

CERN PPE/94-164

21 Oct 1994

Energy and Particle Flow in Three-Jet and Radiative Two-Jet Events from Hadronic Z Decays

L3 Collaboration

Abstract

We report on a detailed study of the energy and particle flow in the event plane of three-jet events ($q\bar{q}g$) and radiative two-jet events ($q\bar{q}\gamma$) in hadronic Z decays recorded with the L3 detector. We find a significant decrease in particle and energy density in the angular region between quark and antiquark jets for $q\bar{q}g$ events as compared with $q\bar{q}\gamma$ events. Several QCD model predictions are compared with the observed effect.

(submitted to Physics Letters B)

Introduction

The measurement of energy and particle flows in the regions between jets (interjet) is known to represent an important test of QCD and fragmentation models. In three-jet events produced in e^+e^- annihilations it has been observed [1] that the region between the two quark jets ($q\bar{q}$) presents lower particle and energy flows relative to that which would be expected from naïve independent-fragmentation models. On the other hand, models based on string fragmentation [2] predicted this effect [3] and have been found to reproduce the data. In these models the string that generates final state particles receives a boost in the gluon direction depleting the $q\bar{q}$ region in favor of the qg and $g\bar{q}$ ones. The success of these models gave origin to the name “string effect” under which the phenomenon is often known. However, it has been observed that in perturbative QCD calculations [4], coherent emission of soft gluons from the color dipoles (qg , $g\bar{q}$ and $q\bar{q}$) produces a similar effect. Assuming “Local Parton-Hadron Duality” [5] (which is equivalent to considering the flow of final hadrons to be proportional to the flow of soft gluons), the effect should be observable at the hadron level without invoking any string fragmentation phenomenology. As a consequence a depletion is also expected from parton shower fragmentation models which include soft gluon interference effects [6].

The experimental comparison of three jet events ($q\bar{q}g$) with two jet events having a hard photon in the final state ($q\bar{q}\gamma$) represents a clean and model independent way of studying the “string effect” [7]. In fact, for similar kinematics the particle and energy yields in the $q\bar{q}$ region are expected to be lower for $q\bar{q}g$ than for $q\bar{q}\gamma$.

In this paper we present a comparison of the energy and particle flow distributions in the event plane of $q\bar{q}g$ and $q\bar{q}\gamma$ events for similar topologies and kinematics. We use 1.5×10^6 hadronic events collected with the L3 detector during 1991, 1992 and 1993 at $\sqrt{s} \approx 91\text{GeV}$. The results are compared with predictions from the COJETS 6.23 [8], HERWIG 5.4 [9] and JETSET 7.3 [10] Monte Carlo event generators¹). These models use a parton shower approach to describe the perturbative phase of gluon emission with differences in the treatment of “gluon coherence”. The hadronization phase is described by a “string” model in JETSET and a “cluster” model in HERWIG. In COJETS partons are fragmented independently and the effects of gluon coherence are neglected.

The L3 Detector

The L3 detector [12] consists of a time expansion chamber (TEC) for tracking charged particles, a high resolution electromagnetic calorimeter of BGO crystals, a barrel of scintillation counters, a hadron calorimeter with uranium and brass absorbers and proportional wire chamber readout, and a muon spectrometer. All subdetectors are installed inside a 12 m diameter solenoidal magnet which provides a uniform 0.5 T field along the beam direction. The fiducial solid angle coverage of L3 is 99% of 4π .

The BGO energy resolution is better than 2% for electromagnetic particles above 1.5 GeV, while the angular resolution for clusters with energy above 5 GeV is better than 0.12° . At 45 GeV the jet angular resolution is 2.5° and the jet energy resolution is 10% .

¹A discussion of the model parameter tuning for L3 is given in reference [11].

Event Selection

The selection of hadronic events is based on the energy measured in the electromagnetic and hadronic calorimeters. Events are accepted if:

$$0.6 < \frac{E_{\text{vis}}}{\sqrt{s}} < 1.4, \quad \frac{|E_{\parallel}|}{E_{\text{vis}}} < 0.4, \quad \frac{E_{\perp}}{E_{\text{vis}}} < 0.4, \quad N_{\text{cluster}} > 12,$$

where E_{vis} is the total energy observed in the detector, E_{\parallel} is the energy imbalance along the beam direction, and E_{\perp} is the transverse energy imbalance. An algorithm is used to group neighboring calorimeter signals, which are likely to be produced by the same particle, into clusters. Only clusters with a total energy above 100 MeV are used. The number of clusters produced is proportional to the number of particles in the event, so the cut on the number of clusters, N_{cluster} , rejects mainly low multiplicity non-hadronic events. Applying the same cuts to simulated events, we find that 98% of the Z hadronic decays are accepted. This efficiency has been found to be constant within errors for photon energies up to 45 GeV.

In the selection of $q\bar{q}g$ and $q\bar{q}\gamma$ events we pay particular attention to have similar kinematics and fiducial volumes for the two classes of events and to obtain a high purity $q\bar{q}\gamma$ sample. While jets are reconstructed in the angular region $5^{\circ} < \theta < 175^{\circ}$ (θ being the angle with respect to the LEP beam axis), photons in $q\bar{q}\gamma$ event candidates are selected only in the barrel region of the electromagnetic detector ($45^{\circ} < \theta < 135^{\circ}$). We select $q\bar{q}g$ events by applying the JADE algorithm [13] with $y_{\text{cut}} = 0.05$ and E0 recombination scheme to our hadronic event sample, retaining three jet events, and then identify the gluon as the softest jet. The purity is estimated to be $(74 \pm 2)\%$ using JETSET with the Matrix Element option.

As a cross-check we perform a gluon identification by requiring the event to have a muon with momentum $p_{\mu} > 4$ GeV in the second or third most energetic jet and identify the two quark jets as the most energetic jet and the one including the muon. The remaining jet is assigned to the gluon. This technique results in a higher gluon identification purity of $(85 \pm 2)\%$, but the semileptonic tag selects quark jets that include a neutrino and hence some missing energy. This makes the event kinematics different from the $q\bar{q}\gamma$ case, so we use this second method only as a cross-check.

In both cases the plane including the two quark jets is taken as the event plane and events are selected in such a way as to have the gluon jet within 10° from it. Similar to the photon in $q\bar{q}\gamma$ events only gluon jets inside the central region of the detector ($45^{\circ} < \theta < 135^{\circ}$) are accepted.

The analysis faces the problems of distinguishing genuine single photons from energetic neutral hadrons and of suppressing photons emitted by the quarks at low Q^2 . Events with a photon radiated at a smaller scale than a gluon should be considered as background, while events with hard photons from initial state radiation are not a background and are not removed from the sample.

In the case where the photon is emitted before any gluon radiation takes place one can make the approximation that the $q\bar{q}\gamma$ event is equivalent to a two-jet event boosted by the photon emission. If one disregards the photon, in the $q\bar{q}$ center-of-mass system the event should have the properties of a two-jet event with a total energy $\sqrt{s'} = \sqrt{s - 2E_{\gamma}\sqrt{s}}$, where E_{γ} is the photon energy in the laboratory frame.

Photon candidates for $q\bar{q}\gamma$ events are extracted from the three-jet sample by requiring that the least energetic jet includes a cluster of energy greater than 5 GeV in the central region of the electromagnetic calorimeter. The requirement that this jet lies within 10° of the event

plane is tightened to 8° in the $q\bar{q}\gamma$ case to take into account the better angular resolution of the photon compared to that of the gluon.

We reject most of the large background of neutral mesons decaying into photons by comparing the transverse shape of their showers to the simulated shape of a single photon [14]. The residual contamination from neutral hadrons is predicted to be $(24 \pm 2)\%$ for JETSET and $(25 \pm 2)\%$ for HERWIG. These numbers have been cross-checked by performing the shower shape analysis with a neural network which retains some discriminating power at very high energies and gives a contamination of $(26 \pm 7 \pm 6)\%$ [15].

In order to be able to compare $q\bar{q}g$ to $q\bar{q}\gamma$ events we need to reassign the hadronic activity in the photon jet to the quark jets for the $q\bar{q}\gamma$ case. To do so we recompute the jets after the photon is removed, and discard events with more than two jets.

We suppress photons radiated at a smaller scale than gluons by imposing isolation cuts. These cuts also further reduce the neutral hadron background. We first boost the event into the $q\bar{q}$ rest frame by using the photon momentum vector. Then we construct a cone of 20° around the photon direction (p_x, p_y, p_z) in a right-handed reference system (x, y, z) with the x axis along the direction of the most energetic jet and the y axis lying in the event plane in the hemisphere opposite to the photon. We then compute the quantity

$$E_c = E_{\gamma_c} - E_\gamma - \frac{E_{c1} + E_{c2} + E_{c3}}{3}$$

where E_{γ_c} is the calorimetric energy in the cone, E_γ is the photon energy, and E_{c1}, E_{c2}, E_{c3} are the energies in three control cones of the same aperture along the directions $(-p_x, -p_y, -p_z)$, (p_x, p_z, p_y) , $(-p_x, -p_z, -p_y)$. The activity in any of these three cones is equivalent to that in the cone including the photon because of the event's two-jet symmetry in the boosted frame. Moreover, they never overlap since $p_y \gg p_z \approx 0$ due to the planarity of the events. The distribution of the variable E_c is plotted in Figure 1a. Events in the region $E_c \simeq 0$ have hadronic activity and instrumental noise around the candidate photon similar to that which is found in symmetric regions away from jets, hence they are likely to be genuine prompt photon events. We use more than one control cone to improve the energy estimate.

A second variable $\varepsilon = E_\gamma/E_{\text{jet}3}$ is defined as the ratio of the photon energy over the total energy of the original photon jet and shown in Figure 1b. The closer ε is to 1 the more isolated is the photon in the event. After applying the cut $|E_c| < 2\text{GeV}$ the hadronic background is reduced to about 6% of the sample and the further requirement $\varepsilon > 0.8$ brings it down to $(1.8 \pm 0.6)\%$ in JETSET and to $(0.8 \pm 0.3)\%$ in HERWIG. We cross-check these background figures in a model independent way with the neural network and find a value of $(3 \pm 2 \pm 4)\%$.

In Figure 2a we show the energy flow distribution projected onto the event plane for $q\bar{q}\gamma$ JETSET events with and without the isolation cut on ε . We observe that the isolation cuts select events with cylindrical symmetry around the quark jets, which is consistent with the hypothesis that the only effect of the photon is a kinematic boost. Analyzing in detail the experimental data for energy flow in the region around the photon compared to the region opposite to it (Figure 2b) we see that a very tight cut on ε can artificially select topologies where the region around the photon has abnormally low activity; the choice of $\varepsilon > 0.8$ gives symmetric events and is therefore used.

We select 813 $q\bar{q}\gamma$ events out of the full hadronic sample and use only a subset of ~ 20000 $q\bar{q}g$ events which is sufficient for the statistical precision needed. Figures 3a and 3b show the angles A_{12} between quark jets and A_{13} between the first jet and the photon or the gluon jet. Figure 3c compares the energy of the third-jet for the gluon and for the photon case. It is clear that a close kinematical similarity between the two classes of events has been achieved.

Results

Particle flow plots for the $q\bar{q}\gamma$ and $q\bar{q}g$ samples are constructed by projecting, for every event, the direction of all particles onto the event plane. A particle is defined as a massless calorimetric object with an energy greater than 100 MeV. The particle flow is measured as a function of the angle increasing from jet 1 through jet 2 to jet 3 and back to jet 1. Energy flow plots result from considering any energy deposition above 40 MeV in the calorimeters. While in the energy flow case each event is normalized to its total visible energy, particle flow plots are not normalized since $q\bar{q}g$ events are bound to have higher multiplicity due to the gluon fragmentation. The results are shown in Figures 4a and 4b. The interquark region shows lower yield for $q\bar{q}g$ than for $q\bar{q}\gamma$ events. In order to normalize the angular distance between the two quark jets, in both the $q\bar{q}g$ and $q\bar{q}\gamma$ cases we recompute the energy and particle flows in the $q\bar{q}$ center of mass frame (Figures 4c and 4d). In order to be insensitive to the different energy resolution for the photon and gluon jet the new reference frame is computed using the momenta of the two quark jets.

To quantify the effect, we integrate the flow distributions of Figures 4c and 4d in the region $[54^\circ, 135^\circ]$. This window was chosen to give maximum sensitivity to the “string effect”, based on Monte Carlo studies. The individual yields integrated over the interjet window for $q\bar{q}g$ and $q\bar{q}\gamma$ are presented in Table 1 along with R_N and R_E , the ratios of $q\bar{q}g$ to $q\bar{q}\gamma$ integrals for particle and energy flows. Also shown are the results from the same analysis applied to 2.0×10^6 JETSET events, 1.7×10^6 HERWIG events and 1.0×10^6 COJETS events, all fully simulated and reconstructed in the L3 detector.

The magnitude of the “string effect” is given in a model independent way by the ratio of the yields listed in the third column. We observe that R_E and R_N indicate a depletion of the region opposite to the gluon of 21% and 18%, for the data. JETSET and HERWIG give a similar effect while COJETS shows no effect. We note that the absolute yields are underestimated by JETSET while HERWIG agrees better with the data. This illustrates the importance of measuring the “string effect” by a normalization to the $q\bar{q}\gamma$ reference sample.

Energy Flow	$q\bar{q}\gamma \times 10^{-3}$	$q\bar{q}g \times 10^{-3}$	R_E
Data	8.06 ± 0.40	6.37 ± 0.06	0.790 ± 0.040
JETSET 7.3	6.26 ± 0.29	5.39 ± 0.07	0.861 ± 0.042
HERWIG 5.4	8.02 ± 0.49	6.29 ± 0.08	0.784 ± 0.039
COJETS 6.23	6.78 ± 0.47	7.36 ± 0.18	1.086 ± 0.079
Particle Flow	$q\bar{q}\gamma$	$q\bar{q}g$	R_N
Data	1.893 ± 0.071	1.549 ± 0.011	0.818 ± 0.031
JETSET 7.3	1.482 ± 0.048	1.273 ± 0.012	0.859 ± 0.029
HERWIG 5.4	1.834 ± 0.066	1.441 ± 0.013	0.786 ± 0.029
COJETS 6.23	1.590 ± 0.090	1.663 ± 0.030	1.046 ± 0.062

Table 1: Particle and normalized energy yields integrated from 54° to 135° in the $q\bar{q}$ center-of-mass frame. The third column gives the ratios $q\bar{q}g/q\bar{q}\gamma$. Energy ordering is used for the gluon jet identification. Errors are statistical.

The following sources of systematics have been estimated:

- The subtraction of the residual neutral hadron background in the amount predicted by JETSET or HERWIG, increases the R values by $\Delta R_N = +0.005$ and $\Delta R_E = +0.004$.
- We vary the cut on ε from 0.75 to 0.85 with the aim of changing the amount of photons emitted at smaller scale than gluons. We observe a change of $\Delta R_N = \pm 0.006$ and $\Delta R_E = \pm 0.010$. The systematics introduced by the E_c cut are found to be negligible.
- The use of the DURHAM algorithm [16] with $y_{cut} = 0.02$ in the analysis, rather than the JADE algorithm, results in a 2% increase of both R_N and R_E . This is compatible with a 5% reduction of gluon purity as predicted by JETSET. Hence we do not add this effect to the systematic error.
- For $q\bar{q}\gamma$ events, not recomputing the jet directions without the γ candidate increases the number of events by 0.8% and increases the angle between the quark jets by 0.4° on average. The resulting changes in the ratios are $\Delta R_N = -0.005$ and $\Delta R_E = -0.008$.
- The definition of a calorimetric object was modified by introducing a preclustering procedure which uses the JADE algorithm with $y_{cut} = 1.2 \times 10^{-6}$, corresponding to a mass of about 100 MeV at LEP energies. This causes a change of $\Delta R_N = +0.010$ (and obviously no change in ΔR_E).
- Changes of $\pm 2^\circ$ in the cut on the angle between the photon and the event plane produce variations $\Delta R_N = \Delta R_E = \pm 0.007$.
- The flavor composition of $q\bar{q}\gamma$ and $q\bar{q}g$ events is different because of the different quark charges resulting in different couplings to the photon. We therefore reweighted, in JETSET events, the composition of $q\bar{q}g$ events to match the flavor composition of $q\bar{q}\gamma$ ones. This was found to have no effect on R_N or R_E .
- By a study of Monte Carlo events at generator level we have also tested the influence of cracks in the detector acceptance. The magnitude of the phenomenon is left unchanged by the addition of a blind region covering $\pm 4^\circ$ around the beam axis. This is the consequence of the fiducial region adopted for jet 3 in both the $q\bar{q}\gamma$ and $q\bar{q}g$ cases.

From the above study the total systematic error is ± 0.015 for both R_N and R_E . This gives

$$R_E = 0.790 \pm 0.040 \pm 0.015 \quad \text{and} \quad R_N = 0.818 \pm 0.031 \pm 0.015,$$

so that the depletion of the region opposite to the gluon compared to the one opposite to the photon has a significance of 5σ for both particle and energy flows. The results obtained by identifying the gluon jet with a μ -tag give a somewhat larger effect $R_E = 0.737 \pm 0.042 \pm 0.020$ and $R_N = 0.753 \pm 0.032 \pm 0.020$, which is compatible with the higher gluon purity.

It has been remarked [17] that the observed effect could have a purely kinematic origin, being caused by the difference between the massless photon and the effective mass of the gluon jet. In this scenario the quark jets of the $q\bar{q}g$ events, having less energy to share, are slimmer and result in lower interjet activity. In fact, we observe a small difference between the $q\bar{q}\gamma$ and $q\bar{q}g$ kinematics as a shift of the order of 10% in the masses of the two quark jets in our data and in all the Monte Carlo models used. The difference also occurs for COJETS even though it does not reproduce the “string effect”. Also, this mass shift is reduced by half if the jets are

not recomputed after the removal of the photon, while the magnitude of the “string effect” is left unchanged. We conclude that the effect cannot be explained on these grounds.

As noted by several authors [4, 18] the magnitude of the “string effect” is expected to increase by selecting for each event only particles with a large momentum component, P_{out} , perpendicular to the event plane. This phenomenon, observed by MarkII [19] and JADE [20] at lower energies, is predicted by perturbative QCD to decrease at LEP energy and to vanish asymptotically. In practice the investigation of the P_{out} dependence is difficult as the P_{out} selection reduces further the already limited statistical power of the $q\bar{q}\gamma$ control sample. To partially overcome this problem we use here the cylindrical symmetry of the $q\bar{q}\gamma$ event boosted to the $q\bar{q}$ rest frame. Because of this symmetry the definition of the event plane is arbitrary in the case of $q\bar{q}\gamma$ events and, instead of selecting one plane for the flow calculations, we can average the distributions obtained from all the possible planes containing the jet axis. This means that a particle gives a contribution to a specific flow-plot bin which is a function of its angle α relative to the $q\bar{q}$ axis. In the case of a cut on P_{out} the condition $P_{out} > P_{out}^{cut}$ is applied in each plane separately. The systematic effect introduced by the above algorithm [15] has been found to be negligible by a study of JETSET at generator level. In the case of $q\bar{q}g$ events where the event plane has a precise meaning even in the $q\bar{q}$ rest frame (and the statistics is more abundant) we select particles having $P_{out} > 0.2$ or 0.3 GeV. We then compare the region $[0^\circ, 180^\circ]$ of the $q\bar{q}g$ flow plot with that obtained for $q\bar{q}\gamma$. The bin-by-bin ratio of $q\bar{q}g$ to $q\bar{q}\gamma$ events is shown in Figures 5a and 5b for energy and particle flows, with no P_{out} cut. The observed dip corresponds to the “string effect”. In Figures 5c and 5d we plot the variation of the effect when a cut $P_{out} > 0.2$ GeV is applied.

The double ratios $\rho_E(P_{out}) = R_E^{P_{out}}/R_E$ and $\rho_N(P_{out}) = R_N^{P_{out}}/R_N$ for $P_{out} > 0.2$ GeV and $P_{out} > 0.3$ GeV are shown in Table 2. We only give statistical errors since the systematics in the double ratios cancel and are found to be negligible. In a similar fashion detector corrections are also negligible for the quantities ρ_E and ρ_N so that high statistics generator level runs are used for JETSET, HERWIG and COJETS in the table.

	$\rho_E(0.2\text{GeV})$	$\rho_N(0.2\text{GeV})$	$\rho_E(0.3\text{GeV})$	$\rho_N(0.3\text{GeV})$
Data	0.989 ± 0.028	0.911 ± 0.036	1.002 ± 0.038	0.908 ± 0.052
JETSET 7.3	0.982 ± 0.013	0.900 ± 0.014	0.984 ± 0.017	0.873 ± 0.020
HERWIG 5.4	1.007 ± 0.014	0.940 ± 0.017	1.028 ± 0.019	0.943 ± 0.024
COJETS 6.23	1.037 ± 0.017	1.009 ± 0.022	1.057 ± 0.024	1.017 ± 0.030

Table 2: Double ratios $\rho_E(P_{out}) = R_E^{P_{out}}/R_E$ and $\rho_N(P_{out}) = R_N^{P_{out}}/R_N$ computed over the interval $[54^\circ, 135^\circ]$. Data is compared to Monte Carlo generators for energy and particle flows. The systematics give negligible contribution to the errors.

Within the present statistics the particle flow shows an enhancement of the “string effect” at large P_{out} with a $\sim 3\sigma$ significance, while the energy flow shows no enhancement. Both JETSET and HERWIG follow the data while the comparison with the MarkII and JADE lower energy measurements gives a picture consistent with a vanishing dependence on P_{out} at large center of mass energies. This is compatible with perturbative QCD predictions.

Conclusions

We have studied the energy and particle flow in the region opposite to the gluon jet in three-jet events by comparing them with kinematically analogous events with two jets and one hard isolated photon. We find clear evidence, with a significance of 5 standard deviations, for lower flows in the three-jet event case as predicted by the string fragmentation model and by soft gluon coherence in the context of perturbative QCD. This effect is correctly reproduced by the JETSET and HERWIG event generators. We find, however, that the COJETS event generator does not reproduce the data. We have extended the analysis to particles having a large momentum component outside the event plane and found a small enhancement only in the case of particle flow.

Acknowledgments

We express our gratitude to the CERN accelerator divisions for the excellent performance of the LEP machine. We acknowledge the effort of all engineers and technicians who have participated in the construction and maintenance of this experiment.

We wish to thank T. Sjöstrand for many helpful discussions.

The L3 Collaboration:

M.Acciarri,²⁶ A.Adam,⁴³ O.Adriani,¹⁶ M.Aguilar-Benitez,²⁵ S.Ahlen,¹⁰ J.Alcaraz,²⁵ A.Aloisio,²⁸ G.Alverson,¹¹
M.G.Alvigi,²⁸ G.Ambrosi,³³ Q.An,¹⁸ H.Anderhub,⁴⁶ A.L.Anderson,¹⁵ V.P.Andreev,³⁷ T.Angelescu,¹² L.Antonov,⁴⁰
D.Antreasyan,⁸ G.Alkhadov,³⁷ P.Arce,²⁵ A.Arefiev,²⁷ T.Azemoon,³ T.Aziz,⁹ P.V.K.S.Baba,⁸ P.Bagnaia,^{36,17}
J.A.Bakken,³⁵ L.Baksay,⁴² R.C.Ball,³ S.Banerjee,⁹ K.Banicz,⁴³ R.Barillere,¹⁷ L.Barone,³⁶ A.Baschiroto,²⁶ M.Basile,⁸
R.Battiston,³³ A.Bay,²² F.Becattini,¹⁶ U.Becker,¹⁵ F.Behner,⁴⁶ Gy.L.Bencze,¹³ J.Berdugo,²⁵ P.Berges,¹⁵ B.Bertucci,¹⁷
B.L.Betev,^{40,46} M.Biasini,³³ A.Biland,⁴⁶ G.M.Bilei,³³ R.Bizzarri,³⁶ J.J.Blaising,⁴ G.J.Bobbink,^{17,2} R.Bock,¹ A.Böhm,¹
B.Borgia,³⁶ A.Boucham,⁴ D.Bourilkov,⁴⁶ M.Bourquin,¹⁹ D.Boutigny,¹⁷ B.Bouwens,² E.Brambilla,¹⁵ J.G.Branson,³⁸
V.Brigljevic,⁴⁶ I.C.Brock,³⁴ M.Brooks,²³ A.Bujak,⁴³ J.D.Burger,¹⁵ W.J.Burger,¹⁹ C.Burgos,²⁵ J.Busenitz,⁴²
A.Buytenhuijs,³⁰ A.Bykov,³⁷ X.D.Cai,¹⁸ M.Capell,¹⁵ G.Cara Romeo,⁸ M.Caria,³³ G.Carlini,²⁸ A.M.Cartacci,¹⁶
J.Casaus,²⁵ R.Castello,²⁶ N.Cavallo,²⁸ M.Cerrada,²⁵ F.Cesaroni,³⁶ M.Chamizo,²⁵ Y.H.Chang,⁴⁸ U.K.Chaturvedi,⁸
M.Chemarin,²⁴ A.Chen,⁴⁸ C.Chen,⁶ G.Chen,^{6,46} G.M.Chen,⁶ H.F.Chen,²⁰ H.S.Chen,⁶ M.Chen,¹⁵ G.Chiefari,²⁸
C.Y.Chien,⁵ M.T.Choi,⁴¹ S.Chung,¹⁵ L.Cifarelli,⁸ F.Cindolo,⁸ C.Civinini,¹⁶ I.Clare,¹⁵ R.Clare,¹⁵ T.E.Coan,²³
H.O.Cohn,³¹ G.Coignet,⁴ N.Colino,¹⁷ S.Costantini,³⁶ F.Cotorobai,² B.de la Cruz,²⁵ X.T.Cui,¹⁸ X.Y.Cui,¹⁸ T.S.Dai,¹⁵
R.D'Alessandro,¹⁶ R.de Asmundis,²⁸ A.Degré,⁴ K.Deiters,⁴⁴ E.Dénes,¹³ P.Denes,³⁵ F.DeNotaristefani,³⁶
D.DiBitonto,⁴² M.Diemoz,³⁶ H.R.Dimitrov,⁴⁰ C.Dionisi,³⁶ M.Dittmar,⁴⁶ L.Djambazov,⁴⁶ I.Dorne,⁴ M.T.Dova,^{18,4}
E.Drago,²⁸ D.Duchesneau,¹⁷ F.Duhem,⁴ P.Duinker,¹ I.Duran,³⁹ S.Dutta,⁹ S.Easo,³³ H.El Mamouni,²⁴ A.Engler,³⁴
F.J.Eppling,¹⁵ F.C.Erné,^{2,17} P.Extermann,¹⁷ R.Fabbretti,⁴⁴ M.Fabre,⁴⁴ S.Falciano,³⁶ A.Favara,¹⁶ J.Fay,²⁴ M.Felcini,⁴⁶
T.Ferguson,³⁴ D.Fernandez,²⁵ G.Fernandez,²⁵ F.Ferroni,³⁶ H.Fesefeldt,¹ E.Fiandrini,³³ J.H.Field,¹⁹ F.Filthaut,³⁰
P.H.Fisher,⁵ G.Forconi,¹⁵ L.Fredj,¹⁹ K.Freudenreich,⁴⁶ M.Gaillard,²² Yu.Galakionov,^{27,15} E.Gallo,¹⁶ S.N.Ganguli,⁹
P.Garcia-Abia,²⁵ S.Gentile,³⁶ J.Gerald,¹⁵ N.Gheordanescu,¹² S.Giagu,³⁶ S.Goldfarb,²² J.Goldstein,¹⁰ Z.F.Gong,²⁰
E.Gonzalez,²⁵ A.Gougas,⁵ D.Goujon,¹⁹ G.Gratta,³² M.W.Gruenewald,⁷ C.Gu,¹⁸ M.Guanzirola,¹⁸ V.K.Gupta,³⁵
A.Gurtu,⁹ H.R.Gustafson,³ L.J.Gutay,⁴³ A.Hasan,²⁹ D.Hauschildt,² J.T.He,⁶ T.Hebbeker,⁷ M.Hebert,³⁸ A.Hervé,¹⁷
K.Hilgers,¹ H.Hofer,⁴⁶ H.Hoorani,⁹ S.R.Hou,⁴⁸ G.Hu,¹⁸ B.Ille,²⁴ M.M.Ilyas,¹⁸ V.Innocente,¹⁷ H.Janssen,⁴ B.N.Jin,⁶
L.W.Jones,³ P.de Jong,¹⁵ I.Josa-Mutuberria,¹⁷ A.Kasser,²² R.A.Khan,¹⁸ Yu.Kamyshkov,³¹ P.Kapinos,⁴⁵
J.S.Kapustinsky,²³ Y.Karyotakis,¹⁷ M.Kaur,¹⁸ S.Khokhar,¹⁸ M.N.Kienzle-Focacci,¹⁹ D.Kim,⁵ J.K.Kim,⁴¹ S.C.Kim,⁴¹
Y.G.Kim,⁴¹ W.W.Kinnison,²³ A.Kirkby,³² D.Kirkby,³² J.Kirkby,¹⁷ S.Kirsch,⁴⁵ W.Kittel,³⁰ A.Klimentov,^{15,27}
A.C.König,³⁰ E.Koffeman,² O.Kornadt,¹ V.Koutsenko,^{15,27} A.Koulbardi,³⁷ R.W.Kraemer,³⁴ T.Kramer,¹⁵
V.R.Krastev,^{40,33} W.Krenz,¹⁴ H.Kuijten,³⁰ K.S.Kumar,¹⁴ A.Kunin,^{15,27} P.Ladron de Guevara,^{25,17} G.Landi,¹⁶
D.Lanske,¹ S.Lanzano,^{28,1} P.Laurikainen,²¹ A.Lebedev,¹⁵ P.Lebrun,²⁴ P.Lecomte,⁴⁶ P.Lecoq,¹⁷ P.Le Coultre,⁴⁶
D.M.Lee,²³ J.S.Lee,⁴¹ K.Y.Lee,⁴¹ I.Leedom,¹¹ C.Leggett,³ J.M.Le Goff,¹⁷ R.Leiste,⁴⁵ M.Lenti,¹⁶ E.Leonardi,³⁶
P.Levtchenko,³⁷ C.Li,^{20,18} E.Lieb,⁴⁵ W.T.Lin,⁴⁸ F.L.Linde,² B.Lindemann,¹ L.Lista,²⁸ Y.Liu,¹⁸ W.Lohmann,⁴⁵
E.Longo,³⁶ W.Lu,³⁶ Y.S.Lu,⁶ J.M.Lubbers,¹⁷ K.Lübelsmeyer,¹ C.Luci,³⁶ D.Luckey,¹⁵ L.Ludovici,³⁶ L.Luminari,³⁶
W.Lustermann,⁴⁴ W.G.Ma,²⁰ M.MacDermott,⁴⁶ M.Maity,⁹ L.Malgeri,³⁶ R.Malik,¹⁸ A.Malinin,²⁷ C.Maña,²⁵
S.Mangla,⁹ M.Maolinba,⁴⁶ P.Marchesini,⁴⁶ A.Marin,¹⁰ J.P.Martin,²⁴ F.Marzano,³⁶ G.G.G.Massarò,² K.Mazumdar,⁹
P.McBride,¹⁴ T.McMahon,⁴³ D.McNally,³⁸ S.Mele,²⁸ M.Merk,³⁴ L.Merola,²⁸ M.Meschini,¹⁶ W.J.Metzger,³⁰ Y.Mi,²²
A.Mihul,¹² G.B.Mills,²³ Y.Mir,¹⁸ G.Mirabelli,³⁶ J.Mnich,¹ M.Möller,¹ V.Monaco,³⁶ B.Monteleoni,¹⁶ R.Morand,¹⁴
S.Morganti,³⁶ N.E.Moulai,¹⁸ R.Mount,³² S.Müller,¹ E.Nagy,¹³ M.Napolitano,²⁸ F.Nessi-Tedaldi,⁴⁶ H.Newman,³²
M.A.Niaz,¹⁸ A.Nippe,¹ H.Nowak,⁴⁵ G.Organtini,³⁶ R.Ostenson,²¹ D.Pandoulas,¹ S.Paoletti,³⁶ P.Paolucci,²⁸ G.Pascale,³⁶
G.Passaleva,^{16,33} S.Patricelli,²⁸ T.Paul,⁵ M.Pauluzzi,³³ C.Paus,¹ F.Pauss,⁴⁶ Y.J.Pei,¹ S.Pensotti,²⁶ D.Perret-Gallix,⁴
A.Pevsner,⁵ D.Piccolo,²⁸ M.Pieri,¹⁶ J.C.Pinto,³⁴ P.A.Piroué,³⁵ E.Pistolessi,¹⁶ F.Plasil,³¹ V.Plyaskin,²⁷ M.Pohl,⁴⁶
V.Pojidaev,^{27,16} H.Postema,¹⁵ N.Produit,¹⁹ J.M.Qian,³ K.N.Qureshi,¹⁸ R.Raghavan,⁹ G.Rahal-Callot,⁴⁶
P.G.Rancoita,²⁶ M.Rattaggi,²⁶ G.Raven,² P.Razis,²⁹ K.Read,³¹ M.Redaelli,²⁶ D.Ren,⁴⁶ Z.Ren,¹⁸ M.Rescigno,³⁶
S.Reucroft,¹¹ A.Ricker,¹ S.Riemann,⁴⁵ B.C.Riemers,⁴³ K.Riles,³ O.Rind,³ H.A.Rizvi,¹⁸ S.Ro,⁴¹ A.Robohm,⁴⁶
F.J.Rodriguez,²⁵ B.P.Roe,³ M.Röhner,¹ S.Röhner,¹ L.Romero,²⁵ S.Rosier-Lees,⁴ R.Rosmalen,³⁰ Ph.Rosselet,²²
W.van Rossum,² S.Roth,¹ A.Rubbia,¹⁵ J.A.Rubio,¹⁷ H.Rykaczewski,⁴⁶ J.Salicio,¹⁷ J.M.Salicio,²⁵ E.Sanchez,²⁵
G.S.Sanders,²³ A.Santocchia,³³ M.E.Sarakinos,⁴³ S.Sarkar,⁹ G.Sartorelli,¹⁸ M.Sassowsky,¹ G.Sauvage,⁴ C.Schäfer,¹
V.Schegelsky,³⁷ D.Schmitz,¹ P.Schmitz,¹ M.Schneegans,⁴ N.Scholz,⁴⁶ H.Schopper,⁴⁷ D.J.Schotanus,³⁰ S.Shotkin,¹⁵
H.J.Schreiber,⁴⁵ J.Shukla,³⁴ R.Schulte,¹ K.Schultze,¹ J.Schwenke,¹ G.Schwering,¹ C.Sciacca,²⁸ I.Scott,¹⁴ R.Sehgal,¹⁸
P.G.Seiler,⁴⁴ J.C.Sens,^{17,2} L.Servoli,³³ I.Sheer,³⁸ S.Shevchenko,³² X.R.Shi,³² E.Shumilov,²⁷ V.Shoutko,²⁷ D.Son,⁴¹
A.Sopczak,¹⁷ V.Soulimov,²⁸ C.Spartiotis,²¹ T.Spickermann,¹ P.Spillantini,¹⁶ M.Steuer,¹⁵ D.P.Stickland,³⁵ F.Sticozzi,¹⁵
H.Stone,³⁵ K.Strauch,¹⁴ K.Sudhakar,⁹ G.Sultanov,¹⁸ L.Z.Sun,^{20,18} G.F.Susinno,¹⁹ H.Suter,⁴⁶ J.D.Swain,¹⁸ A.A.Syed,³⁰
X.W.Tang,⁶ L.Taylor,¹¹ R.Timellini,⁸ Samuel C.C.Ting,¹⁵ S.M.Ting,¹⁵ O.Toker,³³ M.Tonutti,¹ S.C.Tonwar,⁹ J.Tóth,¹³
G.Trowitzsch,⁴⁵ A.Tsaregorodtsev,³⁷ G.Tsipolitis,³⁴ C.Tully,³⁵ J.Ulbricht,⁴⁶ L.Urbán,¹³ U.Uwer,¹ E.Valente,³⁶
R.T.Van de Walle,³⁰ I.Vetlitsky,²⁷ G.Viertel,⁴⁶ P.Vikas,¹⁸ U.Vikas,¹⁸ M.Vivargent,⁴ H.Vogel,³⁴ H.Vogt,⁴⁵
I.Vorobiev,^{14,27} A.A.Vorobyov,³⁷ An.A.Vorobyov,³⁷ L.Vuilleumier,²² M.Wadhwa,²⁵ W.Wallraff,¹ J.C.Wang,¹⁵
X.L.Wang,²⁰ Y.F.Wang,¹⁵ Z.M.Wang,^{18,20} A.Weber,¹ J.Weber,⁴⁶ R.Weill,²² C.Willmott,²⁵ F.Wittgenstein,¹⁷
D.Wright,³⁵ S.X.Wu,¹⁸ S.Wynhoff,¹ Z.Z.Xu,²⁰ B.Z.Yang,²⁰ C.G.Yang,⁶ G.Yang,¹⁸ X.Y.Yao,⁶ C.H.Ye,¹⁸ J.B.Ye,²⁰ Q.Ye,¹⁸
S.C.Yeh,⁴⁸ J.M.You,¹⁸ N.Yunus,¹⁸ M.Yzerman,² C.Zaccardelli,³² P.Zemp,⁴⁶ M.Zeng,¹⁸ Y.Zeng,¹⁸ D.H.Zhang,²
Z.P.Zhang,^{20,18} B.Zhou,¹⁰ G.J.Zhou,⁶ J.F.Zhou,¹ R.Y.Zhu,³² A.Zichichi,^{8,17,18} B.C.C.van der Zwaan,²

-
- 1 I. Physikalisches Institut, RWTH, D-52056 Aachen, FRG[§]
 - III. Physikalisches Institut, RWTH, D-52056 Aachen, FRG[§]
 - 2 National Institute for High Energy Physics, NIKHEF, NL-1009 DB Amsterdam, The Netherlands
 - 3 University of Michigan, Ann Arbor, MI 48109, USA
 - 4 Laboratoire d'Annecy-le-Vieux de Physique des Particules, LAPP, IN2P3-CNRS, BP 110, F-74941 Annecy-le-Vieux CEDEX, France
 - 5 Johns Hopkins University, Baltimore, MD 21218, USA
 - 6 Institute of High Energy Physics, IHEP, 100039 Beijing, China
 - 7 Humboldt University, D-10099 Berlin, FRG
 - 8 INFN-Sezione di Bologna, I-40126 Bologna, Italy
 - 9 Tata Institute of Fundamental Research, Bombay 400 005, India
 - 10 Boston University, Boston, MA 02215, USA
 - 11 Northeastern University, Boston, MA 02115, USA
 - 12 Institute of Atomic Physics and University of Bucharest, R-76900 Bucharest, Romania
 - 13 Central Research Institute for Physics of the Hungarian Academy of Sciences, H-1525 Budapest 114, Hungary[‡]
 - 14 Harvard University, Cambridge, MA 02139, USA
 - 15 Massachusetts Institute of Technology, Cambridge, MA 02139, USA
 - 16 INFN Sezione di Firenze and University of Florence, I-50125 Florence, Italy
 - 17 European Laboratory for Particle Physics, CERN, CH-1211 Geneva 23, Switzerland
 - 18 World Laboratory, FBLJA Project, CH-1211 Geneva 23, Switzerland
 - 19 University of Geneva, CH-1211 Geneva 4, Switzerland
 - 20 Chinese University of Science and Technology, USTC, Hefei, Anhui 230 029, China
 - 21 SEFT, Research Institute for High Energy Physics, P.O. Box 9, SF-00014 Helsinki, Finland
 - 22 University of Lausanne, CH-1015 Lausanne, Switzerland
 - 23 Los Alamos National Laboratory, Los Alamos, NM 87544, USA
 - 24 Institut de Physique Nucléaire de Lyon, IN2P3-CNRS, Université Claude Bernard, F-69622 Villeurbanne Cedex, France
 - 25 Centro de Investigaciones Energeticas, Medioambientales y Tecnológicas, CIEMAT, E-28040 Madrid, Spain
 - 26 INFN-Sezione di Milano, I-20133 Milan, Italy
 - 27 Institute of Theoretical and Experimental Physics, ITEP, Moscow, Russia
 - 28 INFN-Sezione di Napoli and University of Naples, I-80125 Naples, Italy
 - 29 Department of Natural Sciences, University of Cyprus, Nicosia, Cyprus
 - 30 University of Nymegen and NIKHEF, NL-6525 ED Nymegen, The Netherlands
 - 31 Oak Ridge National Laboratory, Oak Ridge, TN 37831, USA
 - 32 California Institute of Technology, Pasadena, CA 91125, USA
 - 33 INFN-Sezione di Perugia and Università Degli Studi di Perugia, I-06100 Perugia, Italy
 - 34 Carnegie Mellon University, Pittsburgh, PA 15213, USA
 - 35 Princeton University, Princeton, NJ 08544, USA
 - 36 INFN-Sezione di Roma and University of Rome, "La Sapienza", I-00185 Rome, Italy
 - 37 Nuclear Physics Institute, St. Petersburg, Russia
 - 38 University of California, San Diego, CA 92093, USA
 - 39 Dept. de Física de Partículas Elementales, Univ. de Santiago, E-15706 Santiago de Compostela, Spain
 - 40 Bulgarian Academy of Sciences, Institute of Mechatronics, BU-1113 Sofia, Bulgaria
 - 41 Center for High Energy Physics, Korea Advanced Inst. of Sciences and Technology, 305-701 Taejon, Republic of Korea
 - 42 University of Alabama, Tuscaloosa, AL 35486, USA
 - 43 Purdue University, West Lafayette, IN 47907, USA
 - 44 Paul Scherrer Institut, PSI, CH-5232 Villigen, Switzerland
 - 45 DESY-Institut für Hochenergiephysik, D-15738 Zeuthen, FRG
 - 46 Eidgenössische Technische Hochschule, ETH Zürich, CH-8093 Zürich, Switzerland
 - 47 University of Hamburg, 22761 Hamburg, FRG
 - 48 High Energy Physics Group, Taiwan, China
- § Supported by the German Bundesministerium für Forschung und Technologie
‡ Supported by the Hungarian OTKA fund under contract number 2970.
‡ Also supported by CONICET and Universidad Nacional de La Plata, CC 67, 1900 La Plata, Argentina
† Deceased.

References

- [1] JADE Collaboration, W. Bartel *et al.*, Phys. Lett. **B101** (1981) 129-134;
JADE Collaboration, W. Bartel *et al.*, Z. Phys. **C21** (1983) 37-52;
JADE Collaboration, W. Bartel *et al.*, Phys. Lett. **B134** (1984) 275-280;
TASSO Collaboration, M. Althoff *et al.*, Z. Phys. **C29** (1985) 29-40;
TPC collaboration, H. Aihara *et al.*, Z. Phys. **C28** (1985) 31-44;
OPAL Collaboration, P.D. Acton *et al.*, Z. Phys. **C58** (1993) 387-404;
OPAL Collaboration, M.Z. Akrawy *et al.*, Phys. Lett. **B261** (1991) 334-346.
- [2] B. Andersson, G. Gustafson, G. Ingelman and T. Sjöstrand, Phys. Rep. **97** (1983) 31.
- [3] B. Andersson, G. Gustafson and T. Sjöstrand, Phys. Lett. **B94** (1980) 211.
- [4] Y.I. Azimov, Y.L. Dokshitzer, V.A. Khoze, S.I. Troyan, Phys. Lett. **B165** (1985) 147-150;
Y.I. Azimov, Y.L. Dokshitzer, V.A. Khoze, S.I. Troyan, Yad. Fiz. **43** (1986) 159;
Y.L. Dokshitzer, V.A. Khoze, A.H. Mueller, S.I. Troyan, Basics of Perturbative QCD éd. Frontières (1991).
- [5] Y.L. Dokshitzer, S.I. Troyan, Proceedings of the XIX Winter School of the LNPI Vol. 1 (1984) 144;
Y.I. Azimov, Y.L. Dokshitzer, V.A. Khoze, S.I. Troyan, Z. Phys. **C27** (1985) 65-72.
- [6] G. Marchesini, B. Webber, Nucl. Phys. **B238** (1981) 1-29.
- [7] TPC/2 γ collaboration, H. Aihara *et al.*, Phys. Rev. Lett. **57** (1986) 945-948;
MARK II Collaboration, P.D. Seldon *et al.*, Phys. Rev. Lett. **57** (1986) 1398-1401;
JADE Collaboration, F. Ould Saada *et al.*, Z. Phys. **C39** (1988) 1-6.
- [8] R. Odorico, Comput. Phys. Commun. **32** (1984) 139-172;
R. Odorico, Comput. Phys. Commun. **34** (1985) 431-436 (erratum).
- [9] G. Marchesini, B. Webber, Nucl. Phys. **B310** (1988) 461-526;
I.G. Knowles, Nucl. Phys. **B310** (1988) 571-588.
- [10] T. Sjöstrand, Comput. Phys. Commun. **39** (1986) 347-407;
T. Sjöstrand, M. Bengtsson, Comput. Phys. Commun. **43** (1987) 367-379.
- [11] L3 Collaboration, B. Adeva *et al.*, Z. Phys. **C55** (1992) 39-61.
- [12] L3 Collaboration, B. Adeva *et al.*, Nucl. Inst. Meth. **A289** (1990) 35-102.
- [13] JADE Collaboration, W. Bartel *et al.*, Z. Phys. **C33** (1986) 23-31;
JADE Collaboration, S. Bethke *et al.*, Phys. Lett. **B213** (1988) 235-241.
- [14] L3 Collaboration, O. Adriani *et al.*, Phys. Lett. **B292** (1992) 472-484.
- [15] D. Duchesneau, PhD thesis #2644, University of Geneva (1993) unpublished.
- [16] S. Catani *et al.*, Phys. Lett. **B269** (1991) 432;
N. Brown and W.J. Stirling, Z. Phys. **C53** (1992) 629.
- [17] G. Balocchi and R. Odorico, Nucl. Phys. **B345** (1990) 173-185.
- [18] V. Khoze, L. Lönnblad, Phys. Lett. **B241** (1990) 123.
- [19] MARK II Collaboration, P.D. Seldon *et al.*, Phys. Rev. Lett. **57** (1986) 1398-1401.
- [20] JADE Collaboration, F. Ould Saada *et al.*, Z. Phys. **C39** (1988) 1-6.

List of Figures

- 1 Isolation variables (a) E_c , (b) ε after the cut $|E_c| < 2\text{GeV}$ has been applied. Solid points represent the data, while the histogram represents the JETSET prediction. The background contribution from neutral hadrons is shown as the hatched area. The arrows represent the cuts used.
- 2 (a) Energy distribution projected onto the event plane in the $q\bar{q}$ rest frame for JETSET $q\bar{q}\gamma$ events after removal of the photon, which otherwise appears around 260° . Angles run from highest energetic jet direction towards the second jet. Neutral hadron background is removed and the E_c cut has been applied. (b) Relative energy flow difference δ between the photon region $[234^\circ, 297^\circ]$ and the symmetric one $[63^\circ, 126^\circ]$ for data as a function of the cut on ε .
- 3 (a) Angle A_{12} between the two quark jets and (b) between the most energetic jet and the third jet A_{13} . (c) Energy of the third jet E_3 .
- 4 (a) Distribution of the normalized energy flow and (b) particle flow in the laboratory frame. (c) and (d) are the corresponding distributions in the $q\bar{q}$ center of mass frame, after the photon has been removed. The arrows show the angular range used to measure the effect.
- 5 Bin-by-bin ratios of the $q\bar{q}g$ and $q\bar{q}\gamma$ (a) energy and (b) particle flow plots after the application of the algorithm described in the text to $q\bar{q}\gamma$ events. The theoretical predictions have statistical uncertainties of similar magnitude to the ones shown for data. (c) and (d) show the ratios of the distributions with and without a $0.2\text{ GeV } P_{out}$ cut. Systematic errors are not shown in (a) and (b), while they are negligible in (c) and (d). The arrows show the angular range used to measure the effect.

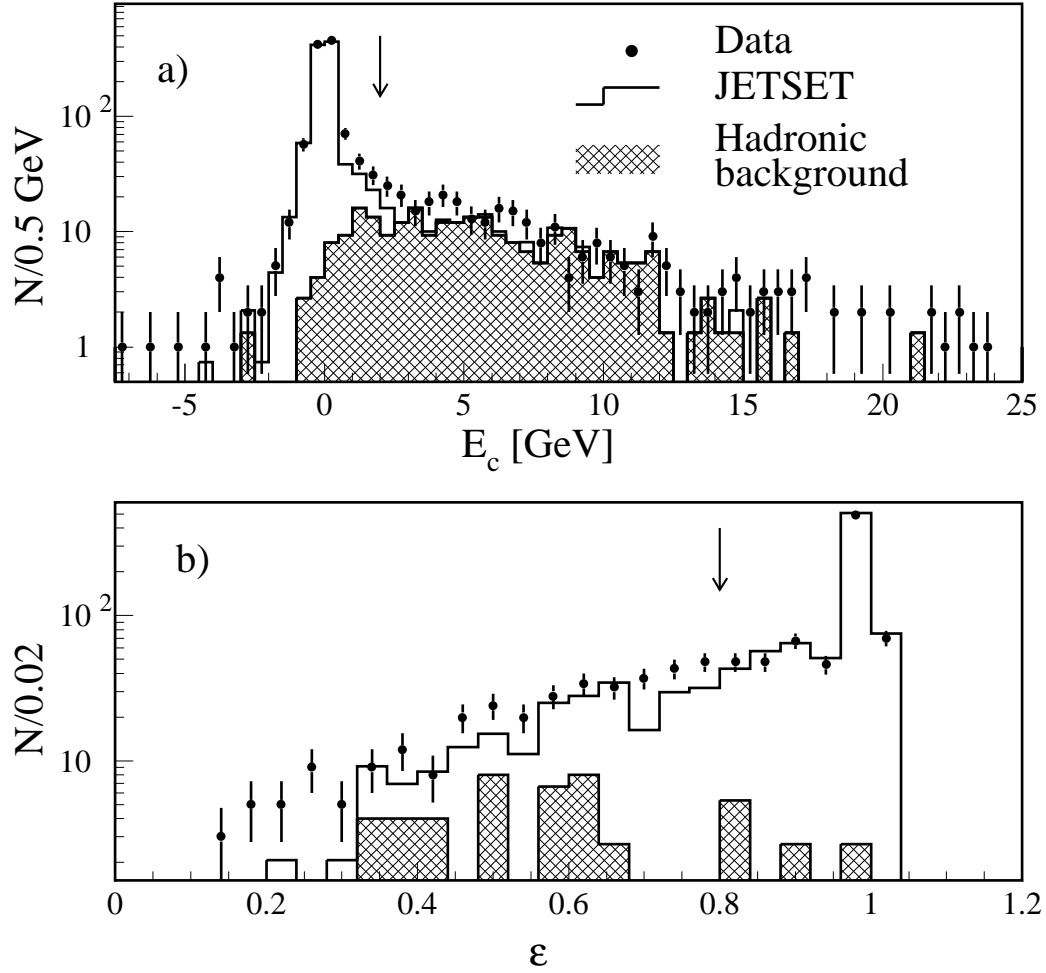


Figure 1: Isolation variables (a) E_c , (b) ε after the cut $|E_c| < 2 \text{ GeV}$ has been applied. Solid points represent the data, while the histogram represents the JETSET prediction. The background contribution from neutral hadrons is shown as the hatched area. The arrows represent the cuts used.

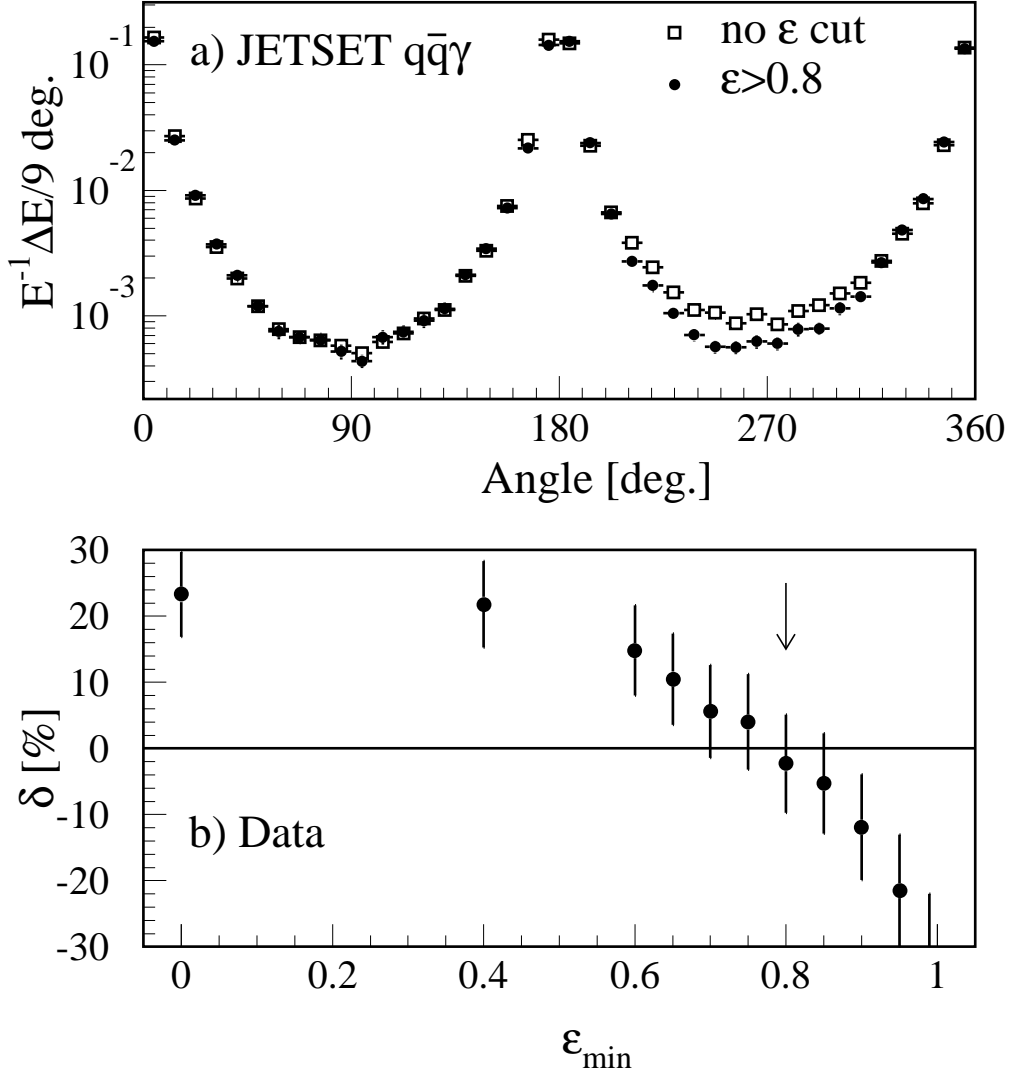


Figure 2: (a) Energy distribution projected onto the event plane in the $q\bar{q}$ rest frame for JETSET $q\bar{q}\gamma$ events after removal of the photon, which otherwise appears around 260° . Angles run from highest energetic jet direction towards the second jet. Neutral hadron background is removed and the E_c cut has been applied. (b) Relative energy flow difference δ between the photon region $[234^\circ, 297^\circ]$ and the symmetric one $[63^\circ, 126^\circ]$ for data as a function of the cut on ϵ .

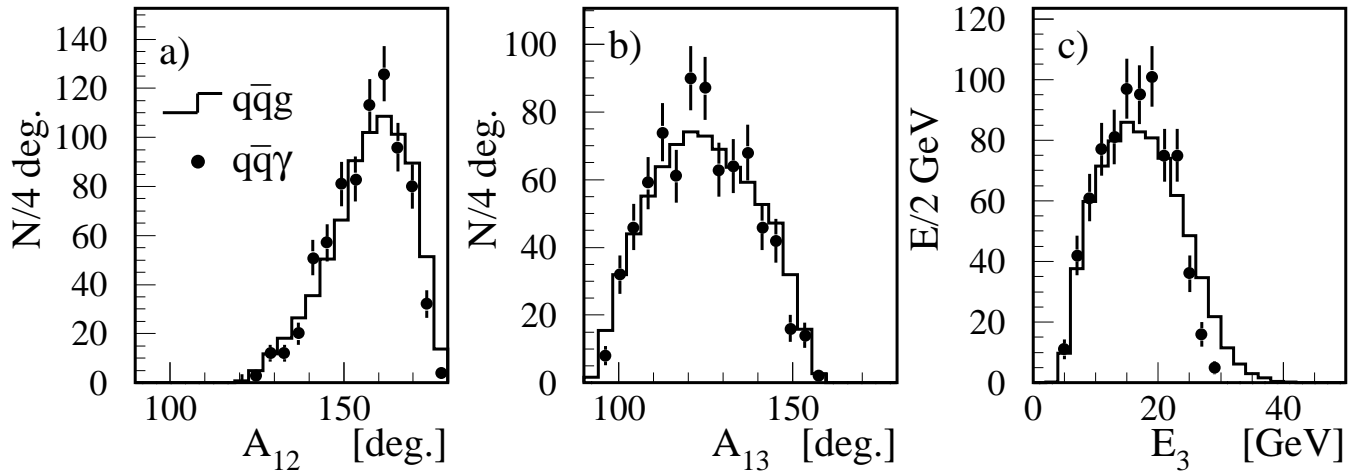


Figure 3: (a) Angle A_{12} between the two quark jets and (b) between the most energetic jet and the third jet A_{13} . (c) Energy of the third jet E_3 .

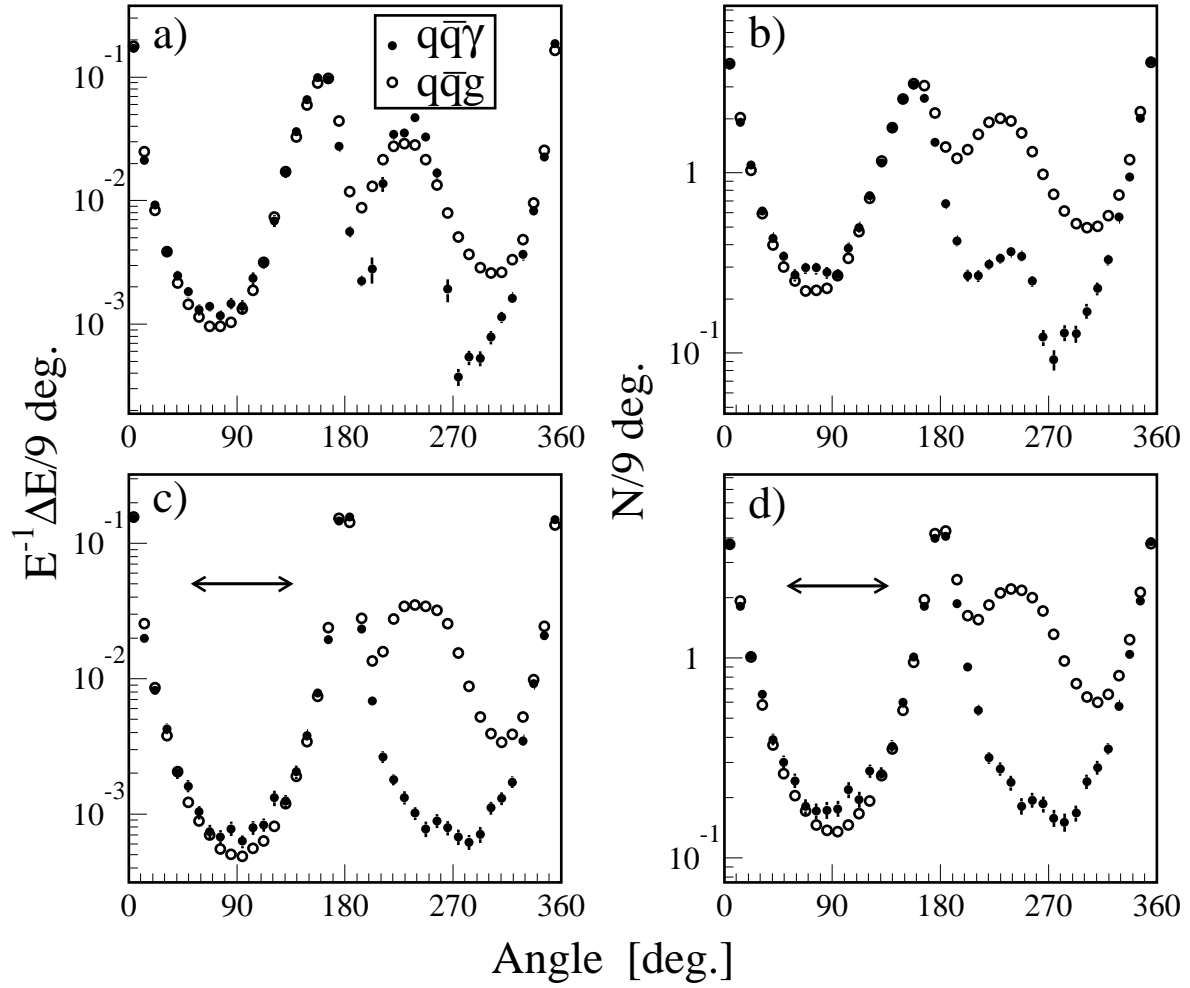


Figure 4: (a) Distribution of the normalized energy flow and (b) particle flow in the laboratory frame. (c) and (d) are the corresponding distributions in the $q\bar{q}$ center of mass frame, after the photon has been removed. The arrows show the angular range used to measure the effect.

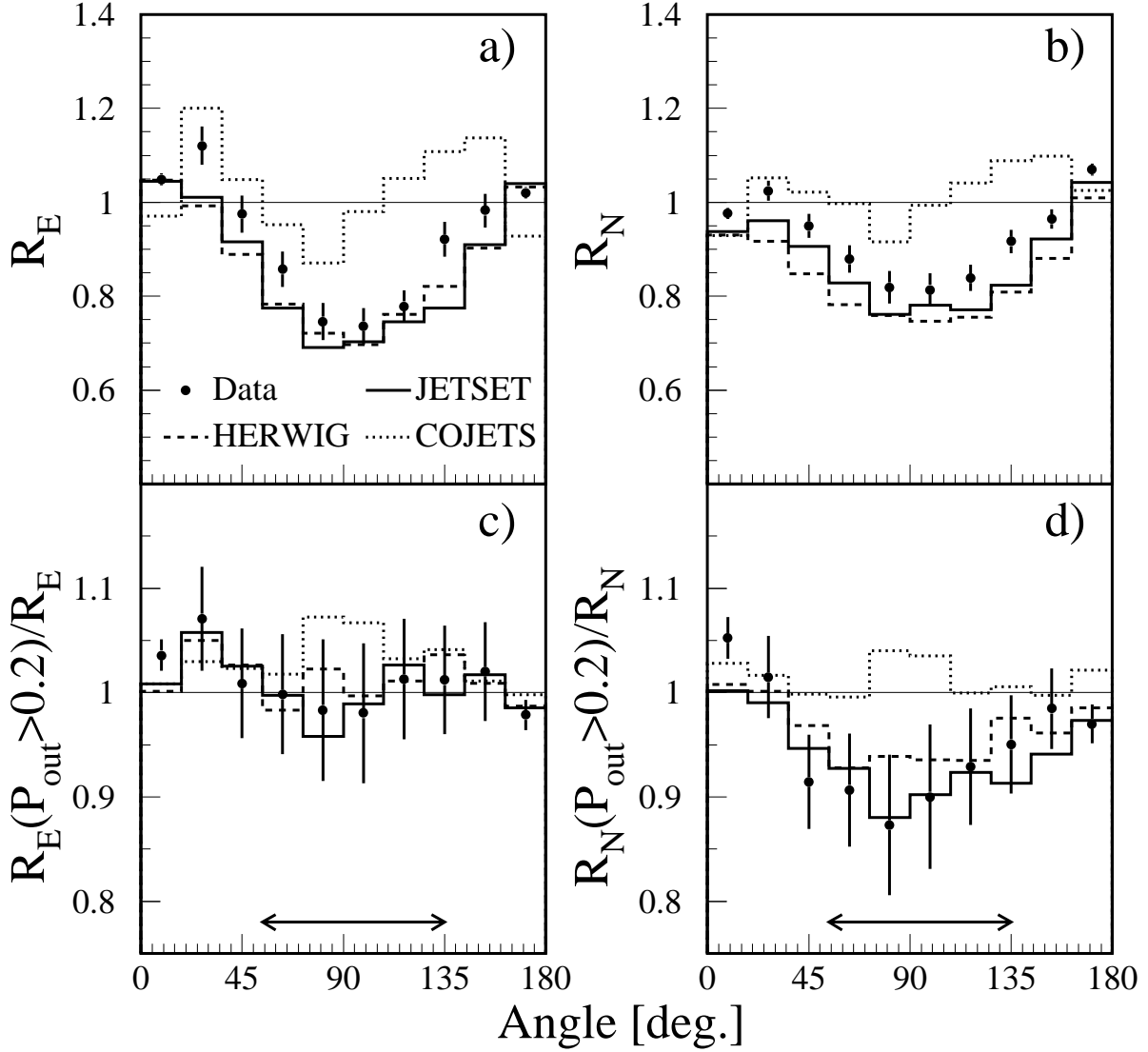


Figure 5: Bin-by-bin ratios of the $q\bar{q}g$ and $q\bar{q}\gamma$ (a) energy and (b) particle flow plots after the application of the algorithm described in the text to $q\bar{q}\gamma$ events. The theoretical predictions have statistical uncertainties of similar magnitude to the ones shown for data. (c) and (d) show the ratios of the distributions with and without a 0.2 GeV P_{out} cut. Systematic errors are not shown in (a) and (b), while they are negligible in (c) and (d). The arrows show the angular range used to measure the effect.