**Natural Hazards
and Earth
System Sciences**

Correlation analysis technique revealing ionospheric precursors of earthquakes

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Abstract. In this paper we focus on the variability of electron concentration in the ionosphere measured by ground based ionosondes and GPS receivers around the time of strong earthquakes. It has been detected and statistically proven that several days before the seismic shock the level of this variability increases at the station closest to the epicenter, a fact which can be regarded as precursory phenomenon. More precisely the localness of this specific kind of ionospheric variability is used for the correlation analysis of data of several observation points. The similarity of geographical location of the observation points leads to the similarity of ionospheric variations registered at these sites during both quiet and disturbed geomagnetic conditions, except in the case of those located at the seismoactive zone. As a rule, the local anomalies in the F2 layer and TEC accompanying the preparation of strong earthquakes show themselves in the breaking of the mutual correlation of the critical frequencies f_oF2 or TEC between stations situated in and outside the seismic zone. The precursory phenomenon appears 1 to 7 days before the time of the seismic shock.

1 Introduction

In short-term earthquake prediction two principal directions can be separated. First one – the deterministic approach which studies the temporal and spatial distribution behavior of some precursor, for example, the radon emanation (Allegri et al., 1983; King et al., 1993). The other one – the statistical patterns processing on the purpose to find some regularity in the behavior of statistical characteristics of the given parameter. Self organized criticality is one of the main streams of statistical earthquake prediction at the present moment (Rundle et al., 2000).

It was established recently that seismic activity is one of the sources of the day-to-day ionospheric variability (Pu-

linets, 1998; Pulinets and Boyarchuk, 2004; Pulinets and Liu, 2004; Liu et al., 2004). The coupling between the ground surface and the ionosphere is due to the anomalous electric field generated in the earthquake preparation area (Pulinets et al., 2000). The earthquake preparation area conception was introduced by Dobrovolsky et al. (1979) using the elastic deformation calculations. The size of the earthquake preparation area depends on the earthquake magnitude. The same (or very similar) dependencies were obtained not only in the case of the elastic deformations, but also in that of the spatial distribution of different types of precursors in the seismic activation zone (Bowman et al., 1998; Kossobokov et al., 2000) including geochemical ones (Toutain and Baubron, 1999) and local seismicity. Penetrating the ionosphere the anomalous electric field causes the ion drift that results in the formation of electron density irregularities (Kim and Hegai, 1997). These anomalies that appear in the ionosphere before the main seismic shock can be considered as ionospheric precursors (Pulinets and Boyarchuk, 2004). The existence of the ionospheric anomalies/ionospheric precursors is well established not only by physical modeling but statistically as well (Pulinets et al., 2002; Liu et al., 2004; Chen et al., 2004).

For the ionospheric precursors of earthquakes, both approaches are used. One way is to track the specific ionosphere parameters trying to detect in the measurements the recently revealed main features of the ionospheric precursor (Pulinets et al., 2003). The other way is to use the statistically established behavior of some parameter (for example, the critical frequency f_oF2) as a signature of the impending earthquake (Pulinets et al., 2002). Both approaches have their advantages as well as their drawbacks. The first method could fail in magnetically disturbed conditions, while the second requires an a priori knowledge of the precursor behavior, which must be acquired through many years of observations. Obviously, this amount of information will be unattainable for locations with recently installed ionosonde or GPS receiver.

For the present study, one of the most important characteristics of the ionospheric precursors of earthquakes is their
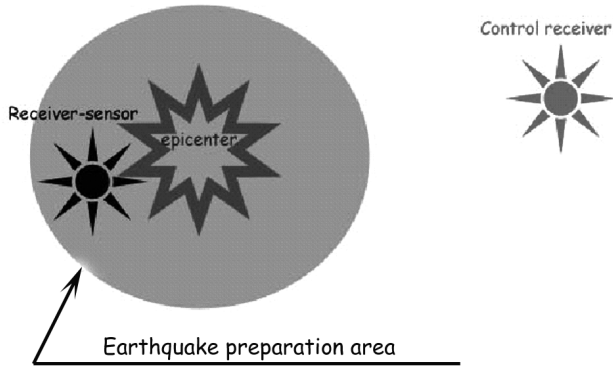

Fig. 1. Configuration of the measurement points positions and earthquake preparation area for the correlation technique described in the paper.

Fig. 2. From top to bottom: autocorrelation coefficient for Petropavlovsk ionospheric station, autocorrelation coefficient for Magadan ionospheric station, cross-correlation coefficient between Petropavlovsk and Magadan stations for period January–April 1974. Triangles indicate the days with earthquakes, diamonds – magnetically disturbed days.

local character. The localness of seismo-ionospheric variations has been demonstrated by different techniques, being the most effective the topside sounding that shows the configuration of the modified areas in the ionosphere, their size and temporal dynamics (Pulinets and Legen'ka, 2003). The size of the modified area in the ionosphere is of the same order of magnitude as the size of the earthquake preparation area on the ground surface (Dobrovolsky, 1979; Pulinets et al., 2004). This fact offers us an opportunity to propose a very simple but quite effective technique of detecting the ionospheric variations associated with the earthquake preparation process.

2 Description of the technique

In the simplest configuration two measurement points are used: one ("receiver-sensor") located inside the earthquake preparation area (see Fig. 1), and the other ("control-receiver") located outside it.

Two important considerations regarding receivers localization are taken into account

1. receivers should be in the same (or very close) geomagnetic latitude, in order to ensure the similarity of their reaction to geomagnetic disturbances.

2. the longitude of the receivers should not differ too much because of the LT (local time) dependence of ionosphere reaction to geomagnetic storm commencement.

In general, the ionospheric variability in terms of critical frequency variations is lower for those variations associated with seismic activity than for those associated with geomagnetic storms. Therefore, the seismically generated variations may be shadowed by the storm-time variations. However, if two measurement points are used with the configuration shown in Fig. 1, storm-time variations can be excluded by cross-correlation of the records at the given points as storm-time variations will be practically identical for both stations. It has been shown (Szuszczewisz et al., 1998) that in a large
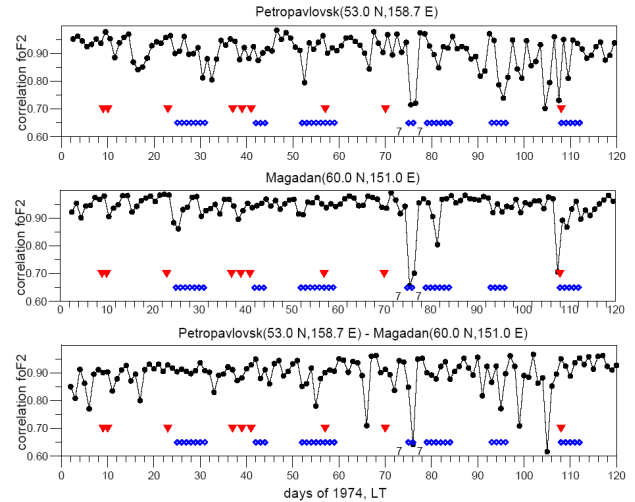
range of latitudes and longitudes the ionospheric reaction to geomagnetic disturbances is very similar (see Fig. 3 in Szuszczewisz et al., 1998), and this may provide high correlation in the daily variations between different ionospheric stations. At a given time, the "receiver sensor" will be much more sensitive to the seismogenic variations in comparison with the "control receiver". This fact is used in the proposed technique.

For the calculation of the daily correlation coefficients we use the standard definition of the cross-correlation coefficient (Devore, 2000) where the records of the critical frequency, or vertical total electron content (TEC), with equal time intervals for the given day are used:

$$C = \frac{\sum\limits_{i=0,k} (f_{1,i} - af_1)(f_{2,i} - af_2)}{k(\sigma_1 \sigma_2)}.$$

The indices 1 and 2 correspond to the first and second ionospheric station(s), $f = f_o F2$ (hourly values of the critical frequency scaled from the ionograms), k=23 and af and σ are determined by the following expressions (in principle, other sampling intervals can be used, for example 15 min intervals as it is used at ionospheric stations, or 10 min intervals, which we use for vertical TEC calculations, respectively, k will correspond to the number of records):

$$af = \frac{\sum\limits_{i=0,k} f_i}{k+1}$$

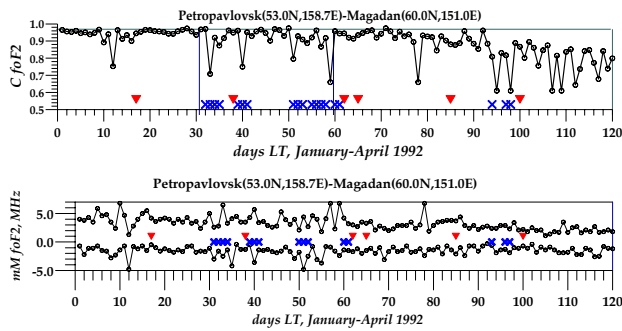$$\sigma^2 = \frac{\sum\limits_{i=0,k} (f_i - af)^2}{k}$$

Fig. 3. Upper panel – cross-correlation coefficient for Petropavlovsk and Magadan stations for period January–April 1992. Bottom panel M and m coefficients for the same stations and the same period. Triangles indicate the days with earthquakes, crosses – magnetically disturbed days.

af is a daily mean value of the critical frequency, σ is the standard deviation.

3 The hypothesis testing

The proposed technology was tested on the series of earthquakes in the Western Pacific area (Russia Far East, Taiwan, Japan). As an example we will consider the data of two Russian stations: Petropavlovsk-na-Kamchatke (53.0° N, 158.7° E) and Magadan (60.0° N, 151.0° E). The first one is inside the main Russian seismoactive area – Kamchatka peninsula. To demonstrate the "clearing process" we present the autocorrelation coefficients of both stations for a period of 4 months (January–April, 1974) in the upper two panels of the Fig. 2. Autocorrelation means that every consequent day was correlated with the preceding one. Every magnetic disturbance causing a change in the daily variation of the critical frequency would be tracked by each station in the form of the drop of the autocorrelation coefficient. However, due to increased ionospheric variability caused by the seismic activation mentioned in Introduction, the additional drops of autocorrelation coefficient appeared only on the record of Petropavlovsk station, because of its location inside the earthquake preparation area. The cross-correlation is shown in the bottom panel of Fig. 2. One can see that, at least during the first part of the observed period, only the drops connected with the seismic events are left at the cross-correlation coefficient records in comparison with autocorrelation records. A similar pattern can be observed for another period (January–April 1992) in the upper panel of the Fig. 3. In both cases (Figs. 2 and 3) the drops of the cross-correlation coefficient happened from 5 to 7 days before the time of the seismic shock.

Another parameter that can be used for estimating the spatial ionospheric variability is the daily maximum and minimum difference of the critical frequencies hourly values of both stations (Gaivoronskaya and Pulinets, 2002):

$$M = \max \{f_{1,i} - f_{2,i}\}_{i=0,k}$$

Table 1. Coordinates of INEGI GPS receivers used for the analysis of GPS TEC around the time of Colima earthquake.

Station	Latitude (N)	Longitude (W)
COL2	19.244	103.702
CUL1	24.799	107.384
INEG	21.856	102.284
MEXI	32.633	115.476
TOL2	19.293	99.64

$$m = \min \{f_{1,i} - f_{2,i}\}_{i=0,k}.$$

It is obvious that the larger difference between indices M and m means the increased variability. Sometimes (like in equinoctial conditions), when the daily maximum of the critical frequency is not so expressed due to extension of daylight hours, the use of these indices of the variability can be even more effective, a fact which is demonstrated at the bottom panel of Fig. 3. It can be seen from the figure that the instability observed in April in upper panel disappeared in the bottom one, but precursory effects are seen in the figure as well.

4 The technique testing by GPS TEC data

It has been shown (Liu et al., 2001) that the correlation coefficient between the variations of the peak electron concentration $NmF2$ and vertical TEC (Total Electron Content) is 0.953, including in periods of anomalous variations connected with seismic activity. This opens the possibility of applying the developed technique to the TEC variations derived from the GPS receivers network. Such attempt was made for the recent strong (M_w=7.8) Colima earthquake in Mexico, occurred on 21 January (20:06:48.09 LT), or 22 January (02:06:48.09 GMT) of 2003.

To detect the possible ionospheric variations associated with this earthquake the data of 5 stationary GPS receivers of the National Institute of Statistics, Geography and Informatics (INEGI) were used. The stations coordinates are shown in Table 1.

The data of the closest to epicenter receiver (COL2) were analyzed first. To this purpose the monthly median was calculated to compare with current data, and to determine the deviations from the monthly median. Results are shown in Fig. 4. For the better time resolution only several days around the time of the Colima earthquake are shown, clearly demonstrating the presence of anomalous variations out of the upper bound on 18 and 19 of January.

The current observations are indicated with a thick line, and represent the vertical TEC in TEC units (1 TECu=10^{16} el/m^2). Monthly mean is indicated with a thin line, and the upper bound with a dashed one. For the time when anomalous peak of TEC was registered on 18 January (10:10 LT on 18 January 2003), the map of the TEC deviation
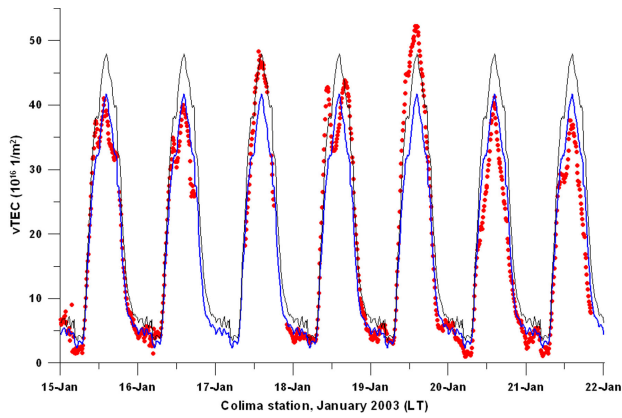
Fig. 4. Vertical TEC variations (points) in comparison with the monthly mean (thick line). Thin line – upper bound calculated as monthly mean $+\sigma$.
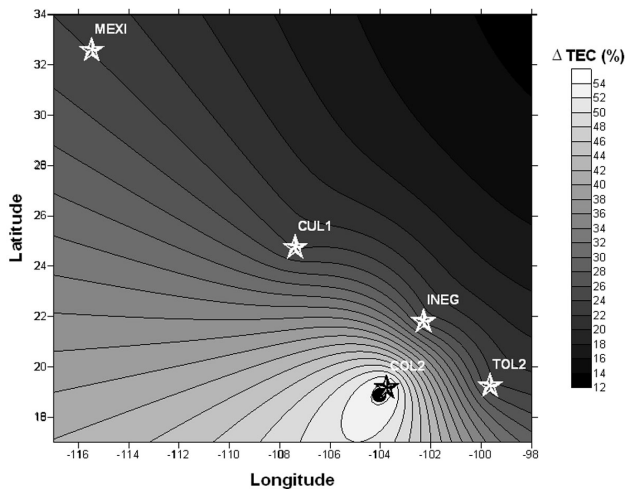

Fig. 5. Spatial distribution of the vTEC deviation from the monthly median at 10:10 LT on 18 January 2003.
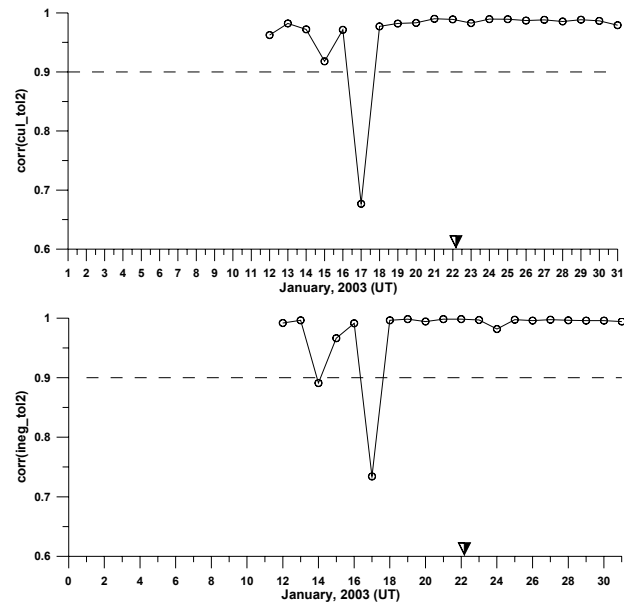

Fig. 6. Daily cross-correlation coefficients for vertical TEC derived from data of Toluca (TOL2), Culiacan (CUL) and Aguascalientes (INEG) receivers for the period around the time of Colima earthquake. Upper panel – correlation coefficient between Culiacan and Toluca stations, bottom panel – correlation coefficient between Aguascalientes and Toluca stations. The time of the Colima earthquake is indicated in figures by sign.

from the monthly median was constructed (Fig. 5) using the data of 5 receivers (their coordinates are shown in Table 1). Acknowledging the limitations of such map (low spatial resolution, lack of measurements in the left bottom corner of the map, which is in the Pacific Ocean) it clearly demonstrates the presence of an anomaly just around the epicenter position of the impending earthquake. Keep in mind that distribution is built for a period of time of more than 3 days before the seismic shock.

To determine whether the correlation technique works for the GPS data, the cross-correlation coefficient between different stations was calculated. Taking into account that Colima receiver stopped measurements immediately after the seismic shock, due to damage and incompleteness of data records on 17 January (important day for the precursors identification), the Toluca receiver (TOL2) was used as a "sensor" station. In Fig. 6 the cross-correlation coefficients for the pairs TOL2-INEG and TOL2-CUL are presented. The drop

of the correlation coefficient 5 days before the seismic shock in the both panels and a smaller drop, 7 and 8 days before the shock respectively, can be seen.

As one can see, the correlation technique works for GPS TEC data as well. It shows the same time scale for precursors as for the vertical sounding: precursors appear 5 days before the seismic shock as it was described by Pulinets et al. (2003). The high correlation between the stations records is violated within the period several days before strong seismic shock.

The second fast check of the correlation technique was made for the San Simeon earthquake in central California in December 2003: M=6.5, 35.7° N, 121.1° W, 19:15:56 GMT on 22 December 2003. The map of the GPS receivers used for the analysis and the epicenter position are shown in Fig. 7. The receiver closest to the epicenter (VNDP) is used as a "sensor". The graphs of the correlation coefficient for 3 stations are shown in Fig. 8. Both curves indicate the gradual drop of the cross-correlation coefficient starting from 15 of December, i.e. 7 days before the shock with absolute minima registered one day and three days before the shock respectively. CASA indicates a minimum the day after the shock which can be associated with the acoustic action of the shock on the ionosphere. It should be noted that not all the stations from Fig. 7 showed the drop of the correlation coefficient, which indicates the dependence of the technique on the receiver position. The reason of this fact was explained by Pulinets et al. (2004) and is connected with the complex distri-
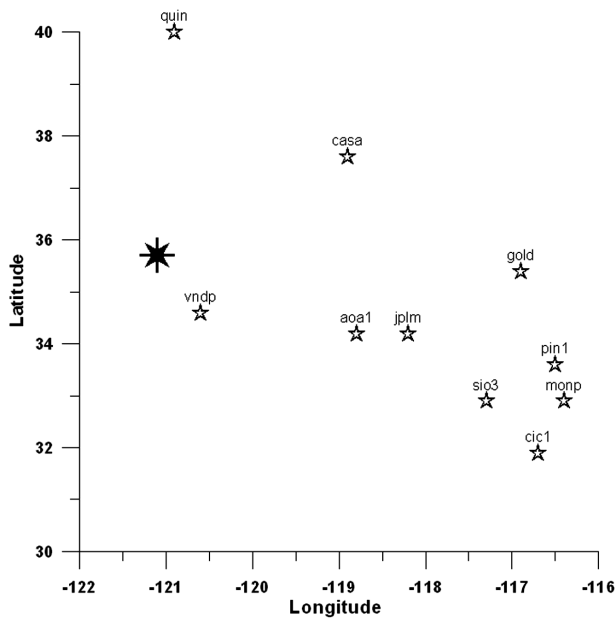
Fig. 7. Positions of GPS receivers (stars) used in analysis of TEC variations around the time of San Simeon earthquake 22 December 2003. Earthquake epicenter position.
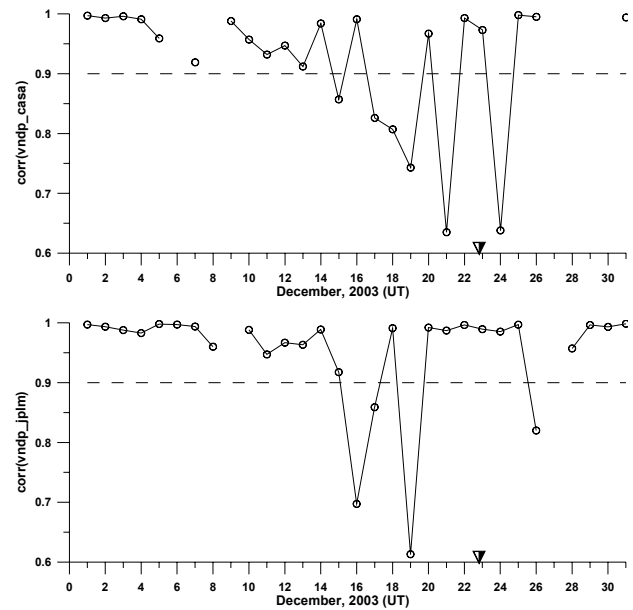

Fig. 8. Daily cross-correlation coefficients for vertical TEC derived from GPS receivers network at California, USA for December 2003. Upper panel – correlation coefficient between VNDP and CASA stations, bottom panel – correlation coefficient between VNDP and JPLM stations. The time of the San Simeon earthquake is indicated in figures by sign. The stations and the epicenter positions are shown in the map (Fig. 7).

bution of electron concentration anomaly in the ionosphere. It could happen that the station does not "feel" the anomaly at all, as sometimes happens in our correlation analysis. This question needs more careful investigation, and is the purpose of a future work. Such study demands a very dense network of GPS receivers, but at the time only Japan and the State of California (USA) have enough receivers to provide the necessary resolution.

5 Conclusions

Very simple but powerful technique was presented which is based on the correlation of records of two receiving stations (ionosondes or GPS receivers). One of them is situated within the area of earthquake preparation, while the other one (being in the same geophysical conditions) is outside the earthquake preparation area (or its outer edge). Due to similar geophysical conditions the correlation coefficient for the registering stations is very high (usually, more than 0.9), but few days before the strong seismic shock (from 7 to 1) sharp drops of the daily correlation coefficient appear manifesting the increased variability of the ionosphere over the earthquake preparation area. The proposed technique permits to identify the ionospheric precursors even in geomagnetically disturbed conditions. The other parameters which can be used for ionosphere variability estimation is the difference between maximal and minimal daily values of the critical frequency f_oF2 (or vertical TEC) for the stations used in correlation analysis.

Some limitation of the proposed technique is connected with the fact that an arbitrary location of the "sensor" station

may not give the positive result. This fact is connected with the complex configuration of anomalous variations within the ionosphere. The ionospheric irregularity may be shifted along the geomagnetic field lines equatorward against the vertical projection of the epicenter of the impending earthquake on the ionosphere. In such a situation the "sensor" station becomes blind and cannot "feel" the anomalous variations. This situation may be avoided by an accurate selection of the positions of the "sensor" and "control" stations. It requires the additional investigations within the particular zone of seismic activity. Nevertheless the proposed technique permits a low cost monitoring of ionospheric precursors of earthquakes avoiding the use of expensive satellite technologies.

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References

Allegri, L., Bella, F., Delia Monica, G., Ermini, A., Impora, S., Sgrigna, V., and Biagi, P. F.: Radon and tilt anomalies detected before the Irpinia (South Italy) earthquake of 23 November 1980 at great distance from the epicenter, Geophys. Res. Lett., 10, 269–272, 1983.

Bowman, D. D., Ouillon, G., Sammis, C. G., Sornette, A., and Sornette, D.: An observation test of the critical earthquake concept, J. Geophys. Res., 103, 24 359–24 372, 1998.

Chen, Y. I., Liu, J. Y., Tsai, Y. B., and Chen, C. S.: Statistical tests for pre-earthquake ionospheric anomaly, Terr. Atm. Ocean Sci., 15, 385–396, 2004.

Devore, J. L.: Probability and Statistics for Engineering and the Sciences, Duxbury Thomson Learning, USA, 775, 1999.

Dobrovolsky, I. R., Zubkov, S. I., and Myachkin, V. I.: Estimation of the size of earthquake preparation zones, Pageoph., 117, 1025–1044, 1979.

Gaivoronskaya, T. V. and Pulinets, S. A.: Analysis of F2-layer variability in the areas of seismic activity, Preprint IZMIRAN No. 2(1145) Moscow, 20, 2002.

Kim, V. P. and Hegai, V. V.: On possible changes in the midlatitude upper ionosphere before strong earthquakes, J. Earthq. Predict. Res., 6, 275–280, 1997.

King, C.-Y., Zhang, W., and King, B.-S.: Radon Anomalies on Three Kinds of Faults in California, Pageoph., 141, 111–124, 1993.

Kossobokov, V. G., Keilis-Borok, V. I., Turcotte, D. L., and Malamud, B. D.: Implications of a Statistical Physics Approach for Earthquake Hazard Assessment and Forecasting, Pure Appl. Geophys., 157, 2323–2349, 2000.

Liu, J. Y., Chen, Y. I., Chuo, Y. J., and Tsai, H. F.: Variations of ionospheric total electron content during the Chi-Chi earthquake, Geophys. Res. Lett., 28, 1383–1386, 2001.

Liu, J. Y., Chuo, Y. J., Shan, S. J., Tsai, Y. B., Pulinets, S. A., and Yu, S. B.: Pre-earthquake ionospheric anomalies monitored by GPS TEC, Ann. Geophys., 22, 1585–1593, 2004,
SRef-ID: 1432-0576/ag/2004-22-1585.

Pulinets, S. A.: Seismic activity as a source of the ionospheric variability, Adv. Space Res., 22, 903–906, 1998.

Pulinets, S. A., Boyarchuk, K. A., Khegai, V. V., Kim, V. P., and Lomonosov, A. M.: Quasielectrostatic Model of Atmosphere-Thermosphere-Ionosphere Coupling, Adv. Space Res., 26, 1209–121, 2000.

Pulinets, S. A., Boyarchuk, K. A., Lomonosov, A. M., Khegai, V. V., and Liu, J. Y.: Ionospheric precursors to earthquakes: a preliminary analysis of the f_oF2 critical frequencies at Chung-Li ground-based station for vertical sounding of the ionosphere (Taiwan island), Geomagnetism and Aeronomy, 42, 508–513, 2002.

Pulinets, S. A. and Legen'ka, A. D.: Spatial-temporal characteristics of the large scale disturbances of electron concentration observed in the F-region of the ionosphere before strong earthquakes, Cosm. Res., 41, 221–229, 2003.

Pulinets, S. A., Legen'ka, A. D., Gaivoronskaya, T. V., and Depuev, V. Kh.: Main phenomenological features of ionospheric precursors of strong earthquakes, J. Atmos. Solar-Terr. Phys., 65, 1337–1347, 2003.

Pulinets, S. A. and Boyarchuk, K. A.: Ionospheric Precursors of Earthquakes, Springer, Berlin, Germany, 315, 2004.

Pulinets, S. A., Liu, J. Y., and Safronova, I. A.: Interpretation of a statistical analysis of variations in the f_oF2 critical frequency before earthquakes based on data from Chung-Li ionospheric station (Taiwan), Geomagn. Aeronom., 44, 102–106, 2004.

S. A. Pulinets and Liu, J. Y.: Ionospheric variability unrelated to solar and geomagnetic activity, Adv. Space Res., 34, 1926–1933, 2004.

Rundle, J. B., Turcotte, D. L., and Klein W. (eds.): GeoComplexity and the Physics of Earthquakes, Geophysical Monographs Series, American Geophysical Union, Washington D. C., 2000.

Szuszczewicz, E. P., Lester, M., Wilkinson, P., Blanchard, P., Abdu, M., Hanbaba, R., Igarashi, K., Pulinets, S., and Reddy, B. M.: Global ionospheric storm characteristics during solar maximum equinox, J. Geophys. Res., 103, 11 665–11 684, 1998.

Toutain, J.-P. and Baubron, J.-C.: Gas geochemistry and seismotectonics: a review, Tectonophysics, 304, 1–27, 1998.