

## The Rest Mass of the Electron Neutrino from the Electron Capture of $^{163}\text{Ho}$

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The mass of the electron antineutrino has been studied for a long time using the tritium  $\beta$ -ray spectrum, while the mass of the electron neutrino ( $m_{\nu_e}$ ) has been recently investigated using electron capturing isotopes including  $^{163}\text{Ho}$ ,  $^{193}\text{Pt}$  and so on.<sup>1-3)</sup> In the latter there are two ways to measure  $m_{\nu_e}$ ; one proposed by De Rújula<sup>4)</sup> which is essentially based on three-body phase space in radiative electron capture process, and another which utilizes the  $m_{\nu_e}$ -dependence of the electron capture rate as discussed by Bennett et al.<sup>5)</sup> In both cases, electron capturing nuclei having a low Q value seem to be favorable. A nucleus that decays by electron capture with the lowest Q value of any known  $\beta$ -decay process is holmium-163, which was discovered by the Princeton group in 1968.

Considerations of the intensity of internal bremsstrahlung spectra at electron capture in  $^{163}\text{Ho}$  seem to indicate that the first approach is rather difficult for measuring  $m_{\nu_e}$ . The present report describes our recent measurement of the mass of the electron neutrino using electron capture in  $^{163}\text{Ho}$ , which falls under the second category.

If  $S_p^{163}\text{Ho}$  stands for an M X-ray spectrum from  $^{163}\text{Ho}$ , where the number of photons per atom per second is plotted as a function of the energy of the photons, we then have

$$\begin{aligned} S_p(x)^{163}\text{Ho} &= (1/N) \times [(dN_{M_1}/dt)S_{M_1}(x) + (dN_{M_2}/dt)S_{M_2}(x)] \\ &= \lambda_{M_1} S_{M_1}(x) + \lambda_{M_2} S_{M_2}(x), \end{aligned} \quad (1)$$

where  $S_{M_i}(x)$  ( $i=1,2$ ) is the M X-ray spectrum when there is one vacancy in the  $M_i$  subshell only;  $x$  is the channel number;  $dN_{M_i}/dt$  ( $i=1,2$ ) is the number of vacancies produced per second in the  $M_i$  subshell in the decay  $^{163}\text{Ho} \xrightarrow{\text{EC}} ^{163}\text{Dy}$ ;

$N$  is the total number of  $^{163}\text{Ho}$  atoms in a  $^{163}\text{Ho}$  source;  $\lambda_{M_i}$  ( $i=1,2$ ) is the partial  $M_i$ -capture decay constant.

Eq. (1) tells us that when we reconstruct  $S_p^{163}\text{Ho}$  using the  $S_{M_1}$  and  $S_{M_2}$  spectra, the coefficients of  $S_{M_1}$  and  $S_{M_2}$  used in the reconstruction correspond to  $\lambda_{M_1}$  and  $\lambda_{M_2}$ , respectively.

The photon spectrum from the  $^{163}\text{Ho}$  source was measured in vacuum with a Si(Li) detector (ORTEC) having a Be window 0.3 mm thick (nominal). The production of  $^{163}\text{Ho}$  using the  $^{164}\text{Dy}(p,2n)$  reaction and the preparation of the  $^{163}\text{Ho}$  source are described in our previous paper.<sup>2)</sup> The whole apparatus was shielded with lead 100 mm thick. The counting time was 28.89 d. The geometry of the Si(Li) detector, including the effective area of a silicon crystal and the solid angle, was carefully measured using several radioactive sources. The thickness of the Be window of the Si(Li) detector was also checked by comparing a photon spectrum measured using this detector with that measured using a windowless Si(Li) detector (HORIBA, Japan).<sup>6)</sup>

The total number of  $^{163}\text{Ho}$  atoms in the  $^{163}\text{Ho}$  source,  $N$ , was measured with isotope-dilution mass spectrometry to be  $N = (6.481 \pm 0.012) \times 10^{15}$  atoms, which is in good agreement with the previous value determined by the PIXE method<sup>5)</sup> within experimental uncertainties.

The number of photons included in the  $S_{M_1}$  and  $S_{M_2}$  are represented by

$$\begin{aligned}
 S_{M_1}: & \omega_1 + f_{12}\omega_2 + (f_{13} + f_{12}f_{23})\omega_3 \\
 & + (f_{14} + f_{12}f_{24} + f_{13}f_{34} + f_{12}f_{23}f_{34})\omega_4 \\
 & + (f_{15} + f_{12}f_{25} + f_{13}f_{35} + f_{14}f_{45} + f_{12}f_{23}f_{35} \\
 & + f_{12}f_{24}f_{45} + f_{13}f_{34}f_{45} + f_{12}f_{23}f_{34}f_{45})\omega_5, \quad (2)
 \end{aligned}$$

$$\begin{aligned}
 S_{M_2}: & \omega_2 + f_{23}\omega_3 + (f_{24} + f_{23}f_{34})\omega_4 \\
 & + (f_{25} + f_{23}f_{35} + f_{24}f_{45} + f_{23}f_{34}f_{45})\omega_5, \quad (3)
 \end{aligned}$$

where  $\omega_i$  ( $i=1, \dots, 5$ ) is the  $M_i$  subshell fluorescence yield and  $f_{ij}$  is the Coster-Kronig coefficient for vacancy transition from the  $M_i$  subshell to the  $M_j$  subshell. When the total level width of the  $M_i$  subshell is  $\Gamma_i$ , the fluorescence yield for this subshell is defined as

$$\omega_i = \sum_j \gamma_{ij} / \Gamma_i,$$

where  $\gamma_{ij}$  is the partial radiative width corresponding to the electron transition from the  $X_j$  subshell to the  $M_i$  subshell, and  $X$  denotes shells higher than the  $M$  shell.

Since no relativistic calculation of nonradiative transition probabilities for dysprosium has been reported so far, we estimated the values of  $f_{ij}$  and  $\Gamma_i$  from the nonrelativistic values of McGuire<sup>7)</sup> and the

relativistic values of Chen et al.<sup>8,9)</sup> for holmium and ytterbium. The results are shown in Table 1. The partial radiative width  $\gamma_{ij}$  was taken from the relativistic calculations by Mukoyama and Adachi.<sup>10)</sup>

The  $S_{M_1}(x)$  and  $S_{M_2}(x)$  spectra were constructed from various characteristic X-ray lines corresponding to  $\gamma_{ij}$  in Eqs. (2) and (3) using response functions of the Si(Li) detector used in the measurement of the photon spectrum from the  $^{163}\text{Ho}$  source. The response functions were measured using monochromatic photons from the undulator beam line of the 2.5 GeV Electron Storage Ring at the Photon Factory in KEK.

When we tried to reconstruct the  $S_p^{163}\text{Ho}$  spectrum using the theoretical  $S_{M_1}(x)$  and  $S_{M_2}(x)$  spectra mentioned above, it was found that there were some discrepancies around the 1.3 keV and 2.0 keV peaks. Therefore, the non-linear least-squares method was applied to minimize the  $\chi^2$ -value for fitting Eq. (1), taking three radiative widths,  $\gamma_{M_5N_7}$ ,  $\gamma_{M_4N_6}$  and  $\gamma_{M_1O_{2,3}}$ , as unknowns in addition to  $\lambda_{M_1}$  and  $\lambda_{M_2}$ , as shown in Fig. 1.

The results are

$$\begin{aligned}\lambda_{M_1} &= (0.9740 \pm 0.0041) \times 10^{-12} \text{ s}^{-1}, \\ \lambda_{M_2} &= (0.0817 \pm 0.0035) \times 10^{-12} \text{ s}^{-1},\end{aligned}$$

with

$$\begin{aligned}\gamma_{M_5N_7} &= 1.749 \times 10^{-3} \text{ eV}, \\ \gamma_{M_4N_6} &= 1.340 \times 10^{-3} \text{ eV}, \\ \gamma_{M_1O_{2,3}} &= 2.159 \times 10^{-3} \text{ eV}.\end{aligned}$$

It is worth mentioning that the  $S_{M_1}$  and  $S_{M_2}$  thus obtained, are compatible with those deduced from fluorescence spectrum measurements on dysprosium using monochromatic photon beams at the Photon Factory in KEK.<sup>6)</sup>

On the other hand the half-life of the  $^{163}\text{Ho}$  nucleus was determined by measuring the production rate of  $^{163}\text{Dy}$  due to electron capture in  $^{163}\text{Ho}$  with isotope-dilution mass spectrometry<sup>11)</sup> as initially done by Baisden et al.<sup>12)</sup> Our result was

$$T_{1/2} = 4569 \pm 27 \text{ yr (68\% CL)}$$

or

$$\lambda_t = (4.807 \pm 0.028) \times 10^{-12} \text{ s}^{-1},$$

which is in excellent agreement with the value of Baisden et al.<sup>12)</sup>

Using the experimental values of  $\lambda_{M_1}$ ,  $\lambda_{M_2}$  and  $\lambda_t$  thus obtained as three constrains,  $m_{\nu e}$ , the Q-value and the nuclear matrix element,  $|m_N|^2$ , for the decay of  $^{163}\text{Ho}$ , were determined from the formula of the electron capture rate as follows:

$$m_{\nu_e} = 205^{+345}_{-205} \text{ eV} , \quad Q = 2.70^{+0.13}_{-0.02} \text{ keV} ,$$

$$|m_N|^2 = 0.0409^{+0.0033}_{-0.0016}$$

or

$$\log ft = 4.98^{+0.04}_{-0.02} .$$

A summary of the final results for  $m_{\nu_e}$  and the Q-value is shown in Fig. 2.

Therefore we conclude

$$m_{\nu_e} < 550 \text{ eV} \quad (68\% \text{ CL}).$$

In addition it should be noted that our estimation of the  $\log ft$  value lies in between the value of the CERN-Aarhus group<sup>1)</sup> and that of the Princeton-Livermore group.<sup>12)</sup>

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Table 1. M-shell Coster-Kronig coefficients  $f_{ij}$   
and level width  $\Gamma_i$  for dysprosium.

$f_{ij}$	value	$\Gamma_i$	value(eV)
$f_{12}$	0.307	$\Gamma_1$	14.94
$f_{13}$	0.599	$\Gamma_2$	9.04
$f_{14}$	0.085	$\Gamma_3$	9.27
$f_{15}$	0.116	$\Gamma_4$	1.81
		$\Gamma_5$	1.24
$f_{23}$	0.091		
$f_{24}$	0.665		
$f_{25}$	0.141		
$f_{34}$	0.149		
$f_{35}$	0.747		
$f_{45}$	0.348		

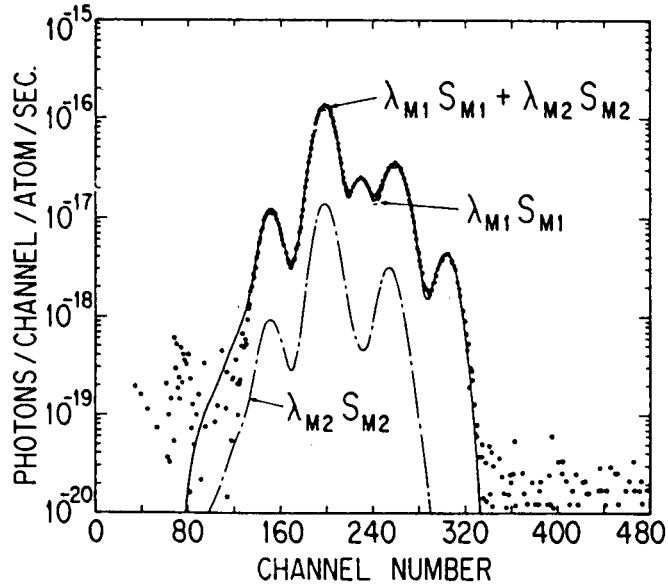


Fig. 1. Reconstruction of the  $S_p^{163}\text{Ho}$  spectrum using the  $S_{M_1}$  and  $S_{M_2}$  spectra. The solid curve, the broken curve and the dot-dashed curve represent  $\lambda_{M_1} S_{M_1} + \lambda_{M_2} S_{M_2}$ ,  $\lambda_{M_1} S_{M_1}$  and  $\lambda_{M_2} S_{M_2}$ , respectively. Closed circles represent experimental data of  $S_p^{163}\text{Ho}$ .

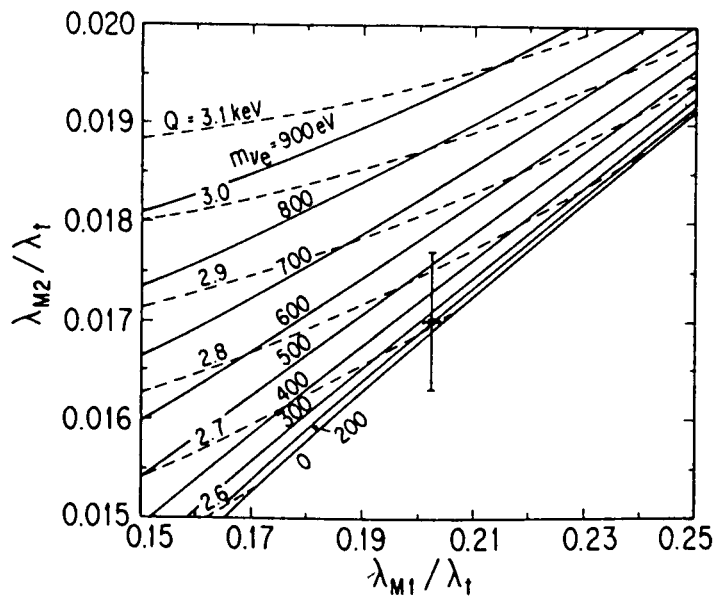


Fig. 2. Summary of the final results for  $m_{\nu_e}$  and  $Q$ -value.