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DISCRETE PARTICLE SWARM OPTIMIZATION FOR THE ORIENTEERING PROBLEM

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Discrete particle swarm optimization (DPSO) is gaining popularity in the area of combinatorial optimization in the recent past due to its simplicity in coding and consistency in performance. A DPSO algorithm has been developed for orienteering problem (OP) which has been shown to have many practical applications. It uses reduced variable neighborhood search as a local search tool. The DPSO algorithm was compared with ten heuristic models from the literature using benchmark problems. The results show that the DPSO algorithm is a robust algorithm that can optimally solve the well known OP test problems.

Keywords: Discrete particle swarm optimization, reduced variable neighborhood search, orienteering problem.

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1. INTRODUCTION

Particle Swarm Optimization (PSO) is an evolutionary optimization algorithm that is inspired by nature. PSO has been widely used to optimize several continuous nonlinear functions as well as combinatorial problems. Many researchers are using PSO as a tool for solving combinatorial problems due to its simplicity in structure, ease of implementation and performance robustness (Pan et al., 2008). Orienteering Problem (OP), which is also called the generalized traveling salesman problem, is a combinatorial optimization problem. OP has been proved to be a NP-hard problem (Golden et al., 1987). A limited number of exact methods have been developed to solve smaller problem instances of the OP. Many heuristic approaches have been implemented for larger sized OPs. Various adaptive optimization heuristics such as tabu search, genetic algorithm, and ant colony optimization algorithms (discussed in section 2) have been developed for the OP. In this paper a DPSO algorithm has been designed for OP. The performance of the DPSO heuristic was measured against other metaheuristic algorithms from the literature using benchmark problems.

1.1 Particle Swarm Optimization

Particle swarm optimization, inspired by the social behavior of bird flocking and fish schooling, is a population based metaheuristic introduced by Kennedy and Eberhart (1995). In PSO, each particle represents a solution and the swarm of particles flies through the search space in an effort to reach the global optimum. All members (particles) of the population are maintained throughout the search procedure and their information is socially shared among the individuals to direct the search toward the best position in the search space. The particles fly through the multi-dimensional problem space with specific velocities and follow the current best known particles. During flight each particle adjusts its position according to its own experience and the experience of the neighboring particles. The neighborhood could encompass either a local neighborhood or the global neighborhood which forms the two variation of the fundamental PSO algorithm. The particle's best solution is called the p_{ibest}, global best is called the g_{best} and the restricted neighborhood's best particle is named the l_{best} (Kennedy and Eberhart, 2001). In each iteration the particle flies to the next position with a certain velocity using the p_{ibest} and g_{best} values as shown in equations 1 and 2 (Shi and Eberhart, 1999). Replace g_{best} with l_{best} for the restricted neighborhood version of the PSO. PSO combines local search methods with global search techniques thus balancing between exploitation and exploration.

$$v_i^{k+1} = w.v_i^k + c_1 r_1 \left(p_{ibest} - x_i^k \right) + c_2 r_2 \left(g_{best} - x_i^k \right) \quad \ldots \quad (1)$$

$$x_i^{k+1} = x_i^k + v_i^{k+1} \quad \ldots \quad (2)$$

where

x_i^k is the position of the ith particle at iteration k, v_i^k is the velocity of the ith particle at iteration k, w is the inertia parameter, c_1 is the cognitive parameter, c_2 is the social parameter, r_1 and r_2 are random numbers.

1.2 Discrete Particle Swarm Optimization

Discrete PSO (DPSO) is a modified version of PSO which applies discrete or qualitative distinction between variables. Kennedy and Eberhart (1997) developed the first DPSO with binary valued particles. Since then several versions of DPSO have been developed. DPSO will facilitate solving the combinatorial optimization problems due to its ease of

implementation, simple structure and its robustness (Pan et al., 2008; Tasgetiren, 2007). DPSO algorithms that have been implemented so far can be broadly classified in to five categories namely (i) binary valued DPSO (Kennedy and Eberhart, 1997; Liao et al., 2007; Pan et al., 2008), (ii) DPSO with dummy variable to transition from combinatorial to discrete state and vice-versa (Jarboui et al., 2007; Jarboui et al., 2008a; Jarboui et al., 2008b), (iii) DPSO with crossover and mutation techniques (Lian et al., 2006; Lian et al., 2008; Pan et al., 2008), (iv) modified continuous PSO with smallest position value rule (Chen et al., 2006; Tasgetiren et al., 2007) and, (v) the miscellaneous DPSO models which includes the other versions of DPSO algorithm seen in the literature such as quantum particle version DPSO (Pang et al., 2004), fuzzy DPSO (Anghinolfi and Paolucci, 2009), DPSO with pseudo-insertion and extract-reinsert operators (Hu et al., 2004) to name a few.

1.3 Industry Applications of PSO Algorithm

Since 2002, research applying PSO has grown rapidly. The number of papers using PSO as an optimization tool has totaled over 300 until 2004 (Venter and Sobieski, 2002) and is growing exponentially ever since. Popularity of PSO is due to its several strengths namely (i) very few parameters to adjust, (ii) simple structure, (iii) ease of implementation, (iv) robustness, and (v) convergence speed. Some of the PSO applications include communication satellite design (Abido, 2002), power and voltage control problem (Fukuyama et al., 1999; Yeh, 2003), supplier selection and ordering problem (Van den Bergh and Engelbecht 2000), neural network training (Brandstatter and Baumgartner, 2002), mass spring system (Allahverdi and Al-Anzi, 2006), Golinski speed reducer problem, and Rosenbrock function problem (Abido, 2002). Combinatorial optimization problems that have been solved using DPSO include vehicle routing problem (Pang et al., 2004), traveling salesman problem (Venter and Sobieski, 2002), scheduling problem (Anghinolfi and Paolucci, 2009; Jarboui et al., 2008a; Jarboui et al., 2008b; Lian et al., 2006; Lian et al., 2008; Pan et al., 2008; Tasgetiren et al., 2007; Tseng and Liao, 2008; Jin et al., 2007), clustering problem (Jarboui et al., 2007), transmission network expansion problem (Jin et al., 2007), and orienteering problem (Dallard et al., 2006; Dallard et al., 2007; Sevkli et al., 2007).

This paper has been structured into the following sections: section 2 describes the problem under study (OP); section 3 gives a detailed description of the DPSO algorithm; section 4 expands upon the parameter value selection process; section 5 discusses the results of the DPSO algorithm performance and section 6 provides the concluding remarks along with the future extension recommendations.

2. PROBLEM DESCRIPTION

The orienteering problem initiated from the sport of orienteering which involves cross-country running and navigation through a forest using a map and compass. There are several control points or nodes to be visited and each node has a score tied to it. Lower scores are usually allocated to nodes near the start and finish areas and larger scores to those further away. The difficulty of reach and the distance of the node with respect of other nodes are also taken into consideration while allocating scores to control points. The competitors start and end their tour at specified control points (which do not have any scores). The term OP which was introduced by Tsiligirides (1984) is the *score orienteering event* version of the sport in which the competitors do not have to visit all the nodes. The objective is to maximize the score within a certain prescribed time limit. Competitors who arrive at the terminal point after the prescribed time limit are disqualified.

2.1 Industry Applications of Orienteering Problem

Literature reveals several applications of OP including routing oil tankers to service ships (Golden et al., 1987), customer vehicle assignment problem (Golden et al., 1981; Golden et al., 1984), inventory routing problem (Golden et al., 1981; Golden et al., 1984), production scheduling (Balas, 1989), bank/postal delivery and industrial refuse collection problems (Kantor and Rosenwein, 1992), and single ring design problem while constructing telecommunication networks (Thomadsen and Stidsen, 2003). Recent applications of OP include mobile tourist guide application (Souffriau et al., 2008; Wang et al., 2008) to help tourists pick the most valuable attractions to visit within the given time span of their visit, and a military application (Wang et al., 2008) to aid surveillance aircrafts to choose a subset of places to photograph within the given amount of time or fuel constraint.

Since OP is a NP hard problem a few exact methods using branch and bound (Ramesh et al., 1992; Ramesh et al., 1992b), branch and cut (Fischetti et al., 1998), Lagrangean relaxation (Balas, 1989), and minimum directed 1-subtree relaxation (Kataoka et al., 1998) have been developed in the past. Several heuristic approaches have been developed in the last two decades. Golden et al. (1987) implemented a heuristic with center of gravity technique. Golden et al. (1988) improved the center of gravity technique with learning capabilities. Keller (1989) altered his algorithm using Multi-Objective Vending Problem (MVP) to solve the OP. Ramesh and Brown (1992) created a four phase heuristic to solve the OP. Chao et al. (1996) developed a 'fast and effective heuristic' for OP. Many metaheuristic algorithms such as Genetic Algorithm (GA) (Tasgetiren, 2002), Ant Colony Optimization (ACO) (Ke et al., 2008; Liang et al., 2002; Liang and Smith, 2006), Tabu Search (TS) (Kulturel-Konak et al., 2004; Liang et al., 2002), and PSO (Dallard et al., 2006; Dallard et al., 2007; Sevki et al., 2007) have also been implemented to solve the OP. In this paper a novel DPSO algorithm has been introduced which calculates the new position of the particle using p_{ibest}, g_{best} and the current position of the particle using a discrete representation as discussed in the following section.

3. DPSO ALGORITHM

In the DPSO algorithm of OP each particle constitutes a tour encompassing the list of nodes visited such that T_{max}, the distance constraint was obeyed. The starting and the ending nodes are distinct and specified. In order to ensure a good starting solution in the population, the first particle was built using the *s/d* (score/distance) ratio. Starting from the first node, the feasible node with the highest *s/d* value was chosen as the next city to be visited. Guided by the *s/d* values a feasible tour was constructed for the first particle. The initial solutions for the remaining particles were constructed randomly.

The new position (new tour) for each particle was calculated as follows: For each node in the current particle a random number Λ is generated. If $\Lambda < w$, the node is accepted as a part of a temporary array, Ω. In a similar fashion nodes were included in the temporary array from the p_{ibest} particle if $\Lambda < c_1$, and the g_{best} particle if $\Lambda < c_2$. Duplicate nodes were removed from Ω. If the temporary array was feasible it was accepted as the new position of the particle otherwise nodes were randomly deleted till a feasible solution was reached. In order to improve the efficacy of the algorithm so as to prevent it from being caught in local optima a Reduced Variable Neighborhood Search (RVNS) was used as a local search tool (Sevkli and Sevilgen, 2006). In RVNS the solution space is searched by switching neighborhoods. The two neighborhoods used in the algorithm include *insert* and *exchange*. In the insert neighborhood a new node is inserted in the existing tour while in the exchange neighborhood a new node is exchanged for an existing node in the tour. After the completion of the RVNS procedure a 2-opt operation is performed to optimize the tour. If the tour length has been reduced by the 2-opt method, a node insert procedure is conducted in an attempt to increase the fitness value (total score) of the tour. The flowchart for the DPSO algorithm is given in Figure 1 and the pseudo code for RVNS is shown in Figure 2 (Sevkli et al., 2007).

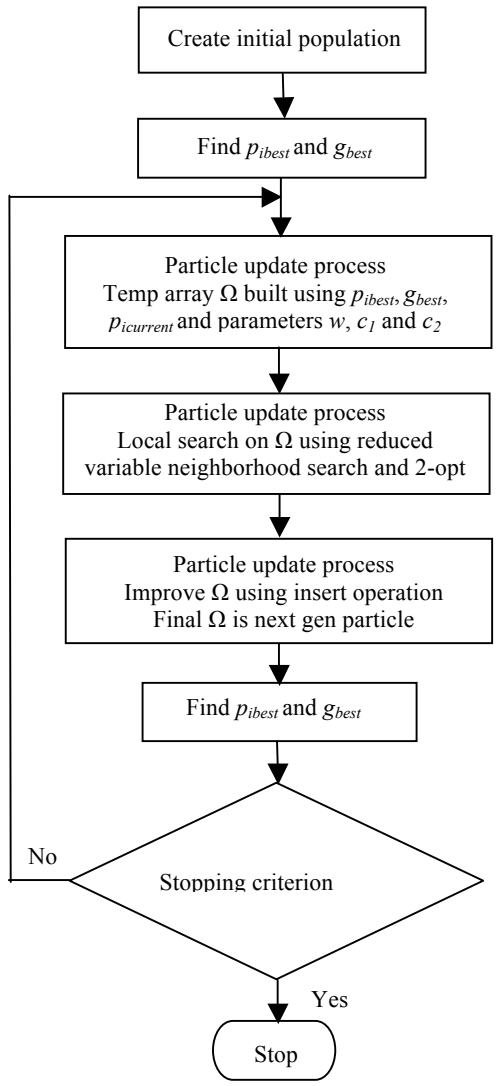

Figure 1. DPSO algorithm flowchart

```
Initial solution, S_init
New solution, S_new
Initial solution tour length, S_init_len
New solution tour length, S_new_len
while stopping criterion not satisfied
neighborhood ←1
if neighborhood =1
S_new ←Insert (S_init)
end if
if neighborhood =2
S_new ← Exchange (S_init)
end if
if Fitness(S_new) > Fitness(S_init) | S_new_len < S_init_len
S_init ← S_new
S_init_len ← S_new_len
neighborhood ←1
else
neighborhood ←2
end if
end while
```

Figure 2. RVNS pseudo code

In order to better comprehend the DPSO algorithm the construction of the temporary array Ω is illustrated in Figure 3(a). Based on $\Lambda(x_i^n)$, $\Lambda(x_p^n)$ and $\Lambda(x_g^n)$ values assume Ω to be Figure 3(b). Remove duplicates to get the updated value of Ω as shown in Figure 3(c). Using the updated Ω the next position of the particle is constructed as shown in the flowchart (Figure 1).

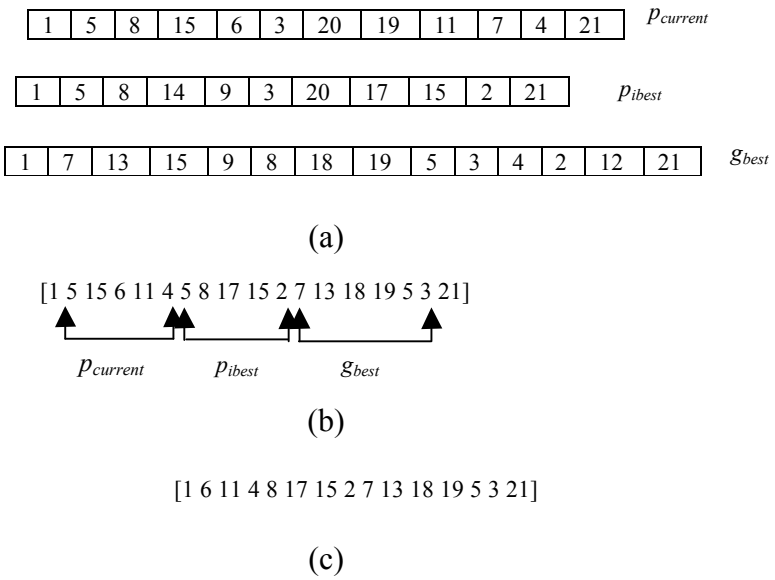

Figure 3. DPSO particle (a) DPSO particle configuration (b) Temporary array Ω (c) Updated Ω

4. PARAMETER VALUE SELECTION

For the DPSO algorithm of OP, six parameters including the population size, number of generations, w, c_1, c_2, and the stopping criterion were chosen using Design of Experiments (DOE). The stopping criterion was the number of generations for which the best solution found remains unchanged. Based on preliminary experimentation two levels were chosen for the six factors as shown in Table 1.

Table 1. DOE Parameters and Levels

Factor #	Factors	Level 1	Level 2
1	Number of particles	30	40
2	Number of generations	50	100
3	w	0.4	0.8
4	c1	0.4	0.8
5	c2	0.9	1
6	stopping criterion	25	40

The experimentation was carried out using a 2^6 full factorial design. Each factor level combination was tested for 10 replications. The response variables used were the Relative Percentage Error (RPE) and the Average Relative Percentage Error (ARPE). RPE is defined as the error between the best known solution and the best solution of all ten replications. It shows if the algorithm can find the best known solution.

$$RPE = \frac{best\ known\ \ score - best\ score}{best\ known\ \ score} * 100 \quad \ldots \quad (3)$$

ARPE is defined as the average error of all replications. It shows the robustness of the algorithm.

$$ARPE = \frac{\sum_{i=1}^{10}\left(\frac{best\ known\ score - i^{th} replication\ score}{best\ known\ score} * 100\right)}{10} \quad \ldots \quad (4)$$

Figure 4 shows the main effects plots of the Analysis of Variance (ANOVA) results.

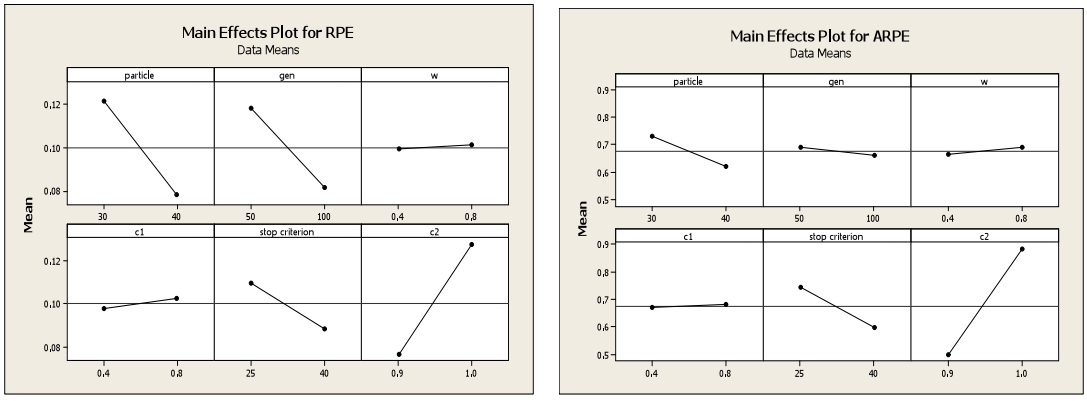

Figure 4. ANOVA main effects plots (a) For response variable RPE (b) For response variable ARPE

Figure 4(a) shows that the parameters, number of particles, number of generations, c_2, and the stopping criterion significantly affect the response variable RPE. Similarly Figure 4(b) shows that the parameters, number of particle, c_2, and the stopping criterion influence the ARPE more than the other parameters. The parameter values of the DPSO (see Table 2) were chosen such that the overall RPE and ARPE were minimized.

Table 2. DPSO Parameters and their Values

Factor #	Factors	Value
1	Number of particles	40
2	Number of generations	100
3	w	0.4
4	c1	0.4
5	c2	0.9
6	stopping criterion	40

5. RESULTS AND DISCUSSION

The performance of the DPSO algorithm was validated using four benchmark problem sets from the literature totaling to 67 problems. Tsiligirides (1984) developed the three problem sets namely, dataset 1 with 32 nodes (18 problems), dataset 2 with 21 nodes (11 problems), and dataset 3 with 33 nodes (20 problems). Chao et al. (1996) corrected an error in Tsiligirides's dataset 1 and named it dataset 4 (32 nodes with 18 problems). The size of the entire search space (including feasible solutions, and infeasible solutions that violate the T_{max} constraint) for these problems were 3.3 x 10^{17} (21 node problem), 7.2 x 10^{32} (32 node problem), and 2.2 x 10^{34} (33 node problem). The results of the DPSO algorithm were compared with ten different heuristic models from the literature. Table 3 summarizes the acronym abbreviations of various heuristic models that were used for comparison. The experiments were conducted on a windows XP environment on an Intel CPU T2400@1.83 GHz processor using 1 GB RAM. The code was implemented using MATLAB 7.1.0.

Table 3. Acronym Abbreviations for the Model Names

Acronym abbreviations	
Tmax	Maximum tour length allowed
UB	Upper bound on score (Leifer and Rosenwein, 1994)
TS	Tsiligirides's heuristic (Tsiligirides, 1984)
TC	Tsiligirides's heuristic implemented by Chao et al. (Chao et al., 1996)
MVP	Keller's MVP heuristic (Keller, 1989)
GLV	Golden et al.'s heuristic (Golden et al., 1987)
GWL	Golden et al.'s heuristic (Golden et al., 1988)
ANN	Wang et al.'s artificial neural network model (Wang et al., 1995)
CGW	Chao et al.'s heurisitc (Chao et al., 1996)
GA	Tasgetiren's genetic algorithm (Tasgetiren, 2002)
ACO	Liang and Smith's ant colony optimization model (Liang and Smith, 2006)
Tabu	Kulturel-Konak et al.'s tabu model (Kulturel-Konak et al., 2004)
PSO	Sevkli et al.'s PSO algorithm (Sevkli et al., 2007)
DPSO	New DPSO algorithm proposed

Tables 4, 5, 6 and 7 provide the comparison of the best solution of 10 replications obtained by the DPSO algorithm against the best solution of various heuristic models for problem sets 1 through 4. A '+' symbol denotes that the DPSO algorithm found a superior solution than the heuristic model in comparison and vice-versa for the '-' sign. The results in the tables show that the DPSO algorithm is competitive. It was able to reach the best known solutions for all of the 67 problem instances.

Table 4 . Comparison of DPSO Algorithm with the Other Heuristic Models for Problem Set 1

		Compared with heuristics from literature										DPSO vs. other heuristics								
Tmax	UB	TC	MVP	GLV	GWL	ANN	CGW	GA	ACO	Tabu	DPSO	TC	MVP	GLV	GWL	ANN	CGW	GA	ACO	Tabu
5	10	10	10	10	10	10	10	10	10	10	10									
10	20	15	15	15	15	15	15	15	15	15	15									
15	45	45	45	45	45	45	45	45	45	45	45									
20	70	65	65	65	65	65	65	65	65	65	65									
25	95	90	90	90	90	90	90	90	90	90	90									
30	120	110	110	110	110	110	110	110	110	110	110									
35	140	135	130	125	135	135	135	135	135	135	135		+	+						
40	160	150	155	140	155	155	155	155	155	155	155	+		+						
46	180	170	175	165	175	175	175	175	175	175	175	+		+						
50	195	185	185	180	190	190	190	190	190	190	190	+	+	+						
55	210	195	200	200	205	205	205	205	205	205	205	+	+	+						
60	230	220	225	205	225	225	225	225	225	225	225	+		+						
65	245	235	240	220	240	240	240	240	240	240	240	+		+						
70	260	255	260	240	260	260	260	260	260	260	260	+		+						
73	270	260	265	255	265	265	265	265	265	265	265	+		+						
75	270	265	270	260	270	270	270	270	270	270	270	+		+						
80	285	270	280	275	280	280	280	280	280	280	280	+		+						
85	285	280	285	285	285	285	285	285	285	285	285	+								
Summary of DPSO model vs. other heursitics											+	11	3	11	0	0	0	0	0	0
											-	0	0	0	0	0	0	0	0	0

Table 5. Comparison of DPSO Algorithm with the Other Heuristic Models for Problem Set 2

		Compared with heuristics from literature										DPSO vs. other heuristics								
Tmax	UB	TS	MVP	GLV	GWL	ANN	CGW	GA	ACO	Tabu	DPSO	TS	MVP	GLV	GWL	ANN	CGW	GA	ACO	Tabu
15	145	120	120	120	120	120	120	120	120	120	120									
20	200	190	200	200	200	200	200	200	200	200	200	+								
23	215	205	210	210	205	205	210	210	210	210	210	+			+	+				
25	240	230	230	230	230	230	230	230	230	230	230									
27	265	230	230	230	230	230	230	230	230	230	230									
30	275	250	260	260	265	265	265	265	265	265	265	+	+	+						
32	305	275	300	260	300	300	300	300	300	300	300	+		+						
35	350	315	320	300	320	320	320	320	320	320	320	+		+						
38	375	355	360	355	360	360	360	360	360	360	360	+		+						
40	400	395	380	380	395	395	395	395	395	395	395		+	+						
45	450	430	450	450	450	450	450	450	450	450	450	+								
Summary of DPSO model vs. other heursitics											+	7	2	5	1	1	0	0	0	0
											-	0	0	0	0	0	0	0	0	0

Table 6. Comparison of DPSO Algorithm with the Other Heuristic Models for Problem Set 3

		Compared with heuristics from literature										DPSO vs. other heuristics								
Tmax	UB	TS	MVP	GLV	GWL	ANN	CGW	GA	ACO	Tabu	DPSO	TS	MVP	GLV	GWL	ANN	CGW	GA	ACO	Tabu
15	175	100	170	170	170	170	170	170	170	170	170	+								
20	210	140	200	200	200	200	200	200	200	200	200	+								
25	290	190	260	250	260	250	260	260	260	260	260	+		+						
30	340	240	320	320	320	320	320	320	320	320	320	+								
35	395	290	370	380	390	390	390	390	390	390	390	+	+	+						
40	445	330	430	420	430	420	430	430	430	430	430	+		+						
45	490	370	460	450	470	470	470	470	470	470	470	+	+	+						
50	535	410	520	500	520	520	520	520	520	520	520	+		+						
55	575	450	550	520	550	550	550	550	550	550	550	+		+						
60	605	500	570	580	580	580	580	580	580	580	580	+	+							
65	635	530	610	600	610	610	610	610	610	610	610	+		+						
70	665	560	640	640	640	640	640	640	640	640	640	+								
75	695	590	670	650	670	670	670	670	670	670	670	+		+						
80	725	640	700	690	710	700	710	710	710	710	710	+	+	+						
85	750	670	740	720	740	740	740	740	740	740	740	+		+						
90	785	690	760	770	770	770	770	770	770	770	770	+	+							
95	800	720	790	790	790	790	790	790	790	790	790	+								
100	800	760	800	800	800	800	800	800	800	800	800	+								
105	800	770	800	800	800	800	800	800	800	800	800	+								
110	800	790	800	800	800	800	800	800	800	800	800	+								
Summary of DPSO model vs. other heursitics											+	20	5	10	0	3	0	0	0	0
											-	0	0	0	0	0	0	0	0	0

Table 7. Comparison of DPSO Algorithm with the Other Heuristic Models for Problem Set 4

	Compared with heuristics from literature								DPSO vs. other heuristics						
Tmax	TS	TC	ANN	CGW	GA	ACO	Tabu	DPSO	TS	TC	ANN	CGW	GA	ACO	Tabu
5	10	10	10	10	10	10	10	10							
10	15	15	15	15	15	15	15	15							
15	45	45	45	45	45	45	45	45							
20	65	65	65	65	65	65	65	65							
25	90	85	90	90	90	90	90	90		+					
30	110	110	110	110	110	110	110	110							
35	135	135	130	135	135	135	135	135			+				
40	150	150	155	155	155	155	155	155	+	+					
46	175	175	175	175	175	175	175	175							
50	190	185	190	190	190	190	190	190		+					
55	205	200	205	205	205	205	205	205		+					
60	220	220	220	220	225	225	225	225	+	+	+	+			
65	240	240	240	240	240	240	240	240							
70	255	250	260	260	260	260	260	260	+	+					
73	260	265	265	265	265	265	265	265	+						
75	270	265	270	275	270	275	275	275	+	+	+		+		
80	275	270	280	280	280	280	280	280	+	+					
85	280	285	285	285	285	285	285	285	+						
Summary of DPSO model vs. other heursitics								+	7	8	3	1	1	0	0
								-	0	0	0	0	0	0	0

Table 8 summarizes the total number of problems in which the DPSO algorithm outperforms the other heuristic models. A '-' symbol indicates the heuristic is not applicable to that dataset. The DPSO algorithm was at par with the ACO (Liang and Smith, 2006) and TS (Kulturel-Konak et al., 2004) models for all the datasets. It outperformed the GA (Tasgetiren, 2002), Tsiligirides's heuristic implemented by Chao et al. (1996), and the Golden et al.'s heuristic (Golden et al., 1988) in one instance each. In comparison to the other models the DPSO performed far better as shown in Table 8.

Table 8. Summary of Problems in Which DPSO Outperformed Other Heuristics

	Total number of problems in which DPSO outperformed other heuristics			
	Problem set 1	Problem set 2	Problem set 3	Problem set 4
TS	-	7	20	7
TC	11	-	-	8
MVP	3	2	5	-
GLV	11	5	10	-
GWL	0	1	0	-
ANN	0	1	3	3
CGW	0	0	0	1
GA	0	0	0	1
ACO	0	0	0	0
Tabu	0	0	0	0

Sevkli et al.'s PSO model (2007) contains two error metrics RPE and ARPE to measure the robustness of their model. The RPE and the ARPE were calculated for the 67 problems using the DPSO algorithm and compared with Sevkli et al.'s PSO model. Table 9 shows that both the models reach the best known solutions with their RPE values of zero. However, the ARPE of the DPSO algorithm is 0.84% lower than the PSO algorithm indicating that the DPSO algorithm is more robust than the PSO model.

Table 9. DPSO vs. PSO Model Comparison

	PSO	DPSO
RPE	0	0
ARPE	1.05	0.21

On an average the DPSO algorithm took 21.66 seconds to solve an OP instance. The CPU time comparison between different models has not been done since it is a machine and language/tool dependent criterion.

6. CONCLUSIONS

In this paper a DPSO algorithm was presented for the OP. In order to enhance the efficacy of the algorithm RVNS technique was used as a local search tool and 2-opt was performed to further optimize the solution. This algorithm was compared with ten different heuristic models from the literature using the benchmark datasets. The DPSO algorithm was able to find the best known solutions for all the problems and outperformed seven of the heuristics in one or more problem instances. In comparison to the PSO model from the literature the DPSO algorithm's ARPE was 0.84% lower which exhibits the robustness of the DPSO algorithm. As a future extension this DPSO algorithm could be enhanced to represent the team orienteering problem and other routing problems.

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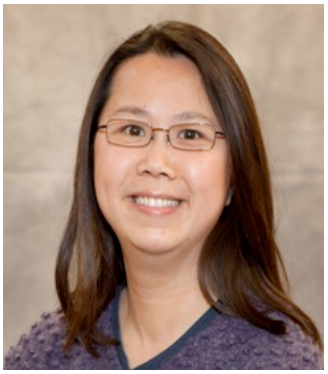

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