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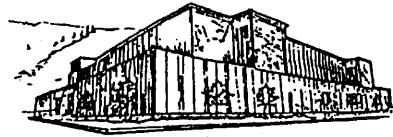
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# A Breeder Algorithm for Stellarator Optimization

By

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B.S. in Mathematic Science, Hunan Normal University, China, 1988

Presented in partial fulfillment of the requirements

For the degree of

Master of Science

The University of Montana

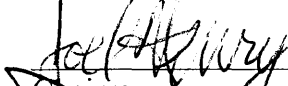
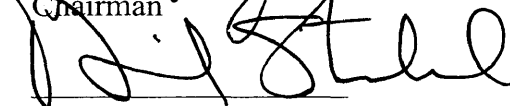
December 2004

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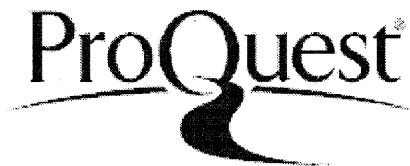


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A Breeder Algorithm for Stellarator Optimization

Committee Chair: Dr. Joel Henry 

A comparison of Levenberg-Marquardt and Genetic optimization algorithms is presented and a hybrid optimization algorithm which combines these two is developed. A number of different optimization algorithms have been applied to optimization in various physical areas including both steepest descent and evolutionary optimization algorithms. Each algorithm has both advantages and disadvantages. This paper provides a comparison of optimization between the Levenberg-Marquardt routine, a steepest descent optimization method, and the Genetic Algorithm, a global evolutionary optimization algorithm, in an applied plasma physics area. To take the advantages of both steepest descent optimization and evolutionary optimization, the Breeder Algorithm which combines the Genetic Algorithm with the Levenberg-Marquardt algorithm is introduced. A description of the design and structure of the Breeder Algorithm is presented, as well as the code reviews which present the strategy and challenges of the implementation.

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## 1. Introduction

A number of different optimization algorithms have been applied to stellarator optimization including both steepest descent and evolutionary optimization algorithms. A stellarator is a device used to confine a high-temperature plasma with magnetic fields with the long-term goal of sustaining a controlled nuclear fusion reaction. In a stellarator, the magnetic field necessary to confine the plasma is completely generated by external coils. The first such devices were built at the Princeton Plasma Physics Laboratory in 1951. In recent years, the design of stellarator experiments has been aided by extensive use of computational algorithms used to optimize confinement and stability properties of the magnetic configuration. In this paper, we present two major works: (1) a comparison of two different algorithms applied to the optimization of three-dimensional equilibria: a Levenberg-Marquardt routine (LM), and a Genetic Algorithm (GA); and (2) the development of a new optimization algorithm, the Breeder Algorithm (BA), which combines the methods of GA and LM.

The speed and efficiency of numerical codes used to calculate equilibrium, stability, and transport properties of three-dimensional plasmas has been sufficiently enhanced so that global (in parameter space) optimization methods are now feasible. In principle, the primary advantage of evolutionary algorithms such as GA is that they perform a global parameter space search. This is in contrast to steepest descent methods which perform a local parameter space search for the optimal configuration. LM, for example is prone to finding local extremum. The primary disadvantage of evolutionary algorithms is that they can be inefficient when compared to steepest descent algorithms. In the first part of this work, we present a comparison of the GA and LM methods when applied to stellarator optimization.



The Breeder Algorithm combines a global Genetic Algorithm with a local Levenberg-Marquardt optimizer used to refine each generation. The goal of the BA algorithm is to take advantage of the global parameter space search of the evolutionary algorithm while maintaining the efficiency of the LM method. Here, we present a description of the Breeder Algorithm and the first results from the application of the BA to stellarator optimization.

## 2. The Existing Search Algorithms

In this section we give brief descriptions of the two optimization algorithms most commonly used for stellarator optimization. An example stellarator optimization case is presented and the optimization results for both algorithms on this case are discussed.

### 2.1. The Levenberg-Marquardt Algorithm

#### 2.1.1. A brief introduction to the Levenberg-Marquardt algorithm

The problem for which the LM was developed is called *nonlinear least squares minimization*. Suppose that we have a function:  $f(\bar{x}) = \frac{1}{2} \sum_{j=1}^m r_j^2(\bar{x})$ , where

$\bar{x} = (x_1, x_2, \dots, x_n)$  is a vector, and each  $\chi^2$  is a function from  $R^n$  to  $R$ . The  $\chi^2$  are referred to as a residual and it is assumed that  $m \geq n$ . Also,  $f$  can be represented as a residual vector  $r: R^n$  to  $R^m$  defined by  $r(x) = (r_1(x), r_2(x), \dots, r_m(x))$ . Therefore,  $f$  can be written as

$f(x) = \frac{1}{2} \|r(x)\|^2$ . The derivatives of  $f$  can be written using the Jacobian matrix  $J$  of  $r$

with respect to  $x$  defined as  $J_{ij} = \frac{\partial r_j}{\partial x_i}, 1 \leq j \leq m, 1 \leq i \leq n$ .

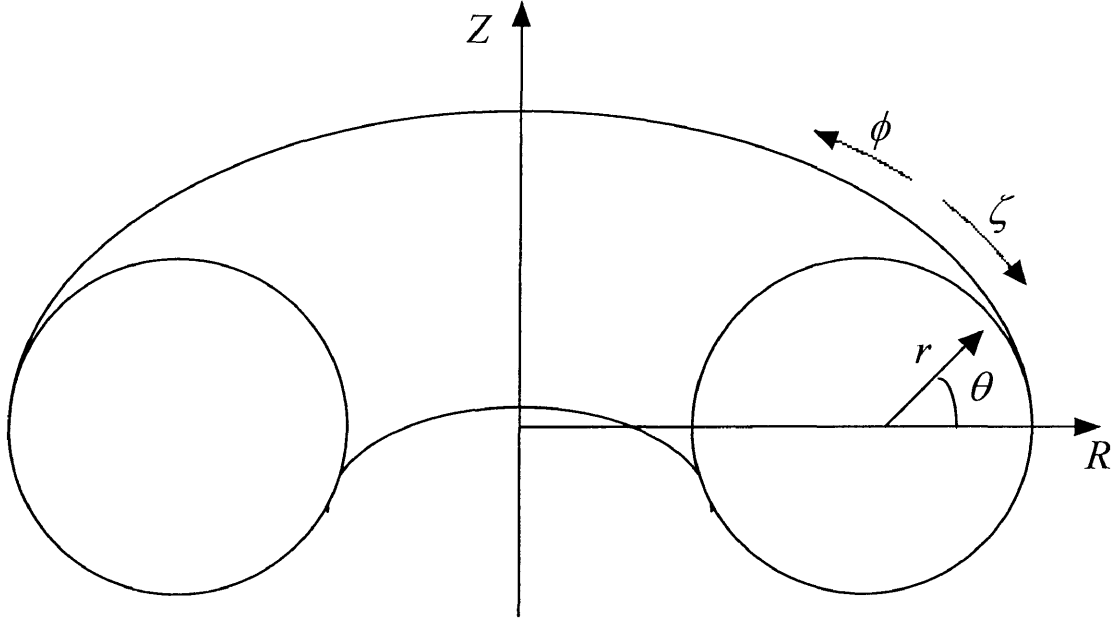
The LM is a blend of gradient decent and Gauss-Newton iteration. Vanilla gradient descent is the simplest technique to find minima in a function. Parameter updating is performed by adding the negative of the scaled gradient at each step,  $x_{i+1} = x_i + \lambda \nabla f$ . There are some disadvantages using pure gradient descent updating. One well known is when the given function is not differentiable, pure gradient descent won't work properly.

Using a Taylor series, there is an update rule:  $x_{i+1} = x_i - (\nabla^2 f(x_i))^{-1} \nabla f(x_i)$ . Based on that, and Levenberg's update rule:  $x_{i+1} = x_i - (H + \lambda I)^{-1} \nabla f(x_i)$ , Marquardt introduced an improved updating formula in 1963:  $x_{i+1} = x_i - (H + \lambda \text{diag}[H])^{-1} \nabla f(x_i)$ . Where  $H$  is the Hessian Matrix,  $H_{ij} = \frac{1}{2} \frac{\partial^2 \chi^2}{\partial \alpha_i \partial \alpha_j}$  [1].

To summarize, LM is an iterative method to minimize the sum of squares  $\chi^2$  ("Chi-Square") of  $M$  functions in  $N$  variables. LM requires the finite-difference approximation of the Jacobian matrix in each iteration. LM uses the Jacobian to minimize  $\chi^2$  in a local region of parameter space.

### 2.1.2. A typical LM search example

In this section we discuss a typical stellarator optimization case and the results of an LM optimization on the case. This plasma equilibrium has a three-dimensional fixed boundary determined by the Fourier coefficients,  $R_{bc}(m,n)$  and  $Z_{bc}(m,n)$ , where  $m$  and  $n$  represent the poloidal and toroidal mode numbers, respectively. A schematic of the cylindrical coordinates  $(R, \phi, Z)$  and the toroidal coordinates  $(\rho, \theta, \zeta)$  is shown in Figure 1.



**Figure 1.** A schematic of cylindrical  $(R, \phi, Z)$  and the toroidal  $(\rho, \theta, \zeta)$  coordinates.

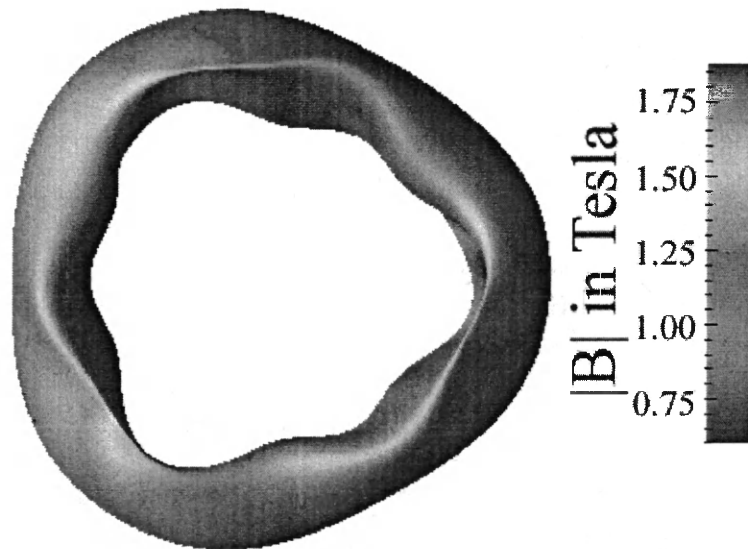
The outer boundary is given by

$$R(\theta, \zeta) = \sum_{m,n} R_{bc}(m, n) \cos(m\theta - n\zeta)$$

$$Z(\theta, \zeta) = \sum_{m,n} Z_{bc}(m, n) \sin(m\theta - n\zeta)$$

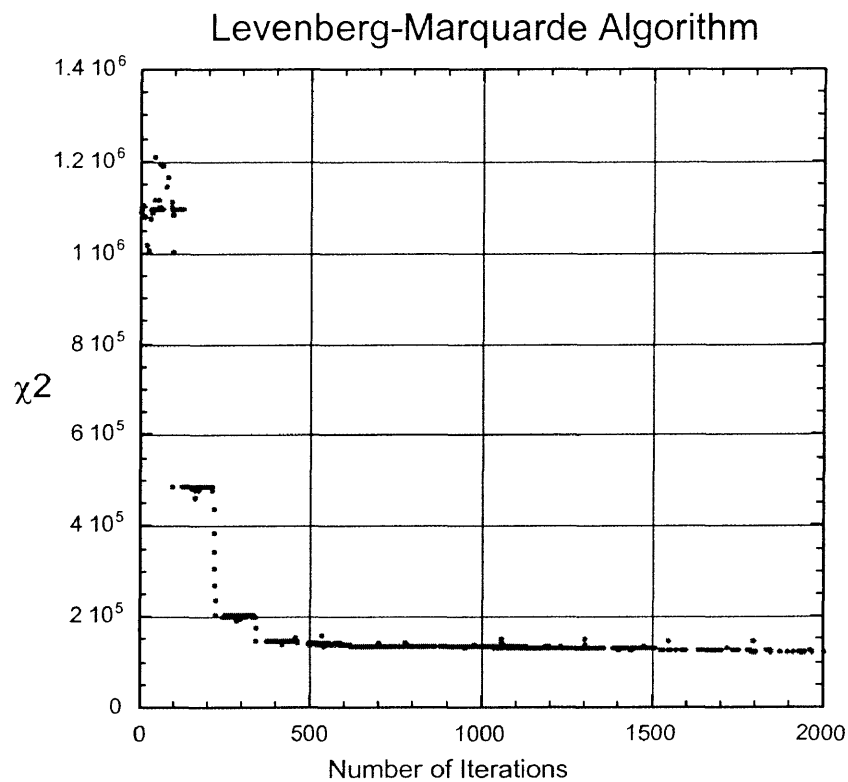
where a symmetry called stellarator symmetry has been assumed. These boundary coefficients are some of the independent variables,  $m$  and  $n$ , which LM can vary to improve the plasma properties as discussed below. The strength of the magnetic field varies throughout the plasma including on the outer surface. Figure 2 shows the outer plasma boundary for one of the test cases we used which is called QPS15. The color on the surface indicates the strength of the magnetic field at that point. Some of the basic plasma parameters of QPS15 are as follows. The average magnetic field strength is 1.0 T. The average plasma pressure is measured relative to the magnetic field strength squared

and is called the plasma beta,  $\beta = \langle p/B^2 \rangle$  and for the QPS15 plasma,  $\beta = 15\%$ . This is a very-high plasma beta relative to existing stellarator plasma experiments. The aspect ratio,  $A$ , is the ratio of the average major radius,  $R$ , to the average minor radius,  $a$ . For QPS15,  $A = 3.7$ . This is low relative to most three-dimensional confinement devices. This configuration has an electrical current running through the loop of plasma with a total current of 176 kA. This is in contrasting to most stellarators which have zero net plasma current.



**Figure 2.** The outer plasma surface of the QPS15 test case.

The initial  $\chi^2$  was  $1.20 \times 10^6$  and this was primarily due to the plasma being unstable to certain types of perturbations. A number of stability checks are part of the calculation for each case and a stable plasma is one of the targets. There were  $N = 8$  independent variables which included the plasma boundary coefficients and coefficients describing the pressure and current profiles. The final  $\chi^2$  was  $1.213 \times 10^5$  and this reduction was primarily due to improvement in the stability of the plasma.



**Figure 3.** The evolution of the total  $\chi^2$  during an LM optimization.

Figure 3 shows the total  $\chi^2$  vs. the number of iterations in the optimization. In the first 100 iterations as the Jacobian was being determined, the average  $\chi^2$  remained around the initial  $\chi^2$  value, then between 100 to 105 iterations, the value of  $\chi^2$  drops significantly as the algorithm moves down the gradient in parameter space. The Jacobian is recalculated at the new position in parameter space during iterations 105-200 and then the algorithm again makes significant progress in reducing  $\chi^2$  as it moves down the new gradient. This process is repeated several times. After 400 iterations,  $\chi^2$  remains relatively constant as the optimizer ceases making any significant progress. This indicates

a local minimum in the  $\chi^2$  function has been obtained. This is typical for an LM optimization.

### **2.1.3. Advantages and disadvantages of the LM search algorithm**

Since LM is a single-shot method which attempts to find the local fit-statistic minimum nearest to the starting point. Its principal advantage is that it uses information about the first derivative of the fit-statistic as a function of the parameter values to guess the location of the fit-statistic minimum. Thus this method works well (and fast) if the statistic surface is well-behaved. For the testing case shown above and other cases tested, initial results show that the LM algorithm is most effective in minimizing  $\chi^2$  after ~500 iterations

The principal disadvantages of LM are that it will not work as well with pathological statistic surfaces, the first or second derivatives of the function of the surfaces do not exist, and there is no guarantee it will find the global fit-statistic minimum.

## **2.2. The Genetic Algorithm**

### **2.2.1. A brief introduction to the Genetic Algorithm**

Genetic algorithms (GA) were formally introduced in the 1970s by John Holland [2]. The continuing performance improvements of computational systems have made them attractive for some types of optimization. In particular, genetic algorithms work very well on mixed (continuous and discrete), combinatorial problems. The three most important aspects of using genetic algorithms are: (1) definition of the objective function, (2) definition and implementation of the genetic representation, and (3) definition and

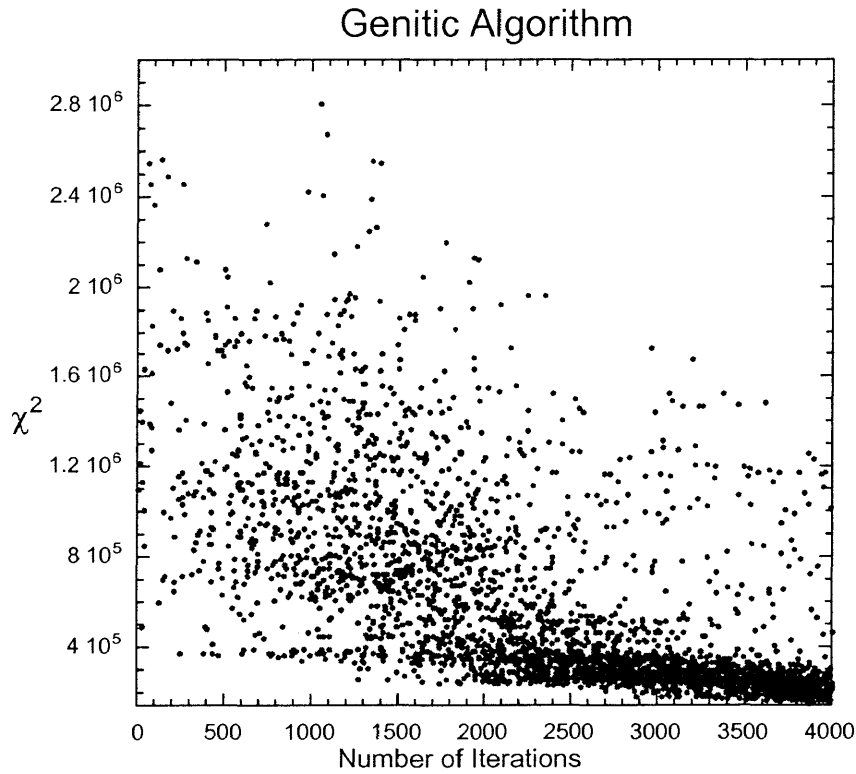
implementation of the genetic operators. Once these three have been defined, the generic genetic algorithm often works well. Beyond that you can try many different variations to improve performance, find multiple optima or parallelize the algorithms.

Genetic algorithms are inspired by the theory of evolution. The solution method used by genetic algorithms is an evolutionary process. The GA begins with a set of randomly selected solutions (represented by chromosomes) called a population. Solutions from one population are taken and used to form a new population. These are generated by genetically-inspired operators, of which the most well known are *crossover* and *mutation*. Crossover is performed with probability  $p_{cross}$  (the “crossover probability”) between two selected individuals, called *parents*, by exchanging parts of their genomes to form two new individuals, called *offspring*; in its simplest form, substrings are exchanged after a randomly selected crossover point. This operator tends to enable the evolutionary process to move toward “promising” regions of the search space. The mutation operator is introduced to prevent premature convergence to local optima by randomly sampling new points in the search space. It is carried out by flipping bits at random, with some (small) probability  $p_{mut}$  [3] This is motivated by a hope that members of the offspring will be better (i.e., have a lower  $\chi^2$ ) than the old one. A new population is formed from the parents and offspring with the lowest  $\chi^2$  values (also called their fitness) - the more suitable the cases are the more chances they have to reproduce.

This is repeated until some condition (for example number of generations or improvement of the best solution) is satisfied.



### 2.2.2. A typical GA search example



**Figure 4.** The evolution of the total  $\chi^2$  during an GA optimization.

In order to compare GA with LM, we used the same configuration of testing files as we used for LM algorithm, namely the QPS15 case. In order to make the parallel computation more efficient, we chose 48 as the population size because we use 3 nodes and each node contains 16 processors in IBM-SP environment. The generations are 12 to 15 because after 15<sup>th</sup> generation, the  $\chi^2$  won't have significant improvement from our experiment. The total  $\chi^2$  is shown as a function of the number of iterations in Figure 4. In the first thousand iteration  $\chi^2$  is scattered around the initial value with a wide range of values and the density of  $\chi^2$  points is relatively low. After this initial period, more and more  $\chi^2$  points are clustered in a high density area near a minimum  $\chi^2$  value. The number

of excursions far from the optimal value decreases. This behavior of  $\chi^2$  is typical for a GA search.

### **2.2.3. Advantages and disadvantages of the GA search algorithm**

Since GA is based on a set of randomly selected solutions, its principal advantages are: (1) GA is less susceptible to getting 'stuck' at local optima than gradient search methods; (2) It's faster than the simulation evaluation; (3) It's more deterministic in terms of the evaluation provided for a given candidate.

The principal disadvantages of GA are: (1) There are few jobs that GA can do better than a heuristic-based search (i.e., if you have some ideas of how to solve your problem, you're probably better off implementing those ideas than you are turning your problem over to a GA, which relies on randomness); (2) The Genetic Algorithm was effective only on certain cases. We have been tested 4 different cases for this project, GA can not work for one of them at all; and (3) global algorithms such as GA tend to be computationally expensive relative to steepest descent methods since the number of iterations for GA is relatively greater than that for LM.

### **3. The Breeder Algorithm**

The Breeder Algorithm combines a global Genetic Algorithm with a local Levenberg-Marquardt optimizer used to refine each generation. For each individual in GA, BA applies LM to refine it for producing the next generation. The goal of the BA algorithm is to take advantage of the global parameter space search of the evolutionary algorithm while maintaining the efficiency of the LM method.

#### **3.1. Design Description and Diagrams**

The BA combines the global coverage of the GA with intermediate optimization steps using the LM routine. The primary structure of BA is:

- (1) Initial generation production by the genetic algorithm (outer loop)
- (2) Refinement of the members of this generation using a Levenberg-Marquardt step (inner loop)
- (3) Evolving to future generations back in the genetic algorithm.

The Figures 5-7 show the primary structure of BA. Figure 5 indicates the existing structure of the Stellarator Optimization code. It takes an input file, runs through one of three existing optimizations, Levenberg-Marquardt, GA or DE (Differential Evolution algorithm, similar to GA but not discussed here), and produces a number of output files. Figure 6 illustrates the highest level BA structure which is a modification of the Figure 5. Generally, we add a new optional optimization, BA, to the existing ORNL structure (ORNL is the existing stellarator optimization code developed by scientists from Oak Ridge National Laboratory). The major BA structure is shown in Figure 7, as well a comparison to the GA structure. GALM\_DRIVER is modified from GA\_DRIVER. A

subroutine called SUB\_OPTIMIZE which implements LM is inserted into GA\_EVALOUT subroutine. This is the core part of BA.

### 3.1.1. Existing Structure:

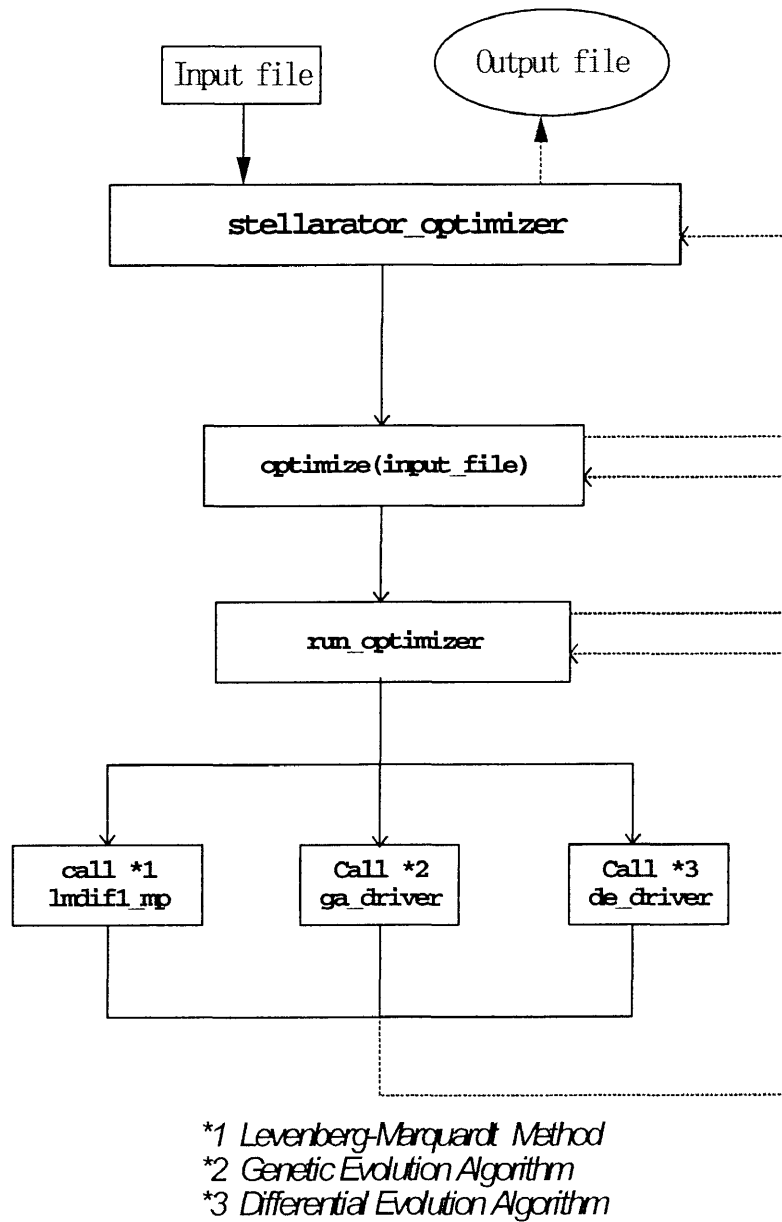
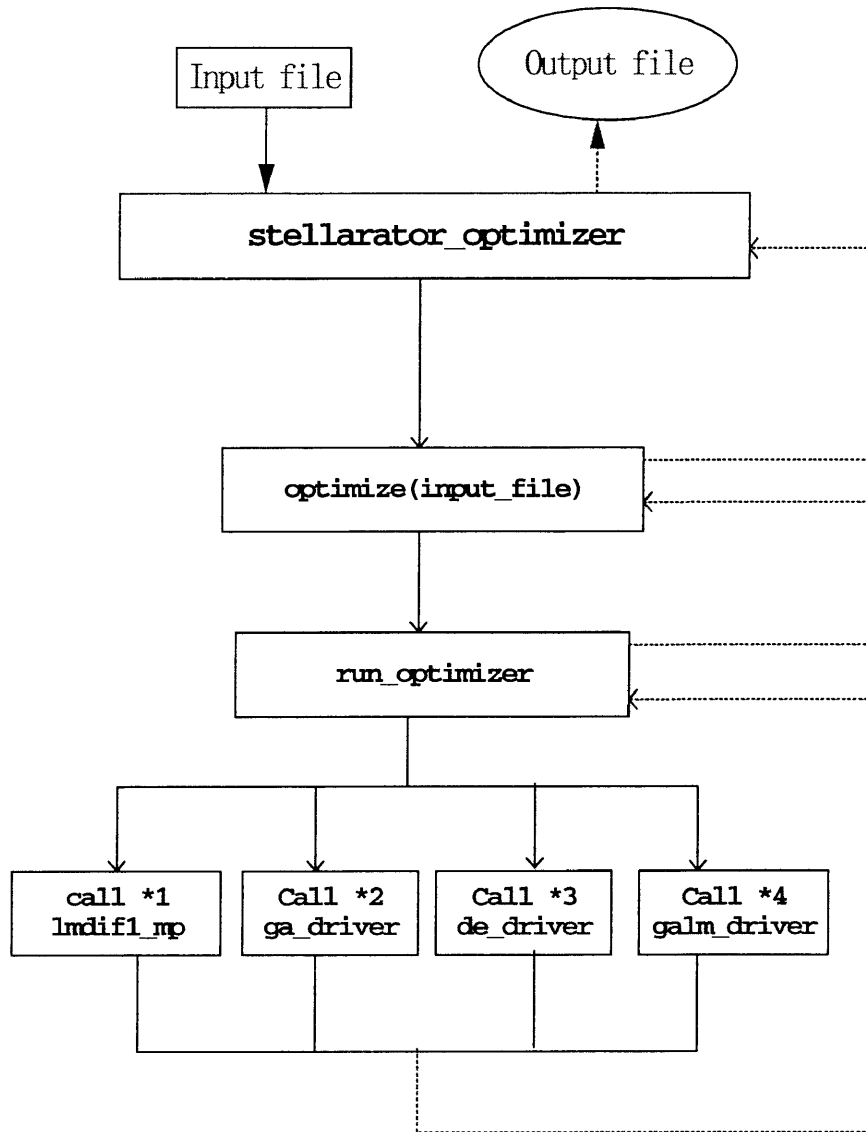


Figure 5. Existing structure of ORNL code

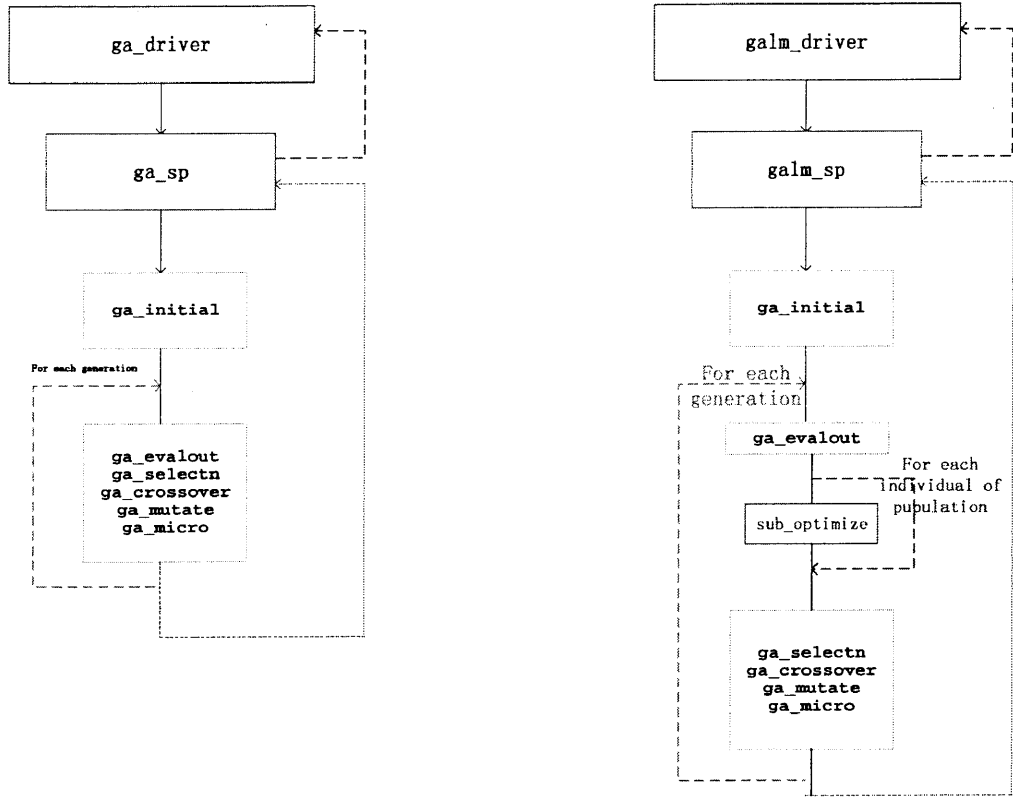
### 3.1.2. Modified Structure:



- \*1 Levenberg-Marquardt Method
- \*2 Genetic Evolution Algorithm
- \*3 Differential Evolution Algorithm
- \*4 Breeding Algorithm

Figure 6. Modified structure to ORNL code

### 3.1.3. BA modifies GA structure



Where sub\_optimize(input\_file) using the input files produced by each population is similar as optimize but only runs through Levenberg-Marquardt routine

**Figure 7. Comparison of GA and BA structures**

### 3.2. Coding strategy for the BA

The original code of Stellarator Optimization was developed by Oak Ridge National Laboratory (ORNL). The Stellarator Optimization code consists of multiple packages to achieve various purposes including the calculation of magnetic fields produced by a set of coils, determination of a three-dimensional plasma equilibrium, assessment of the stability of the equilibrium, estimation of the transport properties of the plasma, and an overall optimization structure that modifies the input plasma properties to approach a user-defined goal of a stable, high-pressure plasma. The Breeder Algorithm is a modification to the structure of two of these packages called LIBSTELL and STELLOPT. The LIBSTELL library consists of subroutines used by many of the packages and includes the optimization algorithms. The STELLOPT code (this is short for Stellarator Optimizer) is the primary code which makes calls to the optimization subroutines contained in LIBSTELL and also makes system calls to execute other packages that calculate plasma properties such as equilibrium and stability.

In the STELLOPT package, we added a BA optimization option to the RUN\_OPTIMIZER subroutine which implements the different optimizations using various approaches selected by the user, as well as adding a routine called RUN\_SUB\_OPTIMIZER which implements the LM routine when called by the GA\_EVALOUT subroutine in the LIBSTELL package.

In the LIBSTELL package, we created a routine called GALM\_DRIVER which performs the role of entry to BA. The most significant part of BA is the modification to the GA\_EVALOUT subroutine. The primary purpose of the GA\_EVALOUT subroutine is for GA to evaluate the population, assign fitness, establish the best individual, and

output essential information. The modification we made here is to insert an LM search for each individual of each population. The most challenging task in this portion of the project was making the “inner” LM work properly in parallel computation environment handling the working space including temporary working files, and correctly cleaning up memory space after each LM routine. Since both GA and LM share the same extensions of temporary files when those optimizations were implemented independently, once those two were combined together, it was necessary to develop a new system of shared extensions. An obvious example of a potential problem here is that after completing each LM step, the program will operate a cleanup process which removes most of the temporary files. In our modification, we must consider which temp files can be cleaned up and which ones must be kept since they hold the information for the future computations. To approach this goal, in addition to the existing temp filename extension for optimization, `_opt` extension, we introduced a new temp filename extension called `_oga` extension using for BA only. Therefore, after completing each LM routine for an individual, all reusable information will be copied to files with `_oga` extension from files with `opt` extension, and those files with `opt` extension will be removed in the clean up process. After an LM step for all individuals in a generation have been completed, all those files with either `_opt` extension or `_oga` extension will be cleaned up. The files with a `_min` extension that contain the minimum optimal case are saved.



### 3.3. Coding challenges for BA

The implementation environment of the Stellarator Optimization is an IBM SP. The language is Fortran90 using MPI libraries. In an average case, we use 3 nodes with 16 processors in each node.

As in most parallel programs, file operation is a big issue. In the entire optimization process, the program has to deal with hundreds of operations to input, output, and temporary files. When BA is added, the number of file operations increases rapidly. In the implementation of a parallel program, usually one processor performs the role of master while others perform the workers. Who, when, and how to perform file operations becomes very important. In the ORNL code, the primary coders designed a routine called `SAFE_OPEN` to deal with file open operation in the parallel environment which is the critical portion to the file operation. However, in some places, ORNL code still uses regular “open” system call for opening a file. It has been challenging to study code written by a physicist without professional commenting.

Memory allocation and re-allocation is another big issue. Since we merged existing LM and GA algorithms to make BA, many variables, especially global array variables, with the same name are used in both the outer loop GA and inner loop LM had to be taken care of carefully with allocation and re-allocation handled properly. One of the direct results with improperly memory allocation is the program crashes.

Another big issue in parallel programming is debugging. There is essentially no good parallel debugger forcing us to use the debugger TotalView with limited success. Due to the properties of parallel implementation, the error we located by using print/write statement is not the actual location where the error occurs. The debugging issue we are

still facing originally was considered to be an MPI call issue. After a considerable amount of effort, we determined it is a filename extension handling issue.

### 3.4. Code Review

#### 3.4.1. Review 1: To handle BA temp filename properly.

##### Code Segment 1

<u>Line</u>	<u>Code</u>
0	<i>do 20 i=istart,maxgen+istart-1</i>
1	<i>!----added by S.Wang -----</i>
2	<i>!---Using fixed_seq_ext to store seq_ext at the first place-----</i>
3	<i>!---Since it is to be changed when calling LM in ga_evalout-----</i>
4	<i>if (i.eq. 1) then</i>
5	<i>fixed_seq_ext = seq_ext</i>
6	<i>end if</i>
	<i>!-----</i>
	<i>! other code ... ..</i>
55	<i>!-----added by S.Wang-----</i>
56	<i>!--getting original seq_ext back from fixed_seq_ext at end of</i>
56	<i>!--each generation -----</i>
58	<i>seq_ext = fixed_seq_ext</i>
59	<i>!-----</i>

The code segment 1 shown above which is selected from the subroutine GALM\_GRIVER illustrates the strategy that handles the BA temp filename properly.

Line 0 shows that  $i$  is the do-loop variable which represents the  $i$ th generation of population in the outer GA loop. Here we create a variable called `fixed_seq_ext` to store the initial filename extension (shown in line 5). Otherwise, LM and the inner loop of BA using the same variable `seq_ext` results in corruption of the value of `seq_ext`. This strategy avoids that error. Line 58 indicates that at the end of each generation, the program will send the initial filename extension value back to `seq_ext` from `fixed_seq_ext`.

**3.4.2. Review 2: The core functionality of BA, to insert inner loop, LM routine, into existed GA routine.**

**Code Segment 2**

<u>Line</u>	<u>Code</u>
0	<i>IF (NOPT_ALG .eq. 3) THEN</i>
1	<i>!-- Making a temp directory to store _opt files as _oga files-----</i>
2	<i>if (myid .eq. master) then</i>
3	<i>temp = 'mkdir tempdir1'</i>
4	<i>call system(temp)</i>
5	<i>end if</i>
6	<i>DO k=1,npopsiz</i>
7	<i>write (char_npopsiz,'(i5)') k</i>
8	<i>myoga_ext = trim(fixed_seq_ext)//'_oga'//</i>
9	<i>1 trim(adjustl(char_npopsiz))</i>
10	<i>myopt_ext = trim(fixed_seq_ext)//'_opt'//</i>

```

11      1      trim(adjustl(char_nposts))
12      input_file = 'input.//myopt_ext
13
14      !----- cp opt file to oga and tempdir1/oga
15      if (myid .eq. master) then
16      tempd = 'tempdir1'
17      ! ----Copy input.myopt_ext into input.myoga_ext-
18      temp = 'cp '//input_file//' '//input.//myoga_ext
19      call system(temp)
20      !-----Copy input.myopt_ext into tempdir1/input.myoga_ext
21      temp = 'cp '//input_file//' '//trim(tempd)//
22      1      '/input.//myoga_ext
23      call system(temp)
24      end if
25
26      oga_ext = myoga_ext
27      !-----run sub_optimize-----
28      call sub_optimize(myoga_ext)
29
30      if (myid .eq. master) then
31      open(3333)
32      read(3333,iostat=istat) funcval_breed
33      close(3333)

```

```

34          fitness(k) = funcval_breed
35      end if
36      !-----Copy input.oga..min files produced by LM into super directory
37      !---replace input.myopt_ext
39          temp = "cp " // "stellopt_ " // trim(seq_ext) // " // "
40          1      "input." // trim(seq_ext) // ".min" //
41          2      " " // "input." // trim(myopt_ext)
42          print *, temp
43          call system(temp)
44      !-----
45      !-- need to do before continue GA routine:
46      ! 1. replace input._optk by input...ogak.min
47          END DO
48          END IF ! end of (nopt_alg = 3)

```

The code segment 2 shown above is selected from the subroutine GA\_EVALOUT. The initial purpose of this subroutine is to evaluate the population, assign fitness, establish the best individual, and output information for the GA routine.

Per GA's structure, it creates a temporary input files for each individual for each generation. The GA\_EVALOUT subroutine then evaluates the population, assigns fitness, creates the best member, and outputs the information for the following calculation of next generation.

BA then chooses to insert the inner routine, LM, into GA by adding code segment 2 into GA\_EVALOUT routine.

In line 0, `nopt_alg = 3` indicates the BA algorithm.

In line 2 to line 5, program creates a temporary directory called `tempdir1` which stores those temporary input files with `_opt` extension generated by GA. Also, the duplicated of those `_opt`-extended files are also created as `_oga`-extended files.

Line 6 is the do-loop entry for each individual to implement LM routine.

The purpose of line 8 to line 11 is to avoid the name extension problem in a future computation. Therefore, program creates two temporary variables, `myopt_ext` and `myoga_ext`.

After all files and directory are setup, line 28 calls the LM routine. Instead of calling LM driver directly, we built a routine, `SUB_OPTIMIZE`, in the `STELLOPT` package. `SUB_OPTIMIZE` provides similar functionality to the `optimize` routine but is simpler because it only needs to direct the program to the LM routine. Since `SUB_OPTIMIZE` is in `STELLOPT` package, we define it as an external function.

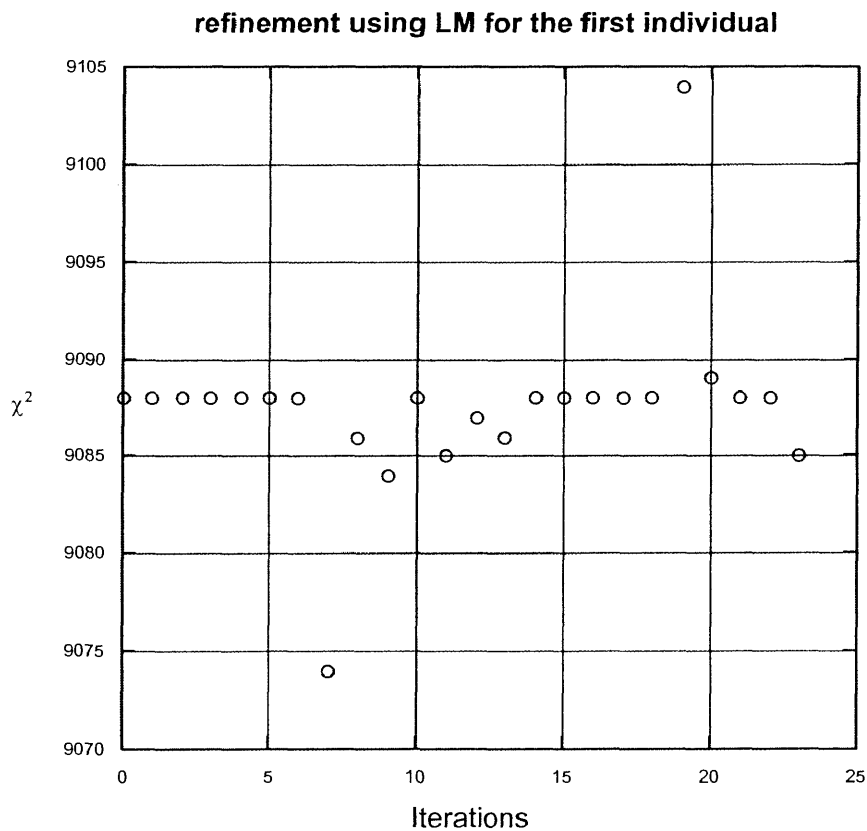
One purpose of the `GA_EVALOUT` routine to GA is to store fitness values to the fitness array. Since in BA we insert LM in `GA_EVALOUT`, the program needs to replace those old values in the fitness array with those new values generated by LM. Line 30 to 35 performs this function. There are two steps here. In the LM routine, the program writes those values into a temporary file called `fort.3333`, after returning from LM, the fitness array is populated with values from that file.

The last important feature of code segment 2 is to implement the replacement of those temporary input files with `_opt` extension with the input files generated by LM routine with `.min` extension. Line 38 to line 40 performs this functionality.

## 4. Comments to BA

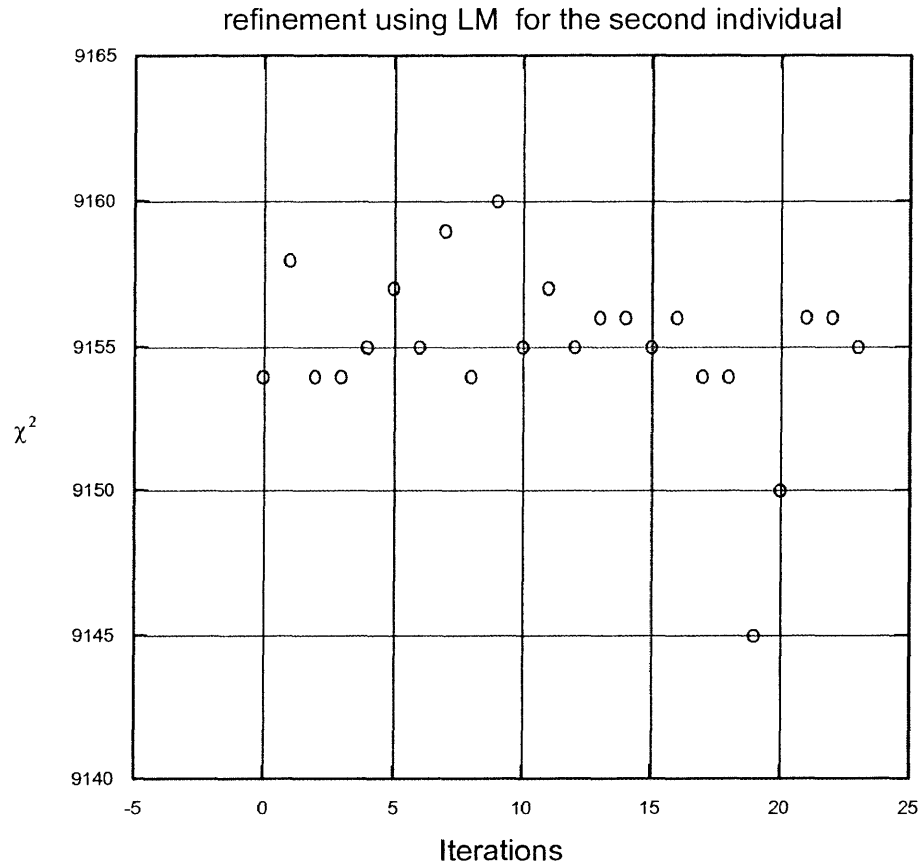
### 4.1. Initial results of BA

Though there is a bug existing for the BA, we still observe the improvement of BA when implementing LM routine that refines each individual in GA. Figure 8 and 9 indicate this improvement to a test case called SIMPLE. This case, we only use few generations, as well as a small population size. It is obvious that each time the  $\chi^2$  is getting improved for each individual.



**Figure 8. initial results of BA (1)**





**Figure 9. initial results of BA (2)**

#### 4.2. Advantages and disadvantages of BA search

Since BA combines GA with LM, the major advantages of BA are: (1) BA refines each individual in GA using LM's steepest descent search strategy which produces better offspring than only using pure GA. (2) BA avoids the local extremum to be considered as global extremum when LM encounters the surface of variables is not differentiable in first or/and second derivatives at some points (inflection points) because the evolutionary

optimization GA will produce some child points out of those inflection points which guarantees that BA can climb out of those local extremum points.

The major disadvantage of BA is that the implementation is more expensive at the computing time consuming point of view. When implementing BA under a parallel computation environment, it takes twice time as implementing LM or GA alone, roughly.

### **4.3. Existing issue and future work**

The challenges remaining in the development of BA are to deal with the memory allocation and file IO in a parallel environment. When using Totalview as the debugging tool, the existing unmatched array dimensions in the ORNL code cause unpredictable termination because unmatched array dimensions will cause memory allocation issues when assigned values between two unmatched arrays. Also, there is still a bug existing related to the file IO. We have been working to debug this issue for months.

In this work, we use MPI libraries as implementing LM, GA, and BA. As the future work, we may consider using Open MP libraries as the inner loop, LM, and MPI as the outer loop, GA for BA algorithm. This may reduce the complication and confliction when using MPI for both inner and outer loop for BA.

## 5. References

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- [5] “Stellarator Optimization: A Comparison of Genetic, Differential Evolution, and Levenberg-Marquadt Optimization Algorithms” 2003 International Sherwood Fusion Theory Conference, April 28-30, 2003, Corpus Christi, Texas. S. Wang, A.S. Ware, S.P. Hirshman & D.A. Spong
- [6] “A Breeder Algorithm for Stellarator Optimization” 45th Annual Meeting of the APS (American Physical Society) Division of Plasma Physics, October 27-31, 2003, Albuquerque, New Mexico. S. Wang, A.S. Ware, S.P. Hirshman & D.A. Spong
- [7] Hybridization of Differential Evolution for Aerodynamic Design, by T. Rogalsky [Department of Mathematics, University of Manitoba] and R. W. Derksen [Department of Mechanical and Industrial Engineering, University of Manitoba]
- [8] Genetic Algorithm and Optimizing Chemical Oxygen-Iodine Lasers, by David L. Carroll, Research Scientist, University of Illinois, Urbana, Illinois
- [9] Levenberg-Marquardt Method, by Carleton DeTar, Physics Department, University of Utah, Salt Lake City, UT

## 6. Appendix: Source Code

### 6.1 run\_optimizer.f

```
SUBROUTINE run_optimizer(xc_opt, var_descript,
1      nopt, nvar, lwa, info)
USE stel_kinds
USE optim, ONLY: home_dir, lone_step, lrestart
USE optim_params, ONLY: epsfcn, niter_opt, seq_ext,
1 num_processors, num_levmar_params, nopt_alg
USE vparams, ONLY: zero
USE mpi_params                                ! MPI
IMPLICIT NONE
C-----
C  D u m m y   A r g u m e n t s
C-----
INTEGER :: nopt, nvar, lwa
REAL(rprec), DIMENSION(nvar) :: xc_opt
CHARACTER(len=*), DIMENSION(nvar) :: var_descript      !description of independent variables
C-----
C  L o c a l   V a r i a b l e s
C-----
INTEGER, PARAMETER :: info_size = 33
CHARACTER(len=*), PARAMETER :: describe_string =
1  "DESCRIPTION OF INDEPENDENT VARIABLES",
2  stop_string = 'Allocation error in STELLOPT run-optimizer!'
INTEGER :: info, niter
INTEGER :: mode
REAL(rprec), DIMENSION(:), ALLOCATABLE :: fvec, diag
REAL(rprec) :: tol
CHARACTER*120, DIMENSION(1:info_size) :: info_array
C-----
C  E x t e r n a l   F u n c t i o n s
C-----
EXTERNAL lsfun1
C-----
data info_array/
1  'error in read_wout_opt opening wout file',
2  'error in load_physics_codes in system call',
3  'error opening indata file in write_indata',
4  'error opening output file in lsfun',
5  'error writing new input file in load_params',
6  'vmec2000 executable file not found',
7  'i/o error in clean_up routine',
8  'error reading wout file in call to read_wout_opt',
9  'allocation error in load_target',
a  'boozer array dimension mismatch in load_target',
b  'nvar and nopt do not match in load_target',
c  'i/o error opening cobra file in chisq_ballooning',
d  'i/o error opening bootstrap file in chisq_bootsj',
e  'i/o error in open_comm_files',
f  'error in chk_rzmnbn',
g  'boozer transform module - xbooz_xform - not found',
```

```

h 'could not locate executable in load_physics_codes',
i 'error reading output file in chisq_jinvar subroutine',
j 'error in external kink computation',
k 'error running xdkes code in chisq_dkes subroutine',
l 'error in vacuum vessel matching subroutine',
m 'system call to xcoilgeom failed in generate_mgrid',
n 'coils data file was not produced by xcoilgeom',
o 'error opening extcur file in generate_mgrid',
p 'error opening coil_targets file in chisq_coilgeom',
q 'error reading boozmn file in call to read_boozers_file',
r 'error opening neo code input file neo_in',
s 'trouble running eq3d in chisq_orbit',
t 'trouble running mkjmc in chisq_orbit',
u 'trouble running orbit in chisq_orbit',
v 'error opening orbsum in chisq_orbit',
w 'error opening ft79jmc in chisq_dsubr',

x 'error in chisq_vac_island'
z /

```

```

ALLOCATE (fvec(nopt), diag(nvar), stat = info)
IF (info .ne. 0) STOP stop_string

```

```

tol = 1.e-6_dp
mode = 1
niter = niter_opt
IF (lone_step) niter = 1

```

```

!
! print description of independent variables at top of screen
!

```

```

IF (myid .eq. master) THEN
  WRITE (6, '(60(=")/,a/,60(=")/,a)') describe_string,
1  'VAR# TYPE'
  DO info = 1, nvar
    WRITE(6, '(i5,2x,a)') info, var_descript(info)
  END DO
  WRITE (6, *)
END IF

```

```

IF(NOPT_ALG .eq. 0) THEN
  CALL lmdifl_mp (lsfun1, nopt, nvar, xc_opt, fvec, tol, epsfcn,
1  niter, diag, mode, info, lwa)
ELSE IF(NOPT_ALG .eq. 1) THEN
  CALL ga_driver (lsfun1, nopt, nvar, xc_opt, fvec, tol, epsfcn,
1  niter, num_processors, seq_ext, info, lwa, lrestart )

```

```

ELSE IF(NOPT_ALG .eq. 2) THEN
  CALL de_driver (lsfun1, nopt, nvar, xc_opt, fvec, tol, epsfcn,
1  niter, num_processors, seq_ext, info, lwa, lrestart )

```

```

ELSE IF(NOPT_ALG .eq. 3) THEN
  CALL galm_driver (lsfun1, nopt, nvar, xc_opt, fvec, tol,
1  epsfcn, niter, num_processors, seq_ext, info, lwa, lrestart)
  !! BREED: A new option
  !! BREED: A new option
  !! BREED: A new option

```

```
ELSE
  IF (myid.eq.master)
1   WRITE(6,*) "NOPT_ALG = ", NOPT_ALG, "; unable to proceed"
  STOP
ENDIF
DEALLOCATE (fvec, diag)

IF (myid.eq.master .and. info.lt.0) WRITE (*, '(/,1x,a,a)')
1  'Stellopt status: ',TRIM(info_array(-info))

END SUBROUTINE run_optimizer
```

## 6.2 galm\_driver.f

```

SUBROUTINE GALM_driver(fcn, n_opt, n_var, x, fvec, tol, eps, !! BREED: This is the Breed driver
  l_num_iter_opt, max_processors, filename, info, lwa, lrestart )
  USE ga_mod
  USE system_mod
  USE safe_open_mod
  USE mpi_params, ONLY: master, myid
  IMPLICIT NONE
  include 'mpif.h'          !mpi stuff
  INTEGER :: ierr
  INTEGER :: n_opt, n_var, info, lwa, num_iter_opt, max_processors
  REAL(rprec), DIMENSION(n_opt), TARGET :: fvec
  REAL(rprec), DIMENSION(n_var) :: x
  REAL(rprec), DIMENSION(n_var) :: partemp
  REAL(rprec) :: tol, eps, chi_sq, tmp          !ga_evaluate
  EXTERNAL fcn
  CHARACTER*(*) :: filename
  LOGICAL :: lrestart

  INTEGER :: num_iter_max
  INTEGER :: i, iflag, nfev

c *****
c entries for the 'ga' NAMELIST
c
c npopsiz - population size
c idum - if < 0, then |idum| is used as seed for random-number gen.
c pmutate - probability for random jump mutation
c pcross - crossover probability
c ielite - /=0 make sure best parent is preserved into decendent populations
c icreep - creep mutation flag: only do creep mutations if .ne. 0
c pcreep - probability for random creep mutation
c iuniform - =0 single point crossover at random chromosome point
c          /=0 uniform crossover
c iniche - /=0 turn on niching
c nichflg - array of flags for the free-parameters,
c          each non-zero entry enables niching for that free-parameter
c iskip
c iend
c nchild - default=1; if =2, then each crossover creates 2 children,
c          the second child having the second parents genes
c parmin - array specifying minimum value for each free-parameter,
c parmax - array specifying maximum value for each free-parameter,
c ibound - =1 then interpret parmin and parmax as scale-factors to be
c          multiplied by the initial guess values for each parameter
c nposibl
c nowrite - =0 then write output during optimization
c microga - =0 perform random mutations
c          /=0 perform micro-GA
c unique_ind
c itourny
c
c IMPORTANT: MPI_PARAMS MODULE MUST BE LOADED BY EXTERNAL CALLS
c TO MPI_COMM_RANK PRIOR TO THIS SUBROUTINE CALL
c *****
  info = 0
  num_iter_max = num_iter_opt

  itoumy=1
  maxgen=ngen
  kountmx=maxgen
  nparam=n_var
  num_obj = n_opt

  IF( ibound .eq. 1 ) THEN
    par_max(:n_var) = x(:n_var)*parmax(:n_var)
    par_min(:n_var) = x(:n_var)*parmin(:n_var)

```

```

WHERE (par_max(:n_var) < par_min(:n_var) )
  partemp(:n_var) = par_max(:n_var)
  par_max(:n_var) = par_min(:n_var)
  par_min(:n_var) = partemp(:n_var)
END WHERE

ELSE
  par_max = parmax
  par_min = parmin
END IF

IF (ALL(nposibl .eq. 0 )) nposibl=15

nfev=1
f_obj => fvec

! IF (myid .eq. master) WRITE(6, nml = ga_de)

irestrt = 0
IF( lrestart ) irestrt = 1
c
c store initial parameter values as a unique individual
parent = 0
child = 0
iparent = 0
ichild = 0
IF(unique_ind .gt. 0 ) THEN
  unique_ind=MIN(unique_ind, npopsiz)
  parent(1:nparam,unique_ind) = x(1:nparam)
END IF

CALL galm_sp(fcn, n_opt, fvec, chi_sq, filename, nfev,    !! BREED: Calling galm_sp
> iflag, max_processors, myid)                !! BREED: Calling galm_sp

IF (myid .eq. master) THEN
  WRITE(6,*) "final solution: "
  WRITE(6,*) "best individual : ", jbest
  WRITE(6,*) "x ", (parent(i,jbest),i=1,nparam)
c  WRITE(6,*) "fvec ",(fvec(i),i=1,n_opt)
  WRITE(6,*) "y ", chi_sq
END IF

x(1:n_var) = parent(1:n_var,jbest)

iflag=-100
CALL fcn(n_opt, npopsiz, parent(1,jbest), fvec, iflag, nfev)

END SUBROUTINE GALM_driver                !! BREED: End of Breed driver

```



### 6.3 galm\_sp.f

```

SUBROUTINE galm_sp(fcn, nopt, fvec, best, filename, nfev, iflag, !! BREED: Start of galm_sp
  l      max_num_processors, myid)
  USE ga_mod
  USE safe_open_mod
  USE mpi_params, ONLY: master
  USE optim_params, ONLY: fixed_seq_ext, seq_ext      !! BREED: *DANGER* Using optim_params in library
  IMPLICIT NONE
  include 'mpif.h'          !mpi stuff
  EXTERNAL fcn

  INTEGER :: nopt
  REAL(rprec), DIMENSION(nopt) :: fvec

  INTEGER :: kount, npossum, ig2sum, istart, istore
  INTEGER :: ncross, ipick, mate1, mate2, istat
  INTEGER :: i, j, nfev, iflag, max_num_processors, myid
  REAL(rprec) :: fbar, best, evals
  CHARACTER*(*) :: filename
  CHARACTER*(len_trim(filename)+10) :: temp
  SAVE

c
c  CALL input
c
c  Perform necessary initialization and read the ga.restart file.
  CALL ga_initial(istart, npossum, ig2sum, filename, myid)
c
c  $$$$$ Main generational processing loop. $$$$$
  kount=0
  nfit_eval=nfev
  istore=0
  iunit_ga_out = 24
  IF (myid .eq. master) THEN
    temp = "ga_out." // filename
    CALL safe_open(iunit_ga_out, istat, TRIM(temp),
  l      'unknown', 'formatted')
  END IF

  DO 20 i=istart,maxgen+istart-1
    IF (i .eq. 1) THEN          !! BREED: Using fixed_seq_ext to store seq_ext
      fixed_seq_ext = seq_ext    !! BREED: since seq_ext will be changed when
    END IF                    !! BREED: calling LM in ga_evalout
    iflag=-1
    IF (myid .eq. master) THEN
      WRITE (6,1111) i
      WRITE (iunit_ga_out,1111) i
    c
c  Evaluate the population, assign fitness, establish the best
c  individual, and write output information.
      WRITE(6,*) 'pre ga_evalout', max_num_processors
      WRITE(6,*) fbar,best,nopt,nfev,max_num_processors,iflag
      END IF
      CALL ga_evalout(fbar, best, fcn, nopt, fvec, nfev,      !! BREED: Added filename
  >      max_num_processors, iflag, myid, filename)        !! BREED: to ga_evalout call
      istore=istore+1
      geni(istore) = REAL(i, kind=rprec)
      genavg(istore)=fbar
      genmax(istore)=best
      IF (npopsiz.eq.1 .or. iskip.ne.0) THEN
        IF (myid .eq. master) CLOSE(iunit_ga_out)
        CALL ga_restart(i,istart,kount,filename, myid)
        RETURN
      END IF
    c
c  niching
    IF (iniche.ne.0) CALL ga_niche(myid)
  c

```

```

c selection, crossover and mutation
  ncross=0
  ipick=npopsiz
  DO 45 j=1,npopsiz,nchild
c
c Perform selection.
  CALL ga_selectn(ipick,j,mate1,mate2)
c
c Now perform crossover between the randomly selected pair.
  CALL crossovr(ncross,j,mate1,mate2)
45  CONTINUE

  IF (myid .eq. master) THEN
    WRITE(6,1225) ncross
    WRITE(iunit_ga_out,1225) ncross
  END IF
c
c Now perform random mutations. If running micro-GA, skip mutation.
  IF (microga.eq.0) CALL ga_mutate (myid)
c
c Write child array back into parent array for new generation. Check
c to see IF the best parent was replicated.
  CALL ga_newgen(npossum,ig2sum,myid)
c
c Implement micro-GA IF enabled.
  IF (microga.ne.0) CALL ga_micro(i,npossum,ig2sum,myid)
c
c Write to restart file.
  CALL ga_restart(i,istart,kount,filename,myid)
  seq_ext = fixed_seq_ext          !! BREED: Setting seq_ext back to the original value
20  CONTINUE

c $$$$$ End of main generational processing loop. $$$$$

  IF (myid .eq. master) THEN
    WRITE(iunit_ga_out,3000)
    DO 100 i=1,maxgen
      evals = npopsiz*geni(i)
      WRITE(iunit_ga_out,3100) geni(i),evals,genavg(i),genmax(i)
100  CONTINUE
    CLOSE (iunit_ga_out)
  END IF

1050 FORMAT(1x,' Binary Code',16x,'Parameter Values and Fitness')
1111 FORMAT(//,'##### Generation',i5,
1 ' #####')
1225 FORMAT(/' Number of Crossovers   =',i5)
3000 FORMAT(2x//'Summary of Output'/
+ 2x,'Generation Evaluations Avg.Fitness Best Fitness')
3100 FORMAT(2x,3(e10.4,4x),e11.5)

  END SUBROUTINE galm_sp          !! BREED: End of galm_sp

```

## 6.4 ga\_evalout.f

```

SUBROUTINE ga_evalout(fbar, best, fcn, nopt, fvec, nfev, !! BREED: filename added to
> num_processors, iflag, myid, filename) !! BREED: argument list of ga_evalout
c#####
c
c this subroutine evaluates the population, assigns fitness,
c establishes the best individual, and outputs information.
  USE optim_params, ONLY: opt_ext, oga_ext, seq_ext, nopt_alg, !! BREED: *DANGER* Using optim_params
  l fixed_seq_ext, funcval_breed !! BREED: *DANGER* in ga_evalout
  USE ga_mod
  USE system_mod !! BREED: ga_evalout now uses system calls
  USE mpi_params, ONLY: master
  IMPLICIT NONE
  EXTERNAL fcn, sub_optimize !! BREED: New external sub_optimize
  INTEGER :: nopt, n, j, k, kk, iflag, myid
  REAL(rprec), DIMENSION(nopt) :: fvec
  REAL(rprec), DIMENSION(npamax) :: paramsm,paramav
  INTEGER :: nfev, num_processors
  REAL(rprec) :: fitsum, funcval, fbar, best
  INTEGER :: jstart, jend, istat, jstat
  LOGICAL :: ldiag_opt
  CHARACTER(5) :: char_npopsiz !! BREED: Added character variable char_npopsiz
  CHARACTER(10) :: tempd !! BREED: Added character variable tempd
  CHARACTER(60) :: temp_seq_ext, temp_oga_ext, temp_opt_ext !! BREED: Added temp character variables
  CHARACTER(*) :: filename !! BREED: Added character variable filename
  CHARACTER*(len_trim(filename)+12) :: input_file !! BREED: Added character variable input_file
  CHARACTER*(100) :: temp !! BREED: Added character variable temp
  CHARACTER*(100) :: myopt_ext, myoga_ext !! BREED: Added character variables myopt_ext, myoga_ext

  SAVE
c
c
  fitsum = 0
  best=-1.0e30_dp

  ldiag_opt = .false.

  IF (myid .eq. master) WRITE(6,*) 'in ga_evalout',num_processors
  IF (myid .eq. master) WRITE(6,*) fbar,best,nopt,nfev,iflag

  DO 29 n=1,npamax
    paramsm(n)=0
29 CONTINUE
  jstart=1
  jend=npopsiz
  IF(iskip.ne.0) jstart=iskip
  IF(iend.ne.0) jend=iend
c
  DO j=jstart,jend

    CALL ga_decode(j,parent,iparent)

    IF(LDIAG_OPT .and. myid.eq.master) THEN
      IF(nchrome .le. 120) THEN
        WRITE(iunit_ga_out,1075) j,(iparent(k,j),k=1,nchrome)
      ELSE
        WRITE(iunit_ga_out,1075) j,(iparent(k,j),k=1,120)
        WRITE(iunit_ga_out,1077) (iparent(k,j),k=121,nchrome)
      END IF
      WRITE(iunit_ga_out,1076) (parent(kk,j),kk=1,npamax)
    END IF
  END DO
  CALL ga_fitness_mpi (jend-jstart+1, f_obj, num_obj,
  l fcn, nfev, fitness)
  nfev=nfev+jend-jstart+1
  nfit_eval=nfev

```

```

IF (NOPT_ALG .eq. 3) THEN
    !! BREED: File manipulation in Breed
    IF (myid .eq. master) THEN
        !! BREED: Only the master makes directories
        temp = 'mkdir tempdir1'
        !! BREED: Stores _opt files as _oga files
        CALL system(temp)
        !! BREED: Making the directory here
    END IF
    !! BREED: The master loop is done
    DO k=1,npopsiz
        !! BREED: Starting loop over the population members
        write(char_npopsiz,(i5)' k
        !! BREED: Writing the population member # to an integer
        myoga_ext = trim(fixed_seq_ext)['_oga']
        !! BREED: Set up local variable myoga_ext
    1   trim(adjustl(char_npopsiz))
        !! BREED: using fixed_seq_ext and member #
        myopt_ext = trim(fixed_seq_ext)['_opt']
        !! BREED: Set up local variable myopt_ext
    1   trim(adjustl(char_npopsiz))
        !! BREED: using fixed_seq_ext and member #
        input_file = 'input.'//myopt_ext
        !! BREED: Avoiding using global variable opt_ext
        !! BREED
        IF (myid .eq. master) THEN
            !! BREED: Only the master copies files
            tempd = 'tempdir1'
            !! BREED: Define the temp directory name
            temp = 'cp '//input_file/' '//input.'//myoga_ext
            !! BREED: Storing the input_file in the file input.myoga_ext
            CALL system(temp)
            !! BREED: Make it so
            temp = 'cp '//input_file/' '//trim(tempd)
            !! BREED: Make a copy in the temp
    I   '/input.'//myoga_ext
            !! BREED: directory as well. Why?
            CALL system(temp)
            !! BREED: Make it so
        END IF
        !! BREED: Done with the master loop
        oga_ext = myoga_ext
        !! BREED: TESTING-----08302004
        CALL sub_optimize(myoga_ext)
        !! BREED: *DANGER* library calling sub_optimize
        !! BREED
        IF (myid .eq. master) THEN
            !! BREED: Only the master stores the funcval
            open(3333)
            !! BREED: from file 3333 (written in sub_optimize)
            read(3333,iostat=istat) funcval_breed
            !! BREED: Read in the value
            close(3333)
            !! BREED: Close the fort.3333 file
            fitness(k) = funcval_breed
            !! BREED: Store this value in the fitness array
        END IF
        !! BREED: Done with the master loop
        temp = "cp " //_"stellopt_"//trim(seq_ext)['_']
        !! BREED: Copy the .min oga files back to the main directory
    1   "input."//trim(seq_ext)['_min']
        !! BREED: the main directory but with a different
    2   " " //_"input."//trim(myopt_ext)
        !! BREED: extensiuon, the myopt_ext
        CALL system(temp)
        !! BREED: Make it so
    !! BREED
    !! BREED: need to do before continue GA routine:
    !! BREED: 1. replace input_optk by input...ogak.min
    !! BREED: 2. clean tempdir
    !! BREED
    END DO
    !! BREED: End of the loop over the population
    !! BREED
    !! BREED: A couple of questions here:
    !! BREED: 1. only consider these input_opt files?
    !! BREED: 2. for using each LM routine, when doing clean up operation
    !! BREED: whether it impact other input_opt(oga) files or not?
    !! BREED
    END IF
    !! BREED: End of Breed file loop

!   Clean up...
iflag=-100
CALL fcn(nopt, npopsiz, parent(1,jbest), fvec, iflag, nfev)
IF (NOPT_ALG .eq. 3) THEN
    !! BREED: Clean up for Breed
    IF (myid .eq. master) THEN
        !! BREED: Only the master removes the temp directory
        temp = 'rm -rf '//trim(tempd)
        !! BREED: Remove the temp directory
        CALL system(temp)
        !! BREED: Make it so
    END IF
    !! BREED: Done with the master loop
END IF
!! BREED: Done with clean up for Breed
DO j = jstart, jend
    fitsum=fitsum+fitness(j)
    DO n=1,nparam
        paramsm(n)=paramsm(n)+parent(n,j)
    END DO
c
c Check to see IF fitness of individual j is the best fitness.
IF (fitness(j).gt.best) THEN
    best=fitness(j)
    jbest=j
    DO k=1,nchrome
        ibest(k)=iparent(k,j)
    END DO

```

```

        END IF
    END DO

c compute parameter and fitness averages.
    fbar=fitsum/npopsiz
    DO n=1,nparam
        paramav(n)=paramsm(n)/npopsiz
    END DO

c
c write output information
    IF (myid.eq.master) THEN
        IF (ldiag_opt) THEN
            IF (npopsiz.eq.1) THEN
                IF (nchrome .le. 120) THEN
                    WRITE(iunit_ga_out,1075) 1,(iparent(k,1),k=1,nchrome)
                ELSE
                    WRITE(iunit_ga_out,1075) 1,(iparent(k,1),k=1,120)
                    WRITE(iunit_ga_out,1077) (iparent(k,j),k=121,nchrome)
                END IF
                WRITE(iunit_ga_out,1076) (parent(k,1),k=1,nparam)
                WRITE(iunit_ga_out,1078) fitness(1)
                WRITE(iunit_ga_out,*) ' Average Values:'
                WRITE(iunit_ga_out,1275) (parent(k,1),k=1,nparam)
                WRITE(iunit_ga_out,1276) fbar
            ELSE
                WRITE(iunit_ga_out,1275) (paramav(k),k=1,nparam)
                WRITE(iunit_ga_out,1276) (fitness(j),j=1,npopsiz)
            END IF
        END IF
        WRITE(6,1100) fbar
        WRITE(iunit_ga_out,1100) fbar
        WRITE(6,1200) best
        WRITE(iunit_ga_out,1200) best
    END IF

1075 FORMAT(i3,1x,(120i1))
1077 FORMAT(3x,1x,(120i1))
1076 FORMAT(3x,1x,10(1x,e10.4))
1078 FORMAT(10x,e12.5)
1100 FORMAT(1x,'Average Function Value of Generation=',e12.5)
1200 FORMAT(1x,'Maximum Function Value      =',e12.5/)
1275 FORMAT(/' Average Values:',18x,10(1x,e10.4))
1276 FORMAT(10x,10e12.5)

    END SUBROUTINE ga_evalout

```