

Mechanisms of TiB₂ and graphite nucleation during TiC-B₄C high temperature interaction

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Abstract

Reactive hot pressing of TiC-B₄C precursors was undertaken at 1800 °C to produce TiB₂ with carbon inclusions. Atomic mechanisms of titanium diboride nucleation, as well as sponge-like carbon inclusions and submicron platelets of graphite precipitation has been investigated. Precursor grain size, green body composition and synthesis time were varied to analyse phases transformation. Boron from B₄C grain sublimation is shown to result in carbon-based foam formation. Ab-initio calculations confirm that the boron atoms accumulation on (111) TiC plains leads to tensile stress. The developed stress cleaves TiC grains and enhances further reaction. Most of carbon expelled from TiC during its transformation into TiB₂ forms graphite platelets.

Key words: titanium boride, titanium carbide, hetero-modulus ceramics, reactive sintering, reaction mechanisms, inclusions, precipitation, graphite platelets.

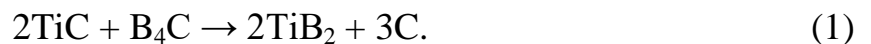
1. Introduction

Presence of graphite or hexagonal boron nitride phases in superhard and refractory carbides, nitrides and borides result in substantial increase of thermal shock resistance [1-3], and machinability [4-6], with no impediment of high temperature properties. Some penalty, associated with the soft phases to hardness and strength are considered to be a “fair price” for other gains. The inclusions positive influence has been demonstrated by numerous investigations of hetero-modulus ceramics (HMC): $\text{Si}_3\text{N}_4\text{-BN}$ [5, 6], TiC-C [2, 7, 8], $\text{B}_4\text{C-BN}$ [4, 9], SiC-BN [10], $\text{TiB}_2\text{-TiC-C}$ [11], $\text{ZrB}_2\text{-SiC-C}$ [12 – 15], $\text{HfB}_2\text{-HfC-C}$ [16] and glass-BN [17]. Theoretical and experimental research, presented in all the mentioned studies, have showed that the influence of low-modulus phase on the material characteristics is closely related to sizes, shapes, and the distribution of the soft inclusions within the solid matrix. As it can be concluded from numerous works [6, 9, 11, 17, 18], soft particles can not only “weaken” material but also improve its fracture resistance. This is achieved when cracks are arrested by blunting crack tips at low-E – high-E material interfaces. Achieving maximum of the interface area at the given and minimal low soft phase volume is therefore one of the most important directions of HMC structure optimization. As was shown in [18] the optimal interface/volume ratio can increase material toughness at least two fold. Moreover, effective optimization can be done with a specific architecture of ultra-fine, supposedly plate-like, soft inclusions evenly distributed inside the hard matrix.

One of the most valuable ways to create the mentioned ceramics is the reactive hot pressing of $\text{TiC-B}_4\text{C}$ precursors [18]. The process bases on quick (for 1 min at 1800 °C [19]) precursor disappearance accompanied with TiB_2 and graphite solid phase synthesizing. During the process, titanium diboride forms the material hard matrix, while graphite can be observed as (i) 2 – 4 μm sponge-like areas or (ii) submicron platelets [18]. As is shown in [20], other transitional metal carbides can also interact with B_4C in similar way. This paves the way of reactive sintering approach, which can be applied to sintering of various refractory systems.

In order to maximize mechanical characteristics of such materials, one need to select sintering process and precursor composition in such a way that graphite phase segregates in the form of submicron platelets. At the same time, sponge-like soft graphite phase should be minimized. The particle shape and distribution optimization is impossible without the understanding of microscopic mechanisms of the phase formation process.

Hence, the main aim of the presented work is to uncover mechanisms of TiB₂ and graphite nucleation and growth during the reaction:



Bearing in mind reactive sintering of different MeB₂-C-based heteromodulus ceramics with preassigned composite structure and mechanical characteristics we will try to address the following questions:

- what is the cause of quick TiC to TiB₂ solid phase transformation;
- where does the carbon move from a metal carbide being replaced with boron;
- how do carbon ‘platelets’ and ‘sponges’ form?

2. Experimental

Commercially available powders of TiC (~70μm), TiC (~3μm), B₄C (~60 μm) and B₄C (~2μm) (all of them produced by Donetsk Reactive Factory, Ukraine) were used as the green body materials. The material purity was at around 99.00 at%. Material powders with big grains are later referred as “rough” and powders with small grains are referred as “fine”.

Table 1. Samples green body compositions and dwelling times at 1800 °C

#	TiC (3 μ m), at.%	TiC (70 μ m), at.%	B ₄ C (2 μ m), at.%	B ₄ C (60 μ m), at.%	t, min
1.1	60	-	-	40	2
1.2	60	-	-	40	4
1.3	60	-	-	40	8
1.4	60	-	-	40	16
2.1	-	30	70	-	2
2.2	-	30	70	-	4
2.3	-	30	70	-	8
2.4	-	30	70	-	16
3.1	30	-	70	-	2
3.2	30	-	70	-	4
3.3	30	-	70	-	8
3.4	30	-	70	-	16

The powder mixtures of three different composition sets (Table 1) were mixed in a planetary mill for 5 minutes and hot-pressed in a graphite die at 1800°C and 30 MPa. Maximum temperature isothermal dwelling time ranged between 2 and 16 min. Sample compositions were chosen to provide the excess of one of the components. This was done to observe the process evolution of boron carbide (1.1 – 1.4, 3.1 – 3.4) and titanium carbide (2.1 – 2.4) during sintering.

Crystalline phases in the sintered specimens were examined by X-Ray diffraction (XRD) (DRON-4M, St. Petersburg, Russia). Analysis of the microstructure and compositional analysis were performed with Scanning Electron Microscopy (SEM) and Energy Dispersive X-Ray Spectroscopy (EDX) (FEI Quanta 3D and Oxford Instruments INCA systems). For SEM and EDX analysis, samples were cleaved as this allowed to avoid polishing artefacts in material with great variation of constituent structures hardness. All SEM images presented in this work are taken with an electron backscatter detector (BSD) in so named Z-contrast mode. It means that the structures (grains) with the higher Z elements (and/or higher concentration of such elements) appear as the brighter areas on the images shown.

Ab initio calculation of boron impurities influence on TiC structure was carried out by density functional theory (DFT) in generalized gradient approximation (GGA) using ABINIT

software package [22]. The annealing of the atomic positions was simulated according to the algorithm described in [23].

3. The experimental results

3.1. Evolution of B₄C during high temperature decomposition and mechanisms of graphite sponge-like areas formation

The phase composition of samples # 1.1 – 1.4 with grainy B₄C and the excess of finer TiC particles in the green bodies was, as expected, changing with the sintering time by diminishing of boron and titanium carbides alongside with the gaining in TiB₂ and graphite (See Fig. 1). It could be observed that: (i) boron carbide disappears between 4 and 8 minutes of the sintering and the process is accompanied by the most pronouncing change in TiB₂-TiC ratio; (ii) while the reaction (1) is almost completed after 8 minutes, the distinct graphite peak appears only in XRD pattern of sample 1.4 (sintering time 16 min). This suggests that the carbon crystallization is a relatively slow process which continues after the main reaction completion.

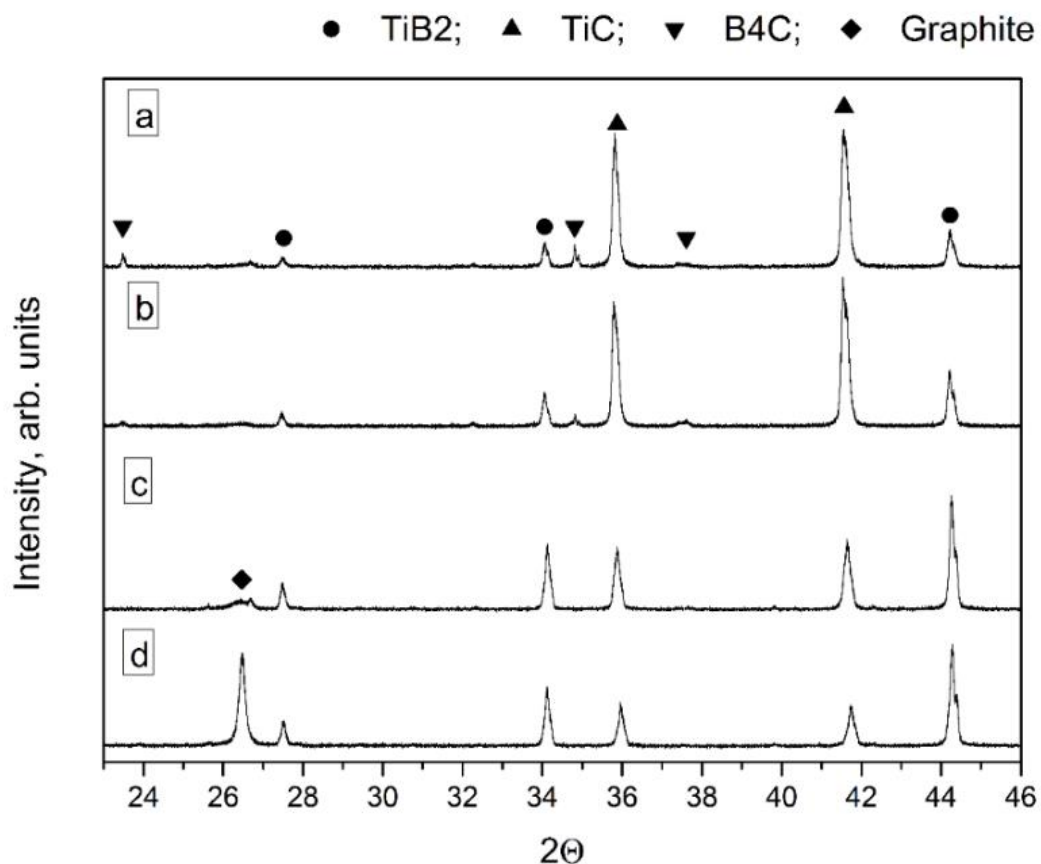


Fig.1. XRD of samples with rough B₄C and excess TiC sintered at 1800°C for 2min (a), 4min (b), 8min (c), 16min (d) (samples #1.1 – 1.4)

Fracture surface of sample number 1.2 (dwelling time 4 min) is presented on Fig. 2. It shows large (~40µm) dark appearing grains surrounded with little (<5µm) lighter ones. Element composition of the central dark cleavage (See Fig. 2) fairly corresponds to boron carbide. Line EDX elemental intensity profile analysis shows that boron content gradually decreases near the B₄C grain indicating new-formed TiB₂-based layer. Sharp peaks of carbon can be seen at the B₄C area edges.

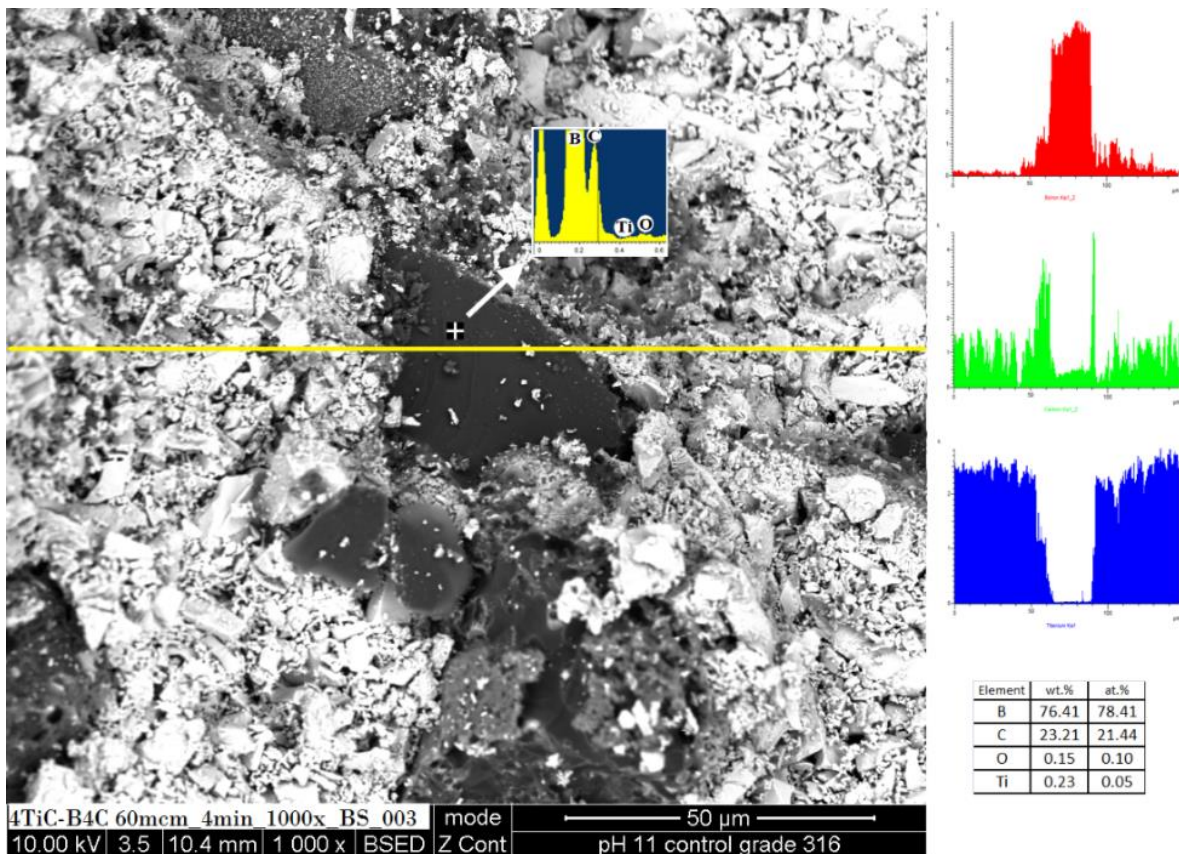
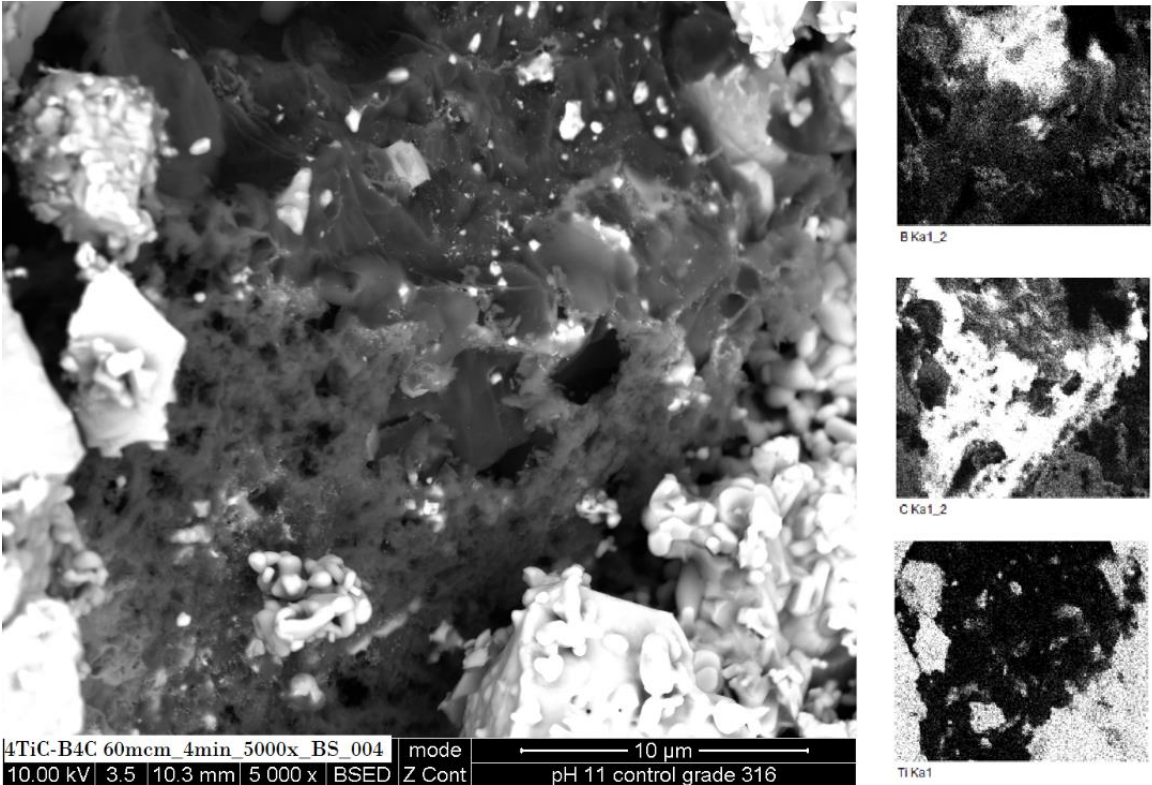


Fig. 2. BSE image of the fractured sample number 1.2 surface. The point EDX analysis spectra is shown with the quantification data table on the right. Elemental intensity profiles (boron, carbon and titanium) along the line on the right.

EDX mapping of the boron carbide particle surface presented on Fig. 3, allows observing three types of different structures: (i) boron rich area, evidently revealing what remains of B_4C grain; (ii) submicron Ti-rich objects embedded in B_4C – which, considering the XRD-analysis, are TiB_2 nuclei; and (iii) carbon-rich foam-like (possibly amorphous) substance covering boron carbide. Hence, here we can see the initial stage, as shown in [19, 21], of TiC- B_4C reaction process, manifesting itself by boron transportation from B_4C into titanium carbide. During this stage of sintering, the near surface layers mount up high concentration of B vacancies and in the end transform into foam-like carbon material. Some titanium atoms diffuse from TiC via the cover carbon and accumulate in the inner parts of the boron carbide grain. This results in titanium diboride nucleation inside the Fig. 3. BSE image of the fractured sample number 1.2 surface



(1800°C, 4min). EDX elemental maps (boron, carbon and titanium) are shown on the right.

B_4C crystals.

Foam-like carbon cannot prevent transportation of sublimated boron. As the result, green body boron carbide grain size distribution does not affect the speed of decomposition. Fig. 4 presents a BSE image and EDX elemental maps of the powder mixture after 8min annealing (sample 1.3).

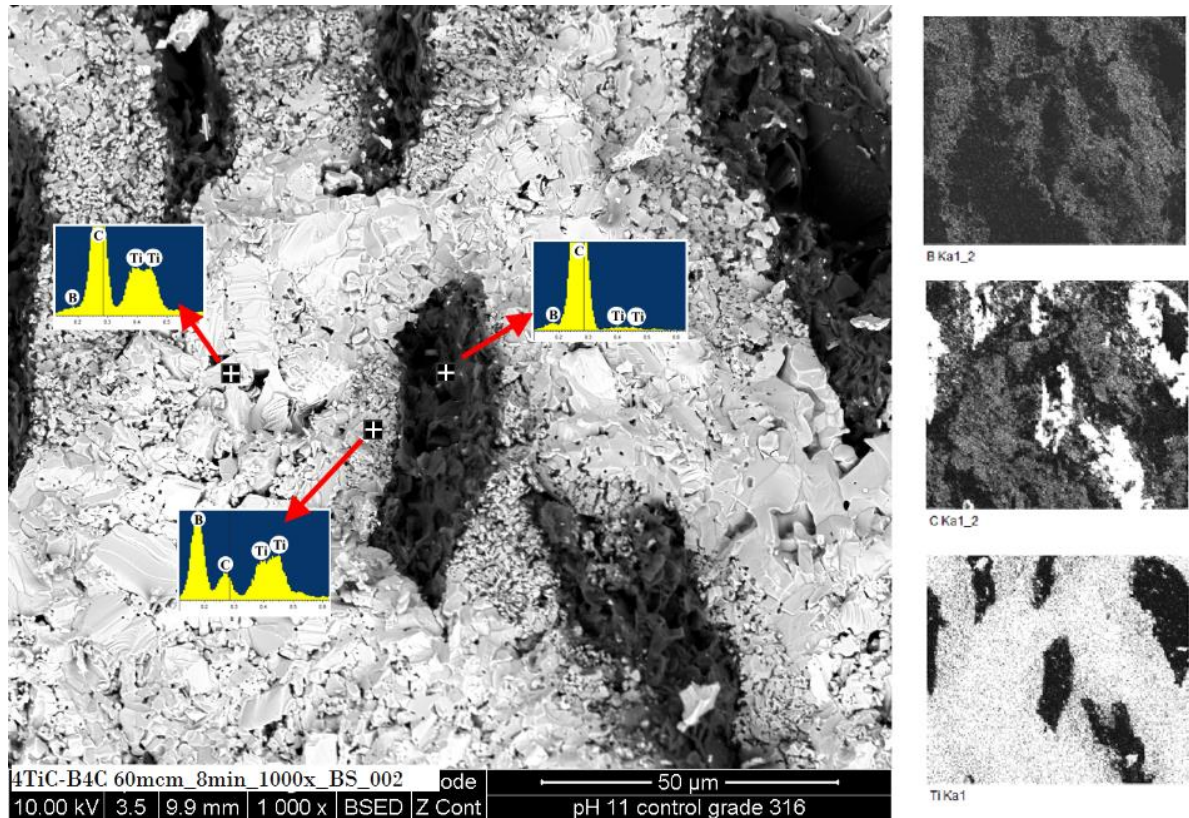


Fig. 4. BSE image of the fractured sample number 1.3 surface (sintering time 8 min). EDX elemental maps (Boron, carbon and titanium) are shown on the right.

The observed material maps support the above statement and demonstrate three different phases: (i) carbon (dark grey, rather porous areas), (ii) titanium diboride containing considerable amount of carbon (grey areas surrounding carbon ones), and (iii) residual titanium carbide containing slight boron addition (light grey regions).

Considering the initial grain sizes, the large sponge-like carbon regions can only be leftovers of boron carbide grains. Small titanium diboride particles can be observed inside (See Fig. 4). Further sintering (for 16 min) leads to graphitization and partial densification of carbon sponges

(See Fig. 1 and Fig. 5) alongside with segregation of graphite plates within new TiB_2 grains (See Fig. 5 and the text below). Basing on the initial sizes of B_4C grains ($\sim 70\mu m$), a sponge consists $1/2 - 1/3$ of the precursor crystal.

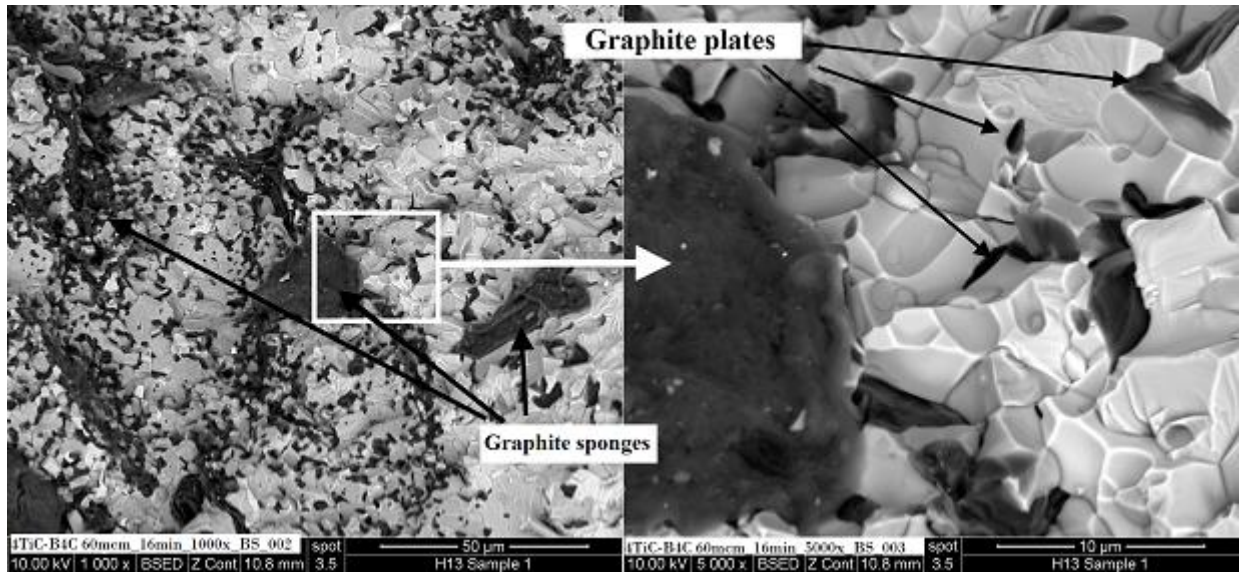


Fig. 5. BSE image of the fractured sample number 1.4 surface (sintering time 16 min). Two types of carbon: foam-like covering in place of grainy B_4C leftovers and separate carbon plates within TiB_2 grains.

It should be noted that fracture surfaces of the samples containing large boron carbide grains (See Fig. 2, 4, 5) show no faceted voids presented in [21]. The possible explanation of the fact could be as follows: boron carbide in samples 1.1 – 1.4 was in deficiency. Thus, B_4C crystals decomposed too fast and the voids did not have time to be formed by boron vacancy aggregation. To prove the statement, we produced additional sample sequence 3.1 – 3.4 (See Tab.1) with the excess of large B_4C particles. The XRD pattern of sample 3.4 (Fig. 6) shows clear B_4C peaks after 16 min sintering.

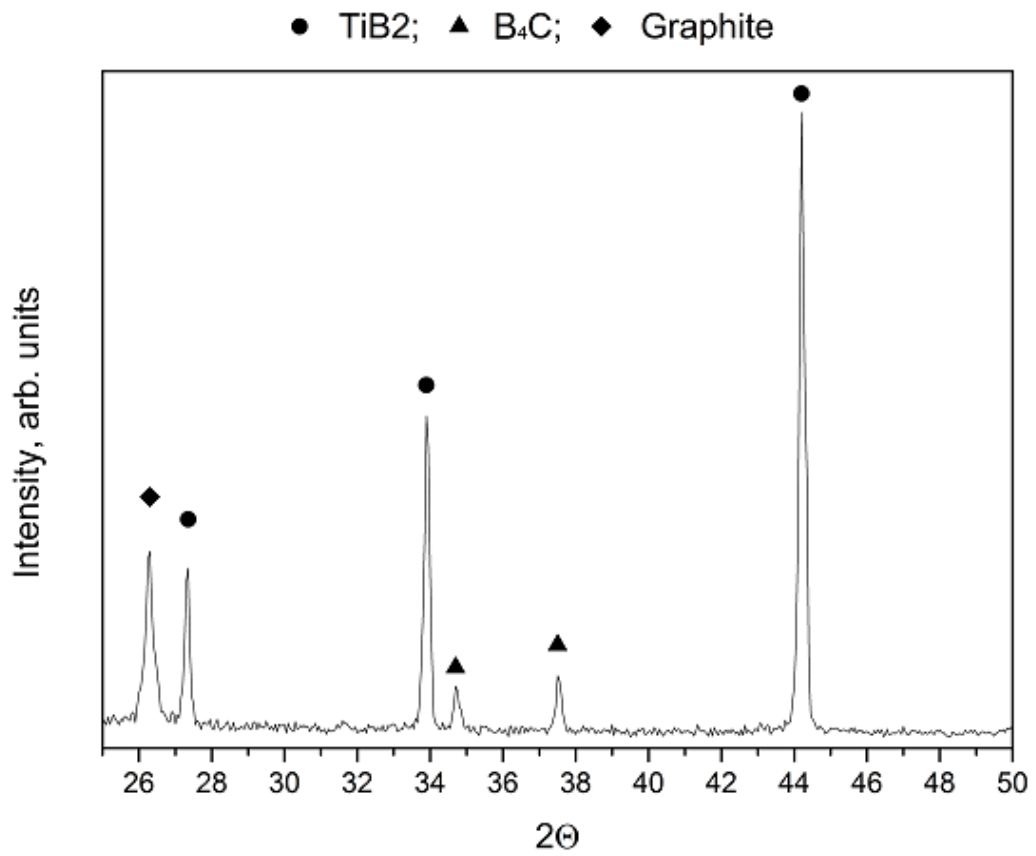


Fig. 6. XRD spectra of sintered for 16 min sample (sample 3.4)

As is shown on Fig.7 boron carbon contains fair amount of discussed faceted voids. Worth noting, that many of the voids contain tiny titanium diboride particles inside.

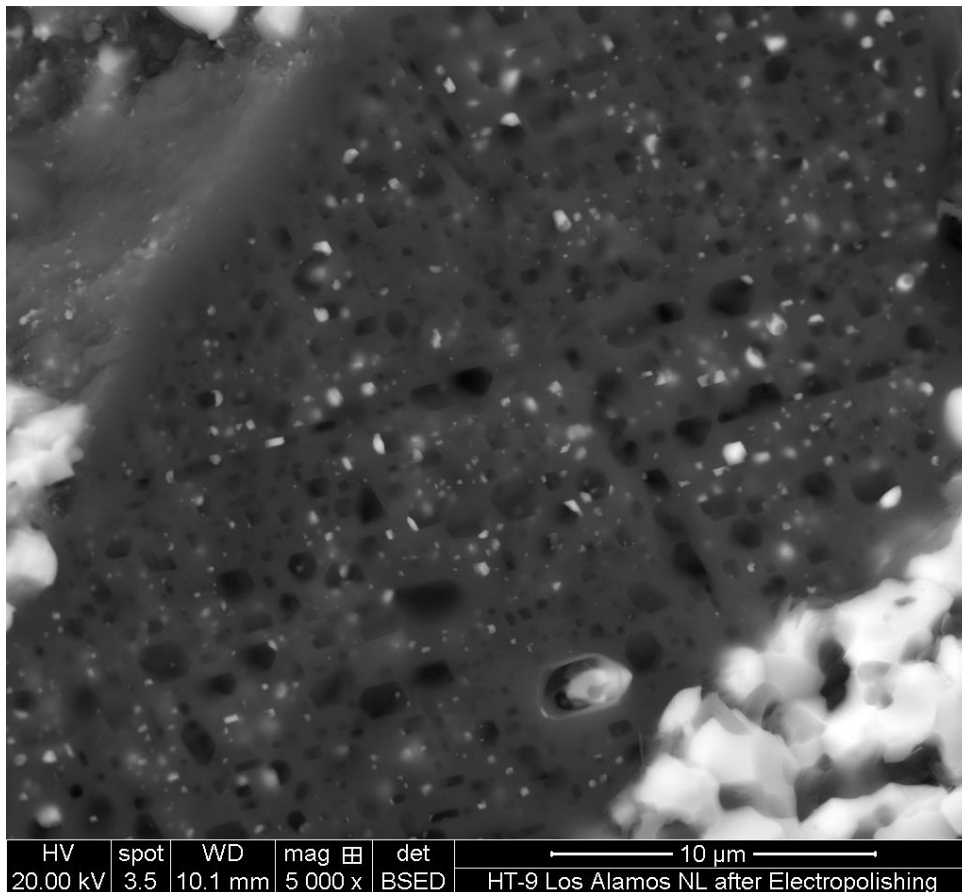


Fig. 7. BSE image of the fractured sample # 3.4 surface (sintering time 16 min).

3.2. TiC to TiB₂ transformation and graphite platelets precipitation

So far, we investigated phenomena following the process of boron atoms leaving B₄C crystals. The second part is to examine process of boron moving into the titanium carbide grains. For this we explored samples 2.1 – 2.4 produced via hot pressing of large (~70μm) TiC particles mixed with the excess of finely dispersed (~2μm) boron carbide powder (See Tab. 1).

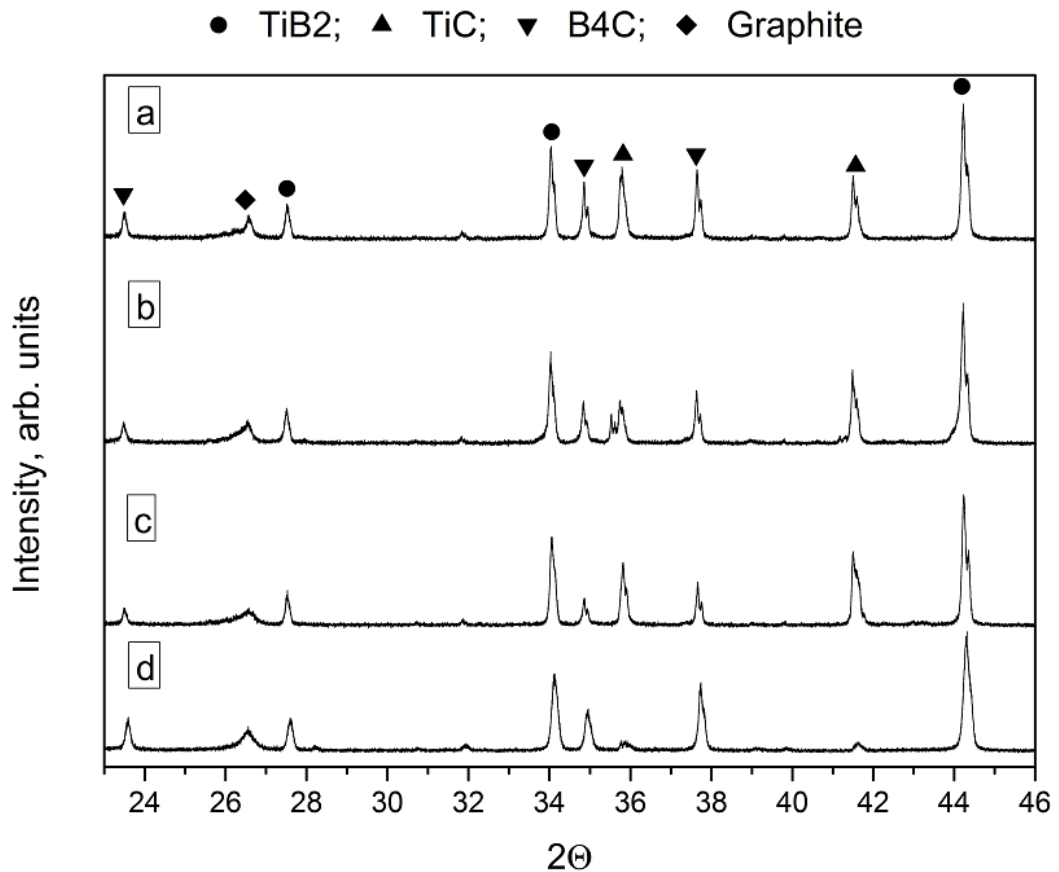


Fig. 8. XRD spectra of sintered samples with grainy TiC and excess of B₄C in the green body. Sintering time at 1800°C: 2min (a), 4min (b), 8min (c), 16min (d), (samples 2.1 – 2.4, Tab.1).

The evolution of sample phase composition (XRD data, Fig. 8) reflects, in general, the reaction (1) progression. SEM image of sample 2.1 fracture surface (see Fig. 9) shows formation of inhomogeneous reaction layer between B₄C and TiC precursors after 2min sintering. There are three different parts of the structure: The “outer” one (most remote from TiC bulk) containing roughly equiaxial submicron B₄C grains, “middle” one consisted of elongated micron sized features, and the most porous “inner” one with seemingly amorphous phase. There are also visible planar defects in TiC near the grain border.

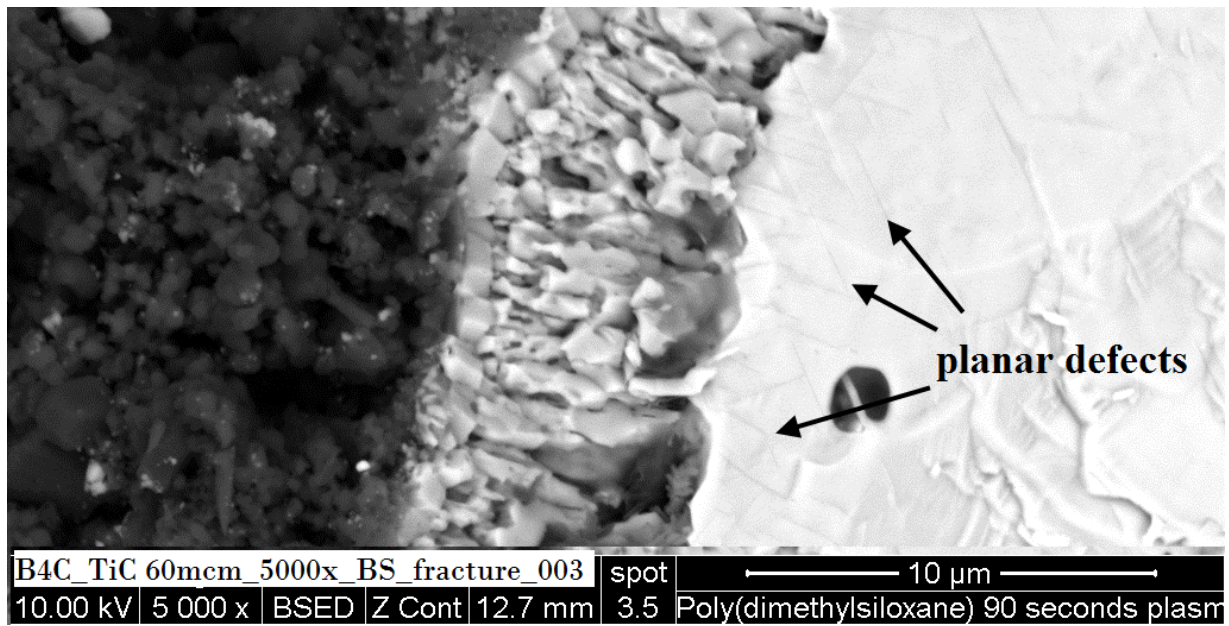


Fig. 9. BSE image of sample # 2.1 fracture surface (sintering time 2 min). B₄C (dark grey) and TiC (light grey) precursors separated with Ti-B-C (grey) reaction layer

EDX analysis of the reaction layer (See Fig. 10) cannot be interpreted in terms of precise atomic composition of the explored areas (as the surface is not plain and grains are too small); however, it is evident that all the grains have substantial amounts of all main elements (carbon, boron and titanium). Hence, the observed reaction layer has neither carbon inclusions nor diboride particles and can be identified as a “proto-structure” of future TiB₂ covering. Interestingly, that border TiC contains considerable amount of boron atoms (See Spectrum 3, Fig. 10) which should seemingly be connected to the reaction mechanisms.

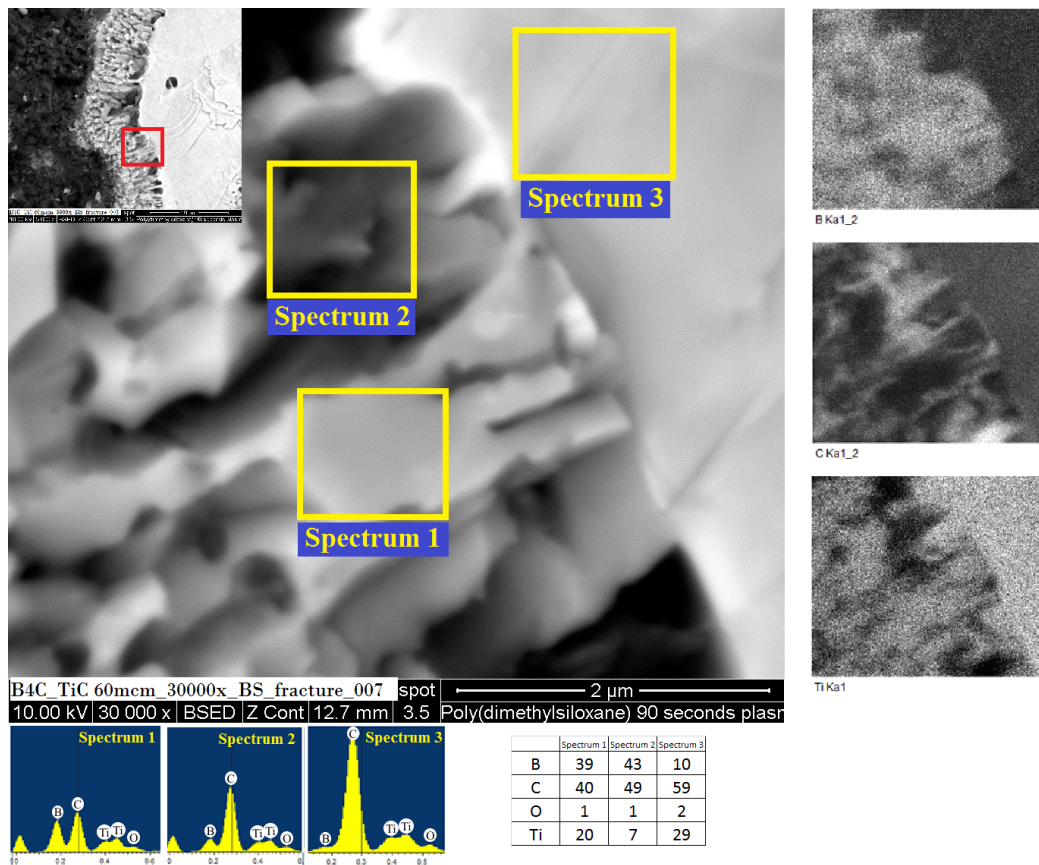


Fig. 10. BSE image of the fractured surface of sample 2.1 (sintering time 2 min). The reaction layer. EDX elemental maps on the right.

Fracture surface of sample 2.3 sintered for 8min (see Fig. 11) presents already formed continuous TiB_2 layer (spectrum 2, Fig. 11) which separates B_4C and TiC precursors. It should be noted that EDX analysis indicates no diffused titanium atoms inside the B_4C grain while both titanium carbide and titanium diboride contain considerable amounts of boron and carbon respectively (See Tab. 2).

Table 2. EDX quantification data from the analysis spots of sample 2.3 (See Fig. 11)

Spectrum #	B, at. %	C, at. %	Ti, at. %
1	78	22	-
2	66	2	34
3	6	45	49

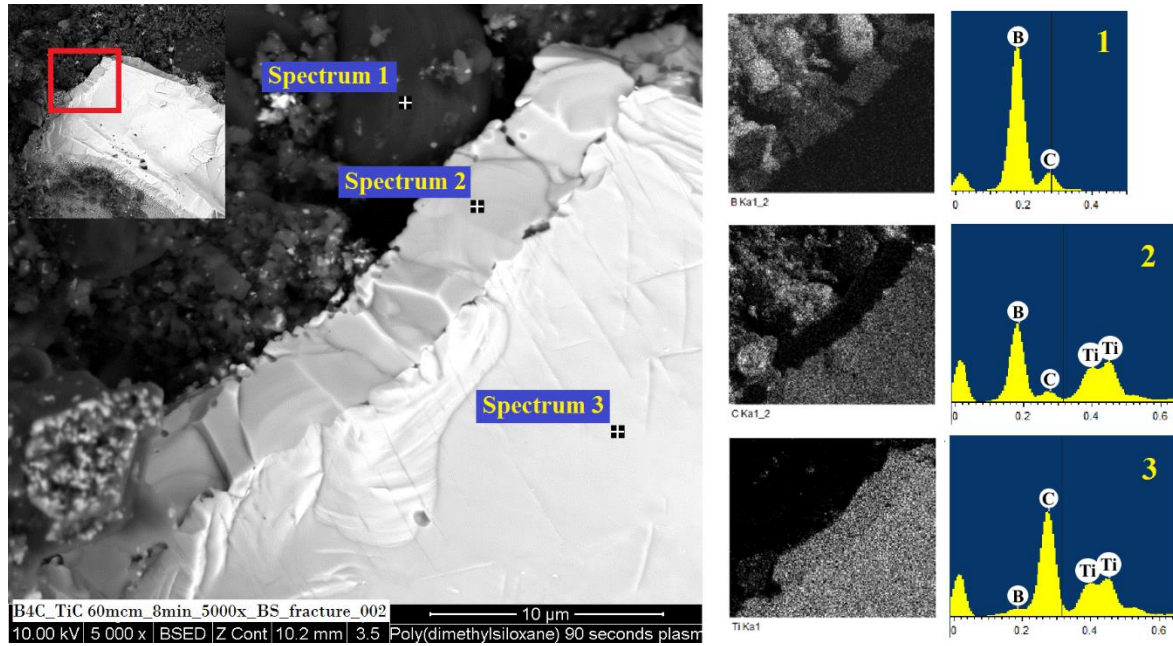


Fig. 11. BSE image of the fractured sample number 2.3 surface (sintering time 8 min). EDX elemental maps (boron, carbon and titanium) and EDX spectra from the distinctive areas (See Tab. 2) on the right.

Sintering of the precursor mixture for longer, for 16 min in total, results in further changes in the reaction area (see Fig. 12). Similarly to the 8 min sample 2.3, titanium diboride layer is solid and has the same thickness ($\sim 6\mu\text{m}$) which indicates that TiB_2 formation mostly accomplished during first 8 minutes of the sintering. However, as opposed to sample 2.3, 16 min sintering led to formation of carbon inclusions in TiB_2 -TiC interface. The carbon inclusions have platelet shape and could only origin from consolidation of TiC grain carbon being replaced with boron atoms in the reaction region.

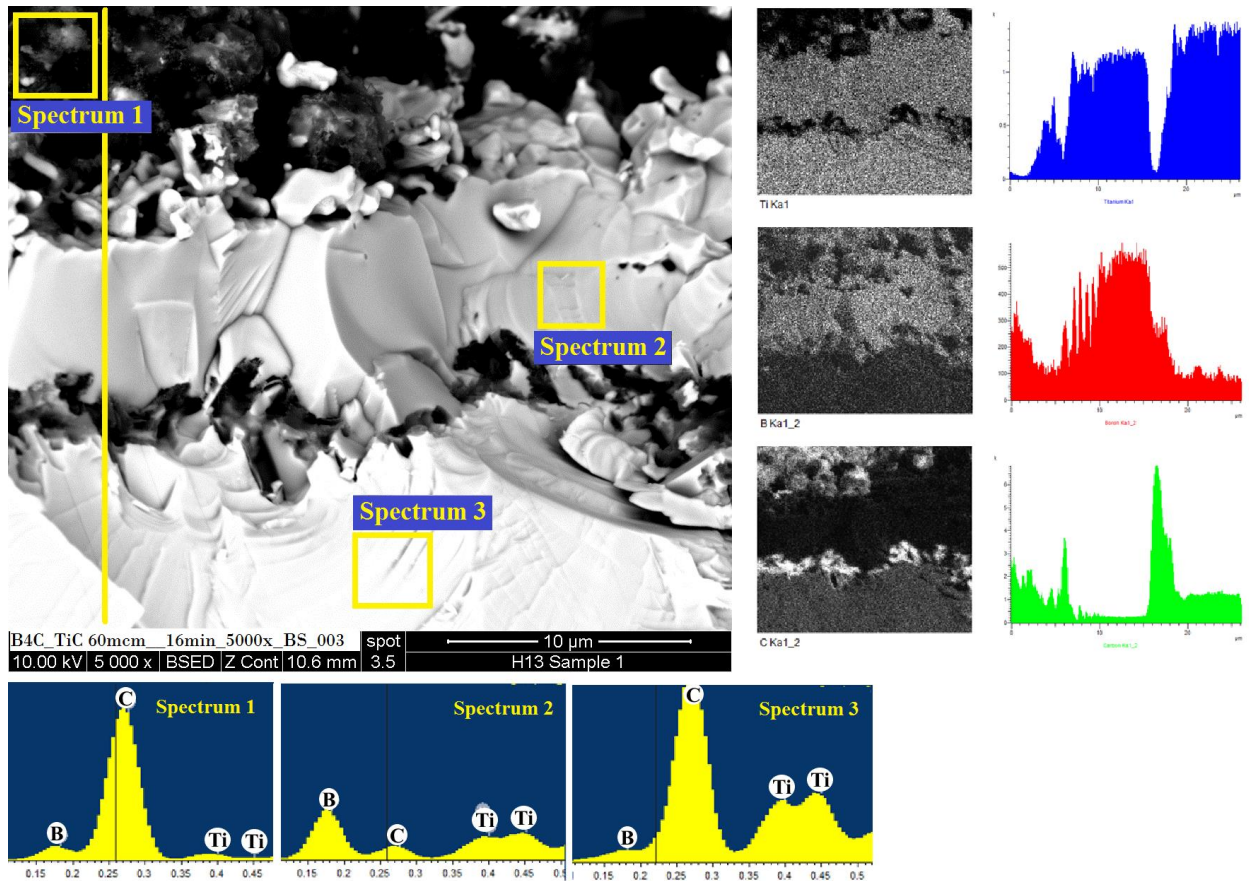


Fig. 12. BSE image of the fractured sample number 2.4 surface (sintering time 16min). Image of TiC-B₄C reaction layer. EDX elemental maps and EDX elemental intensities along the line are on the right.

4. Discussion

As has been shown earlier [19, 21], TiC-B₄C high temperature reaction starts with boron evaporation from boron carbide surface. It can be seen from Fig. 3 that such boron depletion of B₄C near-surface layer converts it into carbon-based foam. The foam, having a high amount of extra fine vacancies and pores, provides a high permeability media for sublimated boron efficient transfer from the inner areas of B₄C crystals and enables the reverse diffusion of Ti-atoms. Further association of B-vacancies leads to formation of submicron faceted voids inside the remnant B₄C (See Fig. 7). Great Ti diffusion fluxes cause its essential concentration gradients inside the

decomposing B_4C phase. As it is shown in [24], such gradients strongly affects the incubation time of new phase nucleation. That is why the TiB_2 particles do not appear near TiC interfaces (where the concentration of titanium atoms is higher). It looks like that the void surface provides best energy opportunity for the titanium diboride formation (See Fig. 7).

In case of no boron carbide excess (regarding the stoichiometry of $TiC:B_4C = 2:1$), the boron depletion at last turns B_4C grains into carbon-based sponge-like areas with tiny TiB_2 particles inside (Fig. 4).

Titanium diboride forming on TiC grain surface could, in principle, create a diffusion barrier for further atomic exchange between the precursors. For instance, Schmidt and Borchardt [25] showed that the diffusivity of boron in TiB_2 obeys Arrhenius' law, with an activation energy of 2.2eV and a preexponential factor of $4 \cdot 10^{-12} m^2/s$. Considering sample 2.3 annealing parameters ($t = 8$ min and $T = 1800$ °C), the value of diffusion length ($L = 2(Dt)^{1/2}$) is ~ 250 nm which is at least one order less than TiB_2 covering thickness (See Fig. 11). On the other hand, Fan et al [26] reported the diffusion energy barrier of B in TiC to be 0.84 eV along (001) plain and 0.69 eV along (111), thus boron atoms migration in titanium carbide can be several orders of magnitude greater.

Vekables [27] and Chien et al [28] showed that the “trace” boron concentration in titanium carbide initiates precipitation of TiB_2 platelets along (111) plane of TiC lattice. The TiB_2 platelets [27] had ~ 1 nm thickness and $\sim 0.5 \mu m$ length, which are too small to be identified by SEM themselves, however the precipitate traces are possibly seen as already mentioned TiC planar defects close to reaction area (see Fig. 9). It is worth noting that titanium planes in TiB_2 (Fig. 13a) are quite similar to Ti (111) in TiC (Fig. 13b). From that point of view, to convert NaCl-type structure of TiC into hexagonal structure of TiB_2 , one need to: (i) replace carbon atoms with boron; (ii) place boron into interstitials (blank circles on Fig. 13b); (iii) shift Ti plates. It is well known [28, 29], that titanium carbide is always carbon deficient (from 2 to 40% of the carbon atoms are absent in TiC crystals), thus the first step can start with migrating boron being captured in the

carbon vacancies. To make first step in understanding of TiC lattice behavior in the case of boron accumulation along (111) planes we employed computer modelling.

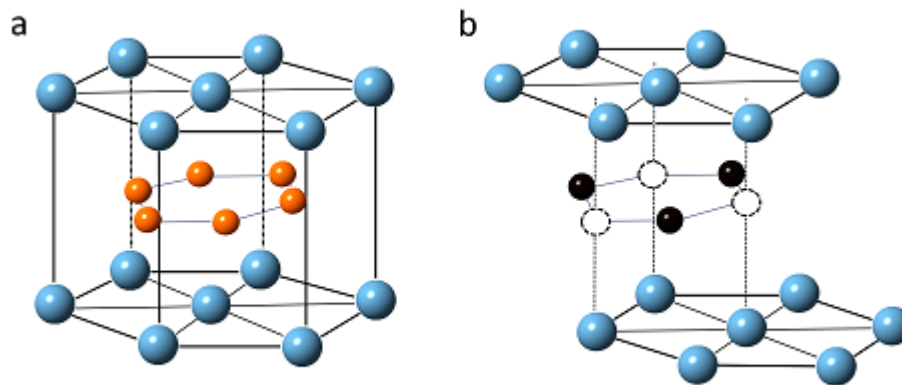


Fig 13. Titanium diboride (a) and titanium carbide (b) lattices. Empty circles mark interstitial positions

Ab initio calculations

A supercell containing 24 atoms: three (111) layers (close-packed ABC structure) by four titanium atoms and corresponding carbon ones, was chosen for the analysis (See Fig. 14a).

Three boron atoms were incorporated into the supercell in two different ways. In the first case, three boron atoms were placed in carbon substitution positions, in the second case, two B substituted C and the third B was placed in the interstitial position, in correspondence to TiB₂ lattice.

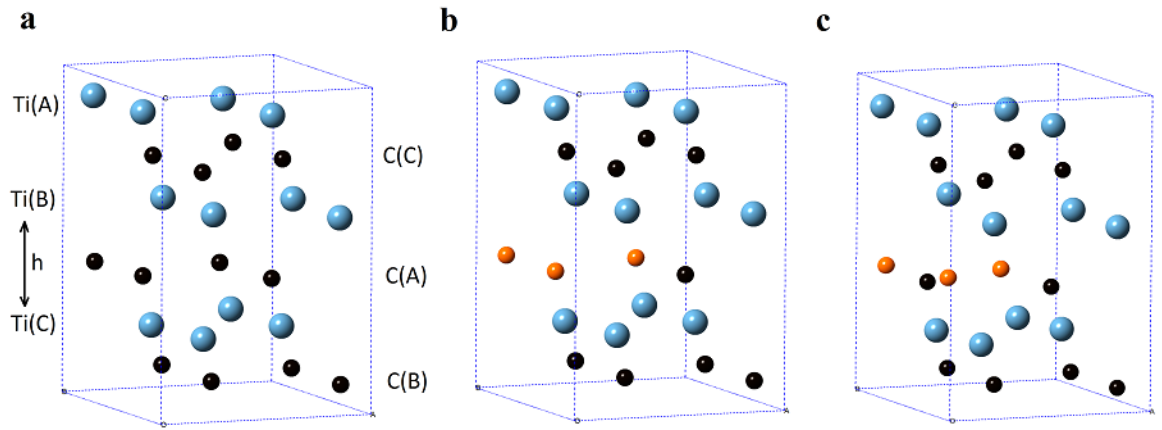


Fig. 14. TiC-based supercell with boron dope (Ti – blue, C – black, and B - orange). Three (111) titanium layers (close-packed ABC structure) with corresponding carbon ones (a); three boron atoms substitute carbon (b); two boron atoms substitute the carbon ones and one boron is situated in the interstitial position (c).

When boron atoms were incorporated into the supercell, the lattice relaxation was simulated according to forces calculated from the first principles. As is evident from Fig. 15, an equilibrium interplanar spacing between adjacent (111) Ti layers rises by 8% in the case of three carbon atoms being substituted with three boron ones (Fig. 14b), and by 10.5% if two boron atoms substitute carbon and one is situated in the interstitial position (Fig. 14c).

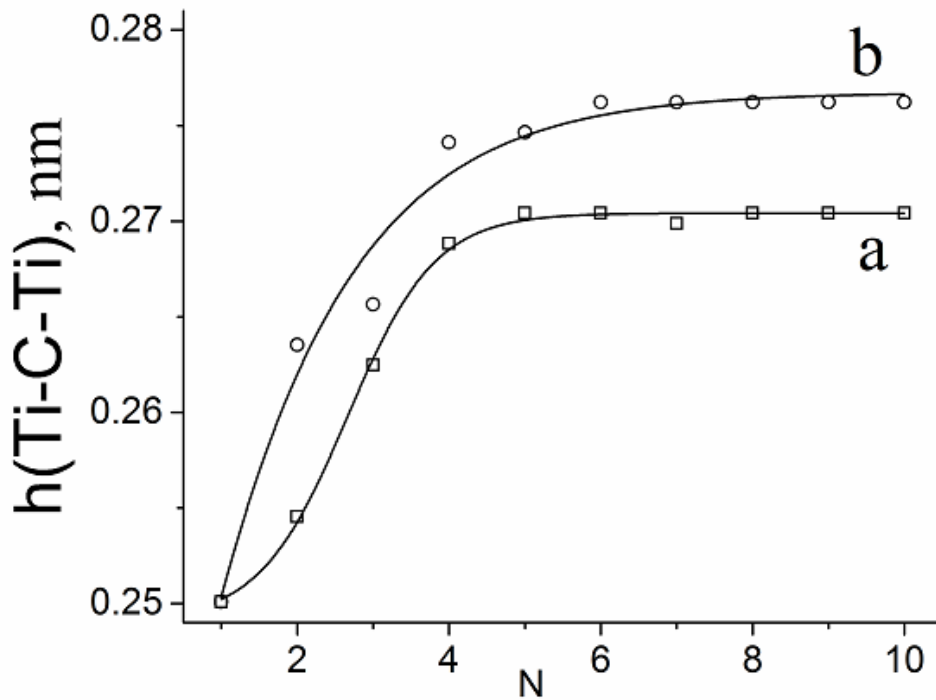


Fig. 15. The change in spacing between adjacent Ti layers after N steps of the lattice relaxation simulated with three B atoms incorporated into the supercell: (a) all the boron atoms replace carbon; (b) two boron atoms replace carbon, and the third one is in the interstitial position.

Therefore, boron atoms being captured by carbon vacancies lead to increase in the distance between (111) planes in TiC and this process possibly increases the probability of further boron incorporation into TiC lattice and leads to TiB₂ formation. Nucleating TiB₂ platelets, with Ti (111) interplanar spacing 28% greater than that of TiC, produce substantial tensile stresses, while the displaced carbon concentrates in TiC-TiB₂ interface and weakens it. At the certain level, the stresses fracture TiC grain, chipping off newly formed titanium diboride grains.

Fig. 16 shows an image of cleaved titanium carbide grain near TiB₂ border. Two faceted pits can be clearly seen on the cleavage surface. It is well known that the cubic crystals are the weakest along (100) set of planes. Therefore, considering the cleavage surface corresponds (100) direction,

the mentioned pits reveal (111) planes and illustrate the TiC grain weakened by the formed TiB₂ platelets.



Fig. 16. BSE image of fracture surface of TiC grain (white) surrounded with TiB₂ (gray) with faceted pull-outs (sample 2.3).

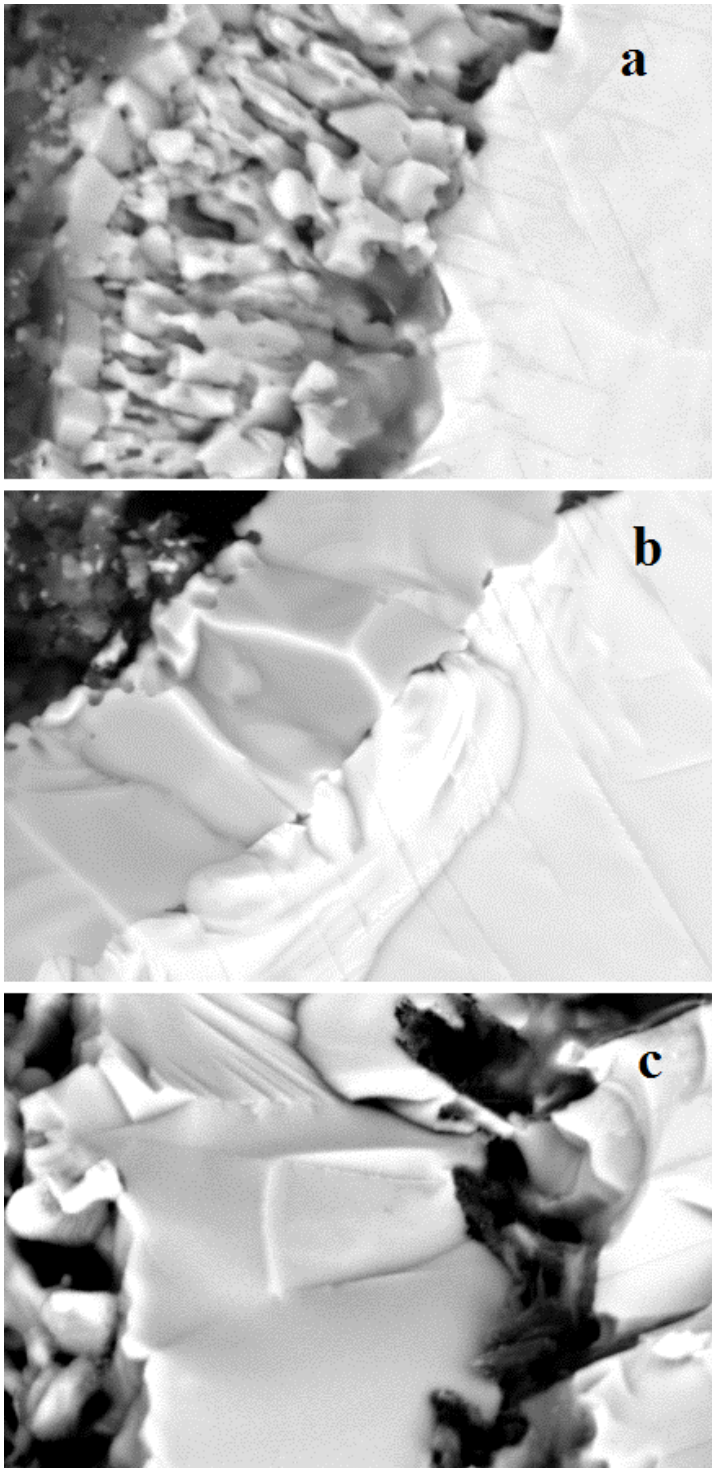


Fig. 17. BSE image of fracture surfaces. TiC-B₄C reaction layer after 2min (a), 8min (b) and 16min (c) sintering at 1800°C (samples 2.1, 2.3, 2.4).

Therefore, as growing TiB₂ nuclei fracture TiC crystals, B via TiB₂ solid-state diffusion can no longer limit the conversion reaction: the sublimated boron diffuses through porous Ti-B-C reaction structure (See Fig. 17a) and condenses on the fresh TiC surfaces. Further sintering leads

to quick densification of initial reaction area due to external pressure and additional reaction heat release (Fig. 17b).

Some carbon atoms remain inside the consolidated diboride layer. As is shown in [20], equilibrium C in TiB_2 concentration, which cannot exceed 2 at.% even at 2500°C, is negligible at 1800°C. Therefore, remaining carbon precipitates after 16 min sintering near TiB_2 border forming submicron graphite plates on TiC-TiB_2 interface (Fig. 17c).

5. Conclusions

The reactive high temperature structure formation of $\text{TiB}_2\text{-C}$ based heteromodulus ceramics starts with boron carbide grain surfaces losing boron via sublimation. Such boron outdiffusion produces a great number of vacancies and vacancy clusters, which create carbon-rich foam. The carbon foam has high diffusion permeability, which allows further boron transport from inside the grain to the surface as well as titanium influx. The process continues until B_4C precursor grains fully transform into the sponge-like graphite volumes with some tiny TiB_2 inclusions. Sponge sizes are approximately 1/3 of the precursor boron carbide particles.

Sublimated boron deposits on all the TiC grains and diffuses inside, leading initially to TiB_2 platelets precipitation. The platelets growth generates high level of tensile stresses resulting in TiC grain chipping. This creates porous structure of the reaction layer and allows sublimated boron depositing on fresh TiC surfaces.

Quick densification of the initial reaction area because of the external pressure prevents further reaction progress at approximately 6 μm of TiB_2 layer thickness. Carbon captured inside the solid diboride layer precipitates after 16 min sintering in the form of submicron graphite platelets in TiC-TiB_2 interfaces.

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