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# Light polarization characteristics of *m*-plane $Al_xGa_{1-x}N$ films suffering from in-plane anisotropic tensile stresses

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Polarization characteristics of the near-band-edge optical transitions in *m*-plane Al<sub>x</sub>Ga<sub>1-x</sub>N epilayers suffering from anisotropic stresses were quantified. The epilayers were grown by both ammonia-source molecular beam epitaxy and metalorganic vapor phase epitaxy methods on an *m*-plane freestanding GaN substrate. The light polarization direction altered from  $E \perp c$  to  $E \parallel c$  at the AlN molar fraction, *x*, between 0.25 and 0.32, where *E* is the electric field component of the light and  $\perp$  and  $\parallel$  represent perpendicular and parallel, respectively. To give a quantitative explanation for the result, energies and oscillator strengths of the exciton transitions involving three separate valence bands were calculated as functions of strains using the Bir–Pikus Hamiltonian. The calculation predicted that the lowest energy transition ( $E_1$ ) is polarized to the *m*-axis normal to the surface ( $X_3$ ) for  $0 < x \le 1$ , meaning that  $E_1$  emission is principally undetectable from the surface normal for any in-plane tensile strained Al<sub>x</sub>Ga<sub>1-x</sub>N. The polarization direction of observable surface emission was predicted to alter from *c*-axis normal ( $X_1$ ) to *c*-axis parallel ( $X_2$ ) for the middle energy transition ( $E_2$ ) and  $X_2$  to  $X_1$  for the highest energy transition ( $E_3$ ) between x=0.25 and 0.32. The experimental results were consistently reproduced by the calculation. © 2010 American Institute of *Physics*. [doi:10.1063/1.3282705]

#### I. INTRODUCTION

Wurtzite  $Al_xGa_{1-x}N$  alloys are an attractive material for realizing ultraviolet light emitters and high power high frequency electronic devices, as their bandgap energies range from 3.43 eV (x=0) to 6.01 V (x=1) and they are principally a hard material. Recently, a 210 nm electroluminescence has been demonstrated for c-plane AlN p-i-n homojunction light-emitting diodes (LEDs),<sup>1</sup> although the external quantum efficiency  $(10^{-6}\% \text{ at } 210 \text{ nm})$  was extremely lower than those of conventional blue or violet InGaN LEDs. One of the major reasons for this is the increase in threading dislocation (TD) and point defect densities<sup>2</sup> with the increase in AlN molar fraction x. Another reason is the reduction in oscillator strength of electron-hole pairs in quantum wells (QWs) due to the quantum-confined Stark effects (QCSEs), which are caused by the spontaneous and piezoelectric polarization discontinuity at the c-plane heterointerfaces. To avoid the QC-SEs in (Al, In, Ga)N heterostructures, epitaxial growths on nonpolar orientations such as *a*-plane (11 $\overline{2}0$ ) or *m*-plane  $(10\overline{10})$  have been attracting attention.<sup>3-6</sup> Recently, good performance *m*-plane InGaN LEDs<sup>7,8</sup> and LDs<sup>9,10</sup> have been fabricated on the low TD density freestanding (FS)-GaN substrates,<sup>11</sup> which were sliced from a subcentimeter-thick *c*-plane FS-GaN grown by halide vapor phase epitaxy. However, for nonpolar epitaxy of (Al, In, Ga)N alloys, in-plane lattice and thermal mismatches between the epilayer and the substrate are anisotropic along parallel and normal to the c-axis, which gives rise to anisotropic strains in the pseudomorphic epitaxial films. Therefore, in order to optimize nonpolar  $Al_xGa_{1-x}N$  LED structures, oscillator strengths f of three interband optical transitions must be quantified as functions of light polarization direction and strains.

The effects of biaxial isotropic strain on excition resonance energies have been investigated for c-plane GaN (Refs. 12–14) and *c*-plane AlN.<sup>15</sup> Because the sign of the crystal-field splitting of AlN is negative, valence band (VB) ordering of strain-free AlN is  $\Gamma_7$ ,  $\Gamma_9$ , and  $\Gamma_7$  in order of decreasing electron energy. On the other hand, the ordering is  $\Gamma_0$ ,  $\Gamma_7$ , and  $\Gamma_7$  for GaN and InN. Consequently, the allowed light polarization direction for the topmost VB of Al<sub>x</sub>Ga<sub>1-x</sub>N alters from  $E \perp c$  to  $E \parallel c$  with the increase in x, where E is the electric field of the light and  $\perp$  and  $\parallel$  represent perpendicular and parallel, respectively. Ikeda et al.<sup>15</sup> have obtained the VB parameters of AlN through the theoretical fitting of exciton transition energies of *c*-plane AlN films as a function of biaxial strain. As a result, they have predicted the critical x (anticrossing point) for the A and C transitions as 0.125.

With respect to the effect of anisotropic strains, optical polarization properties of (Al, In, Ga)N films and QWs of various orientations have been investigated.<sup>16–26</sup> Bhatta-charyya *et al.*<sup>26</sup> have very recently calculated the light polarization characteristics of the transitions involving three separate VBs of *m*-plane  $Al_xGa_{1-x}N$  on GaN, which suffer form anisotropic tensile stresses. They have estimated the anticrossing point as x=0.10, and predicted that the lowest energy transition of  $Al_xGa_{1-x}N$  is predominantly polarization parallel to the substrate normal.

In this paper, results of polarized cathodoluminescence (CL) measurement on *m*-plane  $Al_xGa_{1-x}N$  epilayers grown

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on the *m*-plane FS-GaN substrate are shown. All of the epilayers grown by ammonia-source molecular beam epitaxy (NH<sub>3</sub>-MBE) and metalorganic vapor phase epitaxy (MOVPE) suffer from in-plane anisotropic tensile stresses. The results are quantitatively explained by calculating transition energies and oscillator strengths of excitonic transitions involving three separate VBs as functions of in-plane strains. For the calculation, Bir–Pikus Hamiltonian<sup>27</sup> was used without fitting parameters.

## **II. EXPERIMENTAL DETAILS**

Samples investigated were approximately 100 to 400nm-thick *m*-plane  $Al_xGa_{1-x}N$  epilayers grown on an 1-µm-thick GaN homoepitaxial layer, which was grown on the *m*-plane FS-GaN substrates.<sup>11</sup> The substrates were sliced form approximately 1-cm-thick c-plane FS-GaN grown by halide vapor phase epitaxy on a Al<sub>2</sub>O<sub>3</sub> substrate.<sup>11</sup> The TD and stacking fault densities were lower than  $5 \times 10^{6}$  cm<sup>-2</sup> and  $1 \times 10^3$  cm<sup>-1</sup>, respectively.<sup>11</sup> The NH<sub>3</sub>-MBE of *m*-plane Al<sub>r</sub>Ga<sub>1-r</sub>N epilayers  $(0 \le x \le 0.70)$  were carried out at 870-970 °C using metallic Ga (7N) and Al (6N) sources. The beam equivalent pressures of metallic Ga and NH<sub>3</sub> were  $(2.1-4.0) \times 10^{-5}$  and  $(1.3-4.1) \times 10^{-2}$  Pa, respectively. The growth details will be found in Ref. 28. A 150-nm-thick Al<sub>0.73</sub>Ga<sub>0.27</sub>N and approximately 2.1-µm-thick AlN epilayers were grown at 1120 °C on the same m-plane FS-GaN substrates by MOVPE. The reactor pressure was  $2.02 \times 10^4$  Pa. Trimethylaluminum, triethylgallium, and NH<sub>3</sub> were used as the precursors.

The Al<sub>x</sub>Ga<sub>1-x</sub>N films of  $0 \le x \le 0.32$  were confirmed by x-ray reciprocal space mapping (RSM) method to grow coherently on the base GaN. The films of x > 0.58 were incompletely relaxed because of the lattice mismatch against the GaN substrate.<sup>28</sup> Accordingly, two in-plane and one out-ofplane strains and x values were obtained from the in-plane and out-of-plane lattice parameters measured by the x-ray RSM measurement, taking the degree of lattice relaxation into account.<sup>28</sup> In-plane tensile strains increased with x for the pseudomorphic (coherently grown) films, as shown in Fig. 1(a). Conversely, the strains were gradually relaxed by the partial relaxation for x > 0.32. For the quantitative discussion of polarization properties, we define the notations for the three axes:  $X_1$  (perpendicular to the *c*-axis in the growth plane),  $X_2$  (parallel to the *c*-axis in the growth plane), and  $X_3$ (normal to the growth plane), as shown in Fig. 1(b).

Steady-state CL was excited with an electron beam operated at 3.0 kV. The probe current density was 1.0  $\times 10^{-2}$  A/cm<sup>2</sup> at sample. The emission was dispersed by a 30-cm-focal-length grating monochromator, and detected using a multichannel charge-coupled device. A Glan– Thompson prism polarizer was used for the polarized CL measurement. Polarized near-band-edge (NBE) CL spectra at 12 K of the *m*-plane Al<sub>x</sub>Ga<sub>1-x</sub>N films are shown as a function of *x* in Fig. 2(a). The intensities are normalized to that of stronger polarization direction (X<sub>1</sub> or X<sub>2</sub>) for each *x*. The entire spectra shifted to the higher energy with increasing *x*, although some of them exhibited double emission peaks. As shown, the light polarization direction altered from X<sub>1</sub> to X<sub>2</sub>



FIG. 1. (Color online) (a) Strain components  $\epsilon_{X_1X_1}$ ,  $\epsilon_{X_2X_2}$ , and  $\epsilon_{X_3X_3}$  of the *m*-plane Al<sub>x</sub>Ga<sub>1-x</sub>N films as a function of AlN molar fraction *x*. (b) Schematic diagram of the notations of three axes. The films of  $x \le 0.70$  were grown by NH<sub>3</sub>-MBE and  $x \ge 0.73$  were grown by MOVPE.

between x=0.25 and 0.32. The value of polarization ratio  $\rho$  was defined as  $(I_{X_1}-I_{X_2})/(I_{X_1}+I_{X_2})$ , where  $I_{X_2}$  and  $I_{X_1}$  are the spectrally integrated CL intensities of the NBE emission. The values are plotted by closed circles in Fig. 2(b).



FIG. 2. (Color online) (a) Polarized CL spectra at 12 K of *m*-plane  $Al_xGa_{1-x}N$  epilayers grown on the FS *m*-plane GaN substrates. (b) Polarization ratios, which are defined as  $(I_{X_1}-I_{X_2})/(I_{X_1}+I_{X_2})$ , of the  $Al_xGa_{1-x}N$  films as a function of AlN molar fraction *x*. Corresponding values calculated using the relative oscillator strengths are also shown. The films of  $x \le 0.70$  were grown by NH<sub>3</sub>-MBE and  $x \ge 0.73$  were grown by MOVPE.

## **III. THEORETICAL ANALYSIS**

To quantitatively explain the experimental findings, the energies and oscillator strengths of the interband transitions involving three separate VBs were calculated using the Bir–Pikus Hamiltonian,<sup>27</sup> taking the anisotropic strains into account. At the  $\Gamma$  point, the states at the conduction band minimum (CBM) have an atomic *s* orbital with wave functions of  $|S\rangle$  symmetry. The three VB maximum (VBM) states have atomic *p* orbitals with wave functions of a combination of  $|X\rangle$ ,  $|Y\rangle$ , and  $|Z\rangle$  symmetries. For simplicity, excitonic effects were neglected in the calculation. The Hamiltonian for the strain dependence of VB is given by the following  $6 \times 6$  matrix

$$H = \begin{bmatrix} F & 0 & -H^* & 0 & K^* & 0 \\ 0 & G & \Delta & -H^* & 0 & K^* \\ -H & \Delta & \lambda & 0 & I^* & 0 \\ 0 & -H & 0 & \lambda & \Delta & I^* \\ K & 0 & I & \Delta & G & 0 \\ 0 & K & 0 & I & 0 & F \end{bmatrix},$$

where

$$\begin{split} F &= \Delta_1 + \Delta_2 + \lambda + \theta, \\ G &= \Delta_1 - \Delta_2 + \lambda + \theta, \\ H &= i(A_6k_zk_+A_7k_+ + D_6\epsilon_{z+}), \\ I &= i(A_6k_zk_+ - A_7k_+ + D_6\epsilon_{z+}), \\ K &= A_5k_+^2 + D_5\epsilon_+, \\ \lambda &= A_1k_z^2 + A_2k_\perp^2 + D_1\epsilon_{zz} + D_2(\epsilon_{xx} + \epsilon_{yy}), \\ \theta &= A_3k_z^2 + A_4k_\perp^2 + D_3\epsilon_{zz} + D_4(\epsilon_{xx} + \epsilon_{yy}), \quad \Delta = \sqrt{2}\Delta_3, \\ k_\perp^2 &= k_x^2 + k_y^2, \quad k_+ = k_x + ik_y, \\ \epsilon_{z+} &= \epsilon_{xz} + i\epsilon_{yz}, \quad \epsilon_+ = \epsilon_{xx} - \epsilon_{yy} + 2i\epsilon_{xy}. \end{split}$$

The parameters  $D_j$  (j=1-6) denote the deformation potential constants for the VB and  $A_j$  (j=1-7) are Luttinger parameters, and  $\epsilon_{\ell m}$  and  $k_\ell(\ell, m=X_1, X_2, X_3)$  are the strain and wave-vector components, respectively. Here we assume that nondiagonal elements of the strain tensor are zero.  $\Delta_1 = \Delta_{\rm sr}$  is the crystal field splitting, while  $3\Delta_2 = 3\Delta_3 = \Delta_{\rm so}$  are the spinorbit splitting under quasicubic approximation. The basis functions of Bir–Pikus Hamiltonian are  $(1/\sqrt{2})|X+iY, \alpha\rangle$ ,  $(1/\sqrt{2})|X+iY, \beta\rangle$ ,  $(1/\sqrt{2})|X-iY, \alpha\rangle$ ,  $(1/\sqrt{2})|X-iY, \beta\rangle$ ,  $|Z, \alpha\rangle$ , and  $|Z, \beta\rangle$ . Here  $|\alpha\rangle$  and  $|\beta\rangle$  denote the spin-wave functions corresponding to up spin and down spin. The method described here is universal, and Bhattacharyya *et al.*<sup>26</sup> have also used the same approach to calculate the electronic states of *m*-plane (Al, In, Ga)N alloys.

The exciton transition energies are obtained from the band energies and exciton binding energy

TABLE I. Material parameters of GaN and AlN.

	GaN <sup>a</sup>	AlN <sup>b</sup>	
$E_{g}$ at 10 K (eV)	3.504	6.095	
$\Delta_{cr} = \Delta_1 \text{ (meV)}$	16	-152.4	
$\Delta_{so} = 3\Delta_2 = \Delta_3 \text{ (meV)}$	22	18.9	
$m_{\parallel}^e/m_0$	0.2	0.32	
$m_{\perp}^{e}/m_{0}$	0.18	0.28	
$A_2$	-0.91	-0.28	
$A_4$	-2.83	-1.84	
C <sub>11</sub> (GPa)	390	396	
$C_{12}$ (GPa)	145	137	
$C_{13}$ (GPa)	106	120	
$D_1$ (eV)	-41.4	-17.2	
$D_2 (eV)$	-33.3	7.9	
$D_3$ (eV)	8.2	8.19	
$D_4$ (eV)	-4.1	-4.1	
$D_5 (eV)$	-4.7	-3.4	

<sup>a</sup>Reference 14. <sup>b</sup>Reference 15.

$$E_{j} = E^{*} + E^{c} - E_{j}^{v} - E_{ex}^{b}, \qquad (2)$$

where  $E^* = E_g + \Delta_1 + \Delta_2$ . The parameters  $E_g$ ,  $E^c$ ,  $E^v_j$ , and  $E^b_{ex}$  are the bandgap energy, the CBM energy, the VBM energies, and the exciton binding energy, respectively. The  $E^b_{ex}$  values for the *A*, *B*, and *C* transition were set identical to 26 meV (Ref. 14) for GaN and 51.3 meV for AlN.<sup>29</sup>

The oscillator strength components for the transitions were obtained from momentum matrix elements  $|\langle \Psi^{CB}|p_{\ell}|\Psi^{VB}\rangle|^2$  with  $\ell = x$ , y, and z. Here,  $\langle \Psi^{CB}| = \langle S|$  and  $|\Psi^{VB}\rangle = a_1|X\rangle + a_2|Y\rangle + a_3|Z\rangle$  represent the orbital parts of the CB and VB basis functions, respectively. The coefficients  $a_j$ were obtained by determining the eigenvectors of Hamiltonian. The *relative* values of  $|\langle S|p_x|X\rangle|^2$ ,  $|\langle S|p_y|Y\rangle|^2$ , and  $|\langle S|p_z|Z\rangle|^2$  are set unity under the quasicubic approximation  $\sum_{i=1}^{3} f_{i,\beta} = 1$ . The calculations started herein were carried out exclusively at  $\mathbf{k} = 0$ , meaning that the  $6 \times 6$  matrix was effectively treated as  $3 \times 3$ .

For the practical calculation on  $Al_xGa_{1-x}N$  alloy films, the material parameters of end-point compounds, namely GaN and AlN, were taken from the literature, as shown in Table I. The parameters for the alloys were assumed to obey the Vegard's law and the bowing parameter for the bandgap energy of strain-free  $Al_xGa_{1-x}N$  was chosen as 0.82 eV.<sup>30</sup> We use energy notations  $E_1$ ,  $E_2$ , and  $E_3$  hereafter because the crystal symmetry of the  $Al_xGa_{1-x}N$  films suffering from anisotropic stresses is no longer  $C_{6w}^4$ .

The calculated relative oscillator strengths for the three interband transitions in Al<sub>0.03</sub>Ga<sub>0.97</sub>N alloy are shown as functions of  $\epsilon_{X_1X_1}$  and  $\epsilon_{X_2X_2}$  by gray-scale contour plots in Fig. 3. For each  $E_1$ ,  $E_2$ , and  $E_3$  transition, the measured strain coordinate ( $\epsilon_{X_1X_1}$ ,  $\epsilon_{X_2X_2}$ )=(0.08%, 0.13%) is plotted by a closed red circle on the panel exhibiting the calculated predominant polarization direction. As shown, the calculated polarization directions are  $X_3$ ,  $X_1$ , and  $X_2$  in order of decreasing electron energy. The result means that anisotropic strain induces a remarkable change in the electronic band structures: the ordering is already different from those of strainfree GaN. In the case of Al<sub>0.70</sub>Ga<sub>0.30</sub>N alloy with

(1)



FIG. 3. (Color online) Relative oscillator strengths of  $E_1$ ,  $E_2$ , and  $E_3$  transitions for the *m*-plane Al<sub>0.03</sub>Ga<sub>0.97</sub>N film as functions of in-plane strain coordinate ( $\epsilon_{X_1X_1}, \epsilon_{X_2X_2}$ ). Closed circles indicate the experimentally obtained in-plane strain coordinate ( $\epsilon_{X_1X_1}, \epsilon_{X_2X_2}$ )=(0.08%, 0.13%), which are plotted on the respective predominant polarization directions.

 $(\epsilon_{X_1X_1}, \epsilon_{X_2X_2}) = (0.79\%, 0.35\%)$ , the polarization directions are calculated to be  $X_3$ ,  $X_2$ , and  $X_1$  in order of decreasing electron energy, as shown in Fig. 4. As revealed from Figs. 3 and 4, the polarization ordering of  $Al_{0.70}Ga_{0.30}N$  was different from  $Al_{0.03}Ga_{0.97}N$ , and the oscillator strengths of  $Al_{0.70}Ga_{0.3}N$  showed weaker contrast than  $Al_{0.03}Ga_{0.97}N$ . The reason for this will be explained later. Gil and Alemu<sup>18</sup> have reported a theoretical study on the electronic band structure of *m*-plane GaN under anisotropic biaxial strain. They predicted that  $E_1$  and  $E_3$  transitions were  $E \perp c(X_1)$  polarized under large in-plane compressive strain. With respect to  $E_3$ transition, their result differs from our calculated result for AlGaN alloys suffering from biaxial compressive strain (data not shown in this paper, because our AlGaN films basically



FIG. 4. (Color online) Relative oscillator strengths of  $E_1$ ,  $E_2$ , and  $E_3$  transitions as functions of in-plane strain coordinate  $(\epsilon_{X_1X_1}, \epsilon_{X_2X_2})$  for the *m*-plane Al<sub>0.70</sub>Ga<sub>0.30</sub>N film. Closed circles indicate the experimentally obtained in-plane strain coordinate  $(\epsilon_{X_1X_1}, \epsilon_{X_2X_2}) = (0.79\%, 0.35\%)$ , which are plotted on the respective predominant polarization directions.



FIG. 5. (Color online) Calculated  $E_1$ ,  $E_2$ , and  $E_3$  exciton transition energies for the *m*-plane (a)  $Al_{0.03}Ga_{0.97}N$  and (b)  $Al_{0.70}Ga_{0.30}N$  films. The energy difference between  $E_2$  and  $E_1$ ,  $(E_2-E_1)$ , as functions of in-plane strains  $(\epsilon_{X_1X_1}, \epsilon_{X_2X_2})$  for the *m*-plane (c)  $Al_{0.03}Ga_{0.97}N$  and (d)  $Al_{0.70}Ga_{0.30}N$  films. Closed circles indicate respective in-plane strains.

suffered from in-plane tensile strains). The discrepancy might arise from the fact that we did not consider the excitonic effects. However, it is likely that their notation was different<sup>19</sup> from ours so that their *m*-plane would correspond to *a*-plane in our case, which might be the cause for this discrepancy. Similar arguments have been given by Bhatta-charyya *et al.*<sup>26</sup>

The three exciton transition energies calculated for m-plane Al<sub>0.03</sub>Ga<sub>0.97</sub>N and Al<sub>0.70</sub>Ga<sub>0.30</sub>N films under isotropic in-plane strain  $(\epsilon_{X_1X_1} = \epsilon_{X_2X_2})$  are shown in Figs. 5(a) and 5(b), respectively. In case of  $Al_{0.03}Ga_{0.97}N$ , the VB anticrossing immediately takes place when in-plane biaxial tensile strain is introduced. On the contrary, the VB anticrossing gradually takes place with increasing the tensile strain for Al<sub>0.70</sub>Ga<sub>0.30</sub>N. The latter result means that VBs are strongly hybridized, which gives rise to much lower oscillator strength contrast for  $Al_{0.70}Ga_{0.30}N$ , as shown in Fig. 4. The energy differences between  $E_1$  and  $E_2$  bands for the Al<sub>0.03</sub>Ga<sub>0.97</sub>N and Al<sub>0.70</sub>Ga<sub>0.30</sub>N films are shown using contour lines as functions of  $\epsilon_{X_1X_1}$  and  $\epsilon_{X_2X_2}$  in Figs. 5(c) and 5(d), respectively. Similar to Figs. 3 and 4, the measured strain coordinates are plotted by closed black circles. The  $E_2-E_1$  values are predicted to be 6.2 and 106 meV for Al<sub>0.03</sub>Ga<sub>0.97</sub>N and Al<sub>0.70</sub>Ga<sub>0.30</sub>N, respectively. Table II summarizes the polarization directions for  $E_1$ ,  $E_2$ , and  $E_3$  transitions and  $E_2 - E_1$  values calculated for *m*-plane Al<sub>x</sub>Ga<sub>1-x</sub>N suffering from experimentally obtained strain values. As shown,  $E_1$  transition is  $X_3$ -polarized regardless of x. The result means that  $E_1$  (exciton) emission is essentially undetectable from the surface normal. Apart from  $E_1$ , the polarization directions alter from  $X_1$  to  $X_2$  for  $E_2$  emission ( $X_3$  to  $X_2$  for  $E_3$  emission) between x=0.25 and 0.32. Assuming that the experimentally observed CL peaks originate from  $E_2$  and  $E_3$ transitions, the calculated prediction is consistent with the experimental results, as shown in Fig. 2(b). In Fig. 2(b),  $\rho$ 

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TABLE II. Calculated polarization directions for  $E_1$ ,  $E_2$ , and  $E_3$  transitions and energy differences between  $E_1$  and  $E_2$  band  $(E_2-E_1)$ .

x	$E_1$	$E_2$	$E_3$	$\begin{array}{c} E_2 - E_1 \\ (\text{meV}) \end{array}$
0.00	$X_1$	$X_3$	$X_2$	7.7
0.03	$X_3$	$X_1$	$X_2$	6.2
0.12	$X_3$	$X_1$	$X_2$	48.4
0.25	$X_3$	$X_1$	$X_2$	96.9
0.32	$X_3$	$X_2$	$X_1$	124
0.58	$X_3$	$X_2$	$X_1$	88.4
0.70	$X_3$	$X_2$	$X_1$	106
0.73	$X_3$	$X_2$	$X_1$	108
1.00	$X_3$	$X_2$	$X_1$	142

values of *m*-plane  $Al_xGa_{1-x}N$  films calculated using the oscillator strengths for the measured  $(\epsilon_{X_1X_1}, \epsilon_{X_2X_2})$  coordinates are plotted as a function of x by open circles. As shown, the experimental data nearly agree with the calculated ones, except for the reduced  $\rho$  values for  $x \le 0.25$ . The low  $\rho$  values may be due to the light depolarization caused by the high density surface striations along the c-axis, which had been disclosed using atomic force microscopy observation.<sup>28</sup> We must note in Fig. 2(a) that overall CL intensities for x  $\geq$  0.58 were much weaker than those for  $x \leq$  0.32. From Table II, it is obvious that  $E_2 - E_1$  increases with x. Therefore, Boltzmann distribution gives rise to very low hole populations in  $E_2$  and  $E_3$  bands in comparison with  $E_1$  band for high x samples. This may be one of the reasons for the reduction in overall CL intensities for  $x \ge 0.58$  at low temperature, where the nonradiative recombination channels are in principle frozen.

Finally, calculated  $E_2$  transition energies (closed squares), CL peak energies (open circles), and their energy differences ( $\Delta E$ ) for the *m*-plane Al<sub>x</sub>Ga<sub>1-x</sub>N films are plotted as a function of *x* in Fig. 6. The  $\Delta E$  value, which is similar to the Stokes-type shift, ranged between 3 and 577 meV for the alloys. These values were slightly larger than those reported for *c*-plane AlGaN films grown by MOVPE (100–250 meV).<sup>30</sup>

#### **IV. CONCLUSION**

Interband optical polarization characteristics of *m*-plane  $Al_xGa_{1-x}N$  alloy films grown on the *m*-plane FS-GaN sub-



FIG. 6. (Color online) Calculated  $E_2$  transition energies (closed squares), measured CL peak energies (open circles), and their energy differences (closed diamonds) for the *m*-plane Al<sub>x</sub>Ga<sub>1-x</sub>N films as a function of *x*.

strates were studied by means of polarized CL measurements and theoretical calculations. The predominant light polarization direction of the CL peak for the films suffering from in-plane anisotropic tensile stresses was shown to alter from  $E \perp c(X_1)$  to  $E \parallel c(X_2)$  between x=0.25 and 0.32. Theoretical analysis of the oscillator strengths of interband transitions and exciton transition energies was carried out using Bir-Pikus Hamiltonian, taking the anisotropic strain into account. The calculation predicted that the lowest energy transition  $(E_1)$  is X<sub>3</sub>-polarized regardless of x, meaning that  $E_1$  exciton emission is, in principle, undetectable from the substrate normal. Apart from  $E_1$ , the calculated polarization direction altered from  $X_1$  to  $X_2$  for  $E_2$  transition and  $X_2$  to  $X_1$  for  $E_3$ transition between x=0.25 and 0.32. Both the polarization ratios and overall CL intensities were quantitatively explained through the calculation. These achievements may cut open the way of designing nonpolar AlGaN device configurations.

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