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# X-Ray Scattering from Soft-Matter Thin Films

Materials Science and Basic Research

With 98 Figures



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