

STATE AND PARAMETER ESTIMATOR DESIGN FOR CONTROL OF VEHICLE SUSPENSION SYSTEM

FARGHAM SANDHU

UNIVERSITI TEKNOLOGI MALAYSIA

STATE AND PARAMETER ESTIMATOR DESIGN
FOR CONTROL OF VEHICLE SUSPENSION SYSTEM

FARGHAM SANDHU

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To my family, especially my wife for the nice cuppas of latte and espressos every now and then. Forget bout putting you steady. You may marry someone else. Just a waste of space.

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ABSTRACT

Modern vehicle stability and navigational systems are mostly designed using inaccurate bicycle models to approximate the full-car models. This results in incomplete models with various unknown parameters and states being neglected in the controller and navigation system design processes. Earlier estimation algorithms using the bicycle models are simpler but have many undefined parameters and states that are crucial for proper stability control. For existing vehicle navigation systems, direct line of sight for satellite access is required but is limited in modern cities with many high-rise buildings and therefore, an inertial navigation system utilizing accurate estimation of these parameters is needed. The aim of this research is to estimate the parameters and states of the vehicle more accurately using a multivariable and complex full-car model. This will enhance the stability of the vehicle and can provide a more consistent navigation. The proposed method uses the kinematics estimation model formulated using special orthogonal SO_3 group to design estimators for vehicles velocity, attitude and suspension states. These estimators are used to modify the existing antilock braking system (ABS) scheme by incorporating the dynamic velocity estimation to reduce the stopping distance. Meanwhile the semi-active suspension system includes suspension velocity and displacement states to reduce the suspension displacements and velocities. They are also used in the direct yaw control (DYC) scheme to include mass and attitude changes to reduce the lateral velocity and slips. Meanwhile in the navigation system, the 3-dimensional attitude effects can improve the position accuracy. With these approaches, the stopping distance in the ABS has been reduced by one meter and the vehicle states required for inertial navigation are more accurately estimated. The results for high speed lane change test indicate that the vehicle is 34% more stable and 16% better ride comfort on rough terrains due to the proposed DYC and the active suspension system control. The methods proposed can be utilized in future autonomous car design. This research is therefore an important contribution in shaping the future of vehicle driving, comfort and stability.

ABSTRAK

Sistem keseimbangan dan navigasi pengemudian kenderaan moden kebanyakannya direka dengan menggunakan model dua tayar yang tidak tepat untuk menggambarkan model-model kereta-penuh. Ini akan menghasilkan model yang tidak lengkap dengan pelbagai parameter dan keadaan yang tidak diketahui diabaikan di dalam proses merekabentuk pengawal dan sistem navigasi. Algoritma awal penganggaran menggunakan model dua tayar adalah lebih ringkas tetapi mempunyai banyak parameter dan keadaan yang penting yang tidak ditakrifkan untuk kawalan kestabilan yang sepatutnya. Untuk sistem navigasi kenderaan yang sedia ada, garis penglihatan langsung untuk capaian satelit diperlukan tetapi ia terhad di dalam bandar yang mempunyai banyak bangunan tinggi. Oleh itu, sistem pengemudian inersia yang memberikan anggaran lebih tepat bagi parameter-parameter tersebut adalah diperlukan. Matlamat penyelidikan ini adalah untuk menggambarkan parameter-parameter dan keadaan kenderaan tersebut secara lebih tepat dengan menggunakan model berbilang pemboleh ubah dan kereta-penuh. Ini akan menambahkan kestabilan kenderaan dan memberikan pengemudian yang lebih konsisten. Kaedah yang dicadangkan menggunakan model penganggaran kinematik yang dirumuskan menggunakan kumpulan SO_3 ortogonal khas untuk penganggaran halaju, sikap dan keadaan ampaian kenderaan. Penganggar ini digunakan untuk mengubah skema sistem brek antikunci (ABS) dengan menggabungkan penganggar dinamik halaju untuk mengurangkan jarak berhenti. Sementara itu, sistem ampaian separa aktif dengan menyertakan halaju dan sesaran digunakan bagi mengurangkan sesaran dan halaju ampaian. Ia juga digunakan dalam skema pengawalan rewang terus (DYC) dengan menyertakan perubahan jisim dan sikap untuk mengurangkan halaju dan gelincir sisi. Dalam sistem navigasi pula, kesan sikap ini boleh meningkatkan kejituan posisi. Dengan pendekatan ini, jarak berhenti dalam ABS telah dikurangkan sebanyak 1 meter dan keadaan kenderaan diperlukan untuk navigasi inersia dianggarkan dengan lebih tepat. Keputusan bagi perubahan lorong ketika halaju tinggi ialah 34% lebih seimbang dan 16% lebih selesa di atas permukaan kasar hasil dari DYC dan pengawalan sistem ampaian aktif yang dicadangkan. Kaedah yang dicadangkan boleh digunakan dalam merekabentuk kenderaan autonomi pada masa hadapan. Penyelidikan ini adalah sumbangan penting dalam membentuk masa depan pemanduan, penyelesaian, dan keutuhan kestabilan.

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LIST OF ABBREVIATIONS

<i>BM</i>	–	Bicycle Model
<i>CG</i>	–	Center of gravity
<i>diag</i>	–	Diagonal matrix, a matrix with all non parameters defined in the diagonal column only
<i>DMHE</i>	–	Direct Moving Horizon Estimator
<i>EKF</i>	–	Extended Kalman Filter
<i>EKBF</i>	–	Extended Kalman Bucy Filter
<i>EPF</i>	–	Extended Particle Filter
<i>FCM</i>	–	Full Car Model
<i>FL</i>	–	Fuzzy Logic
<i>GPS</i>	–	Global Positioning System
<i>GINS</i>	–	Global Inertial Navigational System
<i>GLONASS</i>	–	Global Navigation and Observatory System
<i>INS</i>	–	Inertial Navigation System
<i>IMU</i>	–	Inertial Measurement Unit
<i>KF</i>	–	Kalman Filter
<i>KM</i>	–	Kinematics Model
<i>KBF</i>	–	Kalman Bucy Filter
<i>LMS</i>	–	Least Mean Square
<i>MR</i>	–	Magnetorheological
<i>MH</i>	–	Moving Horizon Estimator
<i>MMS</i>	–	Multiple model and switching method
<i>NLO</i>	–	Nonlinear Observer
<i>PF</i>	–	Particle Filter

RLS	–	Recursive Least Square
$RLSF$	–	Recursive Least Square with Forgetting Factor
$RTLSF$	–	Recursive Time varying Least Square with Forgetting Factor
SDC	–	State Dependent Coefficient Form
$SDRE$	–	State Dependent Ricatti Equation
LQR	–	Linear Quadratic Recursion

LIST OF SYMBOLS

Vehicle Physical Parameters

A_p	–	Wind Drag Coefficient
e	–	Lateral Width of the vehicle [m]
f	–	Frequency of the source
h	–	Distance of C.G from roll axis [m]
h_{cg}	–	Height of center of gravity from level ground [m]
I	–	Moment of Inertia along x,y,z axis[Kgm ²][I_x, I_y, I_z].
l_a	–	Distance of C.G from front axle [m]
l_b	–	Distance of C.G from rear axle [m]
l	–	Wheel Base(a + b) [m]
M	–	Vehicle Mass [Kg]
M_1	–	Roll Compensated Vehicle Mass [Kg]
m	–	Lower suspension mass [Kg]
\mathbb{M}	–	Vector of masses [M, m_1, m_2, m_3, m_4]
r_{11}	–	Longitudinal distance from front left damper to wheel joint [m]
r_{12}	–	Lateral distance from front left damper to wheel joint [m]
r_{21}	–	Longitudinal distance from front right damper to wheel joint [m]
r_{22}	–	Lateral distance from front right damper to wheel joint [m]
r_{31}	–	Longitudinal distance from rear left damper to wheel joint [m]
r_{32}	–	Lateral distance from rear left damper to wheel joint [m]
r_{41}	–	Longitudinal distance from rear left damper to wheel joint [m]
r_{42}	–	Lateral distance from rear left damper to wheel joint [m]

R_e	–	Radius of the Earth [m]
R_c	–	Radius of Curvature during turning [m]
t_f	–	Distance between front tires [m]
t_r	–	Distance between rear tires [m]
θ_{bank}	–	Banking angle of road surface
μ	–	Nominal friction coefficient of the road surface

Sensor Parameters

A_{NL}	–	Accelerometer Nonlinearity
aab	–	Accelerometer beam coefficients[aa ₁ ,ab ₁]
a_{bcx}	–	x-axis accelerometer constant potential for running
a_{brx}	–	x-axis accelerometer random potential for running
ae_1	–	Accelerometer demodulator filter effects
ah_1	–	Output filter Coefficient 1/(6.28×50)
aFS	–	Accelerometer Range Selectable (2g/4g/8g/16g)
A_m	–	Accelerations measurement Vector[A_x , A_y , A_z]
A_{maxGPS}	–	operational Limits (Acceleration) [g]
A_R	–	Satellite Received Signal Amplitude
b_{ai}	–	Accelerometer bias[b _{ax} ,b _{ay} ,b _{az}]
b_{ari}	–	Random bias of accelerometer[b _{arx} ,b _{ary} ,b _{arz}]
b_{aci}	–	Constant Accelerometer bias[b _{acx} ,b _{acy} ,b _{acz}]
b_{gci}	–	Constant Gyro bias[b _{gcx} ,b _{gcy} ,b _{gcz}]
b_{gci}	–	Constant Gyro bias[b _{gcx} ,b _{gcy} ,b _{gcz}]
b_{grr_i}	–	Random x-axis run-to-run gyro bias[b _{grrx} , b _{grry} , b _{grrz}]
a_{gcbx}	–	x-axis gyro constant potential for running
a_{grbx}	–	x-axis gyro random potential for running
δt^i	–	Residual satellite clock error after performing the corrections
δ_g	–	Anomalous gravity
$\epsilon(\omega)$	–	gyro error noise
$\epsilon(a)$	–	Accelerometer error noise

$e_g(t)$	–	Error in Gyroscope
f_1	–	L1 Band frequency
f_2	–	L2 Band frequency
F_{slant}	–	VCO clock slant correction factor
g_{bin}	–	Biasing when the gyroscope is running
gT_{comp}	–	Gyro Temperature Compensation
G_s	–	gyro scale factor
gDV_{off}	–	Gyro Digital Zero Rate Level [dps]
g_{NL}	–	gyro Non-Linearity [% FS]
g_{ODR}	–	Gyro rate level change vs Temp [dps/C]
gR_n	–	Gyro rate Noise Density [dps / \sqrt{Hz}]
g_FS	–	Gyro Range [dps]
GPS_{AC}	–	GPS Accuracy
h_{maxGPS}	–	operational Limits (Altitude) [m]
I_r^i	–	Error due to dispersion atmospheric effects
I_r	–	Mobile signal recieved signal struength
k_{a1}	–	Accelerometer amplifier Gain [V/V]
m_{FS}	–	Magnetometer Range [Gauss]
m_{DFS}	–	magnetometer dynamic range [Gauss]
$M_{\rho i}^i$	–	Pseudo-range multiple path errors on the L_i pseudo-range measurements [$M_{\rho 1}^i, M_{\rho 2}^i$]
M_g	–	Magnetometer Sensitivity [LSB/Gauss]
M_N	–	Magnetomter Noise Floor [milli-Gauss]
M_{res}	–	Magnetometer Resolution in [milli-Gauss/bit]
Np	–	Pressure Sensor RMS Noise [m]
N	–	Non-Orthogonalities
\aleph	–	Sensor and Process random white gaussian noise [\aleph, ϕ]
ω_{gbias}	–	Process noise driving the gyroscope bias [rad/s] [$\omega_{xbias}, \omega_{ybias}, \omega_{zbias}$]
ω_{abias}	–	Process noise driving the accelerometer bias [m/s ²]

Ω	–	Gyro measurements Vector [$\Omega_x, \Omega_y, \Omega_z$][radians/s]
ψ_{GPS}	–	GPS Heading [radians]
θ_{GPS}	–	GPS Roll [radians]
ψ_m	–	Magnetometer yaw [radians]
ψ_{INS}	–	INS yaw [radians]
ψ_{MARG}	–	MARG yaw [radians]
KF	–	Magnetometer confidence factor
p_{GPS}	–	Position measured using GPS
V_{GPS}	–	Velocity measured using GPS [$V_{GPS}^{east}, V_{GPS}^{north}, V_{GPS}^{up}$]
P_{AC}	–	Pressure Sensor Absolute Accuracy Pressure [hPa]
p_{FS}	–	Pressure Sensor Resolution [hPa]
PT_{res}	–	Pressure Sensor Temp Resolution [$^{\circ}C$]
Q_{bias}	–	Sensor bias covariance
ρ	–	Pseudorange at position p(x)
σ_{gps}	–	Standard deviation of GPS noise [radians/Hz]
σ_{accel}	–	Standard deviation of accelerometer noise [radians/Hz]
σ_{gyro}	–	Standard deviation of gyro noise [radians/Hz]
σ_N	–	Random white Gaussian sensor noise density [W/\sqrt{Hz}]
σ_{Na}	–	Random white Gaussian Accelerometer noise density [W/\sqrt{Hz}]
σ_{Ng}	–	Random white Gaussian Gyroscope noise density [W/\sqrt{Hz}]
σ_R	–	Random white Gaussian Process noise density [W/\sqrt{Hz}]
S_{gps}	–	GPS sensitivity [dBm]
S_a	–	Accelerometer Sensitivity [LSB/g]
S_g	–	Gyro sensitivity [mdps/digit]
S_2	–	Accelerometer frequency sensitivity factor
S_{gODR}	–	Sensitivity deration per degrees [mg/deg]
T_r^i	–	Error due to non-dispersion atmospheric effects
τ_{bias}	–	Markov Time Constant
T_{gps}	–	Sampling Rate of GPS [s]

T_s	–	Sampling Rate of Inertial sensors [s]
T_R	–	Received signal period [s]
v_{gyro}	–	Gyro sensor noise
v_{accel}	–	Accelerometer sensor noise
v_{gps}	–	GPS sensor noise
$v_{\rho i}^i$	–	random measurement noise on the L_i pseudo-range measurements [$v_{\rho 1}^i, v_{\rho 2}^i$]
V_{maxGPS}	–	operational Limits (Velocity) [m/s]
$V_{\psi_{gps}}$	–	standard deviation of GPS heading noise [radians]
$V_{\theta_{gps}}$	–	standard deviation of GPS grade noise [radians]

Tire Parameters

α_i	–	Lateral tire slip angle [radians] [α_f, α_r]
κ	–	Tire slip ratio
C_α	–	Tire Coefficient along tire slip angle
C_σ	–	Tire Coefficient along tire density
C_i	–	Tire Coefficient along longitudinal and lateral axis [C_x, C_y]
C_α	–	Front and Rear Tire Cornering Stiffness [Nm] [$C_{\alpha f}, C_{\alpha r}$]
E	–	Tire Curvature Factor
γ	–	slip switching function
ϱ	–	Lateral Tire Slip Function
K_t	–	Tire Spring Constant [N/m]
λ	–	Slip in tire
M_z	–	Tire Braking Force [N]
S_i	–	Tire Horizontal and Vertical Shift [S_H, S_v]
T_b	–	Braking torque [N/m]
T_d	–	Traction Torque [N/m]
ς	–	Tire Peak Value
Υ	–	Tire Stiffness Factor
ϖ	–	Tire Shape Factor

Wheel Parameters

I_w	–	Wheel moment of inertia [Kgm/s ²]
J	–	Tire Horizontal Slip Function
ω_w	–	Wheel Angular velocity of wheel [rad/s]
R_w	–	Radius of Wheel [m]
V_w	–	Wheel Linear Velocity [m/s]

Vehicle Dynamic Parameters

α	–	Kinematic model based observer design parameter
A_c	–	Actual linear accelerations vector [a_x, a_y, a_z] [m/s ²]
\mathbb{A}	–	Attitude Vector [θ, ϕ, ψ][Radians]
β	–	Sideslip angle [radians]
δ	–	Steering angle [rad]
δ_c	–	Steering input from controller for assistance [rad]
δ_{max}	–	Maximum steering angle [rad]
F_x	–	Longitudinal Force Component [N]
F_y	–	Lateral Force Component [N]
F_z	–	Vertical Force Component [N]
F_ϕ	–	Force causing vehicle roll [N]
\tilde{h}	–	Odd submatrix of Rotation Matrix
\mathbb{J}	–	Cost Function
K_p	–	Proportional Gain
ω_c	–	Actual Angular velocity vector [$\omega_x, \omega_y, \omega_z$][Radians/s]
p	–	position of the vehicle[x,y,z][m]
θ	–	Roll angle [radians]
ϕ	–	Pitch Angle [radians]
ψ	–	Yaw angle [radians]
\mathbf{r}	–	Coefficient of rotation matrix
\mathbb{R}	–	Rotation Matrix using direction cosines
S	–	Sliding Surface

τ_{δ}	–	Steer system time constant [s]
τ_c	–	Actuator time constant [s]
τ_{CAN}	–	Steer system time constant [s]
τ_{I2C}	–	Steer system time constant [s]
V	–	Velocity of the vehicle [m/s][V_x, V_y, V_z]
\mathbb{W}	–	Lyapunov Energy Function

Suspension Physical Parameters

b_{ϕ}	–	Damping Coefficient of damper along roll axis [Ns/m][$b_{\phi f}, b_{\phi r}$]
B	–	Vector of Damping Coefficient of the MR Dampers [$b_{0_{FL}}, b_{0_{FR}}, b_{0_{RL}}, b_{0_{RR}}$][Ns/rad]
k_{ϕ}	–	Spring Constant along roll axis [N/m][$k_{\phi f}, k_{\phi r}$]
K	–	Vector of spring constants [k_1, k_2, k_3, k_4]
\mathfrak{R}_i	–	Damper Coefficients matrix[$\mathfrak{R}_1, \mathfrak{R}_2, \mathfrak{R}_3$]

MR Damper

$m\alpha_i$	–	Fixed and variable MR fluid factor
A_m	–	MR damper piston surface area [m^2]
β_m	–	MR fluid factor
bm_0	–	Fixed and variable Bingham damping coefficients [Ns/m][b_0a, b_0b]
bm_1	–	Fixed and variable Hysteresis damping coefficients [Ns/m][b_1a, b_1b]
η_m	–	Response time of the MR fluid
γ_m	–	MR fluid factor

System Matrices

A	–	State Matrix
A_N	–	Nominal State Matrix
B	–	Input State Matrix[B_1, B_2]

B_N	–	Nominal Input State Matrix
$B(x, t)$	–	Nonlinear input state dependent function
C	–	Output State Matrix
C_N	–	Nominal Output State Matrix
CCR	–	Submatrix of the state matrix
χ	–	Linear and nonlinear composite controller control effort $[\chi_N, \chi_L]$
D	–	Feedforward State Matrix
D_N	–	Nominal Feedforward State Matrix
$EngineType$	–	DOHC DVVT [K3VE]
$f(x, t)$	–	Nonlinear system state dependent function
F	–	Linear substate state matrix in composite control scheme
G	–	Linear substate input matrix in composite control scheme
Γ	–	Bias Augmented state matrix
I	–	Identity Matrix
K_∞	–	Measurement error gain Covariance Matrix
\mathfrak{K}	–	Estimator Gain matrix
KK	–	Submatrix of the state matrix
Ω_\times	–	Special orthogonal rate matrix
O	–	Zero Matrix
Ψ	–	Observability Matrix
Π	–	Bias Augmented input matrix
Φ	–	Bias Augmented feedforward matrix
P	–	Covariance Matrix
P_∞	–	Steady state kalman error Covariance Matrix
Q	–	Process Noise Covariance Matrix $[Q_i, Q_j]$
R	–	Sensor Noise Covariance Matrix
Θ	–	Bias Augmented output matrix
Ξ	–	Controllability Matrix
$u(t)$	–	Input vector $[u_1, u_2]$

\mathbb{U}	–	Second moment of distance submatrix
\mathbb{V}	–	First moment of distance submatrix
ξ	–	Subfunction in sliding mode controller
$x(t)$	–	State vector
$y(t)$	–	Output vector
y_m	–	System output measurements vector

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CHAPTER 1

INTRODUCTION

1.1 Background

Since the early 19th century, the cars has passed through a number of improvements (Bevly and Cobb, 2010; Leung *et al.*, 2011; Oh and Choi, 2013; Farrell, 2008). During the early days, clutch system and variable speed gear system was introduced to improve the vehicle handling (Lee *et al.*, 2014; davidL, 2000). Similarly flexible suspension system using spring mass damper system and air filled tires were introduced to improve the ride comfort and long term reliability (Lin and Kanellakopoulos, 1997). These innovations were introduced using bulky mechanical system and conceived on paper using expert knowledge; as there were no means of doing simulations (Stensson *et al.*, 1994; Fallah *et al.*, 2009). Earlier introduction of electromechanical systems in the form of motors for engine starting, encouraged the car engineers to replace the bulky mechanical assemblies with electromechanical systems to reduce weight and improve system performance (Bevly and Cobb, 2010; Farrell, 2008). Most of the earlier electromechanical systems used simple drive-by-wire technology for control. The improvements in digital control theory and microprocessors lead to the use of computer for driver assistance in collision avoiding system, like antilock braking system (ABS), and driver assisting systems, like assisted direct yaw control (DYC) (Jagtman and Wiersma, 2003; Abdulrahim, 2006; Aripin *et al.*, 2014; Suzuki and Takeda, 2016). When designing driver assisted control systems, the focus was mainly on improving the specific component of the car. For example, the automatic transmission system design process was focused on how to change the drive train by including electromechanical valves coupled with a large array of speed sensors and a digital controller for gear shift (Ackermann and Buente, 1997; Lee *et al.*, 2014). It did not include the engine block in the design process to optimize speed and torque. Similarly, the antilock braking system (Khachane and Shrivastav, 2016; Rizzi *et al.*, 2016; Boopathi and Abudhahir, 2016) included the speed obtained from the wheels speed sensors (Madau *et al.*, 1993; Mauer, 1995; Suraci *et al.*, 2006)

and did not include the linear accelerations (Bowman and Law, 1993) and angular velocities acting on the vehicle when developing the controller (Peric *et al.*, 2016; Antic *et al.*, 2016; Tang *et al.*, 2016).

The use of electromechanical systems for steering control and navigational system for autonomous driving, is another application which is being developed and refined (Inoue *et al.*, 2016; Zhao *et al.*, 2017). The use of electromechanical systems for direct steering, by using drive-by-wire technology has resulted in the reduction of weight, by reducing heavy mechanical linkages used in the ackermann shaft. It has also resulted in the improvement of the system response time, since direct control with lightening response and very low torque requirements are needed. High torque requirements for turning are common in bigger car, trucks and buses. Excessively high torque requirements had forced the car engineers to design power steering systems. With drive-by-wire technology, power steering systems become irrelevant. The drive-by-wire technology, reduces engine load required by power steering, reduces the weight and converts torque requirements into systems response inputs. The drive-by-wire technology also helps in placing digital controllers to assist the driver by changing the steering input habits of the driver for better control and reduce accident chances (Zhao *et al.*, 2017).

Recently, the drive-by-wire steering system, the automatic cruise control system and the braking system has been integrated with a reliable navigational system to provide the driver with a fully autonomous or partially autonomous system. The aim of this system has been in replacing or comforting the driver by employing various sensors and controllers. These systems have shown promising results under various test conditions. Since these systems have not gone through strenuous testing, they are considered less reliable and their accuracy is also limited. The reliability of these systems has created a sense of uncertainty in the car industry. The industry is also looking for systems which are simpler, since simpler systems are more reliable, have better accuracy and good component and system reliability. A good component reliability can result in higher component service life, which results in lesser maintenance (Dhahri *et al.*, 2012).

When considering the reliability of such systems, the reliability of each component is important. Hence each component is being tested and refined to improve its reliability. The amount of energy consumed is one important factors for judging the reliability of a component, subsystem or system. Some safety and comfort related systems have thus been graded as unreliable or uneconomical. One such system is the

active suspension system, which consumes a lot of power and its components have a very limited operational life. They are thus replaced by sub-optimal semi-active suspension systems, which are much more reliable and consume less energy (Chen *et al.*, 2015). Similarly, in semi-autonomous systems, the global positioning system, because of its direct line of sight requirements and limited 3D accuracy, is considered less reliable. There is a need to have navigational systems which can provide reliable accuracy (Wu *et al.*, 2016; Lin *et al.*, 2016; Sarbishei, 2016).

1.2 Problem Statement

The research work aims to address the following problems:

- i. Most of the current vehicle stability control systems incorporate essential and measurable parameters and states. Essential but non-measurable parameters are either estimated using complex estimation schemes, or are neglected (Sandu *et al.*, 2010; Crivellaro and Alves, 2006; Qazi *et al.*, 2014). The resultant control scheme is therefore, not robust enough or has high computational cost. Earlier control systems did not use expensive sensors or fast processing computers due to their higher cost (Cherouat *et al.*, 2005; Hac and Simpson, 2000). Current technologies has made the cost of sensors to reduce considerably and high end processors are also becoming cheaper. Therefore parameters and states which were neglected must be included to have more robustness and reliability (Chen *et al.*, 2015; Qazi *et al.*, 2014).
- ii. Current navigational systems use direct line of sight satellite communications, which are easily obstructed by underground bridges, sky scrapers and overhead bridges (Cohen *et al.*, 1994; Jwo *et al.*, 2012; Farina *et al.*, 2002). The system has to do a lot of computations to provide accurate 3D positional and velocity accuracy, which makes the system unsuitable for real time navigation (Wu *et al.*, 2016). The inertial navigation system can provide data in real time but does not have high accuracy. It does not require direct line of sight. A fusion of GPS with INS, as used in existing systems, cannot overcome the direct line of sight problem with GPS, without sacrificing the system accuracy. By fusing the inertial navigation system with other sensors to achieve redundancy and by using better algorithms, the INS accuracy can be improved without any direct line of sight problems (Sarbishei, 2016).

- iii. Newer and better control schemes must be provided to improve the stability and control of the vehicle to overcome general problems with existing control schemes.

1.3 Objectives

The objectives of this research are listed as follows:

- i. To estimate the important states and parameters of vehicles for better control of the vehicle.
- ii. To design a simple and robust controller that can improve the longitudinal, lateral and vertical stability of the vehicle.
- iii. To develop a navigational system that has no dependency on GPS.

1.4 Scope of Work

The scope of work in this research are

- i. The systems were tested using hatchback car model, since it has the ability to loose traction during turning. The real time systems were tested on test car since its structure is hatch back with good weight to torque settings for a utility car.
- ii. The important data for states and parameters were obtained using CarsimTM (a nonlinear vehicle simulator) and used for comparison in real time estimation, since those states and parameters were not possible to physically measure them.
- iii. The proposed controllers were only simulated with tests in CarsimTM.
- iv. The proposed navigational algorithm was tested on practical environment and the attitude states were compared with simulated results obtained from CarsimTM since they were not possible to measure in practical environment.

1.5 Dissertation Organization

The research is divided into several chapters. Following is the list of chapters with a brief detail of each chapters.

- i. Chapter 1: This chapter gives a brief introduction of the work. It consists of the problem statement, the objectives of this research, the scope of the work and important contributions of this work.
- ii. Chapter 2: This chapter describes the theory of existing systems. This chapter clearly defines the important parameters, models and states used to build the foundation of this research.
- iii. Chapter 3: This chapter briefly describes the literature review of existing systems. It revisits certain models to introduce important missing parameters. It also revisits the existing observers and controllers to suggest improvements and new control and estimation algorithms.
- iv. Chapter 4: The proposed changes are discussed with elaborate mathematical justification in this chapter. The method used for testing the proposed changes and its implementation are also discussed. The chapter thus includes the methodology of the proposed works. The proposed changes and the method used to test the changes and evaluate them in comparison to the existing methods is also done in this chapter.
- v. Chapter 5: The chapter presents all the test results and provides a comprehensive analysis of each test result, that are compared with existing results. The chapter thus provides the results and analysis of the research.
- vi. Chapter 6: This chapter concludes the work done in this research. It gives all the conclusions drawn from the research. Based on the conclusions, it also suggests recommendations for further research.

REFERENCES

- Abbott, E. and Powell, D. (1999). Land vehicle navigation using GPS. *Proceedings of the IEEE*. 87(1), 145–162.
- Abdeen, M. H. U., Khan, U. S. and Iqbal, J. (2016). A Multipurpose Vehicle Tracking System Based on ARM CORTEX-M3 STM32, HMC5883L, MPU-6050, GSM and GPS. *Journal of Traffic and Logistics Engineering*. 4(1).
- Abdulrahim, M. (2006). *On the dynamics of automobile drifting*. Technical report. SAE Technical Paper.
- Ackermann, J. and Buente, T. (1997). Yaw disturbance attenuation by robust decoupling of car steering. In *Control Engineering Practice*, vol. 5. January. 1131–1136.
- Aggarwal, P., Syed, Z. and El Sheimy, N. (2014). *MEMS based integrated navigation*. Artech House.
- Ahmadian, M., Song, X. and Southward, S. C. (2004). No-jerk skyhook control methods for semiactive suspensions. *Transactions of the ASME-L Journal of Vibration and Acoustics*. 126(4), 580.
- Analog-Device (2014). *Precision $\pm 1.7g, \pm 5g, \pm 18g$ Single Axis iMEMS Accelerometer ADXL103[2014]*. Available from: http://www.analog.com/media/en/technical_documentation/datasheets/ADXL103_203.pdf. Analog Devices.
- Antic, D. S., Mitic, D. B., Jovanovic, Z. D., Peric, S. L., Milojkovic, M. T. and Nikolic, S. S. (2016). Sliding Mode Based Anti-Lock Braking System Control. In *Complex Systems*. (pp. 557–580). Springer.
- Aripin, M., Md Sam, Y., Danapalasingam, K. A., Peng, K., Hamzah, N. and Ismail, M. (2014). A review of active yaw control system for vehicle handling and stability enhancement. *International journal of vehicular technology*. 14.
- Bae, H. S., Ryu, J. and Gerdes, J. C. (2001). Road grade and vehicle parameter estimation for longitudinal control using GPS. In *Proceedings of the IEEE Conference on Intelligent Transportation Systems*. 25–29.

- Bar Itzhack, I. Y. and Berman, N. (1988). Control theoretic approach to inertial navigation systems. *Journal of Guidance, Control, and Dynamics*. 11(3), 237–245.
- Benev, B., Stoev, A. and Stoeva, P. (2013). Portable 3D magnetometer for local geomagnetic field disturbance measurements. *SES 2012*, 345–347.
- Berman, Z. and Powell, J. D. (1998). The role of dead reckoning and inertial sensors in future general aviation navigation. In *Position Location and Navigation Symposium, IEEE*. IEEE, 510–517.
- Bevly, D. M. (2004). Global positioning system (GPS): A low cost velocity sensor for correcting inertial sensor errors on ground vehicles. *Journal of dynamic systems, measurement, and control*. 126(2), 255–264.
- Bevly, D. M. and Cobb, S. (2010). *GNSS for Vehicle Control*. Artech House.
- Bevly, D. M., Gerdes, J. C., Wilson, C. and Zhang, G. (2000). The use of GPS based velocity measurements for improved vehicle state estimation. In *Proceedings of the American Control Conference*, vol. 4. IEEE, 2538–2542.
- Bevly, D. M., Sheridan, R. and Gerdes, J. C. (2001). Integrating INS sensors with GPS velocity measurements for continuous estimation of vehicle sideslip and tire cornering stiffness. In *Proceedings of the American Control Conference*, vol. 1. IEEE, 25–30.
- Biglarbegian, M., Melek, W. and Golnaraghi, F. (2008). A novel neuro-fuzzy controller to enhance the performance of vehicle semi-active suspension systems. *Vehicle System Dynamics*. 46(8), 691–711.
- Boada, B., Boada, M. and Diaz, V. (2005). Fuzzy-logic applied to yaw moment control for vehicle stability. *Vehicle System Dynamics*. 43(10), 753–770.
- Boopathi, A. M. and Abudhahir, A. (2016). Design of grey-verhulst sliding mode controller for antilock braking system. *International Journal of Control, Automation and Systems*. 14(3), 763–772.
- Bowman, J. E. and Law, E. (1993). *A feasibility study of an automotive slip control braking system*. Technical report. SAE technical paper.
- Brown, R. G. (1983). *Introduction to random signal analysis and Kalman filtering*. John Wiley & Sons.
- Canale, M., Fagiano, L. and Novara, C. (2010). Vehicle side-slip angle estimation using a direct MH estimator. In *IEEE International Conference on Control Applications*. 167–172.
- Car-contacts (2013). *Spring-Damper Strut*. Available at: <http://www.carcontacts.com/imagesystem/macphersonstrut.jpg>.

- Car-Engineer (2013). *Pseudo-Mac-Pherson*, Available at: <http://www.car-engineer.com/wp-content/uploads/2013/02/Pseudo-Mac-Pherson.jpg?x53636>.
- Caruso, M. (2003). Compass heading using magnetometers. *Honeywell Application Note AN*. 203.
- Chandrasekaran, G., Vu, T., Varshavsky, A., Gruteser, M., Martin, R. P., Yang, J. and Chen, Y. (2010). Vehicular speed estimation using received signal strength from mobile phones. In *Proceedings of the 12th ACM international conference on Ubiquitous computing*. ACM, 237–240.
- Chen, B. M., Lee, T. H., Peng, K. and Venkataramanan, V. (2006). *Hard disk drive servo systems*. Springer Science & Business Media.
- Chen, K. and Beale, D. G. (2003). Base dynamic parameter estimation of a MacPherson suspension mechanism. *Vehicle System Dynamics*. 39(3), 227–244.
- Chen, M. Z., Hu, Y., Li, C. and Chen, G. (2015). Performance benefits of using inerter in semiactive suspensions. *IEEE Transactions on Control Systems Technology*. 23(4), 1571–1577.
- Cherouat, H., Braci, M. and Diop, S. (2005). Vehicle velocity, side slip angles and yaw rate estimation. In *Proceedings of the IEEE International Symposium on Industrial Electronics ISIE*, vol. 1. IEEE, 349–354.
- Chiang, H.-H., Chen, Y.-L. and Hsu, K.-C. (2015). Optimized sensorless antivibration control for semiactive suspensions with cosimulation analysis. *IEEE/ASME Transactions on Mechatronics*. 20(4), 1898–1911.
- Chiang, H.-H. and Lee, L.-W. (2015). Optimized virtual model reference control for ride and handling performance-oriented semiactive suspension systems. *IEEE Transactions on Vehicular Technology*. 64(5), 1679–1690.
- Cho, K., Son, H., Choi, S. B. and Kang, S. (2010a). Lateral acceleration compensation of a vehicle based on roll angle estimation. In *IEEE International Conference on Control Applications (CCA)*. IEEE, 1363–1368.
- Cho, K., Son, H., Choi, S. B. and Kang, S. (2010b). Lateral acceleration compensation of a vehicle based on roll angle estimation. In *IEEE International Conference on Control Applications (CCA)*. IEEE, 1363–1368.
- Choi, S., Choi, Y. T. and Park, D. (2000). A sliding mode control of a full-car electrorheological suspension system via hardware in-the-loop simulation. *Transactions-American society of mechanical engineers journal of dynamic systems measurement and control*. 122(1), 114–121.
- Cohen, C. E., Parkinson, B. W. and McNally, B. D. (1994). Flight tests of attitude

- determination using GPS compared against an inertial navigation unit. *Navigation*. 41(1), 83–97.
- Corporation, B. (2016). *Bosch Showcase Steering System*. Available at: <https://tiresandparts.net/wp-content/uploads/Electric-Power-Steering-System-Service-Feature.jpg>.
- Crassidis, J. L. and Junkins, J. L. (2011). *Optimal estimation of dynamic systems*. CRC press.
- Crivellaro, C. and Alves, S. J. (2006). *Phenomenological model of a magneto-rheological damper for semi-active suspension control design and simulation*. Technical report. SAE Technical Paper.
- Csekho, L. H., Kvasnica, M. and Lantos, B. (2015). Explicit MPC-based RBF neural network controller design with discrete-time actual Kalman filter for semiactive suspension. *IEEE Transactions on Control Systems Technology*. 23(5), 1736–1753.
- Daiss, A. and Kiencke, U. (1995). Estimation of vehicle speed fuzzy-estimation in comparison with Kalman-filtering. In *Proceedings of the 4th IEEE Conference on Control Applications*. IEEE, 281–284.
- DAmato, F. J. and Viassolo, D. E. (2000). Fuzzy control for active suspensions. *Mechatronics*. 10(8), 897–920.
- davidL (2000). *Automatic Transmission System*, Available at: https://en.wikipedia.org/wiki/Automatic_transmission.
- Deng, W. and Zhang, H. (2006). RLS Based online estimation on vehicle linear sideslip. In *American Control Conference*. IEEE, 6–pp.
- Dhahri, S., Sellami, A. and Ben Hmida, F. (2012). Robust sensor fault detection and isolation for a Steer-by-Wire system based on sliding mode observer. In *16th IEEE Mediterranean Electrotechnical Conference (MELECON)*. IEEE, 450–454.
- Dugoff, H., Fancher, P. S. and Segel, L. (1969). *Tire performance characteristics affecting vehicle response to steering and braking control inputs*. Technical report.
- Elhefnawy, A., Sharaf, A., Ragheb, H. and Hegazy, S. (2016). Active Vehicle Safety using Integrated Control of Body Roll and Direct Yaw Moment. In *Proceedings of the 17th Int AMME Conference*, vol. 19. 17.
- Esmailzadeh, E., Goodarzi, A. and Vossoughi, G. (2003). Optimal yaw moment control law for improved vehicle handling. *Mechatronics*. 13(7), 659–675.
- Fallah, M., Bhat, R. and Xie, W. (2009). New model and simulation of Macpherson suspension system for ride control applications. *Vehicle System Dynamics*. 47(2), 195–220.

- Farina, A., Ristic, B. and Benvenuti, D. (2002). Tracking a ballistic target: comparison of several nonlinear filters. *IEEE Transactions on Aerospace and Electronic Systems*. 38(3), 854–867.
- Farrell, J. (2008). *Aided navigation: GPS with high rate sensors*. McGraw Hill, Inc.
- Farrell, J. (2012). *Integrated aircraft navigation*. Elsevier.
- Farrelly, J. and Wellstead, P. (1996). Estimation of vehicle lateral velocity. In *Proceedings of the IEEE International Conference on Control Applications*. IEEE, 552–557.
- Felix Herran, L., Mehdi, D., Rodriguez-Ortiz, J., Ramirez-Mendoza, R. and Soto, R. (2015). Takagi sugeno fuzzy model of a one-half semiactive vehicle suspension: lateral approach. *Mathematical Problems in Engineering*. 2015.
- Fiala, E. (1954). Lateral forces on rolling pneumatic tires. *Zeitschrift VDI*. 96(29), 973–979.
- Fu, C. and Hu, M. (2015). Adaptive sliding mode-based direct yaw moment control for electric vehicles. In *International Conference on Control, Automation and Information Sciences (ICCAIS)*. IEEE, 470–474.
- Grip, H. F., Imsland, L., Johansen, T., Kalkkuhl, J. C., Suissa, A. *et al.* (2009). Vehicle sideslip estimation. *Control Systems, IEEE*. 29(5), 36–52.
- Grubin, C. (1970). Derivation of the quaternion scheme via the Euler axis and angle. *Journal of Spacecraft and Rockets*. 7(10), 1261–1263.
- Gustafsson, F., Gunnarsson, F., Bergman, N., Forssell, U., Jansson, J., Karlsson, R. and Nordlund, P.-J. (2002). Particle filters for positioning, navigation, and tracking. *IEEE Transactions on Signal Processing*. 50(2), 425–437.
- Hac, A. and Simpson, M. D. (2000). *Estimation of vehicle side slip angle and yaw rate*. Technical report. SAE Technical Paper.
- Hahn, J. O., Rajamani, R. and Alexander, L. (2002). GPS based realtime identification of tire-road friction coefficient. *IEEE Transactions on Control Systems Technology*. 10(3), 331–343.
- Hedrick, J. K. (2002). Modified skyhook control of semi-active suspensions: A new model, gain scheduling, and hardware-in-the-loop tuning. *Journal of Dynamic Systems, Measurement, and Control*. 124, 158–167.
- Hingwe, P. and Tomizuka, M. (1997). Experimental evaluation of a chatter free sliding mode control for lateral control in AHS. In *Proceedings of the American Control Conference*, vol. 5. IEEE, 3365–3369.

- Hu, C., Wang, R. and Yan, F. (2016). Integral Sliding Mode-Based Composite Non-linear Feedback Control for Path Following of Four-Wheel Independently Actuated Autonomous Vehicles. *IEEE Transactions on Transportation Electrification*. 2(2), 221–230.
- Imsland, L., Grip, H. F., Johansen, T. A., Fossen, T. I., Kalkkuhl, J. C. and Suissa, A. (2007). *Nonlinear observer for vehicle velocity with friction and road bank angle adaptation validation and comparison with an extended Kalman filter*. Technical report. SAE Technical Paper.
- Imsland, L., Johansen, T. A., Fossen, T. I., Grip, H. F., Kalkkuhl, J. C. and Suissa, A. (2006). Vehicle velocity estimation using nonlinear observers. *Automatica*. 42(12), 2091–2103.
- Inoue, S., Ozawa, T., Inoue, H., Raksincharoensak, P. and Nagai, M. (2016). Cooperative lateral control between driver and ADAS by haptic shared control using steering torque assistance combined with Direct Yaw Moment Control. In *IEEE 19th International Conference on Intelligent Transportation Systems (ITSC)*. IEEE, 316–321.
- Invetr (2008). *Twisted Beam Rear Suspension*, Available at: http://www.invetr.com/uploads/2/1/8/2/21829402/4665544_orig.jpg.
- Jagtman, H. and Wiersma, E. (2003). Driving with adaptive cruise control in the real world. In *Proceedings of the 16th ICTCT workshop on Improving safety by linking research with safety policy and management*. 1–8.
- Jahromi, A. F. and Zabihollah, A. (2010). Linear quadratic regulator and fuzzy controller application in full-car model of suspension system with magnetorheological shock absorber. In *2010 IEEE/ASME International Conference on Mechatronics and Embedded Systems and Applications (MESA)*. IEEE, 522–528.
- Jiang, F. and Gao, Z. (2000). An adaptive nonlinear filter approach to the vehicle velocity estimation for ABS. In *Proceedings of the IEEE International Conference on Control Applications*. IEEE, 490–495.
- Jwo, D. J., Yang, C.-F., Chuang, C. H. and Lin, K.-C. (2012). A novel design for the ultra tightly coupled GPS/INS navigation system. *Journal of Navigation*. 65(04), 717–747.
- K Yi, B. S. and J.H.Park (1999). Observer based Control of Vehicle suspensions. *Proceeding of the Institute of Mechanical Enineering part.D*. 213(6), 531–543.
- Kachroo, P. and Tomizuka, M. (1994). Vehicle traction control and its applications. *California Partners for Advanced Transit and Highways (PATH)*.

- Karjalainen, M. (2016). *Real-Time Estimation of Tire Stiffness*.
- Khachane, D. and Shrivastav, A. (2016). Antilock Braking System and Its Advancement. *International research journal of engineering and technology (IRJET)*.
- Kim, D., Peng, H., Bai, S. and Maguire, J. M. (2007). Control of integrated powertrain with electronic throttle and automatic transmission. *IEEE Transactions on Control Systems Technology*. 15(3), 474–482.
- Kim, H. S., Bu, S. C., Jee, G. I. and Park, C. G. (2003). An ultra tightly coupled GPS/INS integration using federated Kalman filter. *ION*.
- Kobayashi, K., Cheok, K. C. and Watanabe, K. (1995). Estimation of absolute vehicle speed using fuzzy logic rule based Kalman filter. In *Proceedings of the American Control Conference*, vol. 5. IEEE, 3086–3090.
- Kuo, W., Wang, Y., Shiao, Y., Guo, J., Chiang, M. and Din, Y. (2007). Semi-active control of vehicle suspension system using electrorheological dampers. In *3rd Institution of Engineering and Technology Conference on Automotive Electronics*. IET, 1–9.
- Kwok, C., Fox, D. and Meila, M. (2004). Real-time particle filters. *Proceedings of the IEEE*. 92(3), 469–484.
- Lai, C. Y. and Liao, W.-H. (2002). Vibration control of a suspension system via a magnetorheological fluid damper. *Journal of Vibration and Control*. 8(4), 527–547.
- Lee, S., Zhang, Y., Jung, D. and Lee, B. (2014). A Systematic Approach for Dynamic Analysis of Vehicles With Eight or More Speed Automatic Transmission. *Journal of Dynamic Systems, Measurement, and Control*. 136(5), 051008.
- Leung, K. T., Whidborne, J. F., Purdy, D. and Barber, P. (2011). Road vehicle state estimation using low-cost GPS/INS. *Mechanical Systems and Signal Processing*. 25(6), 1988–2004.
- Lin, C.-C., Jhong, K.-J., Kuo, Y.-C. and Zeng, Y.-X. (2016). A Plane Angle Measurement System Using MARG Sensors. In *2016 International Symposium on Computer, Consumer and Control (IS3C)*. IEEE, 732–735.
- Lin, J.-S. and Kanellakopoulos, I. (1997). Nonlinear design of active suspensions. *Control Systems, IEEE*. 17(3), 45–59.
- Liu, C.-S. and Peng, H. (1998). A state and parameter identification scheme for linearly parameterized systems. *Journal of dynamic systems, measurement, and control*. 120(4), 524–528.
- Liu, H., Yang, J., Yang, H. and Yi, F. (2016). Soft Sensor of Vehicle State Estimation

- Based on the Kernel Principal Component and Improved Neural Network. *Journal of Sensors*. 2016.
- Ma, X. Q., Wang, E. R., Rakheja, S. and Su, C.-Y. (2002). Modeling hysteretic characteristics of MR-fluid damper and model validation. In *Proceedings of the 41st IEEE Conference on Decision and Control*, vol. 2. IEEE, 1675–1680.
- Madau, D., Yuan, F., Davis, L. and Feldkamp, L. (1993). Fuzzy logic anti-lock brake system for a limited range coefficient of friction surface. In *Second IEEE International Conference on Fuzzy Systems, 1993*. IEEE, 883–888.
- Mahony, R., Hamel, T. and Pflimlin, J.-M. (2008). Nonlinear complementary filters on the special orthogonal group. *IEEE Transactions on Automatic Control*. 53(5), 1203–1218.
- Manning, W. and Crolla, D. (2007). A review of yaw rate and sideslip controllers for passenger vehicles. *Transactions of the Institute of Measurement and Control*. 29(2), 117–135.
- Massey, J. P. (2006). *Control and waypoint navigation of an autonomous ground vehicle*. Ph.D. Thesis. Texas A&M University.
- Mauer, G. F. (1995). A fuzzy logic controller for an ABS braking system. *IEEE Transactions on Fuzzy Systems*. 3(4), 381–388.
- Milecki, A. and Hauke, M. (2012). Application of magnetorheological fluid in industrial shock absorbers. *Mechanical Systems and Signal Processing*. 28, 528–541.
- Mortensen, R. (1974). Strapdown guidance error analysis. *IEEE Transactions on Aerospace and Electronic Systems*. 4, 451–457.
- Mousavinejad, E., Han, Q.-L., Yang, F., Zhu, Y. and Vlacic, L. (2017). Integrated control of ground vehicles dynamics via advanced terminal sliding mode control. *Vehicle System Dynamics*. 55(2), 268–294.
- Mracek, C. P. and Cloutier, J. R. (1998). Control designs for the nonlinear benchmark problem via the state-dependent Riccati equation method. *International Journal of robust and nonlinear control*. 8(4-5), 401–433.
- Nasr, E., Kfoury, E. and Khoury, D. (2016). An IoT approach to vehicle accident detection, reporting, and navigation. In *Multidisciplinary Conference on Engineering Technology (IMCET), IEEE International*. IEEE, 231–236.
- Nugroho, P. W., Li, W., Du, H., Alici, G. and Yang, J. (2014). An adaptive neuro fuzzy hybrid control strategy for a semiactive suspension with magneto rheological damper. *Advances in Mechanical Engineering*.

- Oh, J. and Choi, S. B. (2013). Vehicle roll and pitch angle estimation using a cost-effective six-dimensional inertial measurement unit. *Proceedings of the Institution of Mechanical Engineers, Part D: Journal of Automobile Engineering*. 227(4), 577–590.
- Oh, J. J. and Choi, S. B. (2012). Vehicle velocity observer design using 6-d imu and multiple-observer approach. *IEEE Transactions on Intelligent Transportation Systems*. 13(4), 1865–1879.
- Ozyagcilar, T. (2012). Calibrating an ecompass in the presence of hard and soft-iron interference. *Freescale Semiconductor Ltd*.
- Pacejka, H. and Besselink, I. (1997). Magic formula tyre model with transient properties. *Vehicle system dynamics*. 27(S1), 234–249.
- Pacejka, H. B. and Bakker, E. (1992). The magic formula tyre model. *Vehicle system dynamics*. 21(S1), 1–18.
- Peric, S. L., Antic, D. S., Milovanovic, M. B., Mitic, D. B., Milojkovic, M. T. and Nikolic, S. S. (2016). Quasi-sliding mode control with orthogonal endocrine neural network-based estimator applied in anti-lock braking system. *IEEE/ASME Transactions on Mechatronics*. 21(2), 754–764.
- Qazi, A. J., de Silva, C. W., Khan, A. and Khan, M. T. (2014). Performance analysis of a semiactive suspension system with particle swarm optimization and fuzzy logic control. *The Scientific World Journal*. 2014.
- Qin, Y., Dong, M., Langari, R., Gu, L. and Guan, J. (2015). Adaptive hybrid control of vehicle semiactive suspension based on road profile estimation. *Shock and Vibration*. 15.
- Racing, U. (2015). *chassis friendly*, Available at: <http://ultraracing/v1/wp-content/uploads/2015/02/chassis-1024x640.jpg>.
- Ray, L. R. (1997). Nonlinear tire force estimation and road friction identification: simulation and experiments. *Automatica*. 33(10), 1819–1833.
- Rizzi, M., Kullgren, A. and Tingvall, C. (2016). The combined benefits of motorcycle antilock braking systems (ABS) in preventing crashes and reducing crash severity. *Traffic injury prevention*. 17(3), 297–303.
- Saikia, A. and Mahanta, C. (2016). Active Front Steering Using PID based Sliding Mode Control. *History*. 2(7), 378–384.
- Sammier, D., Sename, O. and Dugard, L. (2003). Skyhook and H8 control of semi-active suspensions: some practical aspects. *Vehicle System Dynamics*. 39(4), 279–308.

- Samuel John, J. O. (2013). Active feedback linearization for hybrid slip control for antilock braking systems. In *Acta politechnica Hungarica*, vol. 10. December. 81–99.
- Sandu, C., Southward, S. and Richards, R. (2010). Comparison of linear, nonlinear, hysteretic, and probabilistic models for magnetorheological fluid dampers. *Journal of Dynamic Systems, Measurement, and Control*. 132(6), 061403.
- Sarbishei, O. (2016). On the accuracy improvement of low-power orientation filters using IMU and MARG sensor arrays. In *IEEE International Symposium on Circuits and Systems (ISCAS)*. IEEE, 1542–1545.
- Savaresi, S. M. and Spelta, C. (2009). A single-sensor control strategy for semi-active suspensions. *IEEE Transactions on control systems Technology*. 17(1), 143–152.
- Schwab, A. L. (2002). Quaternions, finite rotation and euler parameters. *Cornell University Notes, Ithaca NY*.
- Setiawan, J. D., Safarudin, M. and Singh, A. (2009). Modeling, simulation and validation of 14 DOF full vehicle model. In *International Conference on Instrumentation, Communications, Information Technology, and Biomedical Engineering (ICICI-BME)*. IEEE, 1–6.
- Shadow, R. R. S. (2013). *Legenda of the diagram*. Available at: <http://www.rrsilvershadow.com/Techn/Hydr/BestH>.
- Sharaf, R. and Nouredin, A. (2007). Sensor integration for satellite-based vehicular navigation using neural networks. *IEEE Transactions on Neural Networks*. 18(2), 589–594.
- Skoglar, P., Orguner, U., Tornqvist, D. and Gustafsson, F. (2009). Road target tracking with an approximative Rao-Blackwellized Particle filter. In *12th International Conference on Information Fusion, 2009. FUSION'09*. IEEE, 17–24.
- Solmaz, S., Akar, M. and Shorten, R. (2006). Online center of gravity estimation in automotive vehicles using multiple models and switching. In *9th International Conference on Control, Automation, Robotics and Vision ICARCV'06*. IEEE, 1–7.
- Song, Y. and Yuan, X. (2016). Low-Cost Adaptive Fault-Tolerant Approach for Semiactive Suspension Control of High-Speed Trains. *IEEE Transactions on Industrial Electronics*. 63(11), 7084–7093.
- Spencer Jr, B., Dyke, S., Sain, M. and Carlson, J. (1997). Phenomenological model for magnetorheological dampers. *Journal of engineering mechanics*.
- Sportrider (2012). *Honda Braking System*, Available at: http://www.sportrider.com/sites/Braking_pressure.jpg.

- ST-Microelectronics (2010). *MEMS Motion Sensor three axis digital output gyroscope* [2015]. Available at: <http://www.st.com/web/en/resource/technical/document/datasheet/CD00265057.pdf>. ST-Microelectronics.
- Stensson, A., Asplund, C. and Karlsson, L. (1994). The nonlinear behaviour of a Macpherson strut wheel suspension. *Vehicle system dynamics*. 23(1), 85–106.
- Suraci, E., Abagnale, P., Amoroso, D. and Mariniello, F. (2006). Development and road tests of an ABS control system. *Vehicle System Dynamics*. 44(sup1), 393–401.
- Suzuki, Y. and Takeda, M. (2016). An overview on vehicle lateral dynamics and yaw stability control systems. *Journal of Advances in Vehicle Engineering*. 2(4).
- Tang, Y., Wang, Y., Han, M. and Lian, Q. (2016). Adaptive fuzzy fractional-order sliding mode controller design for antilock braking systems. *Journal of Dynamic Systems, Measurement, and Control*. 138(4), 041008.
- Tao, P. R., Wereley, P. N. M., Sahin, H., Gordaninejad, F., Wang, X. and Liu, Y. (2012). Response time of magnetorheological fluids and magnetorheological valves under various flow conditions. *Journal of Intelligent Material Systems and Structures*. 23(9), 949–957.
- Tchamna, R. and Youn, I. (2013). Yaw rate and side slip control considering vehicle longitudinal dynamics. *International Journal of Automotive Technology*. 14(1), 53–60.
- Titterton, D. and Weston, J. L. (2004). *Strapdown inertial navigation technology*. vol. 17. IET.
- Toledo Moreo, R., Bétaille, D. and Peyret, F. (2010). Lane-level integrity provision for navigation and map matching with GNSS, dead reckoning, and enhanced maps. *IEEE Transactions on Intelligent Transportation Systems*. 11(1), 100–112.
- Toledo Moreo, R., Zamora-Izquierdo, M., Ubeda Minarro, B., Gomez-Skarmeta, A. F. et al. (2007). High-integrity IMM-EKF-based road vehicle navigation with low-cost GPS/SBAS/INS. *IEEE Transactions on Intelligent Transportation Systems*. 8(3), 491–511.
- Vahidi, A., Druzhinina, M., Stefanopoulou, A. and Peng, H. (2003). Simultaneous mass and time-varying grade estimation for heavy-duty vehicles. In *Proceedings of the American Control Conference*, vol. 6. IEEE, 4951–4956.
- Valenti, R. G., Dryanovski, I. and Xiao, J. (2016). A linear Kalman filter for MARG orientation estimation using the algebraic quaternion algorithm. *IEEE Transactions on Instrumentation and Measurement*. 65(2), 467–481.

- VanBronkhorst, A. (1978). Strapdown system algorithms. *AGARD Strap-Down Inertial Systems 22 p(SEE N 78-26124 17-04)*.
- Wenzel, T. A., Burnham, K., Blundell, M. and Williams, R. (2006). Dual extended Kalman filter for vehicle state and parameter estimation. *Vehicle System Dynamics*. 44(2), 153–171.
- Wiak, S., Smolka, K. and Rudnicki, M. (2005). Modelling and Optimisation of Intelligent Electrostatic Comb Accelerometer. In *Computer Engineering in Applied Electromagnetism*. (pp. 99–104). Springer.
- Won, D. H., Chun, S., Sung, S., Lee, Y. J., Cho, J., Joo, J. and Park, J. (2010). INS/vSLAM system using distributed particle filter. *International Journal of Control, Automation and Systems*. 8(6), 1232–1240.
- Wu, J., Zhou, Z., Chen, J., Fourati, H. and Li, R. (2016). Fast Complementary Filter for Attitude Estimation Using Low-Cost MARG Sensors. *IEEE Sensors Journal*. 16(18), 6997–7007.
- Yao, G., Yap, F., Chen, G., Li, W. and Yeo, S. (2002). MR damper and its application for semi-active control of vehicle suspension system. *Mechatronics*. 12(7), 963–973.
- Yi, K. and Song, B. (1999). A new adaptive sky-hook control of vehicle semi-active suspensions. *Proceedings of the Institution of Mechanical Engineers, part D: Journal of automobile engineering*. 213(3), 293–303.
- Yi, K. and Suk Song, B. (1999). Observer design for semiactive suspension control. *Vehicle System Dynamics*. 32(2-3), 129–148.
- Yu, J. (1997). A robust adaptive wheel-slip controller for antilock brake system. In *Proceedings of the 36th IEEE Conference on Decision and Control*, vol. 3. IEEE, 2545–2546.
- Zareh, S. H., Abbasi, M., Mahdavi, H. and Osgouie, K. G. (2012). Semi-active vibration control of an eleven degrees of freedom suspension system using neuro inverse model of magnetorheological dampers. *Journal of mechanical science and technology*. 26(8), 2459–2467.
- Zareh, S. H., Sarrafan, A., Jahromi, A. F. and Khayyat, A. A. (2011). Linear quadratic Gaussian application and clipped optimal algorithm using for semi active vibration of passenger car. In *IEEE International Conference on Mechatronics (ICM)*. IEEE, 122–127.
- Zhang, H. and Wang, J. (2016). Vehicle lateral dynamics control through AFS/DYC and robust gain-scheduling approach. *IEEE Transactions on Vehicular Technology*. 65(1), 489–494.

- Zhao, J., Wong, P. K., Ma, X. and Xie, Z. (2017). Chassis integrated control for active suspension, active front steering and direct yaw moment systems using hierarchical strategy. *Vehicle System Dynamics*. 55(1), 72–103.
- Zheng, S., Tang, H., Han, Z. and Zhang, Y. (2006). Controller design for vehicle stability enhancement. *Control Engineering Practice*. 14(12), 1413–1421.