

# Status of Electroweak Corrections to Top Pair Production <sup>\*†</sup>

J. Fleischer<sup>1‡</sup>, A. Leike<sup>2</sup>, T. Riemann<sup>3</sup>, A. Werthenbach<sup>3,4</sup>

<sup>1</sup> Fakultät f. Physik, Universität Bielefeld, 33615 Bielefeld, Germany

<sup>2</sup> Sektion Physik der Universität München, 80333 München, Germany

<sup>3</sup> Deutsches Elektronen-Synchrotron, DESY Zeuthen, 15738 Zeuthen, Germany

<sup>4</sup> Theory Division, CERN, 1211 Geneva 23, Switzerland

## Abstract

We review the status of electroweak radiative corrections to top-pair production at a Linear Collider well above the production threshold. We describe the Fortran package `topfit` and present numerical results at  $\sqrt{s} = 500$  GeV, 1 TeV, and 3 TeV.

---

\*Talk presented by T. Riemann at Int. Workshop on Linear Colliders (LCWS 2002), 26-30 Aug 2002, Jeju Island, Korea

†Work supported in part by the European Community's Human Potential Programme under contract HPRN-CT-2000-00149 Physics at Colliders

‡E-mails: fl@physik.uni-bielefeld.de, leike@theorie.physik.uni-muenchen.de,  
Tord.Riemann@desy.de, Anja.Werthenbach@desy.de

## 1 Introduction

Not too much is known about top quarks, and what is known is not as accurate as desired [1]. At a Linear Collider, top-pair production will be one of the dominant and most interesting processes. Very precise measurements are expected. Therefore, the cross-sections have to be predicted with a precision of few per mil [2, 3]. Two quite different experimental set-ups are of interest. One is the top-pair production threshold region, where one expects to get precise values of mass and width. The other one is continuum production at high energy with the hope to get access to some anomalous behavior, potentially manifested in abnormal couplings and/or new final state signatures. Here, we calculate the electroweak Standard Model expectations with one-loop corrections. Earlier series of studies are [4, 5] and [6, 7], and a recent one is [8, 9]. With our study, detailed comparisons of the diverse results were undertaken for the first time [10, 11]. We used the package `DIANA` [12, 13] for automatic generation of the diagrams and `FORM` [14] for the further symbolic calculations, and for the numerics the Fortran packages `FF` [15] and `LoopTools` [16].

## 2 The Fortran Package `topfit`

The package `topfit` [17, 18] was written in order to have a tool for the numerical estimation of the electroweak corrections to top-pair production. We wanted also to have some flexibility for an easy comparison with other codes. As a result, the user of our program may switch on and off several options and may adjust input parameters. The list in Table 1 is by far not complete. Of course, the usual standard model parameters in the on-mass-shell scheme (particle masses and  $\alpha_{em}(0)$ ) may be chosen. The numerical input is as in [10]. Three different options may be chosen for the output:

- Differential and integrated cross-sections and asymmetries in the Standard Model
- Cross-sections and asymmetries with photonic corrections only, at fixed Born couplings
- Six weak form factors, with/without running  $\alpha_{em}$

Flag	Description
IFINAL	choice of final state particle
IQED	inclusion of photonic corrections
CNINI	initial state corrections
CNFIN	final state corrections
CNINT	interference corrections
IWEAK	Born or use <code>LoopTools</code> or use <code>FF</code>
GAMS	choice of $Z$ width
IQEDAA	running of $\alpha_{em}$
IPHOTM	finite photon mass or dimensional regularisation of the IR divergency
IDCOST	top quark angular distribution
ICOSTI	integrated cross-section and asymmetry
IHARD	inclusion of hard bremsstrahlung
SPRCUT	photonic phase space cut

Table 1: A collection of flags of `topfit`; more details may be found in [17].

The latter output might be useful for a Monte Carlo approach to QED and QCD corrections, but also for an estimate of the weak corrections.

### 3 Numerical Results and Conclusions

For comparisons with the results of other groups, with very satisfactory numerical agreements, we refer to [10, 11]. Of course, one has to bear in mind that these comparisons control not more than what is called ‘technical precision’. In Figure 1 we show the order of magnitude of the cross-sections, and in Table 2 purely weak form factors at  $\sqrt{s} = 3$  TeV. To define the normalizations of  $F_3^{11}$  and  $F_3^{51}$ , we mention that  $d\sigma \sim Re[(u^2 + t^2 + 2m_t^2 s)|F_1^{11}|^2 + 2m_t(ut - m_t^4)(F_1^{11*}F_3^{11} + F_1^{51*}F_3^{51})] + \dots$ , and  $t = s(1 - \beta_t \cos \theta)/2$ .

The treatment of the one-loop electroweak corrections to top-pair production is well under control up to  $\sqrt{s} = 3$  TeV. Of course, there is much Standard Model physics to be included in addition: higher orders, notably in the photonic part, but also numerically large QCD corrections, and finally also phenomena like top-quark

f.f.	Born	Born + weak corrections
$F_1^{11}$	-3.4822175 E-09, 0	-2.4672033 E-09, +5.6471323 E-12
$F_1^{15}$	+2.0992410 E-10, 0	-4.6533609 E-10, -3.4235887 E-10
$F_1^{51}$	+7.5582979 E-10, 0	+1.4831421 E-10, -2.6754148 E-10
$F_1^{55}$	-1.8476412 E-09, 0	-1.4913239 E-09, +3.4972393 E-10
$m_t F_3^{11}$	0, 0	+2.9895163 E-12, -6.6708986 E-13
$m_t F_3^{51}$	0, 0	-2.4939160 E-12, +9.1292861 E-13

Table 2: Weak form factors for  $d\sigma/d\cos\theta$  at  $\sqrt{s}=3$  TeV,  $\cos\theta=0.7$ . They yield  $\sigma_B=0.076266014$  pb and  $\sigma_{weak}=0.012482585$  pb, correspondingly. The normalization corresponds to  $F_{1,Born}^{11,\gamma} = e^2 Q_e Q_t / s$  (see also [10]); some flags chosen: IWEAK = 1, GAMS = -1, IQED = IQEDAA = 0.

decays, other background reactions (of different signatures like  $e^+e^- \rightarrow tWb, tbl_1l_2, 6f$ ), or beamstrahlung.

**Acknowledgments.** T.R. and A.W. would like to thank the organizers of LCWS 2002 for the opportunity to visit an interesting, well-organized, and pleasant conference. F.J. and A.L. would like to thank DESY for support.

## References

- [1] E. Simmons, talk at HCP2002, preprint BUHEP-02-39, [hep-ph/0211335](#).
- [2] ECFA/DESY LC Physics Working Group (J. Aguilar-Saavedra et al.), “TESLA Technical Design Report Part III: Physics at an  $e^+e^-$  Linear Collider”, preprint DESY 2001-011 (2001), [hep-ph/0106315](#).
- [3] American Linear Collider Working Group (T. Abe et al.), “Linear collider physics resource book for Snowmass 2001”, Fermilab preprint FERMILAB-PUB-01-058-E (2001).
- [4] J. Fujimoto and Y. Shimizu, **Mod. Phys. Lett.** **3A** (1988) 581.
- [5] F. Yuasa et al., **Prog. Theor. Phys. Suppl.** **138** (2000) 18–23.
- [6] W. Beenakker et al., **Nucl. Phys.** **B365** (1991) 24–78.

- [7] W. Hollik and C. Schappacher, **Nucl. Phys. B****545** (1999) 98–140.
- [8] D. Bardin et al., Dubna preprint JINR E2–2000–292 (2000), **hep-ph/0012080**, v.2 (12 Dec 2001).
- [9] A. Andonov et al., CERN-TH/2001-308 (2001), CERN-TH/2002-068 (2002).
- [10] J. Fleischer, T. Hahn, W. Hollik, T. Riemann, C. Schappacher, and A. Werthenbach, “Complete electroweak one-loop radiative corrections to top- pair production at TESLA: A comparison”, DESY preprint TESLA LC-TH-2002-002 (2002), **hep-ph/0202109**.
- [11] J. Fleischer, J. Fujimoto, T. Ishikawa, A. Leike, T. Riemann, Y. Shimizu, and A. Werthenbach, “One-loop corrections to the process  $e^+e^- \rightarrow t\bar{t}$  including hard bremsstrahlung”, preprint DESY 02-025 (2002), **hep-ph/0203220**.
- [12] M. Tentyukov and J. Fleischer, **Comp. Phys. Comm.** **132** (2000) 124–141.
- [13] M. Tentyukov and J. Fleischer, “DIANA, a program for Feynman diagram evaluation”, **hep-ph/9905560**, see also <http://www.physik.uni-bielefeld.de/~tentukov/diana.html>.
- [14] J. Vermaseren, “Symbolic manipulation with FORM” (Computer Algebra Nederland, Amsterdam, 1991).
- [15] G. van Oldenborgh, **Comp. Phys. Comm.** **66** (1991) 1–15.
- [16] T. Hahn and M. Perez-Victoria, **Comp. Phys. Comm.** **118** (1999) 153–165.
- [17] J. Fleischer, A. Leike, T. Riemann, and A. Werthenbach, Fortran program **topfit.F** v.0.911 (15 Nov 2002), <http://www-zeuthen.desy.de/~riemann/>.
- [18] J. Fleischer, A. Leike, T. Riemann, and A. Werthenbach, in preparation.

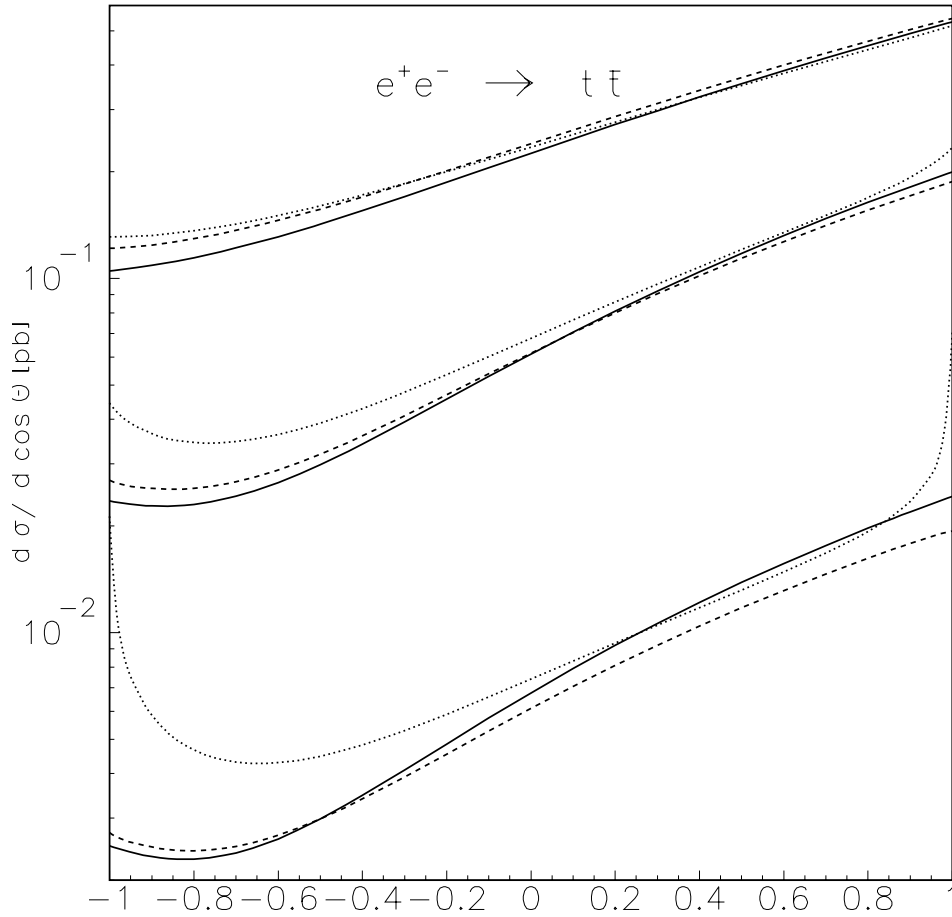


Figure 1: *Differential cross-sections in Born approximation (solid lines), with weak corrections (dashed), and with full electroweak corrections (no cut; dotted). From above:  $\sqrt{s} = 0.5, 1, 3$  (in TeV).*