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# Measurement of Coherent Production of $\pi^{ \pm}$in Neutrino and Antineutrino Beams on Carbon from $E_{\nu}$ of 1.5 to 20 GeV 

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#### Abstract

Neutrino-induced coherent charged pion production on nuclei $\stackrel{(-)}{\nu}_{\mu} A \rightarrow \mu^{ \pm} \pi^{\mp} A$ is a rare, inelastic interaction in which a small squared four-momentum $|t|$ is transferred to the recoil nucleus, leaving it intact in the reaction. In the scintillator tracker of MINERvA, we remove events with evidence of particles from nuclear breakup and reconstruct $|t|$ from the final-state pion and muon. We select low $|t|$ events to isolate a sample rich in coherent candidates. By selecting low $|t|$ events, we produce a model-independent measurement of the differential cross section for coherent scattering of neutrinos and antineutrinos on carbon. We find poor agreement with the predicted kinematics in neutrino generators used by current oscillation experiments.


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Coherent pion production from nuclei is an electroweak process described by the diagram in Fig. 1 in which a virtual pion scatters from a target nucleus that remains unchanged in its ground state after scattering. To achieve this coherence, the square of the four-momentum
exchanged with the nucleus must be small, $|t| \lesssim \hbar^{2} / R^{2}$, where $R$ is the radius of the nucleus, and the particle(s) exchanged can only carry vacuum quantum numbers. Adler's theorem [1] provides a relationship between the coherent scattering cross section at $Q^{2} \equiv-q^{2}=0$ and the


FIG. 1. Feynman diagram for coherent charged pion production.
pion-nucleus elastic cross section [2-4], which in the limit of $m_{\mu}, m_{\pi} \ll E_{\nu}$ is

$$
\begin{equation*}
\left.\frac{d^{3} \sigma_{\mathrm{coh}}}{d Q^{2} d y d|t|}\right|_{Q^{2}=0}=\frac{G_{F}^{2}}{2 \pi^{2}} f_{\pi}^{2} \frac{1-y}{y} \frac{d \sigma(\pi A \rightarrow \pi A)}{d|t|} \tag{1}
\end{equation*}
$$

where $y$ is $E_{\pi} / E_{\nu}$ and $f_{\pi}$ is the pion decay constant. The $\pi A$ elastic scattering cross section falls with increasing $|t| \sim$ $e^{|t| R^{2} / \hbar^{2}} \quad[3,4]$. Models must be used to extrapolate to $Q^{2} \neq 0$. The model most commonly used in neutrino event generators [5-7] is that of Rein and Sehgal [4], which assumes no vector current and extrapolates the axial-vector current using a multiplicative dipole form factor $F_{\text {dipole }}^{2}=$ $1 /\left(1+Q^{2} / m_{A}^{2}\right)^{2}$ to modify Eq. (1). Other authors have proposed alternate extrapolations to $Q^{2} \neq 0$ [8-11]. It is also necessary to parametrize the $\pi A$ elastic scattering cross section, and generators have varied approaches [5-7]. At low energies, modifications to Eq. (1) due to finite masses become important, in particular $Q^{2} \geq m_{\mu}^{2}[y /(1-y)]$ and $|t| \geq\left[\left(Q^{2}+m_{\pi}^{2}\right) /\left(2 y E_{\nu}\right)\right]^{2}[12,13]$. An alternate approach for calculating the cross section at low neutrino energies is to relate it to low $W$ (hadronic invariant mass) inclusive pion production [14-18].

Interest in coherent pion production has recently revived because of accelerator neutrino oscillation experiments [19-22] in which this reaction is a background to quasielastic neutrino-nucleon interactions when a $\pi^{0}$ or a $\pi^{ \pm}$is mistaken for an $e^{ \pm}$or proton, respectively. Recently, lowenergy experiments, K2K [23] and SciBooNE [24], did not observe coherent $\pi^{+}$production at neutrino energies $\sim 1 \mathrm{GeV}$ at the level predicted by the Rein-Sehgal model [4] as then implemented in the NEUT [6] and NUANCE [7] event generators. There is strong experimental evidence for coherent $\pi^{0}$ production at these energies [25,26].

In this Letter, we identify a sample of coherent $\pi^{ \pm}$ candidates from neutrino and antineutrino beams on a scintillator (primarily CH ) target by reconstructing the final-state $\mu^{\mp}$ and $\pi^{ \pm}$, allowing only minimal additional energy near the neutrino interaction vertex and requiring small $|t|$ as a signature of the coherent reaction. Noncoherent backgrounds are constrained with a sideband
with high $|t|$. In contrast to other low-energy measurements [23-28], which rely on selection in the pion kinematics or in $Q^{2}$, this approach uses only model-independent characteristics of coherent pion production and, therefore, allows a measurement of the distribution of pion energies and angles in coherent reactions to test the models.

The MINERvA experiment studies neutrinos produced in the NuMI beam line [29]. A beam of 120 GeV protons strike a graphite target, and charged mesons are focused by two magnetic horns into a 675 m helium-filled decay pipe. The horns focus positive (negative) mesons, resulting in a $\nu_{\mu}\left(\bar{\nu}_{\mu}\right)$ enriched beam with a peak neutrino energy of 3.5 GeV. This analysis uses data taken between October 2009 and April 2012 with $3.05 \times 10^{20}$ POT (protons on target) in $\nu_{\mu}$ mode and $2.01 \times 10^{20}$ POT in $\bar{\nu}_{\mu}$ mode.

The neutrino beam is simulated in a GEANT4-based model $[30,31]$ constrained to reproduce hadron production measurements on carbon by the NA49 and MIPP experiments [32,33]. Hadronic interactions not constrained by the NA49 or MIPP data are predicted using the FTFP hadron shower model [34]. The uncertainty on the prediction of the neutrino flux is set by the precision in these hadron production measurements, uncertainties in the beam line focusing system and alignment [35], and comparisons between different hadron production models in regions not covered by the NA49 or MIPP data.

The MINERvA detector consists of a core of scintillator strips surrounded by electromagnetic and hadronic calorimeters on the sides and downstream end of the detector [36,37]. The triangular $3.4 \times 1.7 \mathrm{~cm}^{2}$ strips are perpendicular to the $z$ axis and are arranged in hexagonal planes [38]. Three plane orientations, $0^{\circ}$ and $\pm 60^{\circ}$ rotations around the $z$ axis, enable reconstruction of the neutrino interaction point and the tracks of outgoing charged particles in three dimensions. The 3.0 ns timing resolution per plane allows the separation of multiple interactions within a single beam spill. MINERvA is located 2 m upstream of the MINOS near detector, a magnetized iron spectrometer [20] that is used in this analysis to reconstruct the momentum and charge of $\mu^{ \pm}$. The MINERvA detector's response is simulated by a tuned GEANT4-based [30,31] program. The energy scale of the detector is set by ensuring that both the photostatistics and the reconstructed energy deposited by momentum-analyzed through-going muons agree in data and simulation. The calorimetric constants used to reconstruct the energy of $\pi^{ \pm}$showers, and the correction for passive material are determined from the simulation [36].

To estimate backgrounds, neutrino interactions are simulated using the GENIE 2.6 .2 neutrino event generator [5]. For quasielastic interactions, the cross section is given by the Llewellyn Smith formalism [39]. Vector form factors come from fits to electron scattering data [40]; the axial form factor used is a dipole with an axial mass $\left(M_{A}\right)$ of $0.99 \mathrm{GeV} / c^{2}$, consistent with deuterium measurements
[41,42], and subleading form factors are assumed from PCAC or exact $G$-parity symmetry [43]. The nuclear model is the relativistic Fermi gas with a Fermi momentum of $221 \mathrm{MeV} / \mathrm{c}$ and an extension to higher nucleon momenta due to short-range correlations [44,45]. Inelastic, low $W$ reactions are simulated with a tuned model of discrete baryon resonance production [46], and the transition to deep inelastic scattering is simulated using the BodekYang model [47]. Hadronization at higher energies is simulated with the AGKY model [48], which is based on the gradual transition from KNO scaling to the LUND string model of PYTHIA with increasing $W$. Final-state interactions, in which hadrons interact within the target nucleus, are modeled using the intranuke package [5]. Uncertainties in the parameters of these models are assigned based either on measurement uncertainties from data or to cover differences between external data sets and GENIE's model.

The MINERvA detector [36] records the energy and time of energy depositions (hits) in each scintillator strip. Hits are first grouped in time, and then clusters of energy are formed by spatially grouping the hits in each scintillator plane. Clusters with energy $>1 \mathrm{MeV}$ are then matched among the three views to create a track. The $\mu^{ \pm}$candidate is a track that exits the back of MINERvA matching a track of the expected charge entering the front of MINOS. The most upstream cluster on the muon track is taken to be the interaction vertex. The resolution of each track cluster is 2.7 mm , and the angular resolution of the muon track is better than 10 mrad in each view. The reconstruction of the muon in the MINOS spectrometer gives a typical muon momentum resolution of $11 \%$. Event pileup causes a decrease in the muon track reconstruction efficiency, which was studied in both MINERvA and MINOS by projecting tracks found in one detector to the other and measuring the misreconstruction rate. This results in a $-7.8 \%$ ( $-4.6 \%$ ) correction to the simulated efficiency for muons below (above) $3 \mathrm{GeV} / \mathrm{c}$.

The interaction vertex is restricted to be within the central 108 planes of the scintillator tracking region and no closer than 22 cm to any edge of the planes. These requirements define a region with a mass of 5.47 metric tons. In the antineutrino exposure, $45 \%$ of the POT were taken during the construction of the MINERvA detector and, therefore, only used a fraction of the downstream tracker, with a fiducial volume of 56 planes and a mass of 2.84 metric tons.

Charged $\pi^{ \pm}$reconstruction requires a second track originating from the vertex. The angular resolution on this shorter track has a narrow central distribution with a full width at half maximum of 17 mrad ; however, the distribution has long tails due to pion scattering in the scintillator and has an rms resolution of 160 mrad in each view. For the neutrino beam, in which CCQE events with a proton misidentified as a $\pi^{+}$are a background, $d E / d x$ along
the track is required to be inconsistent with that expected from a proton ranging out in the detector. This cut removes $64 \%$ of protons in the simulation while retaining $95 \%$ of $\pi^{ \pm}$. The energy of the charged pion is reconstructed calorimetrically with a fractional resolution of $18 \%+8 \% / \sqrt{E_{\pi} / \mathrm{GeV}}$, and it is this resolution that dominates the experimental resolution on $|t|$. From the measured muon and pion energies and directions,

$$
\begin{align*}
|t| & =\left|\left(p_{\nu}-p_{\mu}-p_{\pi}\right)^{2}\right| \\
& \approx\left(\sum_{i=\mu, \pi} E_{i}-p_{i, L}\right)^{2}+\left|\sum_{i=\mu, \pi} \vec{r}_{i, T}\right|^{2}, \tag{2}
\end{align*}
$$

where the approximation made is that zero energy is transferred to the recoil nucleus and where $\vec{p}_{T}$ and $p_{L}$ are the transverse and longitudinal momenta with respect to the known neutrino beam direction.

By definition, a coherent reaction produces a $\mu^{\mp}$, a $\pi^{ \pm}$, and nothing else originating from the interaction vertex. Vertex energy is defined as all energy deposited within five planes of the plane in which the neutrino interacts in strips within 20 cm of the interaction vertex. Energy deposited on the muon and pion tracks is corrected for path length in the bars. For coherent events, this results in a vertex energy of 50 MeV with an rms spread of 10 MeV due to fluctuations in energy deposited by the muon and pion. Background processes typically leave significantly more energy in this region, and this analysis requires the reconstructed vertex energy to be between 30 and 70 MeV . This requirement removes $85 \%(86 \%)$ of the predicted background in the $\nu_{\mu}\left(\bar{\nu}_{\mu}\right)$ measurement and keeps $87.0 \%(86.7 \%)$ of the coherent pion events.

As shown in Fig. 2 (top), after the vertex energy requirement, the simulation exceeds the background at high $|t|$. The incoherent background components are divided into categories based on $W$, and scale factors for the background are estimated by fits to the distributions of $\pi^{ \pm}$energies for events with $0.2<|t|<0.6(\mathrm{GeV} / c)^{2}$. As shown in Table I the fit reduces the predicted background, particularly at low $W$. The reconstructed $|t|$ distribution after background tuning is shown in Fig. 2 (bottom), and a significant excess of low $|t|$ events over the backgroundonly prediction is observed. The scaled background is then subtracted from the events with $|t|<0.125(\mathrm{GeV} / c)^{2}$ to measure the rate of coherent events in the data. There are 1628 and 770 coherent candidates after background subtraction in the neutrino and antineutrino samples, respectively.

The cross section is determined by $\sigma=N_{\text {coh }} / \Phi N_{{ }^{12} \mathrm{C}}$, where $\Phi$ is the total flux of neutrinos incident on the detector. Our scintillator has free protons in numbers equal to the ${ }^{12} \mathrm{C}$ nuclei. GENIE does not simulate the diffractive production of pions from the free protons that might also produce events at low $|t|$. There is no microphysical


FIG. 2. (Top) pion energy distribution for events in the $0.2<|t|<0.6(\mathrm{GeV} / c)^{2}$ sideband, $\nu_{\mu}$ (left) and $\bar{\nu}_{\mu}$ (right) beams and (bottom) reconstructed $|t|$ after background tuning using the sideband. The signal distribution in $|t|$ peaks near zero with its shape dominated by detector resolution.
calculation of this process at our energies. An inclusive calculation of $\stackrel{(-)}{\nu} p \rightarrow \mu^{ \pm} \pi^{\mp} p$ based on $\pi A$ elastic scattering data and the Adler relation [1,49], shows a modest low $|t|$ enhancement not seen in GENIE that falls exponentially with $|t|$. This difference does not identify diffractive events but instead includes all low $|t|$ enhancements in scattering from protons that might be in this calculation. Moreover, most events with $|t|>0.05 \mathrm{GeV}^{2}$ would not pass our vertex energy requirement because of the recoiling proton's ionization. We estimate the acceptance of these low $|t|$ events to be $\approx 20 \%$ of the acceptance for coherent events on carbon. On the basis of this low $|t|$ enhancement and our acceptance, the event rate in our data would be equivalent to $7 \%(4 \%)$ of the GENIE prediction for the coherent cross section on ${ }^{12} \mathrm{C}$ for neutrinos(antineutrinos). We do not correct our result for this possible enhancement.

We measure flux-averaged cross sections of $[3.49 \pm 0.11$ (stat) $\pm 0.37$ (flux) $\pm 0.20$ (other sys.) $] \times 10^{-39}$

TABLE I. Scale factors and their statistical uncertainties determined for different background sources, grouped by hadronic invariant mass $W$ from the high $|t|$ sidebands.

| Source of background | $\nu_{\mu}$ | $\bar{\nu}_{\mu}$ |
| :--- | :---: | :---: |
| Charged current quasielastic | $0.7 \pm 0.3$ | 1 (fixed) |
| Nonquasielastic, $W<1.4 \mathrm{GeV}$ | $0.6 \pm 0.3$ | $0.7 \pm 0.1$ |
| $1.4<W<2.0 \mathrm{GeV}$ | $0.7 \pm 0.1$ | $0.6 \pm 0.1$ |
| $W>2.0 \mathrm{GeV}$ | $1.1 \pm 0.1$ | $1.9 \pm 0.3$ |

and $\quad(2.65 \pm 0.15$ (stat) $\pm 0.31$ (flux) $\pm 0.30$ (other sys.) $) \times$ $10^{-39} \mathrm{~cm}^{2}$ per ${ }^{12} \mathrm{C}$ nucleus in the neutrino and antineutrino beams, respectively. The fluxes of neutrinos and antineutrinos in this analysis are given in the Supplemental Material [50]. In cross sections as a function of $E_{\nu}, E_{\pi}$, and $\theta_{\pi}$, the effect of detector resolution is accounted for by using iterative Bayesian unfolding [51,52]. Figure 3 shows the measured cross sections as a function of $E_{\nu}$ compared with previous measurements for $E_{\nu}<20 \mathrm{GeV}$ and with the neut [6] and Genie [5,53] implementations of Rein and Sehgal [4] with lepton mass corrections [12].

The main sources of systematic uncertainty on the cross sections are the flux, the background interaction model, pion interactions in the detector, muon reconstruction, muon and hadron energy scale, vertex energy, and the model used in the sideband constraint for the background. These systematic uncertainties are shown in Table II. The uncertainty of hadron interactions in the detector as predicted by GEANT4 on tracking and energy measurements is evaluated by varying the pion and proton total inelastic cross sections by $\pm 10 \%$ and the neutron mean free path as a function of kinematic energy by $10-25 \%$ to span differences between GEANT4 and hadron scattering data [58-69].

For muons reconstructed by range in MINOS, the muon energy scale uncertainty is dominated by energy loss uncertainties, and we compared range and curvature measurements to evaluate uncertainties on the reconstruction of muons by curvature in the MINOS magnetic field. Uncertainties in the hadron energy reconstruction result from uncertainties in the energy scale set by muon energy deposition, material composition and dimensions, saturation of ionization in the scintillator, and photosensor cross talk and nonlinearity. Comparisons with the test beam [36] limit the energy scale uncertainty for pions (protons) to $5 \%(3 \%)$. The target mass is uncertain to $1.4 \%$.


FIG. 3 (color online). $\sigma\left(E_{\nu}\right)$ for neutrino (left) and antineutrino (right) coherent $\pi^{ \pm}$production. The inner error bars in the cross section represent statistical uncertainties, and the outer error bars represent the total uncertainties; the cross section is tabulated in the Supplemental Material [50]. Results from other measurements [23,24,28,54-57] are scaled to carbon using the predicted $A^{1 / 3}$ dependence of the Rein-Sehgal model [4].

TABLE II. Fractional systematic uncertainties on $\sigma\left(E_{\nu}\right)$ and $\sigma\left(E_{\bar{\nu}}\right)$ associated with flux (I), neutrino interaction models (II), detector simulation (III), vertex energy (IV), and (V) sideband model. The final column shows the total systematic uncertainty due to all sources.

|  | $E_{\nu(\bar{\nu})}(\mathrm{GeV})$ | 1 | II | III | IV | V | Total |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\nu$ | 1.5-2.0 | 0.101 | 0.041 | 0.031 | 0.017 | 0.002 | 0.115 |
|  | 2.0-3.0 | 0.108 | 0.058 | 0.040 | 0.034 | 0.020 | 0.135 |
|  | 3.0-4.0 | 0.099 | 0.053 | 0.041 | 0.037 | 0.027 | 0.127 |
|  | 4.0-5.0 | 0.163 | 0.046 | 0.040 | 0.038 | 0.029 | 0.180 |
|  | 5.0-7.0 | 0.146 | 0.031 | 0.034 | 0.034 | 0.023 | 0.159 |
|  | 7.0-9.0 | 0.118 | 0.027 | 0.034 | 0.026 | 0.016 | 0.129 |
|  | 9.0-11.0 | 0.132 | 0.034 | 0.044 | 0.029 | 0.019 | 0.147 |
|  | 11.0-15.0 | 0.132 | 0.022 | 0.034 | 0.021 | 0.014 | 0.140 |
|  | 15.0-20.0 | 0.128 | 0.015 | 0.022 | 0.013 | 0.009 | 0.132 |
| $\bar{\nu}$ | 1.5-2.0 | 0.216 | 0.497 | 0.309 | 0.308 | 0.111 | 0.704 |
|  | 2.0-3.0 | 0.135 | 0.144 | 0.075 | 0.027 | 0.030 | 0.215 |
|  | 3.0-4.0 | 0.100 | 0.095 | 0.065 | 0.021 | 0.026 | 0.156 |
|  | 4.0-5.0 | 0.191 | 0.138 | 0.105 | 0.036 | 0.048 | 0.265 |
|  | 5.0-7.0 | 0.164 | 0.065 | 0.073 | 0.025 | 0.028 | 0.194 |
|  | 7.0-9.0 | 0.140 | 0.043 | 0.056 | 0.017 | 0.019 | 0.158 |
|  | 9.0-11.0 | 0.148 | 0.038 | 0.048 | 0.014 | 0.015 | 0.161 |
|  | 11.0-15.0 | 0.157 | 0.016 | 0.024 | 0.008 | 0.006 | 0.160 |
|  | 15.0-20.0 | 0.154 | 0.052 | 0.066 | 0.017 | 0.024 | 0.178 |

Uncertainties in predictions for the noncoherent background from the GENIE generator are evaluated by varying the underlying model tuning parameters according to their uncertainties [5]. The most important parameters are the normalization and axial form factor for baryon resonance production. MINERvA's measurements of the CCQE process $[70,71]$ show that GENIE does not model the energetic final-state proton multiplicity well, which in turn means a mismodeling of the vertex energy. The resulting uncertainty is estimated by turning on and off the addition of energy deposited by a $20-225 \mathrm{MeV}$ final-state proton to the vertex energy of $25 \%$ of background events with a target neutron. Finally, after tuning the background, we find remaining disagreement in the sideband $\theta_{\pi}$ distribution. This disagreement is corrected, and the size of the correction is taken as a systematic uncertainty. The effects of these model variations are reduced by sideband tuning of the background.

Figure 4 compares the flux-averaged differential cross sections as a function of pion energy and angle against the Rein-Sehgal model [4] as implemented in GENIE [5,12] and NEUT [6]. Disagreement at high $\theta_{\pi}$ is evident in both GENIE and neut. In GENIE, whose behavior is more similar to the data, the model predicts $\sim 15 \%$ of the cross section with $\theta_{\pi}>45^{\circ}$ but there is no evidence for such events in the data.

In conclusion, the coherent production of pions on carbon nuclei for both neutrino and antineutrino beams is precisely measured by isolating a sample with no visible nuclear breakup and low $|t|$ transferred to the nucleus. This


FIG. 4 (color online). $\quad d \sigma / d E_{\pi}$ (top) and $d \sigma / d \theta_{\pi}$ (bottom) for $\nu_{\mu}$ (left) and $\bar{\nu}_{\mu}$ (right) with error bars as in Fig. 3 compared against predicted cross sections from GENIE [5] and NEUT [6]. These cross sections are tabulated in the Supplemental Material [50].
allows a study of produced pion kinematics independent of the details of the signal model. The cross sections of the neutrino and antineutrino coherent pion production are similar, indicating that the reaction is likely to be primarily an axial vector process. The discrepancies observed at neutrino energies relevant for the T2K oscillation experiment [21] suggest that these data should be used to revise the predictions of neutrino interaction models used in future measurements.

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