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著者	三上 直彦
journal or publication title	Laser Chemistry
volume	7
number	2/4
page range	197-212
year	1987
URL	http://hdl.handle.net/10097/46231

doi: 10.1155/LC.7.197

Internal Rotation of the Methyl Group in the Electronically Excited State: *o*- and *m*-Toluidine

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The fluorescence excitation and dispersed fluorescence spectra of jet-cooled *o*- and *m*-toluidine were observed. Vibrational analysis of the spectra provided us with the potentials for the internal rotation of the CH₃ group in both ground and excited states. In *o*-toluidine, a large potential barrier to the internal rotation in the ground state is practically removed in the excited state. On the other hand, a nearly free internal rotation of the CH₃ group in the ground state of *m*-toluidine gains a large barrier by the electronic excitation. The great change in the barrier height upon the electronic excitation is more remarkable than that found for fluorotoluene. A close relationship between the barrier height and the π electron density at the ring carbon atom was found, indicating the hyperconjugation as the origin of the barrier height in the absence of steric hindrance.

KEY WORDS: Internal rotation; methyl group; toluidine; laser spectroscopy; supersonic jet; hyperconjugation.

INTRODUCTION

Recently, large amplitude motions of molecules have attracted a great deal of interest with respect to their vibrational potentials in electronically ground and excited states^{1–4} and their role in various relaxation processes^{5,6}. In a series of our studies on large-amplitude motion of large polyatomic molecules, it was demonstrated that electronic

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spectra of molecules in supersonic jets obtained by the use of various laser spectroscopies are very useful for the determination of the potentials⁷⁻⁹ and for the elucidation of the dynamical behaviors¹⁰⁻¹¹ of these molecules. One of the achievements of the studies is the finding of a great change in the potential upon electronic excitation. In our previous study on *o*-, *m*- and *p*-fluorotoluene⁸, we showed that a large barrier to the internal rotation of the CH₃ group in the ground state of *o*-fluorobenzene is almost removed in the lowest excited $S_1(\pi, \pi^*)$ state. On the other hand, a nearly free internal rotation of the CH₃ group in the ground state of *m*- or *p*-fluorotoluene is hindered in the S_1 state and this is especially marked in *m*-fluorotoluene. The results indicated that the internal rotation of a CH₃ group is very sensitive to the nature of the electronic state and also to the location of the CH₃ group attached to the parent molecule. A CH₃ group generally only weakly perturbs the electronic structure of a parent molecule. The internal rotation of a CH₃ group, however, is expected to be greatly affected by the change in the electronic environs of the CH₃ group. Therefore, the internal rotation provides us with a good measure for characterization of the electronic states of a molecule.

The present study is an extension of our previous study on fluorotoluene to *o*- and *m*-toluidine which have an NH₂ group instead of the fluorine atom of fluorotoluene. We observed the fluorescence excitation and dispersed fluorescence spectra of jet-cooled *o*- and *m*-toluidine due to the $S_1(\pi, \pi^*) - S_0$ transition. Many low frequency vibronic bands associated with the internal rotational levels in the S_0 and S_1 states were observed. From the analysis of the vibronic bands, the potentials for the internal rotation of the CH₃ group were accurately determined for both the S_0 and the S_1 states. The results obtained are parallel to those of *o*- and *m*-fluorotoluene, i.e. a large barrier to the internal rotation of *o*-toluidine in its S_0 state almost disappears in the S_1 state, while in *m*-toluidine an almost free internal rotation in the S_0 state gains a great barrier in the S_1 state. The great change in the barrier height upon electronic excitation is more remarkable than that in fluorotoluene. The barrier height for *m*-fluorotoluene and *m*-toluidine, together with that for *m*-cresol (which will be reported in detail elsewhere), show a clear relationship between the barrier height and the π electron density of the meta ring carbon atom of the parent molecule to which the CH₃ group is attached. The relationship strongly suggests that the barrier to internal rotation arises from hyperconju-

gation. A possible cause for the disappearance of the barrier by the electronic excitation in *o*-toluidine is also discussed.

EXPERIMENTAL

The pulsed supersonic free-jet apparatus has already been described elsewhere¹². The sample was heated to 330 K in a nozzle chamber to obtain sufficient vapor pressure and seeded in helium carrier gas. The gaseous mixture (~ 5 atm.) was expanded into a vacuum chamber ($\sim 10^{-5}$ Torr) through an orifice of 0.8 mm diameter. The fluorescence excitation spectra were obtained by monitoring the total fluorescence with a photomultiplier (HTV R-562). The photocurrent was averaged by a boxcar integrator (Brook deal 9415/9425) and recorded. The exciting light used was the second harmonic of a dye laser (Molelectron DL-14P) pumped by a nitrogen laser (Molelectron UV-24). The laser resolution was about 1.0 cm^{-1} (fwhm). The dispersed fluorescence spectra were measured by a Nalumi 0.75-m monochromator with a 0.04-mm slit width and the spectral resolution was about 6 cm^{-1} (fwhm). The signal was detected by a photomultiplier (HTV R-928) and recorded by the same integrator system as that used for the fluorescence excitation spectra.

o-Toluidine and *m*-toluidine were purchased from Tokyo Kasei and purified by distillation.

RESULTS AND DISCUSSION

Fluorescence excitation and dispersed fluorescence spectra

Figure 1 shows the fluorescence excitation spectrum of jet-cooled *o*-toluidine due to the $S_1(\pi, \pi^*) \leftarrow S_0$ transition. The spectrum exhibits a well-resolved vibrational structure. There exist many low frequency bands on the higher frequency side of the lowest frequency band at $34\,316 \text{ cm}^{-1}$. The main bands are those shifted by 3, 28, 58, 91, 142 and 197 cm^{-1} from the $34\,316 \text{ cm}^{-1}$ band. They are connected by a line in the figure. Similar band structures are seen all over the spectrum, some of them being shown in the figure. These low frequency bands are very similar in structure to those observed in *o*-fluorotoluene reported in a previous study⁸, the latter being assigned to the transitions between the internal rotational levels of the CH_3

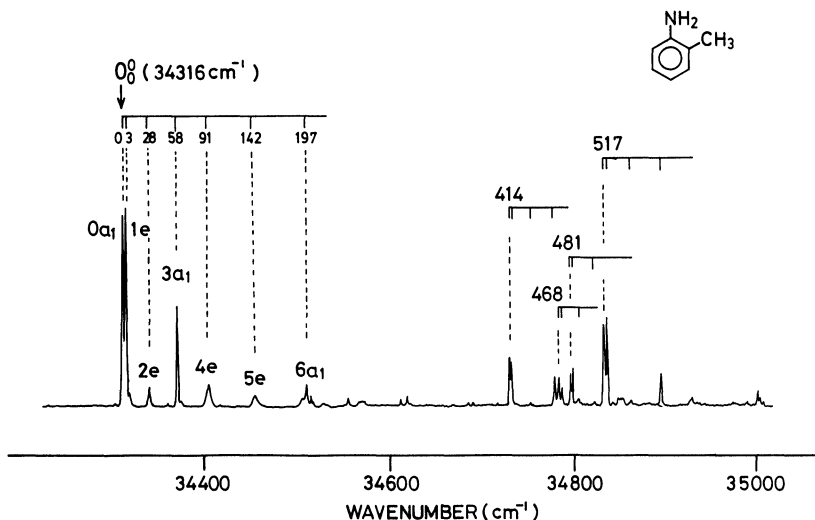


Figure 1 Fluorescence excitation spectrum of jet-cooled *o*-toluidine. Bands associated with internal rotational levels of the methyl group in S_1 are indicated. Frequencies measured from the 0,0 band are shown.

group in the S_0 and S_1 states. The similarity suggests the assignments of the low frequency bands of *o*-toluidine in parallel to those given for *o*-fluorotoluene and these assignments are given in the figure. The internal rotational levels in the S_1 state are denoted by a combination of the rotational quantum number, m , of a one-dimensional free rotor and the symmetry species of the permutation inversion group isomorphous to C_{3v} point group^{13,14}. The assignments are supported from the dispersed fluorescence spectra which will be described below.

Figure 2a shows part of the dispersed fluorescence spectrum of jet-cooled *o*-toluidine obtained by excitation of the 34316 cm^{-1} ($0a_1$) band in the excitation spectrum. It is a difficult task to find the bands associated with the ground state internal rotational levels among many bands. However, when exciting the $3a_1$ ($0 + 58 \text{ cm}^{-1}$) and $6a_1$ ($0 + 197 \text{ cm}^{-1}$) bands in the excitation spectrum, bands at 361 and 578 cm^{-1} show intensity enhancement in the dispersed fluorescence spectra as shown in Figure 2(b and c). Taking into account the $a_1 \longleftrightarrow a_1$ selection rule for the transition between the internal rotational levels, the bands at 361 and 578 cm^{-1} can be assigned to $3a_1$ and $6a_1$ levels, respectively, in the S_0 state.

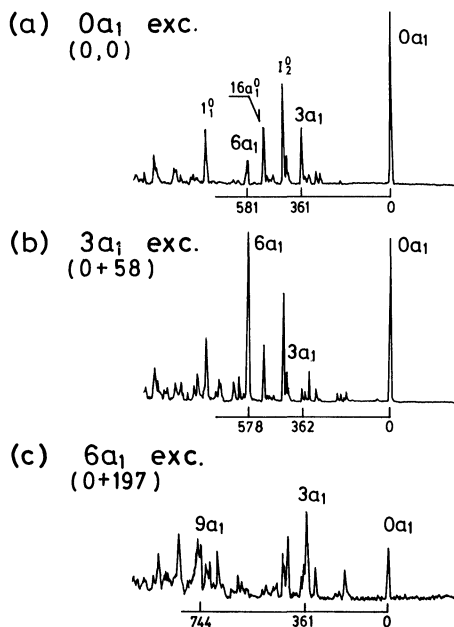


Figure 2 Dispersed fluorescence spectra of jet-cooled *o*-toluidine obtained by exciting the a_1 bands in Figure 1. Each spectrum is shown by relative frequency measured from the excitation frequency.

Figure 3 shows the dispersed fluorescence spectra obtained by exciting the $1e$ ($0 + 3 \text{ cm}^{-1}$), $2e$ ($0 + 28 \text{ cm}^{-1}$), $4e$ ($0 + 91 \text{ cm}^{-1}$) and $5e$ ($0 + 142 \text{ cm}^{-1}$) bands in the excitation spectrum. It is seen from the figure that the bands at 0, 182, 363, 472, 587 and 683 cm^{-1} show characteristic intensity enhancements in the individual dispersed fluorescence spectra. Therefore, they can be assigned to $1e$, $2e$, $4e$, $5e$, $7e$ and $8e$ levels in the S_0 state because of the $e \leftrightarrow e$ selection rule. Thus, we obtained the energies of the internal rotational levels in both the S_0 and S_1 states, which are listed in Table I. In the S_0 state, the $3a_1$ and $4e$ levels are nearly degenerate in energy and the frequency difference between the $6a_1$ and $7e$ levels is about 10 cm^{-1} . This suggests a large potential barrier in the S_0 state compared with that in the S_1 state. The above assignments will be further confirmed from the calculated potentials and relative intensity distributions of the internal rotational bands in the fluorescence excitation and dispersed fluorescence spectra, which will be described later.

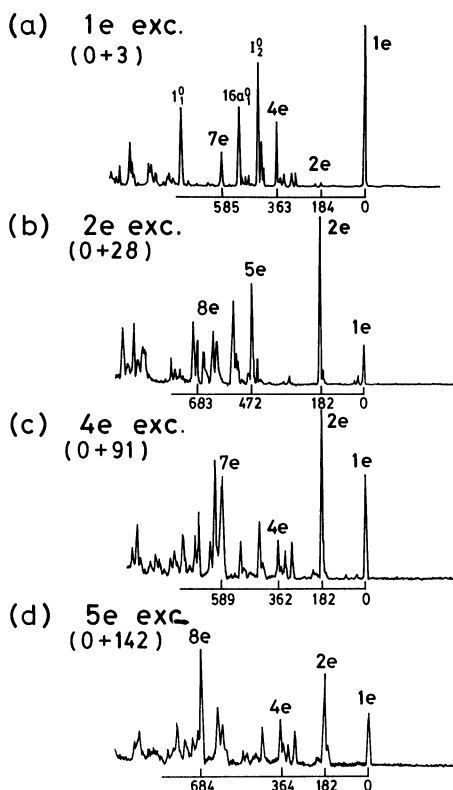


Figure 3 Dispersed fluorescence spectra of jet-cooled *o*-toluidine obtained by exciting the e bands in Figure 1. Each spectrum is shown by relative frequency measured from the excitation frequency.

In Figure 4 is shown the fluorescence excitation spectrum of jet-cooled *m*-toluidine due to the $S_1(\pi, \pi^*) \leftarrow S_0$ transition. The structure of low frequency bands less than 400 cm^{-1} is again similar to that of *m*-fluorotoluene reported in a previous paper⁸, although some of the bands accidentally coincide in energy. The assignments of the low frequency bands can be made in parallel to those for *m*-fluorotoluene and they are shown in the figure. A band at $33\,818\text{ cm}^{-1}$ ($0a_1$) is the 0_0^0 band. A band red-shifted by 5.0 cm^{-1} from the 0_0^0 band is the hot band due to the transition from the $1e$ level in S_0 to the $1e$ level

Table I Internal rotational levels of *o*-toluidine in ground and excited states.

Level species (C_{3v})	Ground state (cm^{-1})		Excited state (cm^{-1})	
	Observed	Calculated ^a	Observed	Calculated ^b
$0a_1$	0	0	0	0
$1e$	0	0	3	4
$2e$	182	190	28	28
$3a_2$	—	190	47	49
$3a_1$	361	356	58	58
$4e$	363	356	91	91
$5e$	472	491	142	139
$6a_2$	—	497	—	198
$6a_1$	578	579	197	198
$7e$	587	604	—	268
$8e$	683	670	—	349
$9a_2$	—	745	—	441
$9a_1$	744	749	—	438

^a Calculated with $V_3 = 703 \text{ cm}^{-1}$, $V_6 = 62 \text{ cm}^{-1}$ and $B = 5.28 \text{ cm}^{-1}$.

^b Calculated with $V_3 = 40 \text{ cm}^{-1}$, $V_6 = -11 \text{ cm}^{-1}$ and $B = 5.40 \text{ cm}^{-1}$.

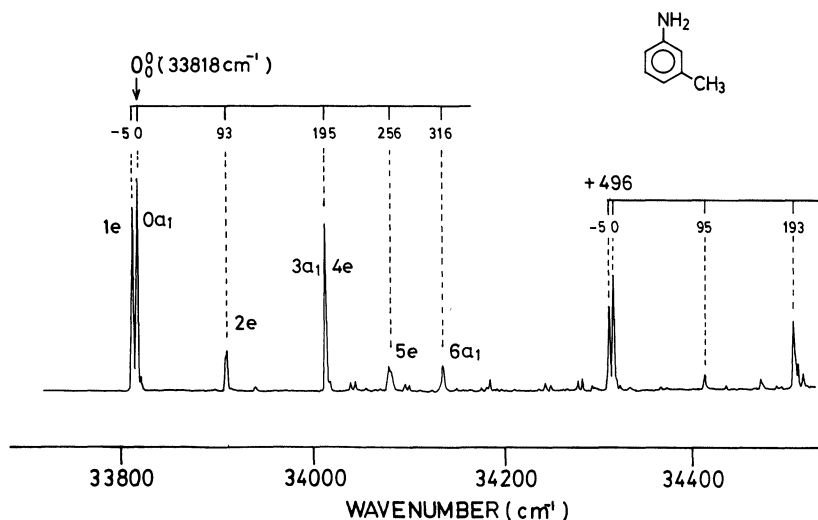


Figure 4 Fluorescence excitation spectrum of jet-cooled *m*-toluidine. Band associated with internal rotational levels of the methyl group in S_1 are indicated. Frequencies measured from the 0,0 band are shown.

in S_1 . The appearance of this band on the lower frequency side of the 0_0^0 band suggests that the barrier to the internal rotation is higher in the S_1 state than in the S_0 state. The assignments of the low frequency bands in the fluorescence excitation spectrum are confirmed from the observation of the dispersed fluorescence spectra obtained by excitation of the low frequency bands, which are shown in Figure 5. As is seen from the figure, in the dispersed fluorescence spectra obtained by exciting the bands of a_1 species in the excitation spectrum, bands at 51 and 192 cm^{-1} measured from the exciting band commonly appear, while another set of bands at 17, 81 and 130 cm^{-1} are commonly observed in the e level dispersed fluorescence spectra. From the $a_1 \longleftrightarrow a_1$ and $e \longleftrightarrow e$ selection rules, the former set of the bands can be assigned to the a_1 levels in the S_0 state and the latter set to the e levels. The energies of the internal rotational levels in both the S_0 and S_1 states thus obtained are listed in Table II. The assignments will be further confirmed later by the calculated energy levels and intensity distributions of the internal rotational bands.

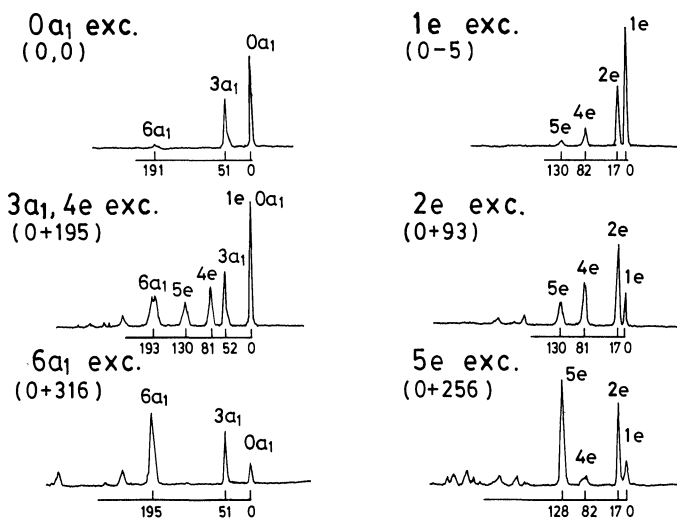


Figure 5 Dispersed fluorescence spectra of jet-cooled *m*-toluidine obtained by exciting the bands in Figure 4. Each spectrum is shown by relative frequency measured from the excitation frequency.

Table II Internal rotational levels of *m*-toluidine in ground and excited states.

Level species (C_{3v})	Ground state (cm^{-1})		Excited state (cm^{-1})	
	Observed	Calculated ^a	Observed	Calculated ^b
$0a_1$	0	0	0	0
$1e$	0	0	-5	-5
$2e$	17	17	93	97
$3a_2$	—	46	—	102
$3a_1$	51	51	195	189
$4e$	82	81	195	191
$5e$	130	129	256	255
$6a_2$	—	194	—	295
$6a_1$	192	194	316	314
$7e$	252	258	—	362
$8e$	—	339	—	437

^a Calculated with $V_3 = 9 \text{ cm}^{-1}$, $V_6 = -10 \text{ cm}^{-1}$ and $B = 5.37 \text{ cm}^{-1}$.

^b Calculated with $V_3 = 317 \text{ cm}^{-1}$, $V_6 = -19 \text{ cm}^{-1}$ and $B = 5.24 \text{ cm}^{-1}$.

Potentials for internal rotation in S_0 and S_1 states

The energy level structures for the internal rotation of the CH_3 group in the S_0 and S_1 states for *o*- and *m*-toluidine have now been obtained. If we assume that the methyl top and the benzene framework are rigid rotors, the wave function $\psi(\varphi)$ for the internal rotation should satisfy the following equation

$$\left[-B \frac{d^2}{d\varphi^2} + V(\varphi) \right] \psi(\varphi) = E\psi(\varphi) \quad (1)$$

where φ is the torsional angle between the two rotors and B is the reduced rotational constants of the rotors about the methyl top axis. The potential $V(\varphi)$ is assumed by

$$V(\varphi) = \frac{V_3}{2} (1 - \cos 3\varphi) + \frac{V_6}{2} (1 - \cos 6\varphi) \quad (2)$$

Equation (1) can be solved by expanding $\psi(\varphi)$ by a basis set of one-dimensional free rotor wave functions and by diagonalizing the Hamiltonian matrix⁵. Three unknown parameters B , V_3 and V_6 were determined by adjusting them to give the calculated energies which give a best fit to the observed energies. The relative intensity distributions of the bands due to the internal rotation in the fluorescence excitation and dispersed fluorescence spectra provide us with a useful

check of the potentials and also with the relative relation between the S_0 and S_1 potentials with respect to the torsional angle. The procedure for the calculation of the intensity distribution was described in detail in a previous paper⁸.

In Table III are summarized the potential parameters V_3 and V_6 and the reduced rotational constant B obtained from the above calculations. Figures 6 and 7 show the potentials and energy levels in the S_0 and S_1 states. Comparison between the calculated and observed level energies is given in Tables I and II. It is seen that the agreement between the observed and calculated energies is satisfactory. In Figures 8 and 9 are shown comparisons between the observed and calculated intensity distributions of the fluorescence excitation and dispersed fluorescence spectra. The agreement is generally very good when assuming the same stable conformations of the CH_3 group for both the S_0 and the S_1 states. In the case of *o*-fluorotoluene, we found the conformation change upon electronic excitation. However, in *o*-toluidine, no sign of the conformation change was found.

It is concluded from the above results that in *o*-toluidine, the barrier to the internal rotation is as large as 700 cm^{-1} in the S_0 state, but it dramatically decreases to only 40 cm^{-1} in the S_1 state. A completely reversed relationship is found in *m*-toluidine, where the barrier is very small (9 cm^{-1}) in the S_0 state, but increases to as large as 300 cm^{-1} in the S_1 state. The decrease of the barrier height in the *o*-isomer and the increase in the *m*-isomer upon electronic excitation are the same as those for *o*- and *m*-fluorotoluene. However, the effect upon the electronic excitation is about three times more remarkable in toluidine than in fluorotoluene.

We shall first consider the ground-state potential. Toluidine has two flexible groups of NH_2 and CH_3 . It is well known that the parent

Table III Potential parameters and rotational constants for internal rotation of CH_3 in ground and excited states.

	Ground state (cm^{-1})	Excited state (cm^{-1})
<i>o</i> -Toluidine	$V_3 = 703$ $V_6 = 62$ $B = 5.28$	$V_3 = 40$ $V_6 = -11$ $B = 5.40$
<i>m</i> -Toluidine	$V_3 = 9$ $V_6 = -10$ $B = 5.37$	$V_3 = 317$ $V_6 = -19$ $B = 5.24$

molecule—*aniline*—has the inversion vibration of NH_2 group analogous to the “umbrella” vibration of ammonia. The potential barrier opposing coplanarity of the NH_2 group and benzene ring is known to be 526 cm^{-1} . The inversion barrier height is 558 and 528 cm^{-1} , respectively, in *o*- and *m*-toluidine¹⁷. Therefore, the substitution of an aromatic hydrogen atom by a CH_3 group does not greatly affect the inversion potential. In contrast to the insensitivity of the inversion potential, the potential for the internal rotation of the CH_3 group changes greatly depending upon its location. These facts show that the electronic structure of toluidine is essentially determined by that of the parent molecule (*aniline*) and the CH_3 group is electronically a weak

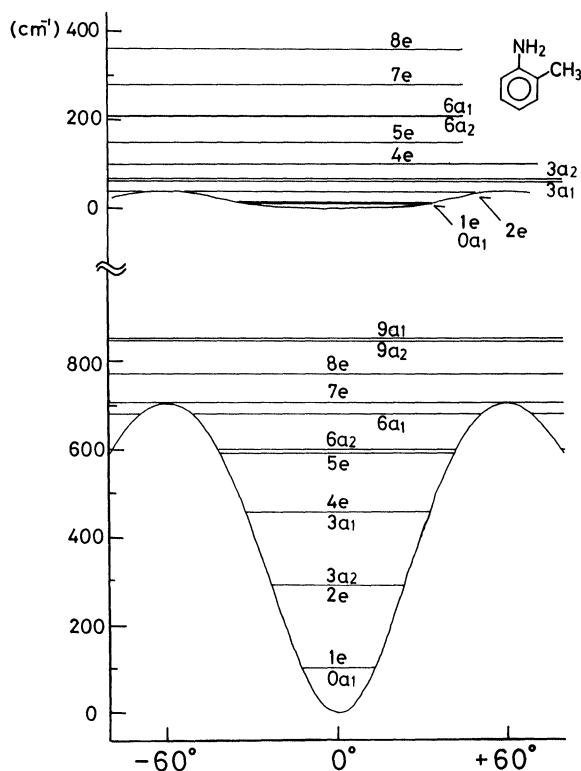


Figure 6 Potentials and energy levels for internal rotation of *o*-toluidine in the ground and excited states.

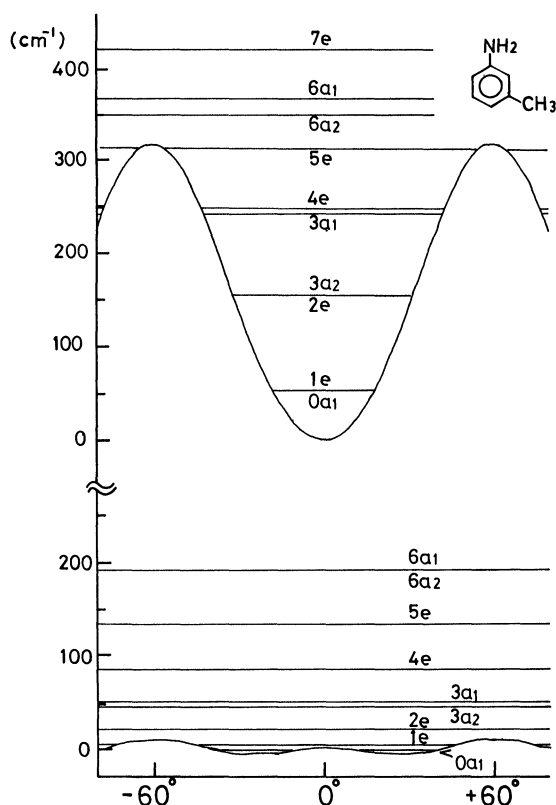


Figure 7 Potentials and energy levels for internal rotation of *m*-toluidine in the ground and excited states.

perturber. However, the internal rotation of the CH_3 group is greatly affected by the local electronic and geometrical structure of the molecule in the vicinity of the CH_3 group. Apparently, the large barrier height in *o*-toluidine (703 cm^{-1}) arises from a great steric hindrance due to nearby NH_2 group. Since NH_2 is a more bulky substituent than the F atom, the barrier height is much larger in *o*-toluidine than in *o*-fluorotoluene (288 cm^{-1}). The very small barrier height (9 cm^{-1}) in *m*-toluidine is easily understood by the absence of steric hindrance, and is comparable with that of 4 cm^{-1} in the S_0 state of toluene¹⁸. Therefore, the NH_2 group at the *m*-position does not exert an appreciable effect on the internal rotation of the CH_3 group in the S_0 state.

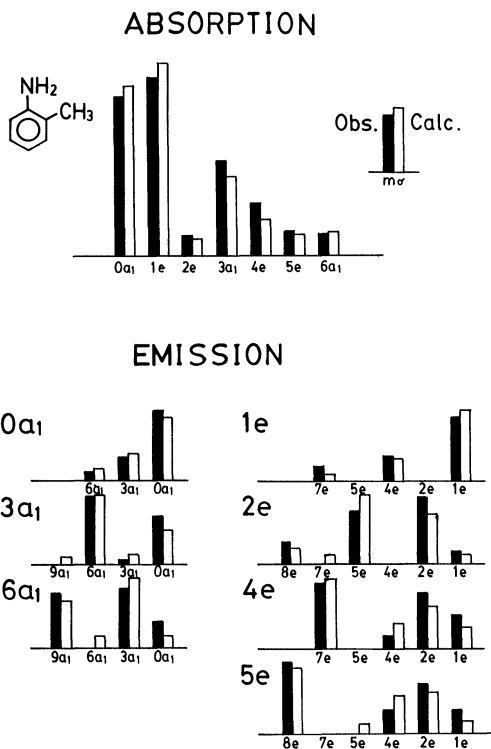


Figure 8 Comparisons between the observed and calculated intensity distributions of the fluorescence excitation and dispersed fluorescence spectra of *o*-toluidine.

Next, we shall discuss the potential barrier in the S_1 state. In the case of *m*-toluidine, the appearance of the large barrier (300 cm^{-1}) in the S_1 state is difficult to explain by steric hindrance. Since the reduced rotational constant B is nearly equal between the S_0 and S_1 states (see Table III), steric environment does not differ greatly between the two states. It seems reasonable that an electronic effect is mainly responsible for the appearance of the large barrier. Table IV summarizes the barrier heights of toluene, *m*-fluorotoluene, *m*-cresol and *m*-toluidine in the S_0 and S_1 states. In the table are also shown the calculated π -electron densities at *m*-carbon atoms of the parent molecules, benzene, fluorobenzene, phenol and aniline, in the S_0 and S_1 states^{19,20}. It is seen from the table that there exists good correlation between the

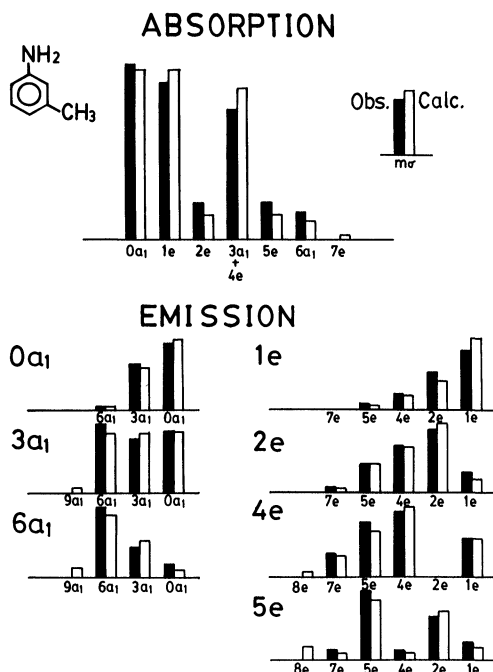


Figure 9 Comparisons between the observed and calculated intensity distributions of the fluorescence excitation and dispersed fluorescence spectra of *m*-toluidine.

Table IV Barrier heights of several *m*-substituted benzenes in S_0 and S_1 states and calculated π -electron densities of *m*-carbon atoms of parent molecules.

Molecule		S_0		S_1	
		Barrier height (cm ⁻¹)	π -electron ^a density	Barrier height (cm ⁻¹)	π -electron ^a density
Toluene	-H	4 ^b	1.00	4	1.00
<i>m</i> -Fluorotoluene	-F	17 ^c	1.00	124 ^c	1.04
<i>m</i> -Cresol	-OH	10 ^d	1.01	200 ^d	1.07
<i>m</i> -Toluidine	-NH ₂	9	1.01	317	1.09

^a π -Electron of *m*-carbon atoms of the parent molecules, benzene, fluorobenzene, phenol and aniline taken from the literature^{19,20}.

^b From Rudolph *et al.*¹⁸

^c From Okuyama *et al.*⁸

^d From K. Okuyama, N. Mikami and M. Ito, unpublished data.

barrier height and the π -electron density. In the S_0 state, the π -electron density at the m -carbon atom is nearly equal for all the parent molecules. This is reflected by the nearly free internal rotation of the CH_3 group in all the m -substituted molecules. In the S_1 state, however, the π -electron density increases markedly in the order benzene, fluorobenzene, phenol and aniline. In the same order, the barrier height progressively increases in the m -substituted molecules (4, 120, 200 and 300 cm^{-1} for toluene, m -fluorotoluene, m -cresol and m -toluidine, respectively). It is concluded therefore that the barrier to the internal rotation of the CH_3 group is controlled by the π -electron density of the ring carbon atom of the parent molecule to which the CH_3 group is attached. The close correlation between the barrier height and the π -electron density suggests that, in the case of the m -substituted molecule, the origin of the barrier to the internal rotation is the hyperconjugation of the CH_3 group. The hyperconjugation contributes to the increase in double bond character of the m -carbon - CH_3 bond depending on the electron density at the m -carbon atom. It is concluded that the great increase of the barrier height in the m -substituted molecule upon electronic excitation results from the enhancement of hyperconjugation. Recent *ab initio* calculation of the electronic structure of m -fluorotoluene in the S_0 and S_1 states carried out by Nishimoto reproduces the observed potentials and supports the effect of hyperconjugation.

The dramatic decrease in the barrier height in the S_1 state of o -toluidine is not easy to understand. Since the situation is similar to the case of o -fluorotoluene, the origin of the great decrease will be the same between o -toluidine and o -fluorotoluene. In the case of o -fluorotoluene, we explained the almost free internal rotation in the S_1 state by a cancellation of the great steric repulsive interaction by some attractive interaction, such as intramolecular hydrogen bonding between a hydrogen atom of the methyl group and the F atom. Recently, Nishimoto²¹ calculated the potentials for the internal rotation of the CH_3 group in o -fluorotoluene and obtained the calculated potentials which agree very well with the observed ones. From the calculation, they concluded that electrostatic interaction between the F atom and the hydrogen atoms of the nearby CH_3 group is responsible for the small barrier height in the S_1 state. A similar electrostatic interaction is probably a cause of the small barrier in o -toluidine. A possible attractive interaction would be intramolecular

hydrogen bonding between the nitrogen atom of the NH₂ group and the hydrogen atoms of the CH₃ group.

In the present work, we did not report the result for *p*-toluidine. Although the fluorescence excitation spectrum of jet-cooled *p*-toluidine was observed, the bands due to the internal rotation of the CH₃ group were so weak that their detailed analysis was not possible. The weak intensity suggests that the potential for the internal rotation in *p*-toluidine does not differ greatly between the S₀ and S₁ states.

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