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# Water residence time in Chesapeake Bay for 1980-2012

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1	Water residence time in Chesapeake Bay for 1980-2012
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15 Abstract: Concerns have grown over the increase of nutrients and pollutants discharged into the estuaries and coastal seas. The retention and export of these materials inside a 16 system depends on the residence time (RT). A long-term simulation of time-varyingRT 17 of the Chesapeake Bay was conducted over the period from 1980 to 2012. The 33-year 18 simulation results show that themeanRT of the entire Chesapeake Bay system ranges from 19 110 to 264 days, with an average value of 180 days. The RT was larger in the bottom 20 layers than in the surface layers due to the persistent stratification and estuarine 21 circulation. A clear seasonal cycle of RT was found, with a much smallerRT in winter 22 23 than in summer, indicating materials discharged in winter would be quickly transported out of the estuary due to the winter-spring high flow. Large interannual variability of the 24 RT was highly correlated with the variability of river discharge ( $R^2=0.92$ ). The monthly 25 variability of RT can be partially attributed to the variability of estuarine circulation. A 26 strengthened estuarine circulation results in a larger bottom influx and thus reduces the 27 RT. Wind exerts a significant impact on the RT. The upstream wind is more important in 28 controlling the lateral pattern of RT in the mainstem. 29

30

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Key words: residence time, Chesapeake Bay, water exchange, estuarine circulation, wind,
 river discharge

#### 35 **1.Introduction**

36 Concerns have grown over the increase of nutrients and other pollutants discharged into the estuaries and coastal seas(Nixon, 1995; Paerl et al., 2006; Smith et al., 1999). 37 These substances have deleterious effects on aquatic organisms and human health 38 through the food chain (Kennish, 1997). Due to the increase of anthropogenic nutrient 39 input, many estuaries and coastal seas have become more eutrophic over the past few 40 decades (Carpenter et al., 1998; Kemp et al., 2005; Murphy et al., 2011; Nixon, 1995). 41 The ecological responses of a waterbody to increased nutrient loads have been widely 42 linked to the flushing capability of the system (Boynton et al., 1995; Josefson and 43 44 Rasmussen, 2000; Monbet, 1992). The available nutrient supply for algae growth and bloom is determined not only by the nutrient loads, but also by the retention of nutrients, 45 which is related to the residence time (RT) of a system (Nixon et al., 1996). For example, 46 47 coastal eutrophication has been built up in Koljo Fjords because of slow water exchange, even though there are no significant nutrient loads (Lindahl et al., 1998; Nordberg et al., 48 2001; Rosenberg, 1990). The export rate of nutrients proved to bestrongly negatively 49 related with the RT(Dettmann, 2001; Nixon et al., 1996). The RT is thus a key parameter 50 in quantifying the impact of hydrodynamics on biochemical processes in an estuary 51 (Boynton et al., 1995; Cerco and Cole, 1992). In addition, from a management perspective, 52 it is essential to know the timescale for a pollutant discharged into a water body to exit 53 the system. Therefore, it is of importance to study the flushing capacity and water 54 55 exchange for an estuary.

To quantify the flushing capacity, several transport timescaleshave been used. Among
them, flushing time, RT, and water age are the three fundamental concepts of transport

58 time (Alber and Sheldon, 1999; Bolin and Rodhe, 1973; Hagy et al., 2000; Huang et al., 2010; Liu et al., 2004; Liu et al., 2008; Shen and Haas, 2004; Shen and Wang, 2007). 59 Flushing time is regarded as a bulk or integrative property that describes the overall 60 exchange or renewal capability of a waterbody (Dyer, 1973; Geyer et al., 2000; Officer, 61 1976; Oliveira and Baptista, 1997). The age of a water parcel is defined as the time 62 63 elapsed since the parcel departed the region in which its age is defined to be zero (Deleersnijder et al., 2001; Takeoka, 1984; Zimmerman, 1976). The RTof a water parcel 64 is defined as the time needed for the water parcel to reach the outlet (Zimmerman, 65 66 1976) and thus can be regarded as the remainder of the lifetime of a water parcel in a waterbody(Takeoka, 1984). Age and RT can be applied not only to steady-state cases, but 67 also to time-varying cases(Deleersnijder et al., 2001; Delhez, 2005; Takeoka, 1984). 68 Although flushing time can be used to estimate the overall flushing capability of a 69 waterbody, the steady-state approach does not provide spatial and temporal variations in 70 a large estuary, especially in a partially mixed estuary (e.g., Chesapeake Bay), where the 71 transportcould vary substantially in different regions and different vertical layers. The 72 transport process for a substance in an estuary has large variability due to the time-73 74 varying estuarine dynamics. It is desirable to know the spatial pattern of the RT and its temporal variation, which can be applied to determine the impact of hydrodynamics on 75 biogeochemical processes and be used for environmental assessment. 76

The water RT of Chesapeake Bay, the largest estuary in the United States, was not welldocumented. The RT of the Bay's tributaries was calculated using box model or efolder time (e.g., Hagy et al., 2000; Shen and Haas, 2004). Hagy et al. (2000) calculated the RT in Patuxent River, one main tributary of Chesapeake Bay, using a box model and

81 found the control of residence time from the head to its mouth changed from primarily river flow to the intensity of gravitational circulation. The spatially averaged RT of 7.6 82 months in Chesapeake Bay was estimated in a numerical model using e-folder 83 time(Nixon et al., 1996). The spatial pattern of transport time in the Bay's mainstemwas 84 initially investigated by Shen and Wang (2007) using the concept of freshwater age. 85 Theyfound that it requires 120-300 days for a marked change in the characteristics of the 86 pollutant source discharged into the Bay from the Susquehanna River to affect 87 significantly the conditions near the Bay mouth for selected wet and dry years. However, 88 89 the spatial variation and long-term temporal variation of the RT still remained largely unknown. 90

Here we aim to investigate the spatial pattern and long-term temporal variability of the
RT in Chesapeake Bay. A long-term numerical simulation of the RT from 1980 to 2012
in Chesapeake Bay was conducted for the first time using a robust algorithm developed
by Delhezet al. (2004). The seasonality and interannual variability of RT will be
examined. Finally, the main factors controlling the variation of RT will be discussed,
including river discharge, estuarine circulation and wind.

97 2.Methods

#### 98 2.1 RT calculation

The RT is often computed using a particle tracking method by injecting some particles at a fixed time, following the path of these particles, and registering the time when they leave the domain of interest (Gong et al., 2008; Monsen et al., 2002). Another method to calculate the RT is to use the remnant function approach proposed by Takeoka(1984), by

103 integrating the model-calculated tracer concentration timeseries to give a mean RT(Wang et al., 2004; Wang and Yang, 2015). With both approaches, the RT depends on the 104 release time and different values of RT will be obtained if particles or tracers are released 105 106 at different times, such as high tide or low tide (Brye et al., 2012). In order to obtain a mean RT for a period, many releases are required with regard to the changing current 107 condition (Monsen et al., 2002). They are not computationally efficient, and therefore it 108 is difficult to evaluate the long-term temporal variation of RT. Delhezet al. (2004) 109 proposes an adjoint method to compute the RT. The method provides variations of RT in 110 111 space and time with a single model run. The method does not require any Lagrangian module. It is based on an Eulerian algorithm that makes it more appropriate for long-term 112 and large-scale simulations than the straightforward Lagrangian approach (Delhez, 2005). 113

114 According to the approach of Delhezet al.(2004), the mean RT, denoted by  $\theta$  as a

function of time t and location x, can be computed using the adjoint equation expressed as,

116 
$$\frac{\partial \theta(t,x)}{\partial t} + \delta_{\omega}(x) + v \cdot \nabla \overline{\theta(t,x)} + \nabla \cdot [\kappa \cdot \nabla \overline{\theta(t,x)}] = 0 \quad (1)$$

117 where *v* is the velocity vector,  $\kappa$  is the symmetric diffusion tensor and

118 
$$\delta_{\omega}(x) = \begin{cases} 1 & if \quad x \in \omega \\ 0 & if \quad x \notin \omega \end{cases} (2)$$

119 where  $\omega$  is the domain of interest. At the boundary of the domain of interest  $\theta = 0$  is 120 used, which ensures the residence time to vanish at the boundary for the first time the 121 water parcel hits the boundary and the computed residence time is the same as the 122 residence time computed using Lagrangian method (Delhez and Deleersnijder, 2006;

123	Blaise et al., 2010). For stability reasons, the adjoint equation must be integrated
124	backward in time with the reversed flow, i.e. velocity vector v changed to $-v$ . The
125	backward procedure is also necessary because one does not know in advance the fate of
126	the particles (Delhez, 2005). In order to calculate the mean RT, two steps were required.
127	In the first step, the hydrodynamic model was used to generate the velocity and
128	turbulence fields, and the intermediate results were saved every half-hour. We ran a
129	hydrodynamic model from 1979 to 2014 and obtained 35years (1980-2014) of
130	hydrodynamic fields. The first year of 1979 was used to spin-up the model and not used
131	to calculate the RT. In the second step, Eq. 1 was integrated backward with the
132	interpolated hydrodynamic field at each time step based on the hydrodynamic field saved
133	in the first step, running from the end of 2014 to the beginning of 1980. The model
134	experiments showed that it takes about 1.5 years for the RTto reach a stable value in
135	Chesapeake Bay. Therefore, results of RT in the last two years (i.e., 2013 and 2014) were
136	not used and only the RTvalues of 1980-2012were used for analysis.
137	In this study, we set the boundary of the domain of interest at the mouthof the Bay
138	and computed the RT at any location <i>x</i> and time <i>t</i> inside the Bay. $\theta(t, x) = T$ denotes that
139	particles released at location $x$ and time $t$ will be transported to the mouth of the Bay for a
140	period of <i>T</i> . In other words, RT is determined by the hydrodynamics after the release.
141	Notes that the domain of interest in this study included the tributaries (Fig. 1b). As
142	freshwater discharges into estuary at its headwater, which would lead to a non-zero RT
143	value at the headwater due to the fact that water parcelsreleased at the headwater of
144	tributaries will not return and hit theupstream boundary.

# **2.2 Simulation of the hydrodynamics**



Fig. 1. (a) Bathymetry of the numerical model; (b) domain of interest (blue grid), the
deep channel section (green line), middle Bay cross-section (red line), and Station s1, s2
and s3 (red triangle)

151

147

152 A numerical model based on the Environmental Fluid Dynamics Code (EFDC)

153 (Hamrick, 1992) was used to simulate the hydrodynamics. EFDC uses a boundary-fitted

154 curvilinear grid in the horizontal and sigma grids in the vertical. The EFDC model used

155 for the Chesapeake Bay was also referred to as the HEM-3D model (Hong and Shen,

156 2012, 2013; Du and Shen 2015). The same model was used for this study with the same

- model configuration and boundary condition. A grid with a horizontal dimension of
- $158 \quad 112 \times 240$  and 20 layers in the vertical was deployed (Fig. 1). The model was forced by

- interpolated observed tide at the open boundary (http://tidesandcurrents.noaa.gov),
- 160 freshwater discharges of eight main tributaries (http://waterdata.usgs.gov/nwis/), and
- 161 wind obtained from the North American Regional Reanalysis (NARR) produced at the
- 162 National Center for Environmental Prediction
- 163 (http://www.esrl.noaa.gov/psd/thredds/catalog/Datasets/NARR/pressure/catalog.html).Th
- is model has been calibrated for tidal and non-tidal surface elevation, current, and salinity
- 165 for the Chesapeake Bay from 1999-2008 and it has simulated reliable stratification and
- destratification responses temporally and spatially in both wet and dry years (Hong and
- 167 Shen, 2012, 2013). Details of model calibration can be found in Hong and Shen (2012).
- 168 We ran the model from 1979 to 2014, and saved the half-hourly hydrodynamic results,
- 169 which were then used to calculate the RT with the adjoint method described above.

#### 170 **3. Results**

## 171 **3.1 Mean RT of Chesapeake Bay**

172 The mean RT of Chesapeake Bayaveraged over the period from 1980 to 2012 is 173 presented in Fig. 2. The spatially and vertically averaged RTvalue of the entire Chesapeake Bay system for 1980-2012 was180 days, shorter than 7.6-month reported in 174 Nixon et al. (1996). It was larger than the flushing time estimated by calculating the ratio 175 of freshwater volume to freshwater flow, which ranged from 90 to 140 days (Goodrich, 176 1988; Kemp et al., 2005; Shen and Wang, 2007). The difference was due to the fact that 177 the flushing time estimation previous studies was actually the mean renewal time of 178 freshwater while the RT in this study includedrenewal of both the freshwater and saline 179 water. Hong and Shen(2012) estimated the RTby releasing dye at the beginning of the 180

model run and using the e-folder method to determine the RT for a typical mean flow
year. Their results suggested that the mean RT in a mean flow year was about 175
days,which is consistent with our results.



Fig. 2. Vertical mean (a), bottom (b), and surface (c) residence time (days) averaged
over 1980-2012; (d) difference between the bottom and surface residence time, positive
denoting larger residence time in bottom layers.

189

190 Considering the entire Chesapeake Bay as a box, the ratio of total water volume *V* to the 191 mean residence time  $T_R$  can be regarded as the total effective outflow of the system,  $Q_{out}$ . 192 For a steady state condition, the total effective outflow should equal the total influx of 193 "clean" water, which has two sources, river freshwater discharge *R* and influx of "clean" 194 water from the outside of the Bay  $Q_{in}$ . Here the clean water from the outside of the Bay 195 refers to the water that was not transported out of the Bay during the previous ebb tide.

196 
$$Q_{out} = V/T_R = Q_{in} + R$$
 (3)

Based on the simulation of the past 3 decades, the mean  $Q_{out}$  is about 4800 m<sup>3</sup>/s, given the volume of the entire Chesapeake Bay system V of  $7.5 \times 10^{10}$  m<sup>3</sup> and  $T_R$  of 180 days. The total mean freshwater discharge from all the rivers R was about 2200 m<sup>3</sup>/s. Therefore,  $Q_{in}$  is about 2800 m<sup>3</sup>/s, which is of the same order of magnitude as the influx at the Bay mouth measured by Wong and Valle-Levinson (2002). This estimation suggests that the influx of coastal ocean water is as equally important as the freshwater discharge on the water renewal in Chesapeake Bay.

There was a clear longitudinal pattern of the RT. The vertical mean RT ranges from0 to 200 days in the lower Bay (37-38N), 200-240 days in the middle Bay (38-39N), and 240-280 days in the upper Bay(39-39.6N) (Fig. 2a). The gradient of RT was larger in the

207 lower Bay than that in the middle-upper Bay. It took about 200 days to transport a water parcel from the Potomac River mouth (~38N) to the Bay mouth (~37N), while it took 208 only 260 days to transport a parcel from the head of the Bay (~39.5N) to the Bay mouth. 209 The lateral distribution of vertical mean RT was different in different regions. The 210 lateralasymmetry of the vertical mean RT in the lowerBay was significant, with a much 211 largerRT in the eastern bank than that in the western bank (Fig. 2a). The difference could 212 be as large as 80days. The lateral asymmetries could be attributed to several factors, such 213 as lateral shearing of the gravitational circulation (Valle-Levinson et al., 2003), the 214 largefreshwater dischargefrom the western tributaries(e.g., Potomac River, York River, 215 216 and James River), and the strengthened ebb flow along the western boundary due to Coriolis force. The lateral pattern was similar in both surface and bottom layers in the 217 lower Bay. In the middle to upper Bay, the vertical mean RT waslarger in the deep area 218 219 than in the shallow region, which was caused by a larger bottom RT in the deep channel due to the typical gravitational circulation with flow in the deep channel directed to the 220 upstream. 221

The vertical patternof the RT can be examined by averaging the RT for the surface and 222 the bottom, respectively (Figs. 2b, 2c). The surface RT is the RT averaged over the 5 223 224 layers near the surface, and the bottom RT is the RT averaged over the 5 layers near the bottom. The bottom and surface RT, and their difference were presented in Figs. 2b-d, 225 and the vertical profile along the deep channel section was shown in Fig. 3. The gradient 226 of RT was much larger in the bottom layers than in the surface layers, especially in the 227 228 deep channel section (Figs. 2, 3). The mean bottom RT of the Bay's mainstemwas about 184 days and the mean surface RT was about 145 days. There were minor vertical 229

differences in the upper Bay and shallow banks, where the water was well-mixed and the
vertical difference was less than 10 days (Fig. 2d). Vertical differences were significant in
the lower to middle Bay, especially in the deep channel where differences had a range of
20-100 days. The maximum vertical difference was found in the deep channel outside of
the Rappahannock River mouth (~37.75N).

235



236

Fig. 3. Vertical profile of residence time (days) along the deep channel section.

238

# 239 3.2 Seasonal cycle of RT

240 The vertical mean RTof the entire Bayexhibited a clear seasonal cycle, with its largest

value in summer (Jun.-Aug.) and smallest value in Nov.-Jan. This seasonal cycle

- suggested that winter has a short retention time for soluble materials. In contrast, material
- released in the summer usually has the longest retention time in the Bay. The minimum
- 244 RT during the winter was mainly due to large freshwater discharge during ensuing

months (e.g. Mar. and Apr.), which caused a large downstream residual current during
this high-flow period (Fig. 4b-c). TakingSusquehanna River as an example, the river
discharge usually peaked in March and troughed in August, which was consistent with
the downstream residual current averaged over the Bay's mainstem.

249



Fig. 4. (a) Seasonal cycle of residence time averaged over the entire Bay; (b) seasonal cycle of Susquehanna River flow; (c) seasonal cycle of vertically mean residual along estuary currentaveraged over the Bay's mainstem. Red lines denote medians of the 33 years of record from 1980 to 2012, blue rectangles denote the first and third quartiles, dashed lines denote the upper and lower whiskers, and red crosses denote the outliers.

256

250

RT values during January and Julywereselected to represent the seasonal minimumand
maximum RT (Fig. 5a-b). In the middle to upper Bay,a small area had RT values larger
than 240 days in January (Fig. 5a), while the major area had RT values exceeding 240
days and some areas hadRT even exceeding 280 daysin July (Fig. 5b). The difference

261 between July and JanuaryRT could be larger than 50 days in the upper Bay, 20-40 days in the middle Bay, and 0-40 days in the lower Bay (Fig. 5c). The seasonaldifferencewas 262 highly asymmetrical between the eastern and western banks in the lower Bay (Fig. 5c). 263 264 The seasonal differencealong the western bank of the lower Bay was usually less than 10 days, but it could be as large as 40 days along the eastern bank. A similar pattern of 265 seasonal difference was found for both bottom and surface layers (not shown). Little 266 seasonal difference of the RT in the western bank of the lower Bay was related to the 267 dominating role of frequent tidal exchange in this area. The tidal current (0-100 cm/s) had 268 a much larger magnitude than the residual current (1-2.5cm/s, Fig. 4c) induced by the 269 river discharge. The dominating ebb current and large influence of the tide caused the 270 persistently small RT and little seasonal difference along the western bank near the Bay 271 272 mouth. The tidal effect decreased in the middle and upper Bay, where the river discharge became more influential on the variation of RT. 273



Fig. 5.Vertical mean residence time (days) averaged over 1980-2012 in January (a)

and July (b); (c) difference between July and January vertical mean residence time,

278 positive value denoting larger residence time in July.

279

## 280 **3.3Interannual variation of RT**

There was high interannual variability of the RT. The vertical mean RT of the entire Bay had a standard deviation of 30 days over the period of 1980-2012. The maximum and minimumof the vertical mean RT averaged over the entire Baywere264days and 110days, respectively (Fig. 6). No significant trend of the RT was found during the past 3 decades. There were several particularly high RT years with a yearly mean RT larger than 200 days, e.g., 1980, 1987, 1988, 1991, 1998, 1999, 2000 and 2001 (Fig. 6). The

maximum RT occurred in 2001, and the minimum RT occurred in 2003-2004.

288



Fig. 6.Time series of vertical mean residence time averaged over the entire Bay for
1980-2012; bar plot indicates the yearly mean.

293	Since the RT highly depends on sub-tidal transport processes, the status of the
294	stratification, and the residual current field, we hypothesized that part of the RT variation
295	was related to the pre-existing condition. Regressions between the RT of a given season
296	and the RT of the following season were conducted. The regressions demonstrated that
297	the interannual variation of the previous season accounted for a large portion of
298	interannualvariation of the RT in the following season (Fig. 7). However, the impact of
299	the pre-existing condition varied from season to season. A stronger effect of the pre-
300	existing condition occurred in the fall and winter with an R <sup>2</sup> value larger than 0.82,
301	followed by summer with an $R^2$ value of 0.72. The effect of the pre-existing condition was
302	relativelyweaker in the spring, as the winter RT variation accounted for only 68% of
303	spring RT variation. The weaker effect of the pre-existing condition in the spring could
304	be attributed to the high variability of the spring river discharge.



306

Fig. 7.Regression of the residence time between winter and spring (a), spring and
summer (b), summer and fall (c), fall and winter (d). The linear regression coefficient is
shown in text.Spring (Mar.-May), summer (Jun.-Aug.), fall (Sep.-Nov.), and winter
(Dec.-Feb.).

311

# 312 4. Discussion

# 313 4.1 Relationship between RT and river flow

Even though the variation of RT is generally believed to behighly controlled by

theriverdischarge (Hagy et al., 2000; Shen and Haas, 2004), it is of interest to examine

the relative importance of river discharge on the RT over different timescales (e.g. 316 monthly, yearly), and to examine the mean delay between RT and river discharge. We 317 chose the river discharge of Susquehanna River to represent the total river discharge, 318 319 since the discharge of Susquehanna River accounts for 51% of the total discharge and river discharges from other rivers are usually proportional to it (Guo and Valle-Levinson, 320 2007). The Susquehanna River daily discharge time series was extracted from the USGS 321 website (http://waterdata.usgs.gov/nwis). The linear regression between the yearly mean 322 RT and the inverse of the yearly mean river flow (without smoothing) has a correlation 323 coefficient  $R^2$  of 0.67 (Fig. 8). 324

325



326

Fig.8.Linear regression coefficient R<sup>2</sup> between the interannual variation of vertical
mean residence time averaged over the entire Bay and the interannual variation of shifted
Susquehanna River flow, x-axis denoting the shifting days of flow.

331 To estimate the delay between river flow and RT, a series of regressions between the yearly mean RT and the inverse of yearly mean flow of the Susquehanna Riverwere 332 conducted, in which the flow (smoothed or unsmoothed) was shifted by different 333 numbers of days. A moving average of 360 days was applied to the flow in order to 334 remove the seasonal frequency. The result showed that the best relation was found when 335 the flow wassmoothed and shifted by83 days, with an R<sup>2</sup>value of 0.92 (Fig. 8). Without 336 smoothing, the largest  $R^2$  value was 0.84 when the flow was shifted by 108 days (Fig. 8). 337 It should be noted that a shift of 83 days meant that the RT of a given time was 338 339 determined by the flow condition afterthat given time, instead of prior. For instance, the yearly mean RT for 1980 (t=0-365 days) is determined by the yearly mean river 340 discharge of 83-448 days. 341

The best relation between yearly mean RT (days) averaged over the entire Bay and the inverse of yearly mean flow (m<sup>3</sup>/s) was shown in Eq. 4, where the flow wasmoving averagedby 360 days and shifted by 83 days(Fig. 9a).

345 
$$RT = 118,813 / flow + 69.3, R^2 = 0.92, N = 33$$
 (4)

This significant relationship suggests that, when itwas averaged yearly, the RT is mainly controlled by river discharge and other factors (e.g. wind, tide) have little impact. However, for a shorter period, the river discharge accounts for a much less percentage of the variation of the RT. Even by shifting the flow by 83 days and applying a moving average of 360 days, the river discharge accounts for 78% of the monthly mean RT variation (Fig. 9b). Without smoothing of the river flow, there is no significant relation between the monthly RT and the monthly flow, with the largest R<sup>2</sup>ofonly 0.22. This can

353 be understood as the variation of RT was between 110-264 days, and the RT depends on the accumulative effect of river flow and other factors (e.g., tide, wind, and the pre-354 existing condition) for a period of more than 110 days. A short-term pulse of river flow 355 does not necessarily result in a significant change of RT, as the impact of the pulse can be 356 confounded by varied flow conditions in the following days. Even though there were 357 usually multiple pulses of high flow in each year, including short-term pulses (e.g., 358 during storm periods in the summer), there was usually only one peak and one trough of 359 RT in each year (Fig. 6). 360

361



**Fig. 9.**(a) Regression between interannual variation of yearly mean residence time averaged over the entire Bay and interannual variation of yearly mean Susquehanna River flow shifted by 83 days and moving averaged by 360 days; two kinds of regression were applied and the correlation coefficient is shown in text, where the red dashed line denotes the linear regression between RT and flow, and the blue solid line denotes the linear regression between RT and 1/flow; (b) regression between monthly mean residence time

averaged over the entire Bay and monthly mean flow shifted by 83 days and movingaveraged by 360 days.

372	Based on the significant flow-RT relationship (Eq. 4), a long-term estimation of yearly
373	mean RT back to 1891was conducted and shown in Fig. 10. The 360-day moving average
374	and the 83-day shifting of the flow were applied. Susquehanna River flow
375	datawerethoseobservationscollected at USGS Station 01578310, which had daily
376	discharge data since 1967. The missing discharge data of 1891-1967 were estimated with
377	the data fromanother nearby Station USGS 01570500, located upstream of Station USGS
378	01578310. Daily discharge values measured at these two stations were highly linearly
379	correlated ( $R^2$ =0.997, from a 10-year linear regression). The estimation showed that RT
380	of the past centuryhad a high variability. It seems the interannual variability became
381	larger after the 1970s. The maximum RT occurred in 1930 (RT=248 days) and the
382	minimum RT occurred in 2004 (RT=132 days). No significant trend could be found for
383	the past century.



Fig. 10. Estimated mean residence time of the entire Bay since 1891; annual meanresidence time from model simulation is shown as a black asterisk.

388

# 389 4.2 Impact of estuarine circulation on RT

390 Despite the high correlation between the yearly mean RT and yearly mean flow, a 391 large part of the monthly RT variation remained to be explained. Besides the river discharge, tidal exchange and estuarine circulation are two main processes that contribute 392 393 to the water exchange between an estuary and coastal waters. The relative importance of 394 tidal exchange and estuarine circulation differs in different systems (Hansen and Rattray, 1965; Officer and Kester, 1991). Tide has proven to be important to affect water transport 395 through tidal pumping (Chen et al., 2012) and thus change the pattern of the RT, 396 397 especially for a small estuary where RT is relatively small (Brye et al., 2012;Andutta et al., 2016). In the Chesapeake Bay, tide contributes to the vertical mixing and the 398 399 formation of asymmetry of west-east RT distribution and to the gravitational circulation 400 that leads to the huge difference between surface and bottom RT.Consistent with the findings of Brye et al. (2012), RT varied more significantly over a tidal cycle than over a 401 spring-neap cycle, especially in the area near the mouth boundary (Fig. 11). The semi-402 403 diurnal tidal component of the RT weakens toward the upstream. No significant signal of the spring-neap cycle in the RT time-series at selected stations was found. As the 404 residence time of the Bay is on the order of 100 days, the semi-diurnal tidal signal 405 becomes insignificant towards the upstream. 406



Fig. 11. Time-series of hourly mean surface residence time at 3 selected stations (i.e.
s1, s2, s3), whose locationsareshown in Fig. 1b.

410

The other important process that may have a significant impact on the RT is the estuarine circulation. Hagy et al. (2000) demonstrated the saline influx at the mouth of a partially mixed estuary is important to the water renewal, especially in the area near the mouth. To quantify the variability of estuarine circulation, we calculated the influx for each month at a mid-Bay cross-section (location shown in Fig. 1b with red line) to

indicate the strength of the circulation. In order to remove the impact of river discharge
on monthly mean RT, the residual value from the monthly RT-flow regression (Fig. 9b)
was used to compare with the monthly influx at the mid-Bay cross-section. Similar to the
regression between river flow and RT, a delay of 83 days was also considered when
conducting the regression between the residual and influx.

421

422



Fig. 12.(a) Time-series of normalized influx at the middle Bay cross section (red line)
and normalized residual value from the monthlyRT-Flow regression (blue line). Both
time series were normalized by removing the mean and dividingby the standard deviation.
A positive value 1.0 of normalized influx denotes the influx is larger than the mean influx
by 1.0 standard deviation.(b) Scatter plot of the influx andresidual value from the
monthly RT-Flow regression.

430 The regression between the residual and influx showed that the residual was highly 431 negatively correlated with the influx, with p<0.001 (Fig. 12). Even though the  $R^2$  is not 432 high, troughs of the residual RT often coincide with peaks of influx. A larger influx will

enhance the outflow and lead to a faster water exchange near the mouth and thus smaller
RT. This significant relation also suggests that thosefactors (e.g., wind, tide, river
discharge) affecting the estuarine circulation could also have potential impact on the RT,
especially on the short-term averaged RT.

#### 437 4.3Impact of wind

438 The influence of wind on estuarine circulation has been recognized for many years

439 (Geyer, 1997; Guo and Valle-Levinson, 2008; Scully, 2010; Li and Li, 2011, 2012;

440 Officer, 1976; Scully, 2010; Wang, 1979). To examine the influence of wind on RT,

441 several numerical experiments were conducted (i.e., without wind, with NE-NW wind,

442 with SE-SW wind, base case with all directions of wind). For these simulations, model

runs were from 2002 to 2005 and the model configuration was unchanged except the

444 wind forcing. For example, in he NE-NW wind case, wind was set to be zero when there

is the SE or SW wind. The RT value of year 2003 was analyzed and compared.

446





448

Fig. 13. (a-d) Yearly and vertically averaged RT of 2003 under different wind forcing
conditions. (e-f) The impact of wind forcing on the RT, indicated by the differences
between model simulations with and without wind forcings.

452

The comparison between different cases suggests that wind can have a significant 453 impact on the lateral pattern of RT. With the NE-NW wind forcing, the RT distribution is 454 very similar to the RT distribution without wind forcing, both with large lateral 455 asymmetry between the eastern and western region in the mainstem (Fig.13a-b). The 456 lateral asymmetry is most significant near the mouth of Potomac River (~38N). Southerly 457 458 wind, however, generates a similar lateral pattern as under base wind condition, in which 459 the asymmetry is highly weakened (Fig. 13c-d). The difference between the no-wind case and the other casesreveals that northerly 460 wind and southerly windshave different impacts in different regions and their impacts are 461 not simply opposite to each other. Both southerly and northerly winds are likely to reduce 462

- the RT in the eastern region of the lower-middle Bay (Fig. 13e-f). Southerly wind
- 464 increase the RT in the middle-upper Bay significantly by up to 100 days (Fig. 13f), while

the northerly wind has little impact (<20 days) in the western region of the middle-upper 465 Bay (Fig.13e). It appears that the southerly wind plays a more dominant role in 466 controlling the long-term transport, which is consistent with findings for the impact of 467 468 wind on freshwater age (Shen and Wang, 2007). The southerly wind causes strong lateral and vertical mixing, reduces the gravitational circulation, and thereby increases the 469 transport time. The influx at the mid-Bay cross-section, indicating the strength of 470 gravitational circulation, was strongly reduced by the SE-SW wind and enhanced by the 471 NE-NW wind (Fig. 14). Compared to NE-NW wind, the influx was reduced by half with 472 473 SE-SW wind.

474



Fig. 14.Along channel residual current at the middle Bay cross section under different
wind forcing conditions, with contour level of 0.02 m/s (black lines). Positive value
denotes an influx to the upstream. Values of laterally and vertically integrated influx are
shown in the text at the bottom.

480

#### 481 **5.** Conclusion

In this study we investigate the water exchange between the Chesapeake Bay and its 482 adjacent coastal sea, using the timescale residence time (RT) thatcan often be used to 483 evaluate the impacts of hydrodynamic conditions on biological and geochemical 484 processes. The long-term simulation of water RT of the Chesapeake Bay was conducted 485 over the period from 1980 to 2012, using an adjoint method, which enables us to compute 486 the time-varying RT in a single model run. The impacts of river discharge, intensity of 487 estuarine circulation, and wind on the RT were discussed. The main conclusions are 488 summarized as follows. (1) The vertically mean RT averaged over the entire Chesapeake 489 490 Bay system ranges from 110 to 264 days, with a mean of 180 days and a standard deviation of 30 days over the past 3 decades. No clear trend was detected during the past 491 three decades. The bottom RT was larger than that of the surface due to the gravitational 492 circulation, and the vertical differences could be as large as 100 days. (2) There was a clear 493 seasonal cycle of RT, with high RT occurringin the summer and low RT occurringin the 494 winter, suggesting materials released in winter would be flushed out most quickly. (3) 495 Interannual variability of the RT was significant and was highly correlated with the 496 variability of river discharge. The correlation coefficient between yearly mean RT and 497 498 yearly mean river discharge can be as high as 0.92, if the river discharge was shifted by 83 days and a moving average of 360 days was applied.(4) The monthly variability of RT 499 can be partially attributed to the variability of estuarine circulation. A strengthened 500 501 estuarine circulation results in a larger bottom influx and thus reduces the RT. (5) Wind exerts a significant impact on the lateral pattern of RT. The upstream wind is more 502 503 important in controlling the lateral pattern of RT in the mainstem than the downstream 504 wind.

# 505 Acknowledgements

- 506 We thank Mac Sisson for his assistance in editing the manuscript. We thank Mark Brush,
- 507 Carl Hershner, Kyeong Park, and Harry Wang for their suggestions. We are grateful to
- 508 Ya Wang, Qubin Qin and Xin Yu for their assistance in coding of the model and helpful
- 509 comments. This work is supported by the National Science Foundation (Award
- 510 #1325518). Additional support is provided by Virginia Institute of Marine Science. This
- 511 is contribution No. xxxxx of the Virginia Institute of Marine Science, School of Marine
- 512 Science, College of William and Mary, Virginia.

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