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High frequency guided mode resonances in mass-loaded, thin film gallium nitride surface acoustic wave devices

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We demonstrate high-frequency (> 3 GHz), high quality factor radio frequency (RF) resonators in unreleased thin film gallium nitride (GaN) on sapphire and silicon carbide substrates by exploiting acoustic guided mode (Lamb wave) resonances. The associated energy trapping, due to mass loading from the gold electrodes, allows us to efficiently excite these resonances from a 50 Ω input. The higher phase velocity, combined with lower electrode damping, enables high quality factors with moderate electrode pitch, and provides a viable route towards high-frequency piezoelectric devices. The GaN platform, with its ability to guide and localize high-frequency sound on the surface of a chip with access to high-performance active devices, will serve as a key building block for monolithically integrated RF front-ends.

A modern smartphone has \sim 50 RF filters to enable seamless communication across a wide variety of frequency bands¹. As we move towards widespread adoption of 5G standards, and expect ever-greater functionality from our phones, the number of RF filters is expected to significantly increase and the filter packaging problem becomes increasingly acute². Monolithic integration of piezoelectric acoustic wave filters with amplifiers is the only scalable long-term solution. While integration of aluminum nitride (AlN) film bulk acoustic wave resonator (FBAR) filters with complementary metal-oxide semiconductor (CMOS) electronics is being actively pursued, the process incompatibility between microelectro-mechanical systems (MEMS) and CMOS foundries, mainly substrate release, makes monolithic integration challenging. In the past decade, three trends have converged to make GaN an interesting alternative^{3,4}: improvements in material growth, especially interface quality for thin films, steady displacement of GaAs based power-amplifiers (PA) with GaN PAs and finally, the availability of GaN foundry services providing ready-access to high performance amplifiers. Working with GaN allows us to trade-off a lower piezoelectric device performance (cf. AlN, lithium tantalate) for the benefits of monolithic integration with active devices.

The prospect of building piezoelectric, primarily surface acoustic wave (SAW), resonators and filters in GaN was recognized from the beginning of GaN device research⁵ and there has been a lot of exciting recent progress⁶. On the other hand, relatively little work has been done on exploiting the main advantage that GaN provides over traditional SAW substrates like lithium tantalate⁷. In particular, GaN supports guided acoustic waves whose dispersion can be engineered, on account of its lower acoustic velocity, compared to the growth substrate (mainly silicon, silicon carbide and sapphire) and buffer layers⁸. Guiding sound on the surface of the chip allows us to confine acoustic energy and increase the effective electromechanical coupling coefficient⁹. In addition, by trapping these sound waves using guided mode resonances¹⁰, one can engineer high quality factor (Q_{mech}) resonators without requiring substrate release. Such unreleased resonator platforms are also being explored for monolithic integration in nonpiezoelectric CMOS-MEMS platforms^{11–14}. In this work, we demonstrate high Q_{mech} GaN resonators on unreleased substrates (sapphire and silicon carbide) by utilizing the metallic interdigitated transducer (IDT) electrodes for mass loading and energy trapping¹⁵. By avoiding patterning of the GaN device layer, our approach is compatible with current GaN HEMT foundry process flows and is attractive for the nearterm monolithic integration of piezoelectric acoustic wave devices with GaN HEMT amplifiers.

A representative device, shown in Fig.1 (a), consists of the standard IDT geometry, with the IDT period (Λ_{IDT}) chosen to match the SAW frequency. The devices were fabricated either on SiC or sapphire substrates with the GaN thickness ($t_{GaN} \approx 1-1.5 \ \mu m$) and electrode thickness ($t_{Au} \approx 75 \ nm$). In addition to exciting the Rayleigh SAW waves (shown in Fig.1 (b, left)), the transducer with the same period (Λ_{IDT}), also excites a higher-frequency guided Lamb wave mode (also referred to as a Sezawa mode), shown in Fig.1 (b, right)^{7,16,17}. In contrast to the Rayleigh SAW mode, the Lamb wave mode has a higher phase velocity (~1.5x) allowing higher frequency operation for the same Λ_{IDT} . In addition, a significant fraction of the acoustic energy resides within the GaN layer, away from the GaN-electrode interface, leading to lower acoustic dissipation and higher Q_{mech} at high-frequencies (2-6 GHz).

To convert the IDT from a SAW transducer to a SAW resonator, one needs to confine the acoustic energy, which can be achieved by employing acoustic reflectors on either side of the IDT. Traditionally, SAW resonators have relied on the weak finger reflectivity provided by shorted metallic gratings. But the weak reflectivity increases the number of finger pairs needed to achieve unity reflection, resulting in large device sizes ($\sim mm$). In contrast, we work in the regime of strong finger reflection ($r_f \approx 0.06 - 0.1$)¹⁸ and excitation of trapped acoustic modes to achieve compact high- Q_{mech} resonators. While higher finger reflectivity is generally associated with higher out-of-plane scattering, the scattered waves phased appropriately can destructively interfere in the far-field (sub-

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FIG. 1. (a) SEM image of a fabricated GaN-on-SiC device (Λ_{IDT} = 1.75 μm , t_{Au} = 75 nm) (b) Finite element method (FEM) simulation performed using linear elastic piezoelectric theory in COMSOL Multiphysics v5.3 of the mode displacement of a 1.6 μm GaN on sapphire device with 350 nm AlN buffer layer (Λ_{IDT} = 1.75 μm , t_{Au} = 75 nm) for the SAW ($f_{SAW} \approx 2.06$ GHz) and Lamb wave ($f_{Lamb} \approx 3.02$ GHz) modes (c) FEM simulation of the mode displacement for the fundamental ($f \approx 3.056$ GHz) and higher-order ($f \approx 3.049$ GHz) trapped Lamb wave resonances ($N_{pairs} = 40$).

strate leakage), leading to high quality factors and tight mode confinement. Photonic and phononic crystal structures, similarly rely on strong index contrast¹⁹ to simultaneously achieve high Q and low mode volumes. In addition, the increased radiation conductance associated with energy trapping allows us to match the device impedance to 50 Ω and avoid the need for on-chip impedance matching networks^{20,21}. Effectively, the increased radiation conductance (G_{IDT}) dominates the IDT static capacitance ($C_{0,IDT}$) and thus resistive matching is sufficient²⁰.

The higher r_f is achieved by using gold (Au) electrodes for the IDT. For the same thickness, a Au electrode was measured to have a higher ($\approx 50x$) r_f for SAW waves compared to aluminum (Al) electrodes²². In a guided wave geometry, the r_f is higher on account of the higher spatial mode overlap of the acoustic field with the metal electrode. Traditionally, Au electrodes have not been used with SAW devices, especially at high-frequencies (> 1 GHz), due to the high acoustic wave damping. Compared with traditional Rayleigh wavebased SAW devices that have acoustic energy confined to the electrode-GaN interface and thus suffer from high damping, the Lamb wave has a significant fraction of the acoustic energy below the interface (Fig.1(b)) and thus reduced spatial mode overlap with the electrode. Coupled with the higher phase velocity, which increases the IDT period and reduces the transducer series resistance, Lamb waves provide a viable alternative to traditional SAW and FBAR devices for building high-frequency, high- Q_{mech} piezoelectric devices.

If the r_f exceeds a threshold value determined by the total number of fingers in the structure, the structure resembles a 1D acoustic Bragg stack with the IDT electrodes (GaN+Au) and the inter-electrode gaps (GaN) serving as the two effective acoustic materials comprising the stack. The strong finger reflection couples the forward and backward propagating Lamb waves, leading to a 1D phononic bandgap. Since the guided modes in the IDT region have a lower frequency (due to mass loading) compared to the bare GaN regions, the overall structure can be visualized as a 1D Bragg stack surrounded by two semi-infinite bare GaN regions that do not support propagating modes at the same frequency. Provided the frequency difference $(\Delta \omega)$ for the guided mode in the IDT and non-IDT regions exceeds the modal decay rate (κ), the mode is trapped in the IDT, and a guided mode resonance can be observed in an RF reflection $(|S_{11}|)$ measurement. We would like to note here that the trapped acoustic modes are analogous to the bound states observed in GaAs/AlGaAs superlattice structures and a similar transfer-matrix based tunneling resonance approach can be used to calculate them²³. Using an FEM simulation, the trapped Lamb wave resonances' displacement profiles can be calculated and two of these are shown in Fig.1 (c,d). The fundamental mode has the highest quality factor and electromechanical coupling coefficient, with the higherorder modes being more weakly confined. While we have performed experiments on both GaN-on-SiC and GaN-onsapphire devices, we restrict our FEM simulations to GaNon-sapphire.



FIG. 2. (a) Measured RF reflection coefficient magnitude $|S_{11}|$ and (b) phase response for a GaN on SiC device with 125 finger pairs and IDT period 1.5 μ m. The red dashed curve in (a) shows a Lorentzian fit to the fundamental mode response.

These guided mode resonances can be observed in the RF reflection ($|S_{11}|$) spectrum of the IDT. A representative spectrum, for a 1.5 μ m IDT period device fabricated on a GaN on SiC sample, is shown in Fig.2. In contrast to the expected

 $sinc^2(f)$ response for the S_{11} magnitude as in a traditional IDT, we instead observe a series of sharp Lorentzian resonances, corresponding to the different trapped modes. The effect can also be observed in the phase response, where a series of phase inflections can be clearly seen in Fig.2(b), corresponding to the dips in Fig.2(a). The fundamental resonance, fit with a Lorentzian lineshape (red curve in Fig.2(a)) has a quality factor, $Q_{mech} \approx 2000$, which corresponds to an $f.Q \sim 7 * 10^{12}$. Since acoustic waves at such high frequencies are expected to be strongly scattered by GaN growth defects, such as threading dislocations, such high Q_{mech} point to the high-material quality in a GaN-SiC platform, especially at the GaN-buffer interface.



FIG. 3. Simulated frequencies of the two non-degenerate higher order Lamb wave modes (blue, inset right and red, inset left) as a function of inverse electrode period $1/\Lambda_{IDT}$. The respective mode displacement profiles for the two modes are shown in the inset. The Lamb wave resonance (inset, bottom) frequency ($N_{pairs} = 40$) is also shown (magenta). A zoomed-in section (shown by the dashed box) of the plot is shown in the inset for visualization. Simulation parameters: $t_{GaN} = 1.5 \ \mu m, t_{AIN} = 0.35 \ \mu m$ and $t_{Au} = 75 \ nm$

To quantify the effects of r_f , we can use the idea of degenerate mode-splitting. A bare GaN on sapphire substrate unit cell supports two degenerate Lamb wave modes (forward and backward propagating). Adding a gold electrode (as part of the IDT) couples the forward and backward modes, lifting the frequency degeneracy and forming two modes (shown as a function of IDT period, by the red and blue curves in Fig.3). The frequency splitting between the two modes is governed by the coupling between the original forward and backward propagating modes, and thus is a measure of r_f . For the IDT unit-cell, Fig.3 is plotting the 1D phononic bandgap at the Γ point as a function of Λ_{IDT} . It is important to keep in mind that only the lower mode is excited by the IDT due to RF excitation symmetry. Also shown in Fig.3 is the trapped fundamental mode frequency $(N_{pairs} = 40)$ and we can see that the trapped modes lie within the 1D phononic bandgap (zoomed inset in Fig.3). As long as the frequency separation ($\Delta \omega \approx$ 30 MHz) of the bound mode (magenta) from the guided band (blue) is greater than the mode decay rate ($\kappa \approx 3-5$ MHz in our devices), a sharp Lorentzian response, corresponding to the guided mode resonance, will be observed in the RF reflection spectrum and the IDT acts as a resonator. On the other hand, if $\Delta \omega \sim \kappa$, then bound mode spectrum overlaps with the guided mode band and the IDT acts as a transducer.



FIG. 4. Simulated Lamb wave fundamental resonance mode frequency (blue) and quality factor (brown) for GaN-on-sapphire devices with varying IDT periods ($N_{pairs} = 40$). Simulation parameters: $t_{GaN} = 1.5 \ \mu m$, $t_{AlN} = 0.35 \ \mu m$ and $t_{Au} = 75 \ \text{nm}$.

From a resonator design perspective, it is critical to understand the dependence of center frequency (f_c) of the resonator on the GaN device layer thickness (t_{GaN}), as that becomes the key fabrication parameter to control. While the IDT-based design does ensure that the f_c changes with IDT period, the quality factor (Q_{mech}) of the guided mode resonance is not constant as a function of frequency. Given a GaN layer thickness, there is an optimal frequency range (f_{opt}) for achieving high Q_{mech} . At $f \ll f_{opt}$, the finger reflection drops due to reduced $t_{Au}/\lambda_{acoustic}$. At the other extreme $f \gg f_{opt}$, the out-of-plane scattering and metal damping increases due to increased finger reflection and greater spatial mode overlap with the metal, on top of the standard f^2 acoustic wave attenuation dependence²⁴. We can visualize the confinement dependence on IDT period by plotting the simulated quality factor (Q_{sim}) for the fundamental Lamb wave resonance, for devices with N = 40 finger pairs ($t_{GaN} = 1.5 \mu m$, $t_{AIN} = 0.35 \mu m$ and $t_{Au} = 75$ nm). The results are shown in Fig.4. The quality factor (Q_{sim}) is calculated from an eigenfrequency calculation by $Q_{sim} = f_{real}/2f_{imag}$ ²⁵ where f_{real} and f_{imag} correspond to the real and imaginary components of the complex eigenfrequency. It is important to note that the FEM calculation does not properly account for high-frequency metal damping and the Q_{sim} is primarily an estimate of out-of-plane (substrate) scattering losses. As the plot shows, there is an optimal period for a given combination of t_{GaN} and t_{Au} to achieve the highest Lamb wave Q_{mech} . From the plots, we can construct a rule-of-thumb of ≈ 500 MHz of f_c tuning using the IDT period, while maintaining a high $Q_{sim} > 2000$.

While the Q_{mech} achieved by the device in Fig.2 is high, the presence of multiple closely spaced resonances distorts both the amplitude and phase response, making it challenging to use in practical applications. Ideally, one would like to work with a single isolated resonance with high Q_{mech} so that more complex elements, like coupled resonator filters, can be synthesized. The IDT device in Fig.2 had 125 finger pairs and as shown in Fig.1 (c,d), in a uniform period (dutycycle) IDT, adjacent sections of the transducer can support resonant modes, as shown in Fig.1(d), leading to an inher-



FIG. 5. (a) Measured RF reflection coefficient magnitude $|S_{11}|$ and phase $\angle S_{11}$ response for a GaN on SiC device with 50 finger pairs and IDT period 1.75 μ m. (b) Comparison of the measured RF $|S_{11}|$ response for the 50 ($\Lambda_{IDT} = 1.75 \ \mu$ m) and 125 ($\Lambda_{IDT} = 1.5 \ \mu$ m) finger pairs devices. The response of the N=50 device has been shifted in frequency for easier comparison.

ent multi-moded response. By reducing the number of finger pairs, we can effectively achieve single-mode operation in the device, shown in Fig.5. As both the amplitude ($|S_{11}|$) and phase ($\angle S_{11}$) response show in Fig.5(a), the response is primarily dominated by the fundamental mode. On the other hand, reducing the cavity size leads to lower mode confinement and reduced mode quality factors (Q_{mech}). This can be clearly seen in Fig.5(b) where the multi-mode and single mode (frequency-shifted) responses are plotted on the same scale. The single-mode device has a $Q_{mech} \approx 500$, compared to the $Q_{mech} \approx 2000$ for the multi-mode device. Ideally, one would like to combine the high Q_{mech} achievable with large N, with a single-mode response to enable design of more complicated circuit elements like coupled resonator filters.

To implement a high- Q_{mech} single-mode response, we can borrow ideas from the photonic crystal community on Gaussian 1D confinement^{26,27} of electromagnetic fields to achieve extremely high quality factors. In contrast to the optical domain where the refractive index is shaped in response to plane wave excitation, in the acoustic case, the metal electrodes provide both the excitation field and the confinement potential (due to the mass loading) and thus the mode shape and excitation efficiency are intimately linked, constraining the designs. Fig.6 (a) shows the mode shape for a uniform period IDT and Fig.6 (b) plots the mode displacement as a function of position. As the red Gaussian curve fit shows, the fundamental cavity mode shape can be well-approximated by a Gaussian with a peak displacement in the cavity centre.

By apodising the duty cycle of the IDT to match the Gaussian mode-shape, we can both improve the Q_{mech} and achieve single-mode operation. The improvement in Q_{mech} occurs due



FIG. 6. (a) Mode displacement of the trapped Lamb wave mode in a GaN-on-sapphire device (b) Line-cut of the mode displacement (magenta) alongwith a Gaussian fit (black) (c) Measured RF reflection ($|S_{11}|$) response of apodized IDTs fabricated on a GaN-sapphire platform ($t_{GaN} = 1.15\mu m$, $t_{AlN} = 0.575 \mu m$, $t_{Au} = 75nm$) with different duty cycle chirps. The Q_{mech} of the Lamb wave resonance of each device, calculated from a Lorentzian function fit to the S_{11} power spectrum, are ~ 322, 386 and 478 respectively

to two effects: since the peak of the modal displacement occurs in the cavity centre, by reducing the duty cycle of the IDT, we are effectively reducing the overlap of the acoustic field with the metal, which is the major source of damping and scattering. By apodizing the grating, we also reduce the \vec{k} -space overlap between the Lamb wave resonance and the substrate modes, reducing the overall out-of-plane leakage²⁸. Apodising the IDT-period also ensures single mode operation as the local duty cycle chirp ensures that higher order modes (such as those shown in Fig.1(d)) are not trapped. Fig.6(c) shows the measured RF $|S_{11}|$ spectrum of three devices with identical period and number of finger-pairs ($N_{pairs} = 100$), but varying duty-cycle Gaussian chirp fabricated on a 1.15 μm GaN on Sapphire platform. The measurement results indicate that as we increase the duty-cycle chirp, we observe increased mode separation, a key step towards single-mode operation. We also see that the excitation efficiency (peak $|S_{11}|$ dip) is not uniform and attribute this to the mode excitation and confinement being provided by the same electrodes. We are currently working on achieving independent control of the excitation and confinement by patterning the GaN layer²⁹. Although the phononic crystal designs do show an improvement in Q_{mech} , the GaN-on-sapphire devices do not achieve the performance of the uniform Λ_{IDT} GaN-on-SiC devices, primarily due to the inferior quality of the GaN-substrate interface, which leads to excess acoustic scattering and dissipation.

Finally, as a first step towards integrated resonant Lamb wave filters in GaN, Fig.7 shows the RF transmission spectrum for a coupled resonator device with $\Lambda_{IDT} = 2 \ \mu m$ and resonator spacing 10 $\ \mu m$. The transmission spectrum is peaked around the Lamb wave resonances, which can be seen in the overlaid S_{11} spectra. We would like to note that while the insertion loss is high (~ 18 dB), there is tremendous scope for performance improvement by optimising the device geometry (ensuring high- Q_{mech} single mode operation) and filter design (controlling the coupling rate between the two resonators).



FIG. 7. RF transmission (S_{21}) spectrum of a coupled resonator device fabricated on a GaN on SiC platform ($\Lambda_{IDT} = 2 \ \mu m$ and resonator gap = 10 μm). The resonator response (S_{11}) is overlaid for reference.

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