

# A new three-baryon-force in hypernuclei

著者	Nemura Hidekatsu
journal or publication title	AIP Conference Proceedings
volume	1011
page range	129-134
year	2008
URL	<a href="http://hdl.handle.net/10097/51471">http://hdl.handle.net/10097/51471</a>

doi: 10.1063/1.2932277

# A new three-baryon-force in $\Lambda\Lambda$ hypernuclei

Hidekatsu Nemura

*Advanced Meson Science Laboratory, Nishina Center for Accelerator-Based Science, RIKEN,  
Wako, 351-0198, Japan*

**Abstract.** We describe a few-body calculation of  ${}^5_{\Lambda\Lambda}\text{H}$  as well as  ${}^4_{\Lambda\Lambda}\text{H}$  and  ${}^6_{\Lambda\Lambda}\text{He}$  taking account fully coupled-channel two-baryon potentials acting among the octet of baryons. The wave function includes not only  $pnn\Lambda\Lambda$  and  $ppnn\Xi^-$  components but also  $pnn\Lambda\Sigma^0$ ,  $ppn\Lambda\Sigma^-$ ,  $pnn\Sigma^0\Sigma^0$  and  $ppn\Sigma^0\Sigma^-$ . An effective  $YY$  potential based on Nijmegen model D is used. We find that the  $pnn\Lambda\Sigma^0$  and  $ppn\Lambda\Sigma^-$  components play an important role in producing the  ${}^5_{\Lambda\Lambda}\text{H}$  bound state. The present result requires the introduction of a new coupled-channel three-body-force,  $N\Lambda\Lambda - N\Lambda\Xi$ , if the intermediate  $pnn\Lambda\Sigma^0$  and  $ppn\Lambda\Sigma^-$  states are eliminated from the model space.

**Keywords:** three-body-force, few-body problem, strangeness, hypernuclei

**PACS:** 21.80.+a, 21.45.+v, 21.10.Dr, 13.75.Ev

## INTRODUCTION

Doubly-strange, light hypernuclear systems are important to study in order to understand the baryon-baryon interactions, including the hyperon-hyperon ( $YY$ ) potential as well as the hyperon-nucleon ( $YN$ ) potential. In the study of strangeness  $S = -1$   $s$ -shell hypernuclei, it has been demonstrated that the  $\Lambda N - \Sigma N$  coupled-channel potential plays a significant role in explaining the anomalously small binding of  ${}^5_{\Lambda}\text{He}$ [1]. The “coherent  $\Lambda - \Sigma$  coupling”[1] may also be important in doubly strange hypernuclei.

A  $\Lambda\Lambda$  two-body system couples to the  $N\Xi$  and  $\Sigma\Sigma$  states in free space. For the doubly strange ( $S = -2$ ) hypernucleus,  ${}^5_{\Lambda\Lambda}\text{H}$ , the *core nucleus* +  $\Lambda\Lambda$  system couples to the *core nucleus* +  $\Lambda\Sigma$  component. This is an extension of the coherent  $\Lambda - \Sigma$  coupling to the doubly strange hypernucleus, and it implies that  $\Lambda N - \Sigma N$  coupling should also play an important role in the binding mechanism of the doubly strange hypernuclei. Therefore, precise calculations of the light  $\Lambda\Lambda$  hypernuclei should be made in a fully coupled channel formulation taking account of explicit  $\Sigma$  degrees of freedom. The purpose of this study is to describe a few-body calculation of the  $s$ -shell hypernuclei with  $S = -2$  by taking account of the explicit  $\Sigma$  degrees of freedom in a framework of a fully coupled-channel formulation.

## INTERACTIONS AND METHOD

We assume that the wave function of a system with  $S = -2$ , comprising  $A (= 4 - 6)$  octet baryons, has four isospin-basis components. For example, the  ${}^5_{\Lambda\Lambda}\text{H}$  has four isospin components as  $pnn\Lambda\Lambda$ ,  $NNNN\Lambda\Xi$ ,  $NNNN\Lambda\Sigma$  and  $NNNN\Sigma\Sigma$ . We abbreviate these components as  $\Lambda\Lambda$ ,  $N\Xi$ ,  $\Lambda\Sigma$  and  $\Sigma\Sigma$ , referring to the last two baryons. The Hamiltonian

of the system is hence given by  $4 \times 4$  components as

$$H = \begin{pmatrix} H_{\Lambda\Lambda} & V_{N\Xi-\Lambda\Lambda} & V_{\Lambda\Sigma-\Lambda\Lambda} & V_{\Sigma\Sigma-\Lambda\Lambda} \\ V_{\Lambda\Lambda-N\Xi} & H_{N\Xi} & V_{\Lambda\Sigma-N\Xi} & V_{\Sigma\Sigma-N\Xi} \\ V_{\Lambda\Lambda-\Lambda\Sigma} & V_{N\Xi-\Lambda\Sigma} & H_{\Lambda\Sigma} & V_{\Sigma\Sigma-\Lambda\Sigma} \\ V_{\Lambda\Lambda-\Sigma\Sigma} & V_{N\Xi-\Sigma\Sigma} & V_{\Lambda\Sigma-\Sigma\Sigma} & H_{\Sigma\Sigma} \end{pmatrix}, \quad (1)$$

where  $H_{B_1 B_2}$  operates on the  $B_1 B_2$  component,

$$H_{B_1 B_2} = \sum_{i=1}^A \left( \frac{\mathbf{p}_i^2}{2m_i} + m_i c^2 \right) - T_{c.m.} + \sum_{i < j}^{A-2} v_{NN}(\mathbf{r}_i - \mathbf{r}_j) + \sum_{j=1}^2 \sum_{i=1}^{A-2} v_{NB_j}(\mathbf{r}_i - \mathbf{r}_{B_j}) \\ + v_{B_1 B_2}(\mathbf{r}_{B_1} - \mathbf{r}_{B_2}) + \sum_{i < j}^A \frac{q_i q_j}{|\mathbf{r}_i - \mathbf{r}_j|}, \quad (2)$$

and  $V_{B_1 B_2 - B'_1 B'_2}$  is the sum of all possible two-body transition potentials connecting the  $B_1 B_2$  and  $B'_1 B'_2$  components:

$$V_{\Lambda\Lambda-N\Xi} = v_{\Lambda\Lambda-N\Xi}, \quad V_{\Lambda\Lambda-\Lambda\Sigma} = \sum_{i=1}^N v_{N_i \Lambda - N_i \Sigma}, \quad V_{N\Xi-\Lambda\Sigma} = v_{N\Xi-\Lambda\Sigma}, \quad (3)$$

$$V_{\Lambda\Lambda-\Sigma\Sigma} = v_{\Lambda\Lambda-\Sigma\Sigma}, \quad V_{N\Xi-\Sigma\Sigma} = v_{N\Xi-\Sigma\Sigma}, \quad V_{\Lambda\Sigma-\Sigma\Sigma} = \sum_{i=1}^N v_{N_i \Lambda - N_i \Sigma} + v_{\Lambda\Sigma-\Sigma\Sigma}. \quad (4)$$

In the present calculations, we use the Minnesota potential[2] for the  $NN$  interaction and the  $D2'$  potential for the  $YN$  interaction. The Minnesota potential reproduces reasonably well both the binding energies and sizes of few-nucleon systems. The  $D2'$  potential is a modified potential based upon the original  $D2$  potential[1]. The strength of the long-range part ( $V_b$  in Table I of Ref. [1]) of the  $D2'$  potential in the  $\Lambda N - \Lambda N \ ^3S_1$  channel is reduced by multiplying by a factor (0.954) in order to reproduce the experimental  $B_{\Lambda}({}^5_{\Lambda}\text{He})$  value.

For the  $YY$  interaction, we use a full-coupled channel potential among the octet baryons in both the spin triplet and the spin singlet channels. We assume that the  $YY$  potential consists of only the central component, and the effect due to the non-central force (e.g., tensor force) should be effectively included in the central part. The parameters are selected to reproduce the low-energy  $S$  matrix of the Nijmegen hard-core model D (ND)[3]. We take the hard-core radius to be  $r_c = 0.56(0.45)$  fm in the spin singlet (triplet) channel. Each number is the same as the hard-core radius of the  $YN$  sector in each channel. We denote as  $\text{ND}_S$  the potential simulating the ND model.

The binding energy is calculated in a complete  $A$ -body treatment. Since all of the exotic components ( $\Lambda\Lambda$ ,  $N\Xi$ ,  $\Lambda\Sigma$  and  $\Sigma\Sigma$ ) are taken into account, the variational trial function must be flexible enough to accurately search the eigenenergies. The trial function is given by a combination of basis functions:

$$\Psi = \sum_{k=1}^K c_k \varphi_k, \quad \text{with} \quad \varphi_k = \mathcal{A} \{ G(\mathbf{x}; A_k) \chi_{kJM} \eta_{kIM} \}. \quad (5)$$

Here  $\mathcal{A}$  is an antisymmetrizer acting on the identical particles. For the spin  $\chi_k$  and the isospin  $\eta_k$  functions, all possible configurations are taken into account. The abbreviation  $\mathbf{x} = (\mathbf{x}_1, \dots, \mathbf{x}_{A-1})$  is a set of relative coordinates. For the spatial part, the basis function is constructed by the correlated Gaussian (CG),  $G(\mathbf{x}; A_k)$ , which is given by

$$G(\mathbf{x}; A_k) = \exp \left\{ -\frac{1}{2} \sum_{i < j}^A \alpha_{kij} (\mathbf{r}_i - \mathbf{r}_j)^2 \right\} = \exp \left\{ -\frac{1}{2} \sum_{i,j=1}^{A-1} A_{kij} \mathbf{x}_i \cdot \mathbf{x}_j \right\}. \quad (6)$$

The stochastic variational method[4, 5] with the above CG basis produces accurate solutions. The reader is referred to Refs.[5, 6, 7] for details.

## RESULTS

Table 1 lists the  $B_{\Lambda\Lambda}$  values for the  $S = -2$  hypernuclei. We have obtained the bound-state solutions for  ${}_{\Lambda\Lambda}^4\text{H}$ ,  ${}_{\Lambda\Lambda}^5\text{H}$  and  ${}_{\Lambda\Lambda}^6\text{He}$ . For  ${}_{\Lambda\Lambda}^6\text{He}$ , the  $\Lambda\Lambda$  interaction energy ( $\Delta B_{\Lambda\Lambda}$ ) is given by

$$\Delta B_{\Lambda\Lambda}^{(\text{calc})}({}_{\Lambda\Lambda}^6\text{He}) = B_{\Lambda\Lambda}^{(\text{calc})}({}_{\Lambda\Lambda}^6\text{He}) - 2B_{\Lambda}^{(\text{calc})}({}_{\Lambda}^5\text{He}) = 1.59\text{MeV}, \quad (7)$$

which is slightly larger than the experimental value,[8]

$$\Delta B_{\Lambda\Lambda}^{(\text{exp})}({}_{\Lambda\Lambda}^6\text{He}) = 1.01 \pm 0.20_{-0.11}^{+0.18}\text{MeV}.$$

We have also calculated these systems using a modified  $\text{ND}_S$  ( $\text{mND}_S$ )  $YY$  potential; The strength of the  $\Lambda\Lambda$  diagonal part of the  $\text{mND}_S$  potential is reduced by multiplying the original  $\text{ND}_S$  by a factor of 0.8 in order to reproduce the experimental  $\Delta B_{\Lambda\Lambda}({}_{\Lambda\Lambda}^6\text{He})$ . Hereafter we use the  $\text{mND}_S$  potential rather than the  $\text{ND}_S$ . Table 2 shows the probabilities for the  $N\Xi$ ,  $\Lambda\Sigma$  and  $\Sigma\Sigma$  components of the  $S = -2$  hypernuclei. We should emphasize that the probability of the  $N\Xi$  component,  $P_{N\Xi}({}_{\Lambda\Lambda}^5\text{H})$ , has a surprisingly large value (4.56%) in spite of the fact that the  $\Lambda\Lambda - N\Xi$  coupling of the ND is rather weak as will be seen later. This is in remarkable contrast with other calculations based on  $(t + \Lambda + \Lambda)$  and  $(\alpha + \Xi^-)$  two-channel model[9, 10]. We obtained a sizable value for the  $P_{\Lambda\Sigma}({}_{\Lambda\Lambda}^5\text{H})$  probability. The  $\Lambda\Sigma$  component couples to the  $\Lambda\Lambda$  component via the  $v_{N\Lambda-N\Sigma}$  potential, as can be seen in Eq. (3), whereas the  $v_{\Lambda\Lambda-N\Xi-\Sigma\Sigma}$  potential in the  ${}^1S_0$ ,  $I = 0$  channel does not directly connect the  $\Lambda\Sigma$  component and the  $\Lambda\Lambda$  component.  $P_{\Sigma\Sigma}$ 's are

**TABLE 1.**  $\Lambda\Lambda$  separation energies, given in units of MeV, for the  $A = 4 - 6$ ,  $S = -2$   $s$ -shell hypernuclei.

$YY$	$B_{\Lambda\Lambda}({}_{\Lambda\Lambda}^4\text{H})$	$B_{\Lambda\Lambda}({}_{\Lambda\Lambda}^5\text{H})$	$B_{\Lambda\Lambda}({}_{\Lambda\Lambda}^6\text{He})$
$\text{ND}_S$	0.107	4.05	7.94
$\text{mND}_S$	0.058	3.75	7.54
Exp			$7.25 \pm 0.19_{-0.11}^{+0.18}$

**TABLE 2.** Probabilities, given in percent, for the  $N\Xi$ ,  $\Lambda\Sigma$  and  $\Sigma\Sigma$  components of the  $A = 4 - 6$ ,  $S = -2$   $s$ -shell hypernuclei.

	${}^4_{\Lambda\Lambda}\text{H}$			${}^5_{\Lambda\Lambda}\text{H}$			${}^6_{\Lambda\Lambda}\text{He}$		
	$P_{N\Xi}$	$P_{\Lambda\Sigma}$	$P_{\Sigma\Sigma}$	$P_{N\Xi}$	$P_{\Lambda\Sigma}$	$P_{\Sigma\Sigma}$	$P_{N\Xi}$	$P_{\Lambda\Sigma}$	$P_{\Sigma\Sigma}$
mND $_S$	0.06	0.25	0.00	4.56	2.49	0.06	0.28	1.17	0.05

very small for both systems, due to a large mass difference between the  $\Lambda\Lambda$  and  $\Sigma\Sigma$  channels ( $m_{\Sigma\Sigma} - m_{\Lambda\Lambda} \cong 155$  MeV).

Although the present calculation assumes no simplified structures, such as  $(t + \Lambda + \Lambda)$  and  $(\alpha + \Xi^-)$ , this kind of model is useful to provide a clear explanation of the complicated full coupling dynamics of the  $A = 5, S = -2$  hypernucleus. Let us consider a set of simple *core nucleus* +  $Y(+Y)$  model wave functions for the  ${}^5_{\Lambda\Lambda}\text{H}$ :

$$\begin{aligned}
 |{}^5_{\Lambda\Lambda}\text{H}\rangle &= \psi_t \times \psi_{\Lambda\Lambda} \times \psi_{\Lambda\Lambda-t}, & |{}^5_{\Xi}\text{H}\rangle &= \psi_\alpha \times \psi_{\Xi^-} \times \psi_{\Xi^- - \alpha}, & (8) \\
 |{}^5_{\Lambda\Sigma}\text{H}\rangle_{S_{\Lambda\Sigma}} &= \sqrt{\frac{1}{3}} \left[ \psi_t \times [\psi_{\Lambda\Sigma^0}]_{S_{\Lambda\Sigma}} \right] \times \psi_{\Lambda\Sigma^0-t} - \sqrt{\frac{2}{3}} \left[ \psi_h \times [\psi_{\Lambda\Sigma^-}]_{S_{\Lambda\Sigma}} \right] \times \psi_{\Lambda\Sigma^- - h} \\
 & \text{(for } S_{\Lambda\Sigma} = 0 \text{ or } 1), & & & (9)
 \end{aligned}$$

where  $\psi_c$  ( $c = t, h, \alpha$ ) is the wave function (WF) of the core nucleus,  $\psi_{YY}$  ( $YY = \Lambda\Lambda, \Xi^-, \Lambda\Sigma$ ) is the WF of the hyperon(s), and  $\psi_{YY-c}$  is the WF that describes the relative motion between  $YY$  and  $c$ . We assume that all of the baryons occupy the same ( $0s$ ) orbit. For the  ${}^5_{\Lambda\Sigma}\text{H}$  state, we have two independent states for the WF  $\psi_{\Lambda\Sigma}$ , that the spin of two hyperons ( $S_{\Lambda\Sigma}$ ) is either a singlet or a triplet. Since the  $\Sigma\Sigma$  component plays a minor role, we omit the  ${}^5_{\Sigma\Sigma}\text{H}$  state. Using these WFs, we can obtain the algebraic factors for each averaged coupling potential of the allowed spin state,  $\bar{v}^s$  or  $\bar{v}^t$ :

$$\langle V_{\Lambda\Lambda-N\Xi} \rangle = \sqrt{\frac{1}{2}} \bar{v}_{\Lambda\Lambda-N\Xi}^s, \quad (10)$$

$$\langle V_{\Lambda\Lambda-\Lambda\Sigma} \rangle = \begin{cases} \sqrt{\frac{9}{8}} \bar{v}_{N\Lambda-N\Sigma}^t + \sqrt{\frac{1}{8}} \bar{v}_{N\Lambda-N\Sigma}^s & \text{(for } S_{\Lambda\Sigma} = 0), \\ \sqrt{\frac{3}{8}} \bar{v}_{N\Lambda-N\Sigma}^t - \sqrt{\frac{3}{8}} \bar{v}_{N\Lambda-N\Sigma}^s & \text{(for } S_{\Lambda\Sigma} = 1), \end{cases} \quad (11)$$

$$\langle V_{N\Xi-\Lambda\Sigma} \rangle = \begin{cases} -\sqrt{\frac{3}{4}} \bar{v}_{N\Xi-\Lambda\Sigma}^s & \text{(for } S_{\Lambda\Sigma} = 0), \\ \frac{3}{2} \bar{v}_{N\Xi-\Lambda\Sigma}^t & \text{(for } S_{\Lambda\Sigma} = 1). \end{cases} \quad (12)$$

The  $v_{\Lambda\Lambda-N\Xi}$  potential is suppressed by a factor of  $\sqrt{1/2}$  for the  $A = 5$  hypernucleus. The  $v_{N\Lambda-N\Sigma}$  and  $v_{N\Xi-\Lambda\Sigma}$  potentials, particularly in the spin triplet channel, play significant roles instead. Namely, these equations imply that the  $\Lambda\Sigma$  component strongly couples both to the  $\Lambda\Lambda$  and to the  $N\Xi$  components, and the  $\Lambda\Sigma$  component plays a crucial role in the hypernucleus.

The normalized energy expectation values of the Hamiltonian (1) for  ${}_{\Lambda\Lambda}^5\text{H}$  are (given in units of MeV),

$$h = \begin{pmatrix} \frac{\langle H_{\Lambda\Lambda} \rangle}{P_{\Lambda\Lambda}} & \frac{\langle V_{N\Xi-\Lambda\Lambda} \rangle}{\sqrt{P_{\Lambda\Lambda}P_{N\Xi}}} & \frac{\langle V_{\Lambda\Sigma-\Lambda\Lambda} \rangle}{\sqrt{P_{\Lambda\Lambda}P_{\Lambda\Sigma}}} \\ \frac{\langle V_{\Lambda\Lambda-N\Xi} \rangle}{\sqrt{P_{\Lambda\Lambda}P_{N\Xi}}} & \frac{\langle H_{N\Xi} \rangle}{P_{N\Xi}} & \frac{\langle V_{\Lambda\Sigma-N\Xi} \rangle}{\sqrt{P_{N\Xi}P_{\Lambda\Sigma}}} \\ \frac{\langle V_{\Lambda\Lambda-\Lambda\Sigma} \rangle}{\sqrt{P_{\Lambda\Lambda}P_{\Lambda\Sigma}}} & \frac{\langle V_{N\Xi-\Lambda\Sigma} \rangle}{\sqrt{P_{N\Xi}P_{\Lambda\Sigma}}} & \frac{\langle H_{\Lambda\Sigma} \rangle}{P_{\Lambda\Sigma}} \end{pmatrix} = \begin{pmatrix} -9.12 & -1.82 & -14.52 \\ -1.82 & 5.01 & -10.39 \\ -14.52 & -10.39 & 92.41 \end{pmatrix}. \quad (13)$$

Here, we display only the  $3 \times 3$  components of the Hamiltonian (1), comprising  $\Lambda\Lambda$ ,  $N\Xi$ , and  $\Lambda\Sigma$ , since the contributions from the  $\Sigma\Sigma$  component are not large. These numbers reflect the nature of the  $YY$  potential model (ND). The ND model has a weak  $\Lambda\Lambda$ - $N\Xi$  coupling and a weakly attractive  $N\Xi$ - $N\Xi$  potential.

If we solve the eigenvalue problem,  $\det(h - \lambda I) = 0$ , we obtain the ground state energy,  $E = -11.82$  MeV, and the probability,  $P_{N\Xi} = 3.99\%$ . On the other hand, if we ignore the third row and the third column, the eigenenergy of only the first  $2 \times 2$  subspace becomes  $E = -9.35$  MeV, and the probability,  $P_{N\Xi} = 1.57\%$ . This clearly means that the couplings between the  $(\Lambda\Lambda, N\Xi)$  and  $\Lambda\Sigma$  components play crucial roles to make  ${}_{\Lambda\Lambda}^5\text{H}$  bound. The large coupling potentials,  $\langle V_{\Lambda\Lambda-\Lambda\Sigma} \rangle$  and  $\langle V_{N\Xi-\Lambda\Sigma} \rangle$ , also enhance the  $P_{N\Xi}$  probability.

## COUPLED-CHANNEL THREE-BARYON-FORCE

A coupled-channel Schrödinger equation for three component is written as

$$\begin{pmatrix} h_A & u_{AB} & u_{AC} \\ u_{AB} & h_B & u_{BC} \\ u_{AC} & u_{BC} & h_C \end{pmatrix} \begin{pmatrix} \psi_A \\ \psi_B \\ \psi_C \end{pmatrix} = \varepsilon \begin{pmatrix} \psi_A \\ \psi_B \\ \psi_C \end{pmatrix}. \quad (14)$$

Here the subscript  $(A, B, C)$  reads  $(\Lambda\Lambda, N\Xi, \Lambda\Sigma)$ . The third component yields

$$\psi_C = (\varepsilon - h_C)^{-1} u_{AC} \psi_A + (\varepsilon - h_C)^{-1} u_{BC} \psi_B. \quad (15)$$

Substituting the (15) into (14), we obtain the effective  $2 \times 2$  Schrödinger equation

$$\begin{pmatrix} \tilde{h}_A & \tilde{u}_{AB} \\ \tilde{u}_{AB} & \tilde{h}_B \end{pmatrix} \begin{pmatrix} \psi_A \\ \psi_B \end{pmatrix} = \varepsilon \begin{pmatrix} \psi_A \\ \psi_B \end{pmatrix}, \quad (16)$$

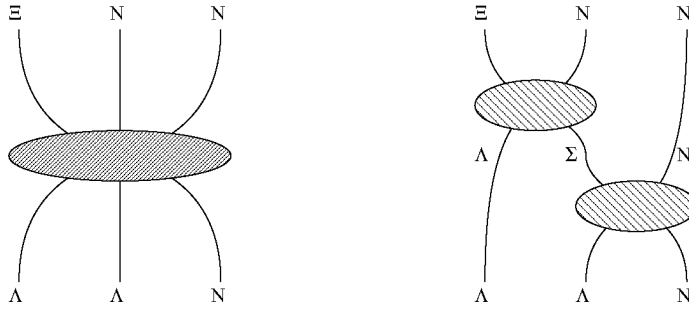
where

$$\tilde{h}_X = h_X + u_{XC} (\varepsilon - h_C)^{-1} u_{XC}, \quad (X = A, B) \quad (17)$$

$$\tilde{u}_{AB} = u_{AB} + u_{AC} (\varepsilon - h_C)^{-1} u_{BC}. \quad (18)$$

Therefore, the effective three-baryon-force is given by

$$w_{AB} = u_{AC} (\varepsilon - h_C)^{-1} u_{BC}. \quad (19)$$



**FIGURE 1.** Schematic description of coupled-channel three-body-force  $\Lambda\Lambda N - \Xi NN$  (left), derived from the intermediate  $\Lambda\Sigma$  component (right).

Figure 1 shows a diagram of the  $\Lambda\Lambda N - \Xi NN$  three-body-force due to the intermediate  $\Lambda\Sigma N$  excitation. In the present case, we can deduce the energy expectation value of the coupled-channel three-baryon-force  $\Lambda\Lambda N - \Xi NN$  by eliminating the  $\Lambda\Sigma$  component,

$$\langle w_{\Lambda\Lambda-N\Xi} \rangle \cong -1.4 \text{ MeV}. \quad (20)$$

This has almost the same magnitude as the energy expectation value of the original  $v_{\Lambda\Lambda-N\Xi}$  potential ( $\cong -1.8 \text{ MeV}$ ). The net attractive energy due to the  $\Lambda\Lambda - N\Xi$  coupling thus becomes approximately three times larger than the original two-body  $\Lambda\Lambda - N\Xi$  potential.

The present study is a first attempt to explore the new three-body-force arising in  $\Lambda\Lambda$  hypernuclei. This kind of coupled-channel three-baryon-force should be taken into account for the study of  $\Xi$  hypernuclei since it affects the net  $\Lambda\Lambda - N\Xi$  coupling and the decay width of the hypernucleus.

## ACKNOWLEDGMENTS

The calculations were made using the supercomputers at RCNP and KEK.

## REFERENCES

1. Y. Akaishi, et al., Phys. Rev. Lett. **84**, 3539 (2000).
2. D. R. Thompson, M. Lemere and Y. C. Tang, Nucl. Phys. A**286**, 53 (1977).
3. M. M. Nagels, T. A. Rijken and J. J. de Swart, Phys. Rev. D**15**, 2547 (1977).
4. V. I. Kukulin and V. M. Krasnopol'sky, J. Phys. G:Nucl. Part. Phys. **3**, 795 (1977).
5. Y. Suzuki and K. Varga, *Stochastic Variational Approach to Quantum-Mechanical Few-Body Problems*, Lecture Notes in Physics, Vol. m54 (Springer-Verlag, Berlin Heidelberg, 1998).
6. H. Nemura, Y. Akaishi and Y. Suzuki, Phys. Rev. Lett. **89**, 142504 (2002).
7. H. Nemura, et al., Phys. Rev. Lett. **94**, 202502 (2005).
8. H. Takahashi, et al., Phys. Rev. Lett. **87**, 212502 (2001).
9. Khin Swe Myint, S. Shimura and Y. Akaishi, Eur. Phys. J. A **16**, 21 (2003).
10. D. E. Lanskoy and Y. Yamamoto, Phys. Rev. C **69**, 014303 (2004).