring device used by civil engineers for a variety of applications, will be used as a benchmark in this design.

Table 3. ANOVA Table

| Variation | Degrees of <br> Freedom | Mean Square |  |
| :--- | :--- | :--- | :--- |
| Between <br> treatments, $\mathrm{V}_{\mathrm{R}}$ | $a-1$ | $\hat{S}_{R}^{2}=\frac{V_{R}}{a-1}$ | $\frac{\hat{S}_{R}^{2}}{\hat{S}_{E}^{2}}$ |
| Between <br> blocks, $\mathrm{V}_{\mathrm{C}}$ | $b-1$ | $\hat{S}_{C}^{2}=\frac{V_{C}}{b-1}$ | $\frac{\hat{S}_{C}^{2}}{\hat{S}_{E}^{2}}$ |
| Interaction, $\mathrm{V}_{\mathrm{I}}$ | $(a-1)(b-1)$ | $\hat{S}_{I}^{2}=\frac{V_{I}}{(a-1)(b-1)}$ | $\frac{\hat{S}_{I}^{2}}{\hat{S}_{E}^{2}}$ |
| Residual or <br> random, $\mathrm{V}_{\mathrm{E}}$ | $a b(c-1)$ | $\hat{S}_{E}^{2}=\frac{V_{E}}{a b(c-1)}$ |  |

In other words, the results photogrammetry, the measuring wheel, and the measuring tape will all be compared to the results of the total station. Following this reasoning, the execution of three (3) separate experiments, one for each measuring technique, will be required. After the completion of each experiment, the results of each will be analyzed.

## Designing of the Experiment

- Type of Design: $2^{3} ; 2$ levels $^{3 \text { factors }}$
- Response Variable: Error (or accuracy or measurement difference)
- Factors: When deciding what factors to include in the experiment, one must ask the following: What would influence the amount of error in each measuring device? Since each measuring device is unique and measures distances in a different way, they should each have their own set of factors, as indicated by Table 4.
- Levels: The levels for each methodology were selected mainly for convenience and ease of use. PhotoModeler: The low and

Table 4. Factors and Levels For Each Experiment

| Factor |  |  |
| :---: | :---: | :---: |
| Number of Pictures Taken | Levels |  |
| Nigital Resolution of Camera | 4 (low), 8 (high) |  |
| Exposure to Road While Taking <br> Measurements | low, high <br> low exposure (rush to get job done), <br> high exposure (take your time) |  |
| Measuring Wheel |  |  |

high levels of \# of photos are 4 and 8 respectively. The digital resolution levels are 0.15 mega pixels (low) and 5 mega pixels (high).
"Exposure to road" on average was 4 minutes for 4 photos and 5 minutes for 8 photos (low level or rush) and 8 minutes for 4 photos and 9 minutes for 8 photos (high level or take time). Measuring Wheel: The levels for roughness of pavement were not rough (on pavement) or rough (in the gravel). Wheel diameter levels were small (4 inches) and large (12 inches). "Exposure to road" levels were on average 30 seconds (low level or rush) and 1.5 minutes
(high level or take time). Measuring Tape: "Type of tape" levels were cloth (low level) and steel (high level). The levels for amount of making tape used were 4 pieces (low) and 8 pieces (high).
"Exposure to road" levels were on average 1.5 minutes (low) and 3 minutes (high).

- Design Matrices: Tables 5a, 5b, and 5c depicts an appropriate design matrix for each experiment.

Table 5a. Photogrammetry Design Matrix

| PhotoModeler Experiment |  |  | Treatment | Interpretation |
| :---: | :---: | :---: | :---: | :---: |
| A: \# of Pix | B: Dig. Res. | C: Exp |  |  |
| - | - | - | (1) | Low levels of A, B, and C |
| + | - | - | a | High A, Low B \& C |
| - | + | - | b | Low A, High B, Low A |
| + | + | - | ab | High A, High B, Low C |
| - | - | + | C | Low A, Low B, High C |
| + | - | + | ac | High A, Low B, High C |
| - | + | + | bc | Low A, High B, High C |
| + | + | + | abc | Hi levels of A, B, and C |

## Table 5b. Measuring Wheel Design Matrix

| Measuring Wheel Experiment |  |  | Treatment | Interpretation |
| :---: | :---: | :---: | :---: | :---: |
| A: Rough | B: Diameter | C: Exp |  |  |
| - | - | - | (1) | Low levels of A, B, and C |
| + | - | - | a | High A, Low B \& C |
| - | + | - | b | Low A, High B, Low A |
| + | + | - | ab | High A, High B, Low C |
| - | - | + | C | Low A, Low B, High C |
| + | - | + | ac | High A, Low B, High C |
| - | + | + | bc | Low A, High B, High C |
| + | + | + | abc | Hi levels of A, B, and C |

Table 5c. Measuring Tape Design Matrix

| Measuring Tape Experiment |  |  | Treatment | Interpretation |
| :---: | :---: | :---: | :---: | :---: |
| A:TapeType | B: Mask. tape | C: Exp |  |  |
| - | - | - | (1) | Low levels of $\mathrm{A}, \mathrm{B}$, and C |
| + | - | - | a | High A, Low B \& C |
| - | + | - | b | Low A, High B, Low A |
| + | + | - | ab | High A, High B, Low C |
| - | - | + | C | Low A, Low B, High C |
| + | - | + | ac | High A, Low B, High C |
| - | + | + | bc | Low A, High B, High C |
| + | + | + | abc | High levels of A, B, and C |

- Number of Replications: It was determined that 5
replications of each experiment should be performed. Since there are 8 treatment combinations and 5 replications, there will be a total of 40 data points. To ensure that the within block confounding is reduced, a Randomized Block Design is utilized. The following table (Table 6) illustrates an order in which the experiments could be conducted. Recall that this table will apply to each experiment: PhotoModeler, measuring wheel and measuring tape.

Table 6. RBD with 5 Blocks

| Block 1 | Block 2 | Block 3 | Block 4 | Block5 |
| :---: | :---: | :---: | :---: | :---: |
| $\mathbf{( 1 )}$ | $\mathbf{b c}$ | $\mathbf{a b}$ | $\mathbf{a}$ | $\mathbf{c}$ |
| $\mathbf{a b c}$ | $\mathbf{c}$ | $\mathbf{b c}$ | $\mathbf{a c}$ | $\mathbf{a b}$ |
| $\mathbf{a}$ | $\mathbf{b}$ | $\mathbf{a}$ | $\mathbf{b}$ | $\mathbf{b}$ |
| $\mathbf{b c}$ | $\mathbf{( 1 )}$ | $\mathbf{c}$ | $\mathbf{b c}$ | $\mathbf{a}$ |
| $\mathbf{b}$ | $\mathbf{a b c}$ | $\mathbf{( 1 )}$ | $\mathbf{a b}$ | $\mathbf{a b c}$ |
| $\mathbf{a c}$ | $\mathbf{a c}$ | $\mathbf{b}$ | $\mathbf{a b c}$ | $\mathbf{( 1 )}$ |
| $\mathbf{a b}$ | $\mathbf{a}$ | $\mathbf{a c}$ | $\mathbf{c}$ | $\mathbf{a c}$ |
| $\mathbf{c}$ | $\mathbf{a b}$ | $\mathbf{a b c}$ | $\mathbf{( 1 )}$ | $\mathbf{b c}$ |

## Selection of Sample

The sample that was measured in this study is a strip of asphalt and gravel located at the hangar area north of runway 28 at the Gatlinburg-Pigeon Forge airport in Sevierville, TN. This particular sample was selected because of its "lack of activity", minimum contact with airport traffic, and interruptions. All experiments for Part Three were conducted on this area. Figure 2 shows this sample. Note the asphalt area and the gravel area.


Figure 2. Part Three's Experiment Area

## Instrument Used

## Photogrammetry Experiment

The primary instrument used in this experiment is the photogrammetry software package called PhotoModeler (version 4 g ), from EOS Systems, Inc. The software is used in conjunction with a calibrated digital camera. Two levels of digital resolution were used in this experiment: high and low. High resolution calibration details are described in Appendix 1; low resolution calibration details are in Appendix 13. A digital camera was used in this experiment, primarily for time and money saving reasons; a film camera would require film processing and digitization via scanner.

## Measuring Wheel Experiment

The primary instrument used in this experiment is a measuring wheel. One can make measurements with this device holding the handle in a standing position while allowing the wheel to roll along the pavement surface. Two types of wheels will be used, of different diameters. Measuring wheels are used quite frequently in accident reconstruction.

## Measuring Tape Experiment

The primary instrument in this experiment is a measuring tape.
Two types of measuring tapes will be used: cloth and steel.
Measuring tapes are also used quite frequently in accident reconstruction.

## Procedures

## Total Station Measurement

The first step in this project is to obtain a total station and measure the road segment of interest. Recall that this must be done first, for the total station is considered the benchmark measuring device in this project. In October 2004, two (2) registered land surveyors from VISION Engineering in Sevierville, TN measured a 48 ft distance on the asphalt and in the gravel. Figure 2 shows the crew measuring the benchmark. Appendix 14 contains all photos of the total station benchmark measurement.

## Photogrammetry Experiment

Utilizing JMP's embedded DOE Tool, the order of experiments were determined.

The photogrammetry experiment proceeded according to the following procedure:
> Place center of targeted cone at the endpoints of the line segment (on pins)
> Place 4 more cones between endpoints (PhotoModeler needs a minimum of 6 points for a project to process
> Take the predetermined amount of pictures (4 or 8) from an upstream and a downstream position
> Take one measurement (usually between 2 arbitrary cones) for scaling purposes
> Download images from camera onto computer
> Use PhotoModeler

- Create a new project
- Mark and reference points
- Scale project
- Process
- Extract needed measurements
> Record results on data sheet.

Figure 3 shows equipment used for this experiment. Figure 4 shows a project with 8 photos. Figure 5 shows a project with 4 photos.

## Measuring Wheel Experiment

Again utilizing JMP's DOE Tool, determine which experiment to perform first. The measuring wheel experiment will proceed as follows:
> Visually locate the two endpoints to be measured.
> Reset the counter, located at the base of the wheel.


Figure 3. Equipment Used For Photogrammetry Experiment


Figure 4. A PhotoModeler Project With 8 Photos


Figure 5. A PhotoModeler Project With 4 Photos
> Start at the first point, firmly holding wheel to pavement so there's good contact.
> Try to track in a straight line as best you can from point to point to increase accuracy.
> Record the results on the data sheet.

## Measuring Tape Experiment

Use JMP's DOE to determine which experiment to perform. The measuring tape experiment will proceed as follows:
> Visually locate the two endpoints to be measured
> Stretch out tape, approximately the entire length of line segment
> Secure measuring tape with masking tape, applying the proper amount specified (4 or 8 pieces). Try to follow a straight line as best as possible to increase accuracy.
> Record the results on the data sheet.

Appendix 15 contains some photos of this experiment.

## Results

## Total Station Result

The RLS in charge on benchmark measurement day in October 2004 said on average, his measurements were "within a $1 / 16^{\text {th }}$ of an inch." This author asked and wanted a data printout from his total station for documentation purposes, but he wasn't able to provide one.

The results of the three experiments are specified below in Figures 6-8:

Results From Photogrammetry Experiment
$\mathbf{2 \times 2 \times 2}$ Factorial PhotoModeler

| Rows | Pattern | $\begin{aligned} & \text { \# of } \\ & \text { pics } \end{aligned}$ | digital resolution | exposure | measurement difference |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | $\rightarrow++$ | -1 | 1 | 1 | 0.891 |
| 2 | +*+ | 1 | 1 | 1 | 0.37 |
| 3 | +-+ | 1 | -1 | 1 | 0.325 |
| 4 | +- | 1 | -1 | -1 | 0.476 |
| 5 | $\xrightarrow{+}$ | 1 | -1 | 1 | 0.867 |
| 6 | -+- | -1 | 1 | -1 | -0.12 |
| 7 | $\rightarrow+$ | -1 | 1 | 1 | 0.203 |
| 8 | +** | 1 | 1 | 1 | 0.46 |
| 9 | $\rightarrow+$ | -1 | 1 | -1 | -0.433 |
| 10 | -- | -1 | 1 | -1 | 0.251 |
| 11 | $\cdots$ | -1 | -1 | 1 | 0.842 |
| 12 | +++ | 1 | 1 | 1 | 0.706 |
| 13 | - | -1 | -1 | -1 | 0.74 |
| 14 | +** | 1 | 1 | 1 | 0.741 |
| 15 | -- | -1 | -1 | -1 | 0.993 |
| 16 | $\longrightarrow$ | -1 | -1 | 1 | 1.185 |
| 17 | +-- | 1 | -1 | -1 | 2692 |
| 18 | +- | 1 | -1 | -1 | 1.297 |
| 19 | -+- | -1 | 1 | -1 | 1.261 |
| 20 | ++- | 1 | 1 | -1 | 0.255 |
| 21 | ++- | 1 | 1 | -1 | 0.4 |
| 22 | +*- | 1 | 1 | -1 | -0.188 |
| 23 | + + | 1 | -1 | 1 | 0.559 |
| 24 | +-- | 1 | -1 | -1 | 2.428 |
| 25 | -- | -1 | -1 | -1 | 1.754 |
| 26 | +-+ | 1 | -1 | 1 | 0.679 |
| 27 | $\rightarrow+$ | -1 | 1 | 1 | 0.954 |
| 28 | $\cdots$ | -1 | -1 | 1 | 0.759 |
| 29 | -- | -1 | -1 | -1 | 1.47 |
| 30 | ++- | 1 | 1 | -1 | 0.07 |
| 31 | $\rightarrow$ | -1 | -1 | 1 | 0.639 |
| 32 | $\cdots$ | -1 | -1 | 1 | 1.384 |
| 33 | -+- | -1 | 1 | -1 | 1.159 |
| 34 | ++- | 1 | 1 | -1 | 0.913 |
| 35 | -- | -1 | -1 | -1 | 1.174 |
| 36 | +++ | 1 | 1 | 1 | -0.178 |
| 37 | +-+ | 1 | -1 | 1 | -0.142 |
| 38 | +- | 1 | -1 | -1 | 0.064 |
| 39 | $-++$ | -1 | 1 | 1 | 0.818 |
| 40 | $\rightarrow+$ | -1 | 1 | 1 | 0.862 |

$2 \times 2 \times 2$ Factorial PhotoModeler- Fit Least Squares
Response measurement difference

## Whole Model

Actual by Predicted Plot


Summary of Fit


Figure 6. JMP Printouts for Photogrammetry Experiment
$2 \times 2 \times 2$ Factorial measuring wheel

| Rows | Pattern | surface | whee diameter | exposure | measurement difference |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | +-- | 1 | -1 | -1 | -2.375 |
| 2 | - | -1 | -1 | -1 | 0.7083 |
| 3 | $\xrightarrow{+}$ | 1 | -1 | 1 | -1 |
| 4 | +- | 1 | -1 | -1 | -1.334 |
| 5 | -+- | -1 | 1 | -1 | 0.33 |
| 6 | +++ | 1 | 1 | 1 | -0.7084 |
| 7 | +-+ | 1 | -1 | 1 | 0.083 |
| 8 | ++- | 1 | 1 | -1 | -0.375 |
| 9 | ++- | 1 | 1 | -1 | -0.75 |
| 10 | $\cdots$ | -1 | -1 | 1 | 0.5416 |
| 11 | +++ | 1 | 1 | 1 | -0.5 |
| 12 | -++ | -1 | 1 | 1 | 0.25 |
| 13 | ++- | 1 | 1 | -1 | -0.5 |
| 14 | -- | -1 | -1 | -1 | 0.666 |
| 15 | $\xrightarrow[+]{+}$ | -1 | -1 | 1 | 0.583 |
| 16 | +++ | 1 | 1 | 1 | -0.417 |
| 17 | --+ | -1 | -1 | 1 | 0.7916 |
| 18 | +++ | 1 | 1 | 1 | -0.25 |
| 19 | +-+ | 1 | -1 | 1 | -0.375 |
| 20 | ++- | 1 | 1 | -1 | -1 |
| 21 | -- | -1 | -1 | -1 | 0.7083 |
| 22 | $\stackrel{+}{+}$ | 1 | -1 | 1 | 0.625 |
| 23 | $+$ | 1 | -1 | 1 | 0.25 |
| 24 | - | -1 | -1 | -1 | 0.583 |
| 25 | +- | 1 | -1 | -1 | -1.125 |
| 28 | +- | 1 | -1 | -1 | -0.584 |
| 27 | +- | -1 | 1 | -1 | 0.166 |
| 28 | -++ | -1 | 1 | 1 | 0.25 |
| 29 | -- | -1 | -1 | 1 | 0.7083 |
| 30 | ++- | 1 | 1 | -1 | -0.167 |
| 31 | -- | -1 | -1 | -1 | 0.583 |
| 32 | +-- | 1 | -1 | -1 | -0.875 |
| 33 | $\rightarrow+$ | -1 | 1 | 1 | 0.168 |
| 34 | +++ | 1 | 1 | 1 | -0.25 |
| 35 | $\rightarrow+$ | -1 | 1 | -1 | 0.166 |
| 36 | $\rightarrow-$ | -1 | 1 | -1 | 0.2083 |
| 37 | $\rightarrow+$ | -1 | 1 | 1 | 0.25 |
| 38 | $\cdots$ | -1 | -1 | 1 | 0.7916 |
| 39 | -+- | -1 | 1 | -1 | 0.25 |
| 40 | $\rightarrow+$ | -1 | 1 | 1 | 0.166 |

20222 Factorial measuring wheel- Fit Least Squares


Figure 7. JMP Printouts for Measuring Wheel Experiment

## Results From Measuring Tape Experiment

## $2 \times 2 \times 2$ Factorial measuring tape

| Rows | Pattern | tape <br> type | amt of tape | exposure | measurement difference |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | -++ | -1 | 1 | 1 | 0.04 |
| 2 | ++* | 1 | 1 | 1 | 0.058 |
| 3 | +-- | 1 | -1 | -1 | 0.0416 |
| 4 | -+- | -1 | 1 | -1 | 0.04 |
| 5 | +- | 1 | -1 | -1 | 0.0416 |
| 6 | ++* | 1 | 1 | 1 | 0.0416 |
| 7 | $\rightarrow-$ | -1 | 1 | -1 | 0.07 |
| 8 | +-- | 1 | 1 | -1 | 0.0416 |
| 9 | +- | -1 | 1 | -1 | 0.03 |
| 10 | + + | 1 | -1 | 1 | 0.052 |
| 11 | -++ | -1 | 1 | 1 | 0.06 |
| 12 | -+- | -1 | 1 | -1 | 0.05 |
| 13 | +- | 1 | -1 | -1 | 0.0416 |
| 14 | - | -1 | -1 | -1 | 0.07 |
| 15 | $\cdots$ | -1 | -1 | 1 | 0.03 |
| 16 | - | -1 | -1 | -1 | 0.055 |
| 17 | -- | -1 | -1 | -1 | 0.03 |
| 18 | $\rightarrow$ | -1 | -1 | 1 | 0.06 |
| 19 | $\rightarrow+$ | -1 | 1 | 1 | 0.035 |
| 20 | +++ | 1 | 1 | 1 | 0.052 |
| 21 | $\xrightarrow[++]{+}$ | -1 | 1 | 1 | 0.035 |
| 22 | $\rightarrow+$ | -1 | 1 | 1 | 0.045 |
| 23 | +-- | 1 | 1 | -1 | 0.052 |
| 24 | - | -1 | -1 | -1 | 0.1 |
| 25 | +- | 1 | -1 | 1 | 0.052 |
| 26 | $\rightarrow+$ | -1 | 1 | -1 | 0.06 |
| 27 | ++- | 1 | 1 | -1 | 0.052 |
| 28 | $\cdots$ | -1 | -1 | 1 | 0.03 |
| 29 | +- | 1 | -1 | -1 | 0.0469 |
| 30 | --- | -1 | -1 | -1 | 0.045 |
| 31 | $\xrightarrow{+}$ | 1 | -1 | 1 | 0.0625 |
| 32 | ++- | 1. | 1 | -1 | 0.0469 |
| 33 | +- | 1 | -1 | -1 | 0.0469 |
| 34 | $\cdots$ | -1 | -1 | 1 | 0.035 |
| 35 | -- | -1 | -1 | 1 | 0.045 |
| 36 | +++ | 1 | 1 | 1 | 0.0469 |
| 37 | +-+ | 1 | -1 | 1 | 0.0416 |
| 38 | *+* | 1 | 1 | 1 | 0.052 |
| 39 | **- | 1 | 1 | -1 | 0.073 |
| 40 | +- | 1 | -1 | 1 | 0.045 |



Figure 8. JMP Printouts for Measuring Tape Experiment

## Conclusions

Even though this experiment truly has categorical (or discrete) factors (smooth/rough; small/large; rush/take time), the experiment was executed as continuous as per the suggestion of the Statistical Consulting Center at UT (the experiment was actually carried out both ways and the results were practically identical). The SCC suggested this because JMP computes more accurately in a continuous setting than in categorical. JMP simply assigns a -1 or +1 to each level; the experimenter has to keep each setting straight as to avoid confusion. Appendix 15 contains all JMP printouts with handwritten notes included.

## Measuring Wheel

The main effects that were significant in this experiment were surface and exposure to the road. Using the prediction profiler in JMP's embedded DOE tool will show that smooth is better for being on target; a smooth surface gives you results that are long of the target (this is possibly due to wavy behavior or bad tracking) and a rough surface give you results short of target (possibly due to lack of
rotation of the wheel); rushing gives a short of target result (wheel possibly skips) and taking your time gives a long of target result (wheel possibly waves about).

The following cross effects will yield the lowest errors: surface and wheel diameter-a smooth surface plus a large wheel diameter will yield a lower error; surface and exposure-if you have a rough surface it is best to take your time; wheel diameter and exposure-if you have a large diameter wheel, it is best to take your time; surface and wheel diameter and exposure-if you have a rough surface plus a small diameter wheel, it is best to take your time.

## Measuring tape

The factors that were thought to have an impact on the response turned out to have no impact at all-this is very clear by looking at the printout-no main nor cross effects were significant. In retrospect, the experiment could have been done differently. A possible factor that was not included in this experiment was length of measurement; shorter measurements would be more accurate than longer measurements because in longer measurements, the tape
measure itself could become more twisted than with shorter measurements.

## Photogrammetry

One main effect and one cross effect were significant at the $\alpha=5 \%$ level: digital resolution=0.0063 and digital resolution* exposure $=0.0325$. If one looks at the mean of response (response being measurement error), measuring tape did the best ( 0.045518 ft or 0.586 inches $)$, followed by measuring wheel $(-0.06901 \mathrm{ft}$ or 0.82812 inches), and then photogrammetry ( 0.7395 ft or 8.874 inches). 8.874 inches translates to a $1.5 \%$ error over 48 feet; this is a reasonable and acceptable measurement error for accident reconstruction applications such as speed estimates from skid marks. Future photogrammetry experiments should utilize the pins themselves; the pins would have to be incorporated into the measurement process, perhaps by highlighting the pins with neon paint to facilitate conspicuity in the digital photos.

## Future Directions and Research

- Incorporate length of measurement into the experiment, at two levels (short/long). Measure a distance at say, 48 feet, and then a distance longer than 48 feet. 48 feet was very manageable by all the techniques, perhaps a bit too manageable. Maybe something like 108 feet could work; this is roughly the distance across a two 4-lane highway with a median. In hindsight, the impact of measurement length could not only affect the results of measuring tape experiments, but the measuring wheel experiments as well, due to more opportunities for skips and wavy motion. The author's initial feeling is that the photogrammetry experiment probably wouldn't be affected by length of measurement, provided that the targets are still clearly seen in all the photos while working within the photogrammetry software, however; there is a point where targets are not easily seen when placed far from the camera, which in case, the target size
would have to be increased or the distances measured decreased; a clear, crisp target placed at a long distance can look a blurry blob when enlarged (zoomed in) within PhotoModeler.
- Study the effect of digital resolution on photogrammetry more closely. To date, no one has published on this topic in the accident reconstruction community. It is especially important since these days, most accident scenes and vehicles are documented with digital cameras. Each day brings new digital cameras to the market. This study utilized the same digital camera (at 5 mega pixels) at two levels of resolution (at 5 MP and 0.15 MP ). Perhaps a new experiment could make use of say, a 12 MP camera and the 5 MP in the study.
- Use the benchmark measurement markers more precisely in the photogrammetry experiment. As mentioned before, enhancing the pins with paint, or even develop a
new technique, maybe something like a small flag with a magnetic bottom to place on the pin. There are a host of similar possibilities that could be employed. The author had planned to revamp this part of the experiment before this document was prepared but the airport was the lucky recipient of a grant for new paving projects; the experiment site used in this study was completely repaved. The precisely placed pins are currently under a substantial amount of asphalt. Even the gravel area adjacent to the old asphalt surface (used for the wheel experiment) is now under asphalt. Permission to reuse the site would most likely be granted, but the site would now have to be considerably prepared for future experiments, or a totally new site would have to be located.


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## APPENDIX 1

CAMERA CALIBRATION OF OLYMPUS C-5050 HIGH RESOLUTION

# APPENDIX 1 <br> CAMERA CALIBRATION OF OLYMPUS C-5050 HIGH RESOLUTION 

This Appendix contains details for the camera calibration procedure, however; early in January 2007, the author was the unlucky victim of a hard disk crash. Photos of the Olympus C-5050 calibration project were lost forever (as were other parts of this dissertation), but the PhotoModeler project itself still exists (go figure). So post-calibration camera parameters are still available, but the eight (8) or so images of the calibration grid no longer exist. This is a good situation if you want to process a project, but not so good if you want to communicate the fine aspects of camera calibration.

The author feels that camera calibration can be best explained using photos from her Thesis [115]. The difference between the Thesis and the Dissertation calibration is that the Thesis work utilized a film camera and the Dissertation utilized a digital. While the two calibration procedures are very similar, they do have their differences. Firstly, the film camera calibration requires a film insert, either EOS's two-point fiducial or the nine-point fiducial. A fiducial is
a device that is installed between the lens and the film. So any pictures taken with a fiducial camera will have particular marks in the image. These fiducial marks help PhotoModeler determine the orientation of the camera (i.e., how the camera is positioned at the time of exposure---up, down, sideways, etc.) which is a significant part of the photogrammetric processing. Figure 1 illustrates the twopoint while Figure 2 shows the nine-point fiducial. Fiducials are indicated in red. Note that the two-point fiducial covers the extreme


Figure 1. Two-point fiducial image


Figure 2. Nine-point fiducial image
left side of the photo, while the nine-point fiducial covers the entire film plane. Figure 2's right-most fiducials are not well seen; this is indicated with the red dashes. A situation like this is no cause for alarm; all nine are not required to be visible in the photograph when using the nine-point insert (when using a two-point fiducial insert, both fiducials must be visible-if only one is marked, then that photo won't be processed by PhotoModeler). In fact, it is quite commonplace to have one or more fiducials covered by dark areas. PhotoModeler requires a minimum of three (3) fiducials, however;
the placement of the fiducials, whether it be three (3) or more, requires some precision [21]. Figure 3 illustrates these requirements.

This particular Appendix is entitled "Camera Calibration of Olympus C-5050, High Resolution". The distinction "High Resolution" was identified as such to differentiate this particular Appendix from Appendix 13, which is associated with Part 3's work. Appendix 1 involves images taken at a $2560 \times 1920$ resolution, which ends up


These are good fiducial configurations, however;

these are not. More than one-third of the image must be covered, i.e., more than a single row or column must be visible.

Figure 3. Good/Bad Fiducial Configurations Source: PhotoModeler Help Files
being a 1.02 MB file. Appendix 13's images are taken at a 1024 x 768 resolution, which ends up being a 0.148 MB file. The resolution used in this appendix is the default setting on the Olympus C-5050, which is the second highest resolution the camera can generate.

It is notable to mention that the Thesis work calibration was performed with PhotoModeler's Camera Calibrator 3.1; the version used in this work is Camera Calibrator 4.0 g . When working with digital cameras, the process of scanning photos has been completely circumvented and there is no need for the film plane insert. The calibration procedures are essentially the same; the calibrator procedural differences in working with film vs. digital makes them a little dissimilar; though, the buttons and drop down menus on Calibrator 3.1 and 4.0 g are exactly the same.

## Overview

Camera calibration involves the projection of a special grid pattern onto a flat wall, which is free of textures. This is generally done by a slide projector. PhotoModeler's software package includes this calibration slide. Pictures are then taken of the slide from eight
(8) different positions: upper, middle, lower and middle vertical on both the left and right sides. Next is the transmission of the digital photos from the camera to the computer. After that, points are marked and the calibration process begins. If the processing is successful, then the camera is calibrated and can be used as a measurement device with PhotoModeler.

## Prepare for Picture Day

Several preparations were made prior to taking photographs of the calibration slide. First, a uniform, flat wall (free of wallpaper) was located. The wall also needs to be as large as possible; 12 ft by 15 ft were the dimensions of the wall used in this calibration project. Also obtained was a slide projector which projected the image onto the wall. The projector used had an adjustment that allowed the image to become as square as possible; this is very important in the calibration process. Figure 4 and Table 1 shoes the values required and obtained, respectively, for squareness verification of the calibration image. A check of Figure 4 reveals that the squareness requirements were indeed fulfilled.


Figure 4. Squareness Verification Equations Source: EOS Systems, Inc.

Squareness Verification Data

| $A=69$ inches | $C=45.625$ inches |
| :--- | :--- |
| $B=68.5$ inches | $D=45.375$ inches |
| $\|A-B\|<A / 40$ | $\|C-D\|<C / 40$ |
| $\|.5\|<69 / 40$ | $\|.25\|<45.625 / 40$ |
| $\|.5\|<1.725$ | $\|.25\|<1.14$ |
|  |  |

Table 1. Squareness Verification Data

Next, a ladder was collected. The ladder was used to allow the user to take pictures of the upper corners of the calibration slide. The ladder used in this project was 4 ft tall. To successfully project the calibration image onto the wall, the room itself needed to be dark; overhead lights ruin the effectiveness or crispness of the image.

Finally, the author found it useful to counteract the harshness of the flash by turning the flash down by navigating through a series of menus on the Olympus C-5050. If this step were not competed, the flash would cause vital parts of the photo of the calibration slide to become washed out, and hence, unusable.

## Take Pictures

As mentioned previously, eight (8) pictures need to be taken of the calibration image on the wall. First, the pictures of the left side were taken, upper left, middle left, middle left vertical, and bottom left. Then the pictures on the right side were taken in a similar manner. To be safe, more than eight (8) pictures were taken, and the best ones were selected at a later time. Figure 5 shows some of the various photograph positions used in this calibration project.


Figure 5. Various Calibration Photos

## Select Pictures

After the pictures were taken, the photos were downloaded onto the computer. The best pictures were selected for the calibration project. Pictures selected had the entire calibration slide in the photograph and were of the needed orientation (upper left, lower right, etc.) The images were given a name, saved, and put into a directory which could be easily found by the user, usually on the desktop.

## Start the Calibration Project

For a Windows operated PC, go to Start, Programs,
PhotoModeler, and then Camera Calibrator 4.0. Once the Camera
Calibrator is open, go to File and New Camera Calibration. A Wizard appears on the screen. The Wizard outlines the steps needed in the camera calibration project; refer to Figure 6 for this information.


Figure 6. Camera Calibrator Wizard

Next the camera information, such as camera name (Olympus C-5050), type of camera (digital), focal length, and image resolution size that was used was entered into the Wizard. Then the images were loaded into the program by finding the correct directory.

## Mark Points

First, the four (4) control points were marked on all photos. Notice that each control point (1,2,3, and 4) has its own button on the tool bar at the top of the screen which corresponds to a unique control point on each image. Figure 7 shows marked control points.

## Scale the Calibration Project

The Camera Calibrator requires that a distance on the projected image be known. This required distance is the diagonal between control points \#1 and \#4. A flexible tape measure was physically taped on the wall between control points \#1 and \#4 and the distance was determined. The Set Scale Dialog (retrieved under the Calibration menu) was brought up and the appropriate distance was entered. Note that control points \#1 and \#4 are highlighted in green. See figure 8 for this information.


Figure 7. Marked Control Points


Figure 8. Scaling the Calibration Project

## Process the Project

Once all the photographs have been appropriately marked and a scale distance has been determined, the actual calibration process can proceed. Under the Calibration menu, select Calibrate. This is usually a time consuming process, although necessary. If calibration is successful, the Camera Calibrator will finish with an error dialog.

Refer to Figure 9 for this project's error dialog.


Figure 9. Error Dialog for Calibration Project

## Check the Parameters

After the processing has been completed, check to see what the actual camera parameters are. For example, the initial focal length entered in this project was 38 mm (a value retrieved directly from the camera), but after calibration, the focal length was found to be 40.9076 mm. The Camera Calibrator certainly does detect variances in these parameters. Notice in Figure 10 that other camera parameters have been solved as well. Now the camera is a suitable measurement device with PhotoModeler software.


[^0]Figure 10. Solved Camera Information Olympus C-5050

The previous two figures (\#9 and \#10) are actually from the calibration of the Olympus C-5050. Apparently, these photos endured despite the hard disk crash. One should note that the final calibrated values for the Pentax and the Olympus are quite different; this is because the focal length for film and digital cameras are differentiated using a totally different system. For a digital camera, PhotoModeler wants the value directly off of the camera itself, and not the 35 mm equivalent. Figure 11 is another screenshot that survived the hard disk crash. Notice how there are no fiducials for a digital camera.


Figure 11. A Surviving Digital Camera Calibration Screenshot

## APPENDIX 2

## RESULTANT SCREENSHOTS "BETWEEN" STUDY

Case 1. '02 Cadillac De Ville


Case 2. '03 Mercedes E320


Case 3. '01 Buick LeSabre



Case 4. '03 Toyota Avalon



Case 5. '02 Audi A4


Case 6. '03 Hyundai Accent


Case 7. '01 Chevy Malibu

## Missing Due To Hard Disk Crash

Case 8. '03 Honda S2000


| 4 start |  |  | $\square$ custastifents | 匈Mrsast Excl-20... | (8) 12004 |
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Case 9. '02 Mini Cooper


Case 10. '03 Toyota Corolla


Case 11. '02 Chrysler PT


Case 12. '02 Ford Explorer Sport



Case 13. '02 Nissan Pathfinder

## Missing Due To Hard Disk Crash

Case 14. '02 Toyota Highlander


Case 15. '03 Subaru Forester


Case 16. '02 Dodge Ram 1500


Case 17. '01 Nissan Frontier


Case 18. '03 Chevy Silverado


Case 19. '01 Dodge Wagon Van


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Case 20. '01 Dodge Caravan
 File Edit Marking Referencing Project Display Window Help

A|x


## APPENDIX 3

## SPREADSHEETS CONTAINING INITIAL COMPUTATIONS OF CRUSH COEFFICIENTS

(USING $\mathrm{b}_{0}=5 \mathrm{MPH}$ )

## Case 1. '02 Cadillace De Ville

Crash Test Information
2002 Cadillac DeVille case \#1

Impact velocity of test:
Maximum speed w/o permanent damage: (bO
Crush measurements from crash test report:
17.6378 in (c1)
20.31496 in (c2)
23.46457 in (c3)
22.99213 in (c4)
20.70866 in (c5)
18.38583 in (c6)

Average crush amount
Test vehicle weight
Width of crush damage

A $\quad 384.5497$
B $\quad 110.4529$

## Case 2. '03 Mercedes E320

Crash Test Information

$$
2003 \text { Mercedes E320 } \quad \text { case \#2 }
$$

Impact velocity of test:
Maximum speed w/o permanent damage: (b0
35.20071 mph
56.65 kph

Crush measurements from crash test repor

| 15.31496 in (c1) | $389 \mathrm{~mm} \mathrm{(c1)}$ |
| :--- | :--- |
| 19.88189 in (c2) | $505 \mathrm{~mm} \mathrm{(c2)}$ |
| 22.83465 in (c3) | $580 \mathrm{~mm} \mathrm{(c3)}$ |
| 22.67717 in (c4) | $576 \mathrm{~mm} \mathrm{(c4)}$ |
| 19.76378 in (c5) | $502 \mathrm{~mm} \mathrm{(c5)}$ |
| 13.97638 in (c6) | $355 \mathrm{~mm} \mathrm{(c6)}$ |


| Average crush amount | 19.0748 in |  |
| :--- | :---: | :---: |
| Test vehicle weight | 4265.945 lbs | 1935 kg |
| Width of crush damage | 71.34646 in | 1990 mm |

b1 1.583277

A $\quad 362.6139$
B $\quad 109.7281$

## Case 3. '01 Buick LeSabre

Crash Test Information

## 2001 Buick LeSabre

| Impact velocity of test: | 35.10129 mph | 56.49 kph |
| :---: | :---: | :---: |
| Maximum speed w/o permanent damage: (bC | 5 mph |  |
| Crush measurements from crash test report: | 13.77953 in (c1) | 350 mm (c1) |
|  | 20.59055 in (c2) | 523 mm (c2) |
|  | 23.74016 in (c3) | 603 mm (c3) |
|  | 23.0315 in (c4) | 585 mm (c4) |
|  | 20.94488 in (c5) | 532 mm (c5) |
|  | 16.73228 in (c6) | 425 mm (c6) |
| Average crush amount | 19.80315 in |  |
| Test vehicle weight | 4102.803 lbs | 1861 kg |
| Width of crush damage | 67.50394 in | 1867 mm |
| slope of line (b1) | 1.520025 |  |
| A | $354.0464 \mathrm{lb} / \mathrm{in}$ |  |
| B | $102.9059 \mathrm{lb} / \mathrm{in}^{\wedge} 2$ |  |

## Case 4. '03 Toyota Avalon

Crash Test Information

## 2001 Toyota Avalon

Impact velocity of test:
Maximum speed w/o permanent damage: (bO

Crush measurements from crash test report:
13.11024 in (c1)
21.5748 in (c2)
22.24409 in (c3)
22.48031 in (c4)
22.24409 in (c5)
15.19685 in (c6)
19.47507 in

Test vehicle weight

Width of crush damage
3880.136 lbs
71.65354 in
56.49 kph

333 mm (c1)
548 mm (c2)
565 mm (c3)
571 mm (c4)
565 mm (c5)
386 mm (c6)

1760 kg

1820 mm

| A | 347.1733 |
| :--- | :--- |
| B | 101.7597 |

Case 5. '02 Audi A4
Crash Test Information

| Impact velocity of test: | 35.00187 mph | 56.33 kph |
| :---: | :---: | :---: |
| Maximum speed w/o permanent damage: (bC | 5 mph |  |
| Crush measurements from crash test report: | 11.49606 in (c1) | 292 mm (c1) |
|  | 16.06299 in (c2) | 408 mm (c2) |
|  | 19.01575 in (c3) | 483 mm (c3) |
|  | 19.25197 in (c4) | 489 mm (c4) |
|  | 17.00787 in (c5) | 432 mm (c5) |
|  | 12.3622 in (c6) | 314 mm (c6) |
| Average crush amount | 15.86614 in |  |
| Test vehicle weight | 4012.413 lbs | 1820 kg |
| Width of crush damage | 69.25984 in | 1937 mm |
| slope of line (b1) | 1.890937 |  |
| A | $418.3359 \mathrm{lb} / \mathrm{in}$ |  |
| B | $150.7293 \mathrm{lb} / \mathrm{in}^{\wedge} 2$ |  |

## Case 6. '03 Hyundai Accent

Crash Test Information

| 2003 Hyundai Accent | case \#6 |
| :---: | :---: |
| 34.6974 mph | 55.84 kph |
| 5 mph |  |
| 12.24409 in (c1) | 311 mm (c1) |
| 18.97638 in (c2) | 482 mm (c2) |
| 19.44882 in (c3) | 494 mm (c3) |
| 20 in (c4) | 508 mm (c4) |
| 19.37008 in (c5) | 492 mm (c5) |
| 16.41732 in (c6) | 417 mm (c6) |
| 17.74278 in |  |
| 2914.511 lbs | 1322 kg |
| 65.90551 in | 1674 mm |

A
319.6495
B $\quad 103.041$

## Case 7. '01 Chevy Malibu

Crash Test Information

| Impact velocity of test: | 34.52341 mph | 55.56 kph |
| :---: | :---: | :---: |
| Maximum speed w/o permanent damage: (bC | 5 mph |  |
| Crush measurements from crash test report: | 16.02362 in (c1) | 407 mm (c1) |
|  | 16.22047 in (c2) | 412 mm (c2) |
|  | 22.00787 in (c3) | 559 mm (c3) |
|  | 21.88976 in (c4) | 556 mm (c4) |
|  | 21.06299 in (c5) | 535 mm (c5) |
|  | 16.77165 in (c6) | 426 mm (c6) |
| Average crush amount | 18.99606 in |  |
| Test vehicle weight | 3545.033 lbs | 1608 kg |
| Width of crush damage | 63.29134 in | 1760 mm |
| slope of line (b1) | 1.554186 |  |


| A | $339.6382 \mathrm{lb} / \mathrm{in}$ |
| :--- | :--- |
| B | $102.7611 \mathrm{lb} / \mathrm{in}^{\wedge} 2$ |

Case 8. '03 Honda S2000
Crash Test Information

Impact velocity of test:
Maximum speed w/o permanent damage: (bO
Crush measurements from crash test report:
35.39955 mph

5 mph
0.354331 in (c1)

9 mm (c1)

Average crush amount
Test vehicle weight
Width of crush damage

## 2001 Chevy Malibu

407 mm (c1)
412 mm (c2)
559 mm (c3)
556 mm (c4)
535 mm (c5)
426 mm (c6)

1608 kg
1760 mm
15.94488 in (c2)
20.43307 in (c3)
21.45669 in (c4)
16.73228 in (c5)
1.692913 in (c6)
12.76903 in 405 mm (c2) 519 mm (c3) 545 mm (c4) 425 mm (c5) 43 mm (c6)
3229.772 lbs

1465 kg
67.59843 in

1717 mm

| A | 429.5746 |
| :--- | :--- |
| B | 172.7581 |

## Case 9. '02 Mini Cooper

Crash Test Information

2002 Mini Cooper $\quad$ case \#9
34.89623 mph

5 mph
Maximum speed w/o permanent damage: (bc
Crush measurements from crash test report:
7.834646 in (c1)
10.43307 in (c2)
13.38583 in (c3)
13.85827 in (c4)
12.20472 in (c5)
6.220472 in (c6)

Average crush amount

| Test vehicle weight |  | 3095.29 |
| :--- | ---: | ---: |
| Width of crush damage |  | 66.45669 |
|  | A | 548.1057 |
|  | B | 287.9386 |

Case 10. '03 Toyota Corolla
Crash Test Information
Impact velocity of test:
Maximum speed w/o permanent damage: (bC
34.74089 mph

5 mph
Crush measurements from crash test report:
15.11811 in (c1)
20.86614 in (c2)
22.08661 in (c3)
21.88976 in (c4)
20.98425 in (c5)
16.9685 in (c6)

384 mm (c1)
530 mm (c2)
561 mm (c3)
556 mm (c4)
533 mm (c5)
431 mm (c6)
Average crush amount
19.65223 in

Test vehicle weight
Width of crush damage
2976.241 lbs

1350 kg
63.6063 in

1768 mm
slope of line (b1)
1.51336

| A | $273.7813 \mathrm{lb} / \mathrm{in}$ |
| :--- | ---: |
| B | $79.9303 \mathrm{lb} / \mathrm{in}^{\wedge} 2$ |

Case 11. '02 Chrysler PT Cruiser
Crash Test Information
35.00187 mph

5 mph
Maximum speed w/o permanent damage: (b0
Crush measurements from crash test report: 11.14173 in (c1) 283 mm (c1)

$$
\begin{aligned}
& 14.29134 \text { in (c2) } \\
& 18.58268 \text { in (c3) } \\
& 19.05512 \text { in (c4) } \\
& 15.11811 \text { in (c5) } \\
& 10.31496 \text { in (c6) }
\end{aligned}
$$

Average crush amount 14.75066 in
Test vehicle weight
Width of crush damage
3723.608 Ibs
67.08661 in
$\begin{array}{ll}\text { A } & 430.2808 \\ \text { B } & 165.9806\end{array}$
56.33 kph

363 mm (c2)
472 mm (c3)
484 mm (c4)
384 mm (c5)
262 mm (c6)

1689 kg
1704 mm

Case 12. '02 Ford Explorer Sport
Crash Test Information
2002 Ford Explorer Sport

| Impact velocity of test: | 34.560693 mph | 55.62 kph |
| :---: | :---: | :---: |
| Maximum speed w/o permanent damage: (b0 | 5 mph |  |
| Crush measurements from crash test report: | 14.094488 in (c1) | 358 mm (c1) |
|  | 14.724409 in (c2) | 374 mm (c2) |
|  | 14.92126 in (c3) | 379 mm (c3) |
|  | 14.96063 in (c4) | 380 mm (c4) |
|  | 14.92126 in (c5) | 379 mm (c5) |
|  | 13.937008 in (c6) | 354 mm (c6) |
| Average crush amount | 14.593176 in |  |
| Test vehicle weight | 4572.3873 lbs | 2074 kg |
| Width of crush damage | 71.889764 in | 1826 mm |
| $\begin{aligned} & \text { A } \\ & \text { B } \end{aligned}$ | $\begin{array}{r} 567.634 \\ 228.1612 \end{array}$ |  |

## Case 13. '02 Nissan Pathfinder

Crash Test Information

| Impact velocity of test: | 34.89623 mph | 56.16 kph |
| :---: | :---: | :---: |
| Maximum speed w/o permanent damage: (bO | 5 mph |  |
| Crush measurements from crash test report: | 14.6063 in (c1) | 371 mm (c1) |
|  | 22.87402 in (c2) | 581 mm (c2) |
|  | 24.6063 in (c3) | 625 mm (c3) |
|  | 23.93701 in (c4) | 608 mm (c4) |
|  | 22.3622 in (c5) | 568 mm (c5) |
|  | 13.4252 in (c6) | 341 mm (c6) |
| Average crush amount | 20.30184 in |  |
| Test vehicle weight | 4720.097 lbs | 2141 kg |
| Width of crush damage | 64.65354 in | 1820 mm |
| slope of line (b1) | 1.472588 |  |

A
399.6121
B $\quad 110.8298$

## Case 14. '02 Toyota Highlander

| Crash Test Information |  |
| :---: | :---: |
| Impact velocity of test: | 34.68497 |
| Maximum speed w/o permanent damage: (bo | 5 |
| Crush measurements from crash test report: | 16.41732 |
|  | 19.13386 |
|  | 19.68504 |
|  | 19.33071 |
|  | 18.38583 |
|  | 14.80315 |
| Average crush amount | 17.95932 |
| Test vehicle weight | 4455.542 |
| Width of crush damage | 69.04724 |
| A | 416.9089 |
| B | 134.3082 |

## Case 15. '03 Subaru Forester

Crash Test Information
2003 Subaru Forester case \#15
Impact velocity of test:
35.39955 mph
56.97 kph

Maximum speed w/o permanent damage: (b0
5 mph

| Crush measurements from crash test report: | 12.24409 in (c1) | 311 mm (c1) |
| :---: | :---: | :---: |
|  | 18.97638 in (c2) | 482 mm (c2) |
|  | 19.44882 in (c3) | 494 mm (c3) |
|  | 20 in (c4) | 508 mm (c4) |
|  | 19.37008 in (c5) | 492 mm (c5) |
|  | 16.41732 in (c6) | 417 mm (c6) |

Average crush amount
17.74278 in

Test vehicle weight
3615.581 lbs

1640 kg

Width of crush damage
61.30709 in

1735 mm

| A | 390.0143 |
| :--- | :--- |
| B | 128.6961 |

## Case 16. '02 Dodge Ram 1500

| Crash Test Information | 2002 Dodge Ram 1500 | case \#16 |
| :---: | :---: | :---: |
| Impact velocity of test: | 35.10129 mph | 56.49 kph |
| Maximum speed w/o permanent damage: (b0 | 5 mph |  |
| Crush measurements from crash test report: | 10.86614 in (c1) | 276 mm (c1) |
|  | 17.83465 in (c2) | 453 mm (c2) |
|  | 21.5748 in (c3) | 548 mm (c3) |
|  | 21.5748 in (c4) | 548 mm (c4) |
|  | 17.91339 in (c5) | 455 mm (c5) |
|  | 11.06299 in (c6) | 281 mm (c6) |
| Average crush amount | 16.80446 in |  |
| Test vehicle weight | 5551.24 lbs | 2518 kg |
| Width of crush damage | 72.88189 in | 2029 mm |
| A | 511.3374 |  |
| B | 171.2839 |  |

## Case 17. '01 Nissan Frontier

Crash Test Information

| Impact velocity of test: | 34.89002 mph | 56.15 kph |
| :---: | :---: | :---: |
| Maximum speed w/o permanent damage: (bO | 5 mph |  |
| Crush measurements from crash test report: | 11.88976 in (c1) | 302 mm (c1) |
|  | 20.55118 in (c2) | 522 mm (c2) |
|  | 23.0315 in (c3) | 585 mm (c3) |
|  | 23.14961 in (c4) | 588 mm (c4) |
|  | 21.45669 in (c5) | 545 mm (c5) |
|  | 11.85039 in (c6) | 301 mm (c6) |
| Average crush amount | 18.65486 in |  |
| Test vehicle weight | 4521.681 lbs | 2051 kg |
| Width of crush damage | 64.1811 in | 1808 mm |
| slope of line (b1) | 1.602265 |  |


| A | $426.772 \mathrm{lb} / \mathrm{in}$ |
| :--- | :--- |
| B | $127.487 \mathrm{lb} / \mathrm{in}^{\wedge} 2$ |

Case 18. '03 Chevy Silverado
Crash Test Information
2003 Chevy Silverado case \#18

Impact velocity of test:
Maximum speed w/o permanent damage: (b0
34.73468 mph
55.9 kph

Crush measurements from crash test report:
20.23622 in (c1)

514 mm (c1)
23.34646 in (c2)

593 mm (c2)
25.07874 in (c3)

637 mm (c3)
25.47244 in (c4) 647 mm (c4)
23.70079 in (c5) 602 mm (c5)
21.06299 in (c6) 535 mm (c6)

Average crush amount
23.14961 in

Test vehicle weight
5200.705 lbs

2359 kg
Width of crush damage
71.26772 in

1988 mm

| A | 367.7621 |
| :--- | ---: |
| B | 92.4775 |



## APPENDIX 4

## SPREADSHEETS FOR CRUSH COEFFICIENT SENSITIVITY ANALYSIS






| 2002 Audi A4 |  | case \#5 |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| A = | $418.3359 \mathrm{lb} / \mathrm{in}$ |  | A $=$ | $400.7307 \mathrm{lb} / \mathrm{in}$ | $A=$ |  | $382.7769 \mathrm{lb} / \mathrm{in}$ | A $=$ |  | $364.4746 \mathrm{lb} / \mathrm{in}$ | $A=$ | $\begin{aligned} & 345.8236 \mathrm{lb} / \mathrm{in}^{2} \\ & 160.9448 \mathrm{lb} / \mathrm{in}^{*} 2 \end{aligned}$ |
| $B=$ | 150 | $\mathrm{lb} / \mathrm{in} * 2$ | $B=$ | $153.2518 \mathrm{lb} / \mathrm{in}^{*} 2$ |  | $B=$ | $155.7952 \mathrm{Ib} / \mathrm{in}^{*} 2$ |  | $B=$ | $158.3595 \mathrm{Ib} / \mathrm{in}^{*} 2$ | $B=$ |  |
| W (width of crı | 69.2598 |  | W ( | 69.25984252 in |  | W (width of | 69.25984 in |  | W (width of | 69.25984 in | W (width o | 69.25984 in |
| c1 = | 11.4960 |  | $\mathrm{c} 1=$ | 11.49606299 in |  | c1 = | 11.49606 in |  | c1 $=$ | 11.49606 in | c1 = | 11.49606 in |
| c2 = | 16.0629 |  | c2 = | 16.06299213 in |  | c2 = | 16.06299 in |  | c2 = | 16.06299 in | c2 = | 16.06299 in |
| c3 $=$ | 19.0157 |  | c3 $=$ | 19.01574803 in |  | c3 $=$ | 19.01575 in |  | c3 $=$ | 19.01575 in | c3 = | 19.01575 in |
| c4 $=$ | 19.251 |  | c4 $=$ | 19.2519685 in |  | c4 = | 19.25197 in |  | c4 = | 19.25197 in | c4 = | 19.25197 in |
| c5 = | 17.0078 |  | c5 $=$ | 17.00787402 in |  | c5 = | 17.00787 in |  | c5 = | 17.00787 in | c5 = | 17.00787 in |
| c6 = | 12.3622 |  | c6 $=$ | 12.36220472 in |  | c6 = | 12.3622 in |  | c6 = | 12.3622 in | c6 = | 12.3622 in |
| $\theta=$ |  | degrees | $\theta=$ | 0 degrees |  | $\theta=$ | 0 degrees |  | $\theta=$ | 0 degrees | $\theta=$ | 0 degrees |
| G = | 580.527 | lbs | G = | 523.9256372 lbs |  | G = | 470.2268 lbs |  | $\mathrm{G}=$ | 419.4309 lbs | $\mathrm{G}=$ | 371.5372 lbs |
| $\mathrm{E}=$ | 199745 | in-lbs | $\mathrm{E}=$ | 1997903.634 in-lbs |  | $\mathrm{E}=$ | 1998361 in-lbs |  | $\mathrm{E}=$ | 1998821 in-lbs | E= | 1999286 in-lbs |
| E= | 166454 | ft -lbs | E= | $166491.9695 \mathrm{ft}-\mathrm{lbs}$ |  | E= | $166530.1 \mathrm{ft-lbs}$ |  | E= | $166568.4 \mathrm{ft}-\mathrm{lbs}$ | E= | $166607.2 \mathrm{ft-lbs}$ |
| $w=$ (weight of | 4012.413172 lbs |  | w = (weigh | 4012.413172 lbs | $w=($ weigh $)$ |  | 4012.413 lbs | $\mathrm{w}=$ ( weight |  | 4012.413 lbs | w = ( weigh | 4012.413 lbs |
| $v=$$v=$ | $51.68772969 \mathrm{ft} / \mathrm{sec}$ $35.07374274 \mathrm{mi} / \mathrm{hr}$ |  | $v=$ | $51.69359731 \mathrm{ft} / \mathrm{sec}$ |  | $\mathrm{v}=$ | $51.69951 \mathrm{ft} / \mathrm{sec}$ |  | $\mathrm{v}=$ | $51.70547 \mathrm{ft} / \mathrm{sec}$ | $\mathrm{v}=$ | $51.71148 \mathrm{ft} / \mathrm{sec}$ |
|  |  |  | $v=$ | $35.07772433 \mathrm{mi} / \mathrm{hr}$ |  | $v=$ | $35.08174 \mathrm{mi} / \mathrm{hr}$ |  | $v=$ | $35.08578 \mathrm{mi} / \mathrm{hr}$ | $v=$ | $35.08986 \mathrm{mi} / \mathrm{hr}$ |
| $\begin{aligned} & \text { bo= } \\ & 5.0 \mathrm{mph} \end{aligned}$ |  |  |  |  |  | bo= 4.5 mph |  |  | $\begin{aligned} & \mathrm{bo}= \\ & 4.25 \\ & \mathrm{mph} \\ & \hline \end{aligned}$ |  | $\begin{aligned} & \text { bo= } \\ & 4.0 \mathrm{mph} \end{aligned}$ |  |
| $56.33 \mathrm{~km} / \mathrm{h}$ is equal to 35.0018673 mph |  |  |  |  | A average | $425.5698 \mathrm{lb} / \mathrm{in}$ |  | $B$ average | $149.5623 \mathrm{lb} / \mathrm{in}^{*} 2$ |  | $\mathbf{v}$ average $=35.0719$ | $35.0719 \mathrm{mi} / \mathrm{hr}$ |
| A $=$ | 435 | $\mathrm{lb} / \mathrm{in}$ | $A=$ | $452.5004 \mathrm{lb} / \mathrm{in}$ |  | $A=$ | $469.0598 \mathrm{lb} / \mathrm{in}$ |  | $A=$ | $485.2706 \mathrm{lb} / \mathrm{in}$ | $A=$ | $501.1329 \mathrm{lb} / \mathrm{in}$ |
| $B=$ | 148 | lb/in*2 | $B=$ | $145.7472 \mathrm{lb} / \mathrm{in}^{*} 2$ |  | $B=$ | $143.2875 \mathrm{lb} / \mathrm{in}^{*} 2$ |  | $B=$ | $140.8488 \mathrm{lb} / \mathrm{in}^{*} 2$ | $B=$ | $138.431 \mathrm{lb} / \mathrm{in}^{*} 2$ |
| W (width of crı | 69.25984252 in |  | W (width of 69.25984252 in |  |  | W (width of | 69.25984 in |  | W (width of | 69.25984 in | W (width o | 69.25984 in |
| c1 = | 11.49606299 in |  | c1 $=\quad 11.49606299$ in |  |  | c1 = | 11.49606 in |  | c1 = | 11.49606 in | c1 = | 11.49606 in |
| c2 = | 16.06299213 in |  | $\mathrm{c} 2=$ | 16.06299213 in |  | c2 = | 16.06299 in |  | c2 = | 16.06299 in | c2 = | 16.06299 in |
| c3 $=$ | 19.01574803 in |  |  | 19.01574803 in |  | c3 $=$ | 19.01575 in |  | c3 = | 19.01575 in | c3 = | 19.01575 in |
| c4 $=$ | 19.2519685 in |  | c3 $=$ | 19.2519685 in |  | c4 = | 19.25197 in |  | c4 = | 19.25197 in | c4 = | 19.25197 in |
| c5 = | 17.00787402 in |  | c5 = | 17.00787402 in |  | c5 = | 17.00787 in |  | c5 = | 17.00787 in | c5 = | 17.00787 in |
| c6 = | 12.36220472 in |  | c6 = | 12.36220472 in |  | c6 = | 12.3622 in |  | c6 = | 12.3622 in | c6 = | 12.3622 in |
| $\theta=$ |  | degrees | $\begin{aligned} & \theta= \\ & \mathrm{G}= \end{aligned}$ | 0 degrees |  | $\theta=$ | 0 degrees |  | $\theta=$ | 0 degrees | $\theta=$ | 0 degrees |
| $\mathrm{G}=$ | 640.0308813 lbs |  |  | 702.4375494 lbs |  | G = | 767.747 lbs |  | $\mathrm{G}=$ | 835.9587 lbs | G = | 907.0735 lbs |
| E = | 1997000.838 in-lbs |  | $\mathrm{E}=$ | $\begin{aligned} & 1996555.149 \mathrm{in}-\mathrm{lbs} \\ & 166379.5957 \mathrm{ft}-\mathrm{lbs} \end{aligned}$ |  | $E=$ | 1996113 in-lbs166342.7 ft -lbs |  | E= | 1995675 in-lbs$166306.3 \mathrm{ft-lbs}$ | E= | $1995241 \mathrm{in-lbs}$166270.1 ft -lbs |
| E= | 166416 | ft -lbs | E= |  |  | E= |  |  |  |  | E= |  |
| $w=$ (weight of | 4012.413172 lbs |  | $\mathrm{w}=$ ( weigh | 4012.413172 lbs |  | w $=$ ( weight | 4012.413 lbs |  | w = (weight | 4012.413 lbs | $\mathrm{w}=$ ( weigh | 4012.413 lbs |
| v= | $51.68191655 \mathrm{ft} / \mathrm{sec}$ $35.06979811 \mathrm{mi} / \mathrm{hr}$ |  | $v=$$v=$ | $\begin{aligned} & 51.67614907 \mathrm{ft} / \mathrm{sec} \\ & ] 5.06588447 \mathrm{mi} / \mathrm{hr} \end{aligned}$ | v= |  | $\begin{gathered} 51.67043 \mathrm{ft} / \mathrm{sec} \\ 35.062 \mathrm{mi} / \mathrm{hr} \end{gathered}$ |  | $v=$ | $51.66476 \mathrm{ft} / \mathrm{sec}$ | $\mathrm{v}=$ | $51.65914 \mathrm{ft/sec}$$35.05434 \mathrm{mi} / \mathrm{hr}$ |
|  |  |  |  |  |  |  | $v=$ | $35.05815 \mathrm{mi} / \mathrm{hr}$ | $v=$ |  |  |
|  | $\begin{aligned} & \text { bo= } \\ & 5.25 \\ & \text { mph } \end{aligned}$ |  |  |  |  |  |  | $\begin{aligned} & \mathrm{bo}= \\ & 5.75 \\ & \mathrm{mph} \end{aligned}$ |  |  | $\begin{aligned} & \text { bo }= \\ & 6.0 \mathrm{mph} \end{aligned}$ |  | $\begin{aligned} & \mathrm{bo}= \\ & 6.25 \\ & \mathrm{mph} \\ & \hline \end{aligned}$ |  |






| A = | $273.7813 \mathrm{lb} / \mathrm{in}$ | A $=$ | $262.2785 \mathrm{lb} / \mathrm{in}$ |  | A = | $250.5456 \mathrm{lb} / \mathrm{in}$ |  | A $=$ | $238.5826 \mathrm{lb} / \mathrm{in}$ | A $=$ | 226.3894 Ib/in |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $B=$ | $79.9303 \mathrm{lb} / \mathrm{in}^{*} 2$ | $B=$ | $81.2797 \mathrm{lb} / \mathrm{in}^{*} 2$ |  | $B=$ | $82.6404 \mathrm{lb} / \mathrm{in}^{*} 2$ |  | $B=$ | $84.0124 \mathrm{lb} / \mathrm{in}^{*} 2$ | $\mathrm{B}=$ | $85.3957 \mathrm{lb} / \mathrm{in}^{*} 2$ |
| W (width of crı | 63.60629921 in | W (width ot | 63.60629921 in |  | W (width of | 63.6063 in |  | W (width of | 63.6063 in | W (width o | 63.6063 in |
| c1 = | 15.11811024 in | c1 = | 15.11811024 in |  | c1 = | 15.11811 in |  | c1 = | 15.11811 in | c1 = | 15.11811 in |
| c2 = | 20.86614173 in | c2 = | 20.86614173 in |  | c2 = | 20.86614 in |  | c2 = | 20.86614 in | c2 = | 20.86614 in |
| c3 $=$ | 22.08661417 in | c3 = | 22.08661417 in |  | c3 $=$ | 22.08661 in |  | c3 = | 22.08661 in | c3 $=$ | 22.08661 in |
| c4 $=$ | 21.88976378 in | c4 = | 21.88976378 in |  | c4 $=$ | 21.88976 in |  | c4 $=$ | 21.88976 in | c4 $=$ | 21.88976 in |
| c5 = | 20.98425197 in | c5 = | 20.98425197 in |  | c5 = | 20.98425 in |  | c5 = | 20.98425 in | c5 = | 20.98425 in |
| c6 = | 16.96850394 in | c6 = | 16.96850394 in |  | c6 = | 16.9685 in |  | c6 = | 16.9685 in | c6 = | 16.9685 in |
| $\theta=$ | 0 degrees | $\theta=$ | 0 degrees |  | $\theta=$ | 0 degrees |  | $\theta=$ | 0 degrees | $\theta=$ | 0 degrees |
| $\mathrm{G}=$ | 468.8847673 lbs | G = | 423.1684637 lbs |  | $\mathrm{G}=$ | 379.7967 lbs |  | $\mathrm{G}=$ | 338.7694 lbs | G = | 300.0863 lbs |
| $\mathrm{E}=$ | 1448398.697 in-lbs | $\mathrm{E}=$ | 1448543.101 in-lbs |  | $\mathrm{E}=$ | 1448689 in-lbs |  | $\mathrm{E}=$ | 1448836 in-lbs | $\mathrm{E}=$ | 1448984 in-lbs |
| E= | 120699.8914 ft -lbs | E= | 120711.9251 ft -lbs |  | E= | 120724.1 ft -lbs |  | E= | 120736.3 ft -lbs | E= | 120748.7 ft -lbs |
| w $=$ ( weight of | 2976.240539 lbs | w = (weigh | 2976.240539 lbs |  | w = (weight | 2976.241 lbs |  | w = (weight | 2976.241 lbs | w = (weigh | 2976.241 lbs |
| $\mathrm{v}=$ | $51.10487842 \mathrm{ft} / \mathrm{sec}$ | $v=$ | $51.10742591 \mathrm{ft} / \mathrm{sec}$ |  | $v=$ | $51.11 \mathrm{ft} / \mathrm{sec}$ |  | $\mathrm{v}=$ | $51.11259 \mathrm{ft} / \mathrm{sec}$ | $\mathrm{v}=$ | $51.11521 \mathrm{ft} / \mathrm{sec}$ |
| $v=$ | $34.67823735 \mathrm{mi} / \mathrm{hr}$ | $v=$ | $34.679966 \mathrm{mi} / \mathrm{hr}$ |  | $v=$ | $34.68171 \mathrm{mi} / \mathrm{hr}$ |  | $v=$ | $34.68347 \mathrm{mi} / \mathrm{hr}$ | $v=$ | $34.68524 \mathrm{mi} / \mathrm{hr}$ |
| bo= <br> 5.0 mph |  | $\begin{aligned} & \hline \text { bo= } \\ & 4.75 \\ & \mathrm{mph} \end{aligned}$ |  |  | bo= 4.5 mph |  |  | $\begin{aligned} & \text { bo= } \\ & 4.25 \\ & \mathrm{mph} \end{aligned}$ |  | bo= 4.0 mph |  |
| 55.91 k | $\mathrm{m} / \mathrm{h}$ is equal to 34.7408912 mph |  |  | A average | 278.497 |  | $B$ average | 79.30638 Ib | b/in*2 | vaverage $=34.67743 \mathrm{n}$ | mi/hr |
| A $=$ | $285.0539 \mathrm{lb} / \mathrm{in}$ | A = | 296.0963 lb/in |  | A $=$ | $306.9087 \mathrm{lb} / \mathrm{in}$ |  | A $=$ | $317.4909 \mathrm{lb} / \mathrm{in}$ | A $=$ | $327.8429 \mathrm{lb} / \mathrm{in}$ |
| $B=$ | $78.5921 \mathrm{lb} / \mathrm{in}^{*} 2$ | $B=$ | $77.2653 \mathrm{lb} / \mathrm{in}^{*} 2$ |  | $B=$ | $75.9498 \mathrm{lb} / \mathrm{in}^{*} 2$ |  | $B=$ | $74.6455 \mathrm{lb} / \mathrm{in}^{*} 2$ | $B=$ | $73.3526 \mathrm{lb} / \mathrm{in}^{*} 2$ |
| W (width of crı | 63.60629921 in | W (width of | 63.60629921 in |  | W (width of | 63.6063 in |  | W (width of | 63.6063 in | W (width o | 63.6063 in |
| c1 = | 15.11811024 in | c1 = | 15.11811024 in |  | c1 = | 15.11811 in |  | c1 = | 15.11811 in | c1 = | 15.11811 in |
| c2 = | 20.86614173 in | c2 = | 20.86614173 in |  | c2 = | 20.86614 in |  | c2 = | 20.86614 in | c2 = | 20.86614 in |
| c3 $=$ | 22.08661417 in | c3 $=$ | 22.08661417 in |  | c3 $=$ | 22.08661 in |  | c3 = | 22.08661 in | c3 $=$ | 22.08661 in |
| c4 $=$ | 21.88976378 in | c4 $=$ | 21.88976378 in |  | c4 $=$ | 21.88976 in |  | c4 $=$ | 21.88976 in | c4 $=$ | 21.88976 in |
| c5 = | 20.98425197 in | c5 = | 20.98425197 in |  | c5 = | 20.98425 in |  | c5 = | 20.98425 in | c5 = | 20.98425 in |
| c6 = | 16.96850394 in | c6 = | 16.96850394 in |  | c6 = | 16.9685 in |  | c6 = | 16.9685 in | c6 = | 16.9685 in |
| $\theta=$ | 0 degrees | $\theta=$ | 0 degrees |  | $\theta=$ | 0 degrees |  | $\theta=$ | 0 degrees | $\theta=$ | 0 degrees |
| $\mathrm{G}=$ | 516.9458884 lbs | G = | 567.3505369 lbs |  | $\mathrm{G}=$ | 620.1001 lbs |  | $\mathrm{G}=$ | 675.1946 lbs | G = | 732.6323 lbs |
| $\mathrm{E}=$ | 1448254.178 in-lbs | $\mathrm{E}=$ | 1448112.122 in-lbs |  | E= | 1447972 in-lbs |  | $\mathrm{E}=$ | 1447831 in-lbs | E = | 1447693 in-lbs |
| E= | 120687.8481 ft -lbs | E= | 120676.0101 ft -lbs |  | E= | 120664.3 ft -lbs |  | E= | 120652.6 ft -lbs | E= | 120641.1 ft -lbs |
| w $=$ ( weight of | 2976.240539 lbs | w = (weigh | 2976.240539 lbs |  | w = (weight | 2976.241 lbs |  | $w=($ weight | 2976.241 lbs | w = (weigh | 2976.241 lbs |
| $v=$ | $51.10232877 \mathrm{ft} / \mathrm{sec}$ | $v=$ | $51.09982245 \mathrm{ft} / \mathrm{sec}$ |  | $v=$ | $51.09734 \mathrm{ft} / \mathrm{sec}$ |  | $v=$ | $51.09486 \mathrm{ft} / \mathrm{sec}$ | $\mathrm{v}=$ | $51.09242 \mathrm{ft} / \mathrm{sec}$ |
| $v=$ | $34.67650723 \mathrm{mi} / \mathrm{hr}$ | $\mathrm{v}=$ | $34.67480652 \mathrm{mi} / \mathrm{hr}$ |  | $\mathrm{v}=$ | $34.67312 \mathrm{mi} / \mathrm{hr}$ |  | $v=$ | $34.67144 \mathrm{mi} / \mathrm{hr}$ | $\mathrm{v}=$ | $34.66978 \mathrm{mi} / \mathrm{hr}$ |
|  | bo $=$ <br> 5.25 <br> mph | bo= <br> 5.5 mph |  |  | $\begin{array}{\|l\|} \hline \text { bo }= \\ 5.75 \\ \mathrm{mph} \\ \hline \end{array}$ |  |  | $\begin{aligned} & \text { bo= } \\ & 6.0 \mathrm{mph} \end{aligned}$ |  | $\begin{aligned} & \mathrm{bo}= \\ & 6.25 \\ & \mathrm{mph} \end{aligned}$ |  |


| 2002 Chrysler PT Cruiser ${ }^{\text {che }}$ case \#1 |  | A $=$ | $412.1729 \mathrm{lb} / \mathrm{in}$ |  | A $=$ | $393.7065 \mathrm{lb} / \mathrm{in}$ |  | A $=$ | $374.8816 \mathrm{lb} / \mathrm{in}$ $174.3829 \mathrm{Ib} / \mathrm{in}^{*} 2$ | A $=$ | $355.6981 \mathrm{lb} / \mathrm{in}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| A = | $430.2808 \mathrm{lb} / \mathrm{in}$ |  |  |  |  |  |  |  |  |  |  |
| $B=$ | $165.9806 \mathrm{Ib} / \mathrm{in}^{*} 2$ | $B=$ | $168.7583 \mathrm{lb} / \mathrm{in}^{*} 2$ |  | $B=$ | $171.5591 \mathrm{lb} / \mathrm{in}^{*} 2$ |  | $B=$ |  | $B=$ |  |
| W (width of crı | 67.08661417 in | W (width of | 67.08661417 in |  | W (width of | 67.08661 in |  | W (width of | 67.08661 in | W (width o | 67.08661 in |
| $\mathrm{c} 1=$ | 11.14173228 in | c1 $=$ | 11.14173228 in |  | c1 $=$ | 11.14173 in |  | c1 = | 11.14173 in | c1 = | 11.14173 in |
| c2 = | 14.29133858 in | c2 = | 14.29133858 in |  | c2 = | 14.29134 in |  | c2 = | 14.29134 in | c2 = | 14.29134 in |
| c3 $=$ | 18.58267717 in | c3 = | 18.58267717 in |  | c3 = | 18.58268 in |  | c3 = | 18.58268 in | c3 = | 18.58268 in |
| c4 $=$ | 19.05511811 in | c4 = | 19.05511811 in |  | c4 = | 19.05512 in |  | c4 = | 19.05512 in | c4 = | 19.05512 in |
| c5 = | 15.11811024 in | c5 = | 15.11811024 in |  | c5 = | 15.11811 in |  | c5 = | 15.11811 in | c5 = | 15.11811 in |
| c6 $=$ | 10.31496063 in | c6 $=$ | 10.31496063 in |  | c6 $=$ | 10.31496 in |  | c6 $=$ | 10.31496 in | c6 = | 10.31496 in |
| $\theta=$ | 0 degrees | $\theta=$ | 0 degrees |  | $\theta=$ | 0 degrees |  | $\theta=$ | 0 degrees | $\theta=$ | 0 degrees |
| G = | 557.7205012 lbs | G = | 503.3426489 lbs |  | G = | 451.7534 lbs |  | $\mathrm{G}=$ | 402.953 lbs | G = | 356.9411 lbs |
| $E=$ | 1873074.349 in-lbs | $\mathrm{E}=$ | 1873735.602 in-lbs |  | $E=$ | 1874403 in-lbs |  | $\mathrm{E}=$ | 1875075 in-lbs | E = | 1875752 in-lbs |
| E= | 156089.5291 ft -lbs | E= | 156144.6335 ft -lbs |  | E= | 156200.2 ft -lbs |  | E= | 156256.3 ft -lbs | E= | 156312.7 ft -lbs |
| w $=$ ( weight of | 3723.607608 lbs | $w=$ (weigh | 3723.607608 lbs |  | $w=$ (weight | 3723.608 lbs |  | w = (weight | 3723.608 lbs | w = (weigh | 3723.608 lbs |
| $\mathrm{v}=$ | $51.95745431 \mathrm{ft} / \mathrm{sec}$ | $\mathrm{v}=$ | $51.96662479 \mathrm{ft} / \mathrm{sec}$ |  | $v=$ | $51.97588 \mathrm{ft} / \mathrm{sec}$ |  | $\mathrm{v}=$ | $51.9852 \mathrm{ft} / \mathrm{sec}$ | $\mathrm{v}=$ | $51.99459 \mathrm{ft} / \mathrm{sec}$ |
| $v=$ | $35.25676977 \mathrm{mi} / \mathrm{hr}$ | $v=$ | $35.26299258 \mathrm{mi} / \mathrm{hr}$ |  | $v=$ | $35.26927 \mathrm{mi} / \mathrm{hr}$ |  | $v=$ | $35.2756 \mathrm{mi} / \mathrm{hr}$ | $v=$ | $35.28197 \mathrm{mi} / \mathrm{hr}$ |
| $\begin{aligned} & \text { bo= } \\ & 5.0 \mathrm{mph} \end{aligned}$ |  | $\begin{aligned} & \hline \text { bo }= \\ & 4.75 \\ & \mathrm{mph} \\ & \hline \end{aligned}$ |  |  | bo= 4.5 mph |  |  | $\begin{array}{\|l\|} \hline \text { bo }= \\ 4.25 \\ \mathrm{mph} \\ \hline \end{array}$ |  | bo= 4.0 mph |  |
| $56.33 \mathrm{~km} / \mathrm{h}$ is equal to 35.0018673 mph |  |  |  | A average | 437.7213 | $\mathrm{b} / \mathrm{in}$ | $B$ average | 164.6955 | $\mathrm{b} / \mathrm{in}$ *2 | v average $=35.25389 \mathrm{~m}$ | mi/hr |
| A = | $448.0301 \mathrm{lb} / \mathrm{in}$ | A $=$ | $465.4209 \mathrm{lb} / \mathrm{in}$ |  | A $=$ | $482.4531 \mathrm{lb} / \mathrm{in}$ |  | A $=$ | $499.1268 \mathrm{lb} / \mathrm{in}$ | A $=$ | $515.442 \mathrm{lb} / \mathrm{in}$ |
| $B=$ | $163.226 \mathrm{lb} / \mathrm{in}^{*} 2$ | $B=$ | $160.4944 \mathrm{lb} / \mathrm{in}^{*} 2$ |  | $B=$ | $157.7858 \mathrm{lb} / \mathrm{in}^{*} 2$ |  | $B=$ | $155.1003 \mathrm{lb} / \mathrm{in}^{*} 2$ | $B=$ | $152.4379 \mathrm{lb} / \mathrm{in}^{*} 2$ |
| W (width of crı | 67.08661417 in | W (width of | 67.08661417 in |  | W (width of | 67.08661 in |  | W (width of | 67.08661 in | W (width o | 67.08661 in |
| c 1 = | 11.14173228 in | c1 $=$ | 11.14173228 in |  | c1 $=$ | 11.14173 in |  | c1 = | 11.14173 in | c1 $=$ | 11.14173 in |
| c2 = | 14.29133858 in | c2 = | 14.29133858 in |  | c2 = | 14.29134 in |  | c2 = | 14.29134 in | c2 = | 14.29134 in |
| c3 $=$ | 18.58267717 in | c3 $=$ | 18.58267717 in |  | c3 $=$ | 18.58268 in |  | c3 $=$ | 18.58268 in | c3 $=$ | 18.58268 in |
| c4 $=$ | 19.05511811 in | c4 $=$ | 19.05511811 in |  | c4 $=$ | 19.05512 in |  | c4 $=$ | 19.05512 in | c4 $=$ | 19.05512 in |
| c5 = | 15.11811024 in | c5 = | 15.11811024 in |  | c5 = | 15.11811 in |  | c5 = | 15.11811 in | c5 = | 15.11811 in |
| c6 = | 10.31496063 in | c6 $=$ | 10.31496063 in |  | c6 $=$ | 10.31496 in |  | c6 = | 10.31496 in | c6 = | 10.31496 in |
| $\theta=$ | 0 degrees | $\theta=$ | 0 degrees |  | $\theta=$ | 0 degrees |  | $\theta=$ | 0 degrees | $\theta=$ | 0 degrees |
| $\mathrm{G}=$ | 614.8866311 lbs | $\mathrm{G}=$ | 674.8416585 lbs |  | $\mathrm{G}=$ | 737.5854 lbs |  | $\mathrm{G}=$ | 803.1176 lbs | $\mathrm{G}=$ | 871.4383 lbs |
| $E=$ | 1872418.922 in-lbs | E = | 1871768.631 in-lbs |  | E = | 1871123 in-lbs |  | $E=$ | 1870484 in-lbs | E = | 1869851 in-lbs |
| E= | 156034.9101 ft -lbs | E= | 155980.7192 ft -lbs |  | E= | 155926.9 ft -lbs |  | E= | $155873.7 \mathrm{ft-lbs}$ | E= | 155820.9 ft -lbs |
| w = (weight of | 3723.607608 lbs | w = (weigh | 3723.607608 lbs |  | w = (weight | 3723.608 lbs |  | w = (weight | 3723.608 lbs | w = (weigh | 3723.608 lbs |
| $v=$ | $51.94836302 \mathrm{ft} / \mathrm{sec}$ | $v=$ | $51.93934141 \mathrm{ft} / \mathrm{sec}$ |  | $v=$ | $51.93039 \mathrm{ft} / \mathrm{sec}$ |  | $v=$ | $51.92152 \mathrm{ft} / \mathrm{sec}$ | $v=$ | $51.91272 \mathrm{ft} / \mathrm{sec}$ |
| $v=$ | $35.25060069 \mathrm{mi} / \mathrm{hr}$ | $v=$ | $35.2444789 \mathrm{mi} / \mathrm{hr}$ |  | $v=$ | $35.2384 \mathrm{mi} / \mathrm{hr}$ |  | $v=$ | $35.23238 \mathrm{mi} / \mathrm{hr}$ | $v=$ | $35.22642 \mathrm{mi} / \mathrm{hr}$ |
|  | bo $=$ <br> 5.25 <br> mph | $\begin{aligned} & \text { bo }= \\ & 5.5 \mathrm{mph} \end{aligned}$ |  |  | $\begin{aligned} & \mathrm{bo}= \\ & 5.75 \\ & \mathrm{mph} \\ & \hline \end{aligned}$ |  |  | bo= 6.0 mph |  | bo= 6.25 mph |  |



2002 Nissan Pathfinder case \#13


2002 Toyota Highlander case \#14

| $\mathrm{A}=$ | $416.9089 \mathrm{lb} / \mathrm{in}$ | $A=$ | $399.399 \mathrm{lb} / \mathrm{in}$ |  | $A=$ | $381.538 \mathrm{lb} / \mathrm{in}$ |  | A $=$ | $363.3259 \mathrm{lb} / \mathrm{in}$ | $A=$ | $344.7627 \mathrm{lb} / \mathrm{in}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $B=$ | $134.3082 \mathrm{lb} / \mathrm{in} * 2$ | $B=$ | $136.5799 \mathrm{lb} / \mathrm{in} * 2$ |  | $B=$ | $138.8708 \mathrm{lb} / \mathrm{in}^{*} 2$ |  | $B=$ | $141.1806 \mathrm{Ib} / \mathrm{in}^{*} 2$ | $\mathrm{B}=$ | $143.5095 \mathrm{lb} / \mathrm{in}^{*} 2$ |
| W (width of crı | 69.04724409 in | W (w | 69.04724409 in |  | W (width of | 69.04724 in |  | W (width of | 69.04724 in | W (width o | 69.04724 in |
| c1 $=$ | 16.41732283 in | c1 = | 16.41732283 in |  | c1 $=$ | 16.41732 in |  | c1 $=$ | 16.41732 in | c1 $=$ | 16.41732 in |
| c2 = | 19.13385827 in | c2 = | 19.13385827 in |  | c2 = | 19.13386 in |  | c2 = | 19.13386 in | c2 = | 19.13386 in |
| c3 $=$ | 19.68503937 in | c3 = | 19.68503937 in |  | c3 $=$ | 19.68504 in |  | c3 $=$ | 19.68504 in | c3 = | 19.68504 in |
| c4 $=$ | 19.33070866 in | c4 = | 19.33070866 in |  | c4 = | 19.33071 in |  | c4 $=$ | 19.33071 in | c4 = | 19.33071 in |
| c5 = | 18.38582677 in | c5 = | 18.38582677 in |  | c5 = | 18.38583 in |  | c5 = | 18.38583 in | c5 = | 18.38583 in |
| c6 = | 14.80314961 in | c6 = | 14.80314961 in |  | c6 = | 14.80315 in |  | c6 = | 14.80315 in | c6 = | 14.80315 in |
| $\theta=$ | 0 degrees | $\theta=$ | 0 degrees |  | $\theta=$ | 0 degrees |  | $\theta=$ | 0 degrees | $\theta=$ | 0 degrees |
| $\mathrm{G}=$ | 647.0678294 lbs | G = | 583.9789061 lbs |  | G = | 524.1247 lbs |  | $\mathrm{G}=$ | 467.5065 lbs | G = | 414.1235 lbs |
| $E=$ | 2157321.988 in-lbs | $\mathrm{E}=$ | 2157445.222 in-lbs |  | $\mathrm{E}=$ | 2157571 in-lbs |  | $E=$ | 2157697 in-lbs | $E=$ | 2157823 in-lbs |
| E= | 179776.8323 ft -lbs | E= | 179787.1019 ft -lbs |  | E= | $179797.6 \mathrm{ft-lbs}$ |  | E= | $179808 \mathrm{ft-lbs}$ | E= | $179818.6 \mathrm{ft-lbs}$ |
| w = (weight of | 4455.542319 lbs | $w=$ | 4455.542319 lbs |  | $\mathrm{w}=($ weigh $)$ | 4455.542 lbs |  | w = (weight | 4455.542 lbs | w = (weigh | 4455.542 lbs |
| $\mathrm{v}=$ | $50.97526699 \mathrm{ft} / \mathrm{sec}$ | $\mathrm{v}=$ | $50.97672292 \mathrm{ft} / \mathrm{sec}$ |  | $v=$ | $50.97821 \mathrm{ft} / \mathrm{sec}$ |  | $v=$ | $50.97969 \mathrm{ft} / \mathrm{sec}$ | $\mathrm{v}=$ | $50.98119 \mathrm{ft} / \mathrm{sec}$ |
| $v=$ | $34.59028692 \mathrm{mi} / \mathrm{hr}$ | $v=$ | $34.59127487 \mathrm{mi} / \mathrm{hr}$ |  | $v=$ | $34.59228 \mathrm{mi} / \mathrm{hr}$ |  | $v=$ | $34.59329 \mathrm{mi} / \mathrm{hr}$ | $v=$ | $34.59431 \mathrm{mi} / \mathrm{hr}$ |
| $\begin{aligned} & \text { bo= } \\ & 5.0 \mathrm{mph} \end{aligned}$ |  | m |  |  | bo= 4.5 mph |  |  | $\begin{aligned} & \mathrm{bo}= \\ & 4.25 \\ & \mathrm{mph} \end{aligned}$ |  | bo= 4.0 mph |  |
| 55.82 | $\mathrm{m} / \mathrm{h}$ is equal to 34.6849 |  |  | A average | 424.0838 Ib |  | $B$ average | 133.258 | b/in*2 | v average $=34.58983$ | mi/hr |
| A $=$ | $434.0676 \mathrm{lb} / \mathrm{in}$ | A = | $450.8753 \mathrm{lb} / \mathrm{in}$ |  | A $=$ | $467.3318 \mathrm{lb} / \mathrm{in}$ |  | A $=$ | $483.4373 \mathrm{lb} / \mathrm{in}$ | A $=$ | $499.1916 \mathrm{lb} / \mathrm{in}$ |
| $B=$ | $132.0555 \mathrm{lb} / \mathrm{in}^{*} 2$ | $B=$ | $129.8218 \mathrm{lb} / \mathrm{in}^{*} 2$ |  | $B=$ | $127.6072 \mathrm{Ib} / \mathrm{in}^{*} 2$ |  | $B=$ | $125.4117 \mathrm{lb} / \mathrm{in}^{*} 2$ | $B=$ | $123.2352 \mathrm{lb} / \mathrm{in}^{*} 2$ |
| W (width of crı | 69.04724409 in | W (w | 69.04724409 in |  | W (width of | 69.04724 in |  | W (width of | 69.04724 in | W (width o | 69.04724 in |
| c1 = | 16.41732283 in | c1 $=$ | 16.41732283 in |  | c1 $=$ | 16.41732 in |  | $\mathrm{c} 1=$ | 16.41732 in | c1 $=$ | 16.41732 in |
| $\mathrm{c} 2=$ | 19.13385827 in | c2 = | 19.13385827 in |  | c2 = | 19.13386 in |  | c2 = | 19.13386 in | c2 = | 19.13386 in |
| c3 $=$ | 19.68503937 in | c3 $=$ | 19.68503937 in |  | c3 = | 19.68504 in |  | c3 $=$ | 19.68504 in | c3 = | 19.68504 in |
| c4 $=$ | 19.33070866 in | c4 = | 19.33070866 in |  | c4 = | 19.33071 in |  | c4 $=$ | 19.33071 in | c4 $=$ | 19.33071 in |
| c5 = | 18.38582677 in | c5 = | 18.38582677 in |  | c5 = | 18.38583 in |  | c5 = | 18.38583 in | c5 = | 18.38583 in |
| c6 = | 14.80314961 in | c6 = | 14.80314961 in |  | c6 = | 14.80315 in |  | c6 = | 14.80315 in | c6 = | 14.80315 in |
| $\theta=$ | 0 degrees | $\theta=$ | 0 degrees |  | $\theta=$ | 0 degrees |  | $\theta=$ | 0 degrees | $\theta=$ | 0 degrees |
| $\mathrm{G}=$ | 713.392026 lbs | G = | 782.952232 lbs |  | $\mathrm{G}=$ | 855.7472 lbs |  | $\mathrm{G}=$ | 931.7776 lbs | G = | 1011.043 lbs |
| $\mathrm{E}=$ | 2157199.062 in-lbs | E= | 2157076.751 in-lbs |  | E= | 2156956 in-lbs |  | $\mathrm{E}=$ | 2156837 in-lbs | E = | 2156718 in-lbs |
| E= | 179766.5885 ft -lbs | E= | 179756.3959 ft f-lbs |  | E= | $179746.3 \mathrm{ft-lbs}$ |  | E= | $179736.4 \mathrm{ft-lbs}$ | E= | 179726.5 ft -lbs |
| w = (weight of | 4455.542319 lbs | $w=$ | 4455.542319 lbs |  | $\mathrm{w}=($ weigh $)$ | 4455.542 lbs |  | $w=($ weight | 4455.542 lbs | w = (weigh | 4455.542 lbs |
| $v=$ | $50.97381467 \mathrm{ft} / \mathrm{sec}$ | $v=$ | $50.97236957 \mathrm{ft} / \mathrm{sec}$ |  | $v=$ | $50.97094 \mathrm{ft} / \mathrm{sec}$ |  | $v=$ | $50.96953 \mathrm{ft} / \mathrm{sec}$ | $v=$ | $50.96813 \mathrm{ft} / \mathrm{sec}$ |
| $v=$ | $34.58930142 \mathrm{mi} / \mathrm{hr}$ | $v=$ | $34.58832082 \mathrm{mi} / \mathrm{hr}$ |  | $v=$ | $34.58735 \mathrm{mi} / \mathrm{hr}$ |  | $v=$ | $34.5864 \mathrm{mi} / \mathrm{hr}$ | $v=$ | $34.58544 \mathrm{mi} / \mathrm{hr}$ |
|  | $b o=$ <br> 5.25 <br> $m p h$ | $\begin{aligned} & \mathrm{bo}= \\ & 5.5 \end{aligned}$ |  |  | $\begin{aligned} & \hline b o= \\ & 5.75 \\ & \mathrm{mph} \\ & \hline \end{aligned}$ |  |  | bo= <br> 6.0 mph |  | $\begin{aligned} & \mathrm{bo}= \\ & 6.25 \\ & \mathrm{mph} \\ & \hline \end{aligned}$ |  |


| 2003 Subaru Forester |  | case \#15 |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $A=$ | 390.01 | $\mathrm{lb} /$ in | $A=$ | $373.5606 \mathrm{lb} / \mathrm{in}$ |  | $A=$ | $356.7862 \mathrm{lb} / \mathrm{in}$ |  | A $=$ | $339.691 \mathrm{lb} / \mathrm{in}$ | $A=$ | $322.2751 \mathrm{lb} / \mathrm{in}$ |
| $B=$ | 128.69 | $1 \mathrm{lb} / \mathrm{in}^{*} 2$ | $B=$ | $130.8215 \mathrm{lb} / \mathrm{in}^{*} 2$ |  | $B=$ | $132.9644 \mathrm{lb} / \mathrm{in}^{*} 2$ |  | $B=$ | $135.1246 \mathrm{lb} / \mathrm{in}^{*} 2$ | $B=$ | $137.3023 \mathrm{lb} / \mathrm{in}^{*} 2$ |
| W (width of crı | 61.307086 |  | W (width of 6 | 61.30708661 in |  | W (width of | 61.30709 in |  | W (width of | 61.30709 in | W (width o. | 61.30709 in |
| c1 = | 12.244094 |  | c1 $=$ | 12.24409449 in |  | c1 = | 12.24409 in |  | c 1 = | 12.24409 in | c1 = | 12.24409 in |
| c2 = | 18.976377 |  | c2 = | 18.97637795 in |  | c2 = | 18.97638 in |  | c2 = | 18.97638 in | c2 = | 18.97638 in |
| c3 $=$ | 19.44881 |  | c3 = | 19.4488189 in |  | c3 $=$ | 19.44882 in |  | c3 $=$ | 19.44882 in | c3 = | 19.44882 in |
| c4 $=$ |  | in | c4 = | 20 in |  | c4 = | 20 in |  | c4 $=$ | 20 in | c4 = | 20 in |
| c5 $=$ | 19.370078 |  | c5 $=$ | 19.37007874 in |  | c5 = | 19.37008 in |  | c5 = | 19.37008 in | c5 $=$ | 19.37008 in |
| c6 = | 16.417322 |  | c6 = | 16.41732283 in |  | c6 = | 16.41732 in |  | c6 = | 16.41732 in | c6 = | 16.41732 in |
| $\theta=$ |  | degrees | $\theta=$ | 0 degrees |  | $\theta=$ | 0 degrees |  | $\theta=$ | 0 degrees | $\theta=$ | 0 degrees |
| $\mathrm{G}=$ | 590.97033 | lbs | $\mathrm{G}=$ | 533.3508707 lbs |  | $\mathrm{G}=$ | 478.686 lbs |  | $\mathrm{G}=$ | 426.9762 lbs | $\mathrm{G}=$ | 378.221 lbs |
| $E=$ | 1829227.9 | in-lbs | $E=$ | 1829444.776 in-lbs |  | $E=$ | 1829664 in-lbs |  | $E=$ | 1829885 in-lbs | $E=$ | 1830108 in-lbs |
| E= | 152435.65 | ft -lbs | E= | 152453.7314 ft -lbs |  | E= | 152472 ft -lbs |  | E= | 152490.4 ft -lbs | E= | 152509 ft -lbs |
| w = (weight of | 3615.58 | lbs | $w=($ weigh $)$ | 3615.5811 lbs |  | w = (weight | 3615.581 lbs |  | w = (weight | 3615.581 lbs | w = (weigh | 3615.581 lbs |
| $v=$ | 52.107131 | ft sec | $v=$ | $52.11022029 \mathrm{ft} / \mathrm{sec}$ |  | $\mathrm{v}=$ | $52.11335 \mathrm{ft} / \mathrm{sec}$ |  | $v=$ | $52.11648 \mathrm{ft} / \mathrm{sec}$ | $v=$ | $52.11966 \mathrm{ft} / \mathrm{sec}$ |
| $v=$ | 35.358336 | $\mathrm{mi} / \mathrm{hr}$ | $v=$ | $35.36043218 \mathrm{mi} / \mathrm{hr}$ |  | $v=$ | $35.36255 \mathrm{mi} / \mathrm{hr}$ |  | $v=$ | $35.36468 \mathrm{mi} / \mathrm{hr}$ | $v=$ | $35.36684 \mathrm{mi} / \mathrm{hr}$ |
| $\begin{aligned} & \text { bo= } \\ & 5.0 \mathrm{mph} \end{aligned}$ |  |  | $\begin{aligned} & \hline \mathrm{bo}= \\ & 4.75 \\ & \mathrm{mph} \\ & \hline \end{aligned}$ |  |  | bo= 4.5 mph |  |  | $\begin{aligned} & \hline \text { bo= } \\ & 4.25 \\ & \mathrm{mph} \\ & \hline \end{aligned}$ |  | bo= <br> 4.0 mph |  |
| 56.97 k | $\mathrm{m} / \mathrm{h}$ is equal | 35.39954 |  |  | A average | 396.7978 |  | B average | 127.7117 lb | b/in*2 | v average $=35.35736 \mathrm{~m}$ | mi/hr |
| A = | 406.14 | $\mathrm{lb} / \mathrm{in}$ | A $=$ | $421.9594 \mathrm{lb} / \mathrm{in}$ |  | A $=$ | $437.4509 \mathrm{lb} / \mathrm{in}$ |  | A $=$ | $452.6216 \mathrm{lb} / \mathrm{in}$ | A $=$ | $467.4716 \mathrm{lb} / \mathrm{in}$ |
| $B=$ | 126.5 | $\mathrm{lb} / \mathrm{in}^{*} 2$ | $B=$ | $124.4974 \mathrm{lb} / \mathrm{in}^{*} 2$ |  | $B=$ | $122.4242 \mathrm{lb} / \mathrm{in}^{*} 2$ |  | $B=$ | $120.3683 \mathrm{lb} / \mathrm{in}^{*} 2$ | $B=$ | $118.3299 \mathrm{lb} / \mathrm{in}^{*} 2$ |
| W (width of crı | 61.307086 |  | W (width oi 6 | 61.30708661 in |  | W (width of | 61.30709 in |  | W (width of | 61.30709 in | W (width o | 61.30709 in |
| c 1 = | 12.244094 |  | c1 = | 12.24409449 in |  | c1 = | 12.24409 in |  | c 1 = | 12.24409 in | c1 = | 12.24409 in |
| c2 = | 18.976377 |  | c2 = | 18.97637795 in |  | c2 = | 18.97638 in |  | c2 = | 18.97638 in | c2 = | 18.97638 in |
| c3 $=$ | 19.44881 |  | c3 $=$ | 19.4488189 in |  | c3 $=$ | 19.44882 in |  | c3 $=$ | 19.44882 in | c3 $=$ | 19.44882 in |
| c4 $=$ |  | in | c4 = | 20 in |  | c4 = | 20 in |  | c4 = | 20 in | c4 = | 20 in |
| c5 = | 19.370078 |  | c5 = | 19.37007874 in |  | c5 = | 19.37008 in |  | c5 = | 19.37008 in | c5 = | 19.37008 in |
| c6 = | 16.417322 |  | c6 $=$ | 16.41732283 in |  | c6 $=$ | 16.41732 in |  | c6 = | 16.41732 in | c6 $=$ | 16.41732 in |
| $\theta=$ |  | degrees | $\theta=$ | 0 degrees |  | $\theta=$ | 0 degrees |  | $\theta=$ | 0 degrees | $\theta=$ | 0 degrees |
| $\mathrm{G}=$ | 651.5449 | lbs | G = | 715.074111 lbs |  | $\mathrm{G}=$ | 781.5583 lbs |  | $\mathrm{G}=$ | 850.9978 lbs | $\mathrm{G}=$ | 923.3917 lbs |
| $E=$ | 1829011.6 | in-lbs | $E=$ | 1828798.173 in-lbs |  | $E=$ | 1828586 in-lbs |  | $E=$ | 1828375 in-lbs | $E=$ | 1828167 in-lbs |
| E= | 152417.63 | $\mathrm{ft-lbs}$ | E= | 152399.8477 ft -lbs |  | E= | 152382.2 ft -lbs |  | E= | 152364.6 ft -lbs | E= | 152347.2 ft -lbs |
| w $=$ ( weight of | 3615.58 | lbs | $\mathrm{w}=($ weigh $)$ | 3615.5811 lbs |  | w = (weight | 3615.581 lbs |  | w = (weight | 3615.581 lbs | $\mathrm{w}=$ ( weigh ) | 3615.581 lbs |
| $v=$ | 52.10405 | $\mathrm{ft} / \mathrm{sec}$ | $v=$ | $52.1010105 \mathrm{ft} / \mathrm{sec}$ |  | $v=$ | 52.09799 ftsec |  | $v=$ | $52.09499 \mathrm{ft} / \mathrm{sec}$ | $\mathrm{v}=$ | $52.09202 \mathrm{ft} / \mathrm{sec}$ |
| $v=$ | 35.356246 | $\mathrm{mi} / \mathrm{hr}$ | $v=$ | $35.35418269 \mathrm{mi} / \mathrm{hr}$ |  | $v=$ | $35.35214 \mathrm{mi} / \mathrm{hr}$ |  | $v=$ | $35.3501 \mathrm{mi} / \mathrm{hr}$ | $v=$ | $35.34808 \mathrm{mi} / \mathrm{hr}$ |
|  |  |  | bo= <br> 5.5 mph |  |  | $\begin{aligned} & \mathrm{bo}= \\ & 5.75 \\ & \mathrm{mph} \end{aligned}$ |  |  | bo= 6.0 mph |  | $\begin{aligned} & \mathrm{bo}= \\ & 6.25 \\ & \mathrm{mph} \\ & \hline \end{aligned}$ |  |


| 2002 Dodge Ram 1500 |  | case \#16 |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| A = | 511.337 | $4 \mathrm{lb} / \mathrm{in}$ | A $=$ | $489.805 \mathrm{lb} / \mathrm{in}$ | $A=$ | $467.8479 \mathrm{lb} / \mathrm{in}$ |  | A $=$ | $445.4661 \mathrm{lb} / \mathrm{in}$ | $A=$ | $422.6597 \mathrm{lb} / \mathrm{in}$ |
| $\mathrm{B}=$ | 171.283 | $\mathrm{lb} / \mathrm{in}$ *2 | $\mathrm{B}=$ | $174.1408 \mathrm{lb} / \mathrm{in} * 2$ | $\mathrm{B}=$ | $177.0214 \mathrm{lb} / \mathrm{in}^{*} 2$ |  | $\mathrm{B}=$ | 179.9256 Ib/in*2 | $\mathrm{B}=$ | $182.8534 \mathrm{lb} / \mathrm{in}^{*} 2$ |
| W (width of crı | 72.8818897 |  | W (w | 72.88188976 in | W (width of | 72.88189 in |  | W (width of | 72.88189 in | W (width o | 72.88189 in |
| c1 $=$ | 10.8661417 |  | c1 = | 10.86614173 in | c1 $=$ | 10.86614 in |  | c 1 = | 10.86614 in | c1 = | 10.86614 in |
| c2 = | 17.8346456 |  | c2 = | 17.83464567 in | c2 = | 17.83465 in |  | c2 = | 17.83465 in | c2 = | 17.83465 in |
| c3 $=$ | 21.5748031 |  | c3 = | 21.57480315 in | c3 $=$ | 21.5748 in |  | c3 $=$ | 21.5748 in | c3 = | 21.5748 in |
| c4 $=$ | 21.5748031 |  | c4 = | 21.57480315 in | c4 = | 21.5748 in |  | c4 = | 21.5748 in | c4 = | 21.5748 in |
| c5 = | 17.9133858 |  | c5 = | 17.91338583 in | c5 = | 17.91339 in |  | c5 = | 17.91339 in | c5 = | 17.91339 in |
| c6 $=$ | 11.0629921 |  | c6 = | 11.06299213 in | c6 = | 11.06299 in |  | c6 = | 11.06299 in | c6 = | 11.06299 in |
| $\theta=$ |  | degrees | $\theta=$ | 0 degrees | $\theta=$ | 0 degrees |  | $\theta=$ | 0 degrees | $\theta=$ | 0 degrees |
| $\mathrm{G}=$ | 763.253103 | lbs | $\mathrm{G}=$ | 688.8360971 lbs | G = | 618.235 lbs |  | $\mathrm{G}=$ | 551.4503 lbs | $\mathrm{G}=$ | 488.4821 lbs |
| $E=$ | 2809728.64 | in-lbs | $E=$ | 2810865.47 in-lbs | $E=$ | 2812013 in-lbs |  | $E=$ | 2813169 in-lbs | $E=$ | 2814334 in-lbs |
| E= | 234144.05 | ft -lbs | E= | 234238.7892 ft -lbs | E= | 234334.4 ft -lbs |  | E= | $234430.7 \mathrm{ft-lbs}$ | E= | 234527.8 ft -lbs |
| w $=$ ( weight of | 5551.23976 | lbs | $w=$ | 5551.239762 lbs | w = (weight | 5551.24 lbs |  | w = (weight | 5551.24 lbs | $w=$ (weigh | 5551.24 lbs |
| $v=$ | 52.1182119 | $\mathrm{ft} / \mathrm{sec}$ | $\mathrm{v}=$ | $52.12875447 \mathrm{ft} / \mathrm{sec}$ | $v=$ | $52.13939 \mathrm{ft} / \mathrm{sec}$ |  | $v=$ | $52.15011 \mathrm{ft} / \mathrm{sec}$ | $v=$ | $52.16091 \mathrm{ft} / \mathrm{sec}$ |
| $v=$ | 35.3658550 | $\mathrm{mi} / \mathrm{hr}$ | $v=$ | $35.37300892 \mathrm{mi} / \mathrm{hr}$ | $v=$ | $35.38023 \mathrm{mi} / \mathrm{hr}$ |  | $v=$ | $35.3875 \mathrm{mi} / \mathrm{hr}$ | $v=$ | $35.39483 \mathrm{mi} / \mathrm{hr}$ |
| $\begin{aligned} & \text { bo= } \\ & 5.0 \mathrm{mph} \end{aligned}$ |  |  | mp |  | bo= 4.5 mph |  |  | $\begin{aligned} & \hline \text { bo= } \\ & 4.25 \\ & \mathrm{mph} \\ & \hline \end{aligned}$ |  | bo= <br> 4.0 mph |  |
| 56.49 k | $\mathrm{m} / \mathrm{h}$ is equal to | 35.10128 |  |  | 520.1925 |  | B average | 169.9617 lb | b/in*2 | $\mathbf{v}$ average $=35.36253$ | mi/hr |
| A = | 532.445 | $1 \mathrm{lb} / \mathrm{in}$ | A = | $553.1281 \mathrm{lb} / \mathrm{in}$ | A $=$ | $573.3865 \mathrm{lb} / \mathrm{in}$ |  | A $=$ | $593.2202 \mathrm{lb} / \mathrm{in}$ | A $=$ | $612.6292 \mathrm{lb} / \mathrm{in}$ |
| $B=$ | 168.450 | lb/in*2 | $B=$ | $165.6409 \mathrm{lb} / \mathrm{in}^{*} 2$ | $B=$ | $162.8548 \mathrm{lb} / \mathrm{in}^{*} 2$ |  | $B=$ | $160.0924 \mathrm{lb} / \mathrm{in}^{*} 2$ | $B=$ | $157.3536 \mathrm{lb} / \mathrm{in}^{*} 2$ |
| W (width of crı | 72.8818897 |  | W (w | 72.88188976 in | W (width of | 72.88189 in |  | W (width of | 72.88189 in | W (width o | 72.88189 in |
| c1 = | 10.8661417 |  | c1 = | 10.86614173 in | c1 = | 10.86614 in |  | c 1 = | 10.86614 in | c1 = | 10.86614 in |
| c2 = | 17.8346456 |  | c2 = | 17.83464567 in | c2 = | 17.83465 in |  | c2 = | 17.83465 in | c2 = | 17.83465 in |
| c3 $=$ | 21.5748031 |  | c3 $=$ | 21.57480315 in | c3 = | 21.5748 in |  | c3 $=$ | 21.5748 in | c3 $=$ | 21.5748 in |
| c4 = | 21.5748031 |  | c4 = | 21.57480315 in | c4 = | 21.5748 in |  | c4 = | 21.5748 in | c4 = | 21.5748 in |
| c5 = | 17.9133858 |  | c5 = | 17.91338583 in | c5 = | 17.91339 in |  | c5 = | 17.91339 in | c5 = | 17.91339 in |
| c6 $=$ | 11.0629921 |  | c6 $=$ | 11.06299213 in | c6 = | 11.06299 in |  | c6 = | 11.06299 in | c6 $=$ | 11.06299 in |
| $\theta=$ |  | degrees | $\theta=$ | 0 degrees | $\theta=$ | 0 degrees |  | $\theta=$ | 0 degrees | $\theta=$ | 0 degrees |
| $\mathrm{G}=$ | 841.486419 | lbs | G = | 923.5360802 lbs | G = | 1009.402 lbs |  | $\mathrm{G}=$ | 1099.085 lbs | G = | 1192.583 lbs |
| $E=$ | 2808600.84 | in-lbs | $E=$ | 2807482.077 in-lbs | E = | 2806372 in-lbs |  | $E=$ | 2805273 in-lbs | $E=$ | 2804183 in-lbs |
| E= | 234050.070 | ft-lbs | E= | 233956.8397 ft -lbs | E= | 233864.4 ft -lbs |  | E= | 233772.8 ft-lbs | E= | 233681.9 ft -lbs |
| w $=$ ( weight of | 5551.23976 | 2 lbs | w = | 5551.239762 lbs | w = (weight | 5551.24 lbs |  | w = (weight | 5551.24 lbs | $\mathrm{w}=$ ( weigh . | 5551.24 lbs |
| $v=$ | 52.1077510 | ft/sec | $\mathrm{v}=$ | $52.09737175 \mathrm{ft} / \mathrm{sec}$ | $\mathrm{v}=$ | $52.08708 \mathrm{ft} / \mathrm{sec}$ |  | $v=$ | $52.07687 \mathrm{ft} / \mathrm{sec}$ | $\mathrm{v}=$ | $52.06675 \mathrm{ft} / \mathrm{sec}$ |
| $v=$ | 35.3587566 | mi/hr | $v=$ | $35.35171355 \mathrm{mi} / \mathrm{hr}$ | $v=$ | $35.34473 \mathrm{mi} / \mathrm{hr}$ |  | $v=$ | $35.3378 \mathrm{mi} / \mathrm{hr}$ | $v=$ | $35.33093 \mathrm{mi} / \mathrm{hr}$ |
|  | bo $=$ <br> 5.25 <br> mph |  |  |  | $\begin{aligned} & \mathrm{bo}= \\ & 5.75 \\ & \mathrm{mph} \end{aligned}$ |  |  | bo= 6.0 mph |  | $\begin{aligned} & \mathrm{bo}= \\ & 6.25 \\ & \mathrm{mph} \\ & \hline \end{aligned}$ |  |


| 2001 Nissan Frontier | case \#17 |
| :--- | :--- |





| 2001 Dodge Caravan | case \#20 |
| :--- | :--- |


| A = | $482.3483 \mathrm{lb} / \mathrm{in}$ | A = | $462.1032 \mathrm{lb} / \mathrm{in}$ |  | A = | $441.4541 \mathrm{lb} / \mathrm{in}$ |  | A = | $420.3969 \mathrm{lb} / \mathrm{in}$ | A $=$ | $398.9318 \mathrm{lb} / \mathrm{in}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $B=$ | $179.0299 \mathrm{lb} / \mathrm{in}^{*} 2$ | $B=$ | $182.0715 \mathrm{lb} / \mathrm{in} * 2$ |  | $B=$ | $185.1387 \mathrm{lb} / \mathrm{in}^{*} 2$ |  | $B=$ | $188.2316 \mathrm{lb} / \mathrm{in}^{*} 2$ | $B=$ | $191.3501 \mathrm{lb} / \mathrm{in}^{*} 2$ |
| W (width of crı | 66.2992126 in | W (width of | 66.2992126 in |  | W (width of | 66.29921 in |  | W (width of | 66.29921 in | W (width o | 66.29921 in |
| c1 = | 12.4015748 in | c1 = | 12.4015748 in |  | c1 = | 12.40157 in |  | c1 = | 12.40157 in | c1 = | 12.40157 in |
| c2 = | 15.59055118 in | c2 = | 15.59055118 in |  | c2 = | 15.59055 in |  | c2 = | 15.59055 in | c2 = | 15.59055 in |
| c3 $=$ | 16.25984252 in | c3 = | 16.25984252 in |  | c3 = | 16.25984 in |  | c3 $=$ | 16.25984 in | c3 = | 16.25984 in |
| c4 $=$ | 16.77165354 in | c4 $=$ | 16.77165354 in |  | c4 = | 16.77165 in |  | c4 = | 16.77165 in | c4 | 16.77165 in |
| c5 = | 17.55905512 in | c5 = | 17.55905512 in |  | c5 = | 17.55906 in |  | c5 = | 17.55906 in | c5 | 17.55906 in |
| c6 = | 14.48818898 in | c6 = | 14.48818898 in |  | c6 = | 14.48819 in |  | c6 = | 14.48819 in | c6 = | 14.48819 in |
| $\theta=$ | 0 degrees | $\theta=$ | 0 degrees |  | $\theta=$ | 0 degrees |  | $\theta=$ | 0 degrees | $\theta=$ | 0 degrees |
| $\mathrm{G}=$ | 649.7794014 lbs | $\mathrm{G}=$ | 586.4162361 lbs |  | $\mathrm{G}=$ | 526.3128 lbs |  | $\mathrm{G}=$ | 469.4577 lbs | $\mathrm{G}=$ | 415.8518 lbs |
| $\mathrm{E}=$ | 2066223.659 in-lbs | $E=$ | 2066366.989 in-lbs |  | E = | 2066516 in-lbs |  | $\mathrm{E}=$ | 2066668 in-lbs | $E=$ | 2066820 in-lbs |
| E= | 172185.3049 ft -lbs | E= | 172197.2491 ft -lbs |  | E= | 172209.7 ft -lbs |  | E= | 172222.3 ft -lbs | E= | 172235 ft -lbs |
| w = (weight of | 4299.014113 lbs | w = (weigh | 4299.014113 lbs |  | w = (weight | 4299.014 lbs |  | w = (weight | 4299.014 lbs | w = (weigh | 4299.014 lbs |
| $\mathrm{v}=$ | $50.78746549 \mathrm{ft} / \mathrm{sec}$ | $v=$ | $50.78922698 \mathrm{ft} / \mathrm{sec}$ |  | $v=$ | $50.79106 \mathrm{ft} / \mathrm{sec}$ |  | $v=$ | $50.79292 \mathrm{ft} / \mathrm{sec}$ | $v=$ | $50.79479 \mathrm{ft} / \mathrm{sec}$ |
| $v=$ | $34.46285046 \mathrm{mi} / \mathrm{hr}$ | $v=$ | $34.46404575 \mathrm{mi} / \mathrm{hr}$ |  | $v=$ | $34.46529 \mathrm{mi} / \mathrm{hr}$ |  | $v=$ | $34.46655 \mathrm{mi} / \mathrm{hr}$ | $v=$ | $34.46782 \mathrm{mi} / \mathrm{hr}$ |
| bo= <br> 5.0 mph | $\begin{aligned} & \text { difference } \\ & -0.091629184 \end{aligned}$ | $\begin{aligned} & \mathrm{bo}= \\ & 4.75 \\ & \mathrm{mph} \end{aligned}$ |  |  | bo= 4.5 mph |  |  | $\begin{aligned} & \text { bo= } \\ & 4.25 \\ & \mathrm{mph} \end{aligned}$ |  | $\begin{aligned} & \mathrm{bo}= \\ & 4.0 \mathrm{mph} \end{aligned}$ |  |
| 55.61 | $\mathrm{m} / \mathrm{h}$ is equal to 34.5544796 mph |  |  | A average | 490.6292 | $\mathrm{b} / \mathrm{in}$ | $B$ average | 177.6244 Ib | b/in*2 | v average $=34.46224$ | mi/hr |
| A $=$ | $502.1773 \mathrm{lb} / \mathrm{in}$ | A $=$ | $521.6024 \mathrm{lb} / \mathrm{in}$ |  | A $=$ | $540.6195 \mathrm{lb} / \mathrm{in}$ |  | $A=$ | $559.2285 \mathrm{lb} / \mathrm{in}$ | $A=$ | $577.4295 \mathrm{lb} / \mathrm{in}$ |
| $\mathrm{B}=$ | $176.0139 \mathrm{lb} / \mathrm{in} * 2$ | $B=$ | $173.0235 \mathrm{lb} / \mathrm{in} * 2$ |  | $B=$ | $170.0587 \mathrm{lb} / \mathrm{in}^{*} 2$ |  | $B=$ | $167.1196 \mathrm{lb} / \mathrm{in}^{*} 2$ | $B=$ | $164.2061 \mathrm{lb} / \mathrm{in}^{*} 2$ |
| W (width of crı | 66.2992126 in | W (width of | 66.2992126 in |  | W (width of | 66.29921 in |  | W (width of | 66.29921 in | W (width o | 66.29921 in |
| c1 = | 12.4015748 in | c1 = | 12.4015748 in |  | c1 = | 12.40157 in |  | c1 = | 12.40157 in | c1 = | 12.40157 in |
| c2 = | 15.59055118 in | c2 = | 15.59055118 in |  | c2 = | 15.59055 in |  | c2 = | 15.59055 in | c2 = | 15.59055 in |
| c3 $=$ | 16.25984252 in | c3 $=$ | 16.25984252 in |  | c3 = | 16.25984 in |  | c3 = | 16.25984 in | c3 = | 16.25984 in |
| c4 $=$ | 16.77165354 in | c4 $=$ | 16.77165354 in |  | c4 = | 16.77165 in |  | c4 = | 16.77165 in | c4 = | 16.77165 in |
| c5 = | 17.55905512 in | c5 = | 17.55905512 in |  | c5 = | 17.55906 in |  | c5 = | 17.55906 in | c5 = | 17.55906 in |
| c6 $=$ | 14.48818898 in | c6 = | 14.48818898 in |  | c6 = | 14.48819 in |  | c6 = | 14.48819 in | c6 $=$ | 14.48819 in |
| $\theta=$ | 0 degrees | $\theta=$ | 0 degrees |  | $\theta=$ | 0 degrees |  | $\theta=$ | 0 degrees | $\theta=$ | 0 degrees |
| $\mathrm{G}=$ | 716.3696749 lbs | $\mathrm{G}=$ | 786.219975 lbs |  | $\mathrm{G}=$ | 859.3193 lbs |  | $\mathrm{G}=$ | 935.6668 lbs | G = | 1015.263 lbs |
| E = | 2066071.426 in-lbs | E = | 2065925.353 in-lbs |  | E = | 2065780 in-lbs |  | $\mathrm{E}=$ | 2065637 in-lbs | E = | 2065495 in-lbs |
| E= | 172172.6188 ft -lbs | E= | 172160.4461 ft -lbs |  | E= | 172148.4 ft -lbs |  | E= | 172136.4 ft -lbs | E= | 172124.6 ft -lbs |
| $w=$ (weight of | 4299.014113 lbs | w $=$ (weigh | 4299.014113 lbs |  | w = (weight | 4299.014 lbs |  | w = (weight | 4299.014 lbs | w $=$ (weigh | 4299.014 lbs |
| $v=$ | $50.78559453 \mathrm{ft} / \mathrm{sec}$ | $v=$ | $50.78379921 \mathrm{ft} / \mathrm{sec}$ |  | $v=$ | $50.78202 \mathrm{ft} / \mathrm{sec}$ |  | $v=$ | $50.78026 \mathrm{ft} / \mathrm{sec}$ | $\mathrm{v}=$ | $50.77851 \mathrm{ft} / \mathrm{sec}$ |
| $v=$ | $34.46158088 \mathrm{mi} / \mathrm{hr}$ | $v=$ | $34.46036263 \mathrm{mi} / \mathrm{hr}$ |  | $v=$ | $34.45915 \mathrm{mi} / \mathrm{hr}$ |  | $v=$ | $34.45796 \mathrm{mi} / \mathrm{hr}$ | $v=$ | $34.45677 \mathrm{mi} / \mathrm{hr}$ |
|  | bo $=$ <br> 5.25 <br> mph | bo= <br> 5.5 mph |  |  | $\begin{array}{\|l\|} \hline \text { bo }= \\ 5.75 \\ \mathrm{mph} \\ \hline \end{array}$ |  |  | $\begin{aligned} & \text { bo= } \\ & 6.0 \mathrm{mph} \end{aligned}$ |  | $\begin{aligned} & \mathrm{bo}= \\ & 6.25 \\ & \mathrm{mph} \\ & \hline \end{aligned}$ |  |

## APPENDIX 5

## EBS DETERMINATIONS FOR THE "WITHIN" SUBJECTS DESIGN

| WITHIN SUBJECTS DESIGN-1998 FORD CONTOUR |  |  |  |  |  |  |  |  | $56.3 \mathrm{~km} / \mathrm{h}$ | $=$ | 34.9832261095204 mph |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| CASE \#1 |  |  | CASE \#2 |  |  | CASE \#3 |  |  | CASE \#4 |  |  | CASE \#5 |  |  |
| A $=$ | 354 | lb/in | A = | 354 | $\mathrm{lb} / \mathrm{in}$ | A = | 354 | lb/in | A = | 354 | lb/in | A = | 354 | lb/in |
| $\mathrm{B}=$ | 186 | lb/in^2 | $\mathrm{B}=$ | 186 | $\mathrm{lb} / \mathrm{in}^{\prime} 2$ | $\mathrm{B}=$ | 186 | $\mathrm{lb} / \mathrm{in}^{\wedge} 2$ | $\mathrm{B}=$ | 186 | $\mathrm{lb} / \mathrm{in}^{\wedge} 2$ | $\mathrm{B}=$ | 186 | $\mathrm{lb} / \mathrm{in}$ ^2 |
| W ( width) $=$ | 66.726 | in | $W$ (width $)=$ | 67.147 | in | W (width) $=$ | 66.777 | in | W (width) $=$ | 66,608 | in | W ( width) $=$ | 66.985 | in |
| C1 $=$ | 4.038 | in | c1 = | 3.888 | in | c1 = | 4.149 | in | c1 = | 4.293 | in | c1 $=$ | 4.091 | in |
| C2 $=$ | 9.374 | in | c2 = | 8.792 | in | $\mathrm{c} 2=$ | 7.965 | in | c2 = | 9.336 | in | c2 = | 9.044 | in |
| c3 $=$ | 16.091 | in | c3 = | 15.172 | in | c3 $=$ | 16.071 | in | c3 = | 17.339 | in | c3 $=$ | 16.941 | in |
| C4 $=$ | 17.399 | in | C4 = | 17.449 | in | c4 = | 17.879 | in | c4 = | 17.879 | in | c4 = | 17.566 | in |
| C5 = | 17.255 | in | C5 = | 17.335 | in | c5 = | 18.669 | in | c5 = | 18.564 | in | c5 = | 17.257 | in |
| c6 = | 7.901 | in | c6 = | 8.128 | in | c6 = | 9.714 | in | c6 = | 9.512 | in | C6 = | 9.095 | in |
| $\theta=$ | 0 | degrees | $\theta=$ | 0 | degrees | $\theta=$ |  | degrees | $\theta=$ | 0 | degrees | $\theta=$ | 0 | degrees |
| G = | 336.87097 | Ibs | G = | 336.871 | Ibs | $\mathrm{G}=$ | 336.87 | Ibs | $\mathrm{G}=$ | 336.871 | lbs | $\mathrm{G}=$ | 336.871 | lbs |
| $\mathrm{E}=$ | 1525509.2 | in-Ibs | E = | 1488560 | in-Ibs | $\mathrm{E}=$ | 2E+06 | in-lbs | $E=$ | 1687990 | in-lbs | E = | 1587167 | in-libs |
| $\mathrm{E}=$ | 127125.76 | ft-lbs | E= | 124047 | ft-lbs | E= | 133874 | ft-lbs | E= | 140665,8 | ft -bs | E= | 132264 | ft-lbs |
| w = (weight) | 3310 | Ibs | w = (weight) | 3310 | Ibs | w = (weight) | 3310 | Ibs | w = (weight) | 3310 | Ibs | w = (weight) | 3310 | Ibs |
| $\mathrm{v}=$ | 49.733122 | $\mathrm{ft} / \mathrm{sec}$ | $\mathrm{v}=$ | 49.1271 | $\mathrm{ft} / \mathrm{sec}$ | $\mathrm{v}=$ | 51.036 | f/sec | $\mathrm{v}=$ | 52.31464 | $\mathrm{ft} / \mathrm{sec}$ | $\mathrm{v}=$ | 50.72823 | ft/sec |
| $\mathrm{v}=$ | 33.747405 | mi/hr | $\mathrm{v}=$ | 33.3362 | $\mathrm{mi} / \mathrm{hr}$ | $\mathrm{v}=$ | 34.631 | mi/hr | $\mathrm{v}=$ | 35.49914 | $\mathrm{mi} / \mathrm{hr}$ | $\mathrm{v}=$ | 34.42265 | $\mathrm{mi} / \mathrm{hr}$ |
| CASE \#6 |  |  | CASE \#7 |  |  | CASE \#8 |  |  | CASE \#9 |  |  | CASE \#10 |  |  |
| A $=$ | 354 | lb/in | $A=$ | 354 | lb/in | $A=$ | 354 | Ib/in | $A=$ | 354 | Ib/in | A = | 354 | Ib/in |
| $\mathrm{B}=$ | 186 | $\mathrm{lb} / \mathrm{in}{ }^{\text {² }}$ | $\mathrm{B}=$ | 186 | $\mathrm{lb} / \mathrm{in}^{\prime} 2$ | $\mathrm{B}=$ | 186 | $1 \mathrm{~b} / \mathrm{in}^{\wedge} 2$ | $\mathrm{B}=$ | 186 | lb/in^2 | $\mathrm{B}=$ | 186 | $1 \mathrm{~b} / \mathrm{in}^{\wedge} 2$ |
| W ( width $)=$ | 66.873 | in | W (width) $=$ | 67.385 | in | W (width) $=$ | 67.063 | in | W (width $)=$ | 67.199 | in | W (width) $=$ | 67.09 | in |
| C1 $=$ | 4.14 | in | c1 = | 3.759 | in | c1 = | 3.986 | in | c1 = | 3.967 | in | c1 $=$ | 3.971 | in |
| C2 $=$ | 9.111 | in | c2 = | 8.728 | in | c 2 = | 8.849 | in | $\mathrm{c} 2=$ | 8.798 | in | c2 = | 8.905 | in |
| c3 $=$ | 18.086 | in | c3 = | 16.782 | in | c3 = | 16.995 | in | c3 = | 16.037 | in | c3 = | 16.554 | in |
| C4 $=$ | 17.644 | in | C4 = | 17.169 | in | C4 = | 17.353 | in | C4 = | 17.299 | in | C4 = | 17.5 | in |
| C5 = | 17.518 | in | c5 = | 17.096 | in | c5 = | 17.261 | in | c5 = | 17.222 | in | c5 = | 18.161 | in |
| c6 = | 9.261 | in | c6 = | 8.656 | in | C6 = | 8.852 | in | C6 = | 8.765 | in | c6 = | 8.998 | in |
| $\theta=$ | 0 | degrees | $\theta=$ |  | degrees | $\theta=$ | 0 | degree: | $\theta=$ | 0 | degrees | $\theta=$ | 0 | degrees |
| $\mathrm{G}=$ | 336.87097 | lbs | G = | 336.871 | lbs | G = | 336.87 | lbs | G = | 336.871 | lbs | G = | 336.871 | lbs |
| $\mathrm{E}=$ | 1656541.7 | in-lbs | $\mathrm{E}=$ | 1543935 | in-libs | $\mathrm{E}=$ | $2 \mathrm{E}+06$ | in-lbs | $\mathrm{E}=$ | 1525121 | in-lbs | $E=$ | 1603759 | in-lbs |
| E= | 138045. 14 | $\mathrm{ft}-\mathrm{bs}$ | E= | 128661 | ft-lbs | E= | 130890 | $\mathrm{ft-bs}$ | E= | 127093.4 | $\mathrm{ft}-\mathrm{lbs}$ | E= | 133646.6 | ft-lbs |
| w = (weight | 3310 | lbs | w = (weight) | 3310 | lbs | w = (weight) | 3310 | lbs | w = (weight) | 3310 | Ibs | w = (weight) | 3310 | Ibs |
| $\mathrm{v}=$ | 51,825023 | $\mathrm{ft} / \mathrm{sec}$ | $\mathrm{V}=$ | 50,0326 | f/sec | $\mathrm{V}=$ | 50.464 | ft/sec | $\mathrm{v}=$ | 49.72679 | $\mathrm{ft} / \mathrm{sec}$ | $\mathrm{v}=$ | 50.99268 | f/sec |
| $\mathrm{v}=$ | 35.166906 | $\mathrm{mi} / \mathrm{hr}$ | $\mathrm{v}=$ | 33.9506 | mi/hr | $\mathrm{v}=$ | 34.243 | mi/hr | $\mathrm{v}=$ | 33.74311 | $\mathrm{mi} / \mathrm{hr}$ | $\mathrm{v}=$ | 34.6021 | mi/hr |


| WITHIN SUBJECTS DESIGN-1998 FORD CONTOUR |  |  |  |  |  |  |  |  | $56.3 \mathrm{~km} / \mathrm{h}$ | $=$ | 34.9832261095204 mph |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| CASE \#11 |  |  | CASE \#12 |  |  | CASE \#13 |  |  | CASE \#14 |  |  | CASE \#15 |  |  |
| A = | 354 | Ib/in | A = | 354 | lb/in | A = | 354 | lb/in | A = | 354 | Ib/in | A = | 354 | Ib/in |
| $\mathrm{B}=$ | 186 | $\mathrm{lb} / \mathrm{in}^{\wedge} 2$ | B = | 186 | $\mathrm{lb} / \mathrm{in}^{\wedge} 2$ | $\mathrm{B}=$ | 186 | Ib/in^2 | $\mathrm{B}=$ | 186 | lb/in² | $\mathrm{B}=$ | 186 | lb/in^2 |
| W (width) ${ }^{\text {a }}$ | 66.864 | in | W (width) $=$ | 67.138 | in | W (width) $=$ | 66.796 | in | W (width) $=$ | 66.876 | in | W (width) ${ }^{\text {a }}$ | 66.962 | in |
| C1 $=$ | 4.078 | in | c1 $=$ | 4.017 | in | c1 $=$ | 4.185 | in | c1 $=$ | 4.064 | in | c1 $=$ | 3.981 | in |
| c2 = | 9.153 | in | c2 = | 8.94 | in | c2 = | 9.213 | in | c2 = | 9.007 | in | c2 $=$ | 9.104 | in |
| c3 $=$ | 17.22 | in | c3 = | 16.084 | in | c3 = | 17.717 | in | c3 = | 16.883 | in | c3 = | 17.02 | in |
| C4 = | 17.667 | in | C4 = | 17.468 | in | c4 = | 17.724 | in | c4 = | 17.618 | in | C4 = | 17.549 | in |
| C5 = | 17.556 | in | C5 = | 17.288 | in | c5 = | 18.323 | in | C5 = | 18.192 | in | c5 = | 17.98 | in |
| c6 = | 9.288 | in | c6 = | 9.072 | in | c6 = | 9.397 | in | c6 = | 8.986 | in | c6 = | 8.974 | in |
| $\theta=$ | 0 | degrees | $\theta=$ | 0 | degrees | $\theta=$ |  | degree: | $\theta=$ | 0 | degrees | $\theta=$ | , | degrees |
| $\mathrm{G}=$ | 336.87097 | Ibs | G = | 336.871 | Ibs | G = | 336.87 | lbs | G = | 336.871 | Ibs | G = | 336,871 | lbs |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| $\mathrm{E}=$ | 1621168 | in-lbs | E = | 1546342 | in-lbs | E = | 2E+06 | in-lbs | E = | 1623608 | in-lbs | E = | 1620430 | in-lbs |
| E= | 135097.33 | ft-lbs | E= | 128862 | ft-lbs | E= | 140353 | t-lbs | E= | 135300.6 | ft - bs | E= | 135035.8 | ft-lbs |
| w= (weight) | 3310 | Ibs | w= (weight) | 3310 | Ibs | w= (weight) | 3310 | lbs | w= (weight) | 3310 | Ibs | w= (weight) | 3310 | bs |
| $\mathrm{v}=$ | 51.268702 | $\mathrm{ft} / \mathrm{sec}$ | $\mathrm{v}=$ | 50.0716 | $\mathrm{ft} / \mathrm{sec}$ | $\mathrm{v}=$ | 52.256 | f/sec | $\mathrm{v}=$ | 51.30726 | $\mathrm{f} / \mathrm{sec}$ | $\mathrm{v}=$ | 51.25703 | f/sec |
| $\mathrm{v}=$ | 34.789403 | $\mathrm{mi} / \mathrm{hr}$ | $\mathrm{v}=$ | 33.9771 | mi/hr | $\mathrm{v}=$ | 35.46 | mi/hr | $\mathrm{v}=$ | 34.81557 | $\mathrm{mi} / \mathrm{hr}$ | $\mathrm{v}=$ | 34.78148 | mi/hr |
| CASE \#16 |  |  | CASE \#17 |  |  | CASE \#18 |  |  | CASE \#19 |  |  | CASE \#20 |  |  |
| A = | 354 | $\mathrm{lb} / \mathrm{in}$ | $A=$ | 354 | $\mathrm{lb} / \mathrm{in}$ | $A=$ | 354 | $\mathrm{lb} / \mathrm{in}$ | $A=$ | 354 | Ib/in | $A=$ | 354 | lb/in |
| $\mathrm{B}=$ | 186 | $\mathrm{lb} / \mathrm{in}^{\wedge} 2$ | $\mathrm{B}=$ | 186 | $\mathrm{lb} / \mathrm{in}^{\wedge} 2$ | $\mathrm{B}=$ | 186 | $\mathrm{lb} / \mathrm{im}^{\wedge} 2$ | $\mathrm{B}=$ | 186 | lb/in ${ }^{\text {² }}$ | $\mathrm{B}=$ | 186 | lb/in^2 |
| W (width) $=$ | 66.566 | in | W (width) $=$ | 63.601 | in | W (width) $=$ | 63.239 | in | W (width)= | 62.627 | in | W (width) $=$ | 63.015 | in |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| C1 $=$ | 5.179 | in | C1 $=$ | 5.35 | in | c1 $=$ | 5.564 | in | c1 = | 5.005 | in | c1 $=$ | 4.878 | in |
| c2 $=$ | 11.93 | in | c2 $=$ | 10.303 | in | c2 = | 10.845 | in | C2 $=$ | 10.165 | in | c2 $=$ | 10.527 | in |
| C3 $=$ | 18.274 | in | c3 $=$ | 17.432 | in | c3 $=$ | 18.436 | in | C3 $=$ | 18.128 | in | c3 $=$ | 17.791 | in |
| C4 $=$ | 19.344 | in | C4 $=$ | 19.407 | in | c4 $=$ | 19.631 | in | c4 = | 18.416 | in | C4 $=$ | 19.306 | in |
| C5 = | 19.222 | in | c5 = | 19.373 | in | c5 = | 20.162 | in | C5 = | 18.157 | in | c5 = | 19.868 | in |
| c6 = | 12.803 | in | c6 = | 10.885 | in | c6 = | 10.116 | in | c6 = | 9.639 | in | c6 = | 11.485 | in |
| $\theta=$ | 0 | degrees | $\theta=$ |  | degrees | $\theta=$ | 0 | degrees | $\theta=$ | 0 | degrees | $\theta=$ | 0 | degrees |
| G = | 336.87097 | lbs | G = | 336.871 | lbs | G = | 336.87 | lbs | G = | 336.871 | lbs | G = | 336.871 | lbs |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| $\mathrm{E}=$ | 1990970.6 | in-lbs | E = | 1789259 | in-lbs | $\mathrm{E}=$ | 2E+06 | in-lbs | E = | 1660541 | in-lbs | E = | 1819705 | in-lbs |
| E= | 165914.21 | ft-lbs | E= | 149105 | ft-lbs | $\mathrm{E}=$ | 156397 | ft-lbs | E= | 138378.4 | ft-lbs | E= | 151642.1 | t-lbs |
| w= (weight) | 3310 | Ibs | w= (weight) | 3310 | Ibs | w= (weight) | 3310 | Ibs | w= (weight) | 3310 | Ibs | w= (weight) | 3310 | bs |
| $\mathrm{v}=$ | 56.81601 | $\mathrm{ft} / \mathrm{sec}$ | $\mathrm{V}=$ | 53.8611 | f/sec | V= | 55.162 | $\mathrm{ft} / \mathrm{sec}$ | $\mathrm{V}=$ | 51.88754 | f/sec | $\mathrm{V}=$ | 54.31738 | t/sec |
| $\mathrm{v}=$ | 38.55364 | $\mathrm{mi} / \mathrm{hr}$ | $\mathrm{v}=$ | 36.5485 | mi/hr | $\mathrm{v}=$ | 37.432 | mi/hr | $\mathrm{v}=$ | 35.20933 | $\mathrm{mi} / \mathrm{hr}$ | $\mathrm{v}=$ | 36.85815 | mi/hr |

## APPENDIX 6

## EBS DETERMINATIONS FOR THE "BETWEEN" SUBJECTS DESIGN

| Between Subjects Design----Using Various M odels |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2002 Cadillac DeVille |  | case \#1 | 2003 Merce des E320 |  | case \#2 | 2001 Buick LeSabre |  | case \#3 | 2003 Toyota Avalon |  | case \#4 | 2002 Audi A4 |  | case \#5 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| $A=$ | 391.22855 | Ib/in | $A=$ | 388.90273 | Ib/in | $A=$ | 360.1776 | Ib/in | A = | 384.91497 | Ib/in | $A=$ | 425.56978 | lb/in |
| $\mathrm{B}=$ | 109.60545 | lb/in"2 | $\mathrm{B}=$ | 108.88369 | lb/in"2 | $\mathrm{B}=$ | 102.1116 | Ib/in*2 | $\mathrm{B}=$ | 118.64122 | lb/in"2 | $\mathrm{B}=$ | 149.56229 | Ib/in'2 |
| W (width of | 70.935 | in | W (width | 70.088 | in | W (width of | 70.301 | in | W(width of | 65.971 | in | W (width of | 66.017 | in |
| c1 $=$ | 15.684 | in | $\mathrm{c} 1=$ | 17.142 | in | c1 = | 18.489 | in | c1 = | 15.445 | in | c1 = | 12.025 | in |
| c2 $=$ | 17.07 | in | c2 = | 18.621 | in | c2 $=$ | 20.557 | in | c2 $=$ | 16.065 | in | c2 = | 18.162 | in |
| c3 $=$ | 19.254 | in | c3 = | 19.126 | in | c3 = | 22.23 | in | c3 $=$ | 20.026 | in | c3 $=$ | 18.831 | in |
| $\mathrm{c} 4=$ | 21.119 | in | $\mathrm{c} 4=$ | 19.839 | in | c4 = | 21.49 | in | c4 = | 20.087 | in | c4 = | 18.701 | in |
| C5 = | 21.349 | in | c 5 = | 18.018 | in | c5 = | 20.034 | in | c5 = | 15.46 | in | c5 = | 16.803 | in |
| c6 $=$ | 20.147 | in | c6 = | 17.616 | in | c6 = | 16.578 | in | c6 $=$ | 14.61 | in | c6 = | 8.965 | in |
| $\theta=$ |  | degrees | $\theta=$ |  | degrees | $\theta=$ |  | degrees | $\theta=$ |  | degrees | $\theta=$ |  | degrees |
| Q = | 698.2306917 | lbs | G = | 624.9293361 | lbs | G = | 635.2261 | Ibs | G = | 624.4016 | Ibs | G = | 605.46558 | lbs |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| $\mathrm{E}=$ | 2054101.75 | in-lbs | E= | 1846235.645 | in-lbs | E= | 2056903 | in-lbs | E= | 1672004.5 | in-libs | E= | 1900287.5 | in-lbs |
| E= | 171175.1458 | $\mathrm{ft}-\mathrm{lbs}$ | E= | 153852.9704 | $\mathrm{ft}-\mathrm{lbs}$ | E= | 171408.6 | ft -lbs | E= | 139333.7 | ft -lbs | E= | 158357.29 | ft -lbs |
| w $=$ (weigh | 4508.453262 | Ibs | w = (weig | 4265.944773 | Ibs | w = (w eight | 4102.803 | Ibs | w = (w eight | 3862.4988 | lbs | w = (w eight | 4012.4132 | Ibs |
| $\mathrm{v}=$ | 49.44808772 | $\mathrm{ft} / \mathrm{sec}$ | $\mathrm{v}=$ | 48.19347719 | $\mathrm{f} / \mathrm{sec}$ | $\mathrm{v}=$ | 51.87031 | $\mathrm{f} / \mathrm{sec}$ | $\mathrm{v}=$ | 48.198869 | $\mathrm{f} / \mathrm{sec}$ | $\mathrm{v}=$ | 50.414927 | $\mathrm{f} / \mathrm{sec}$ |
| $\mathrm{v}=$ | 33.55398888 | mi/hr | $\mathrm{v}=$ | 32.70264782 | mi/hr | $\mathrm{v}=$ | 35.19764 | mi/hr | $\mathrm{v}=$ | 32.706306 | mi/hr | $\mathrm{v}=$ | 34.210057 | mi/hr |


| 2003 Hyundai Accent |  | case \#6 | 2001 Chevy Malibu |  | caso \#7 | 2003 Honda S2000 |  | caso \#8 | 2002 Mini Cooper |  | casc \#9 | 2003 Toyota Corolla |  | case \#10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| A = | 325.15176 | lb/in | A = | 345.46882 | lb/in | A = | 437.046 | lb/in | A = | 557.569 | Ib/in | A = | 278.49701 | Ib/in |
| B = | 102.2357 | lb/in*2 | $\mathrm{B}=$ | 101.95357 | lb/in*2 | $\mathrm{B}=$ | 171.437 | $\mathrm{lb} / \mathrm{in}^{*} 2$ | $B=$ | 285.702 | $\mathrm{lb} / \mathrm{in}^{*} 2$ | $\mathrm{B}=$ | 79.30638 | Ib/in*2 |
| W (width | 57.173 | in | W (width | 61.338 | in | W (width | 64.218 | in | W (width of | 58.425 | in | W (width | 59.993 | in |
| c1 = | 11.896 | in | c1 = | 22.67 | in | c1 = | 12.51 | in | c1 = | 7.434 | in | c1 = | 14.593 | in |
| c2 $=$ | 18.695 | in | c2 = | 24.821 | in | c2 = | 16.543 | in | c2 = | 11.563 | in | c2 = | 19.252 | in |
| c3 = | 19.757 | in | c3 = | 25.071 | in | c3 = | 16.315 | in | c3 = | 15.588 | in | c3 = | 20.375 | in |
| c4 = | 18.34 | in | c4 = | 20.667 | in | c4 = | 12.301 | in | c4 $=$ | 12.127 | in | c4 = | 22.053 | in |
| c5 = | 18.872 | in | c5 = | 16.548 | in | c5 = | 13.549 | in | c5 = | 11.851 | in | c5 = | 21.267 | in |
| c6 = | 16.219 | in | c6 = | 6.827 | in | c6 = | 10.287 | in | c6 = | 10.887 | in | c6 = | 20.399 | in |
| $\theta=$ | 0 | degrees | $\theta=$ | 0 | degrees | $\theta=$ | 0 | degrees | $\theta=$ | 0 | degrees | $\theta=$ | 0 | degrees |
| G = | 517.05846 | lbs | G = | 585.309105 | lbs | G = | 557.084 | lbs | G = | 544.069 | lbs | G = | 488.99335 | lbs |
| E = | 1313086.8 | in-lbs | E = | 1845419.17 | in-lbs | E = | 1528540 | in-lbs | E = | 1665460 | in-lbs | E = | 1332912.1 | in-lbs |
| E= | 109423.9 | ft-lbs | E= | 153784.931 | ft-lbs | E= | 127378 | ft-lbs | E= | 138788 | ft-lbs | E= | 111076 | ft-lbs |
| $\mathrm{w}=$ (weig | 2914.5111 | lbs | w $=$ (wei | 3545.03318 | lbs | w = (weigh | 3229.77 | Ibs | w = (weigh | 3095.29 | lbs | w = (weigh | 2976.2405 | Ibs |
| $\mathrm{v}=$ | 49.171808 | $\mathrm{ft} / \mathrm{sec}$ | $\mathrm{v}=$ | 52.8554376 | $\mathrm{ft} / \mathrm{sec}$ | $\mathrm{v}=$ | 50.397 | $\mathrm{ft} / \mathrm{sec}$ | $\mathrm{v}=$ | 53.7364 | $\mathrm{ft} / \mathrm{sec}$ | $\mathrm{v}=$ | 49.025163 | $\mathrm{f} / \mathrm{sec}$ |
| $\mathrm{v}=$ | 33.366514 | $\mathrm{mi} / \mathrm{hr}$ | $\mathrm{v}=$ | 35.8661143 | $\mathrm{mi} / \mathrm{hr}$ | $\mathrm{v}=$ | 34.1979 | $\mathrm{mi} / \mathrm{hr}$ | $\mathrm{v}=$ | 36.4639 | $\mathrm{mi} / \mathrm{hr}$ | v= | 33.267005 | mi/hr |


| 2002 Chrysler PT Cruiser ${ }^{\text {coase \#11 }}$ |  |  | 2002 Ford Explorer Spt |  | caso \#12 | 2002 Nissan Pathfdr |  | case \#13 | 2002 Toyota Highldr |  | case \#14 | 2003 Subaru Forestor |  | caso \#15 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| A $=$ | 487.37757 | lb/in | A = | 577.3843 | lb/in | A = | 406.512 | lb/in | A = | 424.084 | Ib/in | A = | 396.79779 | lb/in |
| $\mathrm{B}=$ | 183.379 | lb/in*2 | $\mathrm{B}=$ | 226.37027 | lb/in*2 | $\mathrm{B}=$ | 109.969 | lb/in*2 | $\mathrm{B}=$ | 133.258 | lb/in*2 | $\mathrm{B}=$ | 127.71167 | $\mathrm{lb} / \mathrm{in} * 2$ |
| W (width | 66.903 | in | W (widtt | 62.313 | in | W (width ¢ | 61.163 | in | W (width ¢ | 69.39 | in | W (width ¢ | 67.924 | in |
| c1 $=$ | 13.631 | in | c1 = | 12.96 | in | c1 = | 16.98 | in | c1 = | 4.994 | in | c1 = | 15.763 | in |
| c2 $=$ | 11.59 | in | c2 = | 15.249 | in | c2 = | 27.44 | in | c2 = | 16.132 | in | c2 = | 16.169 | in |
| c3 $=$ | 15.659 | in | c3 = | 16.19 | in | c3 = | 27.873 | in | c3 $=$ | 16.305 | in | c3 = | 16.479 | in |
| c4 $=$ | 13.537 | in | c4 $=$ | 17.446 | in | c4 = | 21.03 | in | c4 = | 21.242 | in | c4 = | 16.819 | in |
| C5 = | 13.031 | in | c5 = | 16.306 | in | c5 = | 25.835 | in | c5 = | 20.838 | in | c5 = | 19.231 | in |
| c6 = | 12.584 | in | c6 = | 14.023 | in | c6 = | 9.429 | in | c6 = | 17.863 | in | c6 = | 15.123 | in |
| $\theta=$ | 0 | degrees | $\theta=$ | 0 | degrees | $\theta=$ | 0 | degrees | $\theta=$ |  | degrees | $\theta=$ | 0 | degrees |
| G = | 647.66657 | lbs | $\mathrm{G}=$ | 736.343668 | lbs | G = | 751.356 | Ibs | G = | 674.808 | lbs | $\mathrm{G}=$ | 616.42169 | lbs |
| $\mathrm{E}=$ | 1584425.7 | in-Ibs | E = | 2367994.79 | in-lbs | E = | 2471661 | in-lbs | E = | 1992659 | in-lbs | E = | 1727619.1 | in-lbs |
| E= | 132035.47 | ft -lbs | E= | 197332.899 | ft -lbs | E= | 205972 | ft -lbs | E= | 166055 | ft-lbs | E= | 143968.26 | ft-lbs |
| w = (weigh | 3723.6076 | lbs | w = (wei | 4572.38732 | Ibs | w = (weigh | 4720.1 | Ibs | w = (weigh | 4455.54 | lbs | $\mathrm{w}=$ (weigh | 3615.5811 | lbs |
| $\mathrm{v}=$ | 47.786617 | f/sec | $\mathrm{v}=$ | 52.719487 | f/sec | $\mathrm{v}=$ | 53.0117 | $\mathrm{f} / \mathrm{sec}$ | $\mathrm{v}=$ | 48.9912 | $\mathrm{ft} / \mathrm{sec}$ | $\mathrm{v}=$ | 50.639249 | f/sec |
| $\mathrm{v}=$ | 32.426565 | $\mathrm{mi} / \mathrm{hr}$ | v = | 35.7738623 | $\mathrm{mi} / \mathrm{hr}$ | $\mathrm{v}=$ | 35.9721 | mi/hr | $\mathrm{v}=$ | 33.244 | $\mathrm{mi} / \mathrm{hr}$ | $\mathrm{v}=$ | 34.362275 | $\mathrm{mi} / \mathrm{hr}$ |


| 2002 Dodge Ram 1500 |  | case \#16 | 2001 Niss an Frontier |  | case \#17 | 2003 Chevy Silverado |  | case \#18 | 01 Dodge Ram Wagon V |  | case \#19 | 2001 Dodge Caravan |  | case \#20 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $A=$ | 520.19252 | $\mathrm{lb} / \mathrm{in}$ | $A=$ | 434.13947 | Ib/in | $A=$ | 374.096 | 1b/in | $A=$ | 468.9903 | lb/in | $A=$ | 490.62915 | lb/in |
| $\mathrm{B}=$ | 169,96174 | $\mathrm{lb} / \mathrm{in}^{2}$ | $\mathrm{B}=$ | 126.4965 | lb/in'2 | $\mathrm{B}=$ | 91.75556 | lb/in*2 | $B=$ | 153.2546 | lb/in*2 | $\mathrm{B}=$ | 177.62436 | lb/in*2 |
| W (width o | 75.441 | in | W (width | 59.114 | in | W (width of | 63.216 | in | W (w idth of | 68.947 | in | W (width of | 66.771 | in |
| c1 $=$ | 14.924 | in | c1 = | 16.943 | in | c1 = | 23.045 | in | c1 $=$ | 11.296 | in | c1 = | 13.209 | in |
| c2 = | 22.356 | in | c2 = | 16.34 | in | c2 = | 28.999 | in | c2 = | 14.495 | in | c2 = | 18.65 | in |
| c3 = | 19.527 | in | c3 = | 24.804 | in | c3 = | 30.226 | in | c3 $=$ | 18.73 | in | c3 = | 19.543 | in |
| c4 $=$ | 20.137 | in | c4 = | 24.259 | in | c4 = | 30.027 | in | c4 = | 12.315 | in | c4 $=$ | 17.956 | in |
| c5 = | 13.348 | in | c5 = | 20.848 | in | c5 = | 24.911 | in | c5 $=$ | 28.105 | in | c5 = | 13.865 | in |
| c6 $=$ | 11.513 | in | c6 = | 12.451 | in | c6 = | 18.412 | in | c6 = | 20.757 | in | c6 = | 4.388 | in |
| $\theta=$ | 0 | degrees | $\theta=$ | 0 | degrees | $\theta=$ |  | degrees | $\theta=$ | 0 | degrees | $\theta=$ | 0 | degrees |
| $\mathrm{G}=$ | 796,0622722 | Ibs | $\mathrm{G}=$ | 744.9893057 | Ibs | $\mathrm{G}=$ | 762.6123 | lbs | $\mathrm{G}=$ | 717.603 | lbs | $\mathrm{G}=$ | 677.601211 | lbs |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| $\mathrm{E}=$ | 2837086.734 | in-Ibs | E= | 2133006.34 | in-lbs | E= | 2829007 | in-lbs | E= | 2446384 | in-lbs | E= | 2124822.91 | in-lbs |
| $\mathrm{E}=$ | 236423.8945 | ft -lbs | $E=$ | 177750.5283 | ft -lbs | $\mathrm{E}=$ | 235750.6 | ft -lbs | $\mathrm{E}=$ | 203885.3 | ft -lbs | $\mathrm{E}=$ | 177068.576 | ft -ibs |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| w = (weigh | 5551.239762 | Ibs | w = (weig | 4521.680997 | Ibs | w = (weight | 5200.705 | Ibs | w = (w eight | 4812.691 | Ibs | w $=$ ( w eight | 4299.01411 | Ibs |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| $\mathrm{v}=$ | 52.37133258 | $\mathrm{ft} / \mathrm{sec}$ | $\mathrm{v}=$ | 50.3151097 | $\mathrm{ft} / \mathrm{sec}$ | $\mathrm{v}=$ | 54.0304 | $\mathrm{ft} / \mathrm{sec}$ | $\mathrm{v}=$ | 52.23007 | ft sec | $\mathrm{v}=$ | 51.5026108 | $\mathrm{ft} / \mathrm{sec}$ |
| $v=$ | 35.53761515 | mi/hr | $\mathrm{v}=$ | 34.14232399 | mi/hr | $\mathrm{v}=$ | 36.66341 | mi'hr | $\mathrm{v}=$ | 35.44176 | mi/hr | $\mathrm{v}=$ | 34.9481266 | mi/hr |

## APPENDIX 7 <br> "WITHIN" BOOTSTRAP DATA"

| The Actual Within |  | Bootstrap | Sample |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Differences (Seed Data) |  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| -1.23582145 |  | -0. 19382 | 1.874921 | 0.226101 | 0.515916 | 1.565276 | 0.476458 | -0.73981 | 0.515916 | -0.73981 | -0.73981 |
| -1.647020556 |  | -1.64702 | 0.226101 | 0.515916 | 1.874921 | 0.226101 | 0.226101 | -0.35175 | -0.16768 | -0.73981 | -0.16766 |
| -0.351750929 |  | -0.38112 | 2.448286 | -1.23582 | 3.570414 | 0.18368 | -0.16766 | -1.23582 | -1.64702 | 1.565276 | 1.874921 |
| 0.515916268 |  | -1.24012 | 2.448208 | -1.00617 | -0.38112 | -1.00617 | -0.73981 | 1.874921 | -0.38112 | -0.16786 | 2.448288 |
| -0.560572583 |  | -0.19382 | -1.03263 | 1.874921 | -0.56057 | -0.16766 | -1.24012 | 0.476458 | -0.35175 | -0.16766 | 1.874921 |
| 0.183879795 |  | 0.515916 | 3.570414 | 0.226101 | 0.226101 | -0.20174 | -0.56057 | 1.874921 | 2.448286 | -0.73981 | -1.03263 |
| -1.032827733 |  | -0.35175 | 0.476458 | -0.56057 | -1.03263 | 0.228101 | 0.515916 | 0.228101 | 3.570414 | -0.73981 | -0.19382 |
| -0.73981005 |  | 0.18368 | 3.570414 | 0.515916 | 2.448286 | 0.515916 | -0.38112 | -1.23582 | -1.24012 | -0.19382 | -0.73981 |
| -1.240118814 |  | 1.565276 | -0.73981 | -1.00617 | -0.35175 | 0.226101 | 3.570414 | -1.00617 | -0.56057 | 1.874921 | 0.478458 |
| -0.381123119 |  | 1.585278 | 0.226101 | 2.448288 | -1.23582 | -0.58057 | 0.228101 | -0.38112 | -1.03263 | 1.874921 | -1.00617 |
| $-0.193823157$ |  | -1.64702 | 1.874921 | -1.24012 | 0.18368 | 0.476458 | 0.476458 | -1.00617 | -0.35175 | -0.20174 | -1.03263 |
| -1.006171272 |  | -0.73981 | -0.16798 | 0.515916 | 3.570414 | 0.515916 | -0.73981 | -0.16768 | -0.73981 | 1.565276 | -0.56057 |
| 0.478458007 |  | -1.64702 | -1.24012 | 2.448288 | 0.18388 | -0.73981 | -0.19382 | 0.18388 | 1.874921 | 1.874921 | -1.03263 |
| -0.167657171 |  | -0.56057 | 0.515916 | 3.570414 | -1.03263 | -1.23582 | -1.24012 | 0.226101 | -0.56057 | 0.476458 | -1.24012 |
| -0.201743692 |  | -0.56057 | -0.56057 | -0.16798 | 3.570414 | -1.00617 | 2.448288 | -1.23582 | 0.476458 | 0.226101 | 1.565276 |
| 3.570413542 |  | 0.476458 | -0.35175 | -1.03263 | -1.23582 | 0.228101 | 0.18368 | -1.23582 | 0.476458 | 1.565276 | -0.73981 |
| 1.565275502 |  | -0.73981 | 2.448286 | -0.38112 | -0.16766 | -0.38112 | 0.515916 | 0.18388 | -1.24012 | -1.64702 | -1.00617 |
| 2.448288293 |  | -1.23582 | -0.19382 | -0.73981 | 0.478458 | -1.23582 | -1.24012 | -1.03263 | 0.476458 | -1.00617 | -1.24012 |
| 0.226101071 |  | -1.23582 | -1.00617 | -1.00617 | 1.565276 | 0.515916 | -0.56057 | -0.16766 | -0.73981 | -1.24012 | -1.03263 |
| 1.874921215 |  | -0.38112 | -0.35175 | -1.03283 | -0.38112 | -0.56057 | -1.24012 | 1.565276 | 1.565276 | 0.226101 | -0.73981 |
|  |  |  |  |  |  |  |  |  |  |  |  |
|  | mean | -0.42243 | 0.701791 | 0.146549 | 0.590322 | -0.12089 | 0.016774 | -0.15926 | 0.119563 | 0.183291 | -0.21323 |
|  | variance | 0.884268 | 2.423431 | 1.999573 | 2.620474 | 0.520581 | 1.470753 | 1.023308 | 1.808811 | 1.323174 | 1.408715 |
|  |  | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
|  |  | 3.570414 | 1.565276 | -0.35175 | 0.476458 | -0.35175 | 0.476458 | -0.19382 | -1.00617 | -0.20174 | -0.16766 |
|  |  | -1.00617 | 0.515916 | 0.476458 | -1.03263 | -1.03263 | -1.23582 | -0.35175 | -1.64702 | -0.38112 | -1.24012 |
|  |  | -1.23582 | 2.448286 | 2.448286 | -1.64702 | -1.24012 | -1.03263 | 3.570414 | 0.18368 | -0.35175 | -1.23582 |
|  |  | -1.64702 | -1.23582 | -0.73981 | -0.16766 | 0.476458 | -0.20174 | -0.20174 | -0.73981 | -0.73981 | 0.515916 |
|  |  | -0.16766 | 0.476458 | 0.18368 | 0.476458 | -1.24012 | 0.515916 | -1.23582 | 0.18368 | -0.35175 | 3.570414 |
|  |  | 0.515916 | -1.24012 | 1.565276 | -1.00617 | -1.03263 | -1.64702 | 0.18368 | -1.24012 | -0.16766 | -1.00617 |
|  |  | -0.35175 | 0.226101 | -1.03263 | -1.24012 | -0.35175 | -1.00617 | -0.20174 | 1.874921 | 3.570414 | 2.448286 |
|  |  | 0.515916 | -0.20174 | -1.03263 | 2.448286 | 2.448286 | -0.16766 | -1.00617 | -1.64702 | 0.476458 | -1.03263 |
|  |  | -0.16766 | 1.874921 | -1.64702 | 1.874921 | -1.64702 | -0.19382 | 0.226101 | -0.38112 | -1.00617 | -1.23582 |
|  |  | -1.00617 | 0.515916 | -0.20174 | -0.35175 | 0.476458 | -1.00617 | -1.64702 | 2.448286 | -0.35175 | -0.20174 |
|  |  | 0.476458 | 0.515916 | -1.03263 | -1.64702 | -1.00617 | 3.570414 | 1.565276 | -0.38112 | 1.874921 | 0.18368 |
|  |  | 0.18368 | -1.03263 | 0.476458 | 1.874921 | -0.73981 | -0.35175 | -1.23582 | -1.24012 | 0.515916 | $-0.20174$ |
|  |  | 2.448286 | -1.00617 | -0.20174 | -1.64702 | -0.20174 | 1.874921 | -1.03263 | -1.23582 | 2.448286 | -0.73981 |
|  |  | 0.226101 | -0.38112 | 1.565276 | 0.226101 | -0.73981 | -0.16766 | 2.448286 | -0.16766 | -0.56057 | -1.64702 |
|  |  | -1.23582 | 0.476458 | 0.226101 | 1.874921 | -0.38112 | -1.24012 | -0.38112 | -0.35175 | 0.226101 | 1.874921 |
|  |  | 3.570414 | -0.56057 | -1.23582 | -0.73981 | 3.570414 | -0.38112 | -1.23582 | 0.226101 | 0.476458 | -0.16766 |
|  |  | -0.56057 | -1.64702 | 0.515916 | -1.00617 | 1.874921 | -0.16766 | 1.565276 | 3.570414 | -0.73981 | -1.00617 |
|  |  | -1.03263 | -1.03263 | -1.00617 | 0.515916 | -0.20174 | -1.64702 | 0.515916 | -0.35175 | 0.476458 | 0.515916 |
|  |  | -1.23582 | -0.56057 | -0.38112 | -1.64702 | 0.18368 | 3.570414 | 1.874921 | 0.18368 | 0.515916 | 0.476458 |
|  |  | 0.226101 | 3.570414 | 0.476458 | $-0.73981$ | -1.23582 | 1.874921 | 3.570414 | -1.03263 | $-0.56057$ | $-0.19382$ |
|  |  |  |  |  |  |  |  |  |  |  |  |
|  | mean | 0.10431 | 0.164363 | -0.04646 | -0.15521 | -0.1186 | 0.071834 | 0.339841 | -0.13757 | 0.258411 | -0.02453 |
|  | variance | 2.265645 | 1.853053 | 1.117482 | 1.766093 | 1.815433 | 2.364711 | 2.510927 | 1.855349 | 1.342475 | 1.797738 |


|  |  | 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | -1.00617 | -1.03263 | -1.23582 | 2.448286 | 2.448286 | -0.19382 | -0.56057 | -0.20174 | -0.20174 | -0.73981 |
|  |  | 0.18368 | -1.23582 | -0.35175 | 0.476458 | -1.24012 | 0.18368 | 1.874921 | -0.19382 | -1.64702 | 2.448286 |
|  |  | -0.73981 | 1.874921 | -1.03263 | -0.20174 | -0.19382 | 0.515916 | -1.24012 | 1.565276 | -0.73981 | 1.565276 |
|  |  | -0.19382 | 0.515916 | -1.64702 | -1.23582 | 3.570414 | -0.20174 | 0.476458 | 3.570414 | 1.874921 | -0.38112 |
|  |  | -1.00617 | 0.18368 | 0.18368 | 3.570414 | 0.476458 | -0.73981 | 2.448286 | -1.03263 | 3.570414 | 2.448286 |
|  |  | -1.03263 | 0.515916 | 0.226101 | 0.18368 | -0.56057 | -1.64702 | 2.448286 | -1.23582 | -1.24012 | -1.64702 |
|  |  | 1.565276 | -0.35175 | -0.35175 | 0.476458 | -0.38112 | -0.38112 | -0.38112 | -0.19382 | 1.565276 | 1.874921 |
|  |  | 0.18368 | 1.874921 | -0.19382 | -1.03263 | 0.515916 | 1.565276 | -0.20174 | -0.16766 | -0.19382 | 0.476458 |
|  |  | -0.19382 | -1.03263 | 3.570414 | -1.64702 | -1.03263 | -1.24012 | -0.73981 | -0.73981 | 0.18368 | 2.448286 |
|  |  | 1.565276 | -0.56057 | 0.18368 | 2.448286 | -1.03263 | -1.03263 | -1.23582 | -0.20174 | 1.565276 | -1.00617 |
|  |  | 2.448286 | -0.56057 | 3.570414 | -1.00617 | 0.476458 | -0.16766 | -0.19382 | -1.23582 | 3.570414 | 1.565276 |
|  |  | 0.226101 | -1.23582 | 0.476458 | 0.226101 | 0.476458 | -1.00617 | -0.73981 | 0.226101 | 1.874921 | -0.56057 |
|  |  | -1.24012 | -1.64702 | 0.476458 | 0.18368 | -0.56057 | -1.24012 | -0.73981 | -0.16766 | -0.20174 | -0.16766 |
|  |  | -0.38112 | -1.23582 | 0.476458 | -1.23582 | -0.35175 | -0.20174 | 1.565276 | 0.18368 | 0.18368 | 1.565276 |
|  |  | -0.38112 | -0.19382 | 0.226101 | -0.20174 | 3.570414 | -1.24012 | 0.18368 | 1.565276 | 0.18368 | -1.64702 |
|  |  | 1.565276 | -1.03263 | -0.35175 | -1.23582 | -0.38112 | 3.570414 | 0.476458 | 3.570414 | -1.24012 | -1.24012 |
|  |  | -0.35175 | -0.19382 | 0.18368 | -1.03263 | -1.03263 | -1.03263 | -0.73981 | 1.565276 | 0.476458 | 1.565276 |
|  |  | -0.35175 | 0.515916 | -0.16766 | -1.03263 | 0.226101 | 1.565276 | -0.38112 | -0.73981 | -1.23582 | 1.874921 |
|  |  | -0.20174 | 3.570414 | 1.874921 | 0.18368 | -1.24012 | -1.24012 | -0.73981 | -1.23582 | 0.226101 | 1.874921 |
|  |  | -1.00617 | -1.24012 | 0.18368 | -1.23582 | -0.56057 | -0.73981 | -0.73981 | -0.56057 | 0.515916 | -1.03263 |
|  |  |  |  |  |  |  |  |  |  |  |  |
|  | mean | -0.01743 | -0.12507 | 0.314992 | -0.04504 | 0.159642 | -0.2452 | 0.042009 | 0.216985 | 0.454527 | 0.564253 |
|  | variance | 1.068388 | 1.745082 | 1.773052 | 2.02191 | 2.098722 | 1.586405 | 1.338851 | 2.066258 | 2.20643 | 2.224469 |
| The Actual With in |  | Bootstrap | Sample |  |  |  |  |  |  |  |  |
| Differences (Seed Data) |  | 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 |
| -1.23582145 |  | 0.476458 | -1.00617 | 1.565276 | -1.03263 | 3.570414 | 0.515916 | -1.03263 | -1.24012 | -1.00617 | -1.23582 |
| -1.647020556 |  | 0.515916 | -1.00617 | -1.03263 | -0.35175 | -0.16766 | 0.226101 | -1.23582 | -1.64702 | -0.35175 | -0.20174 |
| -0.351750929 |  | 0.18368 | -0.73981 | -0.35175 | 2.448286 | -0.73981 | -0.56057 | -0.16766 | -0.73981 | -1.64702 | -0.38112 |
| 0.515916268 |  | 0.226101 | 0.476458 | 1.565276 | 0.476458 | -1.24012 | 3.570414 | -1.23582 | 1.565276 | 0.515916 | -1.24012 |
| -0.560572588 |  | -1.24012 | 3.570414 | -1.23582 | -1.03263 | -0.16766 | 0.226101 | -0.19382 | -0.35175 | -0.19382 | 0.515916 |
| 0.183679795 |  | -1.03263 | -1.03263 | 3.570414 | -0.19382 | 0.515916 | 1.874921 | -1.03263 | -1.03263 | -1.03263 | 1.874921 |
| -1.032627733 |  | 1.565276 | 0.476458 | 0.515916 | $-0.56057$ | 0.18368 | -1.00617 | 0.18368 | -1.23582 | -1.64702 | -0.35175 |
| -0.73981005 |  | -0.20174 | 3.570414 | 1.874921 | -0.73981 | 1.565276 | -0.35175 | 1.565276 | -0.20174 | 2.448286 | -0.73981 |
| -1.240118814 |  | -1.00617 | 0.226101 | -1.23582 | -0.20174 | 0.18368 | 0.226101 | 0.226101 | 0.18368 | 0.18368 | 0.515916 |
| -0.381123119 |  | -1.23582 | -1.00617 | 0.476458 | -1.03263 | 3.570414 | -0.38112 | 3.570414 | -1.64702 | -1.24012 | -0.56057 |
| -0.193823157 |  | 0.515916 | 2.448286 | 3.570414 | -0.38112 | -1.23582 | -1.03263 | -1.03263 | -0.73981 | 1.874921 | -0.19382 |
| -1.006171272 |  | -1.24012 | 1.565276 | 3.570414 | 0.476458 | -0.19382 | -0.35175 | -0.73981 | -1.00617 | 0.515916 | 2.448286 |
| 0.476458007 |  | -0.16766 | 0.515916 | 1.874921 | 0.476458 | -1.00617 | 0.18368 | -1.03263 | 0.18368 | 0.226101 | 3.570414 |
| -0.167657171 |  | -1.23582 | -0.19382 | -1.23582 | -1.64702 | -0.56057 | 2.448286 | 3.570414 | -0.73981 | 0.226101 | -0.73981 |
| $-0.201743698$ |  | -0.35175 | 0.476458 | -0.20174 | -0.35175 | 1.565276 | -1.03263 | -0.16766 | $-0.38112$ | 3.570414 | -0. 19382 |
| 3.570413842 |  | -0.16766 | 0.18368 | 1.874921 | -1.03263 | 0.18368 | 2.448286 | -0.19382 | -1.00617 | 0.476458 | -0.38112 |
| 1.565275502 |  | 0.515916 | -1.24012 | 0.476458 | 0.476458 | -1.03263 | -0.20174 | 0.515916 | -0.38112 | -0.20174 | -0.73981 |
| 2.448286293 |  | 0.476458 | 3.570414 | -0.73981 | 2.448286 | 0.476458 | -0.16766 | -1.00617 | -1.23582 | 1.874921 | -1.03263 |
| 0.226101071 |  | -0.19382 | -0.56057 | 0.476458 | -0.19382 | 0.18368 | -0.19382 | -0.73981 | -1.03263 | -0.56057 | 0.515916 |
| 1.874921215 |  | 2.448286 | -0.56057 | 1.874921 | 0.476458 | 0.18368 | $-0.35175$ | $-0.35175$ | $-0.35175$ | -0.73981 | 3.570414 |
|  |  |  |  |  |  |  |  |  |  |  |  |
|  | mean | -0.05747 | 0.480692 | 0.862669 | -0.07365 | 0.291895 | 0.30441 | -0.02654 | -0.65188 | 0.164603 | 0.250991 |
|  | variance | 0.956987 | 2.623009 | 2.612008 | 1.12436 | 1.865942 | 1.628076 | 1.998138 | 0.54812 | 1.906925 | 2.166393 |



| The Actual Within |  | - | Sample |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Differe nces (Seed Data) |  | 61 | 62 | 63 | 64 | 65 | 66 | 67 | 68 | 69 | 70 |
| -1.23582145 |  | -1.64702 | -1.64702 | -0.56057 | 2.448286 | 2.448286 | -1.24012 | -1.03263 | -0.56057 | 2.448286 | 1.565276 |
| -1.647020556 |  | -0.73981 | -0.16766 | -1.03263 | 0.476458 | -1.23582 | -0.38112 | 0.18368 | -0.16766 | 2.448286 | -0.19382 |
| -0.351750929 |  | 1.565276 | -1.03263 | 3.570414 | 1.874921 | -0.20174 | 0.476458 | -0.20174 | 0.18368 | 0.515916 | -0.19382 |
| 0.515916268 |  | -0.35175 | -0.38112 | 1.874921 | 0.226101 | -0,19382 | 2.448286 | -0.38112 | -1,64702 | -1,00617 | 0.226101 |
| -0.560572586 |  | 3.570414 | 0.18368 | -0.20174 | 1.874921 | -1.03263 | 0.18368 | -1.23582 | -1.24012 | -0.38112 | -1.00617 |
| 0.183679795 |  | -1.00617 | -0.73981 | -1.64702 | -0.73981 | -0.19382 | -0.16766 | -0.56057 | 0.226101 | -1.00617 | -0.35175 |
| -1,032627733 |  | -1.24012 | 1,565276 | 0.226101 | 0.515916 | 0.18368 | 1.565276 | 0.476458 | 0,476458 | -0,16766 | 2.448286 |
| -0.73981005 |  | 0.226101 | -1.00617 | -1.03263 | -0.73981 | 1.874921 | -1.03263 | -0.56057 | 0.226101 | 0.226101 | -0.38112 |
| -1.240118814 |  | 2.448286 | -1.03263 | -1.64702 | -0.73981 | -0.35175 | 2.448286 | -0.16766 | 0.18368 | -0.56057 | 0.515916 |
| -0.381123119 |  | -0.38112 | 1.874921 | 0.476458 | -0.16766 | -1.23582 | -1.24012 | -1.23582 | 3.570414 | -1.03263 | 0.476458 |
| -0,193823157 |  | -1,00617 | -1,03263 | -0.38112 | -0.20174 | -1.23582 | 1.565276 | -1.23582 | 1.874921 | -1,64702 | -0,35175 |
| -1.006171272 |  | -1.03263 | -1.24012 | -0.56057 | -1.00617 | 0.515916 | 0.226101 | 0.515916 | -0.56057 | 0.515916 | -1.64702 |
| 0.476458007 |  | -0.35175 | -1.00617 | -0.16766 | -1.64702 | -0.56057 | 1.565276 | -1.64702 | 2.448286 | -0.16766 | 1.565276 |
| -0.167657171 |  | -0.38112 | -1.03263 | -0.35175 | -0.35175 | 1.874921 | -1.00617 | -0.35175 | 0.226101 | 0.226101 | -1.64702 |
| -0.201743692 |  | -0.38112 | -1.00617 | -0.56057 | 1.565276 | 0.476458 | 1.874921 | 1.874921 | -0.38112 | 1.874921 | 1. 874921 |
| 3.570413842 |  | -1.64702 | -0.35175 | 0.226101 | -0.20174 | -0.73981 | 0.515916 | -0.56057 | -0.19382 | 2.448286 | 0.18368 |
| 1.565275502 |  | -1.24012 | -1.24012 | -0.56057 | -1.64702 | -0.16766 | 0.515916 | -1.03263 | -1.03263 | -0.38112 | -0.19382 |
| 2.448286293 |  | -1.03263 | -0,35175 | 0.476458 | 1.874921 | -0,35175 | -0.20174 | -1.24012 | -0.56057 | -1.24012 | -0,35175 |
| 0.226101071 |  | 0.515916 | 0.18368 | -1.64702 | -0.35175 | 0.476458 | -0.19382 | 1.565276 | -0.20174 | 0.226101 | 1.565276 |
| 1.874921215 |  | 0.18368 | -0.38112 | 0.515916 | -0.56057 | -0.35175 | 1.565276 | 1.874921 | -0.20174 | 3.570414 | 3.570414 |
|  |  |  |  |  |  |  |  |  |  |  |  |
|  | mean | -0.19644 | -0.4921 | -0.14923 | 0.125097 | -0,00011 | 0.474364 | -0.24763 | 0.133408 | 0.345504 | 0.383677 |
|  | variance | 1.824229 | 0.81021 | 1.500299 | 1.472232 | 1.09492 | 1.423884 | 1.106669 | 1.521112 | 2.134019 | 1.8057 |
|  |  | 71 | 72 | 73 | 74 | 75 | 76 | 77 | 78 | 79 | 80 |
|  |  | -1.24012 | 0.18368 | -0.38112 | -1.64702 | 0.18368 | -0.73981 | -0.73981 | -1.23582 | -0.20174 | -1.64702 |
|  |  | -1.24012 | 0.226101 | 1.874921 | 1.874921 | 0.515916 | 3.570414 | 3.570414 | -1.00617 | -0.38112 | -1.00617 |
|  |  | -0.20174 | -1.03263 | -0.56057 | -1.03263 | -0.19382 | 2.448286 | -1.03263 | 2.448286 | -0.56057 | -0.19382 |
|  |  | -0.19382 | -1.03263 | -1.23582 | -0.38112 | -1.03263 | -1,64702 | 0.226101 | 1.565276 | 3.570414 | -0,56057 |
|  |  | 0.226101 | -0.16766 | -0.20174 | 0.18368 | -1,00617 | 1.565276 | -0.16766 | -1.64702 | -0.56057 | -1.03263 |
|  |  | -1.64702 | -1.23582 | 1.874921 | 0.18368 | 1.874921 | 0.515916 | 0.476458 | 0.226101 | 2.448286 | 0.515916 |
|  |  | 1.565276 | 1.565276 | -1.03263 | -0.19382 | 3.570414 | -1.23582 | -0.35175 | -0.16766 | 1.874921 | -0.35175 |
|  |  | -1.00617 | -0.35175 | 2.448286 | -0.38112 | 0.515916 | -1.24012 | -1.23582 | -0.19382 | -0.56057 | 0.18368 |
|  |  | 0.18368 | -1.03263 | -1.23582 | -0.35175 | -0.38112 | 1.565276 | -0.38112 | -1.64702 | -1.64702 | -0.20174 |
|  |  | 0.226101 | 0.515916 | -0.16766 | -0.56057 | -1.24012 | -0.35175 | -1.23582 | 0.18368 | 1.874921 | -1.00617 |
|  |  | 1.565276 | 0.476458 | 0.226101 | 1.874921 | -1,64702 | -0.73981 | -0.35175 | -1.23582 | -1,00617 | -1.24012 |
|  |  | -0.38112 | 0.226101 | -1.24012 | -0.73981 | 0.476458 | -1.64702 | 0.515916 | 1.874921 | -1.23582 | 3.570414 |
|  |  | -1.03263 | -1.00617 | 1.874921 | -0.56057 | -1.64702 | -0.38112 | -0.16766 | -1.24012 | -1.64702 | -1.03263 |
|  |  | -1.24012 | 0.515916 | -1.24012 | -1.64702 | -1.64702 | 3.570414 | -1.64702 | -0.73981 | 1.565276 | 1.565276 |
|  |  | -0.20174 | 1.874921 | -0.35175 | -0.38112 | -0.38112 | -0.19382 | -0.19382 | 0.226101 | 0.18368 | 2.448286 |
|  |  | -1.64702 | 0.515916 | -0.56057 | 0.226101 | -1.24012 | -1.03263 | 3.570414 | 0.515916 | -1.24012 | -1.00617 |
|  |  | 0.515916 | 0.18368 | -0.19382 | -1,03263 | -1.23582 | 0.18368 | -1,00617 | -0.38112 | -0.19382 | -1.23582 |
|  |  | 0.476458 | 0.226101 | 1.565276 | 0.18368 | 0.18368 | 0.515916 | 2.448286 | 1.874921 | -0.19382 | -0.20174 |
|  |  | 1.565276 | 3.570414 | 2.448286 | -0.19382 | 2.448286 | 0.515916 | -0.35175 | -1.23582 | 2.448286 | -1.00617 |
|  |  | -0.38112 | 0.515916 | 2.448286 | -0.56057 | -0.16766 | -1.03263 | 2.448286 | -0.73981 | -1.64702 | -1.64702 |
|  |  |  |  |  |  |  |  |  |  |  |  |
|  | mean | -0.20443 | 0.236856 | 0.317962 | -0.25683 | -0.10252 | 0.210477 | 0.219654 | -0.12774 | 0.144519 | -0.2543 |
|  | variance | 1,035304 | 1.315486 | 1,958315 | 0.818233 | 2.002625 | 2.545293 | 2.424563 | 1.548085 | 2.486959 | 1.864642 |


|  |  | 81 | 82 | 83 | 84 | 85 | 86 | 87 | 88 | 89 | 90 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | -1.23562 | 0.15368 | -0.38112 | 0.476458 | -0.16766 | -0.56057 | 0.226101 | -0.19362 | -1.03263 | 2.448266 |
|  |  | -0.16766 | -1.64702 | -0.20174 | -0.19362 | -1.64702 | 0.515916 | 1.565276 | -0.16766 | -1.03263 | 0.226101 |
|  |  | 0.18368 | 2.448266 | -1.24012 | 0.226101 | -0.35175 | -0.56057 | -1.00617 | 0.226101 | 0.18368 | 0.476456 |
|  |  | -0.16766 | 3.570414 | -1.23582 | -1.24012 | 0.515916 | -0.38112 | -1.00617 | -0.20174 | -1.23562 | 0.18366 |
|  |  | -0.73951 | -1.24012 | -1.24012 | -0.56057 | -1.03263 | 0.476458 | 1.565276 | -1.23562 | -0.38112 | 0.18366 |
|  |  | 0.476458 | -1.23582 | -0.16766 | 0.476458 | 1.565276 | -0.73981 | -0.16766 | -0.19362 | -1.64702 | -0.38112 |
|  |  | 1.874921 | -0.35175 | -0.35175 | 1.565276 | -0.35175 | -0.56057 | -1.24012 | -0.73961 | 1.874921 | -0.20174 |
|  |  | 0.515916 | -1.00517 | 3.570414 | 0.476458 | -0.73961 | -0.35175 | -0.19362 | -0.19362 | -0.16766 | 1.565276 |
|  |  | 0.18368 | -1.00617 | 2.445286 | 0.73981 | 2.448266 | -0.20174 | -0.73951 | 0.18368 | 0.226101 | 0.19362 |
|  |  | 0.226101 | -1.03263 | 0.476458 | 0.476458 | 0.18368 | -0.35175 | -0.38112 | -1.03263 | -1.64702 | 2.445206 |
|  |  | -1.24012 | 0.15368 | -1.64702 | 0.18368 | -1.24012 | -1.24012 | -0.35175 | -0.35112 | -0.73981 | -1.24012 |
|  |  | 0.476458 | 0.226101 | -0.16766 | -0.20174 | -0.35175 | -1.24012 | -1.24012 | -1.64702 | -1.24012 | -0.73981 |
|  |  | -0.73981 | -1.00617 | -0.16766 | -1.64702 | -0.38112 | -0.19382 | -1.64702 | 0.228101 | 0.478458 | 0.478458 |
|  |  | -1.00617 | 0.515916 | -0.16766 | -1.24012 | 1.585276 | -0.38112 | 0.18368 | -0.19362 | -0.38112 | 1.565276 |
|  |  | -0.38112 | -0.16766 | -1.64702 | -1.64702 | -1.23582 | -0.56057 | 1.585276 | -1.03283 | -1.24012 | 0.18368 |
|  |  | 0.18368 | 1.585276 | -0.19382 | -0.56057 | 0.18368 | -0.38112 | 2.448288 | -0.73981 | -0.16768 | -0.19362 |
|  |  | -0.38112 | -0.56057 | -1.23582 | -1.64702 | 2.448288 | -1.84702 | -0.35175 | -0.16768 | 0.478458 | -0.35175 |
|  |  | 1.874921 | 2.448286 | -0.38112 | 2.448286 | 0.515916 | 0.228101 | -0.20174 | -0.35175 | -0.16768 | -0.20174 |
|  |  | 0.18368 | $-0.19382$ | 0.228101 | -0.35175 | 3.570414 | -0.20174 | -0.73981 | 0.226101 | -0.20174 | -0.38112 |
|  |  | 0.515916 | -1.03283 | -0.16786 | -0.73981 | -1.23582 | -0.16788 | -0.20174 | -0.35175 | $-1.64702$ | -1.03263 |
|  | mean | 0.031806 | 0.033055 | 0.19363 | -0.22201 | 0.213074 | -0.42514 | -0.09575 | -0.39814 | -0.48458 | 0.241975 |
|  | variance | 0.721145 | 2.052649 | 1,603104 | 1.13633 | 2.041648 | 0.281713 | 1.194397 | 0.269683 | 0.79971 | 1.055054 |
| The Actual Within | Bootstrap Sample |  |  |  |  |  |  |  |  |  |  |
| Differences (Seed Data) |  | 91 | 92 | 93 | 94 | 96 | 96 | 97 | 98 | 99 | 100 |
| -1.23582145 |  | 0.18368 | 0.18368 | 1.565276 | 1,874921 | -0.16766 | 0.476458 | -0,35175 | -1,03263 | -0.20174 | -0,56057 |
| -1,647020556 |  | -1.23582 | -1.23582 | -0,35175 | 0.226101 | -0.73981 | 2.448286 | 2.448286 | -0,35175 | -1,64702 | 2.448286 |
| -0,351750929 |  | 1,565276 | -1.23582 | -0.35175 | -0.73981 | 0.515916 | -1,64702 | -0.19382 | -0,35175 | -0.35175 | -0,35175 |
| 0.515916268 |  | 0.18368 | 0.515916 | 2.448286 | 0.226101 | 3.570414 | 1.565276 | -1.23582 | -1,23582 | -0.35175 | -0,38112 |
| -0.560572586 |  | -0.35175 | -0.16766 | -1,00617 | -0.16766 | -0.35175 | -0.16766 | -0,38112 | -1.23582 | -0.56057 | -1,64702 |
| 0.183679795 |  | -0.20174 | -1.64702 | -0.56057 | -1.00617 | 0.18368 | -0.38112 | -0.56057 | -0.38112 | 0.18368 | -0.20174 |
| -1.032627733 |  | 0.476458 | -1.24012 | 3.570414 | -0.16766 | -1.23582 | -0.38112 | -0.19382 | 1.874921 | 2.448286 | 1.565276 |
| -0.73981005 |  | 1.874921 | -0.16766 | -0.20174 | 0.226101 | 2.448286 | -1.64702 | 1.565276 | 0.18368 | -1.64702 | -1.23582 |
| -1.240118814 |  | -1.03263 | -0.73981 | -1.03263 | -1.24012 | -0.56057 | -1.00617 | -0.56057 | -0.73981 | -1.03263 | -0.35175 |
| -0.381123119 |  | -0.73981 | 0.515916 | -0.56057 | -1.24012 | 0.476458 | -0.35175 | -0.20174 | -0.56057 | -0.56057 | -0.19382 |
| -0.193823157 |  | -0.56057 | -0.73981 | -1.03263 | 0.476458 | -0.20174 | -0.16766 | -0.38112 | -0.16766 | -1.03263 | -0.73981 |
| -1.006171272 |  | 2.448286 | -0.35175 | -0.19382 | 3.570414 | 1.874921 | 3.570414 | 1.874921 | -1.64702 | -0.19382 | -1.03263 |
| 0.476458007 |  | -1.00517 | -1.00617 | -1.00517 | 3.570414 | -0.38112 | -1.64702 | -0.38112 | -0.56057 | -0.56057 | -0.73981 |
| -0.167657171 |  | 1.874921 | 3.570414 | -1.03263 | -0.56057 | -1.64702 | 0.515916 | -1.24012 | -0.56057 | -0.19382 | 1.874921 |
| -0.201743692 |  | -0.20174 | -0.73981 | -1.64702 | 2.448286 | -0.56057 | 0.18368 | -0.19382 | -0.35175 | -0.19382 | -0.35175 |
| 3.570413842 |  | -0.35175 | -0.20174 | 0.515916 | 0.476458 | -0.19382 | -0.35175 | 1.874921 | -0.56057 | 0.18368 | -0.35175 |
| 1.565275502 |  | -1.24012 | 0.515916 | -1.24012 | -0.16766 | -0.20174 | -0.20174 | -0.19382 | -0.35175 | -0.56057 | -0.73981 |
| 2.448285293 |  | 1.565276 | -1.00617 | -1.03263 | -0.16766 | 0.226101 | -0.56057 | -1.23582 | -0.73981 | -1.64702 | -0.56057 |
| 0.226101071 |  | -1.64702 | 0.476458 | 1.874921 | -0.73981 | -0.73981 | 3.570414 | -0.16766 | -1.64702 | -1.64702 | -0.35175 |
| 1.874921215 |  | 0.226101 | -0.35175 | 3.570414 | -0.73981 | 1.565276 | 0.18368 | -0.56057 | -1.64702 | 0.476458 | -1.64702 |
|  |  |  |  |  |  |  |  |  |  |  |  |
|  | mean | 0.091473 | -0.25264 | 0.114751 | 0.307911 | 0.19398 | 0.200176 | -0.01349 | -0.60322 | -0.45451 | -0.2775 |
|  | variance | 1.428955 | 1.255092 | 2.576467 | 2.098587 | 1.626946 | 2.305194 | 1.146574 | 0.60791 | 0.884113 | 1.134259 |
| Mean of 100 BootstrapSample Means: |  |  |  |  |  |  |  |  |  |  |  |
|  | 0.0533 |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |
| Mean Variance of |  |  |  |  |  |  |  |  |  |  |  |
| 100 Bootstrap Samples: | 1.6365 |  |  |  |  |  |  |  |  |  |  |

## APPENDIX 8 <br> "BETWEEN" BOOTSTRAP DATA"

| The Actual Between Differences (Seed Data) |  | Bootstrap Sample |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| -2.575302308 |  | 0,096352 | 1.342703 | -2.4944 | 1,075882 | -1.20164 | 1.213169 | -2.5753 | 0.731935 | 1.342703 | 0.436328 |
| -2.498058383 |  | 0.393647 | -2.4944 | 1.075882 | 1.342703 | 1.342703 | -1.44098 | 1.075882 | 1.567686 | -1.44098 | -1.74614 |
| -2.494399823 |  | 1.567686 | 0.436328 | 1.075882 | 0.096352 | -0.7477 | -2.4944 | 1.567686 | 1.567686 | -1.33088 | -2.4944 |
| -1.746136787 |  | -2.4944 | -1.20164 | -2.5753 | 1.075882 | 1.342703 | -1.33088 | -0.79181 | 1.213169 | -1.74614 | -1.44098 |
| -1.473886444 |  | -2.4944 | 0.393647 | 0.096352 | -0.79181 | -1.33088 | -2.4944 | -0.7477 | -2.49808 | 1.928733 | -1.74614 |
| -1,440979236 |  | -2.49806 | -0.79181 | -0.79181 | -1.47389 | -2.5753 | -2.5753 | 0,436328 | 0.731935 | -0.79181 | -1.74614 |
| -1.330881548 |  | 0.436328 | -2.5753 | -1.47389 | -2.5753 | -1.03727 | 1.075882 | 0.096352 | 1.213169 | 0.731935 | 1.075882 |
| -1.201643376 |  | 0.436328 | -2.4944 | 0.436328 | -0.7477 | -1.74614 | 0.436328 | -1.20164 | -2.4944 | 1.213169 | 0.393647 |
| -1.037270045 |  | 1.213169 | 0.731935 | -1.03727 | -1.33088 | 0.436328 | -2.5753 | 0.098352 | 0.393847 | 1.567688 | 0.393847 |
| -0.791810326 |  | 0.731935 | 1.213169 | 1.075882 | 0.731935 | -0.7477 | 1.928733 | -1.03727 | 1.567686 | 1.213169 | -0.79181 |
| -0.74769637 |  | -1.03727 | -1.74614 | 1.567686 | -1,33088 | 0.436328 | -1.74614 | -1.74614 | -1,47389 | 0.393647 | 0.436328 |
| 0.096351785 |  | 1.075882 | -2.49806 | -1.03727 | 1.213169 | 0.096352 | -2.5753 | 0.731935 | -1.03727 | -0.79181 | -2.49806 |
| 0.393646966 |  | -1.44098 | -2.4944 | 0.096352 | 0.731935 | -0.79181 | 1,342703 | -1.20164 | -1.44098 | 0.393647 | 0,436328 |
| 0.438328416 |  | 1.567888 | -1.20164 | -1.44098 | 0.393647 | -1.33088 | 1.213169 | 1.928733 | 0.436328 | 1.928733 | 0.098352 |
| 0.731934905 |  | -1.74614 | -0.79181 | 1.928733 | -1.03727 | 0.436328 | -1.47389 | -2.5753 | 1.075882 | 1.342703 | 1.075882 |
| 1.075882095 |  | -1.20164 | -0.7477 | -1.44098 | -2.49806 | 1.567688 | 1.342703 | 0.393847 | -1.47389 | 1.928733 | 1.342703 |
| 1.213168948 |  | -2.49806 | 1.075882 | -1.20164 | -1.74614 | 1.928733 | 1.928733 | -1.20164 | 0.393647 | 1.342703 | -2.49806 |
| 1,342703247 |  | -1.74614 | -1.74614 | -1,44098 | 1.075882 | -1,74614 | -2,49806 | -1,20164 | 1.928733 | -2.4944 | 1.213169 |
| 1.567686138 |  | 1.213169 | -0.79181 | -1.47389 | -1.03727 | 1.342703 | -1.44098 | 0.393647 | -1.44098 | -1.20164 | 0.098352 |
| 1.928732533 |  | -2.49806 | $-0.79181$ | 1.213169 | 1.928733 | -2.49806 | 0.096352 | 0.393647 | 1.928733 | -0.79181 | 0.436328 |
|  |  |  |  |  |  |  |  |  |  |  |  |
|  | mean | -0.54615 | -0.85867 | -0.39211 | -0.24515 | -0.34118 | -0.60339 | -0.35829 | 0.144539 | 0.236904 | -0.37644 |
|  | variance | 2.420567 | 1.797805 | 1,889838 | 1,867109 | 1.92718 | 3.041639 | 1.596227 | 2.215988 | 2.007183 | 1.81045 |
|  |  | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
|  |  | -1.33088 | 1.075882 | -0.79181 | 0.731935 | 1.213169 | -1.20164 | 1.567686 | 1.928733 | 0.731935 | 0.731935 |
|  |  | -0.7477 | 0.393647 | 0.436328 | -1.33088 | 0.731935 | -1.74614 | 1.342703 | 1.567686 | 1.567686 | 1.928733 |
|  |  | -2.4944 | -2,49806 | 0.436328 | 1,342703 | -1.47389 | 0.436328 | 1.213169 | 1.567685 | 0.436328 | -2.5753 |
|  |  | 1.075882 | -0.7477 | -2.5753 | -1.74614 | -1.33088 | 1.075882 | -1.47389 | 1.213169 | 1.567686 | -2.4944 |
|  |  | 0.393647 | -1.47389 | -2.4944 | 1.342703 | 0.096352 | -1.03727 | 1.075882 | -1.47389 | -1.20164 | -1.20164 |
|  |  | -2.4944 | 1.075882 | -1.20164 | 0.436328 | 0.436328 | -0.7477 | 0.393647 | 1.567686 | 0.731935 | -1.03727 |
|  |  | -1.47389 | -1.33088 | -1.03727 | -1.20164 | 1.928733 | -1,33088 | $-0.7477$ | 1.342703 | 0.731935 | -1.47389 |
|  |  | -0.79181 | 0.096352 | -2.5753 | -1.74614 | -2.49806 | -1.47389 | -1.03727 | 1.075882 | -1.33088 | -0.79181 |
|  |  | -2.5753 | 1.928733 | -1.33088 | -2.49806 | 1.075882 | 0.393647 | 1.567686 | -2.49806 | -1.47389 | -1.44098 |
|  |  | -1.03727 | 0.096352 | -2.49806 | 1,567686 | 1.928733 | -1,44098 | 0.436328 | 1.342703 | 1.075882 | -2.4944 |
|  |  | -1.47389 | -1.47389 | 0.436328 | 0.393847 | -1.74614 | 1.213169 | -0.79181 | -2.5753 | 1.342703 | -1.74614 |
|  |  | -0.7477 | 0.731935 | -1.20164 | 1.928733 | -1.44098 | -0.7477 | 1.567686 | 0.731935 | 1.075882 | 0.731935 |
|  |  | 1.342703 | 0.731935 | 0.436328 | -1.33088 | 1.567686 | -0.79181 | -2.5753 | 1.567686 | 1.342703 | -1.03727 |
|  |  | -1.03727 | 1.342703 | -1.20164 | -2.49806 | 1.075882 | -2,49805 | -0.79181 | -2.4944 | -0.7477 | 0.393647 |
|  |  | 1.213169 | -1.47389 | -1.74614 | -1.47389 | 1.342703 | -1.33088 | -1.33088 | -1.44098 | -2.5753 | -1.47389 |
|  |  | -1.33088 | 1.567686 | 0.096352 | 1.213169 | 1.928733 | 1.928733 | -1.33088 | -2.5753 | 1.342703 | -1.47389 |
|  |  | 0.393647 | 1.075882 | 1.342703 | -1.74614 | -2.49806 | 1.567686 | 1.342703 | -1.20164 | 1.567686 | -1.03727 |
|  |  | -2.49806 | 1.075882 | 1.342703 | 0.096352 | -1.74614 | 0.393647 | 1.342703 | -1,33088 | 1.213169 | -1.74614 |
|  |  | 1.213169 | -1.44098 | -1.44098 | -1.33088 | 1.213169 | -1.44098 | -1.47389 | 1.213169 | 0.096352 | 1.342703 |
|  |  | -0.79181 | 1.075882 | 0.436328 | 0.731935 | -1.47389 | 1.075882 | -2.5753 | -2.4944 | 0.436328 | 1.567686 |
|  |  |  |  |  |  |  |  |  |  |  |  |
|  | mean | -0.75965 | 0.091474 | -0.75658 | -0.35588 | 0.016564 | -0.38515 | -0.11393 | -0.14829 | 0.398575 | -0.76638 |
|  | variance | 1.705265 | 1.684725 | 1.672453 | 2.142414 | 2.535787 | 1.627363 | 2.080893 | 3.198208 | 1.473624 | 1.922445 |
|  |  |  |  |  |  |  |  |  |  |  |  |



|  |  | 41 | 42 | 43 | 44 | 46 | 46 | 47 | 48 | 49 | 60 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | -1.33088 | -1.47389 | -2.49806 | -1.03727 | -1.74614 | -2.49806 | -2.49806 | 0.731935 | -0.7477 | -2.4944 |
|  |  | -1.33088 | 1.342703 | -2.49806 | -0.7477 | -2.5753 | 0.436328 | 0.731935 | -2.4944 | 0.393647 | -1.20164 |
|  |  | 0.731935 | -1.20164 | 0.393647 | -0.79181 | 0.096352 | -0.79181 | 1.342703 | -1,33088 | 1.213169 | -2.49806 |
|  |  | 1.213169 | -1.44098 | -0.7477 | 1.928733 | -1.33088 | -2.5753 | -0.7477 | -1.20164 | 1.567685 | 1.342703 |
|  |  | 0.436328 | 0.096352 | -2.4944 | 0.393647 | 1.928733 | -1.44098 | -0.79181 | -1.20164 | -1.74614 | 0.393647 |
|  |  | -1,47389 | -0.79181 | 1,213169 | 0.436328 | -2.49806 | -2,49806 | 0.096352 | 1.567688 | 0,393647 | -0.79181 |
|  |  | 0.096352 | 1.567686 | -1.03727 | -1.03727 | -1.33088 | 1.342703 | -1.33088 | -2.4944 | -2.5753 | 1.075882 |
|  |  | -0.79181 | -2.49806 | -0.7477 | -1.33088 | -1.03727 | -1.47389 | 1.56763 | -2.5753 | -0.7477 | -2.5753 |
|  |  | -1,47389 | 1.567686 | -1,20164 | -1.74614 | 0.436328 | 1.567686 | -1.74614 | -0.79181 | -1,20164 | -1,33088 |
|  |  | 0.096352 | 1.342703 | -1.20164 | 1.213169 | 0.731935 | 0.393647 | -0.79181 | -1.47389 | -1.74614 | -2.49806 |
|  |  | -1.47389 | -2.4944 | 1.928733 | 0.436328 | -1.47389 | -2.4944 | -1.03727 | -1.03727 | 1.342703 | -2.4944 |
|  |  | -0.79181 | 1,075882 | 1,342703 | -1.74614 | 0.731935 | 1,342703 | -1.74614 | 0,436328 | -0.79181 | -2.49806 |
|  |  | 1.928733 | 0.731935 | -1.44098 | -2.5753 | -2.4944 | 1.567686 | -0.7477 | -1.47389 | 1.213169 | 0.436328 |
|  |  | 0.393647 | -2.5753 | -1.47389 | 0.096352 | 0.096352 | 0.436328 | 1.567686 | -1.33088 | -2.49806 | -2.5753 |
|  |  | -1.44098 | 1.56768 | -0.7477 | -2.49806 | -1.74614 | -1.47389 | 1.928733 | -1.20164 | 1.213169 | -1.44098 |
|  |  | 0.731935 | 0.436328 | -1.03727 | 0.393647 | -1.44098 | 0.731935 | -1.20164 | 1.075882 | -2.49806 | -2.5753 |
|  |  | 1.567686 | -1.03727 | -1.44098 | 0.436328 | -1.74614 | 0.731935 | 1.075882 | 0.436328 | -1.03727 | 1.342703 |
|  |  | -0.7477 | -2.4944 | -1.74614 | 0.096352 | 1.342703 | -1.47389 | 0.393647 | -0.7477 | 1.075882 | -2.4944 |
|  |  | -1,33088 | 1.567686 | 1.567686 | 1.075882 | 1.928733 | -1,33088 | 0.393647 | 1.213169 | -0.79181 | -1,44098 |
|  |  | -0.79181 | -2.4944 | 1.075882 | -0.79181 | 0.096352 | 1.928733 | 0.436328 | 0.096352 | -1.33088 | -1.74614 |
|  |  |  |  |  |  |  |  |  |  |  |  |
|  | mean | -0.28911 | -0.36028 | -0.63958 | -0.38978 | -0,60153 | -0.37857 | -0. 15523 | -0.68988 | -0,46497 | -1,30322 |
|  | variance | 1.250536 | 2.719336 | 1.967222 | 1.521943 | 2.126548 | 2.489909 | 1.640026 | 1.581639 | 1.983853 | 2.07728 |
| The Actual B |  | 51 | 52 | 53 | 54 | 55 | 56 | 57 | 58 | 59 | 60 |
| Differences (See d Data) |  | 0.393647 | -1.33088 | 0.436328 | -2.49806 | -0.79181 | -1.44098 | -1.20164 | -0.79181 | -2.49806 | 0.731935 |
| -1.746136787 |  | -1.74614 | -1.20164 | 1.213169 | 0.436328 | -1.20164 | -0.7477 | -2.5753 | 0.436328 | -2.4944 | 0.731935 |
| -2.498058383 |  | 1.213169 | 0.436328 | -0.7477 | -1.20164 | -1,44098 | -1.74614 | -1.47389 | -1.44098 | -2.4944 | 0.436328 |
| 0.096351785 |  | -0.7477 | -1.20164 | -0.79181 | 0.096352 | -0.79181 | 1.213169 | -1.74614 | -2.49806 | 0.436328 | 1.567686 |
| -2.494399823 |  | -2.4944 | -1.33088 | 1.075882 | 1.928733 | -1.47389 | 0.731935 | 0.096352 | -1.47389 | 0.096352 | -0.79181 |
| -0.791810326 |  | 1.075882 | -1.20164 | 1.567686 | 0.436328 | -0.79181 | -2.4944 | -1.20164 | 1.928733 | -2.5753 | 0.393647 |
| -1.330881548 |  | -2.5753 | -2.5753 | -0.79181 | -2.4944 | 0.731935 | -1.44098 | 0.096352 | -2.49806 | 0.096352 | -0.79181 |
| 1.342703247 |  | 0.436328 | -1.33088 | 1.928733 | 1.075882 | 1.928733 | 1.342703 | -0.7477 | -1.44098 | -1.33088 | -1.33088 |
| -1.201643376 |  | 1.213169 | -1.47389 | 0.393647 | -0.79181 | -0.79181 | -1.03727 | 1.928733 | -0.79181 | 1.213169 | 1.213169 |
| 1.567686138 |  | -0.7477 | 1.928733 | -0.7477 | -1.44098 | -1.74614 | 0.393647 | -0.7477 | -1.47389 | 1.213169 | -1.47389 |
| -1,473886444 |  | -2.5753 | 1.928733 | 0,436328 | -1.33088 | -1.44098 | 1.213169 | 1.342703 | -2.4944 | 1.213169 | -1.20164 |
| -2.575302308 |  | 1.075882 | 0.731935 | -1.33088 | 0.393647 | -1.33088 | 1.928733 | 1.075882 | -1.20164 | -1.47389 | -0.7477 |
| 1.213168948 |  | -2.5753 | -2.49806 | 0.731935 | 0.731935 | -1.20164 | -1.47389 | 1.567686 | -1.44098 | -1.20164 | 0.731935 |
| 1.075882095 |  | 1.213169 | -1.33088 | 0.731935 | -1.33088 | -2.49806 | -2.49806 | -1.33088 | -1.20164 | -0.79181 | -1.44098 |
| -1.440979236 |  | -1.20164 | -1.44098 | -1.33088 | -2.4944 | -0.7477 | -2.49806 | -1.74614 | -1.47389 | -1.03727 | -2.4944 |
| -1.037270045 |  | -1.47389 | -2.4944 | 0.393647 | -0.79181 | 1.075882 | -0.7477 | 1.928733 | -2.5753 | -1.47389 | -1.20164 |
| 0.436328416 |  | 1.928733 | 1.342703 | 1.075882 | -1.33088 | -1.03727 | -1.33088 | -1.74614 | -2.5753 | 1.075882 | -2.49806 |
| -0.74769637 |  | -1.33088 | 1.075882 | 0.393647 | -0.79181 | -1.74614 | 0.096352 | -1.03727 | -0.7477 | 0,436328 | -1.20164 |
| 1.928732533 |  | -1.33088 | 0.731935 | 1.213169 | 0.393647 | 0.393647 | -2.4944 | 1.928733 | 1.342703 | -1.47389 | -0.79181 |
| 0.731934905 |  | -1.03727 | 0.436328 | 0.096352 | 0.096352 | 1.075882 | -1.47389 | 0.393647 | 0.436328 | 0.731935 | -2.49806 |
| 0.393646966 |  |  |  |  |  |  |  |  |  |  |  |
|  | mean | -0.56432 | -0.53993 | 0.297378 | -0.54542 | -0.69132 | -0.72523 | -0.25978 | -1.09881 | -0.61664 | -0.63288 |
|  | variance | 2.260366 | 2.146438 | 0.921499 | 1.556434 | 1.296453 | 2.057033 | 2.116133 | 1.640528 | 1.876565 | 1.545553 |



|  |  | 81 | 82 | 83 | 84 | 85 | 86 | 87 | 88 | 89 | 90 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 0.731935 | 1.213169 | 1.213169 | 1.213169 | 1.075882 | -2.5753 | 1.342703 | -2.4944 | 1.075882 | -1.03727 |
|  |  | 1.213169 | 0.393647 | -2.5753 | 0.436328 | -0.79181 | -1.03727 | -1.44098 | -1.74614 | 0.436328 | 1.342703 |
|  |  | 1.567686 | 0.393647 | -2.5753 | -1.20164 | -1.20164 | -2.4944 | -2.4944 | -1.74614 | -1.20164 | 0.731935 |
|  |  | -1.74614 | 1.213169 | -1.03727 | 1.213169 | -1.03727 | 1.213169 | 0.436328 | -1.20164 | 0.393647 | 0.393647 |
|  |  | -0.79181 | 1.342703 | 0.096352 | -0.79181 | 0.731935 | -1.74614 | -2.5753 | -1.20164 | -1.20164 | -2.4944 |
|  |  | -1,33088 | -0.7477 | 1.213169 | 0.096352 | -0.7477 | -2.5753 | -0.79181 | 1,928733 | -1.20164 | 0,096352 |
|  |  | -2.4944 | -2.49806 | 1,342703 | -1.74614 | -1.74614 | -1.47389 | -1.20164 | 1,342703 | -1.33088 | 1.213169 |
|  |  | 1.567686 | 1.928733 | 0.731935 | 0.393647 | -2.49806 | 0.436328 | 0.731935 | 1.075882 | 0.393647 | 0.436328 |
|  |  | 1.213169 | 1.342703 | 0.731935 | 1.928733 | -1.44098 | -1.44098 | -2.4944 | 1.928733 | -2.4944 | -0.7477 |
|  |  | 1.213169 | 1.567686 | -2.49806 | -1.03727 | 0.436328 | 1.213169 | -2.5753 | -1.03727 | 0.731935 | -1.44098 |
|  |  | 1.928733 | -1.33088 | 0.096352 | -1.33088 | 1.075882 | 1.342703 | -2.5753 | 1.075882 | -1.44098 | 0.096352 |
|  |  | -1.33088 | -0.79181 | -2.4944 | 0.436328 | 1.567686 | 1.213169 | 0.096352 | 1.075882 | 0.393647 | 1.928733 |
|  |  | -2.5753 | -1,47389 | -1.74614 | -2.4944 | -2.49806 | -0.79181 | -0.79181 | -2.5753 | -0.7477 | -1,20164 |
|  |  | -1.47389 | 0.731935 | -1.03727 | -0.7477 | 1.075882 | 1.567686 | -0.7477 | 0.436328 | -1.20164 | -1,44098 |
|  |  | 1.928733 | 0.436328 | 1.213169 | -2.49806 | -2.49806 | 1.928733 | -1.44098 | -1.47389 | -0.79181 | -1.03727 |
|  |  | 1.075882 | -0.7477 | -0.79181 | -2.49806 | -1.20164 | 1.075882 | -1.44098 | -0.7477 | 0.393647 | -1.74614 |
|  |  | -0.79181 | -2.5753 | -2.5753 | -1.74614 | 1.928733 | 1.928733 | 0.436328 | 1.075882 | 0.096352 | -2.4944 |
|  |  | 0.096352 | 0.393647 | -0.7477 | -0.7477 | 0.096352 | -1.74614 | -0.7477 | -1.44098 | -1.74614 | -1.33088 |
|  |  | 1.928733 | -0.7477 | 1.928733 | -1,33088 | -0.7477 | 1,567686 | -1.74614 | -1.33088 | -1,33088 | -2.4944 |
|  |  | 1.928733 | 0.731935 | 1.928733 | -0.7477 | 1,342703 | 1,075882 | -1.03727 | -1,47389 | -1,44098 | 0.731935 |
|  |  |  |  |  |  |  |  |  |  |  |  |
|  | mean | 0.192943 | 0.038814 | -0.37912 | -0.66003 | -0.35388 | -0.0659 | -1.0529 | -0.42649 | -0.61076 | -0.52475 |
|  | variance | 2.528453 | 1.765456 | 2.664179 | 1.666464 | 2.06521 | 2.764636 | 1.424595 | 2.215414 | 0.998962 | 1.827204 |
|  |  | 91 | 92 | 93 | 94 | 95 | 96 | 97 | 98 | 99 | 100 |
|  |  | 0.393647 | 0.393647 | -0.7477 | -2.5753 | -2.5753 | 0.393647 | 0.436328 | -1.20164 | -1.20164 | 0.731935 |
|  |  | 1,342703 | 0.393847 | 0.731935 | -1.44098 | -0.79181 | 1.928733 | 1.342703 | -1.20164 | -2.5753 | -0.79181 |
|  |  | -1.47389 | -2.4944 | -1.47389 | 1.828733 | 0.096352 | 1.075882 | 1.075882 | -2.5753 | -2.49808 | -2.49808 |
|  |  | 1.567696 | 1.667686 | -1.20164 | -2.5753 | -0.79181 | -1.44098 | 1.067686 | 1.075882 | 0.436328 | -0.7477 |
|  |  | -2.4944 | -1.20164 | -1,33088 | 1,928733 | -2.4944 | -0.79181 | -1.44098 | -1.47389 | -2.4944 | -2.4944 |
|  |  | -0.7477 | 0.393847 | -2.4944 | 0.436328 | -1.74614 | -1.47389 | 0.096352 | -1.20184 | -1.44098 | -1.74814 |
|  |  | 1.075882 | 0.731935 | -1.03727 | -2.5753 | -1.20164 | -1.47389 | -1.74614 | -2.49806 | 1.928733 | 1.213169 |
|  |  | -1.74614 | -1.74514 | 1.928733 | -1.20164 | -1.33088 | 0.096352 | 0.393647 | 0.393647 | 0.096352 | 1.213169 |
|  |  | -1.33088 | 1.213169 | -1.44098 | -0.7477 | 0.393847 | -2.49806 | 0.096352 | 0.393847 | 0.731935 | -2,5753 |
|  |  | 1.567888 | -0.79181 | 0.096352 | -1.44098 | -1.33088 | 1.213169 | -1.03727 | 0.436328 | 1.228733 | 0.436328 |
|  |  | -1.20164 | -1.20164 | -1.74614 | -2.49006 | -0.7477 | 1.928733 | 1.928733 | 1.928733 | 1.213169 | -1.33085 |
|  |  | 0.436328 | 1.667685 | 0.731935 | 1.075882 | 0.436328 | 1.075882 | -1.44098 | -2.4944 | -1.44098 | 1.067685 |
|  |  | -1.74614 | 1.075882 | 0.731935 | -1.44098 | -2.4944 | 1.567698 | -2.49806 | 1,342703 | 1.075882 | 1,213169 |
|  |  | 0.096352 | -1.03727 | -1.20184 | -1.33088 | -0.7477 | -1.33088 | -1.47389 | -1.20164 | -1.74814 | 1.213169 |
|  |  | -2.49806 | -1.47369 | -0.79181 | $1.56 / 606$ | -2.5753 | -2.4944 | -2.4944 | -1.47389 | $1.928 / 33$ | 1.928733 |
|  |  | -0.79181 | 1.928733 | -2.5753 | 1.075882 | 1.928733 | -1.44098 | 1.342703 | -1.47389 | 0.096352 | -1.44098 |
|  |  | 1.213169 | -2.4944 | -1.74614 | -1.03727 | -2.4944 | -1.44098 | -1.20164 | -0.79181 | -1.74614 | -1.03727 |
|  |  | 1.075882 | 0.096352 | -2.5753 | 1.213169 | 1.075882 | -1.44098 | -1.20184 | 1.828733 | -1.44098 | 0.731935 |
|  |  | -1.20164 | 1.342703 | 1.928733 | -1.03727 | -1.47389 | 1.567606 | -1.44098 | 1.075882 | -2.5753 | -1.03/27 |
|  |  | 1.213169 | 1.667686 | 0.436328 | 1.075882 | -2.49806 | 1.567696 | 1.928733 | -1.33088 | 1.928733 | -1.74614 |
|  |  | 0.26249 | -0.00842 | -0.68385 | -0.47997 | -1.06317 | -0.17057 | -0.28834 | 0.51716 | 0.38975 |  |
|  | marianoe | 1.975324 | 2.041565 | 1.921612 | 2.654063 | 1.745423 | 2.404896 | 2.170458 | 2.131301 | -0.369675 | $\begin{array}{r}-0.35983 \\ \hline 2.269213\end{array}$ |
|  |  |  |  |  |  |  |  |  |  | 2.875076 |  |
|  |  |  |  |  |  |  |  |  |  |  |  |
| Mean of 100 Bootstrap Sample Means: | -0.40621 |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |
| Mean Vaniance of 100 Bootstrap samples: | 2.018009 |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |

## APPENDIX 9

## CRUSH COEFFICIENTS FOR 1998 FORD CONTOUR

| REF NO . | YR | MAKE | MODEL | BODY | TRAN | VN | WB | WT | V.EFF | PDOF | \% O . | \#C's | X_c | bo | b1 | Kv | A | B | TESTH |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Contou06 | 98 | FORD | Contour | 45 | AF | 3FAFP6533Wh118227 | 1065 | 3310 | 350 | 0 | 100\% | 6 | 14.0 | 4.2 | $\begin{array}{\|c\|c\|c\|} \hline 220 & 240 & 354 \\ \hline \text { Defaut Value For } 30^{\circ} \\ \hline \end{array}$ |  |  | 186 A2708 |  |
|  |  |  |  |  |  |  | Welot | 2859 |  |  |  |  |  | 450 |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

[^1]
## APPENDIX 10

## REVIEWERS' COMMENTS

SAE PAPER 2004-01-1208

## REVIEW \#1

I believe the topic of this paper is worthwhile and would make a good SAE paper if modified. Basically the authors need to add a lot of detail concerning the methodologies and equipment used in the study. A lot of new text and new sections have been added to remedy this.

The tables and figures need to be titled, labeled and referenced in the body of the text. The NHTSA numbers need to be added to the two main tables to reference the tests used. Done. The test number for the Ford Contour (the "within" subjects subject) was included also.

A detailed description of the Photomodeler program needs to be included. It should describe how to obtain the software, the principles of its operation, how to use it, define key terms and define precisely the equipment it was used with. The new sections entitled "Description of the Software" and "Description of a Generic PhotoModeler Procedure" have been added.

For instance, how was the Olympus C-5050 calibrated? Why was it chosen for use? More detail has been added to the "Camera Calibration" section. Why is "overlap" necessary? The "Exemplar Modeling" section has been expanded to explain this. What measurements were made to scale the photos? Why were those particular measurements used? This also was clarified in the "Exemplar Modeling" section. How was the dxf file exported? This is answered in the very last sentence of "Exemplar Modeling."Were the photos digitized and saved in photomodeler? How was this done? This is explained better in the last part of paragraph 1 of "Exemplar Modeling" and in "Crushed Vehicle Modeling."What is a screenshot? This is explained in the middle of the "Camera Calibration" paragraph. What is EBS? Why was the research based on Cooper's work? How do you know Cooper's work is correct? Need a short discussion of Cooper's work and discussion of the tables in Appendix 2. The "EBS Determination" section has been revamped. What is bootstrapping? How do you do it? Discuss the two main tables, explain the data. Substantial additions have been made to the bootstrapping section. Why was a study of "between subjects" vehicles undertaken? This is answered in paragraph 4 in the "Introduction."

How are these results applicable to accident reconstruction? This paper could be very helpful if fleshed out. It's obvious the authors know their subject matter, it just needs to be presented so others can understand and use it. Remember the scientific method; the results need to be repeatable by others.

## REVIEW \#2

Crush coefficients (presumably 'A' and 'B' can be easily calculated using the elemental physics inherent in the Crash3 equations used to calculate EBS. If one is not an engineer, one could purchase these from a source such as Neptune but why anybody with even a remote scientific education would do so is beyond me. The authors should
clearly state how they determined 'A' and 'B'. I sincerely hope they calculated them based on the actual crash test data (measured crush, measured speed, measured weight, etc.). I would hope that authors of an SAE paper do not purchase them from someone who uses unknown methods to calculate them (remember that Neptune does that idiotic 'airgap' adjustment and therefore has highly suspect 'A' and 'B' values). A whole new section has been devoted to this-it is entitled "Crush Coefficient Determination."

This paper is actually two studies. First of all, Photomodeler determined measurements so this is actually a study of how well Photomodeler can model measurements made on crash tested vehicles. A statistical study should have been done on how well these crush measurements were determined. The second part of the study is really a sensitivity study on using those measurements from photomodeler and a Crash3 model, how well can EBS be determined based on these errors in crush measurements. These two aspects of the paper should have been much more clearly presented. I would like to see a percent error in crush measurements using Photomodeler before showing EBS conclusions. This is an excellent suggestion, however; it is not feasible due to the intrinsic features of PhotoModeler. There is a way this could work, but it would require that $I$ work closely with the folks at Veridian, TRC, and Karco Engineering---there's no way I could do this before the paper deadline. Let me explain. Look at the following figure. Veridian clearly took this picture after the crash test-you can see c1 thru c6 very clearly indicated with little crosses. We know exactly where the CMM measured.


Now look at the next picture from Karco:


Where exactly are cl-c6? Your guess is as good as mine. I would imagine that it's somewhere in the vicinity of the bumper area. With PhotoModeler, I didn't always measure the bumper (unless it had a distinct feature on it.) Hence, my measurements would most likely be totally different than theirs; but I think they are suitable, because a resultant speed around 35 mph is almost always achieved. Bumpers are rounded and smooth; PhotoModeler needs distinct points for modeling. A curve is not acceptable for measurement extraction. I typically used the badging, edges of the hood, parts of the headlight, and other clear features that are easily seen on the crushed vehicle as well as the exemplar. What you are suggesting would require three things: 1. Prior to testing, the test vehicle would have to be marked with cl-c6 across the bumper. 2. Photos of the exemplar test vehicle (with the "c" marks clearly visible in a lot of the photos) would need to be taken. 3. Photos of the crushed test vehicle need to be taken, again with the "c" marks easily seen. If Veridian (or Karco) and I could agree where we would both measure, your proposition would work. It would be a dandy at that. But this study took a somewhat different direction, and got reasonable results. If I had the time and resources, $I$ certainly would like to do it your way---it is a more comprehensive approach, and would make a better paper, but not very feasible at this juncture, considering the deadline is in a couple of days.

Since part 1 of the suggestion is unresolved, part 2 of the suggestion can't be pursued, but is a good idea nonetheless.

In all of the NHTSA tests I have examined, measured impact speed is given to one or two decimal places yet the authors seem to be reporting much more precise values than that. How did they get these very precise values from test reports. I assumed they used the speed trap data reported in the reports which is the only accurate way of doing this. I assume they didn't use integrated accelerometer data over speed trap data. Reporting actual test velocity to 8 decimal places is ridiculous and needs to be removed from any SAE paper. Please clarify this. Done. The values were initially just pasted from the spreadsheet, which explains the excessive digits. You are not the first to say this. It should have been resolved previously.

In conclusions, remove the statement, "Both of these CI's would be acceptable to an accident reconstructionist." This is editorializing. It may be correct. It may be wrong. But there is no analytical basis in this paper to state what would or would not be acceptable to an accident reconstructionist. Done.

Remove all references in the abstract and elsewhere to what is acceptable or not. Report your data as a scientist. Do not editorialize about what is acceptable or not in accident reconstruction. You may do that in a courtroom if you want but not in a scientific paper. You are not the judgeof what is acceptable or not. Done.

Remove the entire last paragraph. The results speak or themselves. The authors are not the judge by which accident reconstruction tools are divined to be acceptable or not. The authors did a study and presented the results.It may be acceptable. It may not. There is no analytical basis with which to say Photomodeler is or is not "an appropriate crush measurement tool." Done.

Describe the bootstrapping method a bit more fully. It is not in wide use in accident reconstruction. Substantial additions have been made
to the bootstrapping section.
Overall, evaluate your significant figures (decimal places) used in the paper. It seems to be an exercise by someone who has lots of digits on their calculator but doesn't know when to cut them off. Done.

Not a bad paper but these changes will make it acceptable for publication.

## REVIEW \#3

I recommend the paper be accepted if modified.
The paper is well done however, I believe the data used in the paper (study-analysis) is not a true indicator of "real world data." The damage measurements of crush both in "c"
measurements and total damage width and vehicle weight is not representative of real world data due to the level of precision that was used. I would suggest that values of crush and weight be taken to the tenth or whole number. Taking this data to the hundred or thousand is unrealistic and any outcomes derived from this type of data is not indicative of the real world, making this papers' analysis and findings not as valuable as they can be for study.

The vehicle's weight "precision" is due to a conversion from kilograms (from the NHTSA test report) to lbs. (see Figure 4.) This was done in a spreadsheet, and I just left the extra digits where they were. This wasn't an attempt to be overly super-accurate; I just intended to round off the numbers in the end of the analysis. Now on the "c" measurements and the width of crush measurements, those numbers were directly copied from PhotoModeler-no joke. Let me illustrate with a screenshot:

Note that for the Dodge Ram that the width of crush is 75.441 inches, which is indicated with a red circle. This is what PhotoModeler gives me, and that's what I used in the analysis. The computations themselves for this vehicle are shown in Appendix B, second page, second row. I can't illustrate for all of the " $c$ " measurements, but they are the same way also.

You are not the first to bring this subject up. I did allow the numbers to get to a ridiculous amount of precision in the spreadsheet, but I did, in this revision, modify the EBS's to a more agreeable accuracy.


## APPENDIX 11

## SCREENSHOTS FOR PART TWO

Case 1


Case 2


## Case 3



## Case 4

臬 PhotoModeler Pro: project4.pmr


## Case 5



Case 6


Case 7


Case 8


Case 9


Case 10


Case 11

## Missing Due To Hard Disk Crash

Case 12


Case 13


Case 14


Case 15


Case 16


Case 17


Case 18


## Case 19

## Missing Due To Hard Disk Crash

Case 20


Case 21


Case 22


Case 23


Case 24


Case 25


Case 26


Case 27


Case 28


Case 29

# Missing Due To Hard Disk Crash 

Case 30


## APPENDIX 12

## REVIEWERS' COMMENTS <br> PART TWO

```
Your SAE Paper is not approved for publication this year. Please see
comments below. If after reviewing these comments, signifiant changes
are made, we would invite you to resubmit for next year (2006). Thank
you for the submission.
Michael Varat
co organizer
Reviewer:
Professional Experience Well Qualified
Previously Published Yes
Status Disapproved
5 Quality
3 Reference
4 ~ I n n o v a t i v e
7ntegrity
6 Presentation
5 Conclusions
Comments:
The accuracy of photogrammetry has been well established in the literature already and the accuracy of PhotoModler has similarly been established. As the authors point out the CSF analysis has similarly been well published. This current work does nothing to further the knowledge or understanding of these 2 separate topics.
Reviewer:
Professional Experience Well Qualified
Previously Published No
Status Disapproved
```

```
6 Quality
```

6 Quality
3 Reference
3 Reference
3 Innovative
3 Innovative
8 Integrity
8 Integrity
5 Presentation
5 Presentation
8 Conclusions

```
8 Conclusions
```

Comments:

This paper reports on the application of the PhotoModeler program to the measurements of road curvature. The authors report on this facet being an import portion of accident reconstruction, insofar as the application of the critical speed formula is concerned. As these authors are aware the PhotoModeler application has been validated in a number of publications for photographic measurement value. This paper appears to be consistent with the general research that the PhotoModeler software is useful for many different applications within Accident Reconstruction. In reviewing the research it was unclear to this reviewer it's direct application to the field. In many new applications of different software packages in the field, it is useful
and required that actual field application be performed to demonstrate it's usefulness. It seems that this methodology demonstrates its
usefulness on a flat curved roadway (such as an airport), and at least to this reviewer it is unclear how reliable it would be on a curved hilly roadway with a superelevation. Obviously the latter represents a more realistic need for critical speed calculations.

Reviewer:
Professional Experience Moderately Qualified
Previously Published No
Status Disapproved

```
Quality
Reference
Innovative
Integrity
Presentation
Conclusions
```

Comments:

The authors should be commended for conducting a well organized set of tests and describing the results clearly. That said, the study does not significantly expand on prior photogrammetry studies and the usefulness of the method is not established in the paper. Due to the limited scope and reference value of the study I cannot approve the paper for publication as it is. The following specific issues would need to be addresses:

The goal of the study, "to show that the measurement of $l$ and $h$ can be accomplished with photogrammetry", does not expand on prior studies (SAE 930662, 940925 and many others). Photogrammetry has been studied for some time by accident investigators and its ability to produce measurements with an acceptable level of accuracy has been established. A more ambitous, focused study is required to provide a contribution to the research. For example: a comparison of the accuracy of curve radii based on $l$ and $h$ from the photogrammetry method and the traditional tape measure method.

The usefullness of the specific method studied in the paper is not established. Since it relies on numerous photographs taken by a calibrated camera and a known measurement in the scene, improvements over the traditional tape measure or survey equipment methods for measuring chord and mid-ordinate are unclear.

The limitations of the method are not clearly explained. The study tested the best case scenario; a flat scene, known camera and a large number of photographs. The authors need to discuss the consequences of an unknown camera, only a few photographs, and a 3d scene - a common reconstruction scenario.

The method described in the paper requires a known dimension in the scene and the accuracy of the results are directly related to this dimension. The authors need to expand on how their scaling measurement was made, its accuracy, and how its accuracy effects the accuracy of their results.

In summary, this paper does not describe significant or useful results. It does however; summarize well-conducted tests that could be a first step towards a useful contribution for the application of photogrammetry in accident investigation.

## APPENDIX 13

CAMERA CALIBRATION OF OLYMPUS C-5050 LOW RESOLUTION

## Overview

As stated in Appendix 1, camera calibration involves the projection of a special grid pattern (the slide is provided by PhotoModeler with the software CD) onto a flat wall, and in this case, was done with a slide projector. The photos are taken of eight (8) different positions: upper, middle, lower, and middle vertical on both the left and the right sides. Next is the transfer of the digital photos to the computer. Points are marked and calibration begins by selecting "Calibrate" under the Calibration menu. After successful processing, the camera can be used as a measurement device with PhotoModeler.

## Prepare for Picture Day

The process for calibrating a camera at high resolution is the exact same procedure for calibrating at low resolution. Interested readers can consult Appendix 1 for the fine details. A short, abbreviated documentation of the calibration will be shown here. Table 1 shows the Squareness Verification Data for low resolution.

## Squareness Verification Data

| $A=62.1875$ | $C=41.125$ inches |
| :--- | :--- |
| $B=61.25$ | $D=40.875$ inches |
| $\|A-B\|<A / 40$ | $\|C-D\|<C / 40$ |
| $\|.9375\|<62.1875 / 40$ | $\|.25\|<45.625 / 40$ |
| $\|.9375\|<1.555$ <br> $\imath$ | $\|.25\|<1.028$ |
| Scaling distance between control points $1 \& 4: 42.25$ inches |  |

## Table 1. Squareness Verification Data

The following photos Figures 1-8 were the photos used in the low resolution calibration.


Figure 1. Upper Left Calibration Photo


Figure 2. Middle Left Calibration Photo


Figure 3. Lower Left Calibration Photo


Figure 4. Middle Vertical Left Calibration Photo


Figure 5. Upper Right Calibration Photo


Figure 6. Middle Left Calibration Photo


Figure 7. Lower Left Calibration Photo


Figure 8. Left Middle Vertical Calibration Photo

After the user marks control points (using the special control point buttons at the top) and the Camera Calibrator's marking of the all visible triangle intersections, processing will follow. Figure 9 shows the error dialog which happens after successful processing. Figure 10 shows the camera parameters for the low resolution calibration of the Olympus C-5050


Figure 9. Error Dialog for Low Resolution Calibration Project


Figure 10. Solved Camera Information Low Resolution

## APPENDIX 14

## PICTURES FROM BENCHMARK MEASUREMENT DAY


$254$






## APPENDIX 15

## SELECTED PHOTOS FROM TAPE MEASUREMENT EXPERIMENT



## Low Tape-4 pieces



High Tape-8 pieces


Beginning measurement


Ending measurement

## APPENDIX 16

JMP PRINTOUTS WITH HANDWRITTEN NOTES



I would hate to make any sort of predictions based on this model ( $R^{2}=19 \%$ )


## VITA

Lara Lynn O'Shields was born on February 14, 1972 in Sevierville, TN. She is the daughter of David O'Shields and Alesia O'Shields (father and stepmother) and Susan and Wayne Gourley (mother and stepfather) and has a half-brother Seth O'Shields and two stepbrothers, Todd and Seth Gourley, and a stepsister Samantha Gourley Angelopolous. She received a Bachelor of Science in Industrial Engineering in December 1995 and a Master of Science in Industrial Engineering in August 2000. Her Doctor of Philosophy in Industrial Engineering was awarded in August 2007.

For the past 4 years, Lara has enjoyed being a member of the Walters State Sevier Jazz Band playing baritone saxophone. Additionally, she plays piano and sings at Millican Grove Baptist Church in Sevierville. Flying locally and cross-country in her dad's airplane is also a fun pastime of Lara. Lara especially enjoys riding motorcycles, whenever a friend will loan her one to ride. For the past 10 years, Lara has taken pleasure in growing orchids, especially the genus Phalaenopsis. Photography with medium format folder cameras from the post-WWII era is another one of her passions.

Lara currently resides in Sevierville with her pets: cat Pete, bird Cookie, and dog Bart and four angelfish.



Bart at airport helping out with Part III


Pete taking it easy


Photo of Bart taken with a 1951 Voigtlander Perkeo I


[^0]:    
    

[^1]:    Liability Disclaimer
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