Hybrid Control Accommodation for Water-asset Management of Hydraulic Systems Subjected to Large Operating Conditions

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Abstract: The Hybrid Control Accommodation (HCA) strategy was proposed to improve the water-asset management of hydraulic systems by resource allocation and setpoint assignment. Hydraulic system dynamics are taken into account during the setpoint assignment step which consists in controlling gates for large operating conditions. For hydraulic systems subjected to strong disturbances, transfer delays are variable, thus different operating modes must be considered. A multimodelling method, associated to a selection technique of transfer delay, allowing for the determination of the number of models, is proposed. The simulation results on the first reach of the Neste canal show the effectiveness of the HCA strategy.

Keywords: Hybrid control accommodation, resource allocation, setpoint assignment, multimodelling, water management.

1 Introduction

Hydrographic networks naturally convey water quantities upstream to downstream. They are equipped with dams, catchment areas, channels, etc., and are instrumented for water resource management and satisfaction of human activity needs. Several control methods have been designed [9], and are still designed [8, 2], to supply hydraulic systems with water quantities corresponding to the management objectives and rejecting disturbances. Other techniques, such as LPV regulation [10] or supervised internal multimodel controller [3] were recently proposed in order to consider these systems for different operating points. These control methods are accurate for a local control. However, they are not designed to allocate water quantities in excess towards the catchments areas, and water quantities in lack amongst the users. An original proposition for the management of such situations consists in recalculating setpoints according to the resource value (continuous dynamics) and to the resource state (discrete events) of the hydrographic systems. The supervision and hybrid control accommodation strategy by resource allocation and setpoint assignment proposed in [4] allows the water-asset management to take into account the management constraints. The strategy efficiency has been shown by simulation, in the case of an open-channel hydraulic system considering large operating conditions.

The problem addressed in this paper deals with the water-asset management of a hydraulic system subjected to scenarii with large disturbances. In the second section, the supervision and hybrid control accommodation strategy, well adapted to consider large operating conditions, is presented. In the third section, a multimodelling method is proposed for determining the number of Operating Modes (OM) necessary to represent open-surface hydraulic system dynamics, accurately. For each OM, the transfer delay identification is done in the fourth section. Finally, the effectiveness of this proposed strategy is shown by simulation on the first reach of the Neste canal.

2 Hybrid control accommodation

Hybrid Control Accommodation (HCA) strategy (*see* figure 1) allows the computation of new setpoints for each gate G_j of hydraulic systems according to data measured on the measurement points M_i (*see* figure 2). The setpoints are computed according to the resource state e_i , and taking into account management objectives q_{jobj} , λ_j and μ_j weekly fixed by the Management Objective Generation module.



Figure 1: HCA strategy scheme.



Figure 2: Open-surface hydraulic system equipped with measurement points M_i and gates G_j .

The resource state e_i determination is carried out at the detection period T_e by concurrent hybrid automata (*see* figure 3) designed for each measurement point M_i [4]. The five pertinent states retained correspond respectively to no-discrepancy state e_0 , two states where the discharge discrepancy is either positive (e+) or negative (e-) and constant c, and two states where the discharge discrepancy is either positive (e+) or negative (e-) and no constant $\neg c$. Transitions between states are defined as conditions on the measured discharge value and variation:

$$\begin{cases} d_i : [|\Delta Q_{M_i}| > th_i], \\ \psi_i : [\Delta Q_{M_i} < 0], \\ \omega_i : [|\dot{Q}_{M_i}| < dth_i], \end{cases}$$
(1)

with $\Delta Q_{M_i} = Q_{M_i} - \sum_{j=n_i}^n q_{j\,obj}$, where Q_{M_i} is the measured discharge, $q_{j\,obj}$ is the management objective of the gate *j*, n_i the index of the first gate downstream the *i*th measurement point M_i , *n* the number of

gates, \dot{Q}_{M_i} the estimate derivative of Q_{M_i} , th_i and dth_i respectively the detection and diagnosis thresholds.

The discharge discrepancy allocation is carried out according to the resource state. When the state is e_0 , the gate setpoints correspond to their discharge objective $q_{j\,obj}$. When the state is $e \pm \wedge c$, the discharge discrepancy ΔQ_{M_i} is allocated amongst gates, according to their weights λ_j and μ_j , by optimizing, for each measurement point, a cost function. Finally, when the state is $e \pm \wedge \neg c$, the discharge discrepancy is allocated on gate each one on its turn [4]. At each detection date kT_e , the discharge discrepancy allocation leads to the allocation vector $\mathbf{q}_{M_i}^k$:

$$\mathbf{q}_{M_i}^k = \begin{bmatrix} 0 \ 0 \ \dots \ 0 \ q_{n_i}^k \ q_{n_i+1}^k \ \dots \ q_n^k \end{bmatrix}^I \quad , \tag{2}$$



Then, to synchronize the control of the gate with the appearance of lacks or excess of the water due to the disturbances, the setpoints must be assigned at a date taking into account the transfer delays $T_{M_i,j}$ between the measurement point M_i and the gate G_j . It is computed according to the relation (3):

$$T_{M_{i},j} = T_{M_{i},n_{i}} + \sum_{r=n_{i}+1}^{j} t_{r} , \qquad (3)$$

where t_r is the time necessary for the water quantity to go from gate G_{r-1} to gate G_r (see Figure 4).

The delay t_r depends on the physical characteristics of the hydraulic system and on the discharge value Q_r . Thereafter, the allocation vector $\mathbf{q}_{M_i}^k$ is associated with an allocation dates vector \mathbf{T} arising





Figure 4: Time delays between M_i and G_i .

from the transfer delay values $T_{M_i,j}$. Finally, taking into account the allocation date, the setpoints are sent to gates periodically. The control period T_c is chosen as a multiple integer of T_e . In the next section, a multimodelling method is proposed to identify the system dynamics for several OM.

3 Multimodelling steps

The modelling of the free-surface hydraulic system dynamics is generally carried out starting from the diffusive wave equation (4) which is obtained by simplifying Saint Venant equations [1].

$$\frac{dQ}{dt} + C\frac{dQ}{dx} - D\frac{d^2Q}{dx^2} = 0 \quad , \tag{4}$$

where C and D are respectively the celerity and diffusion coefficients.

The diffusive wave equation can be linearized according to an operating discharge Q_e [7], and the identified celerity and diffusion parameters, denoted C_e and D_e , are expressed as:

$$\begin{cases} C_e = \frac{1}{L^2 \frac{\partial J}{\partial Q_e}} \left[\frac{\partial L}{\partial x} - \frac{\partial J L}{\partial z} \right], \\ D_e = \frac{1}{L \frac{\partial J}{\partial Q_e}}, \end{cases}$$
(5)

where *L* is the surface width, *z* is the discharge depth, *J* is the friction slope expressed with the Manning-Strickler relation as $J = \frac{Q^2 P^{\frac{4}{3}}}{K^2 S^{\frac{10}{3}}}$ where *K* is the Strickler coefficient, *P* is the wetted perimeter and *S* the wetted surface. The open-channel systems dynamics can be modelled by transfer functions, as:

$$F(s) = \frac{e^{-\tau s}}{1 + w_1 s + w_2 s^2} \quad , \tag{6}$$

where the coefficients w_1 , w_2 and the pure delay τ are computed according to the coefficients C_e , D_e , to the open-channel system length X, and to the adimensional coefficient $C_L = \frac{2C_e X}{9D_e}$; if $C_L \le \frac{4}{9}$, $w_2 = 0$ and $\tau = 0$, if $\frac{4}{9} < C_L \le 1$, $w_2 = 0$.

This modelling method allows the identification of the free-surface hydraulic system dynamics with good accuracy only around an operating point. However, setpoint assignment must be done for hydraulic system subjected to large operating conditions. Thus, the hydraulic system dynamics must be identified for different OM. Based on the previous modelling method, the multimodelling approach consists in determining the number of OM and their corresponding operating points.

The celerity coefficient *C* is a very relevant parameter of the hydraulic system dynamics. The model identified for each OM is available as soon as the error on the celerity coefficient is less than a predefined percentage Π_C . Thus, a validity domain is defined for each OM, and the number of OM which are necessary to identify the dynamics with a good accuracy, is determined. To limit the switching between two OM, an interval Δ_C is shared by two successive OM validity domains. The selection of parameters Π_C and Δ_C is carried out taking into account the system dynamics. The multimodelling steps are described

Table 1: Multimodelling algorithm.

Input:
$$C_{min}, C_{max}, \Pi_C, \Delta_C,$$

Output: $C_{id_r}, C_{inf_r}, C_{sup_r},$
 $C_{med} = \frac{C_{min} + C_{max}}{2},$
 $r = 1,$
For $i: \left\lfloor \frac{ln \frac{C_{min}}{C_{med}}}{ln^{1+\Pi_C}} \right\rfloor + 1$ to $\left\lfloor \frac{ln \frac{C_{max}}{C_{med}}}{ln^{1+\Pi_C}} \right\rfloor,$
 $C_{id_r} = \left(\frac{1+\Pi_C}{1-\Pi_C}\right)^i C_{med} - \frac{sign(i)\Delta_C}{1-sign(i)\Pi_C} \sum_{j=1}^{|i|} \left(\frac{1+\Pi_C}{1-\Pi_C}\right)^{i-sign(i).j},$
 $C_{sup_r} = (1+\Pi_C) \left(\frac{1+\Pi_C}{1-\Pi_C}\right)^i C_{med} - sign(i) \frac{(1+\Pi_C)\Delta_C}{1-sign(i)\Pi_C} \sum_{j=1}^{|i|} \left(\frac{1+\Pi_C}{1-\Pi_C}\right)^{i-sign(i).j},$
 $C_{inf_r} = (1-\Pi_C) \left(\frac{1+\Pi_C}{1-\Pi_C}\right)^i C_{med} - sign(i) \frac{(1-\Pi_C)\Delta_C}{1-sign(i)\Pi_C} \sum_{j=1}^{|i|} \left(\frac{1+\Pi_C}{1-\Pi_C}\right)^{i-sign(i).j},$
 $r + +,$
EndFor

by an algorithm (*see* Table 1), where the OM are determined starting with C_{med} . This one is computed with the parameters C_{min} and C_{max} corresponding respectively to the minimum and maximum discharges of the system. The algorithm requires the definition of $\lfloor x \rfloor$ which corresponds to the integer part of *x*, and sign(x) such as $sign(x) = \frac{|x|}{x}$.

Then, according to C_{id_r} , the water elevation z_{id_r} of each r^{th} OM is determined, with one millimeter accuracy, using the digital resolution of the relation (7) with the Newton method.

$$C_{id} = \frac{\sqrt{JKS^{\frac{5}{3}}}}{P^{\frac{2}{3}}L^{2}} \left[-\frac{1}{2}\frac{\partial L}{\partial z} - \frac{L}{3P} \left(2\frac{\partial P}{\partial z} - 5\frac{P}{S}\frac{\partial S}{\partial z} \right) \right]$$
(7)

Then, the water elevation z_{id_r} value is used to compute the discharge Q_{id_r} with the relation (8). The same steps are used for parameters C_{inf_r} and C_{sup_r} to obtain the domain validity boundaries of the OM: $[Q_{inf_r}; Q_{sup_r}]$.

$$Q_{id_r} = \frac{\sqrt{JKS^{\frac{5}{3}}}}{P^{\frac{2}{3}}} .$$
 (8)

Finally, the celerity and diffusion coefficients C_{id_r} and D_{id_r} (5), and the transfer function parameters w_1 , w_2 and τ (6) are computed according to the discharge Q_{id_r} . These parameters allow for the computation and the selection of the transfer delays of each OM. This is described in the next section.

4 Transfer delay identification

The hydraulic systems consist of several reaches, *i.e.* a part between two measurement points (*see* Figure 5.*a*), each reach being composed of Open-Channel Reach Section (OCRS), *i.e.* a part between two gates, or between a measurement point and a gate or between a gate and a measurement point. Thus, the reach dynamics are modelled with a concurrent Hybrid Automaton cHA (*see* Figure 5.*b*) composed of several HA defined for each OCRS. This representation is directly inspired from the concurrent hybrid automata proposed in [5, 6]. In the study case, the cHA is deterministic. The input of the first automaton HA_{o_i} of the first OCRS following M_i is the discharge measured on M_i . The input of the second automaton, HA_{o_i+1} is the discharge downstream HA_{o_i} minus q_{n_i} , the discharge setpoint assigned to the gate between this two OCRS.



Figure 5: (a) A canal reach and (b) its modelling by concurrent hybrid automaton (cHA).

The OCRS dynamics (*see* Figure 6.*a*) are modelled using the multimodelling method described in the previous section, and are represented by a HA (*see* Figure 6.*b*). Each state corresponds to one OM identified as transfer function F_l given by the relation (6). The transition conditions are defined according to the upstream discharge Q_o and the l_{th} OM boundaries Q_{inf_l} and Q_{sup_l} .



Figure 6: (a) OCRS with index o and (b) its modelling by Hybrid Automaton (HA).

For each OM, the transfer delay t_r is obtained from the step response of the corresponding transfer function. It is chosen as the time value for which Π_Q percent of step is reached. The percentage Π_Q can be tuned from simulation. In the next section, the HCA strategy is used to valorize water quantities of a hydraulic system subjected to large operating conditions.

OCRS	B[m]	f	X[m]	J [rad]	$Q_{min} [m^3/s]$	$Q_{max} [m^3/s]$
1	5.73	0.79	204	7.10^{-4}	0.8	10
2	5.09	0.96	702	7.10^{-4}	0.8	9
3	5.21	0.95	562	6.10^{-4}	0.7	7
4	3.72	0.94	1360	5.10^{-4}	0.6	5

Table 2: Geometrical characteristics of each OCRS.

5 Simulation results

The effectiveness of the proposed strategy is shown by simulation on the first reach of the Neste canal located in Gascogne, a french southwestern region. It is composed of one measurement point M_1 , three gates G_1 to G_3 and one output considered as a non-controlled gate G_4 (see Figure 7). This canal reach is composed of four OCRS with trapezoidal profile characterized by the bottom width B, the average fruit of the banks f, the profile length X and the reach slope I (see Figure 8). The geometrical characteristics and operating conditions of each OCRS are detailed in Table 2. The fourth OCRS, between G_3 and G_4 , is not modelled, because gate G_4 is not locally controlled. In the case of a trapezoidal profile, celerity and diffusion coefficients C and D are expressed by the following relation:



Figure 7: First reach of the Neste canal.

$$\begin{cases} C = \frac{Q}{L^2} \left[-f + \frac{L}{3} \left(\frac{2B}{P_z} + \frac{5L}{S} - \frac{2}{z} \right) \right] \\ D = \frac{Q}{2LJ} \end{cases}, \tag{9}$$

where L = B + 2fz, $S = zB + fz^2$, $P = B + 2z\sqrt{1 + f^2}$.



Figure 8: Geometrical characteristics of a trapezoidal profile.

The multimodelling steps which are carried out with $\Pi_C = 15 \%$ and $\Delta_C = 0.1$, lead to the determination of three OM for each OCRS. Their corresponding transfer function parameters are given in Table 3. The transfer delays t_r are computed with a value $\Pi_Q = 63 \%$. This value, chosen by simulation, leads to the best water quantity valorization.

OCRS	Q	$Q_{min} [m^3/s]$	$Q_{max} [m^3/s]$	<i>w</i> ₁	<i>w</i> ₂	τ	$t_r[s]$
	1.6	0.8	2.4	161	0	0	160
1	3.2	1.9	5.2	128	0	0	130
	7.7	4.3	10	100	0	0	100
	1.4	0.8	2.2	424	24331	145	575
2	3	1.7	4.9	364	0	89	450
	7.4	4.1	9	355	0	0	355
	1.2	0.7	1.9	377	0	129	505
3	2.4	1.5	4	357	0	29	385
	5.8	3.2	7	320	0	0	320

Table 3: Multiple models of each OCRS.

The Neste canal is supplied with water corresponding to an objective discharge equal to $7 m^3/s$. The objective discharges and the weights of each gate are displayed in Table 4. The canal is subjected to strong withdrawals of $3 m^3/s$ and $4.5 m^3/s$ upstream to M_1 (see Figure 9.a). This scenario was selected among several simulated scenarii, because it reveals accurately the inversion phenomenon of the discharge tendency. The HCA strategy goals consist in the allocation of the water resource amongst the gates according to their weights, and in the minimization of the discharge discrepancy at gate G_4 . The detection and control periods are selected as $T_e = 12 s$ and $T_c = 120 s$. In Figure 9, the simulation results are shown in continuous line when the transfer delay selection method is used, and in dashed line when the transfer delays are fixed to 100 s for the first OCRS, to 355 s for the second and to 320 s for the third. These transfer delay values are selected according to the operating point of each OCRS, *i.e.* $7 m^3/s$, $5 m^3/s$ and $4 m^3/s$. They correspond to the third OM of each OCRS.



Figure 9: Discharge Q_{M_1} (continuous line) and objective discharge Q_{M_1obj} (dotted line) (*a*), resource states (*b*), setpoints assigned q_j (continuous line when the delay selection method is used, dashed line in other case) and objective discharge q_{jobj} (dotted line) to G_1 (*c*), G_2 (*d*), G_3 (*e*) and discharge at G_4 (*f*).

Table 4: Gate objective discharges q_{jobj} , gate weights λ_j and μ_j , and minimum and maximum discharges $q_{j_{min}}$ and $q_{j_{max}}$.

Gate	G_1	G_2	G_3	G_4
$q_{jobj} [m^3/s]$	2	1	2	2
λ_j	10	10	4	—
μ_j	10	4	10	—
$q_{j_{min}} \left[m^3/s \right]$	0.02	0.1	0.02	0.15
$q_{j_{max}} [m^3/s]$	3.6	4.5	3.5	3

Table 5: Criteria computed when the transfer delay selection method is or not used.

Criterion	$\min(q_4 \ [m^3/s])$	$\max(q_4 \ [m^3/s])$	$V[m^3]$
With selection method	1.9778	2.0451	541
Without selection method	1.9763	2.0455	602

Figure 9 displays the discharges Q_{M_1} in (a), the corresponding discharge states in (b), the setpoint assigned at gate G_1 in (c), G_2 in (d), G_3 in (e) and the resulting discharge at G_4 in (f). The resource in lack measured on M_1 is allocated on gates G_1 and G_3 , as long as their setpoints are upper than their respectively minimum discharge characteristics $q_{j_{min}}$, otherwise it is allocated on gate G_2 (see Figures 9.c, 9.d and 9.e). Thus, the gates G_1 and G_3 are controlled between the 1st and 4th hours, and the gate G_2 between the 4th and 7th hours.

During all the simulation time, the discharge on G_4 is close to the objective value of $2m^3/s$ (see Figure 9.*f*). However, when the transfer delay selection method is not used, the setpoints are always assigned too early. Consequently at G_4 , the discharge is in excess when the water resource decreases on M_1 , and the discharge is in lack when the water resource increases on M_1 . The tendency of Q_{M_1} discharge is inverted at G_4 the end of the canal reach.

The use of the transfer delay selection method improves the performances of the HCA strategy and maintains the tendency. The maximum and minimum discharges reached at G_4 and the water volume V which was not allocated, are displayed in Table 5. The maximum discharge discrepancy at G_4 corresponds to 2.26 % of the objective discharge q_{4obj} when the transfer delay selection method is used and to 2.28 % in the other case.

6 Conclusion

The HCA strategy is adapted to valorize the water resource by allocation and setpoint assignment of open-surface hydraulic system submitted to strong disturbances. A multimodelling method is proposed to identify by a determined number of linear models the open-surface hydraulic systems. Then, a transfer delay selection method is proposed to take into account variable transfer delays by the selection of the right setpoint assignment date according to the system dynamics and to the measured discharge. Finally, the HCA strategy performances are shown by simulation on the first reach of the Neste canal subjected to large operating conditions and to strong disturbances. The study of control stability proof of the HCA strategy is a future goal.

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