Strange Messages: Chemical and Freeze-out in Nuclear Collisions Thermal

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single particle spectra and two-particle correlation measurements is pointed out. A in nuclear collisions. The crucial role of correlating strangeness production data with an initial prehadronic stage with deconfined color and with an appreciable isotropic model analyses and review the experimental and theoretical evidence for thermalization out in heavy-ion collisions. I discuss the usefulness and limitations of such thermal particle yields and spectra and to extract the conditions of chemical and thermal freezepressure component. This requires an early onset of thermalization. consistent dynamical picture for the heavy-ion data from the CERN SPS Abstract. Thermal models are commonly used to interpret heavy-ion data on involves

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1. Introduction

phase transition accompanying its hadronization. others that we succeeded in creating the quark-gluon plasma (QGP) and observing the thermodynamic equilibrium. The application of thermal and hydrodynamic models to dynamics, it is rather a necessity for everybody who wants to convince himself and relativistic heavy-ion data is therefore more than a poor man's approach to heavy-ion be reasonably well defined if the system under study is in a state of approximate local thermodynamic language. A phase transition from an initial color-deconfined QGP to a the search for the quark-gluon plasma (QGP). The discussion of a phase diagram requires the phase diagram of strongly interacting matter at high temperatures and densities and color-confined hadronic state (as it is supposed to occur in heavy-ion collisions) can only The stated goal of the relativistic heavy-ion programs at CERN and BNL is the study of

good for qualitative answers; on a more detailed and quantitative level, the failure scales which are comparable to the microscopic thermalization time. the thermodynamic approach, and they undergo a strong dynamical evolution on time systems are small, causing corrections to the infinite volume limit usually assumed in therefore can never provide more than a rough picture of the bulk of the phenomena, level of detail when applied to heavy-ion data. The reason is obvious: the collision Of course, the models may fail; in fact, they must *necessarily* fail beyond a certain Thermal models

of the thermal model will become manifest, and traces of genuine QCD dynamics (as opposed to thermodynamics) will show up. But when trying to assess bulk phenomena like QGP formation, we are not (in fact, we must not be) primarily interested in these deviations from thermodynamic behaviour and the traces of elementary QCD dynamics; the latter can be studied much more easily and cleanly in elementary lepton or hadron collisions. We should rather concentrate on the rough global pattern of the data and try to understand them within a (nota bene: sufficiently sophisticated, see below) thermoand hydrodynamic approach. On the other hand, if it turns out that not even the rough qualitative features of the data can be understood in this way and detailed hadronic dynamics is required even for a superficial understanding of the observations, then we should concede that our attempt to create "hot QCD matter" has failed.

Having argued in favor of a "simple" thermal approach to heavy-ion data, the next questions to be addressed are (i) the level of sophistication which the thermal model should have before being applicable to the description of particle production in nuclear collisions, (ii) which level of agreement between model and data can at best be expected, and (iii) where to draw the line between agreement and disagreement when comparing model and data. This is what this contribution is about. At the end I will try to draw some conclusions about what we have learnt so far from the thermal analysis of heavy-ion data, and which further steps should be taken.

2. Two types of "thermal" behaviour

"Thermal" behaviour can arise in *conceptually different* ways, with different meanings of the "temperature" parameter T. For us the two most important variants of "thermal" behaviour are the following:

1. The statistical occupation of hadronic phase-space with minimum information. The latter is in practice provided by external constraints on the total available energy E, baryon number B, strangeness S and, possibly, a constraint λ_s on the overall fraction of strange hadrons. "Thermal" behaviour arises in this case via the Maximum Entropy *Principle* in which the "temperature" T and "fugacities" $e^{\mu_b/T}$, $e^{\mu_s/T}$ (which in the canonical approach are replaced by so-called "chemical factors" [1, 2]) occur as Lagrange multipliers for the constraints. Examples are nucleon emission from an evaporating compound nucleus in low-energy nuclear physics and hadronization in e^+e^- , pp and $p\bar{p}$ collisions (hadron yields [1, 2] and m_{\perp} -spectra [3]). The number of parameters to fit the data in such a situation is equal to the number of "conserved quantities" (constraints), and it reflects directly the information content of the fitted observable(s). This type of "thermal" behaviour requires no rescattering and no interactions among the hadrons, there is no isotropic pressure and no collective flow in the hadronic final state and, in fact, the concept of *local* equilibrium can *not* be applied. Of course, this type of "thermal" behaviour is not really what we are interested in in heavy ion collisions, except as a baseline against which to differentiate interesting phenomena.

2. Thermalization of a non-equilibrium initial state by kinetic equilibration (rescattering). This does require (strong!) interactions among the hadrons. Here one must differentiate between thermal equilibration (reflected in the shape of the momentum spectra), which defines the temperature T, and chemical equilibration (reflected in the particle yields and ratios) which defines the chemical potentials in a grand canonical description. The first is driven by the total hadron-hadron cross section while the second relies on usually much smaller inelastic cross sections and thus happens more slowly. This type of equilibrium is accompanied by pressure which drives collective flow (radial expansion into the vacuum as well as directed and elliptic flow in non-central collisions). In heavy ion collisions it is realized at most locally, in the form of local thermal and/or chemical equilibrium – due to the absence of confining walls there is never a global equilibrium. This is the type of "thermal" behaviour which we are searching for in heavy-ion collisions.

I stress that flow is an unavoidable consequence of this type of equilibration. Thermal fits without flow to hadron spectra are not consistent with the kinetic thermalization hypothesis. Flow contains information; it is described by three additional fit parameters $\vec{v}(x)$. This information is related to the pressure history in the early stages of the collision and thereby (somewhat indirectly) to the equation of state of the hot matter.

Most thermal fits work with global parameters T and μ which, at first sight, appears inconsistent with what I just said. Here the role of freeze-out becomes important: freezeout cuts off the hydrodynamical evolution of the thermalized region via a kinetic freezeout criterium [4] which involves the particle densities, cross sections and the expansion rate. In practice freeze-out may, but need not occur at nearly the same temperature everywhere [4].

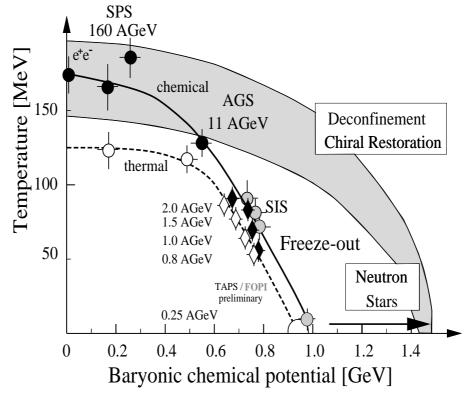
Clearly a thermal fit to hadron production data (if it works) is not the end, but rather the beginning of our understanding. One must still check the *dynamical* consistency of the fit parameters T_f , μ_f , \vec{v}_f : can one find equations of state and initial conditions which yield such freeze-out parameters? Which dynamical models can be excluded?

3. The hadronic phase diagram

In figure 1 I show a recent version of the phase diagram for strongly interacting matter, with various sets of data points included [5, 6, 7, 8, 9]. In the present section I discuss the meaning of this figure and explain how these data points were obtained. In the next section I will discuss some problems connected with the extraction procedures.

3.1. Chemical freeze-out

3.1.1. e^+e^- and pp collisions. Let me begin with the e^+e^- data point in figure 1. (There is also a pp point from Ref. [2] which was omitted for clarity.) In spite of Figure 1. Compilation of freezeout points from SIS to SPS energies. Filled symbols: chemical freeze-out points from hadron abundances. Open symbols: thermal freeze-out points from momentum spectra and two-particle correlations. For each system, chemical and thermal freeze-out were assumed to occur at the same value μ_B/T . The shaded region indicates the parameter range of the expected transition to a QGP.



what I said about case 1. above, a "thermal" analysis of hadron yields in elementary collisions [1, 2] is still interesting. (Of course, in this case the canonical formalism must be used, due to the small collision volume.) The interest arises *a posteriori* from the observed universality of the fit parameters, namely a universal "hadronization" or "chemical freeze-out" temperature $T_{\rm chem} = T_{\rm had} \approx 170$ MeV (numerically equal to the old Hagedorn temperature $T_{\rm H}$ and consistent with the inverse slope parameter of the m_T -spectra in pp collisions [3]), and a universal strangeness fraction $\lambda_s = 2\langle \bar{s}s \rangle / (\langle \bar{u}u \rangle + \langle \bar{d}d \rangle)|_{\rm produced} \approx 0.2-0.25$, almost independent of \sqrt{s} [1, 2, 10].

This is most easily understood [2] in terms of a universal critical energy density $\epsilon_{\rm crit}$ for hadronization which, via the Maximum Entropy Principle, is parametrized by a universal "hadronization temperature" $T_{\rm had}$ and which, according to Hagedorn, characterizes the upper limit of hadronic phase-space. Supporting evidence comes from the observed increase with \sqrt{s} of the fitted fireball volume V_f (which accomodates the increasing multiplicities and widths of the rapidity distributions). Although higher collision energies result in larger *initial* energy densities ϵ_0 , the collision zone subsequently undergoes more (mostly longitudinal and not necessarily hydrodynamical) expansion until $\epsilon_{\rm crit}$ is reached and hadron formation can proceed. The systematics of the data can only be understood if hadron formation at $\epsilon > \epsilon_{\rm crit}$ (i.e. $T > T_{\rm H}$ for

the corresponding Lagrange multipliers) is impossible. With this interpretation, the chemical analysis of e^+e^- , pp and $p\bar{p}$ collisions does provide one point in the T- μ_b phase diagram (see figure 1). – The only "childhood memory" of the collision system is reflected in the low value of λ_s , indicating suppressed strange quark production (relative to u and d quarks) in the early pre-hadronic stages of the collision.

3.1.2. AA collisions: strangeness enhancement. In this light the observation [5] of a chemical freeze-out temperature $T_{\text{chem}} \approx T_{\text{H}} \approx 170$ MeV in heavy-ion collisions with sulphur beams at the SPS (figure 1), taken by itself, is not really interesting. It suggests that in heavy-ion collisions hadronization occurs via the same statistical hadronic phase-space occupation process as in pp collisions. What is interesting, however, is the observation [10, 11] that the global strangeness fraction $\lambda_s \approx 0.4-0.45$ in AA collisions is about a factor 2 larger than in e^+e^- and pp collisions. If pp and S+A collisions hadronize via the same mechanism, and in S+A collisions the Maximum Entropy particle yields fixed at T_{had} are not modified by inelastic hadronic final state rescattering, this increase in λ_s must reflect a difference in the properties of the prehadronic state! In nuclear collisions the prehadronic stage allows for more strangeness production, most likely due to a longer lifetime before hadronization.

It was noted before [10, 11] that the global strangeness enhancement occurs already in collisions between medium size nuclei (S+S) and remains roughly unchanged in Pb+Pb collisions. In this conference we saw data from the WA97 collaboration [12, 13, 14] which provide two important further details:

1. While the bulk of the strangeness enhancement from p+Pb to Pb+Pb collisions is carried by the kaons and hyperons (Λ, Σ) , which are enhanced by about a factor 3 near midrapidity, the enhancement is much stronger for the doubly and triply strange baryons Ξ and Ω and their antiparticles, with an enhancement factor of about 17 (!) for $\Omega + \overline{\Omega}$ at midrapidity. The enhancement clearly scales with the strangeness content [13], as naively expected in statistical and thermal models, but in stark contradiction to expectations based on the consideration of the respective production thresholds in hadronic (re)interactions.

2. In semicentral Pb+Pb collisions the enhancement grows linearly with the number of participating nucleons in the collision, so the enhanced yield of all measured strange hadron species per participating nucleon is *independent of the effective size of the colliding system* from about 150 to 400 participants [12]. Where comparison is possible, this systematics even carries over to central S+S collisions [14] with as few as 55-60 participating nucleons. So whatever causes the enhancement in Pb+Pb collisions (e.g. the existence of a color-deconfined prehadronic stage) is not particular to (semi)central Pb+Pb collisions, but exists already in S+S collisions! I will return to the Aindependence of this effect below.

At most half of the 100% increase of global strangeness production in AA collisions can be explained [15] by the removal of canonical constraints in the small e^+e^- and pp collision volumes (which would be an interesting observation in itself because it would already imply that in nuclear collisions hadron production and the conservation of quantum numbers occurs no longer on nucleonic, but indeed on nuclear length scales). The remainder of the increase must be due to extra strangeness production in the whole fireball volume *before* hadronization. It is interesting to analyze in the same way the strong $\Omega + \bar{\Omega}$ enhancement in Pb+Pb (by a factor 17 relative to p+Pb [13]): of course, the Ω (carrying 3 units of strangeness) suffers a particularly strong canonical suppression due to exact strangeness conservation in the small hadronization volume of a pp (or p+Pb) collision; for $T_{had} \simeq 170 \text{ MeV}$, $\gamma_s = 0.5$ and $V = 17.6 \text{ fm}^3$ (as obtained by fitting pp data at $\sqrt{s} = 27 \text{ GeV}$ [2]) $\Omega + \bar{\Omega}$ are canonically suppressed by a factor 12 relative to a grand canonical treatment [16]. Again the observed enhancement effect in Pb+Pb collisions is considerably larger than expected from a simple removal of the canonical constraints.

The observed strangeness fraction $\lambda_s = 0.45$ in nuclear collisions corresponds to a strangeness saturation coefficient [17] $\gamma_s \approx 0.7$ [10]. On the other hand, a value of $\gamma_s \approx 0.7$ in the hadronic final state may, in fact, be the upper limit reachable in heavy-ion collisions [15] because the corresponding strangeness fraction agrees with that in a fully equilibrated QGP at $T_{\text{had}} \approx 170$ MeV. If both strangeness and entropy are conserved or increase similarly during hadronization, $\gamma_s \approx 0.7$ in the Maximum Entropy particle yield after hadronization would be a universal consequence of a fully thermally and chemically equilibrated QGP before hadronization [15]. The SPS data would then be completely consistent with such a prehadronic state.

The existence of a prehadronic stage without color confinement, both in S+S and Pb+Pb collisions at the SPS, is also suggested by an analysis of baryon/antibaryon ratios of different strangeness. This was stressed at this conference by A. Bialas [18] who redid this analysis with the new data following the ideas of Rafelski [17].

According to figure 1 chemical freeze-out in sulphur-induced collisions at the SPS appears to occur *right at the critical line*, i.e. immediately after hadronization. The SIS data, on the other hand, indicate much lower chemical freeze-out temperatures. The origin of this is probably due to longer lifetimes of the reaction zone at lower beam energies, allowing for some chemical re-equilibration by inelastic hadronic reactions.

A tendency for some chemical re-equilibration after the hadronization of the proposed pre-hadronic stage may also be visible in the still preliminary Pb+Pb data at the SPS: although thermal model analyses of these data still give wildly scattering results [10, 7, 19], some authors [19] find chemical freeze-out temperatures in Pb+Pb below 140 MeV. A thermal model analysis of RQMD simulations also gives chemical freeze-out temperatures of 172 MeV in S+S, but of only 155 MeV in Pb+Pb collisions [20]. Both analyses show a characteristic failure to reproduce the Ω and $\overline{\Omega}$ yields [12]. This was interpreted [20, 21] in terms of early freeze-out of these triply strange baryons due to their small interaction cross sections with other types of hadrons. It is interesting to observe that in the thermal analysis of the data [19] the model underpredicts the measured Ω and $\overline{\Omega}$ yields (which prefer a higher freeze-out temperature $T \geq 170$ MeV [7, 10]) while in RQMD, which is known to produce too few Ω and $\overline{\Omega}$ baryons in pp and

pA collisions, the thermal model *overpredicts* the simulated yields. All this points to the Ω and $\overline{\Omega}$ as relatively early hadronic messengers, and the message they seem to carry in the Pb+Pb *data* is again that of the existence of a prehadronic stage with enhanced global strangeness which hadronizes statistically at $T_{\text{had}} = T_{\text{H}} \simeq 170 \text{ MeV}$.

3.2. Flow and thermal freeze-out

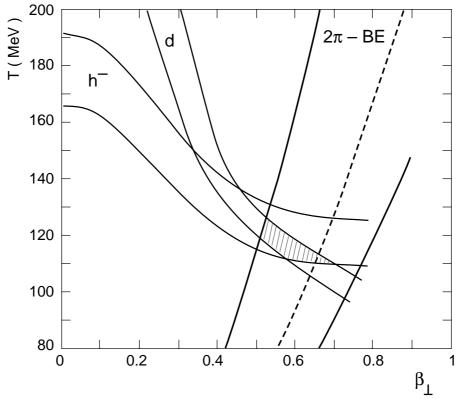
The other important observation in the hadronic sector of nuclear collisions is that of collective flow (radial expansion flow, directed and elliptical flow). It is usually extracted from the shape of the single-particle momentum distributions. Radial flow, for example, leads to a flattening of the m_{\perp} -spectra. For the analysis one must distinguish two domains. In the relativistic domain $p_{\perp} \gg m_0$ the inverse slope $T_{\rm app}$ of all particle species is the same and given by the blueshift formula [4] $T_{\rm app}=T_f\sqrt{(1+\langle v_{\perp}\rangle)/(1-\langle v_{\perp}\rangle)}$. This formula does not allow to disentangle the average radial flow velocity $\langle v_{\perp}\rangle$ and freezeout temperature T_f . In the non-relativistic domain $p_{\perp} \ll m_0$ the inverse slope is given approximately by $T_{\rm app}=T_f+m_0\langle v_{\perp}^2\rangle$, and the rest mass dependence of the "apparent temperature" (inverse slope) allows to determine T_f and $\langle v_{\perp}^2\rangle$ separately. (In *pp* collisions no m_0 -dependence of $T_{\rm app}$ is seen [22].) Plots of $T_{\rm app}$ against m_0 were shown in several talks at this conference, showing that the data follow very nicely this systematics, from SIS to SPS energies.

A notable exception are the Ω -spectra of WA97 [12] which are steeper than expected from this formula. Again, as in the above discussion of their abundance, this reflects their character as "early hadronic messengers" [21]: the Ω and $\overline{\Omega}$ are the only baryons which (due to quantum number mismatch) do not have a strong resonance with pions, the most abundant particles in the fireball. Since resonance scattering is the most efficient thermalization mechanism in a dense hadronic system, the Ω and $\overline{\Omega}$ momentum distributions freeze out earlier than those of all other baryons. This implies [21] that they cannot efficiently pick up the collective transverse flow which builds up among the pions in the later stages of the expansion, and their spectra reflect the much weaker collective transverse flow in the early collision stages, just after hadron formation.

[This also illustrates the important role of the baryon contamination in the hot fireball: in Pb+Pb collisions at the SPS the pion and baryon spectra decouple late and cool down to rather low temperatures of about 120 MeV (see below) because the pions are "glued" together by the baryons via resonance scattering. At RHIC this glue will be less efficient since near midrapidity there will essentially exist only baryon-antibaryon pairs at rather low thermal equilibrium abundances. It is thus expected that at RHIC thermal decoupling occurs at somewhat higher freeze-out temperatures, closer to the hadronization phase transition.]

The separation of collective flow and random thermal motion from an analysis of single particle spectra is not uncontroversial. The main reason is that the fitted values for T and v_{\perp} tend to be strongly correlated. To break the correlation one must study spectra of hadrons with different masses in the low- p_{\perp} region which, on the other hand,

Figure 2. Thermal freeze-out temperature and transverse flow velocities extracted from fits to the transverse momentum spectra of negative hadrons (h^-) and deuterons (d) and to the transverse HBT radius $(2\pi$ -BE). The shaded area indicates the overlap region near $T_{\text{f.o.}} \approx 120 \text{ MeV}$ and $v_{\perp} \approx 0.55 \text{ c}$. (From Ref. [24].)



is contaminated by post-freeze-out resonance decays. As a consequence, fits done in different p_{\perp} windows tend to give different results.

A clearer determination of the transverse collective flow comes from a direct measurement of the flow-induced space-momentum correlations via the M_{\perp} -dependence of the two-pion HBT radii [23]. As shown in [24, 25] the correlations between temperature and transverse flow in a fit of the single particle transverse momentum spectra and of the transverse two-particle HBT radii are essentially orthogonal to each other (see figure 2), and the combined analysis of spectra and correlations allows for a clean separation of random thermal motion from collective flow.

This analysis [24, 25] gave rise to the open circle for the SPS data in figure 1, indicating the point of thermal decoupling in 158 A GeV/c Pb+Pb collisions $(T_{\text{therm}} \approx 120 \text{ MeV}, \langle v_{\perp} \rangle \approx 0.5 c)$. It is consistent with a comparison of the spectral slopes for different mass hadrons by Kämpfer [26]. Earlier analyses of S+S data [27] showed a thermal decoupling at $T_{\text{therm}} \approx 140 - 150 \text{ MeV}, \langle v_{\perp} \rangle \approx 0.25 - 0.35 c$. The open circle for the AGS as well as the open quadrangles for the SIS in figure 1 were obtained similarly as in [26, 27] by comparing transverse momentum spectra of particles with different masses (see [7, 8] for references). All open symbols correspond to heavy collision systems (Pb+Pb, Au+Au). The dashed line connects them by eye in an attempt to construct a "thermal freeze-out curve" for heavy-ion collisions of size 200+200.

It is interesting to analyze the A-dependence of the various hadronic observables, i.e. of strangeness enhancement, chemical and thermal freeze-out temperatures and radial transverse flow. This discussion should include the available information on the impact parameter dependence in Pb+Pb collisions since collisions at different impact parameters also involve different numbers N_{part} of participating nucleons. Whereas the freeze-out temperatures (certainly the thermal freeze-out temperature, but perhaps also the chemical one, see above) seem to come down with increasing size of the collision system, while at the same time the strength of the radial transverse flow goes up, the strangeness enhancement (i.e the strange particle production per participating nucleon relative to pp and pA collisions) appears to be independent of the number of N_{part} , at least in the range $60 \le N_{part} \le 400$. The buildup of radial flow is largely (although not exclusively) a hadronic reinteraction phenomenon [21]; the same is true for the freezeout process. The N_{part} -dependence of both features can be explained in terms of the longer lifetime of the reaction zone as N_{part} increases, giving the system more time to re-equilibrate, cool down and develop collectivity.

In contrast, the A-independence of the strangeness enhancement features suggest that they are not due to hadronic re-interactions, but originate in a prehadronic phase with properties which are essentially independent of the system size once $N_{\text{part}} \ge 50$ or so. My interpretation of these facts is that at SPS energies the energy density threshold for QGP has been overcome by a sizeable margin [28], and that even in small collision systems a deconfined phase is created which interacts sufficiently long and sufficiently strongly to approximately saturate strangeness production. One can even argue that isotropic pressure (a signature of local thermalization) must be present at this early stage [28], and that the observed elliptic flow in non-central Pb+Pb collisions [29] actually signals this early pressure [30]. A future systematic investigation also of the range $1 < N_{\text{part}} < 100$ would be very useful to study the onset and saturation of thermal and collective behaviour as the size and lifetime of the collision system increases. It will *not*, however, be an efficient method to study the onset of deconfinement – for that one must go to *lower* beam energies.

4. Limitations of thermal model analyses

After having explained how the data points in figure 1 were obtained, I would now like to ask the notorious David Mermin question [31] "What's wrong with this phase diagram?" In other words, I want to point out in more detail certain unavoidable problems with thermal model analyses of heavy-ion data. Only by remaining conscious of the limitations of the thermal approach and avoiding the overinterpretation of uncontrollable details one can fully exploit its power in providing essential qualitative insight into the physics of heavy-ion collisions.

4.1. Rapidity dependence of particle ratios

The first problem is of purely practical nature: no heavy-ion experiment so far has full 4π acceptance for identified particles, and particle spectra are available in restricted windows of p_{\perp} and y only. The observed nearly exponential form of the p_{\perp} -spectra allows for an extrapolation of the yields to the full transverse momentum range without introducing large uncertainties (at least if the acceptance covers sufficiently low values of p_{\perp}). A similar extrapolation of the rapidity spectra is not possible: even in a system which is in perfect local thermal equilibrium, particles with different masses tend to have strongly different rapidity distributions. In practice these differences in the shape of the rapidity spectra are even stronger, in the sense that even particles and antiparticles (with obviously identical masses) have different rapidity distributions. Thus there is essentially no way of extrapolating the rapidity distributions without really measuring them.

That this is a serious problem for thermal model analyses is illustrated by the following example: consider a stationary, spherical fireball in global thermodynamic equilibrium. It emits hadrons with the following rapidity distributions:

$$\frac{dN_i}{dy} \sim e^{-m_i \cosh y/T} \left[1 + 2\frac{T}{m_i \cosh y} + 2\left(\frac{T}{m_i \cosh y}\right)^2 \right]$$
(1)

These resemble Gaussians with widths $\Gamma_i \approx 2.35 \sqrt{\frac{T}{m_i}}$ (the approximation being valid for $m_i \gg T$). Clearly, the particle ratios $(dN_i/dy)/(dN_j/dy)$ then depend strongly on the position of the rapidity interval dy: away from y = 0 heavy particles will be much more strongly suppressed relative to light particles than near y = 0. In this case a measurement of particle yields in a small rapidity window is completely useless for a thermal model analysis (irrespective of whether the window is located near y = 0 or at $y \neq 0$) unless it is known a priori that the radiator is a stationary spherical fireball.

The presence of (strong) longitudinal flow in relativistic heavy-ion collisions does not help very much in this connection; only in the limit of infinite beam energy with exact longitudinal boost-invariance due to Bjorken scaling, resulting in flat rapidity distributions, is it possible to base a thermal analysis on data in a finite, narrow rapidity interval. At SPS energies and below, where Bjorken scaling is not observed, thermal fits of data in finite rapidity windows require that the thermal model yields are cut to the actual experimental acceptance; this induces serious dependences on the detailed model assumptions, for example about the strength and profile of the longitudinal and transverse flow of the source. This model-dependence was recently studied in some detail in Ref. [32].

Flow effects drop largely out, however, if one works with particle ratios obtained from 4π yields. (Please note that this requires a *measurement* of some sort, not a blind extrapolation of data from a small window in y and p_{\perp} to full momentum space!) The insensitivity to hydrodynamic flow becomes exact if the freeze-out temperature and chemical potential is everywhere the same. If freeze-out occurs on a sharp hypersurface Strange Messages: Chemical and Thermal Freeze-out in Nuclear Collisions

 Σ , the total yield of particle species *i* is then given by

$$N_{i} = \int \frac{d^{3}p}{E} \int_{\Sigma} p^{\mu} d^{3}\sigma_{\mu}(x) f_{i}(x,p) = \int_{\Sigma} d^{3}\sigma_{\mu}(x) j_{i}^{\mu}(x) , \qquad (2)$$

where

$$j_i^{\mu}(x) = \int d^4 p \, 2\theta(p^0) \delta(p^2 - m_i^2) \, p^{\mu} \frac{g_i}{e^{[p \cdot u(x) - \mu_i]/T} \pm 1} \tag{3}$$

is the number current density of particle species *i*. In thermal equilibrium it is given by $j_i^{\mu}(x) = \rho_i(x) u^{\mu}(x)$ with

$$\rho_{i}(x) = u_{\mu}(x)j_{i}^{\mu}(x) = \int d^{4}p \, 2\theta(p^{0})\delta(p^{2} - m_{i}^{2}) \, p \cdot u(x) \, f_{i}(p \cdot u(x); T, \mu_{i})$$

= $\int d^{3}p' \, f_{i}(E_{p'}; T, \mu_{i}) = \rho_{i}(T, \mu_{i}).$ (4)

Here $E_{p'}$ is the energy in the local rest frame at point x. The total particle yield of species *i* is therefore

$$N_{i} = \rho_{i}(T, \mu_{i}) \int_{\Sigma} d^{3}\sigma_{\mu}(x)u^{\mu}(x) = \rho_{i}(T, \mu_{i}) V_{\Sigma}(u^{\mu})$$
(5)

where only the total comoving volume V_{Σ} of the freeze-out hypersurface Σ depends on the flow profile u^{μ} . Thus the flow pattern drops out from ratios of 4π yields which therefore depend only on T and the chemical potentials. These considerations are easily generalized to "fuzzy freeze-out" (i.e. freeze-out from a space-time volume rather than from a sharp hypersurface): as long as T and μ_i are the same everywhere, 4π particle ratios are independent of the collective dynamics of the source.

For heavy-ion collisions at SPS energies and below one should therefore perform a thermal analysis on 4π -integrated yields and not on particle ratios inside small rapidity windows. This requires a strong experimental effort to measure the rapidity distributions of as many particle species as possible over the full rapidity range.

4.2. Non-constant thermodynamic parameters at freeze-out

The second, even more serious problem is the observation that in reality freeze-out does not happen at constant temperature and chemical potential. For example, it was shown in Ref. [33] that a successful thermal description of the rapidity distributions of hadrons created in 200 A GeV S+S collisions (in particular the different shapes of the rapidity distributions for Λ and $\bar{\Lambda}$, K^+ and K^-) requires not only strong longitudinal flow, but also a baryon chemical potential $\mu_i(\eta)$ which depends on the longitudinal position in the fireball: the central rapidity region is baryon-poorer than the target and projectile fragmentation regions. A second example demonstrating this type of problem is the observed rapidity dependence of the p_{\perp} -slopes of the h^- and proton spectra [34] and of the K_{\perp} -slopes of the transverse HBT radius R_{\perp} [24, 35]. According to a simultaneous analysis (as discussed in section 3.2 above) of spectra and correlations from Pb+Pb collisions at the SPS by Schönfelder [35] the decrease of the inverse slope parameters away from midrapidity must be attributed to *both* a reduction of the transverse collective

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flow and of the freeze-out temperature $T(\eta)$. If true, this would speak against a constant freeze-out temperature.

In such a situation the thermal fit replaces the functions $T(\eta)$ and $\mu_i(\eta)$ by suitably averaged values T, $\bar{\mu}_i$ (see Ref. [32] for a recent detailed study). Obviously the fit will then not be perfect: particle yields from a system in perfect local thermodynamic equilibrium (as, e.g., assumed in all hydrodynamic simulations), but with *spatially* varying temperature and chemical potentials, cannot be exactly recovered by a fit with constant temperature and chemical potential. In practice, this does not appear to be a very serious problem if one believes that the results from a recent thermal model analysis of particle yields from a hydrodynamic simulation [32] are representative for realistic situations: the freeze-out temperature reconstructed from the fit nearly coincided with the input temperature at which the hydrodynamic evolution was stopped, and the fitted chemical potentials agreed approximately with their average values across the freezeout surface. Nevertheless, small differences remain between the real yields from the hydrodynamic simulation and the yields returned by the thermal model fit. In a least mean square fit these systematic deviations would lead to a value for $\chi^2/d.o.f.$ which increases above all limits as the statistical error of the simulated ("measured") yields is further and further reduced, even though the system was, by construction, in perfect local thermal equilibrium.

This illustrates that global thermal fits to heavy-ion data can never be fully successful, due to the dynamics of the collision and its intricate influence on the freezeout process. For this reason one must not expect too much from the thermal model – a perfect fit with extremely small $\chi^2/d.o.f.$ is not necessarily a good and often rather a bad sign, indicating accidental error correlations, e.g. due to the use of redundant fit parameters.

This leaves us with the question where to draw the line between "good" and "bad" thermal model fits, between success and failure of a thermodynamic description of relativistic heavy-ion collisions. The above discussion should have made it clear that $\chi^2/d.o.f.$ is not a good criterium for answering this question. On the other hand, a fit which reproduces particle yields which cover a range of more than three orders of magnitude with individual deviations of less than $\pm 25\%$ [2] is obviously not bad. Quantitative model studies like those presented in [32] give us guidance for separating the grain from the straw; when supplemented by a thermal analysis of microscopic kinetic simulations as those presented at this meeting by Larissa Bravina [36], they are the foundations which we can use when collecting arguments in favor or against the formation of thermalized hot hadronic matter and quark-gluon plasma.

5. Conclusions

Let me summarize shortly: a thermal + flow analysis of yields, spectra and 2-particle correlations in S+A and Pb+Pb collisions at the CERN SPS suggests

• the formation of a *prehadronic* state in which twice as much strangeness is produced

as in pp and pA collisions and in which quarks are uncorrelated, i.e. they are not bound into color singlets;

- statistical hadronization of this state at $T_{had} \approx 170 \pm 20$ MeV with hadron abundances controlled by the *Maximum Entropy Principle*;
- rapid decoupling of the particle abundances, with chemical freeze-out temperatures $T_{\rm chem} \approx T_{\rm had}$ in sulphur-induced and $T_{\rm chem} \leq T_{\rm had}$ in Pb+Pb collisions;
- elastic rescattering among the hadrons (dominated by *s*-channel resonances) after hadronization from the prehadronic state which leads to a cooling of the momentum spectra and the generation of (more) collective flow;
- finally, thermal freeze-out at $T_{\text{therm}} \approx 140 150 \text{ MeV}$ in S+A and at $T_{\text{therm}} \approx 120 \pm 10 \text{ MeV}$ in Pb+Pb collisions, with average transverse collective flow velocities of order $\langle v_{\perp} \rangle \approx 0.4 0.5 c$.

Smaller collision systems distinguish themselves from larger ones not primarily by the achieved maximal energy density, but by the occupied collision volume in space and time. Compared to S+S collisions, Pb+Pb collisions live longer until thermal freeze-out, expand more in the tranverse direction, develop more transverse collective flow and cool down to lower (chemical and thermal) freeze-out temperatures. Of course, this view disagrees with the (present) majority opinion (I refer to the respective contributions to the Proceedings of "Quark Matter '97" [37]) that the critical energy density for deconfinement can be crossed at fixed beam energy of 160 A GeV by changing the size of the projectile and target or the collision centrality, and that the "anomalous" J/ψ suppression observed in central Pb+Pb collisions as a function of produced transverse energy [37, 38] signals this transition.

I find this interpretation irreconcilable with the systematics of light hadron production as discussed in this talk; a more consistent interpretation rests on the observation [38] that, as one increases N_{part} , one first sees "anomalous" suppression of the weakly bound ψ' , then (in semiperipheral Pb+Pb collisions) the "anomalous" suppression of the more strongly bound χ_c states (indirectly, via the disappearance of their 32% feed-down contribution to the measured J/ψ yield), and only in very central Pb+Pb collisions the disappearance of directly produced J/ψ 's which are very strongly bound (this last part of the supression pattern still remains to be confirmed by an improved measurement at very high E_T). This suggests to me that what NA50 is seeing is not the onset of deconfinement (the latter is there even in S+A collisions), but the dissociation of more and more strongly bound heavy quark states (respectively the removal of the corresponding components in the $c\bar{c}$ wavefunction) by collisions with the dense partonic medium in the early stages of the collision. For the more strongly bound states most of these collisions will be subthreshold; for this reason a longer lifetime of the dense early stage, which is achieved in larger collision systems or more central collisions, is crucial for an efficient destruction not only of the weakly bound ψ' , but also of the more strongly bound χ_c and J/ψ . Charmonium suppression is thus, in my opinion,

more a *lifetime effect* than a *deconfinement signal* (although the necessary high density of scatterers with sufficiently large cross sections probably requires deconfinement, too).

The picture which I have painted is, I believe, intrinsically consistent. It is sufficiently simple to be attractive but also sufficiently sophisticated not to be unrealistic. It may not be unique, not least because of the intrinsic systematic uncertainties associated with thermal model analyses which I pointed out and not all of which are quantitatively understood. What is urgently needed is more high-quality data on the chemistry of Pb+Pb collisions, the reconciliation of some puzzling discrepancies between different experiments as discussed at this meeting, and an improved systematics of the impact parameter and A-dependences, both in the light and heavy hadron sector.

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