Do neutrino oscillations allow an extra phenomenological parameter?

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Abstract

trino oscillations is in fact not a free parameter, but a fixed number. The quantity ξ introduced recently in the phenomenological description of neu-

expressions for the neutrino oscillation probability. to equal energy assumption [5, 6]. Authors of [7] emphasize that ξ disappears from final corresponds to the so-called equal momentum assumption [1, 2], while $\xi = 1$ corresponds mixing have introduced a new phenomenological parameter ξ . According to [7], $\xi = 0$ and references therein). In a recent paper [7] Giunti and Kim in the case of two-flavour The literature on phenomenology of neutrino oscillations is vast (see, e.g., [1] - [6]

servation in the process which is responsible for neutrino emission, as explicitly assumed The aim of this note is to indicate that parameter ξ is fixed by energy-momentum con-

auxiliary case of absolutely massless neutrinos and denoting the energy of such neutrinos Following ref. [7] we will consider the decay $\pi \to \mu\nu$ in the framework of two-flavour toy model. The parameter ξ is defined in [7] for the pion rest-frame by considering the

$$\xi = {}^{1}/_{2}(1 + m_{\mu}^{2}/m_{\pi}^{2}) , \qquad (1)$$

neutrinos they get: where m_{μ} and m_{π} are the masses of the muon and the pion. Then for massive (but light!)

$$E_{1,2} = E + (1 - \xi)m_{1,2}^2/2E$$
 , (2)

$$p_{1,2} = E - \xi m_{1,2}^2 / 2E . (3)$$

tively. Wherefrom the above statement about $\xi = 0, 1$ follows: Here $E_{1,2}$, $p_{1,2}$ and $m_{1,2}$ are the energies, momenta and masses of the neutrinos, respec-

$$E_1 = E_2 \text{ for } \xi = 1 \text{ and } p_1 = p_2 \text{ for } \xi = 0 .$$
 (4)

and $\Delta p \equiv p_1 - p_2 = 0$, respectively, are treated by authors of ref. [7] as particular cases of the general kinematical relations (2) and (3): Thus, the equal energy and equal momentum assumptions in the form $\Delta E \equiv E_1 - E_2 = 0$

$$\Delta E = (1 - \xi)\Delta m^2 / 2E = 0 \text{ for } \xi = 1 ,$$
 (5)

$$\Delta p = \xi \Delta m^2 / 2E = 0 \text{ for } \xi = 0 . \tag{6}$$

Unfortunately, both the treatment and the relations (4) - (6) are erroneous.

On one hand, the quantity ξ is not a free parameter for a certain decay process. Indeed, it follows from (1) that ξ has a fixed value ($\simeq 0.8$) for the decay under consideration. On the other hand, it is evident from definitions of E and ξ that

$$E = m_{\pi}(1 - \xi) \quad . \tag{7}$$

The parameter ξ determines sharing of the decay energy. As seen from (7), the values $\xi = 0$ and $\xi = 1$ are senseless ones because they refer accordingly to the limiting cases of $E_{\mu} = 0$ and E = 0. Therefore one cannot assume that ξ can be equal to 1 or 0. Instead of that, the solution of the equalities (5) and (6) is the vanishing Δm^2 , that is absence of the oscillations.

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