

# Automated sliding susceptibility mapping of rock slopes

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**Abstract.** We present a suite of extensions for ARCVIEW GIS<sup>TM</sup> (ESRI) that allows to map the spatial distribution of first-order mechanical slope-properties in hard rock terrain, e.g. for large slope areas like water reservoir slopes. Besides digital elevation data, this expert-system includes regional continuous grid-based data on geological structures that might act as potential sliding or cutoff planes for rock-slides. The system allows rapid automated mapping of geometrical and kinematical slope properties in hard rock, providing the basis for spatially distributed deterministic sliding-susceptibility evaluations on a pixel base. Changing hydrostatic slope conditions and rock mechanical parameters can be implemented and used for simple predictive static stability calculations. Application is demonstrated for a study area in the Harz Mts., Germany.

ternal geometry of the slopes, and data about the geometric relationships between geological structures that might be activated for rockslides and topography. With this data, simple determinations of slope kinematics can be performed on a pixel base (Günther, 2003), providing the basis for spatial slope stability assessments when incorporating hydrological and rock mechanical data.

In this paper, we will present the state of development of RSS-GIS (Rock Slope Stability GIS), an expert-system based on ARCVIEW GIS<sup>TM</sup> software of ESRI (Environmental Systems Research Institute inc.). Grid-based RSS-GIS is build of several extensions (modules) for ARCVIEW GIS<sup>TM</sup> that can be used for a rapid automated mapping of geometrical and kinematical slope properties, and spatially distributed, pixel-based stability calculations of rock slopes.

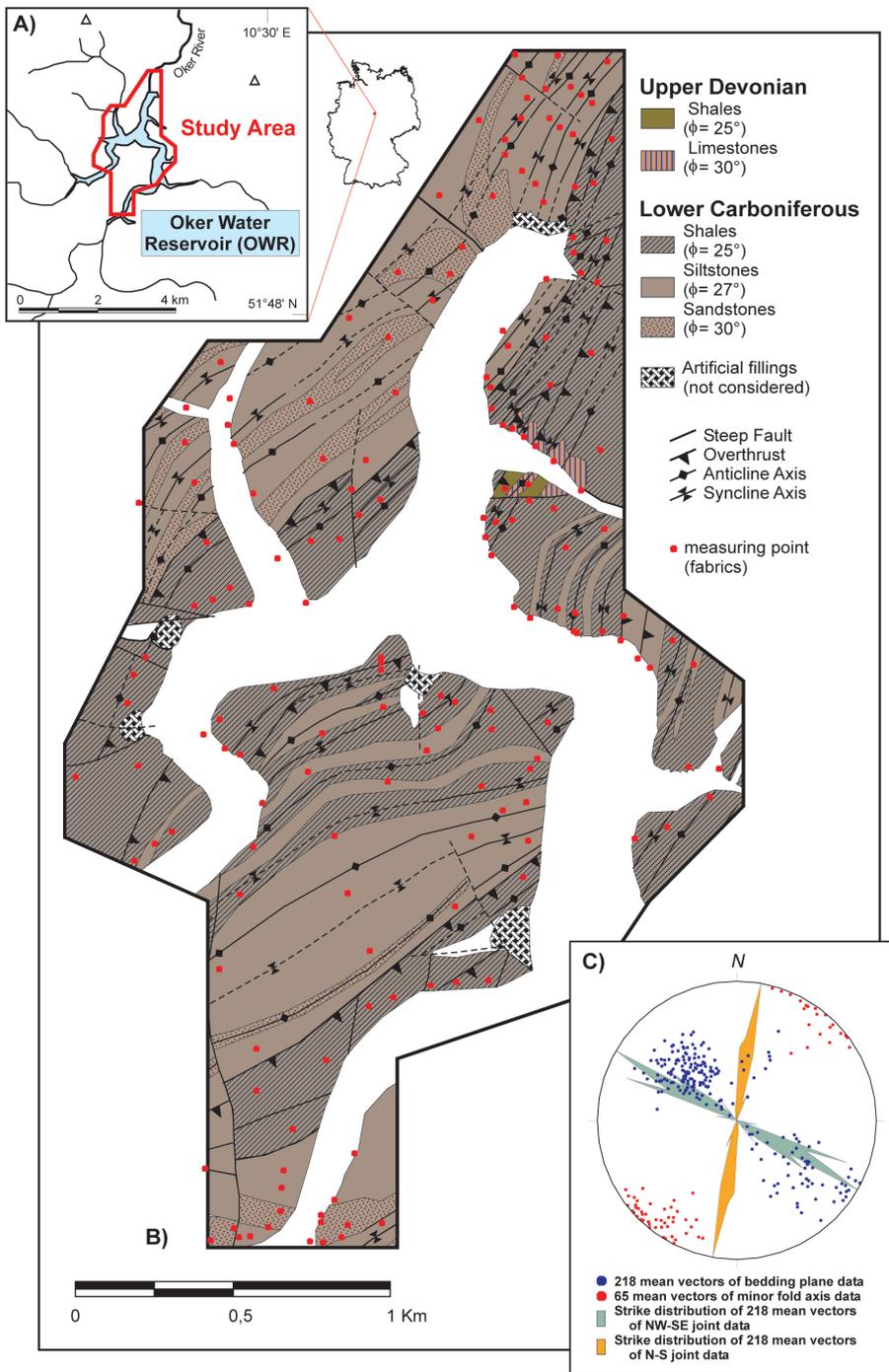
## 1 Introduction

GIS-based landslide susceptibility mapping is generally performed by two different methodological approaches. Qualitative heuristic or quantitative statistical modeling techniques mostly employ polygon data to define the spatial variability of geological, geomorphological, and landslide inventory terrain parameters (e.g. Carrara et al., 1995; Atkinson and Massari, 1998; Van Westen et al., 2003). Raster-based deterministic mapping techniques involve physically based slope stability calculations on a cell-per-cell basis (e.g. Hammond et al., 1992; Montgomery and Dietrich, 1994; Pack et al., 1998) with grid-based mechanical slope data. These models are commonly calibrated with the use of geotechnical material parameters as deduced from field- and laboratory experiments, or landslide data.

Of fundamental importance for the deterministic evaluation of the sliding susceptibility of large slope-areas in hard rock terrain are spatially distributed information about the in-

## 2 Database

The basis for spatially distributed evaluations of slope stability in hard rock terrain consists of continuous orientation data of sliding relevant geological structures (DSM, Digital Structural Models) and topography as derived from DEM (Digital Elevation Model) data. Computation of azimuth and dip (or “aspect” and “slope”) of topography with raster DEM-data is part of ARCVIEW GIS<sup>TM</sup> basic functionalities (e.g., Burrough and McDonnel, 1998). DSM-construction, however, is much more difficult and the suitable methodology depends on the kind and amount of available data and the specific structural geometry. For example, DSM (e.g. spatially distributed information about the orientation of a specific geological structure) might be derived from i) direct spatial interpolation of irregularly distributed measurements of tectonic orientation data (Meentemeyer and Moody, 2000), ii) direction-cosine interpolation of tectonic fabric measurements (Günther, 2003), iii) spatial extrapolation of elevation-registered curvilinear geological features through variable geometric projection techniques (VGP; De Kemp, 1998, 1999), or iv) derivation and spatial



**Fig. 1.** Locality (A) and tectonic map (B) of the study area in the Harz Mts., Germany (based on a modified geological map of Lower Saxony 1:25 000 sheet 4128, Hinze, 1971). The deformed flyschoid stratigraphic successions reveal prominently evolved sedimentary bedding planes and are intensely folded, jointed and faulted. The overall structural trend is oriented NE–SW with the fold structures facing to the NW. Friction angles for discontinuity planes in the different rock units were obtained by RMR-rating (Bieniawsky, 1989) including Schmidt hammer rebound tests at representative outcrop locations. Also shown: locations of fabric measuring points (locations outside study area are not shown). (C) Fabric diagram (equal area projection, lower hemisphere) showing direction distribution of bedding plane and joint data used for interpolation. Orientation of mean vectors of minor fold axis data points to subhorizontal fold geometry.

interpolation of structural contour data from map- and borehole data (Groshong, 1999; Kus and Barthel, 2000). Because of the different methodologies and the limited geostatistical and 3-D capabilities of ARCVIEW GIS<sup>TM</sup>, tools for construction of DSM are not yet implemented into RSS-GIS.

Besides geometrical data, spatially distributed geotechnical data (friction coefficients, cohesion values, etc.) can be used with RSS-GIS on a pixel base, but these parameters may also be estimated and generalized. For static stability calculations, hydrostatic slope conditions are of major importance.

If regional hydrological data for a specific study area is available, the data can be used in RSS-GIS; if not, these data must also be estimated.

In the example data set from a water reservoir in the Western Harz Mountains, Germany, dense structural information is available that allows constructions of DSMs with a pixel size of 10 m<sup>2</sup> for all sliding relevant geological discontinuity planes (Fig. 1). The DSMs were constructed by spatial interpolation of direction cosine-converted mean vectors of field measurements of each discontinuity set (see Günther,

2003) using an inverse distance to a power algorithm (Davis, 1986). For interpolation of bedding plane data, the traces of the horizontal folds from the tectonic map (Fig. 1) were incorporated as breaklines (e.g. pre-defined pixeltraces with a dip value zero). The traces of map-scale faults were incorporated as discontinuities for interpolation due to the fact that the folds are offset by these structures. Orientation data of joint fabrics were interpolated by using the fault traces of the tectonic map as discontinuities and neglecting the fold axes, because field observations indicate that the joints are offset by the faults but do crosscut the fold structures. Mean orientations of NW–SE and N–S striking joints and bedding planes, obtained at 218 observation sites were used to compute corresponding DSMs for our study area (Fig. 1, for a more detailed discussion on interpolation of fabric measurements see Günther, 2003). Structural field mapping was conducted at a scale of 1:5 000, the spatial position of the measuring points was obtained with a hand held GPS receiver and aerial photographs. The fabric measurements were carried out with a double circled geological fabric compass.

Topographic data consist of high-quality elevation data based on a 5 m resolution DEM (ATKIS DGM5) provided by LGN (Landesvermessung und Geobasisinformation Niedersachsen, Hannover). Geotechnical information, primarily consisting of friction coefficients of discontinuity planes for each geological unit, was obtained by rock mass classification (Bieniawski, 1989) procedures at representative field locations including Schmidt hammer rebound tests. Different rock units of the geological map were classified using mean values (Fig. 1). Because at this stage very limited geotechnical information is available, it was not possible to determine the spatial variability of friction coefficients within each geological unit. However, if spatially distributed geotechnical data should be available, it can be used with the software on a pixel base. Hydrological data, consisting of conductivity values for different rock units and hydraulic pressure head measurements in boreholes over tens of years, were obtained from a sample site located outside the western margin of the study area. Moreover, meteorological measurements have been carried out for a time span of 2 years.

### 3 Methodology

All applications described below are based on grid calculations on a pixel base. Despite the fact that the system is mainly dealing with 3-D vector data, 3-D analysis environments are not required because vector data are transformed into azimuth and dip values, respectively direction cosines and hence can be handled using multiple 2-D grids (Günther, 2003). Simple raster-based calculations were programmed directly within the ARCVIEW GIS<sup>TM</sup> environment, more complex computations have been encoded as externally compiled routines that are launched from the ARCVIEW GIS<sup>TM</sup> front end.

RSS-GIS consists of three ARCVIEW GIS<sup>TM</sup> extensions: “SlopeMap”, “StereoMap” and “HydroMap”. Each of these

may also be used independently, or combined with other available ARCVIEW GIS<sup>TM</sup> extensions.

#### 3.1 Spatially distributed determination of slope geometry and kinematics

Geometric properties of hard rock hill slopes consists of cutting edge- and angular relationships between two DSMs, or one DSM and topography (Günther, 2003). Alternatively, Meentemeyer and Moody (2000) presented a technique to calculate either a continuous or a classified index to characterize the alignment of geological fabrics with respect to topography (TOBIA, “Topographic-bedding plane intersection angle”). The RSS GIS extension “SlopeMap” allows the rapid automated calculation of azimuth and dip of cutting-edge and angular values between various DSM and DEM data, and calculation of TOBIA index or classes.

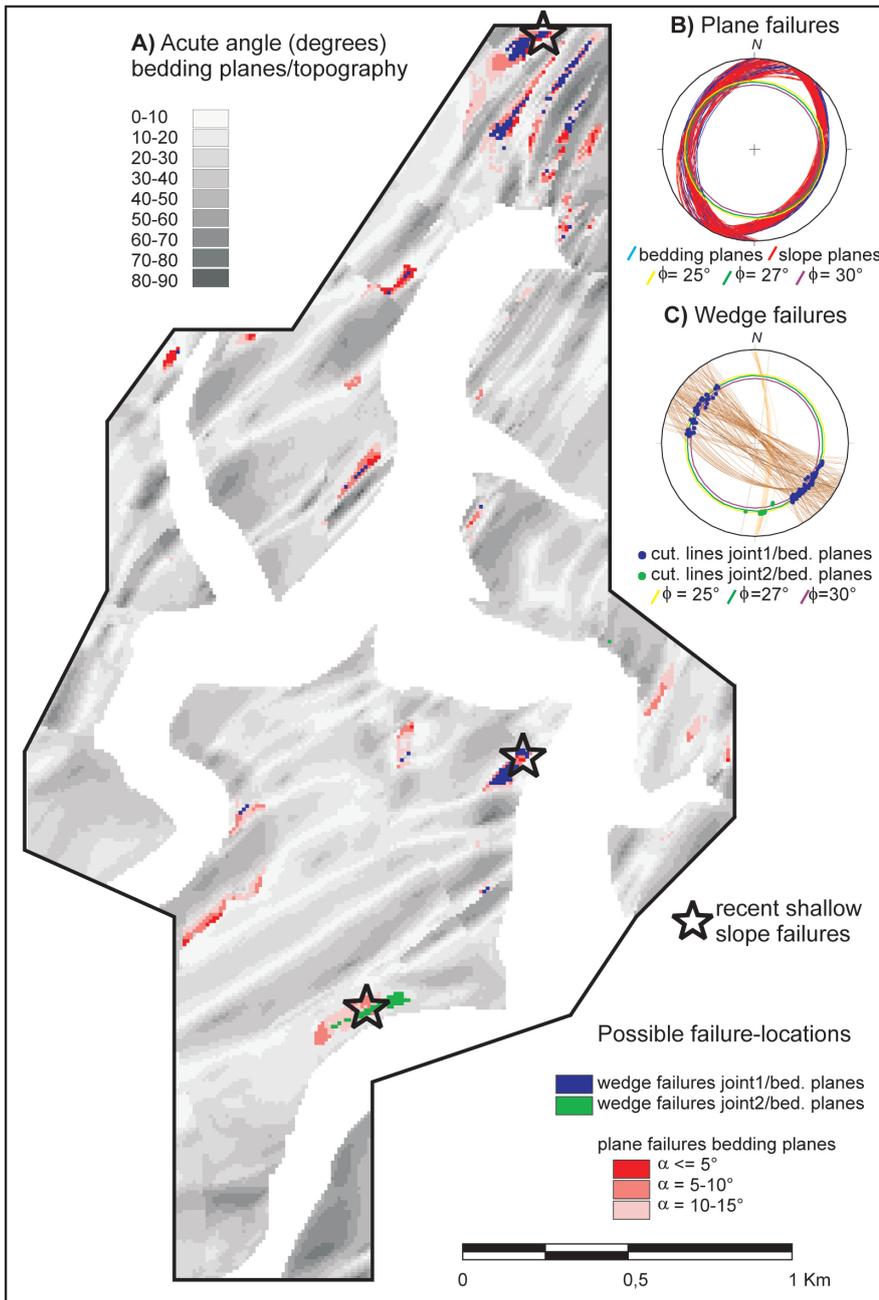
In hard rock hill slopes, three main types of failure kinematics along prominent rock discontinuities can be distinguished: plane failure, wedge failure and toppling (Hoek and Bray, 1981). In RSS-GIS, the kinematical possibility of these failure-types can be broadly evaluated on a regional scale with the extension “SlopeMap” from geometrical slope data (toppling is not discussed in this paper).

With the RSS-GIS extension “StereoMap”, stereographic analysis with grid- or point-based orientation data can be performed. “StereoMap” is based on enhanced routines of Knox-Robinson and Gardoll (1998). Besides plotting and cross-relation of orientation data, this module also allows statistical and eigenvector analysis after Wallbrecher (1986), rotation of vector data, plotting of small circles, and calculation of rose diagrams.

When determining the loci of possible plane failures with “SlopeMap” in RSS-GIS (Fig. 2), initially the conformity of a chosen discontinuity and the slope must be constrained by using either angular values or TOBIA-index. Then, a friction angle can be chosen either globally or for every pixel by defining a corresponding grid-theme. The algorithm evaluates at every pixel if the discontinuity dips steeper or equal to the friction angle, and if a user defined classification of geometrical alignment between slope and discontinuity is fulfilled. It produces a corresponding grid, where those parts of slopes are mapped where the slope dips steeper than or equal to the discontinuity (Fig. 2).

For the spatial evaluation of possible wedge failures along two geological discontinuities (Fig. 2), azimuth and dip grids of cutting edges of the regarded planes must first be calculated. Then, a friction angle can be chosen globally or by using a related grid-theme. The algorithm checks at every pixel if the cutting edge of the discontinuities dips within a space that is defined by the slope plane and a friction cone, whose half-opening angle corresponds to the defined friction angle. It produces a grid where the value 1 is given for cells where wedge-failure is kinematically possible, otherwise a no-data-value is returned.

The results of the kinematical analysis can be plotted into stereographic projections with the RSS-GIS “StereoMap”



**Fig. 2.** Geometrical and kinematical slope analysis. **(A)** Distribution of the acute angle  $\alpha$  between bedding plane DSM and topography. Also shown: Spatial distribution of pixel locations where bedding-plane parallel slope failures are kinematically possible (classified according to angular conformity between the planes, slope angle, and friction angle along potential failure planes), and locations where wedge failures along bedding planes and two joint DSM are kinematically possible. **(B)** Fabric diagram showing bedding plane and slope orientations of pixel locations kinematically susceptible for bedding plane parallel slope failure with associated friction cones. **(C)** Fabric diagram showing cutting line linears between joints and bedding planes, and joint planes of pixel locations where wedge failure along joints and bedding planes are kinematically possible. The directions of the cutting lines between the respective discontinuity pairs indicate the directions of possible sliding.

extension (Fig. 2) and can be back-related to the map to examine critical regions. In the example shown in Fig. 2, possible locations for slope failures on bedding planes as well as wedge failures on bedding planes and the NW–SE resp. N–S striking joint systems are documented. The validity of this analysis is proven by local rock slides with corresponding mechanisms that recently occurred on these slope portions (Fig. 2, Günther et al., 2002).

### 3.2 Spatially distributed determination of hydrological slope conditions

For spatially distributed static stability calculations in hard rock terrain, groundwater pressures on sliding-relevant dis-

continuity planes must be known or estimated. Towards this goal, the relative degree of water saturation of a specific lithostatic column has to be determined for every pixel of a study area from topographical and meteorological data, as well as from physical slope properties (i.e. hydraulic conductivity). Due to the fact that rock mass relaxation and fracture-opening affected the hillslopes of the study site down to depths of about 20 m (Schöniger, 1991), we preliminarily assume that the bulk direction of shallow groundwater flow from and to each pixel is at a first approximation mainly constrained by the orientation of the topography. Although we are concerned with slope stability on individual geological structures, we treat the relaxed slope zone as a continuum for hydrological considerations because the direction of shallow



**Fig. 3.** Relative topographic wetness index calculations according to Pack et al. (1998). The calculations were performed by specifying a thickness of the transmissive layer of 20 m, and by applying a global hydraulic conductivity of  $2.7 \cdot 10^{-5}$  m/s.

subsurface flow must be thought not to be governed by the orientation of individual, but all present conductive structures. For the considered regional scale, this assumption is supported by runoff and pressure head measurements in the study area (Carstensen et al., 2003).

In order to determine flow directions and specific catchment areas for each pixel from the DEM-data, the  $D_{\text{inf}}$ -methodology from the TARDEM program suite presented by Tarboton (1997) was incorporated into the extension “HydroMap” of RSS GIS. A relative topographic wetness index ( $WI$ ) according to Pack et al. (1998) can then be calculated for a specific thickness of a transmissive layer on a pixel base with

$$WI = \frac{R \cdot a}{T \cdot \sin \theta} \quad (1)$$

where  $a$  = specific catchment area ( $\text{m}^2/\text{m}$ ),  $R$  = steady-state recharge rate ( $\text{m}/\text{hr}$ ),  $T$  = hydraulic transmissivity ( $\text{m}^2/\text{hr}$ ), and  $\theta$  = topographic slope angle (Pack et al, 1998). This index ranges for shallow subsurface flow between 0 and 1 with any excess above saturation inducing overland flow. Thus,  $WI$  specifies the relative hydrostatic depths within the transmissive layer at each pixel location.

Topographic wetness index calculations are based on the following general assumptions: i) shallow lateral subsurface flow follows topographic gradients, ii) lateral discharge at every pixel location is in equilibrium with steady state recharge  $R$ , iii) the capacity for lateral flux at each point is  $T \sin \theta$  (Montgomery and Dietrich, 1994; Pack et al., 1998). The last assumption implies that a uniform hydraulic conductivity is assumed for the relaxed slope zone, overlying relatively

impermeable bedrock. The steady state assumption for relative saturation calculations implies that transient groundwater fluctuation and infiltration as a response to varying precipitation are not considered.

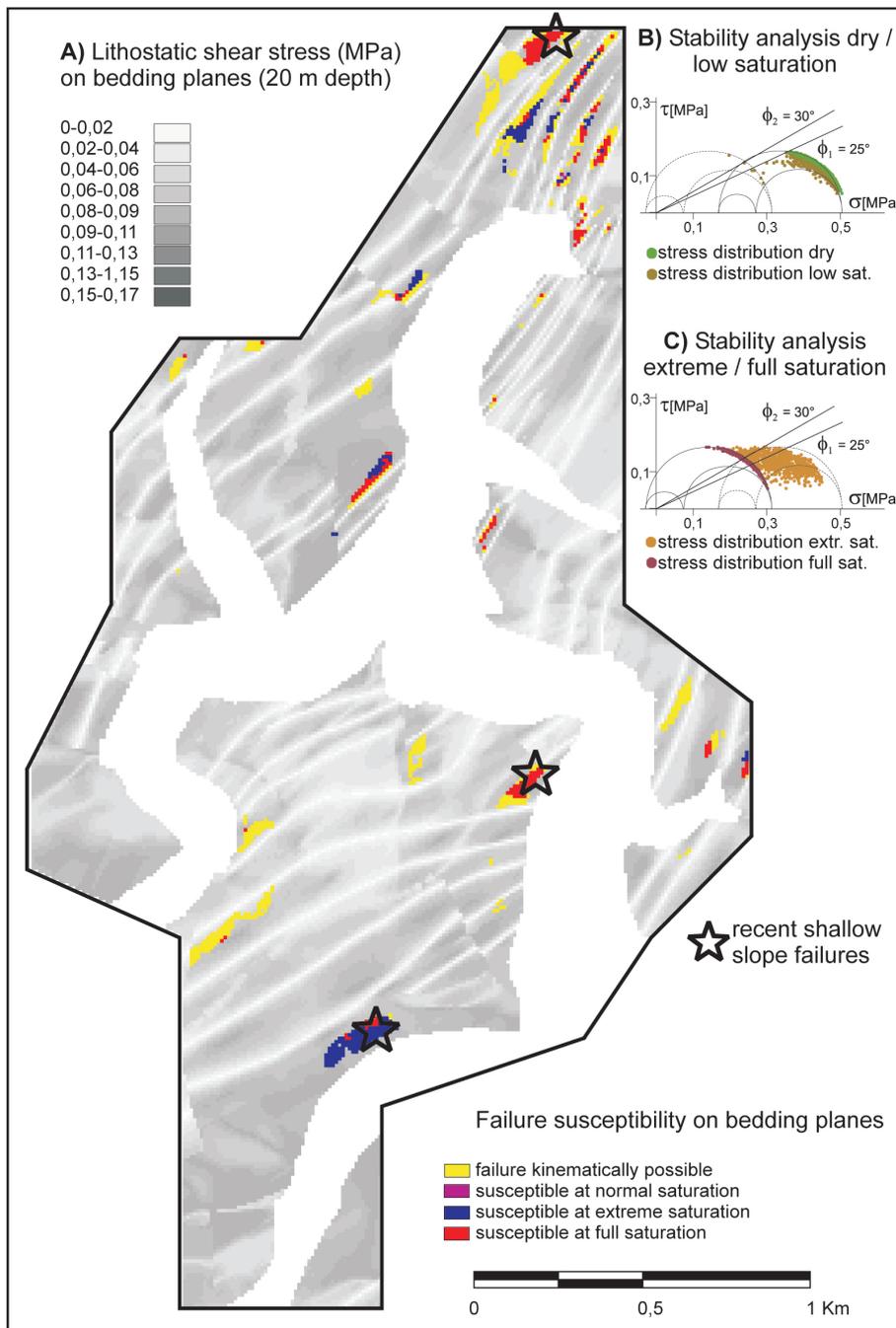
A global hydraulic conductivity of  $2.7 \cdot 10^{-5}$  m/s was set for the whole study area for relative saturation calculations. This value represents a mean value of conductivity data obtained from field- and laboratory analysis within the weathered slope zone west of the study area (Schöniger, 1991). However, it is also possible with “HydroMap” to use spatially distributed conductivity values, if available.

During our meteorological observation period of two years, frequent (“normal”) precipitation events bear about 10.1 mm/day of precipitation. The highest rainfall event measured during our observation period was, however, 10 times higher (110 mm/day) and coincides with a statistical 100 year maximum for the study area. In Fig. 3, the spatial distribution of relative saturation of a transmissive layer of 20 m thickness for both cases is shown.

### 3.3 Spatially distributed determination of slope stability

The stability of kinematically critical slope sections can be evaluated by calculating the slope-orientation dependent lithostatic normal- and shear stress distribution on potential failure planes for each pixel at a specified depth (Günther, 2003), and by relating this to a Mohr-Coulomb failure criterion formulated as

$$\tau_{\text{crit}} = c + (\sigma - u) \tan \phi \quad (2)$$



**Fig. 4.** Spatially distributed stability analysis for bedding plane-parallel slope failure. (A) Distribution of lithostatically induced, slope orientation dependent shear stress magnitudes on the bedding plane DSM at a depth of 20 m. Also shown: Locations of kinematically possible failure (Fig. 2), and spatial distribution of possible instability due to three different saturation-conditions. (B) Stability analysis in Mohr diagram of pixel values for the dry case and low saturation. (C) Stability analysis for high and full saturation. The Mohr circle triplets indicate principal stress magnitudes for dry case and full saturation, respectively.

where  $\tau_{\text{crit}}$  = critical shear stress to exert movement on discontinuity (MPa),  $c$  = cohesion along plane (MPa),  $\sigma$  = normal stress on the plane (MPa),  $u$  = hydrostatic pressure (MPa),  $\theta$  = friction angle along the plane.

In the RSS-GIS extension “SlopeMap”, the effective normal stress ( $\sigma'$ ) for each pixel is calculated by subtracting the isotropic hydrostatic stress ( $u$ ), as resulting from specific slope saturation conditions, from the lithostatically induced normal stress ( $\sigma$ ). Grids of effective normal and shear stress values, and a grid with pixels of  $\tau/\sigma'$  lying above the cell-specific failure-criterion, are produced. Optionally, the pixel values of effective normal and shear stresses can be plotted

into a Mohr-diagram together with the failure criterions. The datapoints in the Mohr-diagram can be cross-related to a map or a stereographic projection.

In Fig. 4, a susceptibility-analysis for slope movements along cohesionless bedding planes at a depth of 20 m with an averaged global rock density of  $2.6 \text{ g/cm}^3$  and a principal stresses ratio  $R$  set to 0.3 is shown for the study area. Clearly, most slope regions are stable even at high saturation. For the unrealistic assumption of full saturation of the whole slope region, still not all slope portions kinematically susceptible to failure would fail.

#### 4 Conclusions

We have presented the stage of development of RSS-GIS, an expert system for distributed deterministic evaluation of slope stability of rock slopes. RSS-GIS is useful for preliminary regional stability assessments of large slope areas under varying hydrological conditions. Because the approach is concerned with regional evaluations, relatively simple methods are applied. Sensitivity analyses may be performed when geotechnical and hydrological data are completely lacking and can only be estimated. If measured data is available, the obtained models can be calibrated to a certain degree. RSS-GIS offers the possibility for a detailed parameterization of stability models if the according data is available, however, it should be kept in mind that such models may become overparametrized considering the regional modelling approach. In the example data shown here, the results obtained with RSS-GIS agree well with recently observed slope instability-phenomena within the study area (Figs. 2 and 4, Günther et al., 2002).

For future developments, it is planned to incorporate the effect of changing reservoir lake levels on groundwater height into the groundwater saturation calculations. This was not treated in the presented study because of a lack of data and missing topographic and geological information below the recent water table. Furthermore, it is planned to implement a transient infiltration model into the hydrological modelling tool to overcome the limitations of steady state calculations (Iverson, 2000). Next, it is important to develop strategies to model multidirectional flow on geological discontinuities represented by DSM to make the system applicable in terrains where bulk shallow subsurface flow direction cannot be approximated by the orientation of topography.

To conclude, it is imperative to note that the results produced with RSS-GIS are only models obtained at a regional scale, and one should remember the quality of the database and the limitations of the methods when interpreting the results. Resolution and validity of the models produced with RSS GIS mainly depend on the amount, density, quality and kind of input-data. Nevertheless, even though RSS-GIS cannot substitute detailed stability assessments of critical slope sections at a local scale, it allows regional first-order assessments and the identification and mapping of critical slope sections.

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