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Effects of Suction-Injection-Combination (SIC) on the onset of Rayleigh-Bénard Electroconvection in a Micropolar Fluid

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Abstract

The effect of Suction - injection combination on the onset of Rayleigh - Bénard electroconvection micropolar fluid is investigated by making a linear stability analysis. The Rayleigh-Ritz technique is used to obtain the eigenvalues for different velocity and temperature boundary combinations. The influence of various parameters on the onset of convection has been analysed. It is found that the effect of Prandtl number on the stability of the system is dependent on the SIC being pro-gravity or anti-gravity. A similar Pe-sensitivity is found in respect of the critical wave number. It is observed that the fluid layer with suspended particles heated from below is more stable compared to the classical fluid layer without suspended particles.

Keywords: Micropolar fluids, Rayleigh-Bénard convection, Suction-injection-combination and electroconvection.

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1. Introduction

Convection in Eringen's micropolar fluid has been the subject of intensive study because of the remarkable physical properties of the fluid as well as its practical applications (see Power [1], Lukasazewicz [2] and Eringen [3]). The Rayleigh-Bénard convection in Eringen's micropolar fluid [4] have been studied by many of authors (Datta and Sastry [5], Ahmadi [6], Bhattacharya and Jena [7], Siddheshwar and Pranesh [8-11], Pranesh and Riya Baby [12] and Pranesh and Arun Kumar [13]).

The classical Rayleigh problem of onset of convection instabilities in a horizontal layer of fluid heated from below has its origin in the experimental observations of Bénard [14]. In the standard classical problem there is no flow across the horizontal boundaries. A modified problem, where the boundaries are permeable and there is injection of fluid at one boundary and suction of fluid at the other boundary, was studied by Sharvartsblat [15]. He pointed out, that the problem is of interest because of possibilities of controlling the convection instability by adjusting of SIC. The effect of SIC is in general quit complex because not only the basic temperature profile is altered, but in the perturbation equations contribution arises from the convection of both temperature and velocity, and there is an interaction between Prandtl number comes into play. Nield [16] considered the classical problem for viscous fluid and studied analytically the effect of SIC on the onset of convection in a fluid layer between permeable horizontal boundaries. He gave a new theory for the destabilizing effects of SIC, when flow is from a dynamically rigid and thermally conducting boundary to a dynamically free and thermally insulating boundary. He also pointed that when Prandtl number is close to unity the amount of destabilization is small but this is not true when Prandtl number is either large or small. Many authors (Siddheshwar and Pranesh [17], Shivakumara and Suma [18], Murty and Ramana Rao [19] and Murty [20, 21]) have studied the effect of SIC on Newtonian and non-Newtonian fluid using classical Fourier law.

The objective of this paper is to study the effect of suction-injection-combination on the onset of Rayleigh-Bénard electroconvection in a micropolar fluid.

2. Mathematical Formulation

Consider an infinite horizontal layer of a Boussinesquian, electrically conducting micropolar fluid of depth 'd' permeated by an externally applied uniform magnetic field normal to the layer. A cartesian coordinate system is taken with origin in the lower boundary and z-axis vertically upwards. Let ΔT be the temperature difference between the upper and lower boundaries (see Figure (1)). A constant flow in the vertical direction, known as SIC, is maintained at the boundaries.

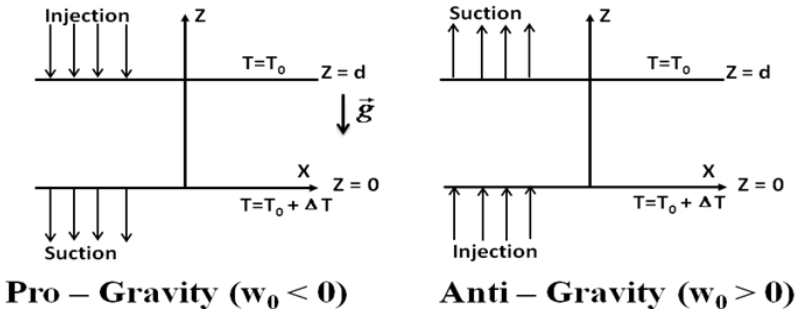


Fig 1: Schematic diagram of the flow configuration.

The governing equations for the Rayleigh-Bénard situation in a Boussinesquian micropolar fluid are:

Continuity equation:

$$\nabla \cdot \vec{q} = 0, \quad (1)$$

Conservation of linear momentum:

$$\rho_0 \left[\frac{\partial \vec{q}}{\partial t} + (\vec{q} \cdot \nabla) \vec{q} \right] = -\nabla p - \rho_0 \vec{g} \hat{k} + (2\zeta + \eta) \nabla^2 \vec{q} + \zeta \nabla \times \vec{\omega} + (\vec{P} \cdot \nabla) \vec{E}, \quad (2)$$

Conservation of angular momentum:

$$\rho_0 I \left[\frac{\partial \vec{\omega}}{\partial t} + (\vec{q} \cdot \nabla) \vec{\omega} \right] = (\lambda' + \eta') \nabla (\nabla \cdot \vec{\omega}) + (\eta' \nabla^2 \vec{\omega}) + \zeta (\nabla \times \vec{q} - 2\vec{\omega}), \quad (3)$$

Conservation of energy:

$$\frac{\partial T}{\partial t} + (\vec{q} \cdot \nabla) T = \frac{\beta}{\rho C_v} (\nabla \times \vec{\omega}) \cdot \nabla T + \chi \nabla^2 T, \quad (4)$$

Equation of state:

$$\rho = \rho_o[1 - \alpha(T - T_o)], \tag{5}$$

Equation of state for dielectric constant:

$$\epsilon_r = (1 + \chi_e) - e(T - T_o), \tag{6}$$

Faraday's law:

$$\nabla \times \vec{E} = 0, \vec{E} = \nabla \phi, \tag{7}$$

Equation of polarisation field:

$$\nabla \cdot (\epsilon_o \vec{E} + \vec{P}) = 0, \vec{p} = \epsilon_o (\epsilon_r - 1) \vec{E} \tag{8}$$

where, \vec{q} is the velocity , ρ_o is density of the fluid at temperature $T = T_o$, p is the pressure, ρ is the density, \vec{g} is acceleration due to gravity, ζ is coupling viscosity coefficient or vortex viscosity, \vec{P} is dielectric polarization, \vec{E} is the electric field, λ and η are the bulk and shear spin-viscosity coefficients, $\vec{\omega}$ is the angular velocity, I is moment of inertia, λ' and η' are bulk and shear spin-viscosity coefficients, T is the temperature, χ is the thermal conductivity, β is micropolar heat conduction coefficient, α is coefficient of thermal expansion, determining how fast the density decreases with temperature, σ is electrical conductivity, ϵ_r is the dielectric constant, χ_e is electric susceptibility, ϵ_o is the electric permittivity of free space and ϕ is the electric scalar potential.

3. Basic State

The basic state of the fluid being quiescent is described by

$$\left. \begin{aligned} \vec{q}_b = w_o \hat{k}, \vec{\omega}_b = 0, p = p_b(z), \rho = \rho_b(z), \vec{E} = \vec{E}_b(z), \\ \vec{P} = \vec{P}_b(z), T = T_b(z), \epsilon_r = \epsilon_{rb}(z), \end{aligned} \right\} \tag{9}$$

where, w_o is the strength of the imposed constant suction (or injection) and \hat{k} is the unit vector in the z-direction. The pro-gravity SIC and anti-gravity SIC is shown schematically in figure (1).

Substituting equation (10) into basic governing equations (1)-(8), we obtain the quiescent state solutions as:

$$\left. \begin{aligned}
 \frac{dp_b}{dz} &= -\rho_b g + P_b \frac{\partial E_b}{\partial z}, \\
 w_0 \frac{dT_b}{dz} &= \chi \frac{d^2 T_b}{dz^2}, \\
 \rho_b &= \rho_o [1 - \alpha(T_b - T_o)], \\
 \varepsilon_r &= (1 + \chi_e) - e(T_b - T_o), \\
 E_b &= \left[\frac{(1 + \chi_e) E_0}{(1 + \chi_e) + \frac{e \Delta T}{h} z} \right], \\
 P_b &= \varepsilon_o E_0 (1 + \chi_e) \left[1 - \frac{1}{(1 + \chi_e) + \frac{e \Delta T_z}{h}} \right]
 \end{aligned} \right\} \quad (10)$$

Solving equation for T_b using the boundary conditions

$$T_b = T_o + \Delta T \quad \text{at } z = 0,$$

$$T_b = T_o \quad \text{at } z = d,$$

we get,

$$T_b = T_o + \frac{\Delta T}{\left[1 - e^{-\frac{w_o d}{\chi}} \right]} \left[e^{-\frac{w_o z}{\chi}} - 1 \right]. \quad (11)$$

We now superpose infinitesimal perturbations on the quiescent basic state and study the instability.

4. Linear Stability Analysis

Let the basic state be disturbed by an infinitesimal thermal perturbation. We now have

$$\left. \begin{aligned} \bar{q} &= w_0 \hat{k} + \bar{q}', \bar{\omega} = \bar{\omega}_b + \bar{\omega}', p = p_b + p', \rho = \rho_b + \rho', \\ \varepsilon_r &= \varepsilon_{rb} + \varepsilon_r', \bar{E} = \bar{E}_b + (E_1 \hat{i} + E_3 \hat{k}), \bar{P} = \bar{P}_b + (P_1 \hat{i} + P_3 \hat{k}), \\ T &= T_b + T', \end{aligned} \right\} \tag{12}$$

The primes indicate that the quantities are infinitesimal perturbations and subscript 'b' indicates basic state value.

Substituting equation (12) into equations (1)-(8) and using the basic state equations (10), we get linearised equations governing the infinitesimal perturbations in the form:

$$\nabla \cdot \bar{q}' = 0, \tag{13}$$

$$\rho_o w_0 \left[\frac{\partial \bar{q}'}{\partial t} \right] = -\nabla p' - \rho' g \hat{k} + (2\zeta + \eta) \nabla^2 \bar{q}' + (\zeta \nabla \times \bar{\omega}') + (\bar{P}_b \cdot \nabla) \bar{E}' + (\bar{P}' \cdot \nabla) \bar{E}_b \tag{14}$$

$$\rho_o I w_0 \left[\frac{\partial \bar{\omega}'}{\partial t} \right] = (\lambda' + \eta') \nabla (\nabla \bar{\omega}') + (\eta' \nabla^2 \bar{\omega}') + \zeta (\nabla \times \bar{q}' - 2\bar{\omega}'), \tag{15}$$

$$w_0 \frac{dT'}{dz} = \frac{\Delta T}{\left[1 - e^{-\frac{w_{0d}}{\chi}} \right]} \left(\frac{w_0 z}{\chi} \right) \left[\frac{\beta}{\rho_o C_v} \nabla \times \bar{\omega}' - W' \right] + \chi \nabla^2 T', \tag{16}$$

$$\rho' = -\alpha \rho_o T', \tag{17}$$

$$\varepsilon_r' = -\varepsilon_0 e T', \tag{18}$$

$$\nabla \cdot (\varepsilon_0 \bar{E}' + \bar{P}') = 0. \tag{19}$$

Using equation (17) in (14), operating curl twice on the resulting equation, operating curl on equation (15) we get,

$$\left. \begin{aligned} \rho_0 w_0 \frac{\partial}{\partial z} (\nabla^2 w') &= \rho_0 \alpha g \nabla_1^2 T' + (2\zeta + \eta) \nabla^4 w' + \zeta \nabla^2 (\nabla \times \bar{\omega}') \\ &- \frac{\Delta T}{\left(1 - e^{-\frac{w_0 d}{z}}\right)} \frac{w_0}{\chi} e^{\frac{w_0 z}{\chi}} \left[\frac{\epsilon_0 e^2 E_0^2 \nabla_1^2 T'}{(1 + \chi_e)} - \epsilon_0 e E_0 \nabla_1^2 D\phi' \right], \end{aligned} \right\} \quad (20)$$

$$\rho_0 I w_0 \left[\frac{\partial (\nabla \times \bar{\omega}')}{\partial z} \right] = \eta' \nabla^2 (\nabla \times \bar{\omega}') + \zeta (\nabla^2 w - 2 \nabla \times \bar{\omega}'), \quad (21)$$

$$(1 + \chi_e) \nabla^2 \phi' - e E_0 D T' = 0. \quad (22)$$

The perturbation equations (16), (20), (21) and (22) are non-dimensionalised using the following definition:

$$\left. \begin{aligned} (x^*, y^*, z^*) &= \frac{(x, y, z)}{d}, \quad W^* = \frac{W'}{\left(\frac{\chi}{d}\right)}, \quad \omega^* = \frac{\omega'}{\left(\frac{\chi}{d}\right)}, \\ t^* &= \frac{t}{\left(\frac{d^2}{\chi}\right)}, \quad T^* = \frac{T'}{\Delta T}, \quad \phi^* = \frac{\phi'}{e E_0 \Delta T d}, \quad \Omega^* = \frac{\nabla \times \bar{w}}{d^3} \end{aligned} \right\} \quad (23)$$

Using equation (23) into equations (16), (20), (21) and (22) we get the dimensionless equations in the form (after neglecting the asterisks):

$$\left. \begin{aligned} \frac{Pe}{Pr} \frac{\partial}{\partial z} (\nabla^2 w) &= R \nabla_1^2 T + (1 + N_1) \nabla^4 W + N_1 \nabla^2 \Omega_z \\ &- \frac{Pe (e^{PeZ})}{(1 - e^{Pe})} \left[L \nabla_1^2 T - L \frac{\partial}{\partial z} (\nabla_1^2 \phi) \right] = 0 \end{aligned} \right\} \quad (24)$$

$$\frac{N_2 Pe}{Pr} \frac{\partial \Omega_z}{\partial z} = N_3 \nabla^2 \Omega_z - N_1 \nabla^2 W - 2 N_1 \Omega_z, \quad (25)$$

$$Pe \frac{\partial T}{\partial z} = \nabla^2 T + \frac{Pe(e^{PeZ})}{(1-e^{Pe})} (N_5 \Omega_z - W), \tag{26}$$

$$\nabla^2 \phi - \frac{\partial T}{\partial z} = 0. \tag{27}$$

The non-dimensional parameters $N_1, N_2, N_3, N_5, Pr, L, Pe$ and R are as defined as

$$N_1 = \frac{\zeta}{\zeta + \eta} \tag{Coupling Parameter},$$

$$N_2 = \frac{I}{d^2} \tag{Inertia Parameter},$$

$$N_3 = \frac{\eta'}{(\zeta + \eta)d^2} \tag{Couple Stress Parameter},$$

$$N_5 = \frac{\beta}{\rho_o C_v d^2} \tag{Micropolar Heat Conduction Parameter},$$

$$Pr = \frac{\zeta + \eta}{\rho_o \chi} \tag{Prandtl Number},$$

$$L = \frac{\epsilon_0 e^2 E_0^2 \Delta T^2 d^2}{(1 + \chi_e)(\zeta + \eta)\chi} \tag{Electric Rayleigh Number},$$

$$Pe = \frac{w_0 d}{\kappa} \tag{Peclet number},$$

$$R = \frac{\rho_o \alpha g \Delta T d^3}{\chi(\zeta + \eta)} \tag{Rayleigh number}.$$

The infinitesimal perturbation W, Ω_z, T and ϕ are assumed to be periodic waves (see Chandrasekhar [36]) and hence these permit a normal mode solution in the form

$$\begin{bmatrix} W \\ \Omega_z \\ T \\ \phi \end{bmatrix} = \begin{bmatrix} W(z) \\ G(z) \\ T(z) \\ \phi(z) \end{bmatrix} e^{i(lx+my)}, \quad (28)$$

where l and m are horizontal components of the wave number a^2 ,
Substituting equation (28) into equations (24)-(27), we get

$$\left. \begin{aligned} \frac{Pe}{Pr} D(D^2 - a^2)W &= (1 + N_1)(D^2 - a^2)^2 W - Ra^2 T + N_1(D^2 - a^2)G \\ &- \frac{Pe(e^{PeZ})}{(1 - e^{Pe})} [-La^2 T + La^2 D\phi] \end{aligned} \right\}, \quad (29)$$

$$\frac{N_2 Pe}{Pr} DG = N_3(D^2 - a^2)G - N_1(D^2 - a^2)W - 2N_1 G, \quad (30)$$

$$PeDT = (D^2 - a^2)T + \frac{Pe(e^{PeZ})}{(1 - e^{Pe})}(W - N_5 G), \quad (31)$$

$$(D^2 - a^2)\phi - DT = 0, \quad (32)$$

where, $D = \frac{d}{dz}$.

Equations (26)-(29) are solved using the Galerkin technique. Multiplying equation (29) by W , equation (30) by G , equation (31) by T , and equation (32) by ϕ and integrating the resulting equation by parts with respect to z from 0 to 1 and taking $W = AW_1$, $G = BG_1$, $T = CT_1$ and $\phi = E\phi_1$ in which A, B, C and E are constants with W_1, G_1, T_1 and ϕ_1 are trial functions. This procedure yields the following equation for the Rayleigh number R :

$$R = \frac{Y_1 Y_3 Y_4}{a^2 \langle W_1 T_1 \rangle Y_2} + L \frac{Y_5}{\langle W_1 T_1 \rangle \langle \phi_1 (D^2 - a^2) \phi_1 \rangle}, \quad (33)$$

where,

$$\begin{aligned}
 Y_1 &= N_3 \langle G_1(D^2 - a^2)G_1 \rangle - 2N_1 \langle G_1^2 \rangle, \\
 Y_2 &= N_1 N_5 \langle G_1(D^2 - a^2)W_1 \rangle \langle T_1 G_1 f(z) \rangle - \langle T_1 W_1 f(z) \rangle Y_1, \\
 Y_3 &= P_e \langle T_1 D T_1 \rangle - \langle T_1(D^2 - a^2)T_1 \rangle, \\
 Y_4 &= (1 + N_1) \left\langle W_1(D^2 - a^2)^2 W_1 \right\rangle - \frac{P_e}{Pr} \left\langle W_1 D(D^2 - a^2)W_1 \right\rangle \\
 &\quad + N_1^2 \frac{\langle G_1(D^2 - a^2)W_1 \rangle \langle W_1(D^2 - a^2)G_1 \rangle}{Y_1} \left. \vphantom{Y_4}} \right\rangle, \\
 Y_5 &= \langle W_1 T_1 f(z) \rangle \langle \phi_1(D^2 - a^2)\phi_1 \rangle - \langle W_1 D\phi_1 f(z) \rangle \langle \phi_1 D T_1 \rangle.
 \end{aligned}$$

In the equation (33), $\langle \dots \rangle$ denotes integration with respect to z between $z=0$ and $z=1$. We note here that R in equation (33) is a functional and the Euler–Lagrange equations for the extremisation of R are equations (29)–(32).

The value of critical Rayleigh number depends on the boundaries. In this paper we consider the following boundary combinations:

Free–free isothermal and no spin.

$$W = D^2 W = T = G = D\phi = 0, \quad \text{at } z = 0, 1.$$

Rigid–rigid isothermal and no spin.

$$W = DW = T = G = D\phi = 0, \quad \text{at } z = 0, 1.$$

Rigid–free isothermal and no spin.

$$W = DW = T = G = D\phi = 0, \quad \text{at } z = 0,$$

$$W = D^2 W = T = G = D\phi = 0, \quad \text{at } z = 1.$$

Free–free adiabatic and no spin.

$$W = D^2 W = DT = G = D\phi = 0, \quad \text{at } z = 0, 1.$$

(a) Rigid–rigid isothermal and no spin.

$$W = DW = DT = G = D\phi = 0, \quad \text{at } z = 0, 1.$$

(b) Rigid-free isothermal and no spin.

$$W = DW = DT = G = D\phi = 0, \quad \text{at } z = 0,$$

$$W = D^2W = DT = G = D\phi = 0, \quad \text{at } z = 1.$$

The trial functions satisfying the boundary conditions are presents in Table 1.

Table 1: Trial functions for the different for the different boundary conditions.

Boundary conditions	Free-free	Rigid-rigid	Rigid-free
W_1	$z^4 - 2z^3 + z$	$W_1 = z^4 - \frac{5}{2}z^3 + \frac{3}{2}z^2$	$W_1 = z^4 - 2z^3 + z^2$
G_1	$z(z-1)$	$z(z-1)$	$z(z-1)$
ϕ_1	$z^2(3-2z)$	$z^2(3-2z)$	$z^2(3-2z)$
Isothermal T_1	$z(1-z)$	$z(1-z)$	$z(1-z)$
Adiabatic T_1	1	1	1

5. Results and Discussion

In this chapter, we study the effects of suction-injection-combination and electric field on the onset of Rayleigh-Bénard convection in a micropolar fluid.

Before discussing the results obtained in this paper, the following observations are made from the equation (33). In the case of symmetric boundaries (free-free and rigid - rigid) the value of R_c is same for both pro and anti-gravity suction-injection-combinations as R_c is an even function of Pe and in the case of non-symmetric boundary combination (rigid - free) R_c is not an even function, thus the value of R_c is not the same for both $Pe < 0$ and $Pe > 0$ even in the absence of magnetic field.

The critical Rayleigh number R_c obtained using Galerkin method for different values of $N_1, N_3, N_5, L,$ and Pr are shown in figures (3) - (14). Figures (3) - (8) pertain to different velocity boundary

combination and isothermal temperature boundaries and figures (9) – (14) pertain to adiabatic temperature boundaries.

Figure (3) is the plot of R_c versus Pe for different values of coupling parameter, N_1 , and for different velocity boundary combinations with isothermal temperature conditions. It is found that R_c increases with the increase in N_1 . N_1 represents the concentration of microelements in the fluid. When N_1 increases concentration of the microelements are also increases, this microelemetns consume greater part of the energy in forming the gyration velocity, which delays the onset of convection. From this we conclude that increase in concentration of microelements stabilizes the system.

Figure (4) are the plot of R_c versus Pe for different values of couple stress parameter, N_3 , for different velocity boundary combinations with isothermal temperature conditions. From the figure we observe that the increase in N_3 decreases R_c . This is because, when N_3 increases the couple stress of the fluid increases, which decreases the microrotation and thereby destabilizing the system.

Figure (5) are the plot of R_c versus Pe for different values of micropolar heat conduction parameter, N_5 , for different velocity boundary combinations with isothermal temperature conditions. Clearly, R_c increase with N_5 . When N_5 increases, the heat induced into the fluid due to microelements also increases, thus reducing the heat transfer from bottom to top. The decrease in heat transfer is responsible for delaying the onset of instability. Thus, the effect of N_5 is to stabilizes the system.

Figure (6) are the plot of R_c versus Pe for different values of electric Rayleigh number, L , for different velocity boundary combinations with isothermal temperature conditions. It is found that as L increases, R_c decreases. Thus, L destabilizes the system.

Figures (7) are the plot of R_c versus Pe for different values of Prandtl number, Pr , for different velocity boundary combinations with isothermal temperature conditions. From the figure it observed that in the case of anti-gravity SIC increase in Pr , increases R_c , thus stabilizing the system. In the case of pro-gravity SIC we see that R_c decreases with an increase in Pr and thereby destabilizes the system. Thus in deciding stability of the system Prandtl number plays an important role.

Figures (8) – (12) are plots for adiabatic boundaries corresponding to figures (3) – (7) of isothermal boundaries. The results of adiabatic boundaries are qualitatively similar to that of isothermal boundaries.

From the above figures the following points are noted:

- 1) In the case of anti-gravity SIC, i.e., $Pe > 0$, increase in Pe decreases R_c initially (for small values of Pe up to a certain critical value of Pe namely Pe_c) and further increase in Pe beyond Pe_c increases the R_c . Thus the weak anti-gravity SIC in micropolar fluids destabilizes the system. This may be due to distortion of the basic temperature profile caused by SIC. Physically this amounts to an increase in the rate at which energy is supplied to the disturbance. In the case of pro-gravity SIC, i.e., $Pe < 0$, increase in Pe increases R_c and thus the pro-gravity SIC makes the system stable.
- 2) We also find that $R_c^{RR} > R_c^{RF} > R_c^{FF}$, where the superscripts correspond to the three different velocity boundary combinations. Thus rigid-rigid boundary is more stable compared to other velocity boundary combinations.
- 3) In the case of adiabatic boundary the convection sets in at wave number, $a_c = 0$.
- 4) It is also observed from the table that $Pe_c^{RR} < Pe_c^{FF} < Pe_c^{RF}$. The behavior of Pe_c in adiabatic case is quantitatively similar to that observed in the case of isothermal boundaries.

6. Conclusion

It is found that the effect of SIC is to stabilize or destabilize accordingly SIC are Pro-gravity and anti-gravity. Thus, by adjusting the suction-injection-combination and Prandtl number, Pr it is possible to control the convection in a micropolar fluid with electric field.

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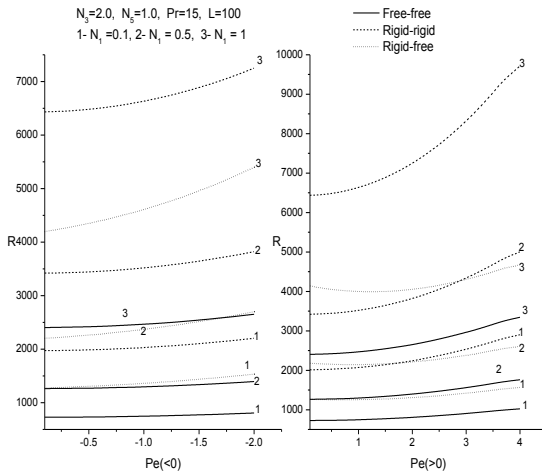


Fig 2: Plot of Rayleigh number R versus Peclet number Pe for different values of coupling parameter N_1 for different velocity boundary combinations and isothermal temperature condition.

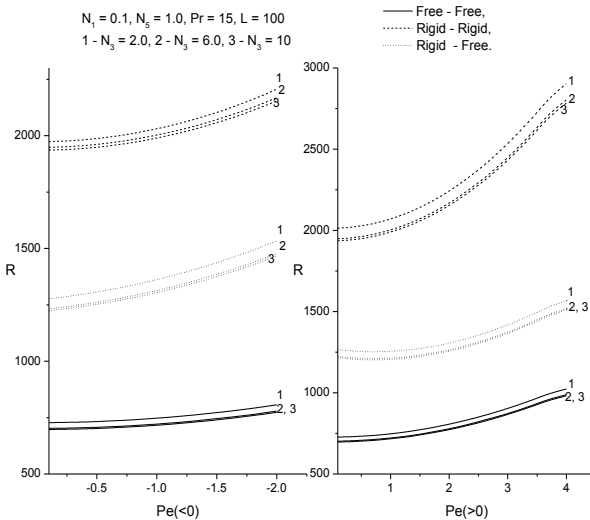


Fig 3: Plot of R versus Pe for different values of couple stress parameter N_3 for different velocity boundary combinations and isothermal temperature condition.

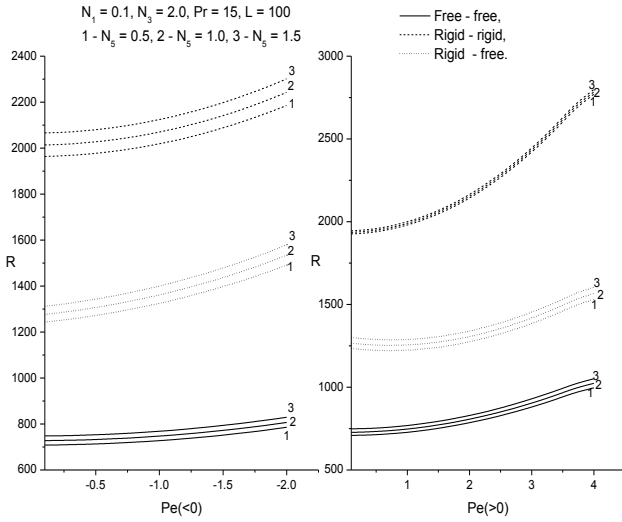


Fig 4: Plot of R versus Pe for different values of micropolar heat conduction parameter N_5 for different velocity boundary combinations and isothermal temperature condition.

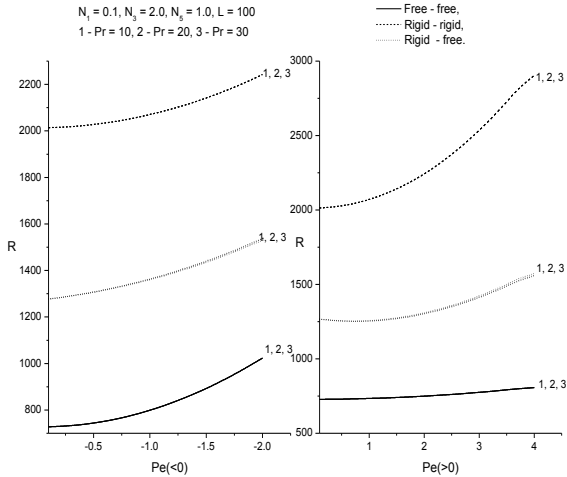


Fig 5: Plot of R versus Pe for different values of Prandtl number Pr for different velocity boundary combinations and isothermal temperature condition.

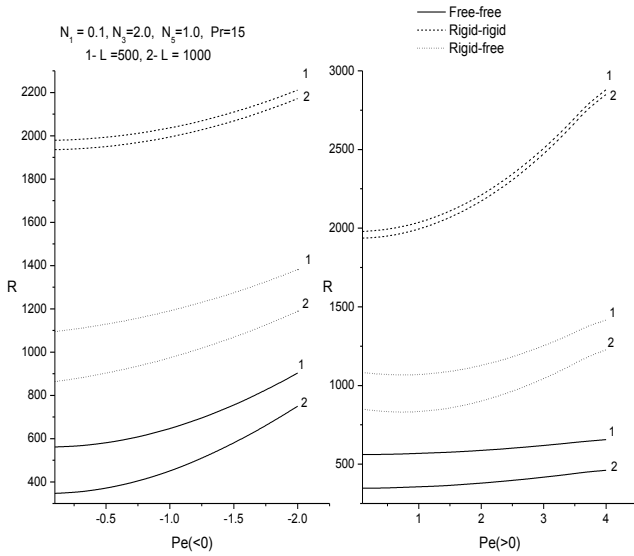


Fig 6: Plot of R versus Pe for different values of Electric Rayleigh number L for different velocity boundary combinations and isothermal temperature condition.

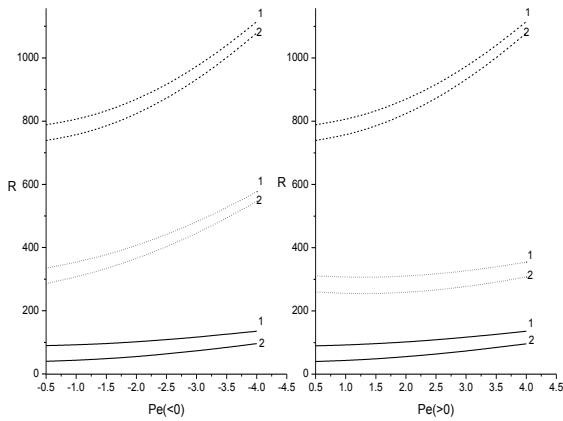


Fig 7: Plot of R versus Pe for different values of Electric Rayleigh number L for different velocity boundary combinations and adiabatic temperature condition.

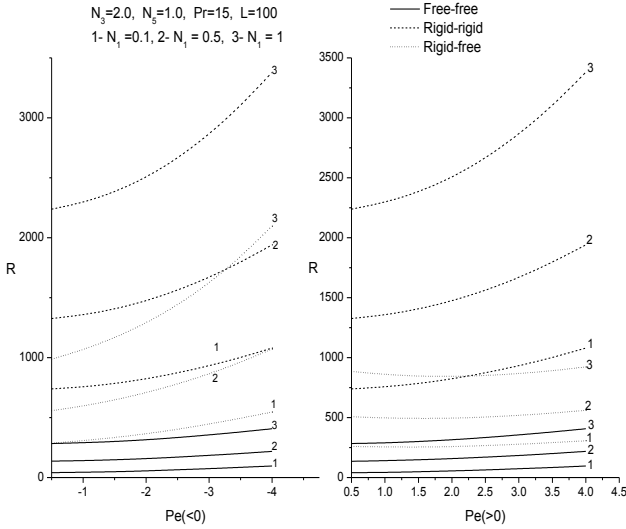


Fig 8: Plot of R versus Pe for different values of coupling parameter N_1 for different velocity boundary combinations and adiabatic temperature condition.

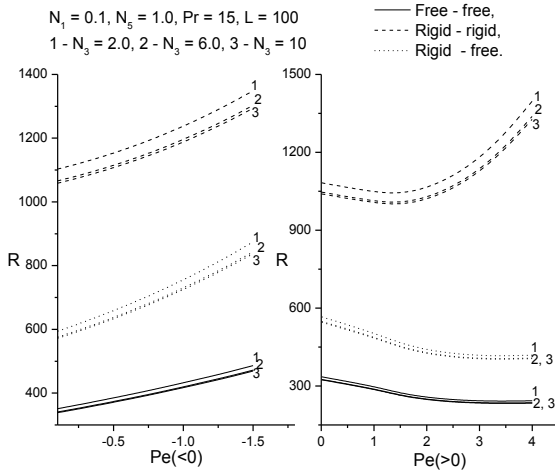


Fig 9: Plot of R versus Pe for different values of couple stress parameter N_3 for different velocity boundary combinations and adiabatic temperature condition.

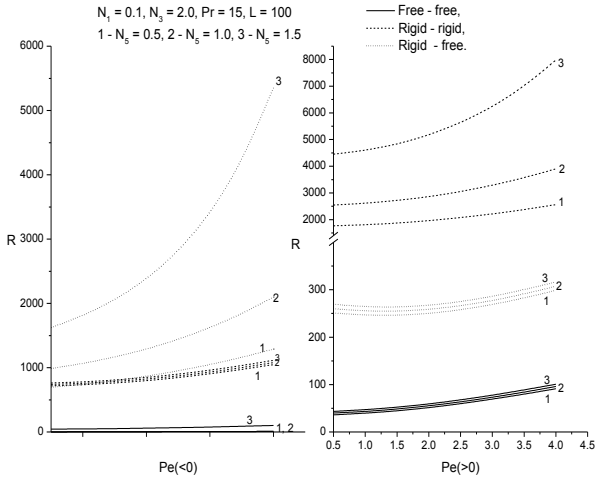


Fig 10: Plot of R versus Pe for different values of micropolar heat conduction parameter N_5 for different velocity boundary combinations and adiabatic temperature condition.

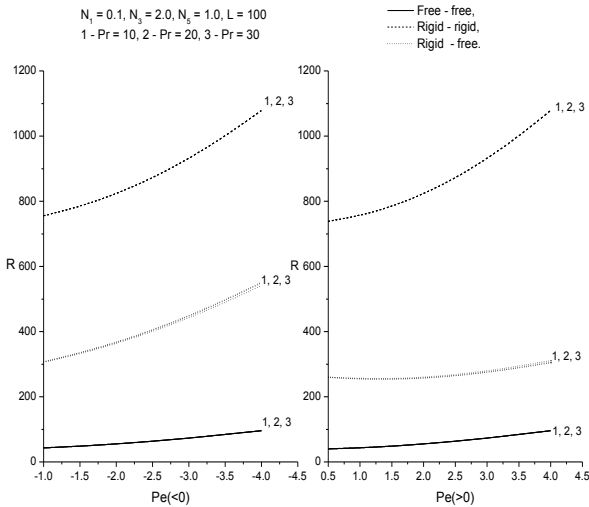


Fig 11: Plot of R versus Pe for different values of Prandtl number Pr for different velocity boundary combinations and adiabatic temperature condition.