

# Simulation of polarimetric radar variables in rain at S-, C- and X-band wavelengths

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**Abstract.** Polarimetric radar variables of rainfall events, like differential reflectivity  $Z_{DR}$ , or specific differential phase  $K_{DP}$ , are better suited for estimating rain rate  $R$  than just the reflectivity factor for horizontally polarized waves,  $Z_H$ . A variety of physical and empirical approaches exist to estimate the rain rate from polarimetric radar observables. The relationships vary over a wide range with the location and the weather conditions.

In this study, the polarimetric radar variables were simulated for S-, C- and X-band wavelengths in order to establish radar rainfall estimators for the alpine region of the form  $R(K_{DP})$ ,  $R(Z_H, Z_{DR})$ , and  $R(K_{DP}, Z_{DR})$ . For the simulation drop size distributions of hundreds of 1-minute-rain episodes were obtained from 2D-Video-Distrometer measurements in the mountains of Styria, Austria. The sensitivity of the polarimetric variables to temperature is investigated, as well as the influence of different rain drop shape models – including recently published ones – on radar rainfall estimators. Finally it is shown how the polarimetric radar variables change with the elevation angle of the radar antenna.

## 1 Introduction

In polarimetric weather radar systems, relationships of the form  $R(K_{DP})$ ,  $R(Z_H, Z_{DR})$ , and  $R(K_{DP}, Z_{DR})$  are generally used to estimate the rain fall rate  $R$ . A wide range of relationships exist (e.g. Aydin and Giridhar, 1992; May et al., 1999; Keenan et al., 2001). The main reason for the wide range of relationships is the drop-size distribution. The drop-size distribution depends on the type of rain event and as a consequence on the geographical region. Also a variety of rain drop shape models exists and so the underlying rain drop

shape model has an influence on the determined rainfall algorithm as well (Matrosov et al., 2002).

At C-band also the temperature can have influence on the polarimetric rainfall estimation algorithms; for example, at 5 cm wavelength resonance occurs for sizes larger than about 5 mm diameter, and therefore several polarimetric observables exhibit non-monotonous dependence on the drop diameter (Zrnić et al., 2000). At C-band also a considerable temperature dependence of polarimetric observables can be observed, as described in Sect. 5. At X-band, resonance occurs for sizes around 4 mm but the temperature dependence is not significant.

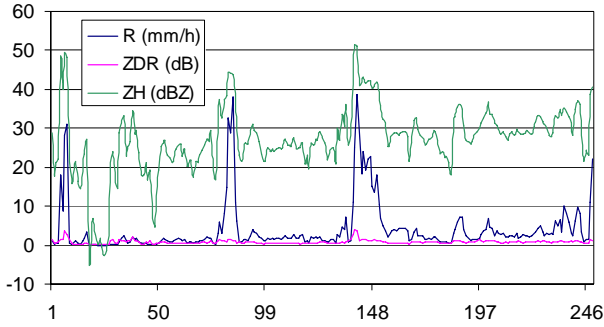
In the present study, the polarimetric radar observables  $Z_H$ ,  $Z_{DR}$ , and  $K_{DP}$  were calculated for 249 1-minute-rain episodes, observed with an imaging distrometer, the 2D-Video-Distrometer (Schönhuber et al., 1994), in the mountains of Styria, Austria.

## 2 Data

The raindrop-size distribution measurements were obtained from the 2D-Video-Distrometer positioned at Mt. Präbichl in the Province of Styria, Austria. The 2D-Video-Distrometer records front- and side-view as well as the time stamp of raindrops falling through its sensing area. The water volume of each rain drop and its equivolumetric sphere diameter is calculated from the recorded front- and side-view. The rain rate is determined from all particles that were falling through the effective measuring area in a certain integration time interval. The detailed algorithm is described in Schönhuber (1998). For this study 249 rain events were observed (Fig. 1). The analyzed data were recorded during convective and stratiform rainfall events in the years 2000 and 2001. The drop-size distribution was discretized in 0.25 mm steps of the equivolumetric sphere diameter  $D_{eq}$ , and averages over 1 min have been considered.



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**Fig. 1.** Rain rate  $R$ , reflectivity factor  $Z_H$  and differential reflectivity  $Z_{DR}$  as measured with the 2DVD for 249 rain episodes of 1 minute each. In this plot  $Z_H$  and  $Z_{DR}$  are determined for 5.625 GHz, 10°C, and assuming Pruppacher-Beard raindrop shapes.

### 3 Methodology

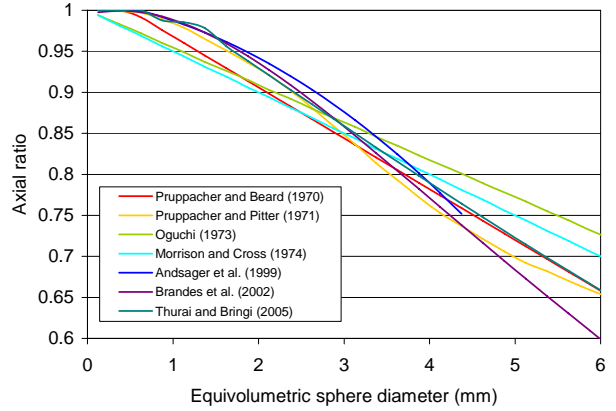
The forward- and backward-scattering amplitudes of single raindrops were calculated with the ESA point matching program (Poiaraes Baptista, 1994). It uses the point matching algorithm of Morrison and Cross (1974). The radar rain rate estimation algorithms of the form  $R(K_{DP})$ ,  $R(Z_H, Z_{DR})$  and  $R(K_{DP}, Z_{DR})$  were established for S-, C- and X-band wavelengths by regression analyses, between the rain rate measured by the 2DVD and the calculated polarimetric radar variables for 249 1-minute-rain episodes, observed with the 2D-Video-Distrometer. In this study, the polarimetric variables  $K_{DP}$ ,  $Z_H$  and  $Z_{DR}$  were calculated with following formulas:

$$K_{DP} = (180 \cdot 10^3) \frac{\lambda}{\pi} \cdot \text{Re}$$

$$\int_{D=0}^{D_{\max}} [f_{hh}(D) - f_{vv}(D)] \cdot N(D) \cdot dD \quad (^\circ\text{km}^{-1}) \quad (1)$$

$$Z_H = \frac{4 \cdot 10^{18} \cdot \lambda^4}{\pi^4 \cdot |K_0^2| \cdot k^2} \int_{D=0}^{D_{\max}} |s_{hh}(D)|^2 \cdot N(D) \cdot dD \quad (\text{mm}^6 \text{ m}^{-3}) \quad (2)$$

$$Z_{DR} = \frac{\int_{D=0}^{D_{\max}} |s_{hh}(D)|^2 \cdot N(D) \cdot dD}{\int_{D=0}^{D_{\max}} |s_{vv}(D)|^2 \cdot N(D) \cdot dD} \quad (3)$$



**Fig. 2.** Summary of several rain drop shape models showing the axial ratio of the drops as a function of the equivolumetric sphere diameter.

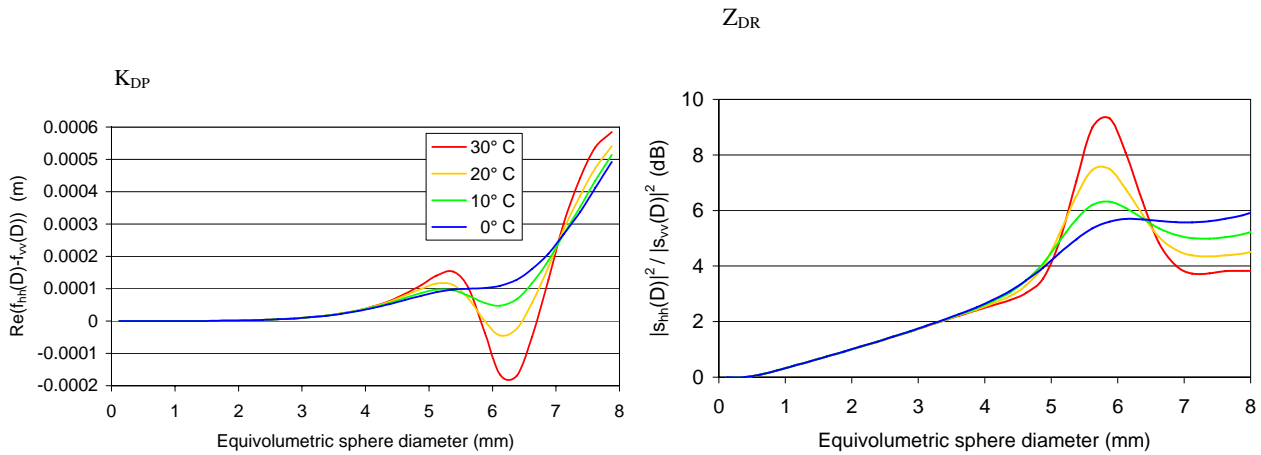
where

$\lambda$	wavelength (m)
$k$	propagation constant ( $2\pi/\lambda$ ) ( $\text{m}^{-1}$ )
$ K_0^2 $	material parameter, 0.931 for water
$N(D)$	drop-size distribution ( $\text{mm}^{-1} \text{m}^{-3}$ )
$D$	drop diameter (mm)
$D_{\max}$	maximum drop diameter (mm)
$\text{Re}$	takes the real part of the integral
$f_{hh}, f_{vv}$	forward-scattering amplitudes for horizontally and vertically polarized waves (m)
$s_{hh}, s_{vv}$	backward-scattering amplitudes for horizontally and vertically polarized waves (m)

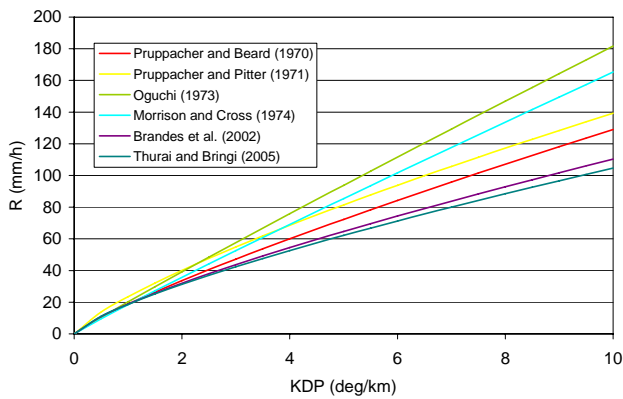
The forward and backward scattering amplitudes were calculated for 10°C raindrop temperature. The effect of temperatures between 0 and 30°C is also discussed. The complex relative dielectric permittivity  $\varepsilon$  of water was determined from Ray (1972). The calculations were carried out at S-band (2.8 GHz frequency/10.7 cm wavelength), C-band (5.625 GHz/5.3 cm) and at X-band (9.6 GHz/3.1 cm).

### 4 Raindrop shape models

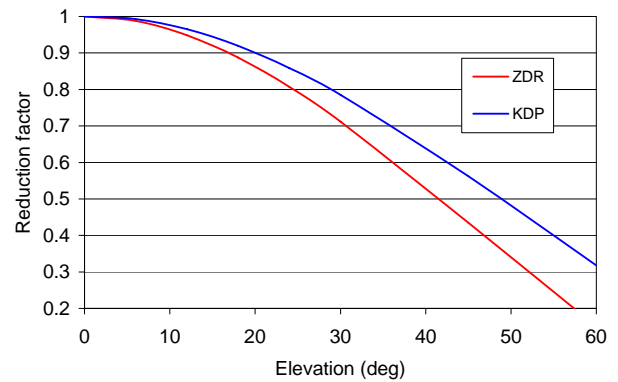
The polarimetric variables are sensitive to the shape of the raindrops. In recent decades, a variety of different raindrop shape models were published and the research is still ongoing. Many of these models describe the full contour of the drops as a function of the equivolumetric sphere diameter. However, for practical applications the full contour shapes are often approximated by oblate spheroids with the same



**Fig. 3.**  $K_{DP}$  and  $Z_{DR}$  as a function of equivolumetric sphere diameter of the raindrop, and temperature (at 5.3 cm wavelength).



**Fig. 4.** Comparison of the different  $R(K_{DP})$  relationships at C-band.



**Fig. 5.** Reduction factor for  $K_{DP}$  and  $Z_{DR}$  with increasing elevation angle for Pruppacher-Beard rain drop shapes averaged over all observed drop-size distributions.

axial ratio. Figure 2 summarizes axial ratio relations of several models.

Polarimetric variables calculated from oblate spheroid approximations in general agree well with non-oblate shape models with equivalent axial ratio. Thurai et al. (2007) found noticeable deviation only within the resonance region for equivolumetric sphere diameters in the 5.5–7 mm range at C-band frequency. Since in our data only in two out of 249 different drop spectra rain drops in that range occurred, raindrops were also approximated by oblate spheroids.

**5 Effect of raindrop temperature on  $K_{DP}$  and  $Z_{DR}$**

The effect of drop temperature on polarimetric radar variables has been studied e.g. by Bringi and Chandrasekhar (2001) and by Keenan et al. (2001). At S-band, effects of temperature on  $K_{DP}$  and  $Z_{DR}$  are rather small. At

C-band, however, effects of temperature are no longer negligible.

For equivolumetric sphere diameters up to 4 mm the temperature has no effect on  $K_{DP}$  and  $Z_{DR}$  while for bigger ones the effect can be significant as shown in Fig. 3. E.g. for 6 mm raindrops  $Re(f_{hh} - f_{vv})$  turns negative at 20°C. This means that  $K_{DP}$  for a rain volume containing 6 mm drops can be less than the same volume without these drops.

This resonance effect occurs also for  $Z_{DR}$  and makes its use ambiguous at C-band frequency and around 6 mm drop diameter. Since in the analyzed distrometer data, 6 mm raindrops occurred only sporadically, no significant variation in the  $R - K_{DP}$  relationship was observed at higher temperatures.

At X-band, the effect of the temperature is rather small. The resonance region resides just below 4 mm drop diameter and is not very pronounced.

**Table 1.** S-band rain rate estimation algorithms for different raindrop-shape models at 10°C. OG refers to Oguchi (1973), M&C refers to Morrison and Cross (1974), P&B refers Pruppacher and Beard (1970), P&P refers to Pruppacher and Pitter (1971). Units:  $R$  in  $\text{mm h}^{-1}$ ,  $K_{\text{DP}}$  in  $^{\circ}\text{km}^{-1}$ ,  $Z_{\text{H}}$  in  $\text{mm}^6 \text{m}^{-3}$ ,  $Z_{\text{DR}}$  in dB.

S-band (2.8 GHz); $\epsilon_r=80.2346-j17.1513$			
Shape model	$R(K_{\text{DP}})$ algorithm	$R(K_{\text{DP}}, Z_{\text{DR}})$ algorithm	$R(Z_{\text{H}}, Z_{\text{DR}})$ algorithm
OG	$R=41.14 K_{\text{DP}}^{0.959}$	$R=51.9 K_{\text{DP}}^{0.98} 10^{-0.082Z_{\text{DR}}}$	$R=0.024 Z_{\text{H}}^{0.90} 10^{-0.769Z_{\text{DR}}}$
M&C	$R=37.51 K_{\text{DP}}^{0.959}$	$R=47.4 K_{\text{DP}}^{0.98} 10^{-0.076Z_{\text{DR}}}$	$R=0.024 Z_{\text{H}}^{0.90} 10^{-0.695Z_{\text{DR}}}$
P&B	$R=35.33 K_{\text{DP}}^{0.842}$	$R=61.9 K_{\text{DP}}^{0.91} 10^{-0.176Z_{\text{DR}}}$	$R=0.017 Z_{\text{H}}^{0.90} 10^{-0.565Z_{\text{DR}}}$
P&P	$R=42.28 K_{\text{DP}}^{0.779}$	$R=86.4 K_{\text{DP}}^{0.87} 10^{-0.263Z_{\text{DR}}}$	$R=0.015 Z_{\text{H}}^{0.87} 10^{-0.535Z_{\text{DR}}}$

**Table 2.** C-band rain rate estimation algorithms for different raindrop-shape models at 10°C. OG refers to Oguchi (1973), M&C refers to Morrison and Cross (1974), P&B refers Pruppacher and Beard (1970), P&P refers to Pruppacher and Pitter (1971), BR refers to Brandes et al. (2002), T&B refers to Thurai and Bringi (2005). Units:  $R$  in  $\text{mm h}^{-1}$ ,  $K_{\text{DP}}$  in  $^{\circ}\text{km}^{-1}$ ,  $Z_{\text{H}}$  in  $\text{mm}^6 \text{m}^{-3}$ ,  $Z_{\text{DR}}$  in dB.

C-band (5.625 GHz); $\epsilon_r=70.46-j29.82$			
Shape model	$R(K_{\text{DP}})$ algorithm	$R(K_{\text{DP}}, Z_{\text{DR}})$ algorithm	$R(Z_{\text{H}}, Z_{\text{DR}})$ algorithm
OG	$R=20.24 K_{\text{DP}}^{0.953}$	$R=25.9 K_{\text{DP}}^{0.98} 10^{-0.090Z_{\text{DR}}}$	$R=0.022 Z_{\text{H}}^{0.86} 10^{-0.538Z_{\text{DR}}}$
M&C	$R=18.46 K_{\text{DP}}^{0.952}$	$R=23.6 K_{\text{DP}}^{0.98} 10^{-0.082Z_{\text{DR}}}$	$R=0.021 Z_{\text{H}}^{0.86} 10^{-0.483Z_{\text{DR}}}$
P&B	$R=18.87 K_{\text{DP}}^{0.835}$	$R=29.1 K_{\text{DP}}^{0.90} 10^{-0.142Z_{\text{DR}}}$	$R=0.017 Z_{\text{H}}^{0.86} 10^{-0.399Z_{\text{DR}}}$
P&P	$R=23.49 K_{\text{DP}}^{0.773}$	$R=39.4 K_{\text{DP}}^{0.85} 10^{-0.197Z_{\text{DR}}}$	$R=0.015 Z_{\text{H}}^{0.84} 10^{-0.377Z_{\text{DR}}}$
BR	$R=18.77 K_{\text{DP}}^{0.769}$	$R=22.4 K_{\text{DP}}^{0.77} 10^{-0.072Z_{\text{DR}}}$	$R=0.015 Z_{\text{H}}^{0.82} 10^{-0.290Z_{\text{DR}}}$
T&B	$R=18.60 K_{\text{DP}}^{0.750}$	$R=24.4 K_{\text{DP}}^{0.71} 10^{-0.048Z_{\text{DR}}}$	$R=0.016 Z_{\text{H}}^{0.82} 10^{-0.330Z_{\text{DR}}}$

**6 Effect of raindrop shape models on radar rainfall estimation algorithms**

Tables 1–3 summarize how different underlying rain drop shape models alter different radar rainfall estimation algorithms. The relationships were established in the same form as in Bringi and Chandrasekhar (2001). The results in this study are comparable to their findings when the different signal frequencies are taken in consideration. The results show that  $R(K_{\text{DP}})$  algorithms are most affected by the used raindrop shape model. The estimated rain rate can vary significantly as seen in Fig. 4. For a maximum  $K_{\text{DP}}$  value in rain of 10 deg/km (Doviak and Zrnić, 1993), the C-band  $R(K_{\text{DP}})$  algorithm reports a rain rate of 180 mm/h, when assuming the drop shape model of Oguchi (1973) in contrast to only 100 mm/h when assuming the model of Thurai and Bringi (2005).  $R(K_{\text{DP}}, Z_{\text{DR}})$  algorithms are less affected than  $R(K_{\text{DP}})$  esti-

mators;  $R(Z_{\text{H}}, Z_{\text{DR}})$  algorithms are most robust to the axial ratio of the raindrops. The lowest rain rates arise when using the model of Pruppacher and Pitter (1971) or that of Brandes et al. (2002), the highest occur with the model of Pruppacher and Beard (1970).

**7 Effect of the elevation angle on  $K_{\text{DP}}$  and  $Z_{\text{DR}}$**

The previous simulations were carried out assuming a radar beam parallel to the earth’s surface. Below it is shown what effect elevation angles  $>0^{\circ}$  on the radar rainfall estimation algorithms have. For these simulations raindrop shapes according to Pruppacher and Beard (1970) were taken. With increasing elevation angle,  $K_{\text{DP}}$  and  $Z_{\text{DR}}$  decrease, because the raindrop shape seen by the radar becomes more spherical. Their decrease with increasing elevation is shown in Fig. 5.

**Table 3.** X-band rain rate estimation algorithms for different raindrop-shape models at 10°C. OG refers to Oguchi (1973), M&C refers to Morrison and Cross (1974), P&B refers Pruppacher and Beard , P&P refers to Pruppacher and Pitter (1971). Units:  $R$  in  $\text{mm h}^{-1}$ ,  $K_{\text{DP}}$  in  $^{\circ}\text{km}^{-1}$ ,  $Z_{\text{H}}$  in  $\text{mm}^6 \text{m}^{-3}$ ,  $Z_{\text{DR}}$  in dB.

X-band (9.6 GHz); $\epsilon_r=54.29-j38.17$			
Shape model	$R(K_{\text{DP}})$ algorithm	$R(K_{\text{DP}}, Z_{\text{DR}})$ algorithm	$R(Z_{\text{H}}, Z_{\text{DR}})$ algorithm
OG	$R=11.91 K_{\text{DP}}^{0.953}$	$R=14.5 K_{\text{DP}}^{0.98} 10^{-0.074Z_{\text{DR}}}$	$R=0.023 Z_{\text{H}}^{0.91} 10^{-0.715Z_{\text{DR}}}$
M&C	$R=10.88 K_{\text{DP}}^{0.953}$	$R=13.2 K_{\text{DP}}^{0.98} 10^{-0.066Z_{\text{DR}}}$	$R=0.023 Z_{\text{H}}^{0.91} 10^{-0.646Z_{\text{DR}}}$
P&B	$R=11.84 K_{\text{DP}}^{0.836}$	$R=17.7 K_{\text{DP}}^{0.90} 10^{-0.135Z_{\text{DR}}}$	$R=0.016 Z_{\text{H}}^{0.91} 10^{-0.536Z_{\text{DR}}}$
P&P	$R=15.30 K_{\text{DP}}^{0.774}$	$R=25.11 K_{\text{DP}}^{0.85} 10^{-0.192Z_{\text{DR}}}$	$R=0.014 Z_{\text{H}}^{0.88} 10^{-0.508Z_{\text{DR}}}$

**Table 4.** C-band radar rain rate estimation algorithms for different elevation angles, for Pruppacher-Beard raindrop shapes and 10°C raindrop temperature.

C-band (5.625 GHz)			
Elevation angle	$R(K_{\text{DP}})$ algorithm	$R(K_{\text{DP}}, Z_{\text{DR}})$ algorithm	$R(Z_{\text{H}}, Z_{\text{DR}})$ algorithm
0°	$R=18.87 K_{\text{DP}}^{0.835}$	$R=29.1 K_{\text{DP}}^{0.90} 10^{-0.142Z_{\text{DR}}}$	$R=0.017 Z_{\text{H}}^{0.86} 10^{-0.399Z_{\text{DR}}}$
6°	$R=19.04 K_{\text{DP}}^{0.835}$	$R=29.4 K_{\text{DP}}^{0.90} 10^{-0.144Z_{\text{DR}}}$	$R=0.017 Z_{\text{H}}^{0.86} 10^{-0.404Z_{\text{DR}}}$
12°	$R=19.58 K_{\text{DP}}^{0.835}$	$R=30.3 K_{\text{DP}}^{0.90} 10^{-0.150Z_{\text{DR}}}$	$R=0.017 Z_{\text{H}}^{0.86} 10^{-0.420Z_{\text{DR}}}$
18°	$R=20.52 K_{\text{DP}}^{0.835}$	$R=32.0 K_{\text{DP}}^{0.90} 10^{-0.160Z_{\text{DR}}}$	$R=0.017 Z_{\text{H}}^{0.86} 10^{-0.449Z_{\text{DR}}}$
24°	$R=21.96 K_{\text{DP}}^{0.835}$	$R=34.5 K_{\text{DP}}^{0.90} 10^{-0.176Z_{\text{DR}}}$	$R=0.017 Z_{\text{H}}^{0.86} 10^{-0.493Z_{\text{DR}}}$
30°	$R=23.99 K_{\text{DP}}^{0.835}$	$R=38.2 K_{\text{DP}}^{0.90} 10^{-0.199Z_{\text{DR}}}$	$R=0.017 Z_{\text{H}}^{0.86} 10^{-0.558Z_{\text{DR}}}$

The curves represent an average over all observed drop-size distributions and is nearly identical at S-, C- and X-band.

The reduction factors obtained are:

$$Red_{K_{\text{DP}}}(\gamma)=1+6.3 \cdot 10^{-4}\gamma-3.2 \cdot 10^{-4}\gamma^2+2 \cdot 10^{-6}\gamma^3 \quad (4)$$

for  $K_{\text{DP}}$  and

$$Red_{Z_{\text{DR}}}(\gamma)=1+3.6 \cdot 10^{-4}\gamma-4.2 \cdot 10^{-4}\gamma^2+3 \cdot 10^{-6}\gamma^3 \quad (5)$$

for  $Z_{\text{DR}}$ . (The elevation angle  $\gamma$  is in degrees.) The formulas are valid for S-, C- and X-band and for elevation angles up to 60°.

Table 4 gives the rainfall estimation algorithms for elevation angles up to 30°.

## 8 Conclusions

In this study, the polarimetric radar variables  $Z_{\text{H}}$ ,  $K_{\text{DP}}$  (specific differential phase) and  $Z_{\text{DR}}$  (differential reflectivity)

were calculated for measured drop-size spectra for S-, C- and X-band wavelengths and radar rainfall estimation algorithms for the alpine region of the form  $R(K_{\text{DP}})$ ,  $R(Z_{\text{H}}, Z_{\text{DR}})$ , and  $R(K_{\text{DP}}, Z_{\text{DR}})$  were found.

It could be shown that different raindrop-shape models could alter  $K_{\text{DP}}$  in the calculation by more than 25% and therefore can also account for a wide range of  $R-K_{\text{DP}}$  relationships. The estimated rain rate can vary significantly for a given  $K_{\text{DP}}$  value when comparing the established shape models. The results also show that at C-band the raindrop temperature can influence  $K_{\text{DP}}$  strongly if the radar volume contains a significant number of raindrops >5 mm. As  $K_{\text{DP}}$  measurements are often noisy, especially at S- and C-band (Matrosov et al., 2002),  $R(K_{\text{DP}})$  estimators are mainly stable at high rain rates with big drop sizes. Especially for such cases the effect of temperature on  $K_{\text{DP}}$  cannot be neglected. It was found that  $R(Z_{\text{H}}, Z_{\text{DR}})$  algorithms are most robust to the axial ratio of the raindrops.

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