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A HPMT based set-up to characterize scintillating crystals

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Abstract

We have developed a fully automatic measurement set-up, capable of measuring light yields arising from scintillating crystals in a linear range of about four orders of magnitude. The photodetector is a Hybrid Photomultiplier Tube especially developed to optimize linear range and photon detection. Crystal and photodetector are temperature controlled by a closed water circuit, as this is essential when measuring low light yield scintillating crystals with a marked temperature dependence of their light yield. Gamma sources can be placed either on top or on the side of the crystal. In this latter case, the source can be automatically moved by a computer-controlled step motor to provide a uniformity profile of the light yield along the crystal. Tagged and not-tagged operation modes are possible. The whole set-up is computer-controlled in an effort to provide fast and reliable measurements, to characterize many crystals per day. This is important for the quality control of the Lead Tungstate crystals that will be applied in the electromagnetic calorimeter of the CMS-detector at the LHC at CERN.

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1. INTRODUCTION

The Large Hadron Collider (LHC) at CERN will be equipped with two multipurpose detectors, CMS [1] and ATLAS [2]. For CMS, the electromagnetic calorimeter (ECAL) will be composed of Lead Tungstate (PbWO₄) scintillating crystals [3] read out via Avalanche Photodiodes (APD). The system has to be controlled and monitored in temperature, as the crystal light yield and the APD gain depend on it. The ECAL will contain some 80,000 crystals, with dimensions ~25 x 25 mm² (base) tapering down to 21.5 x 21.5 mm² (top) along the length of 230 mm. These crystal dimensions will slightly vary with the crystal positions in the calorimeter.

Since a few years, an R&D effort is going on to characterize the specific properties of $PbWO_4$ crystals and to aim at a crystal growing procedure able to furnish uniform quality crystals. They all have to be measured in size, optically characterized and proven to be radiation hard. In particular, because of a poor scintillation yield and a low light extraction due to the high index of refraction of $PbWO_4$ (2.16), only 40 to 100 photons per MeV can be extracted on the coupling face to the photon detector. It is essential, therefore, to provide a system, capable of achieving a fast, precise and reliable measurement of $PbWO_4$ light yield.

A few methods [4,5] have been proposed to measure such a poor light yield with a Photomultiplier Tube (PMT) and a ⁶⁰Co gamma source without having to use an electron accelerator. However, these methods mainly involve deconvolving, via computer simulations, the proper total absorption peak from a noisy and cluttered counting spectrum, generated by PbWO₄. The ⁶⁰Co gammas are emitted at 1.170 and 1.330 keV and, at these energies, Compton scatter interactions amount to almost 70 % of the events. To complicate things, as light yield consists of only a few photoelectrons (5 to 15 photoelectrons in the total absorption peak with the present crystals), all of these signals are smeared by Poisson statistics and therefore all of the contributions are mixed with each other. Finally, single electron resolution (SER) in PMTs is low and limits the recognition of photoelectron peaks in the spectra to the pedestal and the first photoelectron, loading absolute calibration of light yield (photoelectrons detected per MeV) with large errors.

Based on these considerations and encouraged by the results obtained in gamma imaging [6,7], we have proposed [8] to apply Hybrid Photomultiplier Tubes (HPMT) [9] to the

detection of scintillations from gamma excited crystals. To this end, we have developed a specially adapted HPMT in collaboration with DEP^1 and we have built an automatic setup, insuring temperature stability, measurement reliability and minimum operator time. In the following, we shall describe the experimental set-up, report the first results and show that the measured spectra can be interpreted and reproduced by a simple analytical model.

2. EXPERIMENTAL SET-UP

The set-up (Fig. 1) consists of a specially developed HPMT as a photodetector, on which the PbWO₄ crystal is placed. The optical contact between the two is ensured by a drop of silicone oil and by the weight of the crystal (~900 g). The crystal and HPMT are surrounded by a closed-circuit water-cooled envelope, which allows stable and adjustable temperatures during measurements. Outside this envelope and sideways with respect to the crystal longitudinal axis a gamma source (⁶⁰Co or ²²Na) excites the scintillator. The longitudinal position of this source with respect to the HPMT can be changed in order to measure the uniformity of crystal response. Collinear to the source, a tagging system is installed. It is made of a conical YAP-crystal and a small-diameter photomultiplier tube. The whole set-up is operated under computer control and automated to optimize performance and minimize operator time. In the following the main set-up elements will be discussed in detail.

2.1 PbWO₄ crystals

In the present phase of development, the size of lead tungstate crystals [1] is $23.8 \times 23.8 \text{ mm}^2$ on the base and $20.5 \times 20.5 \text{ mm}^2$ on the front face and their length is 230 mm. Specific weight is 8.3 g/cm^3 , therefore a crystal weighs 940 g. In the MeV gamma energy range, absorption properties of PbWO₄ can be estimated by properly scaling the lead absorption coefficient curves for photoelectric absorption, Compton scattering and pair production processes. With ⁶⁰Co excitation, cascade of a 1.17 MeV and a 1.33 MeV gamma, about 30% of interactions are photoelectric absorption and 70% are Compton scattering. Since a large fraction of scattered Compton gammas can

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be reabsorbed by the crystal, the fraction of total absorption events can be estimated to be 50% of the overall counts.

 $PbWO_4$ crystals are birefringent. Their emission spectrum ranges between 400 nm and 650 nm, peaking between 450 and 500 nm, according to the different ions used to dope them (Nb, La, etc.). Transmission starts typically around 350 nm and is constant up to 700 nm. Mean refractive index in the emission region is 2.3 [3]. Its light yield is temperature dependent with a - 2% variation per degree centigrade [10].

2.2 HPMT

The working principle of an HPMT has already been described in detail elsewhere [11, 12 and refs therein]. A high resistivity silicon diode faces a suitable photocathode in a vacuum tube. An appropriate electric field accelerates and focuses electrons produced at the photocathode onto the silicon diode, generating electron-hole pairs in a sufficient amount to be detected by proper electronics. The accelerating potential is typically between 10 and 15 kV.

The HPMT employed in this study was developed in collaboration with DEP specifically to measure scintillation light from inorganic crystals (Fig 2). The active surface is 40 mm diameter. A UV-extended S-20 photocathode was evaporated on the 3 mm thick quartz window. This allows for optimum quantum efficiencies in the near UV-blue spectral region and for optimum light collection efficiency, as the window is flat, thin and wide. The 2 mm diameter silicon diode produces little electronic noise, shows excellent single photoelectron resolution (~20% at FWHM) and resolves peaks with sequentially increasing numbers of photoelectrons up to twenty photoelectrons.

2.3 Processing electronics, temperature and computer controls

Signals from the HPMT are first preamplified, then shaped² and stored in a Multi Channel Buffer³ (MCB) which is directly computer controlled. This MCB-card allows for triggered or free running data acquisitions. The ADC is peak sensing with 13 bits resolution. The source, either ⁶⁰Co (20 kBq)- or ²²Na (20 kBq), together with the

² mod. 672 EG&G Ortec

³ mod. 926 EG&G Ortec

tagging unit is shown in Fig. 3. The tagging unit is composed of a truncated conical YAP-crystal (or BGO - crystal) coupled to a Hamamatsu R-1635 photomultiplier tube. Distances between source and PbWO₄ crystal, and source and tagging unit respectively can be varied within well-defined limits, to optimize counting rate and tagging efficiency. The source and tagging unit are displaced along the length of the PbWO₄ crystal by using a spindle, moved by a fully computer controlled step motor. This allows performing an automatic uniformity scan of the PbWO₄ crystal light yield.

Temperature stabilization of the whole unit is achieved with a closed water circuit powered by a cooling unit⁴. It consists of two water-cooled copper boxes, one very close to the crystal (Fig. 1) and another hosting the whole mechanical part of the set-up. A foam and wood box provides the thermal insulation from the environment. Crystal temperature is controlled and stabilized by temperature probes in a feedback loop [10].

The full set-up operation is integrated and controlled by a specially developed Labview⁵ program together with a computer interfacing card⁶.

3. MEASUREMENTS AND RESULTS

3.1 ⁶⁰Co - measurement (tagging off)

At the present production performance, the resulting $PbWO_4$ crystals produce between 5 and 15 photoelectrons per MeV photon energy as measured by the multialkali photocathode of the HPMT. As Compton processes can amount to as much as 70% of the counted events, the main task when analyzing ⁶⁰Co-spectra obtained with $PbWO_4$ crystals is to extract the total absorption peak from the spectrum and to find the average light yield in terms of photoelectrons per MeV. In Fig. 4, a spectrum of $PbWO_4$ ⁶⁰Co-scintillations (crystal #1494) is shown. A first evident advantage of this HPMT system as compared with standard photomultipliers is the presence of photoelectron peaks, which allows for direct and absolute calibration. Gain stability and reproducibility can be therefore controlled on line, saving measurement time and improving precision dramatically. In Fig. 4, pedestal, photoelectron peak one and peak two have been omitted in order to minimize electronics dead time and low energy (Compton,

⁴ Lauda, mod. R6

⁵ National Instruments

⁶ mod. PC+, National Instruments

backscatters, etc.) noise. This could not have been done with a photomultiplier tube, as pedestal position and first photoelectron peak position (the only clearly visible) have to be known precisely.

A uniformity scan consists of moving the ⁶⁰Co source along the crystal axis, taking a spectrum for each position and analyzing it to get the related number of photoelectrons per MeV. Spectra measurements are performed automatically by a computer routine⁷ controlled in turn by the Labview program that supervises the whole scan.

It is possible to choose two types of on-line analysis. The first consists in subtracting the background (Compton) spectrum which is defined by a Region-Of-Interest (ROI) file⁸ and then fitting the remaining spectrum with a Gaussian distribution. Peak and width of the Gaussian are then stored. This works well for crystals emitting more than ~ 10 photoelectrons per MeV, as the separation between the Compton and photoelectric contributions is sufficiently well-resolved. For smaller photoelectron yields and for tagged measurements (see section 3.2), a fit of the entire spectrum is required. The source is then automatically moved to the next position and the data acquisition starts again. According to the count rates and the required precision, an entire scan along the crystal at 21 positions can take as little as 6 minutes with no operator intervention in between. Most of the time is taken to install the crystal on the HPMT and to wait until the chosen temperature is attained.

In Fig. 5, a ⁶⁰Co-scan of PbWO₄ crystal #1858 is shown. This curve shows a parabolalike behaviour: moving the source away from the HPMT, the emitted light suffers increasing absorption losses in the crystal, therefore the light yield decreases. On the other hand, moving the source further away, a larger fraction of light can overcome the total reflection angle cut-off, due to the geometrical shape of the crystals that tends to decrease light incidence angles on the crystal–HPMT interface. Very transparent crystals will show an almost monotonic increase of the light yield versus increasing distance to the HPMT.

In Fig. 6 ⁶⁰Co-scans of PbWO₄ crystal #1494 are shown with pulse shaping varying from 0.1 μ s to 2 μ s. These results clearly show a small loss due to the light decay time of PbWO₄. 90% of the light is collected in 0.1 μ s, indicating a decay time around 30 ns for this crystal.

⁷ Maestro, EG&G Ortec

⁸ A Region Of Interest defines the spectrum interval of interest for the analysis

For the calorimetric application, it is essential to measure the slope of the scan curve (e.g., Figs 5 and 6) in the ~100 mm furthest from the HPMT. This region represents roughly 5 times the anticipated radiation length X_0 , where most (>99%) of the electromagnetic shower takes place (see Table 1). If the slope of the scan curve is too large, the uniformity characteristics of the crystal will have to be modified to obtain a slope smaller than 0.35% per X_0 of PbWO₄. Therefore, the error of the slope measurement must be kept small and, from a statistical analysis of many crystals measured, we estimated a slope error of ~0.2% per X_0 for the set-up.

3.2 ²²Na-measurement (tagging on)

²²Na is a positron emitter with end point energy of 0.54 MeV. The positron emission is followed by a 1.275 MeV gamma emission. Coming to rest within the source, the positron annihilates with an electron thus emitting two collinear 0.511 MeV photons. The principle of the ²²Na measurements is to tag one 0.511 MeV photon, in order to measure scintillations generated by the second 0.511 MeV photon in PbWO₄. Care has been taken to avoid simultaneous measurements of the 0.511 MeV annihilation photons and the 1.275 MeV photons. A certain distance from the PbWO₄ surface is necessary to minimize this effect. However, the source cannot be too far from the crystal in order to get a good counting rate and to avoid edge effects. Two ²²Na spectra taken with tagging on and off are shown in Fig. 7 for a PbWO₄ crystal. The pedestal peak is omitted for both. The improvement in total absorption peak visibility (the peak generated by totally absorbed 0.511 MeV photons) is evident and the resulting spectra can be described by a simple model (see section 4).

A critical aspect with the tagging technique is the choice of the tagging crystal. In our case we mounted a small YAP crystal with high light yield, fast decay time but a very small total absorption cross-section compared with the Compton cross-section, see Table 1 and Fig. 3. We ruled out the use of a BGO crystal because of the poor light yield and slow decay time.

As the number of photoelectrons achievable with a 0.511 MeV gamma in $PbWO_4$ is between 3 to 8, a complete fit of the resulting spectra is needed. This will be the subject of the next section together with a general discussion of the results. In Fig. 8, two ²²Na tagged spectra measured at different temperatures are shown.

4. **DISCUSSION**

The ²²Na spectra in Fig. 8 show a marked discrete structure superimposed on a small continuum. This distribution is nearly Poissonian and each Gaussian peak represents a photoelectron number, with its normalized area P₁ equal to

$$P_i = \frac{(\mu)^i}{i!} e^{-\mu} \qquad \text{and} \qquad \sum P_i = 1 \tag{1}$$

where μ is the average number of photoelectrons and *i* the actual number of detected photoelectrons. The width of these Gaussian peaks is set by the preamplifier electronic noise added in quadrature with the equivalent capacitive diode noise. As discussed in previous papers (see for example [11]), the diode noise is much smaller than the preamplifier noise. The total noise will therefore not depend in first approximation on the square root of *i* as it does in the case of photomultiplier tubes.

The deviation from a proper Poissonian distribution, characterized by the small continuum, visible between and under the peaks, can be fully accounted for by the backscattering of photoelectrons from the silicon diode. In fact, there is a finite probability (~20 %) that a 15 keV photoelectron is backscattered from the silicon diode surface. In doing so, the photoelectron leaves on average about 60 % of its energy in the diode, with a distribution that spans between 0 and 100 % of the photoelectron energy [13].

To fit the experimental spectra in Fig 8, let us start with a first approximation of the "intrinsic" $PbWO_4$ scintillation spectrum due to ²²Na 511 keV gamma excitation. This can be roughly approximated by the distribution in Fig. 9.

Every time the 511 keV gamma energy is totally absorbed, $\langle n_{\gamma} \rangle$ photoelectrons will be produced from the photocathode on average. Compton scattering on the other hand is responsible for the continuum that starts at zero and ends at the Compton edge energy, given by

$$\langle n_c \rangle = \frac{\langle n_{\gamma} \rangle}{1 + m_0 c^2 / 2E_{\gamma}} \tag{2}$$

As $\langle n_{\gamma} \rangle$ in PbWO₄ is small, the intensity distribution of measured photoelectrons follows a Poissonian distribution given by Eq. 1 for the total absorption peak,

$$P_i\left(\langle n_{\gamma} \rangle\right) = \frac{\left(\langle n_{\gamma} \rangle\right)^i}{i!} e^{-\langle n_{\gamma} \rangle}$$
(3)

where $P_i(\langle n_\gamma \rangle)$ gives the probability of measuring *i* photoelectrons.

To obtain the equivalent expression for the Compton distribution, we have to convolve the square distribution C(x) in Fig. 9 with the Poissonian distribution, that is

$$P_{c_i}(\langle n_c \rangle) = \frac{1}{f_c} \int_0^{\langle n_c \rangle} C(x) P_i(x) dx \quad \text{where} \quad f_c = \int_0^{\langle n_c \rangle} C(x) dx \tag{4}$$

which is still $\sum P_{c_i}(< n_c >) = 1$

Eq. 4 can be solved to give

$$P_{c_i}(< n_c >) = P_{c_{i-1}}(< n_c >) - \frac{P_i(< n_c >)}{< n_c >} \quad \text{and} \quad P_{c_0}(< n_c >) = \frac{1 - e^{-< n_c >}}{< n_c >} \quad (5)$$

with $P_i(< n_c >) = \frac{(< n_c >)^i}{i!} e^{-<n_c >}$ being the Poisson distribution for $< n_c >$.

The resulting spectrum is the weighted sum of total absorption events and Compton events,

$$P_{T_i} = (1 - f_c) P_i(\langle n_{\gamma} \rangle) + f_c P_{c_i}(\langle n_c \rangle) \quad \text{for all } i$$
(6)

Here, $\langle n_{\gamma} \rangle$ is the average number of photoelectrons produced on the photocathode of the HPMT. To obtain now the measured spectrum, we have to again convolve Eq.3 and the set of Eqs 5, first with the backscattering distribution and then with the preamplifier electronic noise shaping function. As we essentially follow equations 5 through 7 in reference [11] for these two steps, we refer to that paper for a detailed discussion. Finally, the result has to be added together as in Eq. 6, where $P_i(\langle n_{\gamma} \rangle)$ and $Pc_i(\langle n_{\gamma} \rangle)$ are now the product of three convolution steps.

The spectrum resulting from all the previous transformations is shown in Fig. 10, together with its total absorption and Compton continuum contributions. It is worth noting the effect of Poisson statistics on the sharp edge of the Compton distribution in Fig. 9, which is now completely smeared out. In Figs 11a,b, comparisons between a

measured spectrum and a calculated spectrum for tagged ²²Na excitation and for ⁶⁰Co excitation are shown respectively. Due to the backscattering process, the average number of measured photoelectrons is lower by a factor ~0.85 from the average number of photoelectrons produced at the photocathode (compare Figs 4 and 11b). Note also that for the ²²Na spectrum, the Compton fraction of events is only ~25%, but the two contributions overlap considerably. On the contrary, in the case of ⁶⁰Co excitation, the resulting Compton fraction is ~50 %, but the total absorption peak is at double the photoelectron number. In Fig. 12, the ratio between ⁶⁰Co and ²²Na scans is shown. It shows the good agreement between the two experimental methods. However, for crystals with a light yield larger than ~10 photoelectrons per MeV, ⁶⁰Co measurements are easier and much faster to perform. For lower light yield values ²²Na tagged measurements will be necessary to achieve the required slope precision.

CONCLUSIONS

We have developed and operated a new set-up, which measures light yields from scintillating crystals. Based on a specially developed HPMT, completely automatic and temperature controlled, this set-up features fast, reliable and precise scintillation measurements. Gain stability and reproducibility can be controlled on line, saving on measurement time and improving precision. In particular, this set-up was constructed to characterize the scintillation performance of PbWO₄ crystals, as they will be used in the electro-magnetic calorimeter of the CMS detector at CERN. It provides two modes of operation (tagged and not tagged), which prove to be useful when the crystal light yield is lower or larger than 10 photoelectrons per MeV, respectively. The evaluation of the crystal light yield can be achieved with a fitting routine based on a simple analytical model and, therefore, it can be performed on-line and in a very short time (a few seconds) even with a small personal computer.

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| Material | NaI(Tl) | CsI | BGO | PbWO ₄ | YAP(Ce) | CeF ₃ |
|--------------------------------------|---------|------|------|-------------------|---------|------------------|
| Density [g/cm ³] | 3.67 | 4.51 | 7.13 | 8.28 | 5.37 | 6.16 |
| Radiation length X ₀ [cm] | 2.59 | 1.85 | 1.12 | 0.89 | 2.7 | 1.68 |
| Light decay time [ns] | 230 | 16 | 300 | 15 | 27 | 25 |
| Refractive index | 1.85 | 1.80 | 2.20 | 2.16 | 1.95 | 1.62 |
| Maximum of emission [nm] | 410 | 315 | 480 | 440 | 365 | 300, 340 |
| Temperature coeff. [%/°C] | ~0 | -0.6 | -1.6 | -2 | ~0 | 0.14 |
| Relative light output | 100 | 20 | 15 | 1.3 | 40 | 8 |

Table 1: Properties of several inorganic crystal scintillators [3]



Fig. 1: Components of the set-up



accelerating potential between 5 kV and 15 kV

Fig. 2 Thin quartz window HPMT (mod. PPO 470 A)



Fig 3: Tagging unit layout.



Fig. 4: ⁶⁰Co spectrum, measured using PbWO₄ crystal # 1494.



Fig. 5: Scan of PbWO₄ crystal #1858 at different excitation positions with laterally arranged 60 Co source. The crystal response in photoelectrons at the total absorption peak is represented as a function of the source distance from the HPMT.



Fig. 6: Non-uniformity plots of PbWO₄ crystal #1494, realised at different shaping times.



Fig. 7: ²²Na spectra realised with tagging off (continuous line) and tagging on (dashed line). Counting rates are different between tagged and not tagged spectra (depending on the geometrical arrangement, between 10 and 20 times lower counting rates for tagged measurements have to be expected). Therefore, the respective acquisitions have been stopped in order to equal the counts of the spectra between channels 300 and 500. In spite of the much lower counting rate, the tagged spectrum shows no background counts at low energies, contrary to the non tagged spectrum, where most of the counts are background-related (especially for the first and second phel. peaks).



Fig. 8: ²²Na spectrum realized with PbWO₄ crystal #1584 at different temperatures (14°C and 26°C); the light yield decreases with increasing temperature at a rate of ~2% per °C giving an average of 4.45 photoelectrons at 18 °C and 3.60 at 26 °C.



Fig. 9: Approximated energy spectrum of the interaction in $PbWO_4$ of ²²Na 511 keV photons.



Fig. 10: Example of ^{22}Na spectrum simulation. Note the calculated energy distribution components - Compton (a) and photoelectric (b) - which have been taken into account in the program and their sum (c) (Eq.6). The photoelectric fraction of events is 0.75 and the average number of photoelectrons $<\!n_{\gamma}\!>$ is 6.0. $<\!n_c\!>=2/3<\!n_{\gamma}\!>$ is calculated from Eq.2 .



Fig. 11a: ²²Na spectrum of crystal #1584 compared with its fit. The Region Of Interest was chosen in order to not account in the simulation of the low energy backgrounds.



Fig. 11b: ⁶⁰Co spectrum of crystal #1808 compared with its fit. The Region Of Interest was chosen in order to not account in the simulation of the low energy backgrounds.



Fig. 12 : Ratio between 60 Co scan and 22 Na tagged scan with the same crystal (#1858).