Single target-spin asymmetries in semi-inclusive pion electroproduction on longitudinally polarized protons*

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We evaluate the single target-spin $\sin \phi_{h}$ and $\sin 2 \phi_{h}$ azimuthal asymmetries in the semiinclusive deep inelastic lepton scattering off longitudinally polarized proton target under HERMES kinematic conditions. A good agreement with the HERMES data can be achieved using only the twist-2 distribution and fragmentation functions.

Significant single-spin asymmetries have been observed in experiments with transversely polarized proton and anti-proton beams [1]. Recently new experimental results on azimuthal asymmetries became available. Specifically, the first measurements of single target-spin azimuthal asymmetries of pion production in semi-inclusive deep inelastic scattering (SIDIS) of leptons off a longitudinally polarized target at HERMES [2] and off a transversely polarized target at SMC [3], and the observation of the azimuthal correlations for particles produced from opposite jets in $Z$ decay at DELPHI [4].

In this note we present estimates of the single spin azimuthal asymmetry in the SIDIS on a longitudinally polarized nucleon target for the HERMES kinematic conditions. Our approach is based on the parton model description of polarized SIDIS [5]. The cross-section contains the $(1 / Q)^{0}$-order terms coming from leading dynamical twist-two distribution and fragmentation functions (DF's and FF's) as well as ( $1 / Q$ )-order kinematic twistthree terms arising due to the intrinsic transverse momentum of the quark in the nucleon. We will neglect the $(1 / Q)$-order contributions of the higher twist DF's and FF's obtained in [6]. Thus, our approach is similar to that of [7] in describing the $\cos \phi_{h}$ asymmetry in unpolarized SIDIS.

Let $k_{1}\left(k_{2}\right)$ be the initial (final) momentum of the incoming (outgoing) charged lepton, $Q^{2}=-q^{2}, q=k_{1}-k_{2}$ - the momentum of the virtual photon, $P$ and $P_{h}(M$ and $\left.M_{h}\right)$ - the target and final hadron momentum (mass), $x=q^{2} / 2(P q), y=(P q) /\left(P k_{1}\right)$, $z=\left(P P_{h}\right) /(P q), P_{h T}\left(k_{1 T}\right)$ - the hadron (lepton) transverse with respect to virtual photon momentum direction and $\phi_{h}$ - the azimuthal angle between $P_{h T}$ and $k_{1 T}$ around the virtual photon direction. Note that the azimuthal angle of the transverse (with respect to the virtual photon) component of the target polarization, $\phi_{S}$, is equal to $0(\pi)$ for the

[^0]target polarized parallel (antiparallel) to the beam (Fig. 1).


Figure 1. The definition of the azimuthal angle $\phi_{h}$ and the target polarization components in virtual photon frame.

We use the approach developed in [8] and consider the cross-section integrated with different weights depending on the final hadron transverse momenta $w_{i}\left(P_{h T}\right)^{4}$ :
$\Sigma_{i}=\frac{Q^{2} y}{2 \pi \alpha^{2}} \int d^{2} P_{h T} w_{i}\left(P_{h T}\right) d \sigma$,
with $w_{1}\left(P_{h T}\right)=1, w_{2}\left(P_{h T}\right)=\left|P_{h T}\right| \sin \phi_{h} / M_{h}$ and $w_{3}\left(P_{h T}\right)=\left|P_{h T}\right|^{2} \sin 2 \phi_{h} / 2 M M_{h}$. Considering only the twist-two contributions, we have:
$\Sigma_{1}=\left(1+(1-y)^{2}\right) f_{1}(x) D_{1}(z)$,
where $f_{1}(x)$ and $D_{1}(z)$ are the usual unpolarized DF's and FF's. Moreover
$\Sigma_{2}=\Sigma_{2 L}+\Sigma_{2 T}$,

[^1]where
$\Sigma_{2 L}=-8 S_{L} \frac{M}{Q}(2-y) \sqrt{1-y} z h_{1 L}^{\perp(1)}(x) H_{1}^{\perp(1)}(z)$
is the $(1 / Q)$-order contribution from twist-two $\operatorname{DF} h_{1 L}^{\perp(1)}(x)$ and FF $H_{1}^{\perp(1)}(z)$ arising due to intrinsic transverse momentum and
$\Sigma_{2 T}=2 S_{T x}(1-y) z h_{1}(x) H_{1}^{\perp(1)}(z)$
is arising due to the small $(\sim(1 / Q))$ transverse component of the target polarization $\left(S_{T x}\right)$ [5,9]. Finally
$\Sigma_{3}=8 S_{L}(1-y) z^{2} h_{1 L}^{\perp(1)}(x) H_{1}^{\perp(1)}(z)$.
The weighted cross sections involve the $p_{T}^{2}\left(k_{T}^{2}\right)$ moment of the DF's (FF's), defined as
$h_{1 L}^{\perp(1)}(x) \equiv \int d^{2} p_{T}\left(\frac{p_{T}^{2}}{2 M^{2}}\right) h_{1 L}^{\perp}\left(x, p_{T}^{2}\right)$,
$H_{1}^{\perp(1)}(z) \equiv z^{2} \int d^{2} k_{T}\left(\frac{k_{T}^{2}}{2 M_{h}^{2}}\right) H_{1}^{\perp}\left(z, z^{2} k_{T}^{2}\right)$.
We note that $h_{1 L}^{\perp}(x)$ and $h_{1}(x)$ describe the quark transverse spin distribution in the longitudinally and transversely polarized nucleon respectively, while $H_{1}^{\perp}(z)$ describes the analyzing power of transversely polarized quark fragmentation (Collins effect) [10].

The single target-spin asymmetries for SIDIS on a longitudinally polarized target are defined as
$\left\langle\frac{\left|P_{h T}\right|}{M_{h}} \sin \phi_{h}\right\rangle \equiv \frac{\int d^{2} P_{h T} \frac{\left|P_{h T}\right|}{M_{h}} \sin \phi_{h}\left(d \sigma^{+}-d \sigma^{-}\right)}{\int d^{2} P_{h T}\left(d \sigma^{+}+d \sigma^{-}\right)}$,
$\left\langle\frac{\left|P_{h T}\right|^{2}}{M M_{h}} \sin 2 \phi_{h}\right\rangle \equiv \frac{\int d^{2} P_{h T} \frac{\left|P_{h T}\right|^{2}}{M M_{h}} \sin 2 \phi_{h}\left(d \sigma^{+}-d \sigma^{-}\right)}{\int d^{2} P_{h T}\left(d \sigma^{+}+d \sigma^{-}\right)}$,
where $+(-)$ denotes positive (negative) longitudinal polarization of the target. Using $\Sigma_{1,2,3}$ one can see that for both polarized and unpolarized lepton these asymmetries are given by

$$
\begin{align*}
& \left\langle\frac{\left|P_{h T}\right|}{M_{h}} \sin \phi_{h}\right\rangle(x, y, z)=\frac{\Sigma_{2}(x, y, z)}{\Sigma_{1}(x, y, z)}  \tag{11}\\
& \left\langle\frac{\left|P_{h T}\right|^{2}}{M M_{h}} \sin 2 \phi_{h}\right\rangle(x, y, z)=\frac{\Sigma_{3}(x, y, z)}{\Sigma_{1}(x, y, z)} . \tag{12}
\end{align*}
$$

We use the non-relativistic approximation $h_{1}(x)=g_{1}(x)$, the upper limit from Soffer's inequality [11] $h_{1}(x)=\left(f_{1}(x)+g_{1}(x)\right) / 2$, and the relation between $h_{1 L}^{\perp(1)}(x)$ and $h_{1}(x)$


Figure 2. The $A_{U L}^{\sin \phi_{h}}(x)$ asymmetry of $\pi^{ \pm}$production. The continuous ( $\pi^{+}$) and dashed $\left(\pi^{-}\right)$curves correspond to $M_{C}=0.7 \mathrm{GeV}, h_{1}=g_{1}$; dotted ( $\pi^{+}$) and dot-dashed ( $\pi^{+}$) to $M_{C}=0.3 \mathrm{GeV}, h_{1}=g_{1}$ and $M_{C}=0.7 \mathrm{GeV} h_{1}=\left(f_{1}+g_{1}\right) / 2$, respectively.
[6] obtained by neglecting the interaction dependent twist-three part of the DF and the term proportional to the current quark's mass:
$h_{1 L}^{\perp(1)}(x)=-x^{2} \int_{x}^{1} d y \frac{h_{1}(y)}{y^{2}}$.
We took the parameterisations of DF's $f_{1}(x)$ and $g_{1}(x)$ from Ref. [12]. To calculate the T-odd FF $H_{1}^{\perp(1)}(z)$ we adopt the Collins parameterisation [10] for the analyzing power of transversely polarized quark fragmentation
$A_{C}\left(z, k_{T}\right) \equiv \frac{\left|k_{T}\right|}{M_{h}} \frac{H_{1}^{\perp}\left(z, k_{T}^{2}\right)}{D_{1}\left(z, k_{T}^{2}\right)}=\frac{M_{C}\left|k_{T}\right|}{M_{C}^{2}+k_{T}^{2}}$
and assume a Gaussian parameterisation of the unpolarized FF [8] with $\left\langle z^{2} k_{T}^{2}\right\rangle=b^{2}$ (in the numerical calculations we use $b=0.5 \mathrm{GeV}[13])$. For $D_{1}^{\pi^{ \pm}}(z)$ we use the parameterisation from Ref. [14].

The $A_{U L}^{\sin \phi_{h}}(x)$ asymmetry for $\pi^{ \pm}$production on the proton target is obtained from the defined asymmetry (Eq.(11)) by the relation $A_{U L}^{\sin \phi_{h}} \approx \frac{2 M_{h}}{\left\langle P_{h}\right\rangle}\left\langle\frac{\left|P_{h T}\right|}{M_{h}} \sin \phi_{h}\right\rangle$ and is presented in Fig. 2 in comparison with preliminary HERMES data [2]. The data corresponds to $Q^{2} \geq 1 \mathrm{GeV}^{2}, E_{\pi} \geq 4 \mathrm{GeV}$, and the ranges $0.2 \leq z \leq 0.7,0.2 \leq y \leq 0.8$. The theoretical curves are calculated by integrating over the same ranges with $\left\langle P_{h T}\right\rangle=0.52$ $\mathrm{GeV},\left\langle P_{h T}^{2}\right\rangle=0.35 \mathrm{GeV}^{2}$. These average values of $P_{h T}, P_{h T}^{2}$ are obtained in mentioned kinematics assuming a Gaussian parameterisation of DF's and FF's with $a=0.7 \mathrm{GeV}$ $\left(\left\langle p_{T}^{2}\right\rangle=a^{2}\right)$ [13]. From Fig. 2 one can see that a good agreement with HERMES data [2] can be achieved by varying $h_{1}(x)$ and $M_{C}$. Note that the main effect comes from the $\Sigma_{2 L}$ term, the contribution of $\Sigma_{2 T}$ is about $20 \div 25 \%$.


Figure 3. The ratio of the amplitudes of the $\sin 2 \phi_{h}$ and $\sin \phi_{h}$ single target-spin asymmetries for $\pi^{+}$production. The curves have the same notations as in the Fig. 2.

We calculate the $\sin 2 \phi_{h}$-weighted asymmetry in the same manner as well and show that the amplitude of the $\sin 2 \phi_{h}$ modulation is about a factor of 2-3 smaller than that of the $\sin \phi_{h}$ modulation (see Fig. 3) in the HERMES kinematics. Note that the ratio of these asymmetries is almost independent of the choice of $h_{1}(x)$ and $M_{C}$.

In conclusion, the $\sin \phi_{h}$ and $\sin 2 \phi_{h}$ single target-spin asymmetries of SIDIS off longitudinally polarized protons related to the time reversal odd FF was investigated. It was shown that the main $(1 / Q)$-order contribution to the spin asymmetry arises from intrinsic
$k_{T}$ effects similar to the $\cos \phi_{h}$ asymmetry in unpolarized SIDIS. A good agreement with the HERMES data can be achieved using only the twist-2 DF's and FF's. The $(1 / Q)^{0}$ order $\sin 2 \phi_{h}$ asymmetry, in contrast to the naive expectations, is suppressed comparing to the $(1 / Q)$-order $\sin \phi_{h}$ asymmetry at HERMES kinematics.

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## REFERENCES

1. D. Adams et al., Phys. Lett. B 264 (1991) 462; Phys. Rev. Lett. 77 (1996) 2626; B.E. Bonner et al., Phys. Rev. D 41 (1990) 13.
2. H.R. Avakian, Proceedings of workshop DIS'99, Zeuthen, 19-23 April 1999.
3. A. Bravar, Proceedings of workshop DIS'99, Zeuthen, 19-23 April 1999, Nucleon'99.
4. A.V. Efremov, O.G. Smirnova and L.G. Tkachev, hep-ph/9812522; A.V. Efremov, Proceedings of workshop DIS'99, Zeuthen, 19-23 April 1999.
5. A. Kotzinian, Nucl. Phys. B 441 (1995) 234.
6. P.J. Mulders, R.D. Tangerman, Nucl. Phys. B 461 (1996) 197.
7. R.N. Cahn Phys. Lett. B 78 (1978) 269; Phys. Rev. D 40 (1989) 3107.
8. A. Kotzinian, P.J. Mulders, Phys. Lett. B 406 (1997) 373; Phys. Rev. D 54 (1997) 1229.
9. K.A. Oganessyan, A.R. Avakian, N. Bianchi, A.M. Kotzinian, hep-ph/9808368; Proceedings of workshop Baryons'98, Bonn, Sept. 22-26, 1998.
10. J. Collins, Nucl. Phys. B 396 (1993 161.
11. J. Soffer, Phys. Rev. Lett. 74 (1995 1292.
12. S. Brodsky, M. Burkardt, I. Schmidt, Nucl. Phys. B 441 (1995) 197.
13. E665 Collaboration, M.R. Adams et al., Phys. Rev. D 48 (1993) 5057.
14. E. Reya, Phys. Rep. 69 (1981) 195.

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[^1]:    ${ }^{4}$ More details can be found in [9].

